

Pupil responses as indicators of value-based decision-making

Joanne C. Van Slooten^{1*} Sara Jahfari^{2,3} Tomas Knapen^{1,3}
Jan Theeuwes¹

¹ Department of Experimental and Applied Psychology, Vrije Universiteit, Amsterdam, The Netherlands

² Spinoza Centre for Neuroimaging, Royal Academy of Sciences, Amsterdam, The Netherlands

³ Department of Psychology, University of Amsterdam, Amsterdam, The Netherlands

*Joanne C. Van Slooten
Vrije Universiteit Amsterdam
Department of Experimental and Applied Psychology
Van Der Boechorststraat 1
1081 BT Amsterdam, The Netherlands
joannevslooten@gmail.com

1

Abstract

2 Pupil responses have been used to track cognitive processes during decision-making. Studies have
3 shown that in these cases the pupil reflects the joint activation of many cortical and subcortical brain
4 regions, also those traditionally implicated in value-based learning. However, how the pupil tracks
5 value-based decisions and reinforcement learning is unknown. We combined a reinforcement learning
6 task with a computational model to study pupil responses during value-based decisions, and decision
7 evaluations. We found that the pupil closely tracks reinforcement learning both across trials and par-
8 ticipants. Prior to choice, the pupil dilated as a function of trial-by-trial fluctuations in value beliefs.
9 After feedback, early dilation scaled with value uncertainty, whereas later constriction scaled with re-
10 ward prediction errors. Our computational approach systematically implicates the pupil in value-based
11 decisions, and the subsequent processing of violated value beliefs. These dissociable influences provide
12 an exciting possibility to non-invasively study ongoing reinforcement learning in the pupil.

13 *Introduction*

14 There is fast-growing interest to understand how the pupil, as a non-invasive proxy of neuromodulation¹,
15 relates to cognition and in particular decision-making. Traditionally, pupil dilation during and after
16 decisions has been related to uncertainty and surprise²⁻⁶, likely via noradrenergic modulations by
17 the locus coeruleus (LC)^{7,8}. Recent work, however, shows that the pupil also tracks activity of other
18 neuromodulatory nuclei. For example, in a recent perceptual decision-making task it was found
19 that pupil dilations were modulated by activity in dopaminergic midbrain nuclei⁹. These nuclei are
20 known to release dopamine in response to rewards and reward-predicting cues to optimize future
21 decisions¹⁰⁻¹². The pupil also dilates in response to the presentation of cues predicting reward¹³⁻¹⁵ and
22 tracks changes in reward expectations¹⁶. These pupil responses are blunted in Parkinson's patients, yet
23 are fully restored by dopamine agonists^{17,18}.

24 These findings raise the intriguing possibility that the pupil is sensitive to a multitude of neuro-
25 modulatory processes, including dopamine, implying that it could be used to non-invasively study the
26 underlying processes that shape value-based decisions and learning. Here, we investigated the interplay
27 between the pupil, reinforcement learning and value-based decision-making by using a computational
28 reinforcement learning (RL) model as a basis for linear systems analysis of pupil size fluctuations.

29 We measured pupil size while thirty-four participants performed a probabilistic reinforcement
30 learning task, consisting of a learning and transfer phase (Fig. 1a,b & Methods). The reliability of
31 choice outcomes varied across three learning pairs¹⁹ with different reward probabilities. These differ-
32 ent reward probabilities create varying degrees of choice difficulty, uncertainty and value expectations
33 across choices. We fit a hierarchical Bayesian version of the Q-learning RL algorithm²⁰ to participants'
34 choices in the learning phase to describe value-based choices and outcome evaluations (Fig. 1c &
35 Methods)²¹⁻²⁴. The Q-learning algorithm describes value-based decision-making using two functions:
36 a choice function and an outcome function. The choice function calculates the probability of choosing

37 one option (Q-chosen) over the other (Q-unchosen), based on one's sensitivity to value differences, or
38 explore-exploit tendency (β ; Fig. 1d, left panel). The outcome function then computes the magnitude
39 by which the reward prediction error (RPE) changes value beliefs about the chosen option, scaled by
40 the learning rate (α ; Fig. 1d, right panel)²⁵. As value beliefs are differentially updated after positive and
41 negative outcomes^{26–28} via different striatal learning mechanisms^{29–31}, we defined separate learning
42 rate parameters for positive (α_{Gain}) and negative (α_{Loss}) choice outcomes^{21,26,27,32}.

43 Our computational approach allows us to investigate the potential utility of the pupil as a proxy
44 for value-based decision-making and value belief updating, across two levels. First, we describe par-
45 ticipants' choice behaviour using parameters that embody core computational RL principles. These
46 parameters provide a strong handle to investigate how inter-individual differences in value-based learn-
47 ing and decision-making relate to pupil responses. Second, by simulating the learning process we can
48 investigate how pupil size depends on trial-to-trial fluctuations in underlying computational variables
49 such as value beliefs, uncertainty and reward prediction errors. That is, our experimental paradigm
50 allowed us to map pupil responses onto separable computational components both across participants
51 and trials.

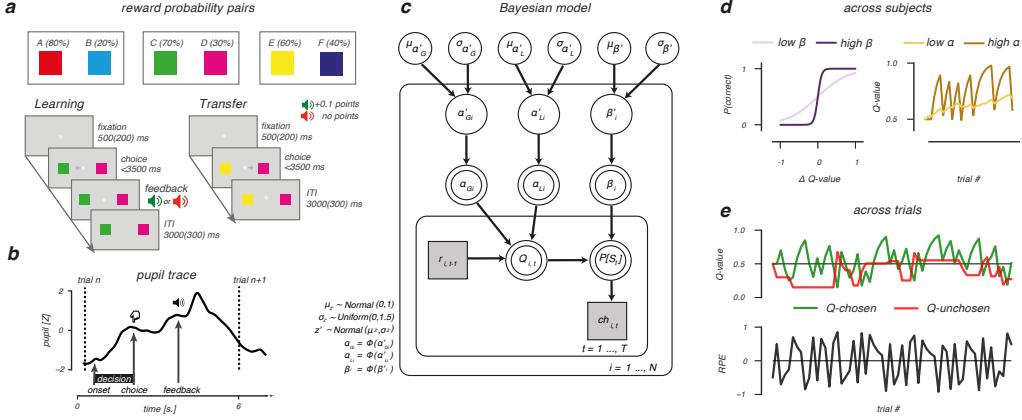


Figure 1: Probabilistic selection task and reinforcement learning model. **a**, During learning, 3 option pairs were presented in random order. Participants had to select the more rewarding option of each pair (option A, C and E) by learning from probabilistic feedback that indicated +0.1 reward points after a ‘correct’ choice, or no points. Choosing option A resulted in a reward in 80% of the times, whereas choosing option B resulted in a reward only in 20% of the times. Reward probability ratios were 70/30 for the CD pair and 60/40 for the EF pair, thereby increasing uncertainty about the correct option to choose. The transfer phase tested how much was learned from the probabilistic feedback. All options were randomly paired with one another, and participants selected the most rewarding option based on earlier learning. In this phase, feedback was omitted. **b**, Example pupil trace for a trial in the learning phase. **c**, Bayesian hierarchical model, consisting of an outer participant ($i = 1 \dots, N$) and inner trial ($t = 1 \dots, T$) plane. Variables of interest are depicted by circular and squared nodes, indicating continuous and discrete variables, respectively. Shaded variables are obtained from the behavioural data and used to fit the model. Double bordered variables are deterministic, as they were derived from the model fit. Arrows indicate dependencies between variables. $\Phi()$ represents the probit transform. **d**, Model parameters governing value-based decision-making. Left panel: the β -parameter describes sensitivity to option value differences (ΔQ -value). Higher β -values indicate greater sensitivity to ΔQ -value and more exploitative decisions for options with highest expected rewards. Right panel: the α -parameter governs value belief updating. Higher learning rates (α) indicate rapid, but more volatile value belief updating compared to lower learning rates. **e**, Across-trial fluctuations in value beliefs (Q-values) for the chosen and unchosen option and RPEs with the EF pair as example.

52 **Results**

53 ***Behavioural and model performance***

54 Participants learned the stimulus-reward contingencies well, as they correctly learned to select the
55 higher reward probability option in all three pairs ($P(\text{correct})$ above chance, all P 's $<.001$; Fig. 2a).
56 Performance was best in AB and decreased progressively from CD to EF, where smaller differences
57 in the reward probability ratios increased the number of incorrect responses ($F_{(2,66)} = 14.45, P<.001$,
58 $\eta_p^2=.19$) and response times ($F_{(2,66)} = 5.5, P=.006, \eta_p^2=.04$). In the transfer phase, choices were guided by
59 the previously learned reward probabilities. Here, participants made more errors ($F_{(2,66)} = 49.3, P<.001$,
60 $\eta_p^2=.53$) and were slower ($F_{(2,66)} = 34.6, P<.001, \eta_p^2=.12$) when confronted with option pairs with small
61 value differences (Fig. 2b), consistent with earlier studies.^{26,33,34}

62 The Q-learning model simulated participants' choice behavior well (Fig. 2c) when using the fitted
63 learning rates ($\alpha_{\text{Gain}}, \alpha_{\text{Loss}}$) and explore-exploit (β) parameter (Fig. 2d). In accordance with behavior,
64 the estimated value beliefs were highest for A and lowest for B (Fig. 2d) with differences in value beliefs
65 being largest for AB, followed by the CD and EF pair ($F_{(2,66)} = 20.63, P<.001, \eta_p^2=.39$).

66 ***Pupil responses predict individual differences in value-based decision-making***

67 We next investigated whether the pupil was sensitive to the underlying processes supporting value-
68 based decisions. To do so, we first characterized the average pupil response pattern across subjects
69 epoched around two separate moments in the trial: leading up to and immediately after the moment of
70 choice and after receiving choice feedback. Around the moment of a choice, average pupil dilation was
71 observed already ~1s. prior to the moment of the behavioural report (Fig. 3a), reflecting the unfolding
72 decision process^{5,35}. After receiving choice feedback, a biphasic pupil response was observed that was
73 characterized by early dilation (~1s. post-event) and late constriction (~2s. post-event; Fig. 3b).

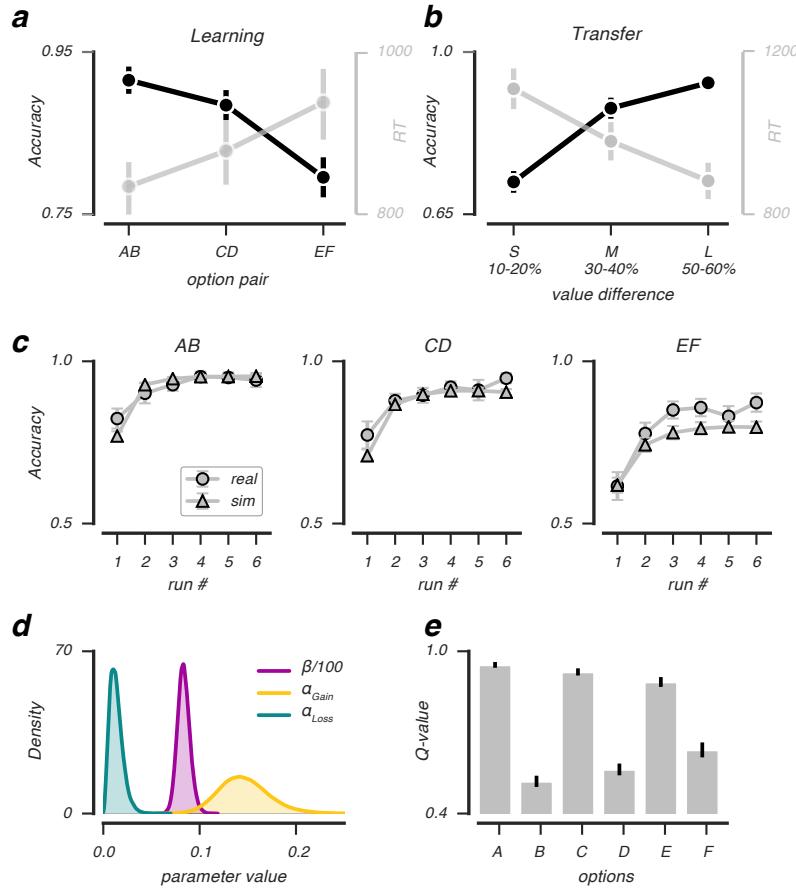


Figure 2: Behavioral and model performance. Average accuracy and RT across subjects ($N=34$) as a function of option pairs in the learning phase (a) and option value differences (derived from the experimental reward probabilities) in the transfer phase (b) that indicated small (S), medium (M) or large (L) value differences between presented options. c, Real and simulated choice accuracy as a function of run number in the learning phase, split by option pair. For all option pairs, simulated and real accuracy was very similar, with real EF accuracy being slightly underestimated by the model. d, Group-level posterior distributions of the obtained parameter estimates for β , α_{Gain} and α_{Loss} . e, Model estimates of value beliefs for each option at the end of the learning phase. $\beta/100$ for visualization; error bars represent mean \pm s.e.m.

74 Across individuals, the observed choice- and feedback-evoked pupil responses corresponded differ-
75 entially to the underlying processes driving value-based decision-making. As shown in Fig. 3c (upper
76 panel), pupil dilation at the moment of a choice was uniquely predicted by an individual's sensitivity
77 to value differences, or explore-exploit tendency (β ; permutation test, $P=.006$; Supplementary Fig. 1a),
78 indicating that a greater tendency to exploit high value options (high β) related to a stronger dilatory
79 response (Fig. 3c, lower panel). Feedback-related dilation and constriction correlated inversely with
80 an individual's positive, but not negative, learning rate (Supplementary Fig. 1b), suggesting that this
81 parameter selectively scaled the amplitude of the feedback-evoked pupil response. Indeed, as shown in
82 Fig. 3d (upper panel), the feedback-evoked response amplitude was uniquely predicted by an individ-
83 ual's positive learning rate (α_{Gain} ; permutation test, $P=.017$), indicating that slower updating of value
84 beliefs after positive feedback predicted a stronger feedback-evoked response (low α_{Gain} ; Fig. 3c, lower
85 panel & Supplementary Fig 1d).

86 In sum, choice- and feedback-evoked pupil responses differentially predicted the underlying pro-
87 cesses supporting value-based decisions in the learning phase. The tendency to exploit high value op-
88 tions (β) predicted stronger pupil dilation leading up to a value-driven choice, whereas less updating of
89 value beliefs after positive feedback (α_{Gain}) predicted an amplified feedback-related response. These re-
90 lations are consistent with theories that describe and formalize Q-learning, in which the explore-exploit
91 parameter determines the outcome of a value-driven choice and learning rates affect how much value
92 beliefs are updated after receiving choice feedback.

93 *Pupil dilation reflects the value of the upcoming choice, during learning but not in transfer*

94 We observed that across-subject variability in pupil responses was explained by model parameters
95 that describe the underlying processes driving value-based decision-making. But do pupil responses
96 also reflect the ongoing reinforcement learning process during value learning? In a next step, we in-

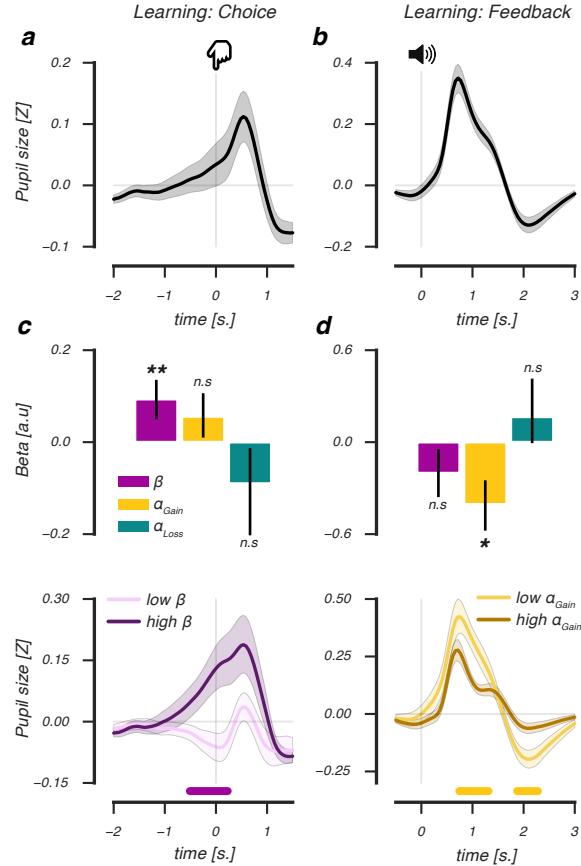


Figure 3: Across-subject relations between model parameters and pupil responses during choice and after feedback. Average deconvolved choice-related (a) and feedback-related (b) pupil response. Regression coefficients of an across-subject GLM of the relation between derived model parameters and pupil dilation at the moment of choice (c, upper panel), and a scalar amplitude measure of the feedback-related pupil response (d, upper panel). Median split across subjects based on modulations of β at the time of choice (c, lower panel), and α_{Gain} after feedback (d, lower panel). Lines and (shaded) error bars represent mean \pm s.e.m of across-subject modulations (N=34). Horizontal significance designators indicate time points where regression coefficients significantly differentiate from zero (P<.05), based on cluster-based permutation tests (n=1000), **P<.01, *P<.05.

97 investigated the extent to which trial-to-trial fluctuations in variables describing ongoing value-based
98 decision-making were tracked by pupil responses.

99 In the learning phase, prior to reaching a value-driven choice, pupil dilation correlated positively
100 with the value difference between options (cluster $P<.001$, 2.0s. pre-event until -0.07s. pre-event, Fig.
101 4a, upper panel), indicating that larger value differences elicited larger pupil dilation before the choice.
102 Specifically, the pupil dilated as a function of trial-by-trial value beliefs of the chosen, but not the un-
103 chosen option (paired t -test, $t(33)=6.98$, $P<.001$; Fig 4b, upper panel), revealing that pupil dilation
104 uniquely reflected the value belief determining the upcoming choice.

105 To rule out the possibility that condition differences (i.e. AB, CD, EF) instead of trial-by-trial fluctu-
106 ations in chosen value beliefs explained pupil dilation prior to a choice, we estimated their independent
107 effects on pupil size in a single regression analysis. We observed no differences between conditions in
108 average pupil dilation prior to a choice (Fig. 4a, lower panel). This also excluded the hypothesis that
109 pre-choice pupil dilation was driven by uncertainty, as we did not observe significantly more dilation
110 in the most difficult, hence most uncertain, EF pair. In all pairs, pre-choice pupil size correlated posi-
111 tively with chosen value ($F_{(2,66)} = 19.76$, $P<.001$, $\eta_p^2=.15$; Fig. 4b, lower panel) irrespective of the condi-
112 tion type ($F_{(2,66)} = 1.8$, $P=.17$). Thus, prior to reaching a value-driven choice, the pupil tracked subtle
113 differences in value beliefs about the upcoming choice, while dilation was not driven by uncertainty
114 differences between the conditions.

115 Next, we asked whether value beliefs also modulated pre-choice pupil dilation in the transfer phase,
116 where feedback was omitted. In contrast to the learning phase, pupil dilation prior to a value-driven
117 choice was not predicted by previously learned value differences between options (Fig. 4c, upper panel),
118 nor by separate chosen or unchosen value beliefs (paired t -test, $t<1$, Fig. 4b, upper panel). Indeed, a
119 repeated measures ANOVA with the factors phase (learning, transfer) and value (chosen, unchosen)
120 indicated that only during learning, but not during transfer, pre-choice pupil dilation was modulated

121 by value beliefs about the upcoming choice ($F_{(1,33)} = 6.9$, $P=.013$, $\eta_p^2=.06$).

122 However, immediately after a value-based choice, learned value beliefs negatively predicted pupil
123 dilation both in the learning (cluster $P=.007$, 0.68s. pre-event until 1.5s. post-event; Fig. 4a, upper
124 panel) and transfer phase (cluster $P=.003$, -0.02s. until 1.48s. post-event; Fig. 4c, upper panel). Now
125 smaller, instead of larger, value differences elicited larger post-choice pupil dilation, suggesting that the
126 difficulty of a recent choice, or the choice conflict it generated, drove pupil size upward. Indeed, we
127 observed a similar post-choice pupil response pattern when regressing choice conflict on the basis of
128 the experimental reward probabilities on pupil size (Fig. 4c, lower panel), indicating that post-choice
129 pupil dilation was modulated by choice conflict, consistent with an earlier report³⁴.

130 These model-based trial-to-trial analyses show that when engaged in active reinforcement learning,
131 pupil dilations differentially reflect value beliefs and choice conflict at different points in time. Prior
132 to value-based choices, pupil size uniquely reflected value beliefs about the upcoming choice, where
133 stronger dilations predicted higher value beliefs. This pattern of pre-choice value dilations was absent
134 in the subsequent transfer phase where rewards could not be obtained, indicating that seemingly similar
135 pupil dilations prior to value-based choices indexed different cognitive processes during learning and
136 transfer.

137 *Feedback-evoked pupil responses reflect value uncertainty and reward prediction errors*

138 Only during active reinforcement learning, we observed that choice-related pupil dilation reflected
139 value beliefs about the upcoming choice. If the pupil reliably tracked ongoing reinforcement learning, it
140 should also provide information about the evaluation of a choice outcome. In the last step, we therefore
141 investigated how feedback-evoked pupil responses covaried with the degree to which outcomes violated
142 value beliefs about a recent choice.

143 We observed larger feedback-evoked pupil dilation (Fig. 5a) after choices between options with

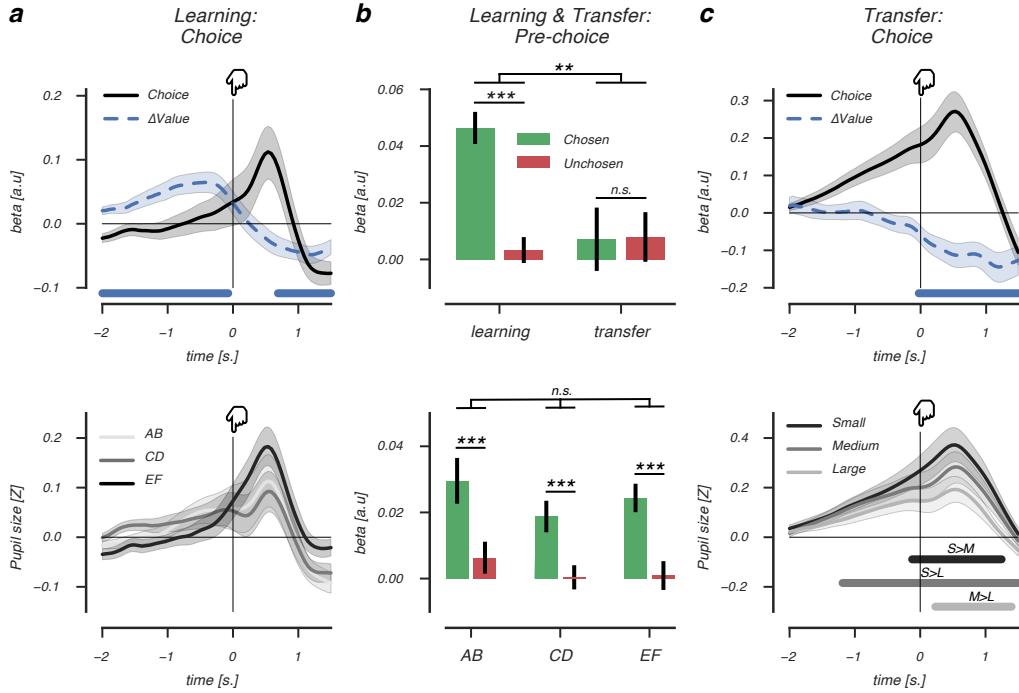


Figure 4: Pre-choice pupil dilation reflects the value of the upcoming choice. **a** (upper panel), Beta coefficients accounting for choice-related pupil dilation in the learning phase. Larger value differences between options (blue dashed line) elicited larger choice-related pupil dilations (black solid line) prior to choice (at $t=0$). After choice, this relationship reversed, as smaller value differences elicited larger post-choice pupil dilations. **a** (lower panel), Average choice-related pupil dilation for AB, CD and EF pairs. **b** (upper panel), Beta coefficients of chosen and unchosen value regressors accounting for pupil size fluctuations in the pre-choice decision interval of the learning (left) and transfer phase (right). **b** (lower panel), Beta coefficients of chosen and unchosen value regressors split by learning phase pairs, showing that pre-choice pupil size is modulated by values of the to-be chosen stimulus, irrespective of uncertainty. **c** (upper panel), Learned value differences did not modulate choice-related pupil dilation prior to choice (at $t=0$). After choice, smaller learned value differences elicited stronger pupil dilation. **c**, (lower panel): Smaller value differences between choice options elicited larger post-pupil dilation, indicating choice conflict drove pupil size. Lines and (shaded) error bars of represent mean \pm s.e.m of within-subject modulations. Horizontal significance designators indicate time points where regression coefficients significantly differentiate from zero ($P < .05$), based on cluster-based permutation tests ($n=1000$), *** $P < .001$, ** $P < .01$, repeated measures ANOVA.

144 small value differences. Specifically, early post-feedback dilation correlated negatively with differences
145 in value beliefs of recently presented options (cluster $P < .001$, -1.5s. pre-event until 1.78s. post-event;
146 Fig. 5b). We furthermore verified that these feedback-evoked dilations were not driven by feedback
147 valence (Supplementary Fig. 2a,b). In contrast to dilation in the choice interval, dilation in the feedback
148 interval was explained by fluctuations in trial-by-trial value beliefs of both the chosen and the unchosen
149 options, in opposite directions (Fig. 5c). Thus, lower beliefs about the chosen and higher beliefs about
150 the alternative option both increased dilation, indicating that uncertainty about the value of a past
151 choice modulated feedback-evoked dilation. In support of this, trial-by-trial chosen and unchosen
152 value beliefs explained feedback-evoked dilation already prior to receiving feedback, showing that it
153 was uncertainty about the outcome of a value-based decision that drove pupil size. Lastly, outcomes that
154 violated value beliefs did not elicit larger feedback-evoked dilations (Supplemental Fig. 2), excluding
155 the hypothesis that these modulations of the feedback response reflected surprise.

156 Importantly, whereas value beliefs about a recent choice affected early dilation, the degree to which
157 outcomes violated those beliefs modulated late feedback-evoked pupil constriction. As shown in Fig.
158 5b, signed RPEs correlated positively with late feedback-evoked pupil constriction ~2s. after receiving
159 feedback (cluster $P < .001$, 1.8s. until 3.0s. post-event). This correlation indicated that worse-than-
160 expected outcomes (-RPEs) elicited stronger pupil constriction compared to better-than-expected out-
161 comes (+RPEs).

162 To summarize, we observed a biphasic feedback-evoked pupil response that tracked the evaluation
163 of a recent value-based choice. Early pupil dilation was modulated by uncertainty about the value of
164 options, as choices between similarly valued options increased dilation the most. Late pupil constric-
165 tion was modulated by the violation of current value beliefs, as worse-than-expected outcomes elicited
166 stronger pupil constriction compared to better-than-expected ones.

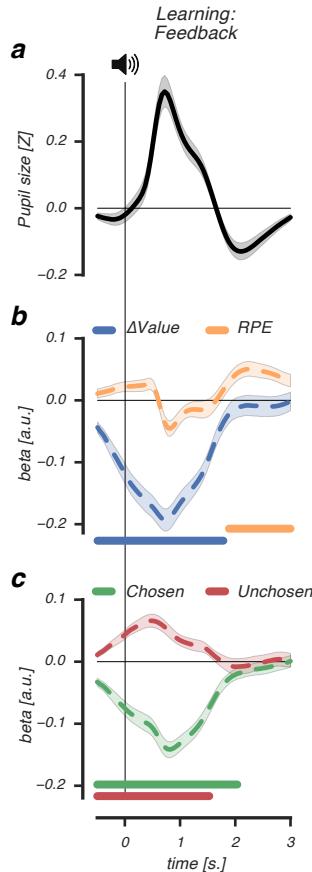


Figure 5: Feedback-evoked pupil responses reflect value uncertainty and reward prediction errors.
a-c, Beta coefficients accounting for feedback-evoked pupil responses in the learning phase. The feedback-evoked pupil response (a) was characterized by early dilation (~1s. post-event) and late constriction (~2s. post-event). **b**, Early in time (~1s. post-event), feedback-evoked pupil dilation correlated negatively with the difference in value beliefs about recently presented options (Δ Value, blue dashed line). Late in time (~2s. post-event), feedback-evoked pupil constrictions correlated positively with signed RPEs (orange dashed line). **c**, Both lower value beliefs of the recently chosen and higher value beliefs of recently unchosen option increased feedback-evoked pupil dilations, already prior to the moment of feedback (at $t=0$). Lines and shaded error bars represent mean \pm s.e.m of within-subject modulations. Horizontal significance designators indicate time points where regression coefficients significantly differentiate from zero ($P < .05$). Statistics based on cluster-based permutation tests, $n=1000$.

Discussion

167 The present results provide the novel insight that the pupil is a reliable reporter of the underlying pro-
168 cess of learning and decision-making based on value. When engaged in active reinforcement learning,
169 but not when choice value was already internalized, the pupil showed two distinct response patterns.
170 Prior to reaching a value-driven choice, pupil dilations scaled with trial-by-trial value beliefs about
171 the upcoming choice and were diagnostic for an individual's sensitivity to choose the option with the
172 highest expected outcome. Feedback about the choice subsequently evoked a biphasic evaluation re-
173 sponse. Early pupil dilation scaled with uncertainty about the value of recent choice options, whereas
174 subsequent pupil constriction scaled with the violation of current choice value beliefs, or signed reward
175 prediction errors. Moreover, the amplitude of this (post-feedback) biphasic response was predicted by
176 variability in learning rates across participants, which determine the updating of value beliefs given the
177 reward prediction error.

179 Previous studies have shown that cues predicting reward increase pupil dilation^{13–15,17,18}. Our ob-
180 servation that value beliefs increase pupil dilation prior to choice are in line with these findings. Criti-
181 cally, we additionally show that pupil dilation increases as a function of value beliefs about the chosen
182 option and signal the value of the upcoming choice. Moreover, we found that pupil dilations were not
183 modulated by the value of the alternative option, indicating that the pupil does not reflect the values as-
184 sociated with all potential options, but specifically, the value that was driving the choice. Interestingly,
185 striatal dopamine concentrations and phasic responses of dopamine neurons are observed to reflect
186 chosen value^{36–38}. This signalling is thought to support value learning of a choice, as the value of the
187 chosen option gets updated according to the reward prediction error after receiving choice feedback.

188 Importantly, only during learning, but not during transfer, was pupil dilation prior to choice mod-
189 ulated by choice value. Why was this the case, when participants had to make value-based decisions in
190 both phases? One important difference between the phases was the ability to learn from the outcomes

191 of actions. In the learning phase, options could be compared to each other and the outcome of a choice
192 was immediately presented. This was very different in the transfer phase, when participants were con-
193 fronted with new choice situations and had no ability to learn from their choices because they never
194 received feedback. Dopamine, particularly in the striatum, plays an important role during reinforce-
195 ment learning³⁹. Striatal dopamine strengthens actions that lead to rewarding outcomes and weakens
196 those that lead to aversive ones^{19,26,30}, thereby flexibly adapting behaviour to maximise rewards. In the
197 transfer phase, value beliefs are consolidated and dopamine no longer plays an important role in learn-
198 ing or modulating choice behaviour. Information used to make a value-based choice is now retrieved
199 from memory, guided by structures that encode learned value representations, such as the ventrome-
200 dial prefrontal cortex^{40,41}. Our finding that the pupil was only sensitive to choice value during active
201 reinforcement learning could mean that the pupil is particularly sensitive to the process of learning the
202 value of choices, or contingency learning.⁴²

203 An individual's sensitivity to value differences between presented options, as quantified by our
204 computational model, predicted the amount of pupil dilation exactly at the time of a value-based
205 choice. Individuals that were more sensitive to small value differences showed stronger dilations. These
206 individuals exploited high value options, leading to better task performance²². Increased pupil di-
207 lation has been associated with better task performance^{43,44}, or with the tendency to exploit in dy-
208 namic environments^{45,46}. The observed relationship between pupil dilation and individual sensitivity
209 to value differences could reflect either of these processes, as choosing a high value option can result
210 from accurate option value representations or from the general tendency to favour exploitation over
211 exploration⁴⁷. Measuring pupil responses during value-based decision-making in a reversal learning
212 paradigm might provide a way to disentangle these two alternative explanations, as optimal task per-
213 formance would then depend on changing decision strategies over time.

214 Uncertainty did not drive pupil size prior to a value-based choice, as our results indicated that the

215 most difficult, hence uncertain, pair (EF) did not increase dilation. On the contrary, higher value be-
216 liefs, indicating more certainty about choice value, elicited greater dilation. This finding contrasts with
217 earlier work relating pupil dilations to situations of increased uncertainty^{2,4,5}, but aligns with those asso-
218 ciating it with certainty^{3,48}. One possible explanation for these differential findings is that in our study,
219 higher value beliefs about the upcoming choice led to increased reward expectations¹⁷, or decreased
220 risk assessment³, driving pupil dilation prior to the choice.

221 However, immediately after a value-based choice, but prior to feedback, we observed that uncer-
222 tainty modulated pupil size, as choices between closely valued options triggered strong post-choice
223 dilation. While our study is the first to relate the pupil directly to value beliefs, these findings are con-
224 sistent with observations of pupil dilation indexing choice conflict after difficult decisions³⁴ or decision
225 uncertainty during perceptual decisions⁶. Our work extends these studies by showing that different cog-
226 nitive processes affect pre- and post-choice dilation, linking pre-choice dilation to chosen value beliefs
227 and post-choice dilation to value uncertainty. This provides a tentative link to dopamine neurons en-
228 coding reward uncertainty⁴⁹, where sustained dopamine activity prior to the moment of the outcome
229 was strongest after cues predicting reward with 50% probability. These highly unpredictable cues are
230 thought to drive learning maximally, as high subjective uncertainty indicates the lack of an accurate
231 reward predictor and the need to improve predictions⁴⁹. Pupil dilation after a choice between options
232 with small value differences may relate to this process, reflecting the allocation of attentional resources
233 to support learning from the upcoming choice outcome.

234 After feedback, a biphasic feedback-evoked pupil response tracked two different evaluation pro-
235 cesses related to the outcome of a choice. First, early dilations were explained by uncertainty about the
236 value of the choice outcome, but not by surprise, as outcomes that violated value beliefs did not trigger
237 stronger dilations. This is a somewhat surprising finding, given that pupil dilations can be stronger
238 after unexpected outcomes^{3,4,50-52}. What our results suggest is that during reinforcement learning, the

239 uncertainty associated with the outcome of a choice increases pupil dilation, irrespective of its positive
240 or negative value. What this may indicate is that early pupil dilation reflected increased attention to
241 uncertain, but potentially rewarding stimuli in the environment.

242 Second, late pupil constriction was explained by signed reward prediction errors, thus, reflecting
243 how much the outcome violated current value beliefs about the chosen option. Lower-than-expected
244 choice outcomes resulted in smaller pupil responses compared to higher-than-expected ones, which
245 shows a striking resemblance to the reward prediction error pattern of phasic dopamine neurons^{10,53,54}
246 that briefly activate after higher-than-expected outcomes and deactivate after lower-than-expected out-
247 comes. In calculating this error term, the obtained reward is compared to the value of the chosen
248 option³⁶, which we observed also modulated pupil dilation prior to a value-based choice. Thus, our
249 findings suggest that pupil responses track specific decision and evaluation signals that promote value-
250 based learning and decision-making.

251 Recently, a more elaborate view of the phasic dopamine reward prediction error response has been
252 proposed, in which an initial unselective component detects any potential reward and a later com-
253 ponent codes the well-known reward value⁵⁵ The dynamic evolution of the feedback-evoked pupil re-
254 sponse is consistent with this pattern, as early dilation unselectively increased after uncertain outcomes
255 and late constriction reflected the evaluation of the outcome's reward value.

256 To conclude, our study provides evidence that the pupil is a reliable indicator of value-based
257 decision-making, as it signalled the processing of value up to a choice and the subsequent evaluation
258 of choice outcomes in terms of uncertainty and violations of value beliefs. There were several aspects
259 to our approach that enabled us to establish these specific relations and to move beyond previous work
260 linking the pupil to reward. First, we characterised the full temporal profile of value-based decisions
261 in the pupil, thereby relating different decision and evaluation processes to different components of
262 the pupil response. Second, these specific relations could only be established with the use of a formal

263 learning model that provided us access to participants' developing value beliefs, and the underlying
264 processes thought to support value-driven decisions. This also highlights our use of subjective value
265 estimates to relate to the pupil. In contrast, previous studies investigating reward-related effects on
266 pupil size employed externally defined value estimates^{2,3,17,18,52}, with one notable exception¹⁶. Lastly,
267 our study describes the temporal evolution of reinforcement learning in the pupil, thereby providing
268 evidence that the pupil can be used to non-invasively track the reinforcement learning process as
269 it takes place. Future studies that combine functional brain imaging and pupillometry will have to
270 further specify the brain areas that contribute to the value-based pupil response.

271 *Methods*

272 *Participants*

273 Forty-two healthy participants with normal to corrected to normal vision completed the experiment
274 (10 males; mean age=24.9; age range=18-34 years). They were paid 16€ for 2 hours of participation
275 and earned an additional performance bonus (mean=10.2€, SD=1.8). The ethical committee of the
276 Vrije Universiteit Amsterdam approved the study and written informed consent was obtained from all
277 participants. Eight participants were excluded from analyses due to the following reasons: inadequate
278 fixation to the center of the screen (N=4), reporting more than three unique stimulus pairs in the
279 learning phase (N=1) and (almost) perfect choice accuracy in the learning phase, which complicated
280 behavioral model fitting (N=3), resulting in a total of 34 participants for the analyses.

281 *Task & Procedure*

282 Participants were seated in a dimly lit, silent room with their head positioned on a chin rest, 60 cen-
283 timeters away from the computer screen. They received written information about the general purpose

284 of the experiment, after which they completed a 30-trial practice session of the learning phase. Subse-
285 quently, participants completed for the learning phase 6 runs of 60 trials each (360 trials in total, 120
286 presentations of each stimulus pair), with small breaks in-between runs. After each run, the earned
287 number of points was displayed. At the end of the learning phase, the total number of earned points was
288 converted into a monetary bonus. Directly after the learning phase, participants entered the transfer
289 phase. They completed 5 runs of 60 trials each (300 trials in total, 20 presentations per stimulus pair),
290 with small breaks in-between runs. Overall choice accuracy was displayed at the end of the transfer
291 phase.

292 *Stimuli & trial structure*

293 Stimuli were presented on a 21-inch Iiyama Vision Master 505 MS103DT with a spatial resolution
294 of 1024 x 768 pixels, at a refresh rate of 120Hz, with mean luminance 60 cd/m². Experiments were
295 programmed in OpenSesame and data analysis were performed using custom software written in
296 Python, using Numpy (v1.11.2), Scipy (v0.18.1), FIRDeconvolution (v0.1.dev1), Hedfpy (v0.0.dev1),
297 MNE (v0.14) and PyStan (v2.14) packages. Luminance effects on pupil size were minimized by
298 keeping the background luminance of the display constant. Color stimuli were near-isoluminant to
299 each other and the background (set via a flicker-fusion color calibration test carried out once at the
300 start of the experiment). To account for luminance bias effects, each participant had a unique color
301 pair (red-blue; yellow-dark blue; green-magenta) to reward probability mapping (AB, CD, EF) that
302 was counterbalanced in order (e.g. red-blue or blue-red for AB).

303 In each learning phase trial, participants continuously fixated on a central white fixation dot. After
304 500ms (SD=200ms), two colored stimuli (1.26°x1.26° visual angle) appeared at the horizontal meridian
305 left and right from the central fixation dot at a distance of 5.04° visual angle. Participants made a choice
306 for one of the options using the 'K' (left choice) and 'L' (right choice) keys. A choice was highlighted by

307 a small dark grey arrow (150ms) pointing in the direction of the chosen option. After a random interval
308 drawn from a Gaussian distribution with a mean of 1500ms (SD=300ms), the choice was followed by
309 auditory feedback, indicating reward (+0.1 points; 500ms ‘correct’ sound) or no reward (500ms; pure
310 sine tone at 300Hz). Omissions or response times (RTs) longer than 3500ms were followed by a neutral
311 tone (500ms; pure sine tone at 660Hz). Inter-trial intervals were drawn from a Gaussian distribution
312 with a mean of 3000ms (SD=300ms) Trials of the transfer phase followed the same trial structure as
313 trials in the learning phase, but had a shorter duration as choices were not followed by feedback.

314 *Behavioural analysis*

315 Choices and RTs were recorded for all trials in the learning and transfer phase. RT on every trial was
316 computed as the time from onset of the stimulus pair until the choice (keypress). Trials with RTs below
317 150ms or above the RT deadline of 3500ms were removed from all analyses. As a choice between two
318 options in the learning phase was never necessarily “correct”, we defined the selection of the optimal
319 option (more reinforcing option of the presented pair) as a correct choice. For the transfer phase, value
320 conflict on a particular trial was defined on the basis of the experimental reinforcement value difference
321 between the presented stimuli, where smaller value differences were associated with higher conflict.

322 *Computational model*

323 Choices during the learning phase were fit with a reinforcement learning (“Q-learning”) model^{20,56}. For
324 each option, the model estimates its expected value, or “Q-value”, on the basis of individual sequences
325 of choices and outcomes. All Q-values were set to 0.5 before learning. After each choice, the chosen
326 option’s Q-value is updated by learning from feedback that resulted in an unexpected outcome, which is
327 captured by the RPE, $r_i(t) - Q_i(t)$. Thus, the Q-value for option i on the next trial t is updated depending
328 on the outcome, r , using the following formula:

$$Q_i(t+1) = Q_i(t) + \begin{cases} \alpha_{Gain}[r_i(t) - Q_i(t)] & \text{if } r=1 \\ \alpha_{Loss}[r_i(t) - Q_i(t)] & \text{if } r=0 \end{cases} \quad (1)$$

329 where parameters $0 \leq \alpha_{Gain}, \alpha_{Loss} \leq 1$ represent positive and negative learning rates, respectively,
 330 that determine the magnitude by which value beliefs are updated depending on the RPE. We modeled
 331 separate learning rates, as different striatal subpopulations are involved in positive and negative feed-
 332 back learning²⁹⁻³¹ and individuals tend to learn more from positive feedback^{21,22,28}. Given the Q-values,
 333 the probability of selecting one option over the other (e.g. selecting option A over B) was described by
 334 a softmax choice rule:

$$P_A(t) = \frac{\exp(\beta \cdot Q_A(t))}{\exp(\beta \cdot Q_B(t)) + \exp(\beta \cdot Q_A(t))} \quad (2)$$

335 Here, $0 \leq \beta \leq 100$, or the explore-exploit parameter, described the sensitivity to option value dif-
 336 ferences, where larger β values indicates greater sensitivity, and more exploitative choices, for options
 337 with relative higher reward values.

338 *Bayesian hierarchical fitting procedure*

339 The Q-learning model was fit using a Bayesian hierarchical fitting procedure, where individual pa-
 340 rameter estimates were drawn from group-level parameter distributions that constrained the range of
 341 possible individual parameter estimates. This procedure allowed for the simultaneous estimation of
 342 group-level and individual-level parameters^{23,57}, thereby capitalizing on the statistical strength offered
 343 by the degree to which participants are similar with respect to the model parameters as well as taking
 344 into account individual differences⁵⁸.

345 As shown in Fig 1c, our model was implemented following Jahfari et al. (2016, 2018). Variables $r_i(t)$

346 1) (outcome for participant i on trial $t-1$) and $ch_i(t)$ (choice of participant i on trial t) were obtained from
 347 the behavioural data. Per-participant parameter estimates α_{Gi} (α_{Gain} participant i), α_{Li} (α_{Loss} participant
 348 i) and β_i (β participant i) were modeled using a probit transformation z'_i (α'_{Gi} , α'_{Li} , β'_i). The probit
 349 transformation is the inverse cumulative distribution function of the normal distribution that can be
 350 used to specify a binary response model. z'_i were drawn from group-level normal distributions with
 351 mean $\mu_{z'}$ and standard deviation $\delta_{z'}$. A normal prior was assigned to group-level means $\mu_{z'} \sim \mathcal{N}(1, 0)$
 352 and a uniform prior to the group-level standard deviations $\delta_{z'} \sim \mathcal{U}(1, 1.5)$ ²³. The Bayesian hierarchical
 353 model was implemented in STAN⁵⁹ and fit to all trials of the learning phase that fell within the correct
 354 response time window $150\text{ms} \leq RT \leq 3500\text{ms}$, (mean=99.5% of trials, SD=0.8%). Multiple chains
 355 were generated to ensure convergence, which was evaluated by the Rhat statistic⁶⁰. The Rhat statistic
 356 confirmed convergence of the fitting procedure (i.e., all Rhats were equal to 1.0). We also tested whether
 357 the derived per-participant parameters could simulate choices that were qualitatively similar to the
 358 observed choices originally used for fitting. Here, choices were simulated 100 times for each participant
 359 using the mode of the derived per-participant parameter distribution. Simulated choice accuracy was
 360 averaged across simulations and evaluated against the observed choice data (Fig. 2c).

361 *Quantifying single-trial estimates*

362 The modes of the per-participant posterior parameter distributions were selected to describe individual
 363 positive and negative learning rates (α_{Gain} , α_{Loss}) and relative reward sensitivity (β). In the learning
 364 phase, these per-participant parameter estimates were used to quantify Q-values and RPEs on each
 365 trial. Specifically, we quantified for each trial the value of the chosen option, the unchosen option
 366 and the difference between presented options (ΔValue). In the transfer phase, when participants did
 367 not receive feedback about their choices, we investigated how previously learned value related to pupil
 368 responses during value-based decisions. To do so, we selected the final Q-value estimates for each

369 option (i.e. at the end of the learning phase) and used these values to quantify for each trial the value of
370 the chosen and unchosen stimulus, given the individual sequences of choices. The obtained single-trial
371 variables were used as covariate regressors in a deconvolution analysis (described below), to investigate
372 how they dynamically varied with trial-by-trial fluctuations in transient pupil responses in the learning
373 and transfer phase.

374 *Pupillometry: preprocessing*

375 The diameter of the pupil was recorded at a 1000Hz using an EyeLink 1000 Tower Mount (SR Research).
376 The eye-tracker was calibrated prior to each run. Blinks and saccades were detected using standard
377 EyeLink software with default settings and Hedfpy, a Python package for preprocessing eye-tracking
378 data. Periods of data loss during blinks were removed by linear interpolation, using an interpolation
379 time window of 200ms before until 200ms after a blink. Blinks not identified by the manufacturer's
380 software were removed by linear interpolation around peaks in the rate of change of pupil size, using the
381 same interpolation time window. The interpolated pupil signal was band-pass filtered between 0.05Hz
382 and 4Hz, using third-order Butterworth filters, z-scored per run, and resampled to 20Hz. As blinks
383 and saccades have strong and relatively long-lasting effects on transient pupil size^{61,62}, these influences
384 were removed from the data, as follows. Blink and saccade regressors were created by convolving all
385 blink and saccade events with their standard Impulse Response Function (IRF)⁶²⁻⁶⁴. These convolved
386 regressors were used to estimate their responses in a General Linear Model (GLM), after which we
387 used the residuals of this GLM for further analysis. For the subsequent deconvolution analysis, trials
388 were removed in which participants made a saccade towards either of the two presented colored stimuli
389 (i.e. saccades exceeding 3.3° visual angle away from fixation) to ensure that pupil responses were not
390 affected by eye movements (percentage removed trials, mean=4.8%; SD=4.5%; range=0.0%-16.3%).

393 Transient pupil responses were analyzed using FIRDeconvolution, a Python package used to perform
 394 Finite Impulse Response fits⁶⁵. For the analysis of the learning phase, a design matrix was constructed
 395 that estimated pupil time courses of the following 3 transient event types: the onset of the choice options
 396 (start of the decision interval), choice (keypress) and feedback (auditory tone). Time courses of the
 397 onset of the options and feedback were estimated in the interval -0.5s. pre-event until 3.0s. post-event.
 398 The time course of the choice was estimated in the interval -2.0s. pre-event until 1.5s post-event, as
 399 decision-related pupil dilation is predominantly driven prior to the behavioral report^{5,35}. Further, the
 400 sustained drive of pupil size during the decision interval, defined as the time period from onset of the
 401 options until the choice, was estimated by a boxcar regressor. The boxcar regressor expanded each
 402 trial's RT (in samples) and was normalized by dividing the height of the boxcar by the mean RT of
 403 the regressor. This procedure ensured that the estimated IRF of all transient and sustained regressor
 404 types were comparable. Lastly, the design matrix included 2 stick regressors to estimate the pupil time
 405 course of the following nuisance events: the onset of the fixation dot and the offset of the options
 406 from the screen. Pupil time courses of both events were estimated -0.5s. pre-event until 3.0s. post-
 407 event. No intercept was added to the design matrix as ridge regression (described below) requires
 408 centered dependent and independent variables⁶⁶. For the decision interval, we investigated how value
 409 beliefs about presented options affected pupil size by adding single-trial chosen and unchosen Q-value
 410 estimates as covariates to the design matrix. These Q-value estimates were also used as covariates
 411 for the feedback interval, to investigate how value expectations about a recent choice affected pupil
 412 size during feedback. Finally, we added single-trial RPE estimates to the design matrix to investigate
 413 how violations of choice beliefs affected the feedback-related response. All covariate regressors were
 414 z-scored per participant, to ensure unbiased across-subject comparisons of deconvolution beta weights.

416 The design matrix for the deconvolution analysis of the transfer phase was identical to that of the learn-
 417 ing phase, with two exceptions: (1) the pupil time course for feedback events was not estimated, as no
 418 feedback events occurred during this phase, (2) a stick regressor was included to investigate the effects
 419 of choice conflict on pupil responses. Choice conflict was determined the basis of experimental rein-
 420 forcement value differences between the presented options, where trials were divided into three bins
 421 (10-20%; 30-40% and 50-60%), that corresponded to large, medium and small choice conflict between
 422 options.

424 We implemented the deconvolution analysis using cross-validated ridge regression, which allows one
 425 to find the general solution to a least-squares problem that would be unstable due to multicollinearity
 426 of regressors⁶⁶. Ridge regression penalizes, or shrinks, regression coefficient weights towards zero to
 427 reduce the estimation variance on the coefficients:

$$\hat{\beta}_{ridge} = (X^T X + \lambda I)^{-1} X^T y \quad (3)$$

428 Here, y is the pupil time series signal and X is the design matrix consisting of a set of vectors that
 429 contain ones at all sample times relative to the event timings of which we estimated the pupil response,
 430 and zeros elsewhere. The identity matrix, I , is multiplied by $\lambda \geq 0$, a tuning parameter that controls the
 431 strength of the penalty term. If $\lambda = 0$, the linear regression solution is obtained, $\lambda = \infty$, $\hat{\beta}_{ridge} = 0$. To
 432 obtain for each participant the optimal λ value, we applied cross validation on the pupil time series data.
 433 Here, the pupil data was divided into a training and test set. A weight matrix was obtained for each λ
 434 value (range = $0 \leq \lambda \leq 1$), using the training set, and was used to predict the test set. This process was

435 repeated for 20 different selections of training and test sets, and the best λ value was selected based on
436 its prediction accuracy. The resulting regression, $\hat{\beta}_{ridge}$, contained the deconvolved pupil responses of
437 all separate event types.

438 *Statistical comparisons*

439 Nonparametric cluster-based permutation t -tests⁶⁷⁻⁶⁹ were used to test for significant regression coef-
440 ficients and to correct for multiple comparisons over time. Briefly, for each time point of a time series
441 signal, t -tests were performed on each set of across-subject coefficient values. The cluster size was de-
442 termined by the number of contiguous timepoints for which the t -test resulted in $P < .05$. The observed
443 cluster size was then compared to a random permutation distribution of maximal cluster sizes: the
444 proportion of random clusters resulting in a larger size than the observed one determined the P -value,
445 corrected for multiple comparisons.

446 To assess the effects of chosen and unchosen value covariates on pupil size across the decision
447 interval, we summed each regressor's coefficient values locked to the start (option onset) and locked to
448 the end of the decision interval (the moment of choice), while discarding their post-choice effects. We
449 normalised the summed regressor coefficient values by the number of samples they explained of the
450 pupil time series signal. The resulting averaged, normalised regressor coefficient values were used in a
451 repeated measures ANOVA to test for main and interaction effects on pupil size, both for the learning
452 and transfer phase.

453 Across-subject analyses of the relation between pupil responses and computational model param-
454 eters were calculated using bootstraps⁷⁰. We randomly drew with replacement 10,000 new pupil size -
455 model parameter estimate pairs which were used in the across-subject GLM. From the resulting boot-
456 strapped regression coefficients, 68% confidence intervals were calculated using a percentile approach.
457 P -values calculations were based on a two-sided hypothesis test, with the P -value being the fraction of

⁴⁵⁸ the bootstrap distribution that fell below (or above) 0.

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⁴⁶² *Author contributions*

⁴⁶³ JCS, SJ and TK designed the study. JCS collected and analysed the data. SJ and TK contributed

⁴⁶⁴ novel methods. JCS and SJ wrote the first draft of the manuscript. JCS, SJ, TK and JT wrote the fi-

⁴⁶⁵ nal manuscript.

⁴⁶⁶ *Conflict of interest*

⁴⁶⁷ The authors declare that there is no conflict of interest.

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