

# 1 The place-cell representation of volumetric 2 space in rats

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12 Main text (8 figures, 2 tables)

## 13 Abstract

14 Place cells are spatially modulated neurons found in the hippocampus that underlie  
15 spatial memory and navigation: how these neurons represent 3D space is crucial for a full  
16 understanding of spatial cognition. We wirelessly recorded place cells in rats as they  
17 explored a cubic lattice climbing frame which could be aligned or tilted with respect to  
18 gravity. Place cells represented the entire volume of the mazes: their activity tended to be  
19 aligned with the maze axes, and when it was more difficult for the animals to move vertically  
20 the cells represented space less accurately and less stably. These results demonstrate that  
21 even surface-dwelling animals represent 3D space and suggests there is a fundamental  
22 relationship between environment structure, gravity, movement and spatial memory.

## 23 Introduction

24 Place cells are neurons in the hippocampus that fire when an animal visits specific  
25 regions of its environment, called place fields, and are thought to provide the foundation for  
26 an internal representation of space, or ‘cognitive map’<sup>1,2</sup>. The question arises as to whether  
27 this map is three-dimensional, and if so whether its properties are the same in all  
28 dimensions, and how information is integrated across these dimensions<sup>3–5</sup>. This is important  
29 not just for spatial mapping *per se* but also because the spatial map may form the framework  
30 for other types of cognition in which information dimensionality is higher than in real space.  
31 Understanding how the brain integrates information across dimensions is thus of theoretical  
32 importance.

33 A previous study of place cells in rats<sup>6</sup> found vertical elongation of the place fields when  
34 rats climbed either a pegboard wall studded with footholds or a helical track, suggesting that  
35 perhaps the cognitive map has a lower resolution for vertical space than for horizontal space  
36 (i.e., is anisotropic). This finding was supported by observations that entorhinal grid cells,  
37 thought to provide a spatial metric for place cells, showed absent spatial processing in the  
38 vertical dimension. However, in a more recent experiment, when rats climbed a wall covered  
39 with chicken wire place cells were found to have normally shaped firing fields, although fields  
40 themselves occurred with lower probability than on the floor<sup>7</sup>. This meant that although the  
41 firing of spatial neurons differed between the floor and the wall, the horizontal and vertical  
42 components of firing on the wall did not appreciably differ. Taking these findings together, it  
43 seems that the differences in spatial encoding previously seen in the vertical dimension may  
44 be due to the different constraints on movement, or the locomotor ‘affordances’ in the  
45 different dimensions<sup>8</sup>. Meanwhile, a study of flying bats found that place fields did not  
46 deviate statistically from spherical<sup>9</sup>, suggesting a spatial map of equal resolution in all  
47 dimensions (isotropic).

48 The different patterns of neural activity in the different types of apparatus could be due  
49 to the different movement patterns afforded by the footholds (aligned vs. orthogonal to  
50 gravity), or to the different encoding requirements of travelling on a surface vs. a volume.  
51 The present experiment aimed to untangle these issues by exploring, in rats, the interaction  
52 between gravity, which is what distinguishes horizontal from vertical, and the locomotor  
53 affordances of the environment. Animals were recorded using digital telemetry as they  
54 explored a volumetric space – an open cubic lattice – through which they could move freely  
55 and which had equal properties in all three spatial dimensions. Place cells exhibited firing  
56 fields throughout this volume, confirming that these cells underlie a fully three-dimensional  
57 volumetric representation of space. Furthermore, we found that place fields tended to be  
58 elongated along the axes of the maze (the directions aligned with the boundaries, and in  
59 which travel was easiest) with greater elongation for the vertical axis and a resultant lower  
60 spatial information and decoding accuracy. We then tilted the lattice so that the three planes  
61 of movement all had the same relationship to gravity, and were thus all equally easy (or  
62 hard) to traverse. We found that the elongation of the axes followed the tilt of the maze, and  
63 the difference between horizontal and vertical place field metrics disappeared. Thus,  
64 differences between horizontal and vertical metrics in spatial encoding seem to arise from  
65 the greater movement constraints for vertical than horizontal travel, rather than from an  
66 intrinsic difference in resolution between directions aligned with vs. orthogonal to gravity.  
67 These findings suggest that locomotor affordances in the environment, of which gravity is  
68 one modulator, have an effect on encoding structure and accuracy of the spatial map. This  
69 may have implications for spatial mapping not just in vertical space but in any space in which  
70 locomotion is difficult or interrupted.

71

## 72 Results

### 73 *Rats explored the lattice maze fully, but adopted a layer strategy*

74 Rats explored the lattice mazes (Fig. 1) fully, with slightly more coverage in the  
75 aligned than the tilted configuration (Fig. S1a-b). In both configurations they spent more time  
76 in the lower half and remained closer to the maze boundaries (Fig. S1c-d). Movement speed  
77 profiles did not differ between environments (Fig. S1f, Supp. Data: *Movement patterns in the*  
78 *lattice mazes*).

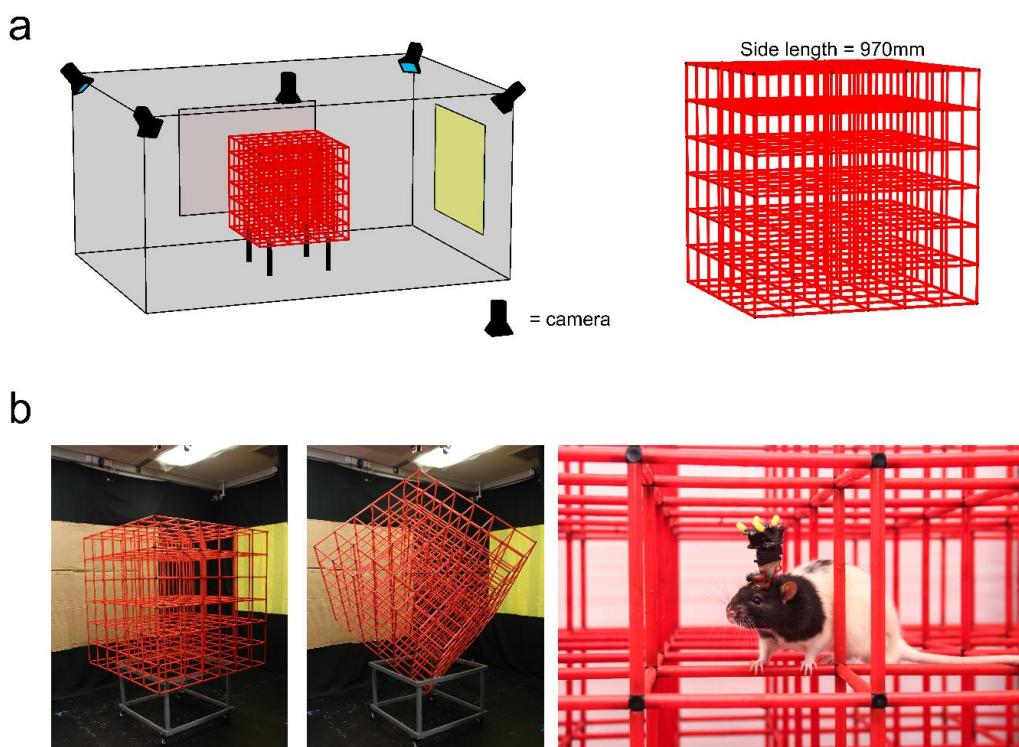


Fig. 1: The recording room and apparatus. **a** Room and maze schematic, shown in aligned configuration. **b** Photographs showing the aligned lattice maze in position for recording (left) the tilted lattice maze in position for recording (middle) and a rat implanted with an Axona microdrive exploring the aligned lattice whilst connected to the wireless headstage (right).

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81 In the arena and aligned lattice animals mostly moved parallel to the horizontal X and Y-  
82 axes with no preference between them (Fig. 2a-b, Table 1). They did not move along any  
83 other axes more than would be expected by chance (Fig. 2b red area). Additionally, in the  
84 aligned lattice animals moved vertically at a much slower speed compared to X or Y,  
85 confirming a strong horizontal bias in their movements <sup>10</sup> (Fig. S1e, Supp. Data: *Movement*

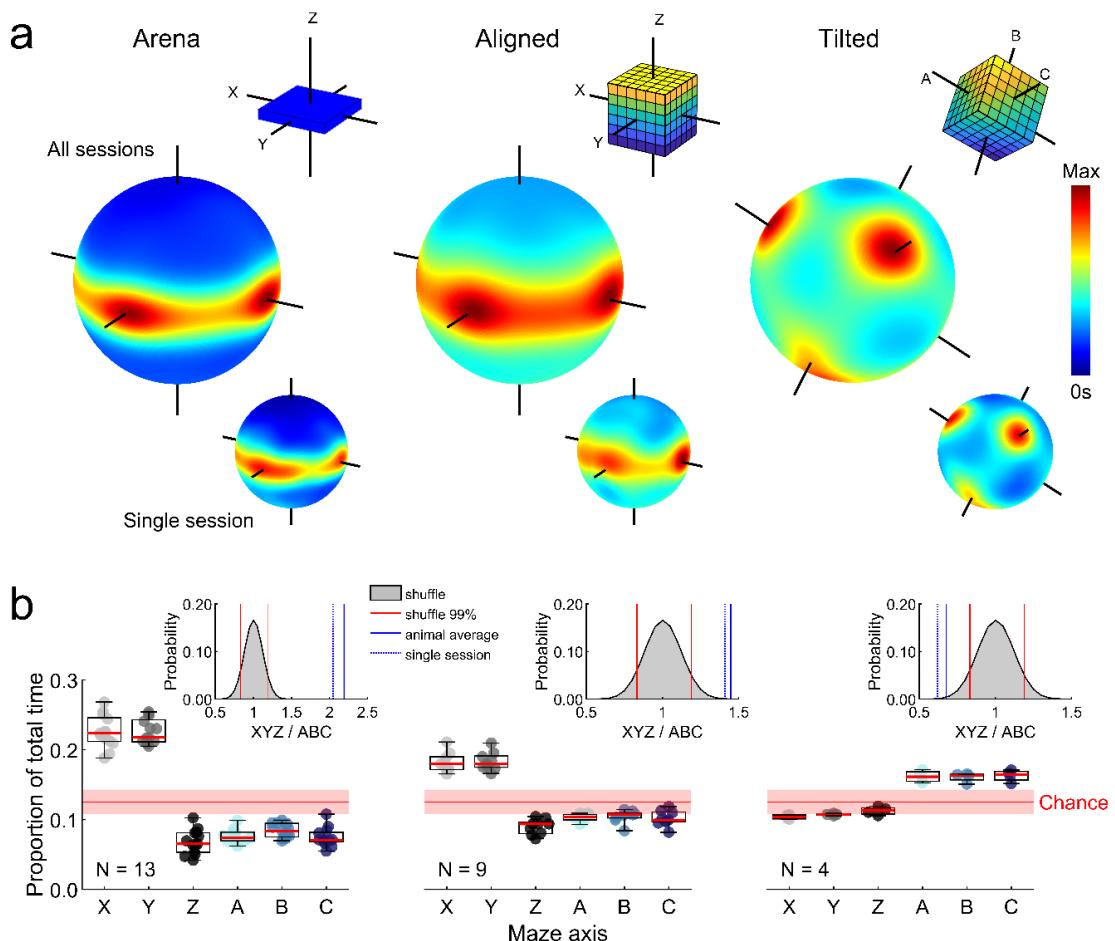


Fig. 2: Animals moved parallel to the maze axes. Statistical test results can be seen in Table 1. **a** For each maze: a schematic of the maze configuration color-coded to show height (top right inset); three-dimensional heat plot of heading direction distribution for all sessions combined (middle); same three dimensional heat plot for a single session (bottom right inset). Note concentration around horizontal trajectories for the arena and aligned maze, and along the three axes for the tilted maze. **b** Each marker represents an animal: graphs show proportion of total time spent moving roughly parallel to each possible maze axis. Red lines show the 1<sup>st</sup>, 50<sup>th</sup> and 99<sup>th</sup> percentile of a shuffle distribution. Inset plots show the result of a shuffle testing the probability of observing this ratio of total XYZ time to total ABC time by chance. Red lines denote the 1<sup>st</sup> and 99<sup>th</sup> percentile rank positions in the shuffled distribution of ratio values (grey area), blue line denotes the overall ratio value averaged across rats, and blue dotted line denotes the ratio value observed in the single session shown in **b**.

86 *patterns in the lattice mazes*, Supplementary Video S3). In the tilted lattice animals moved  
 87 mostly parallel to the now rotated maze axes, which we referred to as A, B and C (Fig. 2a-b)  
 88 and they did not move along any other axes more than would be expected by chance (Fig.  
 89 2b red area). The A, B and C axes were explored at an equal rate (Table 1) and speed (Fig.  
 90 S1e) suggesting that the animals did not have a bias for a specific axis in this configuration.

91

Table 1

*Statistical test results*

Comparison	Test	Results	Fig.
Proportion of total time along X & Y, arena	FT	$\chi^2(1) = 0.08, p = .78, \eta_p^2 = 0.001$	Fig. 2b
Proportion of total time along X & Y, aligned		$\chi^2(1) = 1.00, p = .31, \eta_p^2 = 0.037$	Fig. 2b
Proportion of total time along A, B & C, tilted		$\chi^2(2) = 1.50, p = .47, \eta_p^2 = 0.125$	Fig. 2b
Fields per cell, arena, aligned & tilted	KW	$\chi^2(2) = 83.60, p < .0001, \eta_p^2 = .062$	Fig. 4b
Fields per $m^3$ , arena, aligned & tilted		$\chi^2(2) = 395.49, p < .0001, \eta_p^2 = .297$	Fig. 4c
Field volume, arena, aligned & tilted		$\chi^2(2) = 63.10, p < .0001, \eta_p^2 = .037$	Fig. 4d
Field diameter, arena, aligned & tilted		$\chi^2(2) = 7.30, p = .026, \eta_p^2 = .004$	Fig. 4e
Field elongation, arena, aligned & tilted		$\chi^2(2) = 65.60, p < .0001, \eta_p^2 = .039$	Fig. 6b
Field elongation arena		$Z = 22.80, p < .0001, U3 = 0$	Fig. 6b
Field elongation aligned	(compare to 1)	$Z = 21.29, p < .0001, U3 = 0$	Fig. 6b
Field elongation tilted		$Z = 17.29, p < .0001, U3 = 0$	Fig. 6b
Field sphericity, arena, aligned & tilted		$\chi^2(2) = 426.5, p < .0001, \eta_p^2 = .251$	Fig. 6c
Field sphericity arena	WSR	$Z = -22.80, p < .0001, U3 = 1$	Fig. 6c
Field sphericity aligned		$Z = -21.29, p < .0001, U3 = 1$	Fig. 6c
Field sphericity tilted		$Z = -17.29, p < .0001, U3 = 1$	Fig. 6c
Field length distributions, aligned	Multiple KS with Bonferroni	$X \text{ vs } Y: z = 0.05, p > .99$ $X \text{ vs } Z: z = 0.09, p = .03$ $Y \text{ vs } Z: z = 0.11, p = .003$	Fig. 6d
Field length distributions, tilted		$p > .2 \text{ in all cases}$	Fig. 6d
Autocorrelation aligned, X, Y & Z		$\chi^2(2) = 109.0, p < .0001, \eta_p^2 = .084$ $X \text{ vs } Z \text{ & } Y \text{ vs } Z, p < .0001, X \text{ vs } Y, p > .99$	Fig. 8a
Autocorrelation tilted, A, B & C		$\chi^2(2) = 1.7, p = .44, \eta_p^2 = .002$	Fig. 8a
Proportion of spatial information aligned, X, Y & Z		$\chi^2(2) = 153.3, p < .0001, \eta_p^2 = .119$ $X \text{ vs } Z \text{ & } Y \text{ vs } Z, p < .0001, X \text{ vs } Y, p > .99$	Fig. 8b
Proportion of spatial information tilted, A, B & C	FT	$\chi^2(2) = 1.4, p = .498, \eta_p^2 = .001$	
Area under curve, aligned, X, Y & Z		$\chi^2(2) = 9.1, p = .011, \eta_p^2 = 0.005$ $X \text{ vs } Y, p > .99, X \text{ vs } Z, p = .047, Y \text{ vs } Z, p = .017$	Fig. 8c
Area under curve, tilted, X, Y & Z axes and A, B & C axes		$\chi^2(2) = 4.7, p = .094, \eta_p^2 = 0.0039$ $\chi^2(2) = 2.8, p = .25, \eta_p^2 = 0.0024$	Fig. 8c

Test abbreviations and details can be found in Methods: *Statistics*

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95 *Place fields were distributed uniformly throughout the lattice mazes*

96 In total we recorded 756 place cells in the lattice maze environments from 13 rats

97 (Table S1). Representative place cells can be seen in Fig. 3, Fig. S2&3 and Supplementary

98 Videos S1&S2. Cells were stable throughout the lattice maze recordings (Fig. S4, Supp.

99 Data: *Recording stability*). The proportion of cells with at least one place field did not differ

100 between the mazes (arena, aligned & tilted: 82.5, 85.2 & 83.8%,  $\chi^2(1) = 2.49$ ,  $p = .29$ , CST)

101 but these cells exhibited significantly more fields in the lattice mazes (Fig. 4a-c, Table 1).

102 However, the number of fields expressed per cell did not scale with the volume of the

103 mazes, resulting in fewer fields per  $m^3$  in the lattice mazes (Fig. 4d, Table 1). Instead, place

104 field volume was larger in the aligned lattice than the arena and larger again in the tilted

105 lattice (Fig. 4e, Table 1). However, place field diameter varied very little between mazes with

106 only a small, albeit significant, difference between the arena and tilted lattice (Fig. 4f, Table

107 1). Fields were distributed throughout the lattices uniformly and in each case the median

108 field centroids lay close to the maze center (Fig. 5). There was no significant relationship

109 between the numbers of fields expressed in the arena and the lattice mazes (Fig. S10, Supp.

110 Data: *Comparison of firing properties between mazes*).

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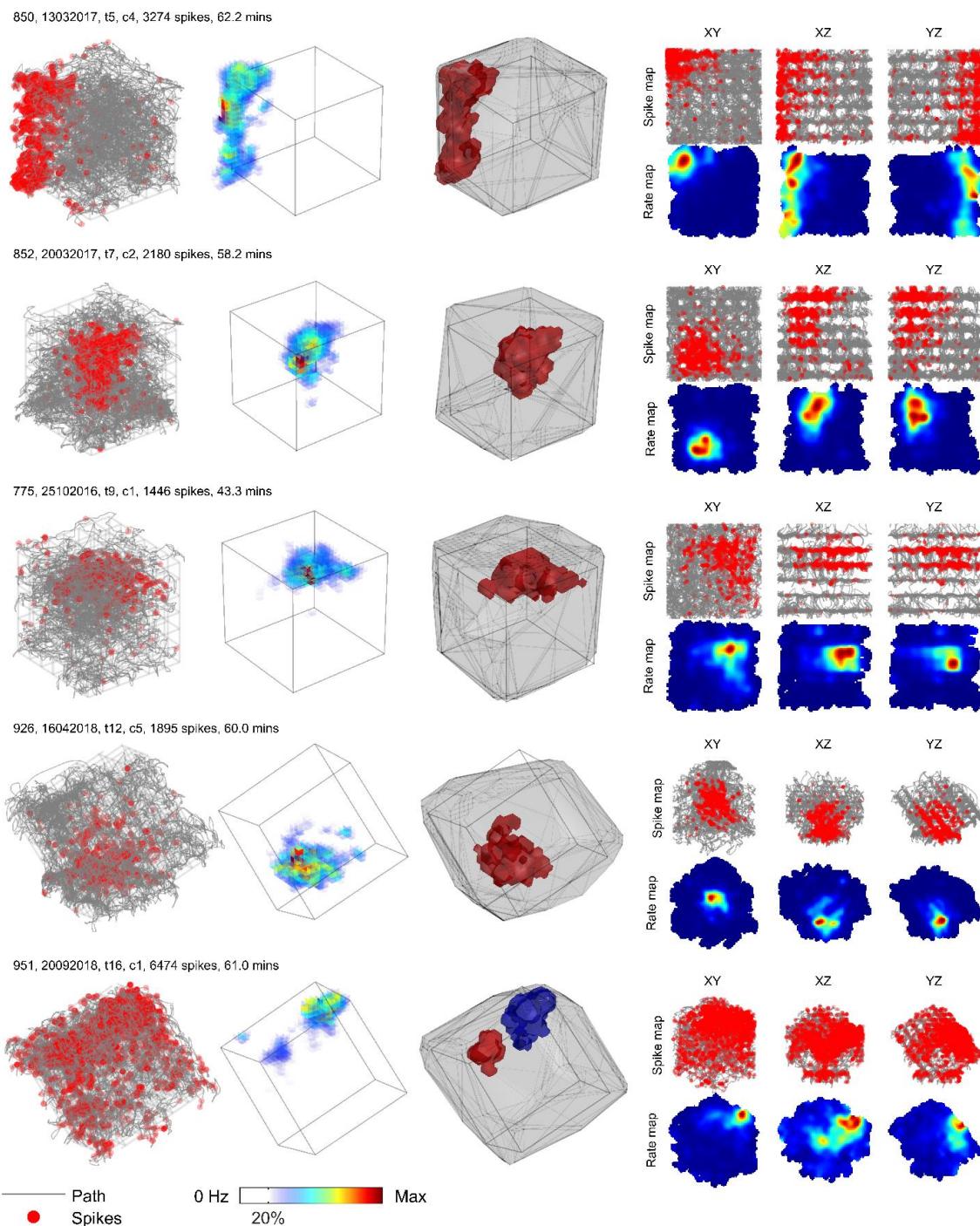


Fig. 3: Representative example place cells and their activity in the lattice mazes. For additional examples see Fig. S3&4 and Supplementary Videos S1&S2. Five cells are shown, one per row. First column shows the path of the animal and spikes plotted as red markers. Second column shows the three-dimensional firing rate map. Colors denote firing rate and areas of low or no firing are transparent. Third column shows the convex hull of the dwell time map as a grey outline and the convex hull of any detected place field(s) as separate (color-coded) polygons. Last column shows the spike and firing rate maps when the data are projected onto the three possible cardinal planes.

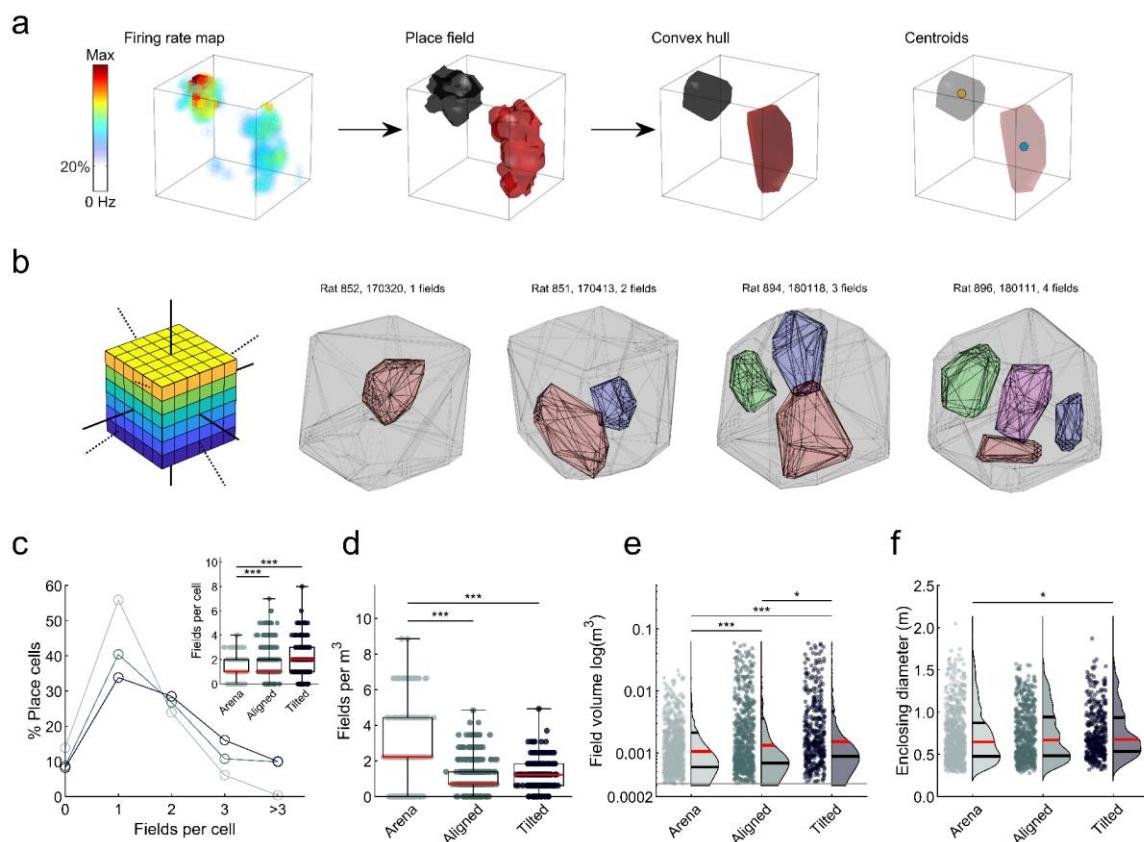


Fig. 4: Fields were less numerous in the lattice mazes but larger in volume. Markers in boxplots represent fields. Omnibus test results can be seen in Table 1; post-hoc test results are displayed here: \* = significant at the .05 level, \*\* = significant at the .01 level, \*\*\* = significant at the .001 level. **a** Schematic demonstrating the process of place field detection and analysis. An example firing rate map (left) is thresholded at 20% of the peak firing rate and regions which passed our criteria were considered place fields (2<sup>nd</sup> plot). We can visualize these regions as convex hulls (3<sup>rd</sup> plot) and extract features such as their centroid (right plot). **b** Aligned lattice maze schematic and place field convex hulls of four example place cells exhibiting 1-4 place fields. **c** Number of place fields exhibited by place cells in each maze. Inset: same data in boxplot representation. **d** Number of fields per cubic meter exhibited by place cells in each maze. **e** Distribution of place field volumes observed in each maze. **f** Enclosing diameter of place fields in each maze.

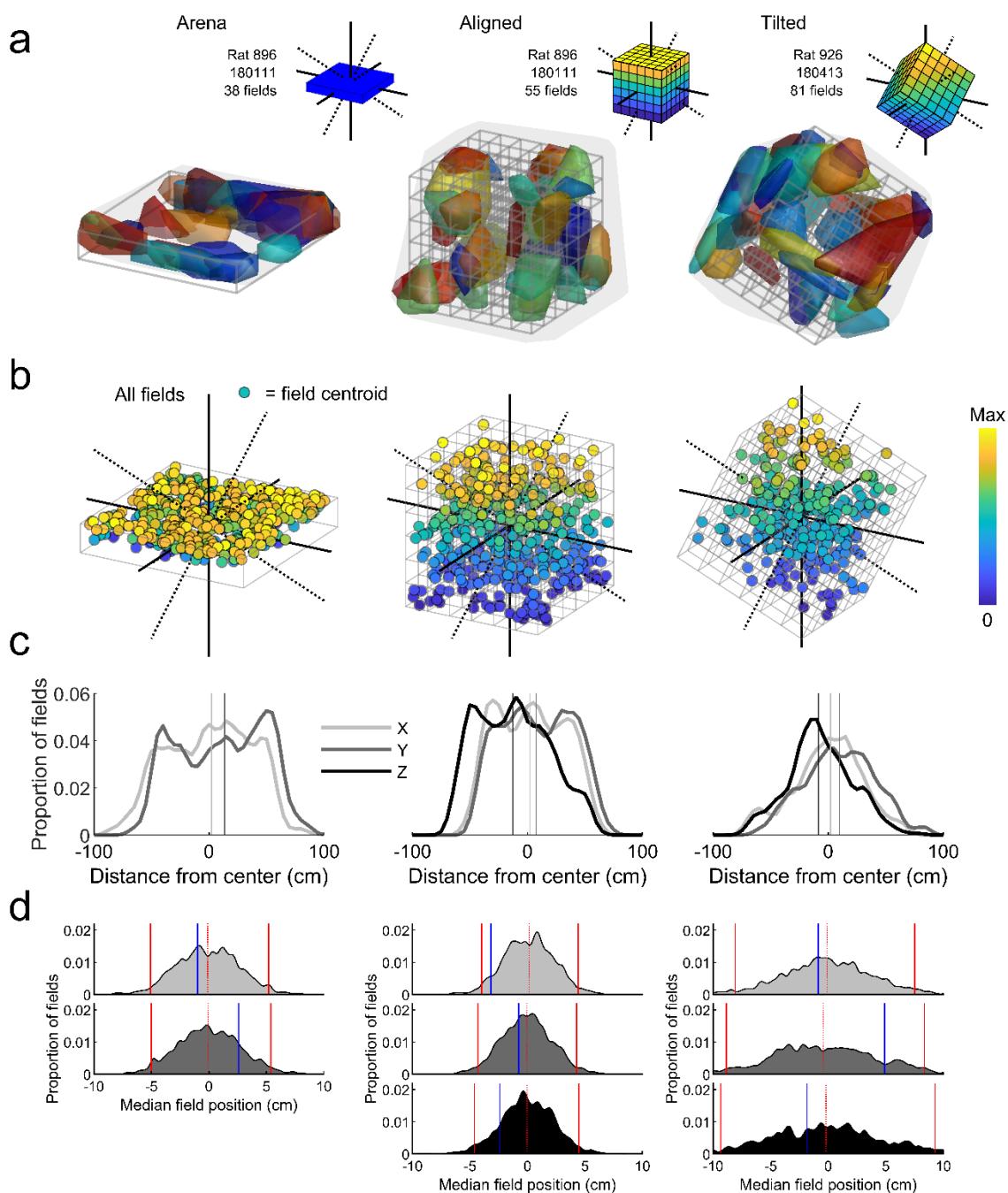


Fig. 5: Place fields were distributed throughout the three mazes. **a** Representative arena, aligned and tilted lattice recording sessions demonstrating homogenous distribution of fields. To allow clearer distinction of separate (color-coded) fields, only fields with a volume less than 300 voxels (one voxel = 50mm cube) are shown (~2/3 total). Inset schematics show the maze orientation and axes. **b** Location of all recorded place field centroids. Colors denote vertical position. **c** Columns follow the mazes as above; the kernel smoothed distribution of place fields along the X, Y and Z dimensions of each maze (Z is not shown for the arena) relative to the maze center. Vertical lines represent the median value of these distributions. **d** Columns follow the mazes as above; from top to bottom graphs show the results of a shuffle analysis on the distribution of fields along the X, Y and Z axes (Z is not shown for the arena). Blue lines denote the median position of real place fields along these axes relative to the maze center. Shaded areas represent the distribution of median values obtained from 1000 shuffles. Red lines show the 2.5 and 97.5 percentile rank positions in the shuffled distributions, red dotted lines denote the 50<sup>th</sup> percentile rank or median of the shuffle distributions.

116 *Place fields were elongated rather than spherical*

117 Place fields took on different shapes in the mazes; most fields were elongated in the  
118 lattice mazes while they exhibited a flattened shape in the arena (Fig. S5). Only a minority of  
119 fields in each maze were isotropic or more spherical than would be expected by chance (Fig.  
120 6b-c text percentages). Instead, place fields in all conditions were slightly elongated, with  
121 elongation indices and sphericity that deviated significantly from 1 (Fig. 6b-c, Table 1). It is  
122 unlikely these effects were due to inhomogeneous sampling (Fig. S6). In the aligned lattice  
123 the distribution of field heights (length along Z) deviated from the distributions of length along  
124 X or Y (Table 1) and had a significant bimodal appearance (Fig. S7a, Supp. Data: *Field*  
125 *elongation*). By contrast, in the tilted maze all axes shared a similar unimodal distribution  
126 (Fig. 6d). Place field elongation in the lattice mazes was weakly but significantly positively  
127 correlated with the distance of the field from the maze center, but we found no relationship  
128 between elongation and experience or cluster quality in any of the mazes (Fig. S7b-d). When  
129 cells had a field in both the arena and aligned lattice there was no relationship between their  
130 elongation in the two configurations, although there was a weakly negative correlation  
131 between the arena and tilted lattice data; when cells had multiple fields in the lattice mazes  
132 their lengths were not more similar than would be expected by chance (Fig. S10b-c, Supp.  
133 Data: *Comparison of firing properties between mazes*).

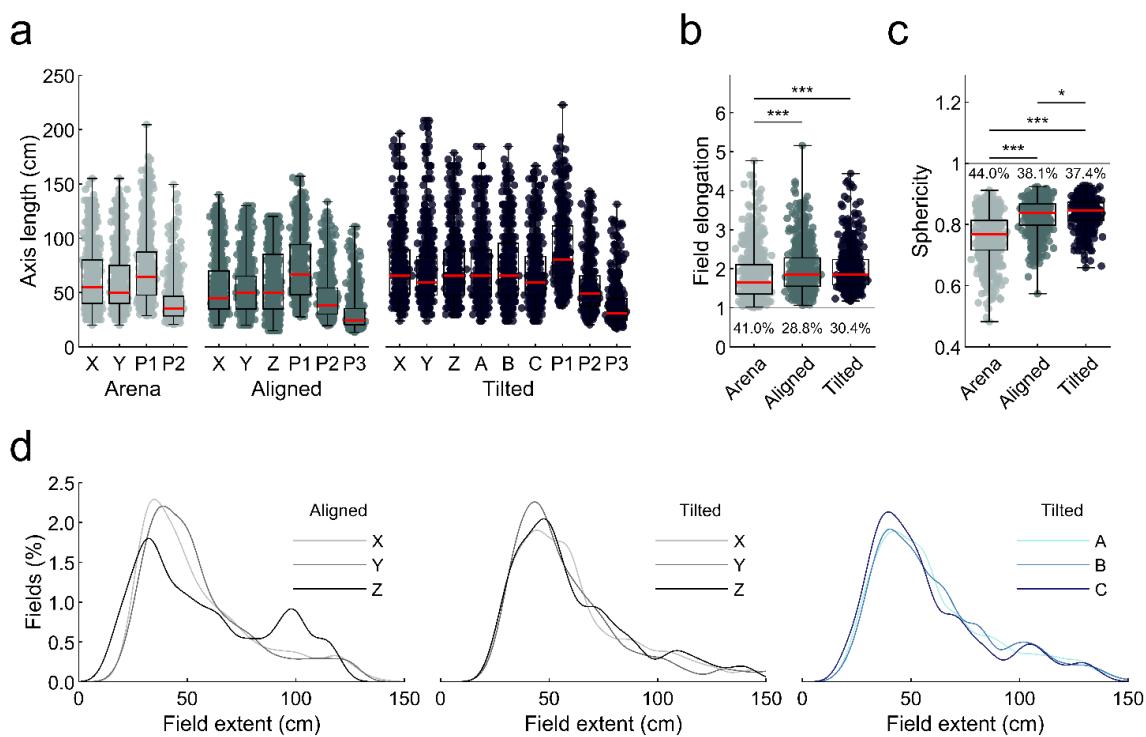


Fig. 6: The majority of place fields were elongated instead of spherical. Markers represent place fields. Omnibus test results can be seen in Table 1, post-hoc test results are displayed here: \* = significant at the .05 level, \*\* = significant at the .01 level, \*\*\* = significant at the .001 level. **a** Cartesian axis and principal axis lengths of place fields in all three mazes (P1-3 are the principal, semi-major and semi-minor axes respectively). **b** Elongation index of all place fields in each maze. An index of 1 (grey line) would indicate a spherical field, higher values indicate elongation. The percentage of fields that are equally or more spherical than would be expected by chance is given by the text below each boxplot. **c** Same as **b** but for sphericity. Values less than 1 indicate deviation away from a sphere. **d** Probability density functions of the XYZ and ABC field length data in **a**. The distribution of Z lengths differs significantly from X and Y in the aligned lattice and the distribution of Z lengths appears to be bimodal (Supp. Data: Field elongation). In the tilted lattice there are no differences between X, Y & Z or A, B & C. See Fig. S7 for further field elongation analyses.

134

135 *Place fields were elongated parallel to the maze axes*

136 Given that the majority of fields were elongated instead of spherical we investigated  
 137 whether they were elongated along a common orientation (Fig. 7a; Supp. Methods: *Field*  
 138 *orientation and size*). In the square arena the 3D orientations of place fields were not  
 139 random; instead the majority of fields had their longest axis running parallel to either the X or  
 140 Y axis, or parallel to the walls of the arena (Fig. 7b). A shuffle analysis revealed that more  
 141 fields were oriented along these axes than would be expected by chance; this was not true

142 of any other axis (Fig. 7c red shaded area). These two axes shared a similar number of  
143 fields (Fig. 7c, overlap with confidence intervals) and these fields all had a similar length  
144 (median X & Y length, 68.5 & 67.0cm,  $\chi^2(1) = 0.01$ ,  $p = .97$ ,  $\eta_p^2 < .0001$ , K-W).

145 In the aligned lattice the majority of fields had their longest axis running parallel to  
146 either the X, Y or Z axes – which were also parallel to the lattice bars (Fig. 7b). Again, a  
147 shuffle analysis revealed that these orientations were the only ones with more fields than  
148 expected by chance (Fig. 7c red shaded area). These shared a similar number of fields (Fig.  
149 7c, overlap with confidence intervals) but in this case the fields aligned with the Z axis were  
150 significantly longer (median length, X, Y & Z: 64.2, 57.6 & 78.2 cm,  $\chi^2(2) = 26.8$ ,  $p < .0001$ ,  
151  $\eta_p^2 = .055$ , K-W, X vs Y,  $p = .074$ , X vs Z,  $p < .0084$ , Y vs Z,  $p < .0001$ ).

152 In the tilted lattice a different pattern of results emerged; fields were mainly oriented  
153 parallel to the A, B and C axes which were also parallel to the (now rotated) lattice bars (Fig.  
154 7b). As before, these orientations were the only ones with more fields than chance (Fig. 7c  
155 red shaded area); they shared an equal proportion of fields (Fig. 7c, overlap with confidence  
156 intervals) and a similar length (median length, A, B & C: 64.3, 57.9 & 78.2 cm,  $\chi^2(2) = 0.80$ ,  
157  $p = .68$ ,  $\eta_p^2 = .002$ , K-W). For all three mazes an independent approach confirmed that field  
158 elongation was best described as parallel to each maze's axes (Fig. S8, Supp. Data: *Field*  
159 *orientation*). Lastly, when cells had multiple fields in the lattice mazes their orientations were  
160 not more similar than would be expected by chance (Fig. S10d, Supp. Data: *Comparison of*  
161 *firing properties between mazes*).

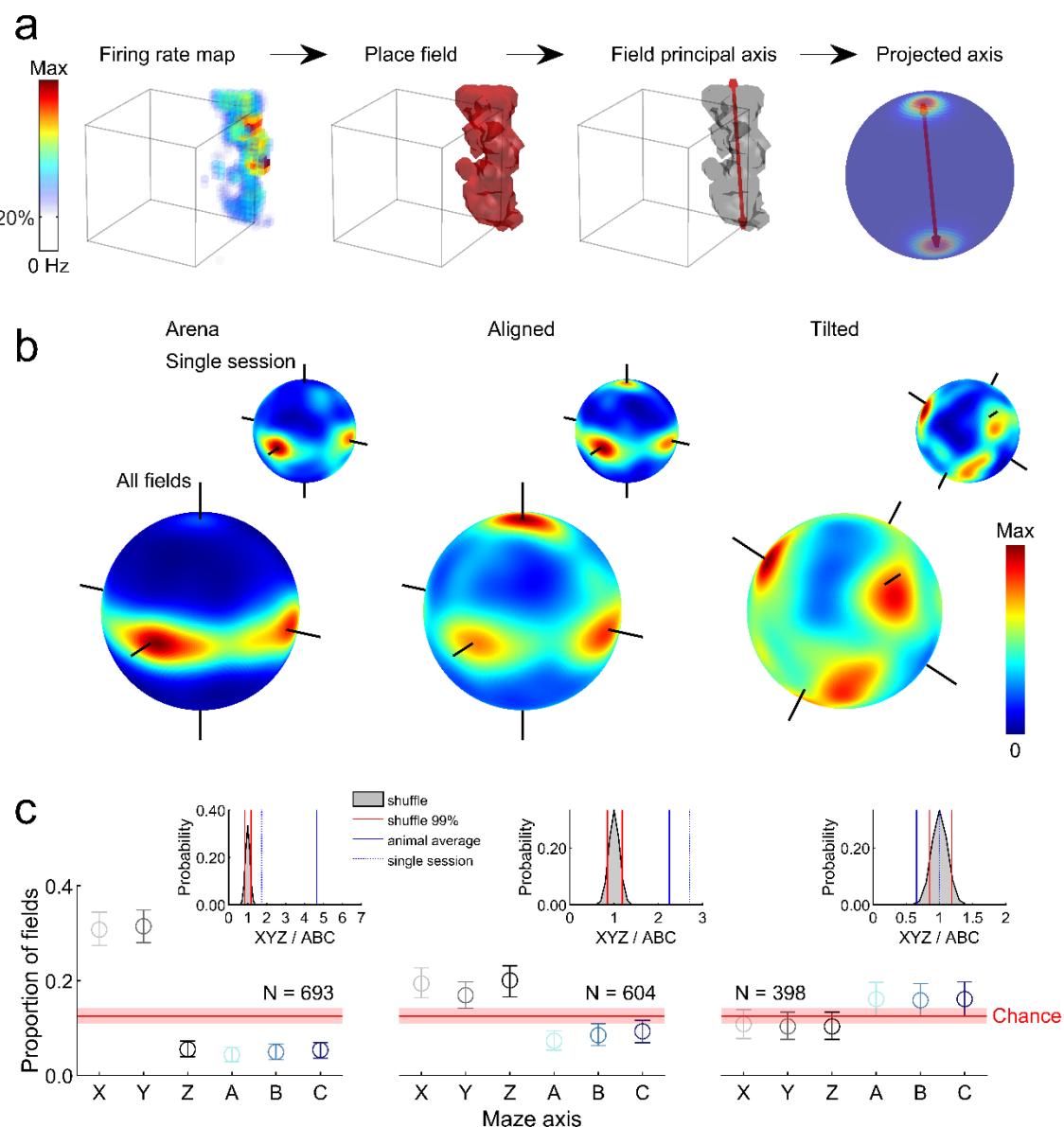


Fig. 7: Place fields were oriented parallel to the maze axes. **a** Schematic showing how the orientation of place fields was extracted and visualised. A place field is detected in an example firing rate map through thresholding, the principal or longest axis of this field can then be extracted (red arrows, 3<sup>rd</sup> plot). To visualize the orientation of multiple fields we project these axes onto a unit sphere and generate a spherical Von-Mises kernel smoothed density map, where hot colors denote that many fields 'pointed' their principal axis in this orientation. **b** Three-dimensional heat plots of place field orientation for the three maze configurations; inset heat plots (top right) show data for a single session, large plots (bottom) show data for all place fields. Note concentration around the three axes of the aligned and tilted mazes. Flat cylindrical projections can be seen in Fig. S8. **c** Graphs show proportion of total fields oriented roughly parallel to each possible maze axis. Circles give the observed proportion per axis, error bars represent 95% confidence intervals calculated through a bootstrapping procedure. Red lines show the 50<sup>th</sup> percentile of a shuffle distribution while shaded red areas denote the interval between the 2.5<sup>th</sup> and 97.5<sup>th</sup> percentiles. Inset plots show the result of a shuffle testing the probability of observing this ratio of total XYZ fields to total ABC fields by chance. Red lines denote the 1<sup>st</sup> and 99<sup>th</sup> percentile rank positions in the shuffled distribution of ratio values (grey area), blue line denotes the overall ratio value averaged across rats, and blue dotted line denotes the ratio value observed in the single session shown in **c**.

163 *Spatial coding was less accurate along the vertical dimension*

164 If fields were larger along a specific dimension, firing rate maps would be more highly  
165 autocorrelated along this dimension and the spatial information content conveyed by the  
166 cell's activity would be lower along this dimension (see Fig. S9a for an example). These  
167 were both true for the Z-axis of the aligned lattice (Fig. 8a-b, Table 1) but not for the tilted  
168 lattice where there were no such differences between the A, B and C axes (Fig. 8a-b, Table  
169 1). Similar effects were also observed using a variety of other measures (Fig. S9c-f; Supp.  
170 Data: *Autocorrelation, spatial information and binary morphology*). Down-sampling trajectory  
171 data to account for the biases in animals' movements confirmed that these do not account  
172 for the effects described here (Fig. S6; Supp. Data: *Trajectory downsampling*).

173 To investigate this reduced vertical resolution at the level of individual place fields we  
174 projected fields onto three orthogonal axes and calculated the area under the curve (AUC)  
175 for each. Place field AUCs in the aligned lattice were significantly larger along the Z  
176 dimension when compared to X and Y (Fig. 8c, Table 1). In contrast, there was no significant  
177 difference in the tilted lattice when comparing the X, Y and Z axes or A, B and C axes (Fig.  
178 8c, Table 1). Place field firing rate curves and the results of a similar but independent  
179 approach can be seen in supplementary data (Fig. S9e-f, Supp. Data: *Autocorrelation,*  
180 *spatial information and binary morphology*).

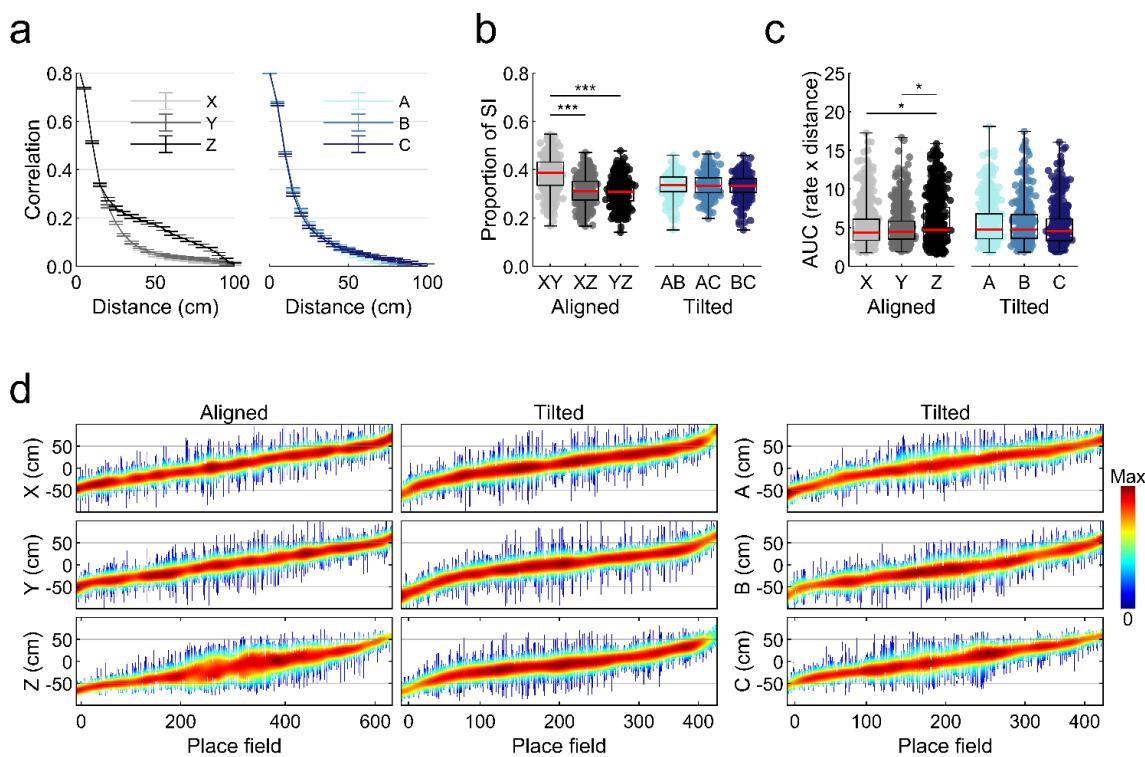


Fig. 8: Spatial information was lowest along the Z dimension of the aligned lattice. Omnibus test results can be seen in Table 1; post-hoc test results are displayed here: \* = significant at the .05 level, \*\* = significant at the .01 level, \*\*\* = significant at the .001 level. **a** Mean and SEM autocorrelation found for all place cells in the aligned lattice (left) and tilted lattice (right) at increasing distances or spatial lag. **b** Proportion of total spatial information found per projection for the aligned lattice (left) and tilted lattice (right). **c** Area under the firing rate curve (AUC) produced when place fields are projected onto each axis for both lattice mazes. **d** Span and normalized activity of every recorded place field in the lattice mazes. Vertical lines represent place fields, ordered along the x-axis by their position relative to the lattice central node. Line color represents normalized firing rate.

181

182 We investigated whether the reduced spatial specificity along the vertical dimension  
 183 may be due to the stability of the cells in the maze over time (Sup. Methods: *Field stability*).  
 184 Correlations between the first and second half of each session were significantly higher than  
 185 chance in all cases; furthermore, in the majority of cases the median correlation value  
 186 exceeded the 95<sup>th</sup> percentile of the shuffled distribution. However, place cell activity was  
 187 generally most stable when projected onto the XY plane, suggesting that cells were indeed  
 188 less stable in the vertical dimension (Sup. Data: *Field stability*). Stability was generally  
 189 lower in the tilted lattice comparisons, which is also in agreement with reduced spatial

190 information and increased sparsity in this maze (Fig. S10a, Supp. Data: *Comparison of firing*  
191 *properties between mazes*).

192 **Discussion**

193 This experiment investigated how hippocampal place cells represent three-dimensional,  
194 volumetric space in rats, which are predominantly surface-travelling animals. The aim was to  
195 see whether all three dimensions would be represented equally, as they are in freely flying  
196 bats, implying a volumetric map of space. We used three-dimensional lattice environments  
197 where the rats were free to move in any direction, restricted only by the underlying structure  
198 of the environment. In one setting the lattice structure was aligned with gravity and in the  
199 other it was tilted, enabling us to disentangle restrictions due to gravity from restrictions due  
200 to maze structure. We found that place fields packed the lattice space with ovoid fields, in a  
201 similar manner to bats, indicating a volumetric map. However the fields were slightly  
202 elongated along the maze axes. This was more pronounced in the vertical dimension for the  
203 aligned lattice, indicating an interaction between the effects of structure and gravity on place  
204 fields. Taken together with previous findings, this suggests that the hippocampal map of  
205 three dimensional space is not fixed but is flexibly shaped by environment structure, perhaps  
206 via the movement constraints/affordances it provides. Below, we discuss the findings that  
207 lead to this conclusion, and its implications.

208 When the lattice was aligned with gravity we found that rats explored using a “layer  
209 strategy” in which they fully explored one level before moving to the next, meaning far fewer  
210 vertical movements than horizontal ones – this replicates previous findings and is consistent  
211 with the notion that animals will execute the easier parts of a multi-stage journey first<sup>10</sup>.  
212 When the maze was tilted, all three principal axes became sloped relative to gravity and thus  
213 equally easy/hard to traverse, and the layer strategy disappeared. We also found that rats  
214 spent more time in the lower part of the mazes.

215 In both maze alignments, we found that place fields were distributed evenly  
216 throughout the volume of the lattices and had broadly similar properties in vertical vs.  
217 horizontal dimensions. They were larger in volume than fields in the open-field arena,

218 suggesting that the hippocampal representation of space scales according to environment  
219 demands. This observation supports the multiscale spatial representation proposed by  
220 Geva-Sagiv et al. <sup>11</sup>. Furthermore, our data followed the same relationship between  
221 environment and place field size reported there. If we treat our arena as a short volume  
222 instead of a 2D plane the predicted volume of fields in the lattice would be much larger than  
223 those observed. A similar effect has also been observed previously in two-dimensional rat  
224 data <sup>12</sup>. One explanation for this effect is that in the arena we did not sample the full height of  
225 each place field, which would suggest that in 2D environments place fields extend upwards  
226 further than rats can reach without assistance; this is supported by the similar place field  
227 diameters in the three mazes. However, we did not observe a significant increase in the  
228 number of place fields exhibited per cell in the lattice maze environments<sup>13</sup>.

229 We next looked at the structure of place fields in the different dimensions, finding that  
230 place fields tended to be elongated, as has been generally seen <sup>6,14,15</sup>. Elongation did not  
231 occur in every direction but was almost always in the direction of the maze axes/boundaries.  
232 Two related explanations for why this might occur present themselves. One is that the maze  
233 boundaries, represented by the termination of the cross-bars, serve to anchor place fields in  
234 a similar way to walls and edges in a flat environment, possibly via boundary cells found in  
235 the subiculum <sup>16</sup> and medial entorhinal cortex <sup>17</sup>. These have been shown to respond to both  
236 walls and drops <sup>18,19</sup> and are able to “reset” the spatial firing of entorhinal grid cells <sup>20</sup>. Since  
237 the effect of anchoring falls off with distance due to accumulating path integration error,  
238 fields should tend to be narrower in the direction orthogonal to the nearest boundary, for  
239 which distance to the wall is small, and elongated in the direction that runs between the two  
240 more distant boundaries. The other explanation is that perhaps fields tend to be elongated in  
241 the direction more frequently traversed by the animals, or that is traversed for a longer  
242 continuous time. Since animals can spend relatively little time running directly towards or  
243 away from a boundary, but much time running back and forth along it, synaptic plasticity  
244 would have more opportunity to “grow” fields along the direction of travel <sup>21,22</sup>. A similar

245 argument could explain elongation along maze axes, because rats rarely moved vertically in  
246 the aligned lattice yet fields were still elongated along this axis. In the present experiment we  
247 did not investigate this further by rotating the axes relative to the boundaries, but this would  
248 be an interesting direction for future experiments.

249 We next looked at whether field elongation was greater in the vertical dimension.  
250 Previous research in rats on vertical surfaces found the vertical dimension to be represented  
251 differently to horizontal dimensions, although the exact nature of this difference depended on  
252 the movement patterns. When the rats climbed on pegs but remained oriented mainly  
253 horizontally then place fields were elongated vertically <sup>6</sup>, whereas when the animals climbed  
254 by clinging to chicken wire and were thus aligned with the wall then place fields were  
255 sparser, but no longer vertically elongated <sup>7</sup>. In a study of flying bats, fields were not different  
256 from spherical <sup>9</sup>. In the present experiment we found an increase in place field elongation in  
257 the vertical dimension, which was also represented less stably: however this was only when  
258 the maze was aligned with gravity, and not when it was tilted. The aligned configuration is  
259 the one that induced differential movement patterns, with freer movement in x-y than in z.  
260 Putting all these experiments together, the hypothesis emerges that place fields have less  
261 resolution in a dimension in which the animal does not freely travel in the direction of its body  
262 axis. This might occur if the distance-tracking process is not uniform in all directions but  
263 works best in the direction of travel.

264 The heterogeneity of findings in the different mazes points to a fundamental  
265 conclusion which is that there is not a fundamental, holistic map of space that permeates  
266 three-dimensional space and is sampled by the animal as it moves through the space over  
267 various surfaces. This is because no unitary map structure could account for field elongation  
268 on the pegboard and field sparsity on the chicken-wire “cling wall”. Rather, it seems that a  
269 different kind of place cell representation is recruited depending on environment structure  
270 and perhaps task demands.

271 Our findings of a volumetric place cell map agree not only with the data from bats but  
272 also from recent neuroimaging work in humans, suggesting the encoding resolution for  
273 movement along a vertical axis in a lattice maze does not differ greatly from horizontal<sup>23</sup>.  
274 However behavioral experiments suggest a subtle difference, with an advantage in memory  
275 for horizontal as compared to vertical space<sup>4</sup>. More recent evidence suggests that people  
276 wrongly estimate the position of objects in a well-known building, giving the overall effect of a  
277 vertically elongated but horizontally contracted spatial representation<sup>24</sup> which is in  
278 agreement with our finding of increased elongation along the vertical dimension (but see<sup>25</sup>).  
279 The path which participants use to explore a building has also been shown to play a crucial  
280 role; people who explore a building by mainly vertical paths were better at recalling the  
281 positions of vertically arranged objects than people who explored the same building by  
282 mainly horizontal paths<sup>26</sup> supporting the importance of environment affordances in the  
283 development of spatial representations.

284 In this paper we have shown that surface-dwelling animals such as rats do have a  
285 volumetric representation of space and that this representation exhibits many of the same  
286 characteristics as two-dimensional representations. Place fields are elongated parallel to the  
287 primary axes of every environment with a slight bias towards vertical elongation and spatial  
288 coding and stability are significantly reduced along this dimension, suggesting that these  
289 animals may not encode the vertical dimension with equal accuracy. Future research will  
290 need to investigate these effects in volumetric animals such as flying bats to determine if  
291 spatial maps share a common organization across species or if separate neural mechanisms  
292 exist in volumetric animals. Our results point to an important effect of environmental  
293 affordances, evidence of which can be seen in other spatial mapping literature. However,  
294 more research is needed to tease apart the relationship between affordances, geometry,  
295 gravity and behavioral sampling. This could look to combine recordings with behavioral  
296 training, to increase sampling of the more difficult vertical dimension. Our results, combined  
297 with those from recent experiments on the head direction system<sup>27,28</sup> suggest that the rodent

298 spatial navigation network may be far better at mapping three-dimensional space than  
299 previously thought. This confirms the relevance of rodents such as rats in studying these  
300 representations and raises questions regarding three dimensional encoding of other spatial  
301 cells such as grid and boundary cells. Overall the strong spatial representations we have  
302 observed in place cells points to the possibility of distinct spatial representations of  
303 volumetric space by grid cells which have yet to be explored.

304

305 **Methods**

306 *Statistics and figures*

307 If data were found to deviate significantly from a normal distribution (Matlab functions  
308 *lillietest*, *skewness*, *kurtosis*) we used non-parametric tests, and post-hoc tests compared  
309 average ranks (Matlab function *multcompare*, Bonferroni correction). Otherwise, we used  
310 parametric tests, and post-hoc tests compared population means (Matlab function  
311 *multcompare*, Bonferroni correction). In the case of multivariate comparisons, where we  
312 sought to determine any interaction effects we employed generalized linear models using  
313 SPSS. Where possible we report effect sizes for each test. Unless otherwise stated all  
314 statistical tests are two-tailed. Table 2 gives a summary of the tests used, how they were  
315 conducted and how they are reported in the text. In all figures \* = significant at the .05 level,  
316 \*\* = significant at the .01 level, \*\*\* = significant at the .001 level. For all box plots, red lines  
317 denote the sample median, boxes denote interquartile range, whiskers span the full range of  
318 the data and markers represent individual data points. Similar results to those reported in  
319 main text were also observed when only analyzing one session per animal (the session with  
320 the most place cells).

Table 2

*Summary of statistical tests, their abbreviations and software used*

Parametric Yes/No	Test	Abbreviation	Effect size	Software
N	Wilcoxon rank sum	WRS	Cohen's U3 (U3, fraction of values in group 1 less than those in group 2 or the test value in a one-sample test)	Matlab function <i>ranksum</i>
N	Wilcoxon signed rank	WSR	-	Matlab function <i>signrank</i>
N	Kolmogorov-Smirnov	KS	-	Matlab <i>kstest2</i>
N	Chi-square test of expected proportions	CST	Odds ratio (OR, the ratio of the odds of an event occurring in one group to the odds of it occurring in another group)	GraphPad, QuickCalcs
Y	Bootstrap modality test	-	-	Matlab function, <i>bootmode</i>
N	Kruskal-Wallis	KW		Matlab function <i>kruskalwallis</i>
N	Friedman test	FT	Partial eta squared ( $\eta_p^2$ , proportion of variance in the dependent variable explained by an independent variable)	Matlab function <i>friedman</i>
Y	Univariate ANOVA	-		SPSS 25, generalized linear models
Y	Repeated measures ANOVA	-		
N	Permutation F-test	-	-	Matlab, custom functions

321

322 *Animals*

323 Thirteen animals were used for single unit electrophysiological recording (9 in the  
324 lattice, 4 in the diagonal lattice), at which point they weighed approximately 400–450 g. Prior  
325 to surgery all animals were housed for a minimum of 8 weeks in a large (2.15m × 1.55m ×  
326 2m) cage enclosure, lined on the inside with chicken wire. This was to provide the rats with  
327 sufficient experience of climbing in a three-dimensional environment. During this time they  
328 were given unlimited access to a miniature version of the lattice maze. This was composed  
329 of similar lattice cubes (55 x 55 x 55) but with a slightly smaller spacing (11cm) and was  
330 oriented to match the experimental version appropriate to the rats (i.e. rats recorded in the  
331 aligned lattice were exposed to a miniature aligned lattice, rats recorded in the tilted lattice  
332 were exposed to a miniature tilted lattice). Animals were housed individually in cages after  
333 surgery and there they were given access to a hanging hammock or climbable nest box for  
334 continued three-dimensional experience.

335                   The animals were maintained under a 12 hr light/dark cycle and testing was  
336                   performed during the light phase of this cycle. Throughout testing, rats were food restricted  
337                   such that they maintained approximately 90% (and not less than 85%) of their free-feeding  
338                   weight. This experiment complied with the national [Animals (Scientific Procedures) Act,  
339                   1986, United Kingdom] and international [European Communities Council Directive of  
340                   November 24, 1986 (86/609/EEC)] legislation governing the maintenance of laboratory  
341                   animals and their use in scientific experiments.

342                   *Electrodes and surgery*

343                   A combination of Axona (MDR-xx, Axona, UK) and tripod design (Kubie, 1984)  
344                   microdrives were used (rats 750, 770, 775 Kubie drives, all other rats Axona drives). Drives  
345                   supported four or eight tetrodes, each of which was composed of four HML coated, 17  $\mu$ m  
346                   diameter, 90% platinum 10% iridium wires (California Fine Wire, Grover Beach, CA) which  
347                   were gold plated (Non-Cyanide Gold Plating Solution, Neuralynx, MT) in order to reduce the  
348                   impedance of the wire to a plated impedance in the range of 180–300 k $\Omega$ . Microdrives were  
349                   implanted using standard stereotaxic procedures under isoflurane anesthesia <sup>29</sup>. Electrodes  
350                   were lowered to just above the CA1 cell layer of the hippocampus (-3.5 mm AP from  
351                   bregma,  $\pm$ 2.4 mm ML from the midline, ~1.5 mm DV from dura surface). See Fig. S15  
352                   histology results.

353                   *Apparatus*

354                   A detailed description of the room and apparatus can be found in Supplementary  
355                   Methods: *Apparatus*, photographs and schematics can be seen in Fig. 1. Briefly, we used  
356                   three main pieces of experimental apparatus: a square open field environment ('arena'), a  
357                   cubic lattice composed of horizontal and vertical climbing bars ('aligned' lattice) and the  
358                   same lattice rotated to stand on one of its vertices ('tilted' lattice). Rats were recorded freely  
359                   foraging in the arena for randomly dispersed flavored puffed rice (CocoPops, Kellogg's,

360 Warrington, UK) and foraging in the lattice maze for malt paste (GimCat Malt-Soft Paste, H.  
361 von Gimborn GmbH) affixed to bars of the lattice.

362 *Recording setup and procedure*

363 A detailed description of the recording setup used can be found in Supplementary  
364 Methods: *Recording setup and procedure*. Briefly, single unit activity was observed and  
365 recorded using a custom built 64-channel recording system (Axona, St. Albans, UK) and a  
366 wireless headstage (custom 64-channel, W-series, Triangle Biosystems Int., Durham, NC)  
367 mounted with infrared LEDs. Five infrared sensitive CCTV cameras (Samsung SCB-5000P)  
368 tracked the animal's position at all times. For experimental sessions, rats were recorded for  
369 a minimum of 18 minutes in the arena, followed by a minimum of 45 minutes in one  
370 configuration of the lattice and a further minimum 16 minutes in the arena. Video footage of  
371 animal behavior and position tracking in the arena and aligned lattice can be seen in  
372 Supplementary Video S4.

373 *Behavioral analyses*

374 A detailed description of positional estimation and three-dimensional trajectory  
375 reconstruction can be found in Supplementary Methods: *Trajectory reconstruction*. A  
376 detailed description of the methods used to analyze 3D behavior and heading directions can  
377 be found in Supplementary Methods: *Behavior and spherical heat maps*. Briefly, we  
378 calculated the instantaneous three-dimensional heading of the animal as the normalized  
379 change in position between time points, essentially 3D vectors pointing from one position to  
380 the next. We projected these heading vectors onto a unit sphere and generated a heatmap  
381 of the result using a density estimation approach designed for spherical data. This process  
382 can be seen in Supplementary Video S3. Using the underlying points we calculated the  
383 proportion of heading vectors (i.e. the proportion of total time) aligned, within a narrow range,  
384 parallel to each maze axis. By dividing position data based on the position of the lattice we  
385 were also able to calculate the time spent in the inner and outer 50% volume of the lattice or

386 the top and bottom 50%. To compare speed profiles between mazes, for each session we  
387 calculated the proportion of time spent moving at speeds between 2 and 50 cm/s in 2 cm/s  
388 wide bins.

389 *Firing rate maps*

390 For all analyses other than those described in *Recording stability* and *Field stability*,  
391 three-dimensional volumetric firing rate maps were constructed using a similar approach to  
392 that reported previously<sup>30</sup>. The firing rate in each voxel (50x50x50mm) was calculated as  
393 the distance from the voxel center to every recorded spike in the neighboring 26 voxels,  
394 divided by the distance to every position data point in these voxels. These distances were  
395 weighted using a truncated Gaussian function such that spikes and position data closer to a  
396 voxel's center had more influence on that voxel's firing rate and data outside the neighboring  
397 26 voxels had no influence on the firing rate. The Gaussian used was defined as:

398 
$$g(x) = e^{-0.5\left(\frac{|x-x|}{\sigma}\right)}$$

399 Firing rate was then calculated as:

400 
$$f(x) = \frac{\sum_{i=1}^n g(S_i - x)}{\int_0^T g(y(t) - x)}$$

401 where  $d$  is the distance threshold of the Gaussian, which was set to 1.5 voxels,  $\sigma$  is the  
402 standard deviation of the Gaussian, which was set to 1 voxel width,  $S_i$  represents the  
403 position of every recorded spike,  $x$  is the voxel center, the period  $[0 T]$  is the recording  
404 session time period,  $y(t)$  is the position of the rat at time  $t$ . If the rat did not explore within  
405 100 mm of a voxel, or if he spent less than 1 second there, the voxel was considered  
406 unvisited.

407 *Recording stability*

408 To verify that cells were stably recorded during our maze sessions we computed the  
409 Pearson correlation between our first and second arena ratemaps (recorded before and after  
410 lattice maze sessions). These maps were generated by projecting data onto the Cartesian  
411 planes before calculating 2D firing rate maps in the standard manner; as bivariate  
412 histograms with 5cm square bins smoothed using a Gaussian with 5cm standard deviation  
413 (Matlab function *imgaussfilt*). Volumetric maps were generated as multivariate histograms  
414 with 5cm cubic bins smoothed using a Gaussian with 5cm standard deviation (Matlab  
415 function *imgaussfilt3*). In both cases spike and position data were truncated to include only  
416 the data falling within the lattice maze frame. We compared this data to values calculated in  
417 the same way but comparing open field sessions from random cells whilst maintaining their  
418 temporal order (i.e. first arena vs second arena from a random cell) for each shuffle we did  
419 this 1000 times.

420 *Place cell criteria*

421 A cluster was classified as a place cell if it satisfied the following criteria in the  
422 session with the greatest number of spikes: i) the peak to trough width of the waveform with  
423 the highest amplitude was >250  $\mu$ s, ii) the mean firing rate was greater than 0.1 Hz but less  
424 than 10 Hz and iii) the spatial information content was greater than 0.5 b/s. Spatial  
425 information content was defined as:

$$426 \quad \text{information content} = \sum P_i \left( \frac{R_i}{R} \right) \log_2 \left( \frac{R_i}{R} \right)$$

427 where  $i$  is the voxel number,  $P_i$  is the probability for occupancy of voxel  $i$ ,  $R_i$  is the mean  
428 firing rate for voxel  $i$ , and  $R$  is the overall average firing rate <sup>31</sup>. In combination with these  
429 parameters we also manually refined the resulting place cell classification in order to resolve  
430 false positives and negatives.

431        *Place field characteristics*

432        A detailed description of the features used to describe place fields can be found in the

433        Supplementary Methods sections: *Field detection*, *Field volume and density*, *Field*

434        *orientation and size*, *Field elongation and sphericity*, *Field stability* and *Field distribution*.

435        Briefly, for ease of comparison to existing literature most of the analyses we used were

436        simply extensions of those used for two-dimensional data. Firing rate maps were constructed

437        as above; these were thresholded at 20% of the peak firing rate and from this contiguous

438        regions of high firing rate were then isolated. Regions larger than 64 voxels and visited more

439        than 5 times were then analyzed as putative place fields. We calculated their volume (total

440        volume of voxels in region), centroid (average voxel position), length along each Cartesian

441        axis (side lengths of minimum enclosing cuboid) and diameter (diameter of minimum

442        enclosing sphere).

443        In a departure from two dimensional analyses we fitted a multivariate normal distribution

444        (i.e. a 3D ellipse) to each field and from this extracted the field's principal axes (the three

445        axes defining the ellipse), orientation (orientation of the field's longest axis), elongation

446        (longest axis length divided by the mean of the other two, or second longest in the arena)

447        and sphericity (ratio of surface area to a sphere of equivalent diameter). To determine

448        whether fields were as or more spherical than would be expected by chance we used a

449        shuffle procedure similar to that reported previously<sup>9</sup> (Supplementary Methods: *Field*

450        *elongation and sphericity*). To calculate fields per m<sup>3</sup> for each maze we estimated the

451        volume of the maze as the average volume of trajectories recorded in the maze

452        (Supplementary Methods: *Field volume and density*). To determine whether fields were

453        homogeneously distributed throughout the mazes we compared their distribution around the

454        center of the maze to a 1000 shuffles of random points (shaded areas Fig. 5e, Supp.

455        Methods: *Field distribution*).

456 *Field orientation*

457 To generate the three-dimensional spherical heatmaps of field orientation and calculate  
458 the number of fields aligned with each maze axis we used the same analysis described for  
459 the behavioral data (see Methods: *Behavioral analyses* and Supp. Methods: *Field orientation*  
460 *and size*). Briefly, we counted the number of fields that had an orientation within a 60° cone  
461 around each maze axis (i.e. a vertical field would have a vertically oriented longest axis  
462 which would also run parallel to the Z-axis). To compare between mazes we calculated a  
463 ratio of XYZ oriented fields to ABC oriented fields.

464 To determine whether fields were oriented parallel to one axis more than another we  
465 calculated 95% confidence intervals for each observed axis value using a bootstrapping  
466 procedure (error bars in Fig. 7c). If the value of one axis fell within the error bounds of  
467 another axis we considered them not significantly different. To determine whether fields were  
468 aligned with one or more axes at a frequency greater than would be expected by chance we  
469 randomly distributed 1000 points across the surface of a sphere 1000 times, and for each  
470 shuffle computed the number of points falling within the region corresponding to each axis. If  
471 the number of real fields aligned with a particular axis exceeded the 2.5<sup>th</sup> or 97.5<sup>th</sup> percentile  
472 of these shuffled counts (red areas in Fig. 7c) it was considered to be significantly under or  
473 overrepresented respectively. For each shuffle we also calculated the ratio of XYZ to ABC  
474 fields and if the observed ratio of a maze exceeded the 1<sup>st</sup> or 99<sup>th</sup> percentile of the ratios  
475 obtained in the shuffle (blue and red lines in Fig. 7c inset respectively) it was defined as  
476 significantly deviating from 1 (no axis bias of any kind) and indicated an overrepresentation  
477 of ABC or XYZ fields respectively.

478 *Spatial coding*

479 A detailed description and schematics of these methods can be found in Supplementary  
480 Methods: *Autocorrelation and spatial information*. Briefly, we generated three dimensional  
481 autocorrelations using an extension of two-dimensional methods. We then extracted the

482 central regions along each axis (i.e. a skewer running through the middle of the cube from  
483 one end to the other would represent one central section) to see whether correlations were  
484 higher along one axis and if this was related to the proximity of voxels (see Fig. S19 for a  
485 schematic). We also projected data onto the three possible cardinal planes by averaging  
486 firing rate maps along each dimension (i.e. averaging ‘floors’ of the aligned lattice results in a  
487 single two-dimensional map in X and Y, which would be the average along the Z axis). After  
488 isolating fields (see Methods: *Place field characteristics*) we also summed the fields along  
489 each dimension, peak-normalized the resulting vectors and calculated the area under the  
490 curve (AUC) for each (Matlab function *trapz*).

491 *Field stability*

492 To test the stability of spatial representations within sessions we divided maze  
493 sessions into two halves of equal length (first 50% and second 50%) and computed the  
494 Pearson correlation (Matlab function *corr*) between the firing rate maps for these halves. As  
495 for *Recording stability*, these maps were generated by projecting data onto the Cartesian  
496 planes before calculating 2D firing rate maps in the standard manner; as bivariate  
497 histograms with 5cm square bins smoothed using a Gaussian with 5cm standard deviation  
498 (Matlab function *imgaussfilt*). Volumetric maps were also generated as multivariate  
499 histograms with 5cm cubic bins smoothed using a Gaussian with 5cm standard deviation  
500 (Matlab function *imgaussfilt3*). In both cases, spike and position data were truncated to  
501 include only the data falling within the lattice maze frame. In all cases, higher correlations  
502 were observed when dividing sessions based on odd and even minutes so these data are  
503 not shown. We compared these values to shuffled distributions generated by comparing  
504 session halves from random cells (i.e. first 50% vs second 50% from a random cell). For  
505 each projection and volumetric map we did this 1000 times with replacement.

506

507

508 **References**

- 509 1. Tolman, E. C. Cognitive maps in rats and men. *Psychol. Rev.* **55**, 189–208 (1948).
- 510 2. O'Keefe, J. & Nadel, L. *The Hippocampus as a Cognitive Map*. (Clarendon Press,  
511 1978).
- 512 3. Jeffery, K. J., Wilson, J. J., Casali, G. & Hayman, R. M. Neural encoding of large-  
513 scale three-dimensional space—properties and constraints. *Front. Psychol.* **6**, 927  
514 (2015).
- 515 4. Jeffery, K. J. K. J. K. J., Jovalekic, A., Verriotis, M. & Hayman, R. Navigating in a  
516 three-dimensional world. *Behav. Brain Sci.* **36**, 523–543 (2013).
- 517 5. Finkelstein, A., Las, L. & Ulanovsky, N. 3-D Maps and compasses in the brain. *Annu.*  
518 *Rev. Neurosci.* **39**, 171–196 (2016).
- 519 6. Hayman, R., Verriotis, M. A., Jovalekic, A., Fenton, A. A. & Jeffery, K. J. K. J.  
520 Anisotropic encoding of three-dimensional space by place cells and grid cells. *Nat.*  
521 *Neurosci.* **14**, 1182–1188 (2011).
- 522 7. Casali, G., Bush, D. & Jeffery, K. J. Altered neural odometry in the vertical dimension.  
523 *PNAS* doi:10.1073/pnas.1811867116
- 524 8. Gibson, J. J. *The Ecological Approach to Visual Perception*. (Lawrence Erlbaum  
525 Associates, 1986).
- 526 9. Yartsev, M. M. & Ulanovsky, N. Representation of three-dimensional space in the  
527 hippocampus of flying bats. *Science* **340**, 367–72 (2013).
- 528 10. Jovalekic, A. *et al.* Horizontal biases in rats' use of three-dimensional space. *Behav.*  
529 *Brain Res.* (2011). doi:10.1016/j.bbr.2011.02.035

- 530 11. Geva-Sagiv, M., Las, L., Yovel, Y. & Ulanovsky, N. Spatial cognition in bats and rats:  
531 from sensory acquisition to multiscale maps and navigation. *Nat. Rev. Neurosci.* **16**,  
532 94–108 (2015).
- 533 12. Muller, R. U. & Kubie, J. L. The effects of changes in the environment on the spatial  
534 firing of hippocampal complex-spike cells. *J. Neurosci.* **7**, 1951 LP – 1968 (1987).
- 535 13. Park, E., Dvorak, D. & Fenton, A. A. Ensemble Place codes in hippocampus: CA1,  
536 CA3, and dentate gyrus place cells have multiple place fields in large environments.  
537 *PLoS One* **6**, e22349 (2011).
- 538 14. O'Keefe, J. & Burgess, N. Geometric determinants of the place fields of hippocampal  
539 neurons. *Nature* **381**, 425–428 (1996).
- 540 15. Burgess, N. & O'Keefe, J. Neuronal computations underlying the firing of place cells  
541 and their role in navigation. *Hippocampus* **6**, 749–762 (1996).
- 542 16. Barry, C. *et al.* The boundary vector cell model of place cell firing and spatial memory.  
543 *Rev. Neurosci.* **17**, 71–97 (2006).
- 544 17. Bjerkenes, T. L., Moser, E. I. & Moser, M.-B. Representation of geometric borders in  
545 the developing rat. *Neuron* **82**, (2014).
- 546 18. Lever, C., Burton, S., Jeewajee, A., O'Keefe, J. & Burgess, N. Boundary vector cells  
547 in the subiculum of the hippocampal formation. *J. Neurosci.* **29**, 9771–9777 (2009).
- 548 19. Solstad, T., Boccara, C. N., Kropff, E., Moser, M. B. & Moser, E. I. Representation of  
549 geometric borders in the entorhinal cortex. *Science (New York, N.Y.)* **322**, 1865–1868  
550 (2008).
- 551 20. Hardcastle, K., Ganguli, S. & Giocomo, L. M. Environmental boundaries as an error  
552 correction mechanism for grid cells. *Neuron* **86**, 827–839

- 553 21. Mehta, M. R., Barnes, C. A. & McNaughton, B. L. Experience-dependent, asymmetric  
554 expansion of hippocampal place fields. *Proc. Natl. Acad. Sci.* **94**, 8918 LP – 8921  
555 (1997).
- 556 22. Mehta, M. R., Quirk, M. C. & Wilson, M. A. Experience-dependent asymmetric shape  
557 of hippocampal receptive fields. *Neuron* **25**, 707–715 (2000).
- 558 23. Kim, M., Jeffery, K. J. & Maguire, E. A. Multivoxel pattern analysis reveals 3D place  
559 information in the human hippocampus. *J. Neurosci.* **37**, 4270–4279 (2017).
- 560 24. Brandt, T. *et al.* “Taller and shorter”: human 3-D spatial memory distorts familiar  
561 multilevel buildings. *PLoS One* **10**, e0141257 (2015).
- 562 25. Wilson, P. N., Foreman, N., Stanton, D. & Duffy, H. Memory for targets in a multilevel  
563 simulated environment: Evidence for vertical asymmetry in spatial memory. *Mem.*  
564 *Cognit.* **32**, 283–297 (2004).
- 565 26. Dollé, L., Droulez, J., Bennequin, D., Berthoz, A. & Thibault, G. How the learning path  
566 and the very structure of a multifloored environment influence human spatial memory.  
567 *Adv. Cogn. Psychol.* **11**, 156–162 (2015).
- 568 27. Page, H. J. I., Wilson, J. J. & Jeffery, K. J. A dual-axis rotation rule for updating the  
569 head direction cell reference frame during movement in three dimensions. *J.*  
570 *Neurophysiol.* **119**, 192–208 (2018).
- 571 28. Laurens, J. & Angelaki, D. E. The brain compass: A perspective on how self-motion  
572 updates the head direction cell attractor. *Neuron* **97**, 275–289 (2018).
- 573 29. Grieves, R. M., Jenkins, B. W., Harland, B., Wood, E. R. & Dudchenko, P. A. Place  
574 field repetition and spatial learning in a multicompartment environment. *Hippocampus*  
575 **26**, (2016).

576 30. Leutgeb, S. *et al.* Independent codes for spatial and episodic memory in hippocampal  
577 neuronal ensembles. *Science* (80-). **309**, 619–623 (2005).

578 31. Skaggs, W. E., McNaughton, B. L., Wilson, M. A. & Barnes, C. A. Theta phase  
579 precession in hippocampal neuronal populations and the compression of temporal  
580 sequences. *Hippocampus*. **6**, 149–172 (1996).

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6 **Author contributions**

7 K.J. conceived the study and obtained funding, S.R., R.G. and K.J. designed the  
8 protocol, R.G., S.J-A., K.M., A.L. and S.R. performed surgeries and recordings, R.G  
9 analyzed data. All authors interpreted data and discussed results. R.G. and K.J. wrote the  
10 manuscript. All authors commented and edited the manuscript.

11 **Competing financial interests**

12 K.J. is a non-shareholding director of Axona Ltd.

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