

1 Distinct sensorimotor feedback 2 loops for dynamic and static control 3 of primate precision grip

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8
9 **Abstract** Volitional limb motor control involves dynamic and static muscle actions. It remains
10 elusive how such distinct actions are controlled in the central nervous system through separated or
11 shared neural circuits. Here we explored the potential separation of neural circuitry for dynamic
12 and static controls in the primate hand actions. We investigated the neuronal interactions between
13 the spinal cord and forelimb muscles, and the motor cortex and the muscles, with an emphasis on
14 their modulation during dynamic and static phase of grasping. While macaque monkeys were
15 performing a precision grip comprising dynamic and static phases, we recorded spinal or cortical
16 local field potentials simultaneously with electromyographic activity, thereafter examined neural
17 coherence between the signals. We observed the emergence of beta-range neural coherence with
18 muscle activity at spinal cord and motor cortex in the separated phases; spinal coherence during
19 the grip phase and cortical coherence during the hold phase. Further, both of the coherence were
20 influenced by bidirectional interactions with reasonable latencies as beta oscillatory cycles. These
21 results indicate that dedicated feedback circuits comprising spinal and cortical structures underlie
22 dynamic and static control of dexterous hand actions.

23 **Introduction**

24 Our motor behaviors comprise a continuum of “moving” a limb and “holding” it still, through dynamic
25 and static control of muscle activity. The control of such distinctive modes appears contrasting.
26 During a dynamic movement, the trajectory and speed are often required to be controlled, whereas
27 holding-still requires the stability of the muscle force. To meet such distinct requirements, it may be
28 beneficial for the neural system to accommodate separate circuits for each control. Indeed, the
29 mammalian central nervous system (CNS) houses such dedicated circuits in the brainstem for the
30 dynamic and static control of saccadic eye movement (*Robinson, 1973*). This separation has been
31 proposed as a potentially common design principle among motor end-effectors (*Shadmehr, 2017*).

32 However, for the skeletomotor control, it is largely unknown whether such distinct circuits are
33 at work, except that some literature support the concept. A subgroup of neurons situated in the
34 rostral part of the motor cortex predominantly exhibited phasic discharges during the dynamic
35 phase (*Crammond and Kalaska, 1996; Shalit et al., 2012*). In contrast, a greater population of tonic
36 discharges during the static phase was reported in the caudal part of the motor cortex (*Crammond*
37 *and Kalaska, 1996; Shalit et al., 2012*), and the premotoneuronal cells with direct connections to
38 the spinal motoneurons, such as corticomotoneuronal (CM) cells (*Maier et al., 1993*) and premotor
39 spinal interneurons (*Takei and Seki, 2013a*). While these studies suggest cortical and spinal neurons

41 are involved in dynamic and static control, a deficiency in these results is the unresolved effective
42 connectivity of the population neuronal activity to the muscular outputs; albeit the individual
43 premotoneuronal cells could affect the target motoneuron activities, their spatial or temporal
44 properties are often incongruent with the target muscles (*Takei and Seki, 2013b; Griffin et al.,*
45 *2015*).

46 Therefore, it is crucial to directly examine an effective connectivity of the population neural
47 activity with muscular outputs, such as coherence analyses between local field potentials (LFPs)
48 of neural structures and electromyography (EMG) (*Baker, 2007; Pesaran et al., 2018*). Although a
49 coherent oscillation has been demonstrated between an LFP of the motor cortex and EMG at a beta
50 frequency range (15–30 Hz) during a sustained control of muscle action (*Conway et al., 1995; Baker*
51 *et al., 1997; Salenius et al., 1997; Kilner et al., 1999; Gross et al., 2000; Divekar and John, 2013*), it is
52 uncertain for the separation of neural circuitry underlying dynamic and static skeletomotor control,
53 since 1) comparable beta-range coherent oscillations with muscles have not been found during
54 the dynamic phase, and 2) it remains unresolved how such coherent oscillations are generated,
55 namely, whether they arise from an efferent entrainment of oscillatory cortical drive transferred
56 to the muscles (*Gerloff et al., 2006*), or from a reciprocal interaction of motor commands and
57 sensory feedbacks between the motor cortex and the muscles (*Baker, 2007; Aumann and Prut,*
58 *2015*). To address these issues, we sought a potential coherent oscillation with muscles in the spinal
59 cord as well as in the motor cortex, since spinal interneurons receive convergent inputs from the
60 descending pathways including the corticospinal and other tracts (*Riddle and Baker, 2010*), and
61 spinal premotor interneurons are clearly discharged in relation to the dynamic and static muscle
62 activity (*Takei and Seki, 2013a*). Also, we sought to disambiguate the two possible mechanisms for
63 emergence of neural coherence in a more decisive way by delineating information flows and the
64 time lag estimates between coherent signals.

65 We analyzed neural coherence and information flows between LFPs from the spinal cord and the
66 motor cortex, and EMG activity of the forearm, while the macaque monkey performed a precision
67 grip task that involved both dynamic grip and static hold controls. We found the emergence
68 of significant spinomuscular and corticomuscular coherence as distinct time-frequency patterns
69 relevant to the dynamic and static grip phases. Furthermore, directional information analyses
70 indicate that spinal and cortical beta-range coherence are composed of a reciprocal interaction
71 with the muscles, with corresponding time lags for beta oscillations. We also show that these
72 two feedback loops differ in the muscles involved (i.e., spinal local feedback vs. cortical divergent
73 feedback loops). These results indicate that distinct sensorimotor feedback loops are engaged in
74 the dynamic and static control of precision grip of primates.

75 **Results**

76 **Experiment, behavior, and analyses**

77 We recorded LFP signals from four macaque monkeys using single microelectrodes in conjunction
78 with EMG activity from the forelimb muscles (Figure 1A, C; see Table S1 for muscle lists for each
79 monkey) while each monkey was performing a precision grip task involving dynamic grip (grip) and
80 static hold (hold) periods. The monkeys were instructed to acquire visual targets that represented
81 lever positions, by pinching a pairs of spring-loaded levers with the thumb and index finger (Figure
82 1B). Spinal LFP signals were recorded from four monkeys, and the analyzed signals included 4 LFPs
83 and 2 EMGs from monkey U, 7 LFPs and 19 EMGs from monkey A, 72 LFPs and 20 EMGs from
84 monkey E, and 1 LFP and 21 EMGs from monkey S; cortical LFP signals were obtained from two
85 monkeys: 71 LFPs and 20 EMGs from monkey E, and 26 LFPs and 21 EMGs from monkey S. LFP-EMG
86 pairs with electrical cross talk were excluded from the analysis (see Materials and Method). The
87 summaries for analyzed LFP-EMG pairs are summarized in Table S2.

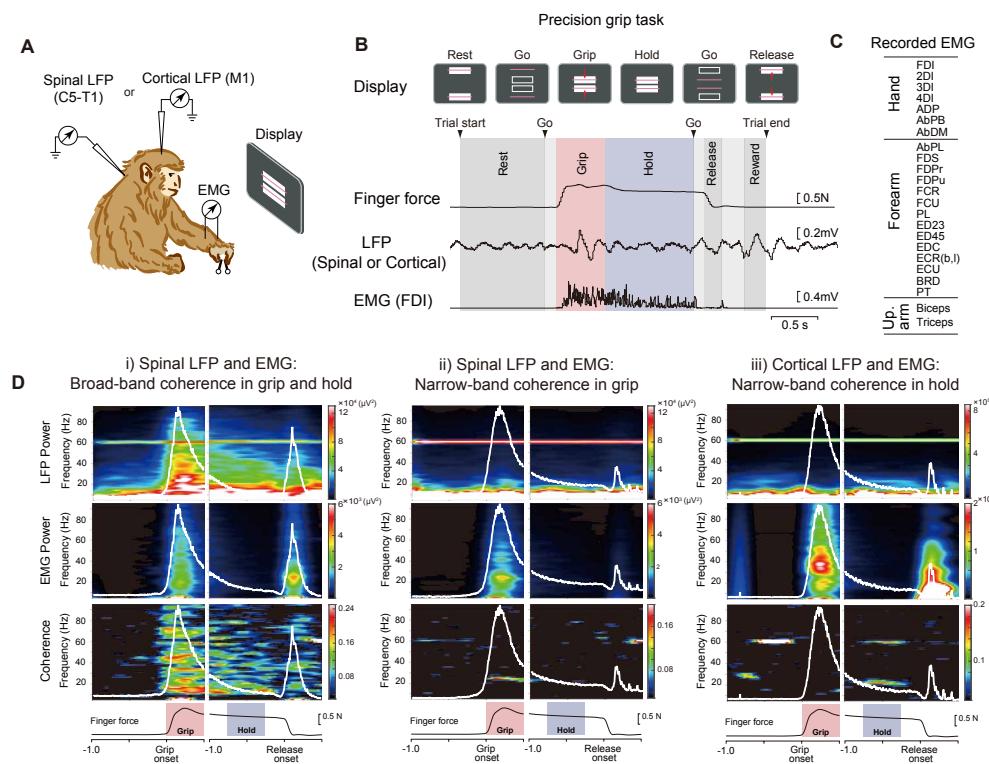


Figure 1. A. Task and recording setup. Monkeys performed a precision grip task by squeezing a pair of spring-loaded pivoted levers; they were instructed to align the bars (corresponding to lever displacements) to prescribed rectangle areas in the front display. During the task either spinal or cortical local field potentials (LFPs) were recorded in conjunction with electromyography (EMG) of forelimb muscles. **B.** Task epochs delineated by events, and exemplar raw traces of finger force (sum of two lever forces), LFP, and EMG. On the visual and auditory cue, the monkey squeezes the levers (grip phase: red-shaded area) maintains the force for 1-2 s (hold phase: blue-shaded area). **C.** A list of forelimb muscles recorded in the present study (for each animal, see Table S1). **D.** Representative patterns of coherence (bottom) and the underlying power spectra (top) of spinal broad-band (i), spinal narrow-band (ii) or cortical narrow-band (iii) LFPs and the corresponding EMGs (middle: AbPB for i), AbPL for ii), and AbDM for iii)). White traces indicate these EMG patterns.

88 Distinct types of time-frequency coherence patterns: spinal broad-band, spinal 89 beta-band, and cortical beta-band coherence

90 To examine the overall time-frequency patterns in coherence, we applied wavelet transformation on
91 LFP and EMG signals with respect to grip onset or release onset (from 1 s before and 0.5 s after the
92 onsets), both of which were then processed for spectral analysis (Figure 1D). We found three major
93 types of coherence patterns in the spinomuscular or corticomuscular coherence. Spinomuscular
94 coherence exhibited two types: one was termed spinal broad-band coherence, which exhibited
95 paralleled temporal evolution with that of the paired EMG pattern, namely phasic-tonic activity
96 during grip—hold phases (Figure 1D-i); the other was termed spinal narrow-band coherence
97 in the beta range, which markedly emerged during the grip phase (Figure 1D-ii). In contrast,
98 corticomuscular coherence appeared as a narrow band in the beta-range, being pronounced
99 specifically during the hold phase (Figure 1D-iii).

100 To objectively classify these time-frequency patterns, we measured the following two features of
101 coherence: 1) the integral of the contours in the wavelet coherence (Figure S1A-i), 2) the frequency
102 width of coherence in a fixed-time period as a supplement (Figure S1A-ii, see Materials and Methods
103 for the detail). The integral of the contours in the wavelet coherence during the grip (0-1 s from the
104 grip onset) or hold phase (-1-0 from the release onset) was calculated as the sum of significant areas
105 at each contour level. With this measurement, we found a bimodal distribution for spinomuscular

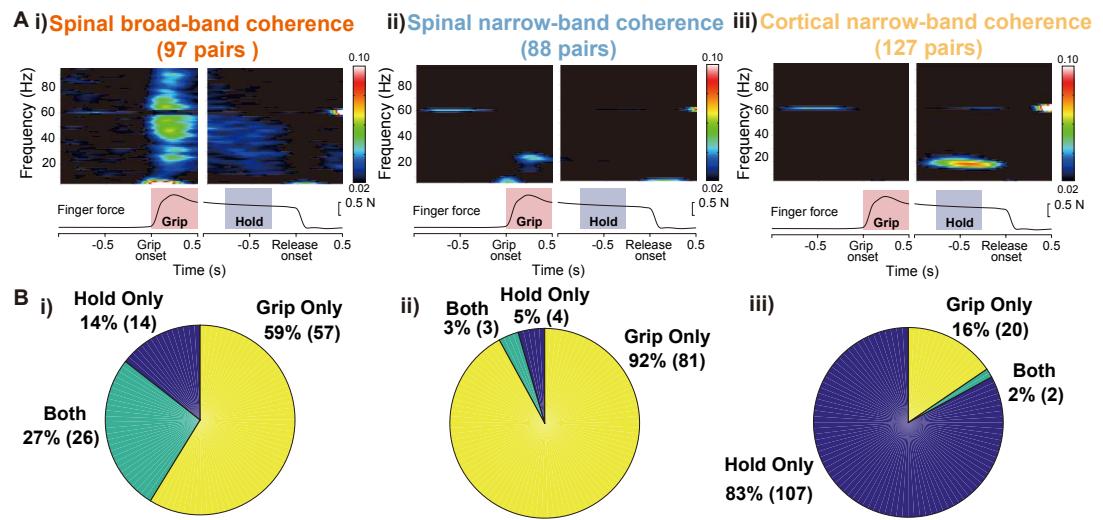


Figure 2. Group averages and proportions in significant pairs in grip vs. hold phases of each coherence pattern. **A.** Averaged wavelet coherence patterns classified according to the distributions shown in Fig S1B. **B.** The proportions of significant pairs in grip, hold, and both phases for each classified coherence pattern. i) Spinal broad-band pattern (BB) spans wide frequency and time ranges over the grip and hold phases (83 out of 97 pairs for grip, 40 out of 97 pairs for hold). ii) Spinal narrow-band (NB) pattern emerges in the beta band during the grip phase (84 out of 88 pairs). iii) Cortical narrow-band (NB) pattern is pronounced in the beta range during the hold phase (107 out of 127 pairs).

106 coherence (Figure S1B-i), which was successfully separated using a Gaussian mixture model (GMM).
 107 The two separated distributions were assigned to the narrow-band type (blue, Figure S1B-i), and
 108 the broad-band type (red, Figure S1B-i), respectively. This dissociation was largely consistent with
 109 the distributions in frequency width (Figure S1B-i, vertical histogram) as was used in a previous
 110 study (*Takei and Seki, 2008*). For corticomuscular coherence we saw solely unimodal distributions
 111 in both frequency width and contour integrals (Figure S1B-ii), which led us to define all of them as
 112 narrow-band.

113 Classified spinomuscular broad-band coherence (97 pairs in total) manifested itself not only in
 114 the grip phase but also in the hold phase (Figure 2A-i), with c.a. 90% of pairs and c.a. 40% of pairs
 115 showing significant coherence during the grip and hold phases, respectively (Figure 2B-i). Spinal
 116 narrow-band coherence (88 pairs in total) emerged in the beta band, predominantly during the
 117 grip phase (Figure 2A-ii) with more than 90% pairs showing significance exclusively during the grip
 118 phase (Figure 2B-ii). This was in a clear contrast with cortical narrow-band coherence (127 pairs in
 119 total), which was evident almost exclusively during the hold phase (Figure 2A-iii), with more than
 120 80% pairs being significant only during the hold phase (Figure 2B-iii).

121 To further explore the functional differences among the coherence types, we examined which
 122 individual muscles were coherent with the spinal or cortical LFPs (Figure 3). Overall, the coherent
 123 LFP—muscle pairs were observed predominantly in intrinsic hand, extrinsic hand, and wrist flexor
 124 muscles. Spinal broad-band patterns (red-shaded area in Figure 3A) were most widely distributed
 125 among those observed muscles, showing reflection of all recruited muscles. Spinal narrow-band
 126 coherence (blue shaded areas in Figure 3A and B) showed a preference in the index finger muscles,
 127 i.e., FDI and FDPr. This specific preference was contrasted with a relatively wider distribution of the
 128 cortical narrow-band coherence observed in the finger muscles (yellow shaded area in Figure 3B).

129 While a substantial proportion of significant pairs in both types of spinal coherence patterns
 130 were found in the grip phase, a significant difference in latency was observed with respect to grip
 131 onset (Figure S2). Spinal broad-band coherence was distributed with the median value of 95 ms
 132 prior to grip onset, whereas spinal beta-band was distributed with the median value of 7 ms prior to
 133 grip onset (*t*-test with unequal variance, $p < 0.001$). The latency of the spinal broad-band coherence

134 indicates that the onset occurred prior to grip onset, as well as spinal beta-band coherence onset
135 by c.a. 100 ms.

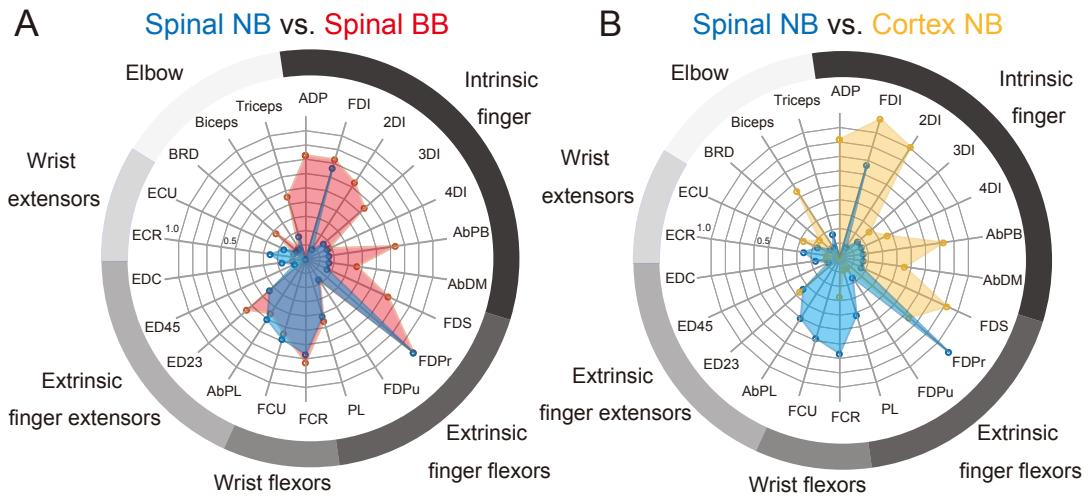


Figure 3. Muscle distributions of LFP-EMG coherent pairs for spinal NB (blue), spinal BB (red) and cortical NB (yellow) groups. Muscles are ordered clockwise from intrinsic finger muscles, extrinsic finger flexors, wrist flexors, extrinsic finger extensors, wrist extensors, to elbow muscles. **A.** Comparison of the distributions between spinal NB (blue) and spinal BB (red) coherent pairs. The muscles are generally overlapped except the spinal NB pairs, which are predominantly partial to FDI and FDPr, both acting in index finger flexion. This is in contrast to a broader distribution of spinal BB pairs, reflecting recruitment of intrinsic finger, extrinsic finger, and wrist flexor muscles in the precision grip. **B.** Comparison of the distributions between spinal NB (blue) and cortical NB (yellow) coherent pairs. A preference of spinal NB to the index finger muscles (FDI and FDPr) is clearly contrasted with cortical NB, which shows rather even distribution to the finger muscles recruited.

136 **Differences in frequency, phase and inter-muscle connections between spinal and**
137 **cortical coherence in the beta range**

138 We then sought to determine whether there exists a difference between the spinal and cortical
139 narrow-band patterns, by comparing frequency and phase distributions between the two coherence
140 patterns (Figure 4). We observed a difference in the normalized frequency distribution between
141 them, where spinal narrow-band coherence showed a slightly higher frequency content than that
142 for cortical narrow-band (Figure 4A). We also found each phase distribution clustered to a specific
143 angle (Rayleigh test, $p < 0.001$ for each) where the spinal narrow-band lagged behind the muscle
144 activity (Figure 4B-i), whereas the cortical narrow-band occurred prior to the muscle activity (Figure
145 4B-ii). These two distributions were statistically different (Mardia-Watson-Wheeler test, $p < 0.001$).
146 These results indicate that the spinal and cortical narrow-band coherence patterns may have arisen
147 from different interaction processes, albeit in close frequency bands.

148 Furthermore, we frequently observed coherence between an LFP and multiple EMGs at a given
149 recording site, which may imply an interaction between the muscles through a shared network. As
150 such, we defined the muscles that simultaneously emerged at a given site as interacting muscles
151 mediated by spinal or cortical narrow-band coherence, and counted the number of combinations
152 of those muscles for each spinomuscular and corticomuscular coherence. Consequently, a marked
153 contrast was found in the inter-muscle connections between the spinal and cortical narrow-band
154 coherence; for spinomuscular coherence (104 pairs in 21 sites) the interacting muscles were pre-
155 dominantly clustered in the forearm flexors (extrinsic hand and wrist flexors) (Figure 5A). In contrast,
156 for corticomuscular coherence (59 combinations in 28 sites) there were divergent connections
157 among the muscles, ranging from the intrinsic hand muscles to upper arm muscles (Figure 5B).

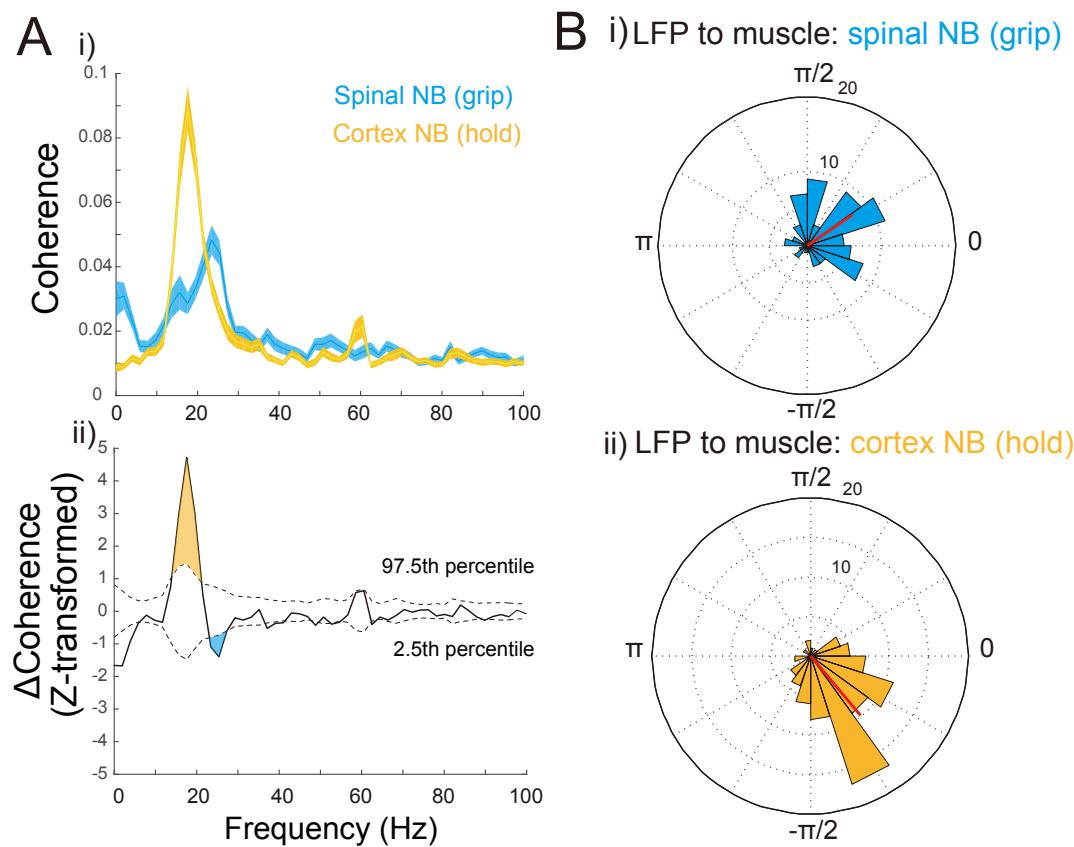


Figure 4. Comparison of frequency (A), phase (B) distributions between the spinal narrow-band coherence during the grip phase (spinal NB) and the cortical narrow-band coherence during the hold phase (cortical NB). **A.** i) Frequency distributions for the mean for spinal NB (blue, $n = 88$) and cortical NB (orange, $n = 127$). The peak frequency for the spinal NB is 23.4 Hz and that for the cortical NB is 17.5 Hz (Shaded areas are $\pm SEM$). ii) Differences between the mean coherence values (Z-transformed). Dashed lines denotes 97.5th and 2.5th confidence intervals obtained from the Monte-Carlo method (10000 iterations). The orange-shaded area represents the frequency band where cortical NB is greater than spinal NB, and blue-shaded area indicates the band where spinal NB is greater than cortical NB. **B. i), ii)** Phase distributions for the spinal NB and cortical NB show clustered angles (0.59 ± 1.19 , -0.87 ± 0.91 , mean $\pm SD$, as represented by red vectors, Rayleigh test, $p < 0.001$ for each), which are statistically inhomogeneous (Mardia-Watson-Wheeler test, $p < 0.001$).

158 **Direction of causality in spinomuscular and corticomuscular coherence**

159 We further examined whether the observed coherence reflects putatively causal interactions with
 160 a particular direction. To explore the direction of an influence and its phase-lag relationship
 161 between the neural structures and muscles, we used a combination of directed and partial directed
 162 coherence measures based on Granger causality and a multivariate autoregressive (MVAR) model;
 163 each measure is complementary to each other in determining a causality and estimating the lag
 164 (see Materials and Methods for details). We found that spinal broad-band coherence predominantly
 165 comprised an efferent pathway with relatively weak beta afferent components (Figure 6A-i, B-i),
 166 whereas spinal beta-band coherence in the grip phase comprised bidirectional interactions in
 167 the beta range with dominant afferent components (Figure 6A-ii). Corticomuscular coherence
 168 comprised a beta-range bidirectional interaction between the afferent and efferent pathways with
 169 dominant efferent components (Figure 6B-iii). The phase delay of spinal broad-band coherence
 170 was c.a. $8.0 (\pm 5.6, \text{quantile})$ ms for the efferent components (Figure 7A-i, B-i), consistent with the
 171 conduction delay between the spinal motoneurons and the muscles (Maier *et al.*, 1998). For spinal
 172 narrow-band coherence, the beta-band afferent and efferent delays were $26.8 (\pm 14.8)$ and 30.2
 173 (± 7.3) ms (Figure 7A-ii), respectively. For cortical beta-band coherence the delays were $27.0 (\pm 8.7)$

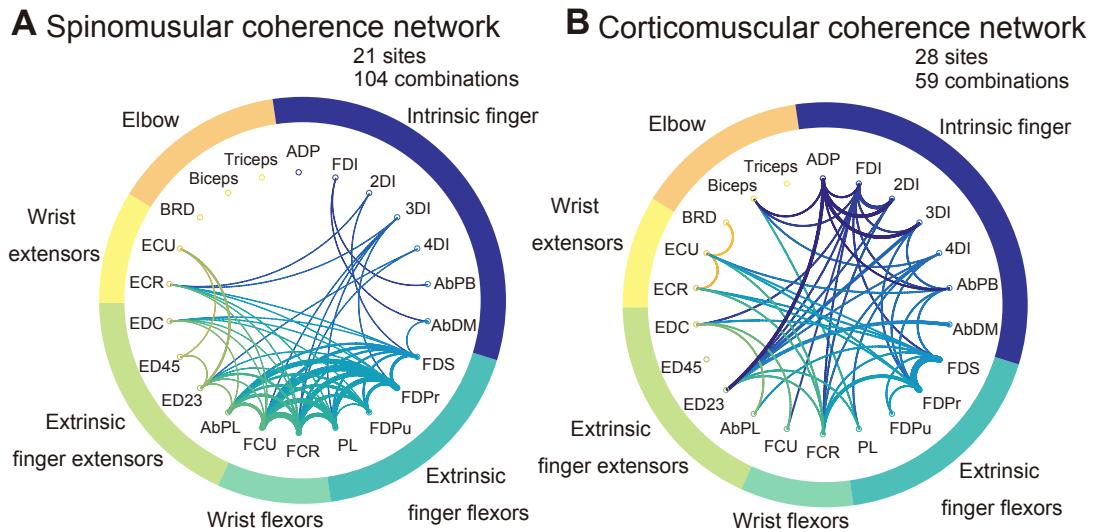


Figure 5. Comparison of putative inter-muscle connections through spinal (A) and cortical (B) narrow-band coherence. The thickness of the line represents the number of connections observed between the muscles; the thinnest line denotes the minimum connection of a value of 1 (e.g., FDI and AbPB in A), whereas the thickest line indicates the maximum connection as a value of 7 (e.g., FDPr and FCU in A). i) The connections mediated by spinomuscular NB coherence are predominantly found among synergistic muscles, i.e., extrinsic finger flexors and wrist flexors. ii) The connections mediated by the corticomuscular NB coherence are observed in diverse combinations of muscles across the forelimb, ranging from the intrinsic hand to the upper arm muscles.

174 and 25.7 (± 14.1) ms (Figure 7, B-iii). It is notable that the aggregate median for the entire delay
175 for spinomuscular and corticomuscular coherence (i.e. sums of afferent and efferent delays) was
176 c.a. to 50–60 ms, a reciprocal of the central frequency of the coherence (c.a. 15–20 Hz). These
177 results corroborate the hypothesis that the beta-band corticomuscular coherence is the result of
178 bidirectional interactions between the cortex and the periphery, which is, further applicable to
179 spinomuscular coherence.

180 Discussion

181 It has been unclear whether distinct circuits are engaged in dynamic vs. static control of limb
182 muscle actions. We found that the beta-range neural coherence with muscles emerged in the spinal
183 cord and motor cortex, each of which was distinctively evident during dynamic or static phases
184 of precision grip. Furthermore, neural information flows were bidirectional in both of beta-range
185 spinomuscular and corticomuscular coherence with reasonable latencies for beta oscillatory cycles,
186 indicating dedicated feedback loops underlie each coherent pattern. The muscle groups involved in
187 each coherence are also distinct; the trans-spinal loop involves the prime movers of the precision
188 grip muscles with interactions among local forearm flexors, whereas the trans-cortical feedback
189 loop arise largely through the recruited finger muscles, with divergent interactions across the
190 forelimb joints.

191 Spinal broad-band coherence reflects population motoneuron pool activity

192 In our previous study, we reported broad-band coherence between the spinal LFP and a forelimb
193 muscle. Further, in light of the wide frequency-range correlation (i.e., paired LFP-EMG signals are
194 correlated in any frequency contents), the depth of electrode from the dorsal surface, and a time
195 domain analysis on lag estimation, the coherent pattern was putatively attributed to motoneuron
196 pool activity (*Takei and Seki, 2008*). However, potent evidence for this claim was lacking such as sim-
197 ilarities in the spatiotemporal patterns and the directionality of information transfer, concomitant
198 with more accurate lag estimation in a particular direction. Here, we found broad-band coherent pat-

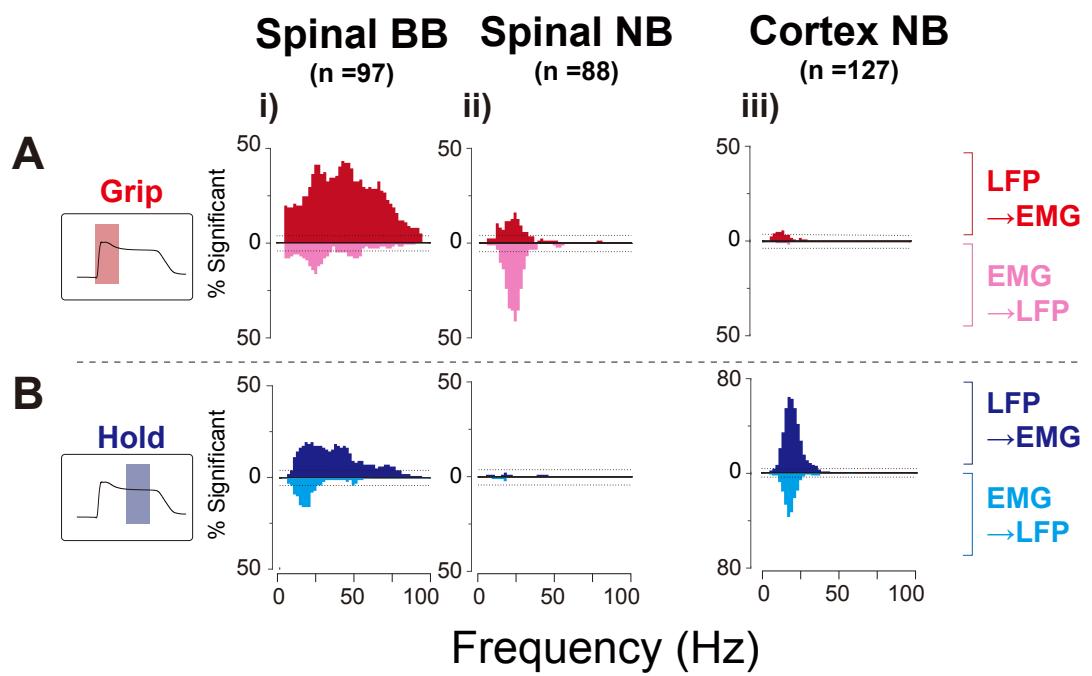


Figure 6. Pooled directed coherence distributions of significant frequency bands for efferent (LFP to EMG: red for grip, blue for hold) and afferent (EMG to LFP: magenta for grip, cyan for hold) components of directed coherence for grip (**A**) and hold (**B**) phases. Each horizontal line represents the significance level (binomial parameter estimation with $p = 0.005$). Spinal broad-band coherence predominantly consists of efferent components in both grip and hold phases, with relatively smaller effects from the afferent components in the beta band (**A**, i) and (**B**, ii)). Spinal NB in the grip phase comprises beta-range efferent and afferent components, with an afferent prevalence (**A**, ii)). Cortical NB comprises a bidirectional interaction through efferent and afferent components in the beta band, with an efferent prevalence (**B**, iii)).

199 turns closely resemble typical temporal EMG profiles (i.e., phasic-tonic activity) (Figure 1D-i, 2A-i, 2B-i,
200 *Takei and Seki (2013a)*), and spatial distribution over the recruited muscles (Figure 3B). Directional
201 information analyses based on MVAR further indicate that the broad-band transfer was exclusively
202 efferent from the spinal LFPs to the muscles (Figure 6A-i, 6B-i), with a physiologically-plausible lag
203 (c.a. 8-9 ms, Figure 7A-i, 7B-i, *Maier et al. (1998)*). Collectively, spinomuscular coherence with a
204 broad range of frequencies represents a direct transfer of a signal between the motoneuron pool
205 and the innervated muscles.

206 **Beta-range coherence in the spinal cord and motor cortex emerge in distinct phases, 207 forming separate bidirectional loops**

208 Most of the beta-band coherence in the spinal cord were observed during the grip phase (Figure 2A-ii, 2B-ii). To the best of our knowledge, this is the first report on a neural structure showing noticeable
209 beta-range coherence with the muscles during the dynamic phase of movement. We initially
210 hypothesized that the coherent pattern would reflect convergence of efferent motor desynchronized
211 discharge upstream in the descending pathway (*Baker et al., 1999, 2003*) and hence, would occur
212 prior to the onset of muscle activity. However, the spinal beta coherence pattern lagged behind the
213 motoneuron pool activity that was reflected by the broad-band coherence (Figure S2). Further, the
214 coherence did not consist of a unidirectional information transfer, but a bidirectional interaction
215 with dominant afferent components to LFPs from EMGs (Figure 6A-ii). These findings indicate that
216 the spinomuscular coherence evident in the dynamic phase reflects a feedback-mediated interaction
217 between the spinal structure and the muscles, rather than a convergent efferent command relayed
218 from the motor cortex to the muscles. The feedback is likely induced by mechanical events
219 associated with the contraction of a muscle (e.g., a stretch of skin and a length and tension change

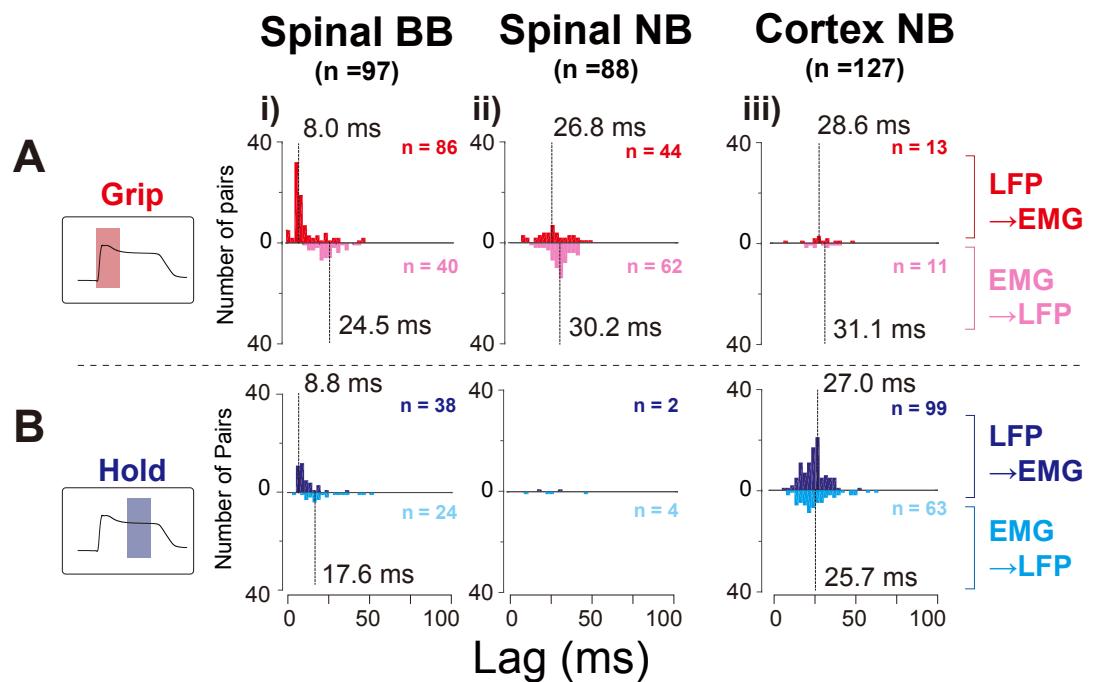


Figure 7. Distributions of phase lag of partial directed coherence for efferent and afferent components. The number of significant pairs, as determined by directed coherence analysis (Figure 6), are shown at the upper right for each distribution. Captions and arrangements of the histograms are the same as in Figure 6. The lags for efferent components for spinal BB are as short as the conduction delay from the motoneuron pool to the muscle (A-i) and B-i). The efferent and afferent lags for cortical NB are comparable to those of the spinal NB afferent components (A-iii) and B-iii) vs. A-ii) and B-ii)). The aggregate lags for the afferent and efferent components of the spinal NB and cortical NB are approximately 50 ms, which corresponds to the whole cycle duration of beta-range oscillation.

221 of the contracting muscle). In effect, the latencies of the afferent components correspond by and
 222 large to that of the peak responses of spinal interneurons to a mechanical perturbation against
 223 the wrist (Fetz *et al.*, 2002), suggesting that the afferent component of the coherence reflects
 224 a somatosensory feedback, including cutaneous and proprioceptive information. Such afferent
 225 components were also found in the spinal broad-band coherence (Figure 6A-i, 6B-i), suggesting that
 226 part of the somatosensory feedback reaches in close proximity to the motoneuron pool. Such an
 227 interaction might reflect a monosynaptic reflex arc (e.g., Ia monosynaptic reflex). Indeed, neurons
 228 in the dorsal root ganglion (DRG) defined as Ia afferent neurons exhibit a sizable magnitude of
 229 coherence through a bidirectional interaction with the innervated muscles (Baker *et al.*, 2006). In
 230 addition, the sum of the medians of the phase delays for the afferent and efferent components
 231 of spinal beta coherence quantitatively matched with the cycle duration in the beta range (Figure
 232 7A-ii).

233 Taken together, beta-band spinomuscular coherence emerging through a feedback loop proba-
 234 bly arises from cutaneous and proprioceptive receptors, which may be triggered by mechanical
 235 events associated with muscle contraction. More complete understanding would be obtained if
 236 one could find spinal premotoneuronal neurons that respond to sensory stimuli are synchronized
 237 with the beta oscillation in the dynamic phase of the grip.

238 In contrast, corticomuscular coherence in the beta band was pronounced predominantly during
 239 the hold phase (Figure 2A-iii, 2B-iii), confirming the results extensively reported in numerous
 240 previous studies (Conway *et al.*, 1995; Baker *et al.*, 1997, 1999; Salenius *et al.*, 1997; Kilner *et al.*,
 241 1999; Kristeva *et al.*, 2007). However, the question regarding how the coherence emerges remains
 242 unanswered. One hypothesis states that it reflects an efferent entrainment of oscillatory cortical
 243 drive observed at the muscle (Gerloff *et al.*, 2006), whereas another suggests that the coherence

244 arises through a reciprocal interaction of motor commands and sensory feedbacks between the
245 cortex and the muscles (*Baker, 2007; Aumann and Prut, 2015*).

246 The unresolved key analysis to addressing this question is the lag estimate; the lag estimates
247 obtained in the previous studies were widely dispersed, sometimes out of the range of the beta
248 band (i.e., less than 30 ms or more than 60 ms) (*Witham et al., 2010, 2011*). This is likely due
249 to an inherent estimation error in the directed coherence measures, as they have limited ability
250 to dissociate direct and indirect influences on the output node (*Schouten and Campfens, 2012*;
251 *Campfens et al., 2013*). Particularly in a nested closed loop, an effect of previous the cycle, which is
252 delayed in a fixed time, can induce phase shifts as a function of the frequency, thereby resulting in a
253 deviation in lag estimates. The partial directed coherence measure, which was proposed as a means
254 of distinguishing direct influences from indirect ones (*Baccalá and Sameshima, 2001*), can provide a
255 rather accurate estimate of lag in the closed loop (*Campfens et al., 2013*). Using the combination of
256 directed coherence and partial directed coherence, we obtained phase lags with tighter distributions
257 as compared with ones reported in the previous studies (Figure 7B-iii). The sum of the medians of
258 the phase delays for corticomuscular afferent and efferent pathways quantitatively matched with
259 the cycle duration in the beta range. These results indicate that corticomuscular coherence is the
260 results of a reciprocal interaction between the motor cortex and muscles in the hold phase.

261 Thus, our results indicates that both of spinomuscular and corticomusclar coherence emerge
262 through separate bidirectional sensorimotor feedback loops for each dynamic and static phase. It
263 would be intriguing if these separate loops are interacting with other. Further studies are warranted
264 to investigate such a corticospinal interaction relevant to dynamic vs. static control of the limb.

265 **Associations of spinomuscular and corticomuscular feedback loops with mechanically- 266 induced short- and long-latency corrective responses**

267 Considering the sensory feedback loops that engage motor outputs through the trans-spinal and
268 trans-cortical loops, we conceived that these loops may share routes with the short- and long-
269 latency corrective responses to a mechanical perturbation, for the research of a feedback controller
270 utilized for motor control (*Scott, 2012, 2016*). Thus, we discuss some commonalities between the
271 feedback loops and such corrective responses.

272 The short latency response is the spinal-mediated, fastest (20–50 ms) response via sensory
273 afferents that is elicited by a local cutaneous and proprioceptive interaction, concomitantly leading
274 to homonymous or synergistic muscle contractions (*Pierrot-Deseilligny and Burke, 2005*). These
275 features are congruent to those of the spinomuscular loop; its latency is comparable to the short
276 latency response (Figure 7A-ii), and it conceivably emerges via cutaneous and proprioceptive
277 feedbacks (*Baker et al., 2006*). Furthermore, it is predominantly observed in FDI and FDPr (Figure
278 3A, B), both of which are prime movers of the forefinger that stretch and contract during a precision
279 grip. In addition, putative inter-muscle interactions observed through the spinomuscular coherence
280 are largely confined to local or synergistic muscles of FDPr (extrinsic hand flexors and wrist flexors
281 (Figure 5A).

282 The long-latency response is routed via the trans-cortical pathway with a latency of 50–100
283 ms (*Cheney and Fetz, 1984; Pruszynski et al., 2011*). This response is modifiable in a task-relevant
284 manner; the response is evoked to a stretch of task-defined, broader range of muscles and adjacent
285 mechanoreceptors via a musculoskeletal interaction, and directed flexibly to the task-related
286 muscles, even beyond the joints, to achieve functionally-oriented compensation (*Kurtzer et al.,
287 2009; Cole et al., 1984; Pruszynski and Scott, 2012*). Likewise, corticomuscular coherence was
288 observed in a broad range of finger muscles, including intrinsic and extrinsic hand flexor muscles
289 (Figure 3B), with putative connections among the muscles being divergent, as reflected by muscle
290 combinations simultaneously observed through corticomuscular coherence (Figure 5B). These
291 hand muscles are mechanically linked through various joints and tendons, and thus their complex
292 mechanical interactions may elicit cutaneous and proprioceptive feedbacks across the muscles,
293 which are concomitantly routed back to various muscles. To stabilize the grip hold, it would be

294 necessary to respond to normal and tangential force errors by supporting the digits from various
295 directions by co-contracting various muscles across the joints. Indeed, it has been demonstrated
296 that the CM system, in which many cells show sustained activities during the hold period, plays a
297 role in joint fixation by recruiting the cells with various (e.g., synergistic, fixator, and antagonistic)
298 target muscles (*Griffin et al., 2015; Lemon, 2019*).

299 Taken together, despite the lack of direct comparative evidence, it is worth noting the com-
300 mon characteristics between the separate trans-spinal and trans-cortical feedback loops, and
301 sophisticated corrective responses to mechanical perturbation with respect to mediated pathways,
302 latencies, and involved muscles. Further studies are required to directly explore these identities.

303 **304 Comparison of neural circuitry implementation for dynamic vs. static control be-
305 between saccadic and prehensile movements**

306 The separation of engaged feedback loops in the dynamic and static phases indicates phase-specific,
307 dedicated circuits at work in the dexterous hand control. This finding is a clearer indication of the
308 implementation of dedicated circuits for dynamic and static control in the skeletomotor system, as
309 compared with the moderate gradation in proportions of neuronal discharge properties between
310 the dynamic and static phases (*Crammond and Kalaska, 1996; Maier et al., 1993; Griffin et al.,
311 2015; Shalit et al., 2012; Takei and Seki, 2013a*). Conceptually, the separation of the circuitry for
312 each phase appears common to the neural circuit implementation for saccadic eye movements
313 accommodated in the brainstem (*Robinson, 1973; Jürgens et al., 1981; Shadmehr, 2017*).

314 However, there is a clear difference between the oculomotor and skeletomotor circuitry; the
315 oculomotor circuitry rests its function on internal circuits for generating sustained activity (neural
316 integrator), and monitoring displacement (displacement integrator) (*Robinson, 1973; Jürgens et al.,
317 1981; Shadmehr, 2017*). Distinctively, in the skeletomotor system, feedbacks arising from sensory
318 afferents seem to be used more for both dynamic and static control. In the dynamic phase,
319 the trans-spinal feedback loop may contribute to accumulating motor commands in a recursive
320 manner such that it works as if a “neural integrator”, whereas in the static phase, displacement
321 monitoring and motor adjustment may be achieved through sensory afferent feedback loops via
322 the supraspinal structure. These features never exclude putative contributions from an internally
323 generated, feedforward command that may have eluded coherence analyses.

324 Nevertheless, at least in part, these different degrees of dependence on afferent information
325 may be explained by their physical properties and interacting environments. As compared with
326 the oculomotor system, the skeletomotor control system (developed later phylogenically) needs to
327 control heavier, redundant multi-articulated effectors with a larger inertia under larger gravitational
328 influences. In these conditions, the system is more susceptible to disturbance and motor noises
329 (*Harris and Wolpert, 1998; Faisal et al., 2008*). With such inherent variability of outputs arising from
330 the effector, it would be difficult to precisely anticipate how much activity would be required to
331 displace and sustain the limb in place. To adapt for this demand, the neural system for skeletomotor
332 control may have shifted its dependence onto feedback control by utilizing afferent information
333 (*Todorov, 2004*).

333 **Conclusions**

334 The findings of this study highlight that two separate feedback controllers, as reflected by trans-
335 spinal and trans-cortical feedback loops via phase-specific coherence patterns, may also be utilized
336 for goal directed, voluntary dynamic and static control of grip. This insight potentially provides a
337 broader framework for understanding in voluntary dynamic and static control of our body from a
338 feedback control perspective. In addition, the insight is particularly helpful to consider functional
339 roles of neural coherence, as it is still debated in recent studies what corticomuscular coherence
340 specifically represents; a motor command for holding the displacement (*Baker et al., 1999*), active
341 sensing such as the rodent whisker system (*Baker, 2007; MacKay, 1997*), recalibration signals (*Baker,*

342 **2007)** or neural gain mechanisms that facilitate sensorimotor interactions (*Schoffelen et al., 2005;*
343 *Womelsdorf et al., 2007*). Our results lend supports to functions arising from a neural-muscle-
344 neural loops, probably related to a feedback controller, providing a direction for designing a more
345 desirable task framework to elucidate the functional roles of the sensorimotor loop for dynamic
346 and static motor control.

347 **Methods and Materials**

348 **Dataset**

349 The datasets used in the present study were obtained from four male macaque monkeys consisting
350 of three *Macaca fuscata* (monkey U: 8.5 kg, monkey A: 6.8 kg, monkey S: 9.0 kg) and one *Macaca*
351 *mulatta* (monkey E: 5.6 kg). Spinal cord datasets were obtained from monkeys U, A, and E; cortical
352 datasets were obtained from monkeys E and S, respectively. All experimental procedures described
353 below were approved by the Animal Research Committee at the National Institute for Physiological
354 Sciences, and National Center of Neurology and Psychiatry, Japan.

355 **Behavioral task**

356 Each monkey was trained to squeeze a pair of spring-loaded levers with its left index finger and
357 thumb (precision grip task; Figure 1A, B) (*Takei and Seki, 2008, 2013a*). The monkey was instructed
358 to track defined targets in a step-tracking manner by squeezing the spring-loaded levers, the
359 positions of which were displayed on a computer screen as cursors. Each trial comprised a rest
360 period (1.0–2.0 s), lever grip, lever hold (1.0–2.0 s), and lever release (Figure 1B). On successful
361 completion of the trial, the monkey was rewarded with a drop of apple puree. The force required
362 to reach the target positions was adjusted independently for the index finger and thumb of each
363 individual monkey.

364 **Surgical procedures**

365 After the monkeys had learned the required task for a sufficient time period, we performed surgeries
366 to implant head restraints, EMG wires, and recording chambers under isoflurane or sevoflurane
367 anesthesia and aseptic conditions. For EMG recordings from forelimb muscles, we performed a
368 series of surgeries to subcutaneously implant pairs of stainless steel wires (AS 631, Cooner Wire,
369 CA, USA) acutely or chronically. Specific muscle sets (ranging from intrinsic hand to elbow muscles)
370 for each animal are listed in Table S1. For spinal recordings, we implanted a recording chamber on
371 the cervical vertebra (C4–C7) of monkeys U, A, E and S where a unilateral laminectomy was made
372 on the ipsilateral side of the employed hand and arm. After completion of the spinal recordings, we
373 performed a surgery on monkeys E and S to implant a recording chamber (a circular cylinder with a
374 50-mm diameter) over the skull where a craniotomy was made covering a cortical area, including
375 the hand representation of pre- and post central gyri on the contralateral side of the employed
376 hand and arm.

377 **Neurophysiological recordings**

378 While the monkey performed the precision grip task, we recorded the local field potentials (LFPs)
379 from the spinal C5–T1 segments, or from the hand area of the motor cortex through the chamber
380 attached either on the spinal vertebrae or on the cranium by inserting a tungsten or Elgiloy alloy
381 microelectrode (impedance: 1 – 2 MΩ at 1 kHz) with a hydraulic microdrive (MO-951, Narishige
382 Scientific Instrument, Japan). The recording sites were explored with aid of positions of vertebral
383 segments for the spinal recordings, and the geometric information adjacent to the central sulcus
384 and electrical microstimulation for the cortical recordings. The LFP signals were referenced to a
385 silver ball electrode placed on a surface of dura mater of spinal cord or cerebral cortex, thereafter
386 amplified (1000 times), band-pass filtered between 0.1 Hz and 10 kHz using a differential amplifier
387 (Model 180, A-M Systems, WA, USA), and digitized at 20 kHz. The EMGs were amplified (3000–25000

388 times) and filtered (between 5 Hz and 3 kHz) using a multichannel differential amplifier (SS-6110,
389 Nihon Kohden, Japan) and digitized at 5 kHz. Signals from the potentiometers and strain gauges
390 attached to levers, and from the capacitive touch sensors were digitized at 1 kHz.

391 **Data analysis**

392 All subsequent analyses were carried out off-line using custom-written scripts in a MATLAB envi-
393 ronment (Mathworks, Natick, MA, USA). Only LFP-EMG pairs that had > 99 trials of the data were
394 averaged for analysis, and LFPs from the intraspinal or intracortical sites < 150 μ m apart were
395 pooled to avoid redundancies resulting from propagation of the potential.

396 Grip onset was defined as the time at which the rate of change in the aggregate grip force (sum
397 of forces exerted by the index finger and thumb) exceeded 2 N/s. Release onset was, likewise,
398 determined as the time at which the rate of change in the grip force reduced below -2 N/s.

399 LFPs were band-pass filtered (4th-order Butterworth filter between 3 and 100Hz) and down-
400 sampled to a 250 Hz sampling rate. EMGs were high-pass filtered at 30 Hz (4th-order Butterworth
401 filter), rectified, and down-sampled to 250 Hz.

402 **Electrical cross talk among EMGs**

403 To exclude spurious coherence arising from electrical cross-talk among EMGs, we quantified the
404 degree of electrical cross talk among EMGs recorded simultaneously using a method developed
405 by *Kilner et al. (2002)*. Original EMGs were down-sampled to 1 kHz and differentiated three times
406 without being rectified. The preprocessed signals were then subjected to cross correlation analysis
407 given as:

$$r(\tau) = \frac{\frac{1}{t_{max}} \sum_{i=0}^{t_{max}} f_1(t)f_2(t-\tau) - \bar{f}_1\bar{f}_2}{\sigma_1\sigma_2} \quad (1)$$

408 where f_1 and f_2 are two differentiated EMG signals, \bar{f}_1 and \bar{f}_2 are their mean values, and σ_1 and σ_2
409 are their standard deviations. r was calculated with 25-ms lags and a maximum modulus of r , $|r|_{max}$,
410 was used as an index of the extent of cross-talk. In each experimental day, $|r|_{max}$ was calculated
411 between EMG signals of every simultaneously recorded muscle pair for a 1-min epoch. We set a
412 significant cross talk threshold to 0.25 for each muscle pair, and in cases where it exceeded the
413 threshold, we randomly excluded either one of the pair from the data pool. Also, to eliminate any
414 influence from the power line, we excluded the frequency band between ± 5 Hz with regard to 50
415 (monkeys U, A, and E) or 60 (monkey S) Hz, and concatenated the neighboring frequencies.

416 **Time Frequency Representation: Wavelet coherence**

417 To analyse the time series containing nonstationary power at different frequencies, we employed a
418 coherence analysis between wavelet-transformed signals. LFP and EMG signals spanning either
419 an onset of grip or an onset of hold release (from 1 s before and 0.5 s after each onset) were
420 transformed using complex gabor wavelets ($\sigma = 128$ ms) (Figure 1D, top traces for LFPs and middle
421 traces for EMGs). We thereafter calculated the coherence between the transformed LFPs and EMGs
422 (Figure 1D, bottom traces), as per the equation below:

$$Coh(t, f) = \frac{|\frac{1}{N} \sum_{j=1}^N X_j(t, f)Y_j(t, f)|^2}{P_X(t, f)P_Y(t, f)} \quad (2)$$

423 where X and Y are time frequency representations and P_X , P_Y are power spectra of LFP and EMG
424 signals calculated using the wavelet transformation.

425 **Coherence in a fixed time window: standard coherence**

426 To compare the coherence measures in the grip and hold phases, we took time windows from 0 to
427 512 ms after grip onset for the grip phase and from 768 to 256 ms prior to the release onset for
428 the hold phase for analysis. Thereafter, 128-point time series were divided into non-overlapping

429 segments for Fast Fourier Transform (FFT). This allowed investigation of spectral measurements with
430 a frequency resolution of 1.95 Hz. We then calculated one-sided power spectra for the 128-point
431 time series of LFP and EMG signals. Denoting the Fourier transform of the i th section of LFPs and
432 EMGs as $F_{1,i}(f)$ and $F_{2,i}(f)$, respectively, the power spectrum of each signal ($j=1,2$) was calculated
433 as:

$$P_j(f) = \frac{2}{256^2 L} \sum_{i=1}^L F_{j,i}(f) F_{j,i}^*(f) \quad (3)$$

434 where L is the number of data segments available and $*$ denotes the complex conjugate (*Witham*
435 *et al.*, 2007). Using this normalization, $P(f)$ has units of μV^2 . The calculation of coherence between
436 an LFP-EMG pair is as follows:

$$Coh(f) = \frac{|\sum_{i=1}^L F_{1,i}^*(f) F_{2,i}(f)|^2}{\sum_{i=1}^L F_{1,i}^*(f) F_{1,i}(f) \sum_{i=1}^L F_{2,i}^*(f) F_{2,i}(f)} \quad (4)$$

437 A significance threshold level S was calculated according to *Rosenberg et al.* (1989) as

$$S = 1 - \alpha^{\frac{1}{L-1}} \quad (5)$$

438 where α is the significance level. Because we were more interested in detecting coherence
439 bands, spurious point-wise significance had to be excluded. Thus, we put a more stringent level for
440 the probability, i.e., $\alpha = 0.005$, corresponding to a threshold coherence value S of 0.0409.

441 **Classification of coherence types**

442 To classify qualitatively different time-frequency patterns of LFP-EMG coherence 1D, we quantita-
443 tively characterize those patterns based on two features of coherence measures; an integral of
444 contours of wavelet coherence (Figure S1A-i) and a frequency width of standard coherence (Figure
445 S1A-ii). The integral of contour was quantified as a volume that exceeded a significant level in a
446 time window from 0 to 1 s with regard to the grip onset for grip, or a time window from -1 to 0
447 s from the onset of hold release, thereby reflecting coherence strength, how wide its significant
448 frequency band distributes, and how long the coherency extends over time. To dissociate two
449 types of spinomuscular coherence, We then applied the Expectation-Maximization (E-M) algorithm
450 to the distribution of integral of contours, under a Gaussian mixture model (GMM) assumption
451 (*Bishop*, 2006). Points assigned as narrow-band in the contour integral dimension were examined
452 for outliers in the frequency width dimension (Smirnov-Grubbs test, $p < 0.05$). Three points were
453 determined as outliers and exceeded 25 Hz in frequency width; a criterion used for classification in
454 the previous study (*Takei and Seki*, 2008). We therefore assigned those points to the broad-band
455 category.

456 **Comparison of frequency distributions between spinal narrow-band and cortical 457 narrow-band coherence**

458 For comparison of frequency distributions between the spinal narrow-band and cortical narrow-
459 band coherence patterns, the normalized (Z-transformed) differences between the two patterns
460 of coherence were tested using the nonparametric Monte Carlo method (*Maris et al.*, 2007). The
461 Z-transformation was undertaken as:

$$Z = \frac{\left(\operatorname{atanh}(|C_1(f)|) - \frac{1}{DF_1-2} \right) - \left(\operatorname{atanh}(|C_2(f)|) - \frac{1}{DF_2-2} \right)}{\sqrt{\left(\frac{1}{DF_1-2} \right) + \left(\frac{1}{DF_2-2} \right)}} \quad (6)$$

462 where $|C_1(f)|$ and $|C_2(f)|$ stand for each coherence, and DF_1 and DF_2 for the degrees of freedom (2
463 x (pairs) x (frequency bin)). Under the null hypothesis the two coherence frequency distributions
464 are equal, the underlying datasets ((88 pairs against 127 pairs) x (64 frequency bins)) for two
465 coherence patterns were randomly permuted, averaged, and calculated into the Z-scores above.

466 The procedure was iterated 10000 times to obtain an empirical distribution, from which 97.5th and
467 2.5th percentiles were assigned for upper and lower limits to determine a significance (Figure 4A-ii).

468 **Spectral analysis on the Multivariate Autoregressive (MVAR) model**

469 Given the significant coherence found between LFPs and EMGs in the grip or hold phase, we further
470 sought to examine whether the coherence reflects putatively causal interactions with a particular
471 direction. Analyses of the causal interaction in the network can involve estimating the extent to
472 which one signal influences another, and assessing whether the lags between them based on the
473 measure are (physiologically) plausible.

474 For this purpose, we performed spectral analysis on the multivariate autoregressive (MVAR)
475 model (*Kamiński and Blinowska, 1991*), that was estimated from the LFP and EMG time series in
476 the same time window as used for standard coherence; 512 ms (128 points). The segmented signals
477 were fitted to an MVAR model of two time series (ARfit package (*Schneider and Neumaier, 2001*))
478 as described by the equation below:

$$\begin{bmatrix} y_1(n) \\ y_2(n) \end{bmatrix} = \sum_{k=1}^p A_k \begin{bmatrix} y_1(n-k) \\ y_2(n-k) \end{bmatrix} + \begin{bmatrix} \epsilon_1(n) \\ \epsilon_2(n) \end{bmatrix} \quad (7)$$

479 where $y_1(n)$ and $y_2(n)$ are the two time series. The off-diagonal components of the 2-by-2 matrix
480 A_k predict the current sample (n) of y_1 and y_2 from the k th past sample of y_1 and y_2 . The model
481 order p defines the maximum lag used to quantify such interactions. When the prediction error ϵ is
482 minimized in the fitting of the coefficients of A_k , if the variance of ϵ_1 is reduced by including the y_2
483 terms in the first equation in (7), then based on Granger causality, one can state that y_2 causes y_1 ,
484 and vice versa.

485 The spectral representation of the MVAR process is derived considering the Fourier transforma-
486 tion of the equation above (7):

$$A(f) \begin{bmatrix} y_1(f) \\ y_2(f) \end{bmatrix} = \begin{bmatrix} \epsilon_1(f) \\ \epsilon_2(f) \end{bmatrix} \quad (8)$$

487 where $A(f)$ is 2-by-2 coefficient matrix calculated as:

$$A(f) = \sum_{k=1}^p A_k e^{-i2\pi f k T} \quad (9)$$

488 where i is an imaginary unit, and T is the sampling interval. The equation (8) is rewritten as:

$$\begin{bmatrix} y_1(f) \\ y_2(f) \end{bmatrix} = H(f) \begin{bmatrix} \epsilon_1(f) \\ \epsilon_2(f) \end{bmatrix} \quad (10)$$

489 where $H(f)$ is 2-by-2 *transfer function matrix* calculated with $A(f)$:

$$H(f) = [I - A(f)]^{-1} = \bar{A}(f) \quad (11)$$

490 where I is the identity matrix.

491 Considering the trade-off between sufficient spectral resolution and overparameterization, we
492 determined the model order as a value of 15 (60 ms for our 250 Hz sampling rate), as a comparable
493 value of 10 (50 ms for 200 Hz sampling rate) was used in the previous study that focused on an
494 MVAR model of sensorimotor cortical networks underlying the beta oscillation (*Brovelli et al., 2004*).

495 **Directed coherence and partial directed coherence**

496 We then derived two measures based on the transfer function matrix $H(f)$ or the coefficient matrix
497 $A(f)$ in the MVAR spectral model, one called directed coherence (*Baker et al., 2006*), while the other
498 called partial directed coherence (*Baccalá and Sameshima, 2001*).

499 Directed coherence ($\gamma_{ij}(f)$) is calculated as:

$$\gamma_{i \leftarrow j}(f) = |H_{ij}(f)|^2 \frac{S_{jj}(f)}{S_{ii}(f)} \quad (12)$$

500 where $S_{kk}(f)$ is the power spectral density of the signal k , calculated based on the AR model as:

$$S(f) = H(f)VH(f)^H \quad (13)$$

501 where V is the covariance matrix of the error term $\epsilon(f)$ and the superscript H denotes the Hermitian
502 conjugate.

503 Partial directed coherence ($\pi_{ij}(f)$) is calculated as follows:

$$\pi_{i \leftarrow j}(f) = \frac{\frac{1}{\delta_i^2} |\bar{A}_{ij}(f)|^2}{\sum_{m=1}^M \frac{1}{\delta_m^2} |\bar{A}(f)_{mj}|^2} \quad (14)$$

504 where δ_k represents a variance of u_k .

505 Partial directed coherence ($\pi_{ij}(f)$), reflecting the off-diagonal elements of $A(f)$, is nonzero if and
506 only if direct causality from y_j to y_i exists, whereas directed coherence ($\gamma_{ij}(f)$), based on $H(f)$ that
507 contains a sum of terms related to every transfer paths, is nonzero whenever any path connecting y_j
508 to y_i is significant, reflecting both direct and indirect causality between y_j and y_i . The two measures
509 also differ in normalization; $\gamma_{ij}(f)$ is normalized with respect to the structure that receives the signal,
510 whereas $\pi_{ij}(f)$ is normalized with respect to the structure that sends the signal.

511 As such, directed coherence provides a total causal influence as the amount of signal power
512 transferred from one process to another but can not distinguish direct causal effects from indirect
513 ones. Conversely, partial directed coherence clearly measures the underlying interaction structure
514 as it provides a one-to-one representation of direct causality, but is hardly useful as a quantitative
515 measure because its magnitude quantifies the information outflow, which does not provide precisely
516 how much information reaches downstream.

517 Documented directed coherence measures applied to corticomuscular interactions (*Baker et al., 2006; Tsujimoto et al., 2009; Witham et al., 2010, 2011*) have limited accuracy in estimating the
518 phase-lag relationship, due to their inability to distinguish the direct and indirect causal effects.
519 This is probably because the sensorimotor corticomuscular interaction comprises closed loops,
520 including a bidirectional interaction between the motor cortex and the muscles (*Schouten and Campfens, 2012; Campfens et al., 2013*). In a nested loop, an oscillation in the past cycle would
521 be recurrently summed, thereby leading to a phase shift owing to the synthesis of oscillations
522 separated with a fixed time lag of the loop cycle. The degree of phase shift is variable for different
523 frequency bands; when a lag in the time domain is converted to a phase in the frequency domain,
524 the phase is increased as a function of the frequency band. Hence, an estimate of a lag based on a
525 phase-lag plot tends to be shorter than actual transmission, as demonstrated by *Campfens et al. (2013)*. The authors further showed in the simulation that partial directed coherence provided the
526 most accurate estimate of the lag that any other directed coherence measures never attained. This
527 is a clear indication that partial directed coherence reflects a direct causal relationship between the
528 two variables as theoretically explained above.

529 Considering the complementary properties of directed coherence and partial directed coherence
530 measures, we decided to employ directed coherence to determine a causal influence between the
531 cortex and muscles, and partial directed coherence to measure the phase-lag relationship for the
532 causally defined interaction by directed coherence. By combining these two measures, we can
533 reliably determine causal influences between the cortex and the muscles, and can also estimate
534 the lag accurately in the presence of open or closed loops interposed in between.

535 *Baker et al. (2006)* showed that the significance limit of directed coherence was comparable
536 with that for standard coherence as stated in equation (5). Based on this assumption, we set
537 α level as the same value for the coherence analysis as for directed coherence ($p = 0.005$). For

541 statistical tests on combined coherence across multiple recorded pairs (pooled coherence), we
542 chose a nonparametric method according to *Baker et al. (2003)* wherein we simply counted the
543 percentage of bins at a particular frequency that exceeded the significance limit in the individual
544 coherence spectra. The percentage was calculated by dividing the significant number by the total
545 number of pairs at a given frequency, and the significance limit was determined using binomial
546 parameter estimation ($p = 0.005$) with the total number of pairs.

547 The phase of partial directed coherence for the significant bins determined by directed coherence
548 was calculated as follows:

$$\theta(f) = \arg \left(\sum_{i=1}^L X_i^*(f) Y_i(f) \right) \quad (15)$$

549 where L is the number of the data sections, X and Y denote each time series, and $*$ denote complex
550 conjugate. The 95% confidence limits on the phase estimates, ($\theta \pm \Delta\theta$) were determined according
551 to *Rosenberg et al. (1989)*:

$$\Delta\theta(f) = 1.96 \sqrt{\frac{1}{2L} \left(\frac{1}{Coherence(f)} - 1 \right)} \quad (16)$$

552 To determine if there is a fixed time delay between the two time series, we fitted a regression
553 line to the phase-frequency relationship, as two correlated signals with a fixed time delay in the
554 time domain give a linear function of frequency in the spectral domain. If the slope is significantly
555 different from zero $p < 0.05$, t -test on the regression coefficient), the constant delay (τ ms) was
556 estimated from the line's slope as follows:

$$\tau = -\frac{1000}{2\pi} A \quad (17)$$

557 where A is the line's slope (rad/Hz). A negative slope (positive delay) indicates that LFP leads EMG
558 with a constant delay and vice versa.

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687 **Supplemental Information**

Table S1. Recorded muscles for each animal

Muscle	monkey U	monkey A	monkey E	monkey S
Adductor Pollicis (ADP)		x	x	x
First Dorsal Interosseous (FDI)	x	x	x	x
Second Dorsal Interosseous (2DI)			x	x
Third Dorsal Interosseous (3DI)			x	x
Fourth Dorsal Interosseous (4DI)			x	x
Abductor Pollicis Brevis (AbPB)		x	x	x
Abductor Digiti Minimi (AbDM)	x	x	x	x
Flexor Digitorum Superficialis (FDS)		x	x	x
Flexor Digitorum Profundus, radial part (FDPr)		x	x	x
Flexor Digitorum Profundus, ulnar part (FDPu)		x	x	x
Palmaris Longus (PL)		x	x	x
Flexor Carpi Radialis (FCR)		x	x	x
Flexor Carpi Ulnaris (FCU)		x	x	x
Abductor Pollicis Longus (AbPL)			x	x
Extensor Carpi Radialis (ECR)		x	x	x
Extensor Carpi Ulnaris (ECU)		x	x	x
Extensor Digitorum Communis (EDC)		x	x	x
Extensor Digitorum-2,3 (ED23)		x	x	x
Extensor Digitorum-4,5 (ED45)		x		
Brachioradialis (BRD)		x	x	x
Biceps Brachii (Biceps)		x	x	x
Triceps Brachii (Triceps)			x	

Table S2. Recorded and analyzed LFP and EMG pairs in studied structures for each animal

Structure	Spinal cord				Motor cortex	
	Monkey	U	A	E	S	E
LFP recordings	4	7	72	1	71	26
EMG recordings	2	19	20	21	20	21
LFP-EMG pairs	8	133	1440	21	1420	546
EMG cross-talk	0	73	240	12	320	111
Analyzed pairs	8	60	1200	9	1100	435

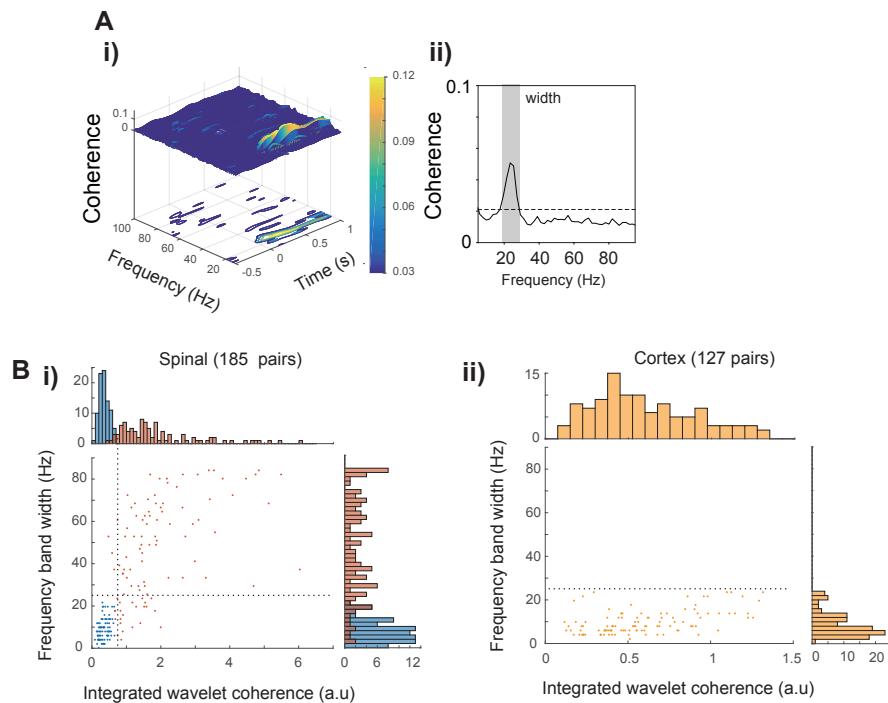


Figure S1. Group classification of coherence patterns. **A.** i) Integrated contour in wavelet coherence and ii) the frequency width in standard coherence for classification. The integrated contour was calculated as a sum of the area above the significance level from the wavelet coherence, whereas the frequency width was taken as consecutive coherence above the significance level at its highest peak (shaded area). **B.** The integrated contours (x-axis) for Spino-muscular coherence exhibited two unimodal distributions, delineating spino-muscular narrow-band and broad-band coherence, whereas corticomuscular coherence was distributed unimodally in narrow band. Using frequency band width (y-axis) some outliers ($> 25\text{Hz}$ in frequency band width in the upper-left quadrant) in narrow-band coherence were corrected to broad band coherence.

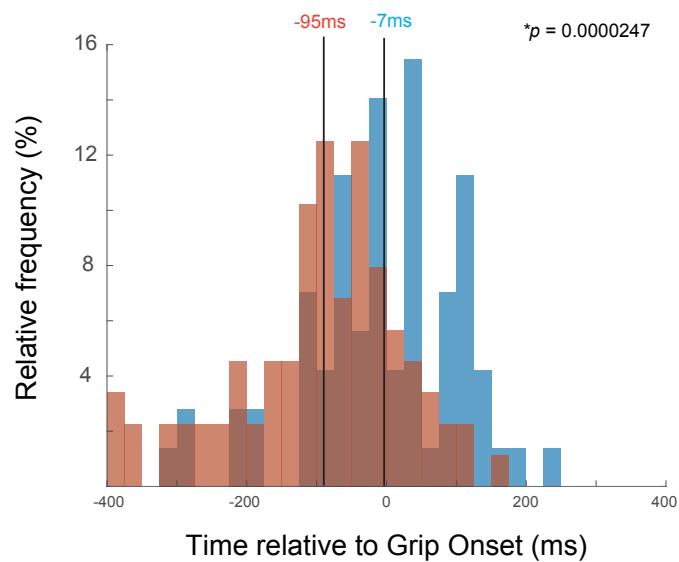


Figure S2. Comparison of latencies for spinal broad-band (BB) and narrow-band (NB) coherence with respect to grip onset. The median latency for BB (red bars: -95 ms) was significantly earlier than that for NB (blue bars: -7 ms). The p -value was calculated using t -test with unequal variance.