

# Sensor localization using magnetic dipole-like coils: A method for highly accurate co-registration in on-scalp MEG

Christoph Pfeiffer<sup>a,\*</sup>, Silvia Ruffieux<sup>a</sup>, Lau M. Andersen<sup>b</sup>, Alexei Kalabukhov<sup>a</sup>,  
Dag Winkler<sup>a</sup>, Robert Oostenveld<sup>d</sup>, Daniel Lundqvist<sup>b</sup>, Justin  
F. Schneiderman<sup>c</sup>

<sup>a</sup>*Department of Microtechnology and Nanoscience - MC2, Chalmers University of Technology, Gothenburg, Sweden*

<sup>b</sup>*NatMEG, Department of Clinical Neuroscience, The Karolinska Institute, Stockholm, Sweden*

<sup>c</sup>*MedTech West and the Institute of Neuroscience and Physiology, Sahlgrenska Academy, University of Gothenburg, Gothenburg, Sweden*

<sup>d</sup>*Donders Institute for Brain, Cognition and Behaviour, Radboud University, Nijmegen, Netherlands*

---

## Abstract

Source modelling in magnetoencephalography (MEG) requires precise co-registration of the sensor array and the anatomical structure of the measured individual's head. In conventional MEG, positions and orientations of the sensors relative to each other are fixed and known beforehand, requiring only localization of the head relative to the sensor array. Since the sensors in on-scalp MEG are positioned on the scalp, locations of the individual sensors depend on the subject's head shape and size. The positions and orientations of on-scalp sensors must therefore be measured at every recording. This can be achieved by inverting conventional head localization, localizing the sensors relative to the head - rather than the other way around.

In this study we present a practical method for localizing sensors using magnetic dipole-like coils attached to the subject's head. We implement and evaluate the method in a set of on-scalp MEG recordings using a 7-channel on-scalp MEG system based on high critical temperature superconducting quantum interfer-

---

\*Corresponding author

Email address: [christoph.pfeiffer@chalmers.se](mailto:christoph.pfeiffer@chalmers.se) (Christoph Pfeiffer)

ence devices (high- $T_c$  SQUIDs). The method provides accurate estimates of individual sensor positions and orientations with short averaging time ( $\leq 2$  mm and  $< 3$  degrees, respectively, with 1-second averaging), enabling continuous sensor localization. Calibrating and jointly localizing the sensor array can further improve the localization accuracy ( $< 1$  mm and  $< 2.5$  degrees, respectively, with 1-second coil recordings).

We demonstrate source localization of on-scalp recorded somatosensory evoked activity based on co-registration with our method. Equivalent current dipole fits of the evoked responses corresponded well (within 5.3 mm) with those based on a commercial, whole-head MEG system.

*Keywords:* Magnetoencephalography (MEG), On-scalp MEG, Co-registration, Sensor localization, Magnetic dipole, coil, High-Tc SQUID.

---

## **1. Introduction**

2 On-scalp magnetoencephalography (MEG) has been shown in simulations  
3 to provide distinct advantages over traditional, low- $T_c$  SQUID-based MEG. At  
4 closer proximity to the head –and thus to the neural sources– on-scalp MEG  
5 should be able to measure weaker signals as well as capture higher spatial fre-  
6 quencies compared to conventional MEG [1, 2]. In addition to smaller standoff,  
7 on-scalp MEG sensors - primarily optically pumped magnetometers (OPMs)  
8 and high- $T_c$  SQUIDs - allow flexible sensing of the head; that is, the sensors  
9 can be moved (individually or in small units containing a few sensors) relative to  
10 each other in order for the sensor array to fit the head of individual subjects [3].  
11 This is especially beneficial for studies on children, whose heads are significantly  
12 smaller than the one-size-fits-all helmets in most commercial MEG systems [4].

13 In general, translating MEG (sensor-level) signals to neural (source-level)  
14 activity requires co-registration of functional and structural data. An important  
15 step in this process is the reliable determination of the measurement/sensor  
16 locations relative to the subject’s head during the recording. In conventional  
17 MEG systems this is achieved by placing a set of small magnetic coils on the

18 subject's head and digitizing their positions with respect to landmarks (e.g.,  
19 fiducials) on the head. Energizing the coils at different times and/or frequencies  
20 and detecting the distribution of the magnetic fields they generate (with the  
21 MEG system) allows accurate localization of the coils relative to the MEG  
22 sensor array [5, 6]. In order to localize the coils in such a way, the positions  
23 and orientations of the sensors relative to each other have to be known. This  
24 presents an issue when using flexible sensor arrays in on-scalp MEG. Because the  
25 sensors in such a system would be at least partially independently positioned,  
26 the sensors' relative positions and orientations vary from subject to subject,  
27 and from session to session. Instead of a one-time calibration as used with  
28 rigid, whole-head sensor arrays, it is necessary to determine the sensor locations  
29 for each MEG recording session.

30 Measuring all the sensor positions and locations in a full-head array manu-  
31 ally would be very time consuming and cumbersome, especially in arrays with  
32 high channel count. We have therefore developed and simulated the efficacy of  
33 a method for localizing independent MEG sensors with an array of small, mag-  
34 netic dipole-like coils attached to the subject's head [7]. Herein, we present the  
35 implementation of this sensor localization method in MEG recordings with a 7-  
36 channel high-  $T_c$  SQUID-based on-scalp MEG system. We furthermore validate  
37 its utility by using in source localization of somatosensory evoked fields.

38 **2. Methods**

39 *2.1. Sensor localization*

For an array of on-scalp MEG sensors recording a set of magnetic dipole-like coils (e.g., head position indicator, HPI, coils), the signal generated at the  $k$ th magnetometer by the  $j$ th magnetic dipole whose moment is  $\vec{m}_j$  can be defined as

$$S_{k,j} = \frac{\mu_0}{4\pi} \left( \frac{3\vec{r}_{j,k}(\vec{m}_j \cdot \vec{r}_{j,k})}{|\vec{r}_{j,k}|^5} - \frac{\vec{m}_j}{|\vec{r}_{j,k}|^3} \right) \cdot \vec{n}_k \quad (1)$$
$$= L_m(\vec{r}_{j,k}) \vec{m}_j \cdot \vec{n}_k$$

40 where  $L_m$  is the lead field,  $\vec{r}_{j,k} = \vec{r}_j - \vec{r}_k$  a vector defining the location of the  
 41 dipole  $j$  relative to sensor  $k$ ,  $\vec{n}_k = |n_k|\hat{n}_k$  a vector combining the orientation  
 42 ( $\hat{n}_k$ ) and sensitivity ( $|n_k|$ ) of sensor  $k$ , and  $\vec{m}_j$  the magnetic moment of dipole  
 43  $j$ .

The position and orientation of a magnetic dipole is fit to recorded data  $S_{k,j}^{rec}$  by finding the dipole location that minimizes the residual variance between the data and the calculated signals.

$$\arg \min_{\vec{r}_j, \vec{m}_j} \left( \frac{\sum_k (S_{k,j}^{rec} - L_m(\vec{r}_{j,k}) \vec{m}_j \cdot \vec{n}_k)^2}{\sum_k S_{j,k}^{rec2}} \right). \quad (2)$$

As described in [7], the standard coil localization procedure can be adapted to determine the position and orientation of an individual MEG sensor with respect to an array of coils by simply swapping the roles of magnetometers and dipoles:

$$\arg \min_{\vec{r}_k, \vec{n}_k} \left( \frac{\sum_j (S_{k,j}^{rec} - L_m(\vec{r}_{k,j}) \vec{n}_k \cdot \vec{m}_j)^2}{\sum_j S_{j,k}^{rec2}} \right). \quad (3)$$

The on-scalp MEG system used here employs seven sensors that are fixed relative to each other in a single cryostat [8]. When multiple sensors are fixed relative to each other it is, in principle, possible to improve their localization by taking into account the array's geometry [7]. Instead of solving eq. 3 for each sensor individually, the array can be combined into a single localization routine, wherein a single rigid transformation (rotation and translation) is applied to the whole sensor array. The number of parameters to be estimated is thus reduced by a factor of 7 compared to localizing the sensors individually. In this case, eq. 3 is replaced by:

$$\arg \min_{T,R} \left( \sum_k \frac{\sum_j (S_{k,j}^{rec} - L_m(\vec{r}'_{k,j}) \vec{n}'_k \cdot \vec{m}_j)^2}{\sum_j S_{j,k}^{rec2}} \right) \quad (4)$$

44 where  $T$  and  $R$  describe the 3-dimensional translation and rotation applied to  
 45 the entire array,  $\vec{r}'_{k,j} = (R\vec{r}_k + T) - \vec{r}_j$  is the location of the rigidly transformed  
 46 position of sensor  $k$  relative to dipole  $j$ , and  $\vec{n}'_k = R\vec{n}_k$  the rigidly transformed  
 47 sensitivity vector.

48 To reduce the impact that noisy sensors can have on the localization accuracy,  
49 the sensors can be weighted according to their signal-to-noise ratio when  
50 summing the residual variances in eq. 4.

$$\arg \min_{T,R} \left( \sum_k w_k \frac{\sum_j (S_{k,j}^{rec} - L_m(\vec{r}'_{k,j}) \vec{n}'_k \cdot \vec{m}_j)^2}{\sum_j S_{j,k}^{rec2}} \right) \quad (5)$$

51 where  $w_k = \frac{SNR_k}{\sum_k SNR_k}$  is the weight applied to the k-th sensor.

## 52 *2.2. Measurement setup*

53 The sensor localizations described here were performed as part of a set of  
54 MEG recordings at the National MEG Facility (NatMEG) at the Karolinska  
55 Institutet in Stockholm, Sweden. The main aim of the recordings was to compare  
56 and contrast recordings with a 7-channel high- $T_c$  SQUID-based on-scalp  
57 system [8] to recordings with a commercial, whole-head system - in this case,  
58 a 306-channel Elekta TRIUX system (Elekta Neuromag Oy). Several different  
59 experimental paradigms were recorded in five neurotypical subjects (4 male and  
60 1 female, ages 30-49). For each session the same paradigm was first recorded  
61 on a subject with the commercial MEG system, followed by the on-scalp MEG  
62 recording. All experiments were approved by the Swedish Ethical Review Authority  
63 (EPN 2018-571-31-1) and conducted in compliance with national legislation  
64 and the code of ethical principles defined in the Declaration of Helsinki.  
65 All participants gave informed consent.

66 Ten dipole-like head position indicator (HPI) coils of the TRIUX system were  
67 used both in the head localization as part of the conventional MEG recordings  
68 and in the sensor localization as part of the on-scalp recordings. The coils were  
69 driven at frequencies from 537 to 987 in steps of 50 Hz. The frequencies were  
70 chosen relatively high in order to spectrally separate them from neural activity  
71 (including high frequency components up to 500 Hz). The frequency steps are  
72 chosen such that potential intermittent-frequency artefacts would coincide with  
73 the power line harmonics (50 Hz in Sweden), which are filtered as part of the  
74 standard preprocessing and therefore do not require any additional treatment.

75 The recordings were divided into blocks of stimulations with the coils energized  
76 for 10 to 30 seconds before and after each block. This was done as a cautionary  
77 measure to prevent potential artifacts from the coils to corrupt the MEG record-  
78 ings. Recording before and after each stimulation block also allowed monitoring  
79 if/how the head moved.

80 The subjects were recorded seated with their heads comfortably stabilized  
81 using vacuum pillows (without being completely immobilized). To further min-  
82 imize head movements during the coil recordings, the subjects were instructed  
83 to keep their head still. For each paradigm (in some cases two paradigms with  
84 similar neural activation) a coarse region of interest was determined prior to the  
85 recording session based on knowledge about the expected activity and/or previ-  
86 ous recordings on the same subject using the same or a similar paradigm. The  
87 coils were then distributed closely around the region of interest, while maintain-  
88 ing sufficient room for placement of the cryostat. In order to minimize relative  
89 movements between coils, nine coils were fixed to small plastic plates (three coils  
90 per plate) that were roughly shaped to fit to the subject's head. The tenth coil  
91 was then fixed to the head individually. Figure 1 shows a set of coils arranged  
92 around a region of interest on an EEG cap on one of the subject's head. The  
93 red tags mark the different target locations for the on-scalp system. The coils,  
94 head shape and target location tags were digitized using a AC electromagnetic  
95 tracking system Polhemus Fastrak (Polhemus, Colchester, VT 05446, USA).

96 At the beginning of each recording the subject was recorded in the TRIUX  
97 system. These recordings were used to localize the underlying neural activity  
98 and project the resulting neuromagnetic fields onto the scalp surface. Such field  
99 maps were used to guide the placement of the cryostat (i.e., the red markers in  
100 Fig. 1) for each experimental paradigm and subject [9, 10]. More importantly  
101 for localizing the sensors, the whole-head recordings were used to determine  
102 the positions, orientations, and magnetic moments of the coils relative to each  
103 other and to the head via traditional head localization [5]. HPI coil locations  
104 and orientations obtained thus were used for the ensuing on-scalp recordings.  
105 Only coil locations where the goodness of fit exceeded 0.98 were used in the

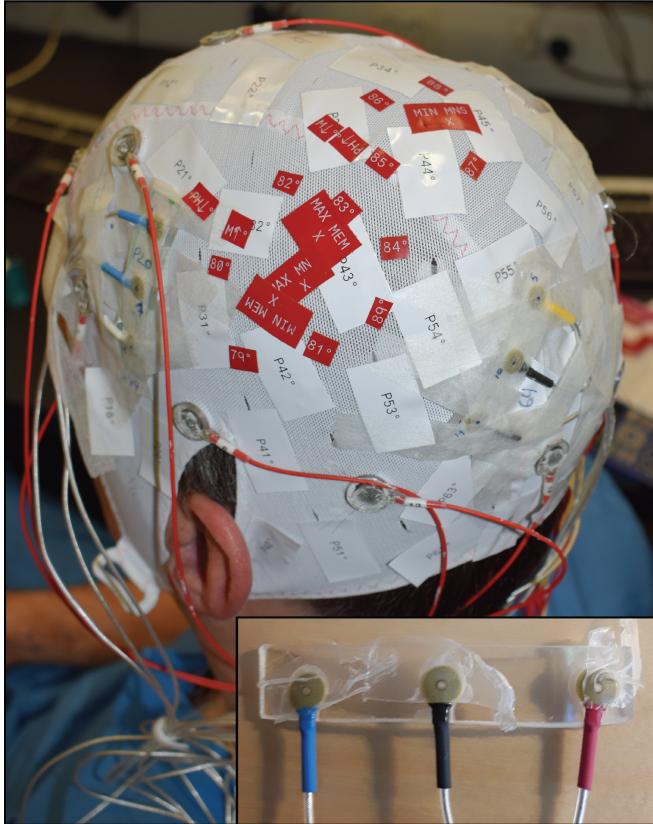


Figure 1: Photograph showing HPI coils attached to a subjects head. Three triplets of coils (each attached to a rectangular plastic holder) can be seen surrounding a region of interest marked by red tags that indicate measurement locations. Inset: a plastic holder with three HPI coils attached.

106 sensor localization.

107 The sensor fits were performed in MATLAB R2015a (Mathworks, Natick,  
108 MA, USA) using the FieldTrip toolbox [11]. The coil amplitudes were extracted  
109 from the data via multitaper frequency transform using Slepian tapers and used  
110 in a linear grid search to provide a starting point for the non-linear fit. Finally,  
111 the sensor locations were fitted to the extracted coil amplitudes by solving eq.  
112 3 using unconstrained optimization (quasi-newton algorithm) with the starting  
113 point obtained from the grid search.

114 When fitting the sensors jointly, the known layout of the sensor array is  
115 rigidly aligned to the individually fitted sensor locations using an iterative clos-  
116 est points (ICP) algorithm that was modified to minimize distances between  
117 corresponding point pairs (that is, points corresponding to the same sensor)  
118 rather than closest points. The resulting transformed sensor array then serves  
119 as starting point for a non-linear fit.

120 *2.3. Evaluation*

121 Defining the performance of the sensor localization is not straightforward in  
122 a realistic measurement setup, like the one we present here, wherein the "ground  
123 truth" (i.e., the true sensor locations relative to the head) is not known with  
124 arbitrary precision. Generally, the accuracy of the fitted locations are affected  
125 by a combination of random errors (e.g., due to sensor noise), systematic errors  
126 (resulting from, e.g., errors in the coil positions) and variations in the true  
127 location (resulting from head movements).

128 *2.3.1. Random errors*

129 Assuming head movements are negligible during a single (30 second) record-  
130 ing, we estimate the effects of random errors. We split each 30-second coil  
131 recording into multiple shorter segments, each of which was independently used  
132 to localize the sensors. Variations in an individual sensor's location over seg-  
133 ments were then used to provide an estimate of the sensor localization accuracy.  
134 To this end, we define  $MD(\vec{r}_{k,i}) = \|\bar{r}_k - \vec{r}_{k,i}\|$  as the euclidean distance of the  
135 i-th segment's fitted position  $\vec{r}_{k,i}$  from the mean location  $\bar{r}_k$  over all such seg-  
136 ments. Describing the spread of the sensor locations around the mean  $MD$  pro-  
137 vides an estimate of random errors - and thus the location accuracy. Similarly,  
138 we define  $aMD(\hat{n}_{k,i}) = 2 \arcsin(\|\bar{n}_k - \hat{n}_{k,i}\|/2)$  as an estimate of the angular  
139 accuracy (i.e., the segment-by-segment angular deviation of the corresponding  
140 sensor orientations from the mean orientation over segments  $\bar{n}_k = \frac{1}{N} \sum \hat{n}_{k,i}$ ).

141 *2.3.2. Systematic errors*

142 One limitation to these metrics is that they do not provide information about  
143 systematic errors that would result in a shift in the mean position. Furthermore,  
144 despite subjects' efforts to minimize head movement during coil recordings, the  
145 possibility of small movements cannot be excluded - the subjects heads were  
146 comfortably stabilized with vacuum pillows, but not immobilized. These issues  
147 can be dealt with by taking advantage of the fact that the sensors are housed in  
148 a common cryostat, i.e., fixed relative to each other. The distances between the  
149 (true) sensor locations are thus constant and independent of head movements.  
150 Localization errors can therefore also be estimated by comparing the distances  
151 between the fitted sensor locations with those from the known layout of the  
152 sensor array. To this end, we estimate a relative localization accuracy as the  
153 average deviation of the distances between the estimated sensor locations from  
154 the distances derived from the known layout:

$$\Delta XD(\vec{r}_{k,i}) = \frac{1}{N-1} \sum_{l=1}^N (||\vec{r}_{k,i} - \vec{r}_{l,i}|| - ||\vec{r}_k^* - \vec{r}_l^*||) \quad (6)$$

where  $\vec{r}_l$  and  $\vec{r}_k$  denote the positions of the localized sensors l and k,  $\vec{r}_l^*$  and  $\vec{r}_k^*$  their respective positions according to the reference (e.g., the system design), and N=7 the number of sensors. The sum is divided by N-1 because the term for l=k is always zero. This metric is only useful for evaluating individual sensor fits because distances between sensors are constant and determined by the sensor array when jointly localizing the sensors (because the positions are a result of rigidly rotating and translating the sensor array). Analogously, we can estimate the relative localization accuracy with respect to the orientation as the average deviation of the angles between the estimated sensor orientations from the angles between the reference sensor orientations:

$$\Delta XA(\vec{n}_{k,i}) = \frac{2}{N-1} \sum_{l=1}^N (\arcsin\left(\frac{||\vec{n}_{k,i} - \vec{n}_{l,i}||}{2}\right) - \arcsin\left(\frac{||\vec{n}_k^* - \vec{n}_l^*||}{2}\right)) \quad (7)$$

155 where  $\vec{n}_l$  and  $\vec{n}_k$  denote the orientations of the localized sensors l and k and  $\vec{n}_l^*$   
156 and  $\vec{n}_k^*$  their orientations according to the reference (e.g., the system design).

157 *2.3.3. Head movements*

158 Localizing sensors from shorter coil recordings/segments is favourable when  
159 trying to detect - and compensate for - head movements as it enables estima-  
160 tion of recording positions with higher temporal resolution. This is how head  
161 movements are conventionally detected/tracked: the sensor locations with re-  
162 spect to the head are estimated at multiple time instances and compared to the  
163 initial position. In order for us to investigate how the accuracy of the sensor  
164 localization depends on the time the coil signals are recorded,  $MD$ ,  $aMD$  and  
165  $\Delta XD$  were computed for different segment lengths  $t_{trial}$  between 1 and 10 sec-  
166 onds. For each segment length, the 30 seconds coil recording was split into  $n =$   
167  $30/t_{trial}$  consecutive trials.

168 *2.3.4. Source localization*

169 Finally, we tested the usefulness of our sensor localization procedure in  
170 localizing neural activity. The MEG experiments included recordings of so-  
171 matosensory evoked fields (SEFs). Using our sensor localization method for  
172 co-registration of the on-scalp data, source localization of the N20m-component  
173 was performed and compared to source localization using the conventional MEG  
174 data recorded with the TRIUX system. Because of the small coverage of the  
175 on-scalp system we recorded at four separate locations (aimed to capture the  
176 dipolar field pattern of the N20m-component) and combined the resulting data.  
177 One sensor was excluded due to excessive noise, resulting in 24 individual sensor  
178 locations. The same experimental paradigm - electric stimulation (below motor  
179 threshold) of the median nerve with 360 ms inter-stimulus interval and 1 000  
180 repetitions - as well as preprocessing - bandpass filter between 5 and 200 Hz  
181 with bandstop filters applied at 50 Hz and harmonics, 50 ms pre- to 200 ms  
182 post-stimulus epochs, baseline correction (-50 to 0 ms baseline window), and  
183 time-locked averaging - was used for the recordings with both systems. For  
184 comparability, only the magnetometers were used for the dipole fit with the  
185 TRIUX system.

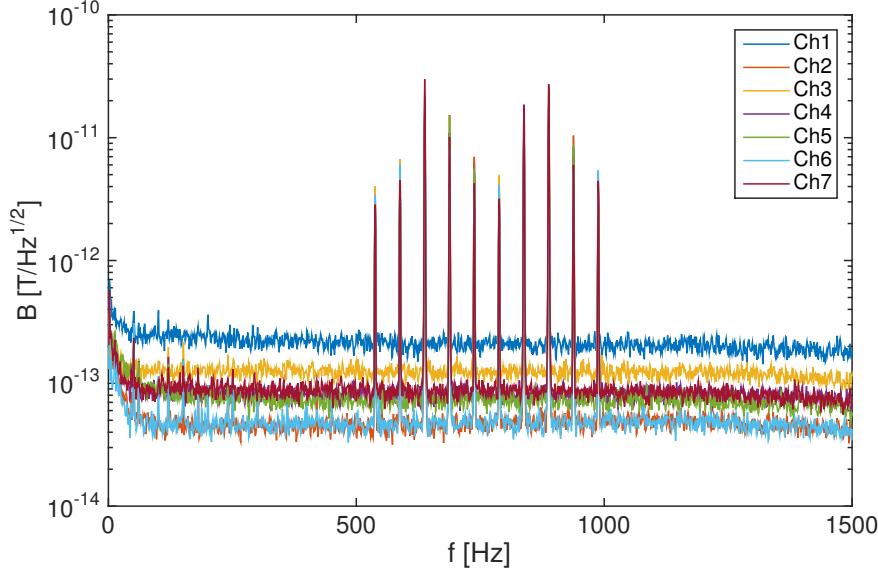


Figure 2: Spectrum of the measured magnetic fields showing peaks at the coil signal frequencies.

186 **3. Results**

187 The Fourier spectrum of a coil recording is shown in Fig. 2. Clear peaks  
188 with a signal-to-noise ratio (SNR) on the order of  $\sim 10^2$  are visible at the coil  
189 frequencies. An example of a sensor localization based on an 10-second trial  
190 can be seen in Fig. 3. In this case, the fitted sensor positions and orientations  
191 match well with the design of the sensor array (all pairs being within 0.5 mm  
192 and 2 degrees of the design) [8].

193 In some recordings, individual sensors trapped flux, which led to a strong  
194 increase in noise ( $\sim 10 \times$  higher white noise and a shift in the  $1/f$ -like noise  
195 knee from 10 to 500-1000 Hz). Localization of these noisy sensors was severely  
196 degraded - with errors on the order of centimeters. However, with such high  
197 noise data from these sensors was not useful for the MEG recordings and the  
198 sensor localization therefore inconsequential.

199 Fig. 4-a shows the mean euclidean distances of the fitted sensor locations

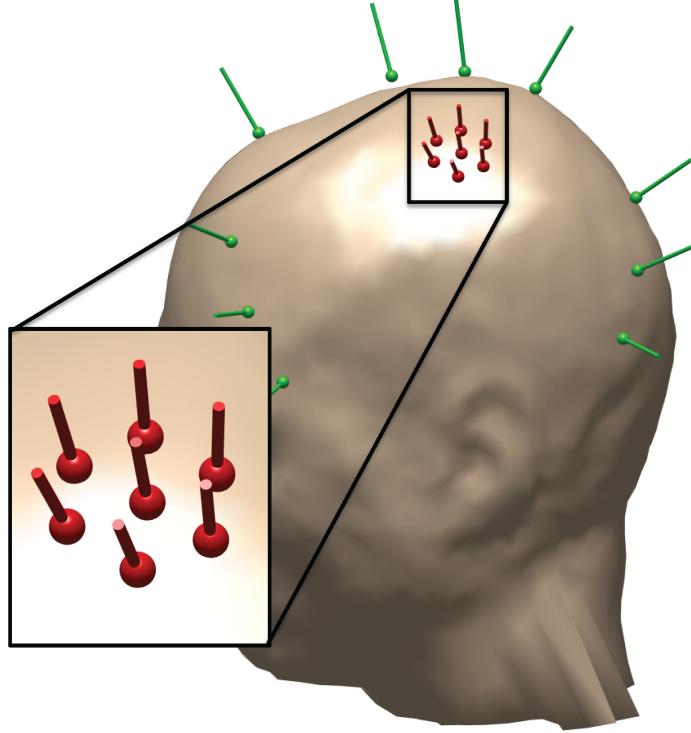


Figure 3: Example of individually fitted sensor locations and orientations (red). Magnetic dipoles from the coils are shown in green.

from the mean locations  $MD(\vec{r}_{k,i})$  as a function of the duration of the coil recording segments  $t_{trial}$  used for the localizations. As expected, a clear correlation between the localization accuracy and the length of the coil recordings can be observed. With the exception of channel 1 (which exhibited high noise in the recording) all channels reach  $MD < 1$  mm even with just 1-second recordings of the coil signals (channel 1 with four seconds or more). The mean angular deviations from the mean fitted sensor orientations  $aMD(\hat{n}_{k,i})$  - seen in Fig. 4-b - show a similar trend versus coil recording time. The orientation fits deviate from the mean by less than 3 degrees with one second of coil signal recording.

Fig. 5-a shows the mean differences of the distances between the fitted sen-

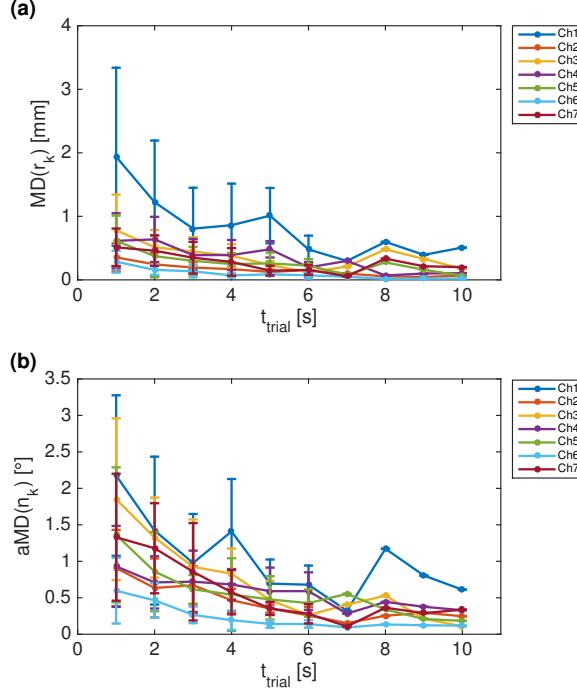


Figure 4: Sensor localization accuracy. a) Mean distance from the mean location  $\text{MD}(\vec{r}_{k,i})$  as a function of the segment length. b) Mean angular deviation from the mean orientation  $\text{aMD}(\vec{n}_{k,i})$  for different segment lengths. Error bars indicate one standard deviation.

210 sors from the distances between sensors in a reference array,  $\Delta XD(\vec{r}_k)$ . In this  
 211 case, we used the design of the system as the reference and again present results  
 212 for different lengths of coil recording segments  $t_{\text{trial}}$ . On average all channels  
 213 differ by less than 1 mm from the design already with 1-second coil record-  
 214 ings. With increasing  $t_{\text{trial}}$ , the mean  $\Delta XD(\vec{r}_k)$  converge to values  $< \pm 0.4$   
 215 mm. These can be assumed to stem from a combination of systematic errors  
 216 and small deviations between the actual sensor array and the design. As before,  
 217 the decrease of the standard deviation (i.e., the segment-by-segment spread)  
 218 with longer coil recording time indicates a decrease in random localization er-  
 219 rors. The mean differences of the angles between the fitted sensors from the  
 220 angles between the sensors in the design of the system  $\Delta XA(\vec{n}_k)$ , seen in Fig.

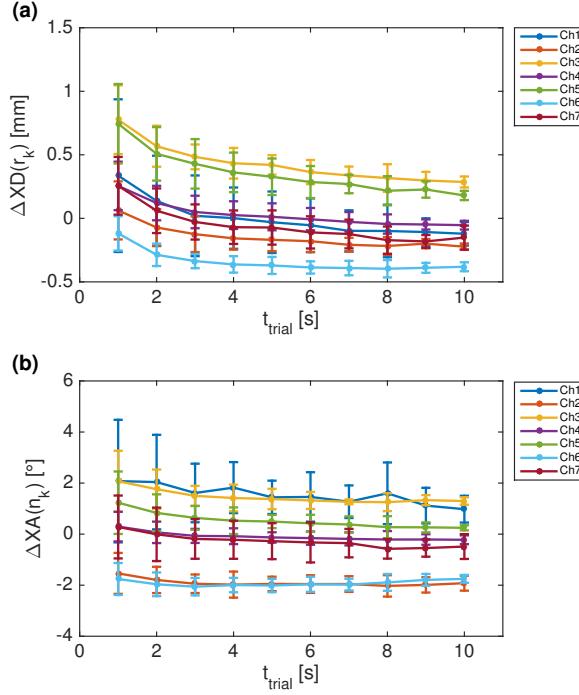


Figure 5: Pairwise sensor localization accuracy, with the cryostat design as the reference. a) Mean difference in distance to the other sensors  $\Delta XD(\vec{r}_k)$ . b) Mean difference in angle to the other sensors  $\Delta XA(\vec{n}_k)$ .

221 5-a, show a similar decrease in standard deviation with increasing coil recording  
 222 time. With 1 second coil recordings all channels differ by  $\sim 2$  degrees or less  
 223 from the design of the system.

224 Using short segments, it is possible to continuously monitor the sensor loc-  
 225 locations in order to detect movements of the head relative to the sensors. Head  
 226 movements manifest themselves as a shift and/or rotation of the whole sensor  
 227 array between segments. An example of a head movement captured with 2-  
 228 second coil recordings can be seen in figure 6. In this case, the subject's head  
 229 moved approximately 2 mm upwards during a stimulus session.

230 Distances from the mean location  $MD(\vec{r}_{k,i})$  as well as angular deviations  
 231 from the mean orientation  $aMD(\vec{n})_{k,i}$  when localizing the sensors jointly are

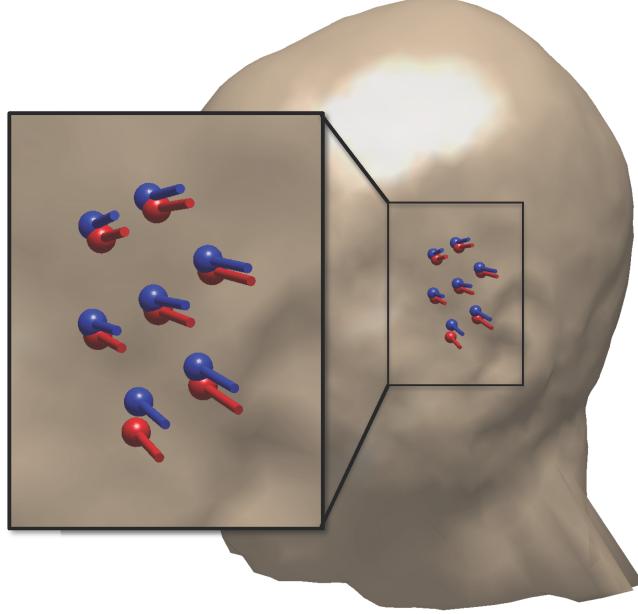


Figure 6: Successive sensor localizations (red and blue) showing head movement ( $\sim 2$  mm) between coil recordings.

232 shown in Fig. 7. The joint localizations were performed on the same data used  
233 to individually localize the sensors in Fig. 4. Both  $\text{MD}(\vec{r}_{k,i})$  and  $\text{aMD}(\vec{n}_{k,i})$   
234 show a similar trend as when localizing the sensors individually. Compared to  
235 the individual localization, the noisier sensors show significant improvement (es-  
236 pecially in  $\text{MD}(\vec{r}_{k,i})$ ) while the lower noise sensors worsen. However, the spread  
237 in location and orientation around the mean decreases in general, indicating an  
238 overall improvement in localization accuracy. This is especially pronounced in  
239 case of the location: with one second of data, all sensors exhibit  $\text{MD}(\vec{r}_{k,i}) < 1$  mm  
240 and  $\text{aMD}(\vec{n}_{k,i}) < 2.5$  degrees (compared to  $\leq 2$  mm and  $< 3$  degrees, respec-  
241 tively, when localizing them individually). The joint localizations shown here  
242 were performed using the sensor positions obtained via individually localizing  
243 the sensors with a 10-second coil recording to define the sensor array.

244 Weighting the sensors according to SNR to reduce the impact of noisy sensors  
245 (here, e.g., Ch1) did not result in an improvement in accuracy. In fact, the

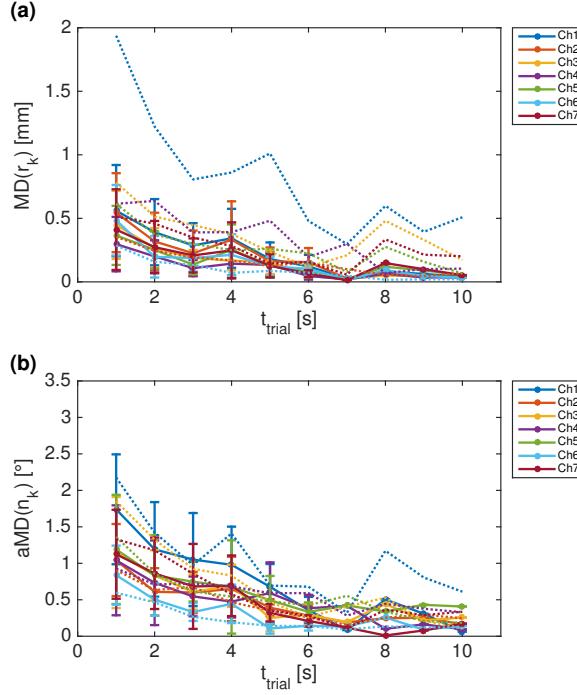


Figure 7: Joint sensor localization accuracy using the sensor locations obtained from 10-second coil recording individual localization as rigid sensor array. a) Mean distance from the mean location  $MD(\vec{r}_k)$  as a function of the segment length. b) Mean angular deviation from the mean orientation  $aMD(\vec{n}_k)$  for different segment lengths. Error bars indicate one standard deviation. For reference, we include the mean of the corresponding deviations that were obtained when localizing the sensors individually as dotted lines.

246 average accuracy for long coil recordings when localizing SNR-weighted sensors  
 247 was worse compared to localizing equally weighted sensors.

248 Dipole fits of the N20m-component recorded on-scalp and conventionally  
 249 can be seen in Fig. 8. The two dipoles are 5.3 mm apart, which is within the  
 250 localization accuracy of conventional whole-head MEG systems [12, 13].

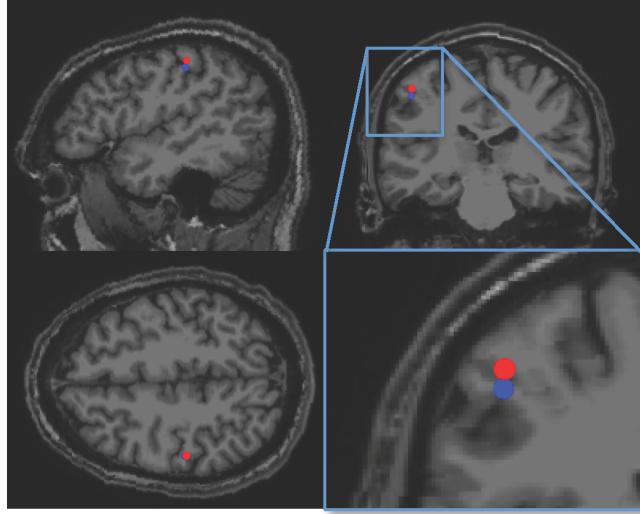


Figure 8: Dipole fits of N20m component based on on-scalp (red) and conventional (blue) MEG recording. The on-scalp dipole fit was performed using individually localized sensor positions estimated with our method.

251 **4. Discussion**

252 With  $\leq 2$  mm and  $< 3$  degrees for 1-second coil recordings, the sensor local-  
253 ization method described here reaches significantly higher accuracy than what  
254 has been suggested as required for on-scalp MEG ( $< 4$  mm and  $< 10$  degrees,  
255 according to [14]).

256 An advantage of our method is that it allows for continuous co-registration  
257 in parallel with the MEG recording. Movements of the subject's head during  
258 the MEG recording can thus be detected and accounted for, similarly to con-  
259 tinuous head localization used in commercial whole-head MEG systems. The  
260 measurements shown here were a first practical attempt of using the method  
261 described theoretically in [7]. However, as the experimental session was per-  
262 formed in parallel with other on-scalp MEG experiments, we erred on the side  
263 of caution by turning the coils off during stimulations (in order to avoid the  
264 possibility that they would generate artifacts that might compromise the MEG  
265 recordings). While it remains to be experimentally verified, it is likely that our

266 method can be used during a stimulus or other experimental protocol because  
267 the coil recordings showed no interference at frequencies below 500 Hz (see Fig.  
268 2). Furthermore, in cases where neural signals of interest coincide with the coil  
269 frequencies, it is trivial to change the coil frequencies to avoid potential inter-  
270 ference (if the neural frequencies of interest are known). The upper limit for  
271 the coil frequencies is strictly set by the Nyquist frequency (half of the sampling  
272 frequency, in this case  $5 \text{ kHz}/2 = 2.5 \text{ kHz}$ ) and generally should be kept well  
273 below any low-pass filters used by the data acquisition system (e.g., anti-aliasing  
274 filters, in our case 1 600 Hz).

275 Taking advantage of the fixed geometry of the sensor array to jointly localize  
276 the sensors proved useful. The increased accuracy at shorter segment lengths is  
277 especially important for continuous sensor localization. Furthermore, by using  
278 individually localized sensor positions from a longer coil recording to define the  
279 array geometry, the method is not limited to systems where the sensor array  
280 is rigid. For systems consisting of multiple individually positionable sensors  
281 [15, 16, 17] or units containing a few sensors [18], one can calibrate the sensor  
282 array at the start of a recording by carefully recording the coil signals for a  
283 longer duration of time (while minimizing head movement) and localizing the  
284 sensors individually. The calibrated array can then be used for fast, joint sensor  
285 localization. This, of course, assumes that the sensors are fixed with respect to  
286 one another for the duration of the recording.

287 Localized sensor positions and orientations were used to fit an equivalent  
288 current dipole to somatosensory evoked activity recorded sequentially at multiple  
289 locations. The estimated dipole position from the on-scalp recording was  $\sim 4 \text{ mm}$   
290 from that which was estimated from the conventional MEG recording. This lies  
291 well within the 8-11 mm variability seen between different commercial, whole-  
292 head MEG systems [13]. Considering the differences in sampling between on-  
293 scalp and conventional MEG, it is also possible that the on-scalp system is  
294 differently sensitive to neural activity, as compared conventional MEG. Previous  
295 works by our group with a high- $T_c$  SQUID [10] as well as by Zetter et al. [14]  
296 with OPMs also report differences between the N20m-components detected with

<sup>297</sup> on-scalp and conventional MEG systems.

<sup>298</sup> The measurements reported here were part of a series of benchmarking  
<sup>299</sup> recordings to compare an on-scalp MEG system [8] to a commercial, whole-  
<sup>300</sup> head MEG system. It was therefore possible to use full-head recordings of the  
<sup>301</sup> coil array on the subject's head in order to reliably estimate the positions and  
<sup>302</sup> orientations of the dipolar coils. This is, however, not a viable solution for on-  
<sup>303</sup> scalp systems in general. The coil orientations should instead be inferred from  
<sup>304</sup> other measurements. Flat coils with markers to digitize the orientation as part  
<sup>305</sup> of the head-digitization would be able to solve this issue in the future.

<sup>306</sup> **5. Conclusion**

<sup>307</sup> We have presented a method for localizing MEG sensors with the help of  
<sup>308</sup> magnetic dipole-like coils (introduced in [7]) and implemented it in a set of  
<sup>309</sup> on-scalp MEG recordings using a 7-channel, high- $T_c$  SQUID-based system [8].  
<sup>310</sup> The method provided high accuracy estimates of the sensor positions and ori-  
<sup>311</sup> entations with short averaging time ( $\leq 2$  mm and  $< 3$  degrees respectively  
<sup>312</sup> with 1-second coil recordings). It enables continuous estimation of the posi-  
<sup>313</sup> tions of sensors with respect to a subject's head (i.e., head localization) with  
<sup>314</sup> good temporal resolution. Calibrating and jointly localizing the sensor array  
<sup>315</sup> can furthermore improve the localization accuracy ( $< 1$  mm and  $< 2.5$  degrees  
<sup>316</sup> respectively with 1-second coil recordings). We demonstrate the efficacy of the  
<sup>317</sup> method by using it in localization of neural activity.

<sup>318</sup> **Acknowledgments**

<sup>319</sup> Data for this study was collected at NatMEG, the National infrastructure for  
<sup>320</sup> Magnetoencephalography, Karolinska Institutet, Sweden. The NatMEG facility  
<sup>321</sup> is supported by the Knut & Alice Wallenberg foundation (2011-0207). This  
<sup>322</sup> work was financially supported by the Knut and Alice Wallenberg foundation  
<sup>323</sup> (KAW 2014.0102), the Swedish Research Council (2017-00680), the Swedish

<sup>324</sup> Childhood Cancer Foundation (MT2014-0007), and Tillväxtverket via the Eu-  
<sup>325</sup> ropean Regional Development Fund (20201637).

<sup>326</sup> **References**

- <sup>327</sup> [1] E. Boto, R. Bowtell, P. Krüger, T. M. Fromhold, P. G. Morris, S. S. Meyer,  
<sup>328</sup> G. R. Barnes, M. J. Brookes, On the potential of a new generation of mag-  
<sup>329</sup> netometers for MEG: a beamformer simulation study, PLOS ONE 11 (8)  
<sup>330</sup> (2016) e0157655.
- <sup>331</sup> [2] J. Iivanainen, M. Stenroos, L. Parkkonen, Measuring MEG closer to the  
<sup>332</sup> brain: Performance of on-scalp sensor arrays, NeuroImage 147 (2017) 542–  
<sup>333</sup> 553.
- <sup>334</sup> [3] J. F. Schneiderman, S. Ruffieux, C. Pfeiffer, B. Riaz, On-scalp meg. in:  
<sup>335</sup> Supek s., aine c. (eds) magnetoencephalography, Springer (2019) 1–23.
- <sup>336</sup> [4] B. Riaz, C. Pfeiffer, J. F. Schneiderman, Evaluation of realistic layouts for  
<sup>337</sup> next generation on-scalp MEG: spatial information density maps, Scientific  
<sup>338</sup> Reports 7 (1) (2017) 6974.
- <sup>339</sup> [5] S. Erné, L. Narici, V. Pizzella, G. Romani, The positioning problem in bio-  
<sup>340</sup> magnetic measurements: A solution for arrays of superconducting sensors,  
<sup>341</sup> IEEE Transactions on Magnetics 23 (2) (1987) 1319–1322.
- <sup>342</sup> [6] K. Uutela, S. Taulu, M. Hämäläinen, Detecting and correcting for head  
<sup>343</sup> movements in neuromagnetic measurements, NeuroImage 14 (6) (2001)  
<sup>344</sup> 1424–1431.
- <sup>345</sup> [7] C. Pfeiffer, L. M. Andersen, D. Lundqvist, M. Hämäläinen, J. F. Schnei-  
<sup>346</sup> derman, R. Oostenveld, Localizing on-scalp MEG sensors using an array of  
<sup>347</sup> magnetic dipole coils, PLOS ONE 13 (5) (2018) e0191111.
- <sup>348</sup> [8] C. Pfeiffer, S. Ruffieux, L. Jönsson, M. L. Chukharkin, A. Kalaboukhov,  
<sup>349</sup> M. Xie, D. Winkler, J. F. Schneiderman, A 7-channel high-Tc SQUID-based  
<sup>350</sup> on-scalp MEG system, bioRxiv (2019) 534107.

351 [9] M. Xie, J. F. Schneiderman, M. L. Chukharkin, A. Kalabukhov, B. Riaz,  
352 D. Lundqvist, S. Whitmarsh, M. Hämäläinen, V. Jousmäki, R. Oostenveld,  
353 et al., Benchmarking for on-scalp MEG sensors, *IEEE Transactions on*  
354 *Biomedical Engineering* 64 (6) (2017) 1270–1276.

355 [10] L. M. Andersen, R. Oostenveld, C. Pfeiffer, S. Ruffieux, V. Jousmäki,  
356 M. Hämäläinen, J. F. Schneiderman, D. Lundqvist, Similarities and dif-  
357 ferences between on-scalp and conventional in-helmet magnetoencephalog-  
358 raphy recordings, *PLOS ONE* 12 (7) (2017) e0178602.

359 [11] R. Oostenveld, P. Fries, E. Maris, J.-M. Schoffelen, Fieldtrip: Open source  
360 software for advanced analysis of MEG, EEG, and invasive electrophys-  
361 iological data, *Computational Intelligence and Neuroscience* 2011 (2011)  
362 1–9.

363 [12] R. Leahy, J. Mosher, M. Spencer, M. Huang, J. Lewine, A study of dipole  
364 localization accuracy for MEG and EEG using a human skull phantom,  
365 *Electroencephalography and clinical neurophysiology* 107 (2) (1998) 159–  
366 173.

367 [13] T. Bardouille, L. Power, M. Lalancette, R. Bishop, S. Beyea, M. J. Tay-  
368 lor, B. T. Dunkley, Variability and bias between magnetoencephalography  
369 systems in non-invasive localization of the primary somatosensory cortex,  
370 *Clinical neurology and neurosurgery* 171 (2018) 63–69.

371 [14] R. Zetter, J. Iivanainen, M. Stenroos, L. Parkkonen, Requirements for  
372 coregistration accuracy in on-scalp MEG, *Brain topography* 31 (6) (2018)  
373 931–948.

374 [15] O. Alem, R. Mhaskar, R. Jiménez-Martínez, D. Sheng, J. LeBlanc,  
375 L. Trahms, T. Sander, J. Kitching, S. Knappe, Magnetic field imaging with  
376 microfabricated optically-pumped magnetometers, *Optics Express* 25 (7)  
377 (2017) 7849–7858.

378 [16] J. Iivanainen, R. Zetter, M. Grön, K. Hakkarainen, L. Parkkonen, On-  
379 scalp MEG system utilizing an actively shielded array of optically-pumped  
380 magnetometers, *NeuroImage* 194 (2019) 244 – 258.

381 [17] E. Boto, N. Holmes, J. Leggett, G. Roberts, V. Shah, S. S. Meyer, L. D.  
382 Muñoz, K. J. Mullinger, T. M. Tierney, S. Bestmann, et al., Moving magne-  
383 toencephalography towards real-world applications with a wearable system,  
384 *Nature* 555 (7698) (2018) 657.

385 [18] A. Borna, T. R. Carter, J. D. Goldberg, A. P. Colombo, Y.-Y. Jau, C. Berry,  
386 J. McKay, J. Stephen, M. Weisend, P. D. Schwindt, A 20-channel mag-  
387 netoencephalography system based on optically pumped magnetometers,  
388 *Physics in Medicine & Biology* 62 (23) (2017) 8909.