

1 TITLE

2 **Challenging the point neuron dogma: FS basket cells as 2-stage nonlinear integrators**

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12 ABSTRACT

13 Interneurons are critical for the proper functioning of neural circuits. While often  
14 morphologically complex, their dendrites have been ignored for decades, treating them as  
15 linear point neurons. Exciting new findings reveal complex, non-linear dendritic  
16 computations that call for a new theory of interneuron arithmetic. Using detailed  
17 biophysical models, we predict that dendrites of FS basket cells in both hippocampus and  
18 prefrontal cortex come in two flavors: supralinear, supporting local sodium spikes within  
19 large-volume branches and sublinear, in small-volume branches. Synaptic activation of  
20 varying sets of these dendrites leads to somatic firing variability that cannot be explained  
21 by the point neuron reduction. Instead, a 2-stage Artificial Neural Network (ANN), with  
22 sub- and supralinear hidden nodes, captures most of the variance. Reduced neuronal circuit  
23 modeling suggest that this bi-modal, 2-stage integration in FS basket cells confers  
24 substantial resource savings in memory encoding as well as the linking of memories across  
25 time.

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GABAergic interneurons play a key role in modulating neuronal activity and transmission in multiple brain regions<sup>1-5</sup>. Among others, they are responsible for controlling the excitability of excitatory and inhibitory cells, modulating synaptic plasticity and coordinating synchrony during neuronal oscillations<sup>2,6-8,9</sup>. GABAergic interneurons come in a variety of molecular profiles, anatomical features and electrophysiological properties<sup>1,3,5,10</sup>. Despite this variability, many interneuron types exhibit similar computations, the most common being a precise EPSP-spike coupling<sup>2,11,12</sup>. As they innervate a large number of cells, near the site of action potential initiation, they are believed to generate a powerful widespread inhibition, also referred to as an inhibitory blanket<sup>13</sup>.

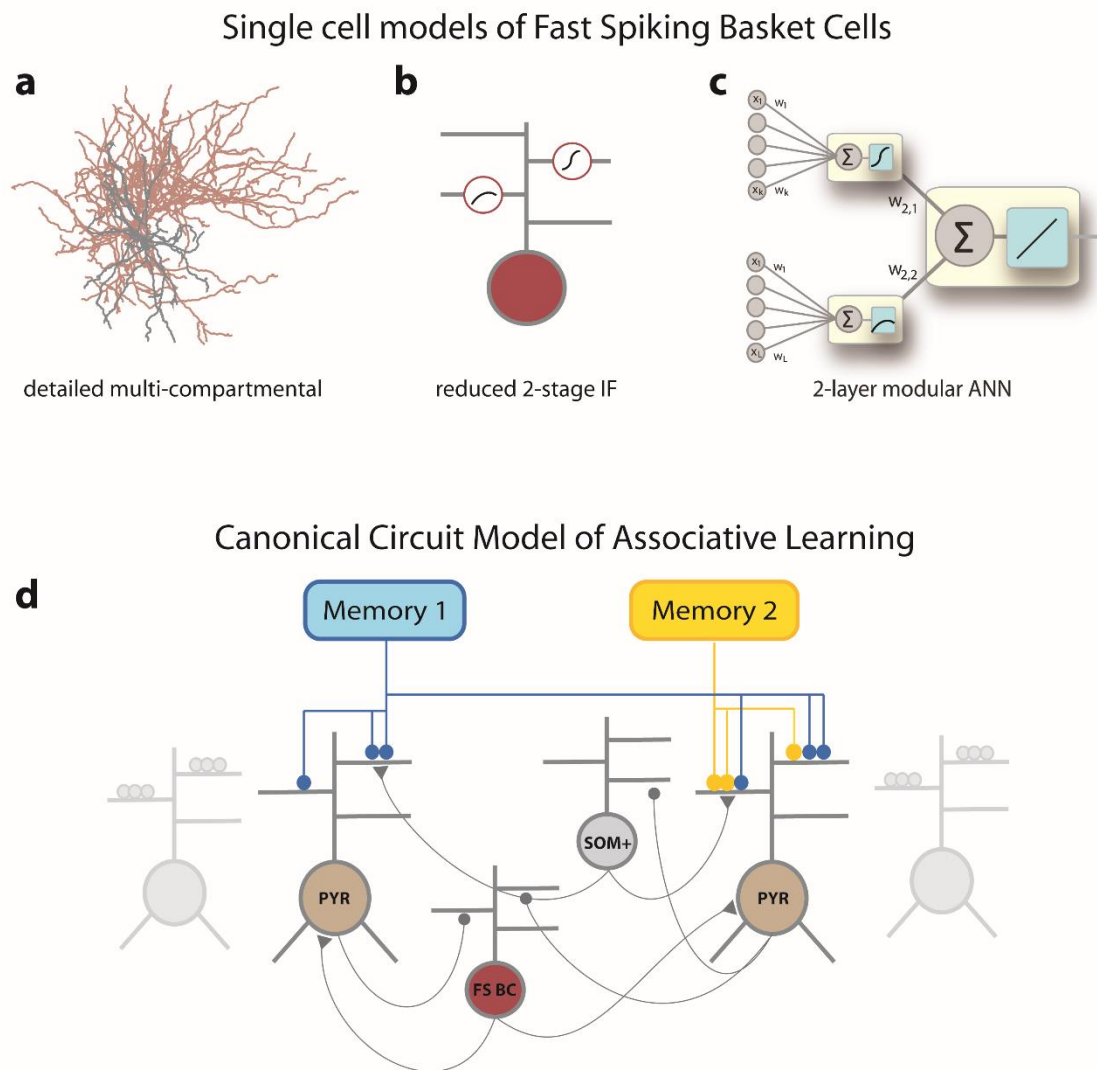
Fast Spiking basket cells (FS BCs) constitute one of the main types of hippocampal and neocortical interneurons<sup>6,13,14</sup>. They are part of the PV positive interneuron class, which also includes the axo-axonic, chandelier and bistratified sub-types. FS BCs are distinguished from other subtypes by their anatomical features<sup>15</sup>, synaptic connectivity patterns<sup>13,16</sup> and membrane mechanisms. These include the presence of calcium permeable AMPA (cp-AMPA) receptors<sup>17,6,18,19</sup>, the low expression of NMDA receptors<sup>19,20</sup>, a weak backpropagation of APs<sup>6,21</sup>, a low density of sodium channels<sup>6</sup> and a high density of potassium channels in their aspiny dendritic trees<sup>5,15,23,6,4,24</sup>.

A growing body of literature recognizes the importance of FS BCs in controlling executive functions such as working memory and attention as well as their role in neurodegenerative disorders<sup>4,25,26</sup>. However, little is known about the mechanistic underpinnings of FS BC contributions to these functions. Most studies have focused on the molecular and anatomical features of FS BCs<sup>7,13</sup> and led to the dogma that FS BCs serve as “on-off” cells, integrating inputs like linear –or at best sublinear- point neurons<sup>28,29</sup>.

This dogma is based on the assumption that FS BCs integrate synaptic inputs in a linear manner, completely ignoring potential dendritic influences<sup>6</sup>. Dendritic integrative properties however, can play a pivotal role in translating incoming information into output signals<sup>30,31,32</sup>. In pyramidal neurons for example, this is often done in highly nonlinear ways that facilitate memory and other executive functions<sup>31,33-36</sup>.

Exciting new findings suggest a potentially similar contribution of dendrites in interneuron function. Sublinear dendritic EPSP integration along with supralinear calcium accumulations has been reported in cerebellar Stellate Cells<sup>11,37</sup>. Moreover, certain

interneuron sub-types in the CA1 area exhibit dendritic supralinearities<sup>38,39</sup> while in the CA3, both calcium nonlinearities and sodium spikes in FS BC dendrites during sharp wave ripples have been reported<sup>2</sup>. The exact nature of dendritic computations in FS BCs, however, is unknown. As a result, whether a linear point neuron or a more sophisticated abstraction -like the two-stage<sup>40</sup> or multi-stage integration proposed for pyramidal neurons- can successfully capture their synaptic integration profile, remains an open question.



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**Figure 1:** Modeling tools used to study dendritic integration in FS BCs and its functional implications. **a)** Detailed, biophysically constrained multi-compartmental models using realistic reconstructions. **b)** Reduced 2-stage integrate and fire models of FS BCs. **c)** 2-layer ANN reduction describing the FS BCs **d)** Reduced network model with simplified pyramidal, FS BCs and SOM+ interneurons. FS-BCs and SOM+ interneurons provide feedback inhibition to excitatory neurons (beige), with FS-BCs interneurons targeting the somatic subunit while SOM+ neurons target the dendritic subunits. Memory encoding afferents provide inputs to excitatory cell dendrites.

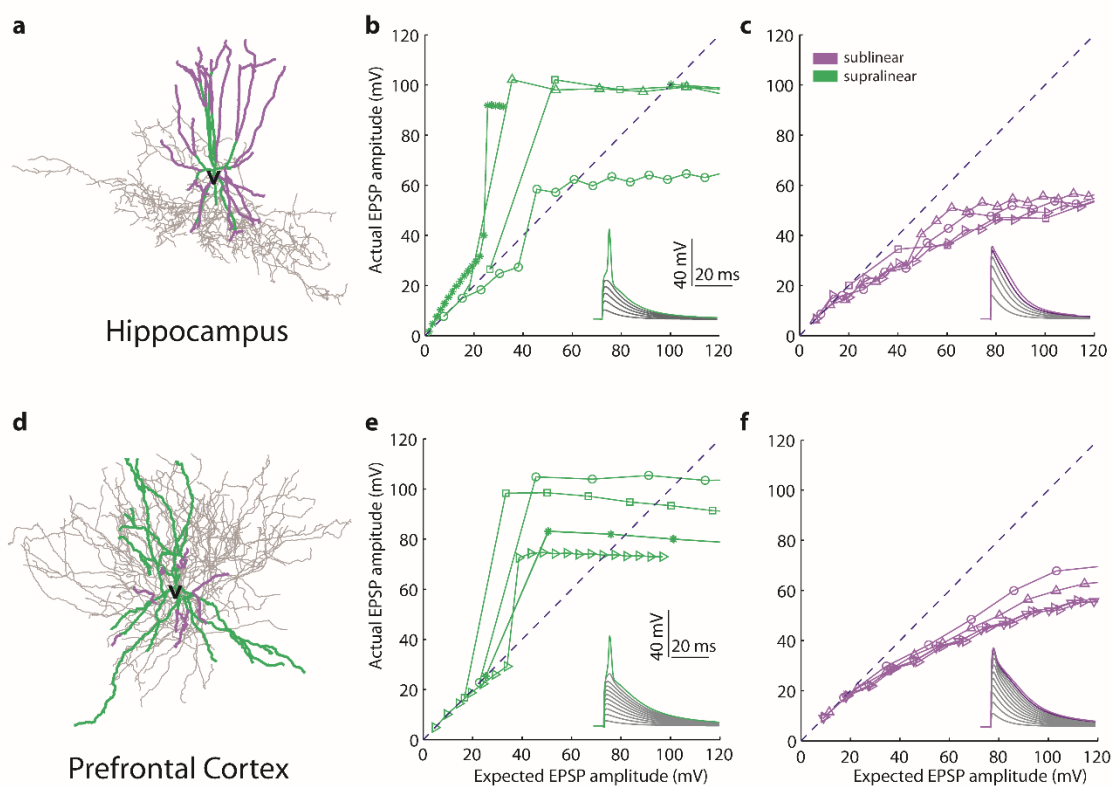
To address these questions, we developed an elaborate toolset that consists of a) detailed, biologically constrained biophysical models of hippocampal and cortical FS BCs, b) reduced 2-stage integrate-and-fire models of these cells, c) 2-layer Artificial neural network abstractions and d) a large scale microcircuit model of 2-stage pyramidal, FS BC and dendrite targeting (SOM) interneurons (See **Online Methods** and **Figure 1**). We first characterized the integration profiles of FS BC dendrites using the detailed biophysical models. Synaptic stimulation predicted the co-existence of two distinct modes within the same tree: some dendrites exhibited supralinear while others sublinear summation of inputs (**Figure 2, Supplementary Figures 4, 5**). Supralinear dendrites supported local, sodium-dependent spikes (**Supplementary Figure 7**) and were characterized by large volume and low input resistance (**Figure 3**), which are shaped by the combination of dendritic length and diameter. Direct manipulation of these anatomical features in biophysical models gated the induction of sodium spikes and determined the integration mode (**Figure 3**). Using an array of different activation patterns, we found that spatially dispersed inputs lead to higher firing rates than inputs clustered within a few dendrites (**Figure 4**), opposite to respective findings in pyramidal neurons<sup>33</sup>. Moreover, these different activation patterns result in a wide range of firing rates that are better explained by a 2-layer Artificial Neural Network (ANN) with non-linear hidden layer activation functions rather than a linear ANN (**Figures 5, 6, Table 1**). Finally, in order to assess the functional implications of these predictions, we built a reduced network model<sup>41</sup> of 2-stage integrator neurons (**Figure 1D**) and showed that bi-modal nonlinear integration in FS BCs is beneficial for memory engram storage as well as the linking of memories across time (**Figure 7**).

This work provides a systematic, cross-area analysis of dendritic integration in FS BCs and its functional implications. Our findings challenge the current dogma, whereby interneurons are treated as linear summing devices, essentially void of dendrites. We predict that the dendrites of FS BCs in both Hippocampal and Neocortical regions can operate in distinct non-linear modes. As a result, FS BCs, similar to pyramidal neurons<sup>40</sup>, are better represented by a 2-stage integrator abstraction rather than a point neuron. Importantly, non-linear dendritic integration in these cells offers substantial advantages for memory encoding in large scale networks.

## RESULTS

## Multi-compartmental, biophysical models

A total of 8 biophysical model neurons were built using realistic reconstructions of FS BCs from rat hippocampal areas (5 cells) and from the prefrontal cortex of mice (3 cells) (Supplementary Figure 5). To ensure biological relevance, ionic and synaptic conductances as well as basic membrane properties of model cells were heavily validated against experimental data<sup>6,13,16,23</sup> (Supplementary Table 1-4, Supplementary Figures 1-3). Moreover, for consistency reasons, the same set of biophysical mechanisms (type and distribution) was used in all model cells.



**Figure 2:** Bimodal dendritic integration in multi-compartmental FS BC models. Examples of Hippocampal (a) and PFC (d) FS BC morphological reconstructions. Representative input-output curves from supralinear (b, e) and sublinear (c, f) dendritic branches in Hippocampal (top) and PFC (bottom) models, in response to synaptic stimulation. Increasing numbers of synapses (from 1 to 20 with step=1) are uniformly distributed within each stimulated branch and are activated with a single pulse. The y-axis shows the amplitude of the dendritic EPSP caused by synaptic activation while the x-axis shows the expected EPSP amplitude that would result from the linear summation of synaptic EPSPs. The dashed line indicates linear summation. Insets show representative traces.

## Bi-modal dendritic integration in Fast Spiking Basket cells

The first step for deducing a realistic abstraction of FS BCs is the systematic characterization of dendritic/neuronal integration properties across a significant number of neurons and dendrites. Towards this goal, we simulated gradually increasing excitatory synaptic input to the dendrites of all neuronal models and recorded the voltage response both locally and at the soma<sup>11,44</sup>. Increasing numbers of synapses (1-20) were uniformly distributed in each stimulated dendrite and activated synchronously with a single pulse. For this particular experiment, sodium conductances in somatic and axonal compartments were closed to avoid backpropagation contamination effects<sup>55,42</sup> that were detectable in some dendrites. We compared measured EPSPs to their linearly expected values, given by the number of activated inputs multiplied by the unitary EPSP. We found that within the same dendritic tree, branches summate inputs either in a supralinear or a sublinear mode (**Figure 2, supplementary Figures 4, 5**). While there were differences in the number of dendrites and proportions of sub- vs. supralinear dendrites, all of the morphologies tested expressed both integration modes (**Supplementary Table 5**). Moreover, while both modes have been suggested in distinct interneuron types<sup>11,38</sup>, their co-existence in the same tree has yet to be reported.

To assess the robustness of this finding, we first performed a sensitivity analysis whereby the cp-AMPA, NMDA, VGCCs, sodium and A-type potassium conductances were varied by  $\pm 20\%$  of their control value. We found no changes in the integration mode of dendrites (data not shown) and only insignificant alterations in the spike threshold of supralinear dendrites (**Supplementary Figure 6b**). The only manipulation that eliminated supralinearity was the blockade of dendritic sodium channels (**Supplementary Figure 7**).

Next, we examined whether the two modes are influenced by the presence of Gap junctions, which are well established in FS BCs<sup>46</sup>. Towards this goal, we connected pairs of Hippocampal and PFC cells with 10 electrical synapses (see **Online Methods**). Presynaptic cells were synaptically activated so as to fire at gamma rate frequency as per Tamas et al 2000<sup>46</sup> and the integration mode was assessed, as previously, in the dendrites of the post-synaptic cell. We found no influence of gap junctions on the integration mode, apart from a slightly increased membrane potential (**Supplementary Figure 8**).

The same effect was observed in simulations of more physiological conditions such as active whisking<sup>47</sup>. This was done via weak synaptic activation of randomly selected dendrites resulting in a somatic firing rate of  $3 \pm 1$  Hz<sup>47</sup> (see **Online Methods**). Both modes



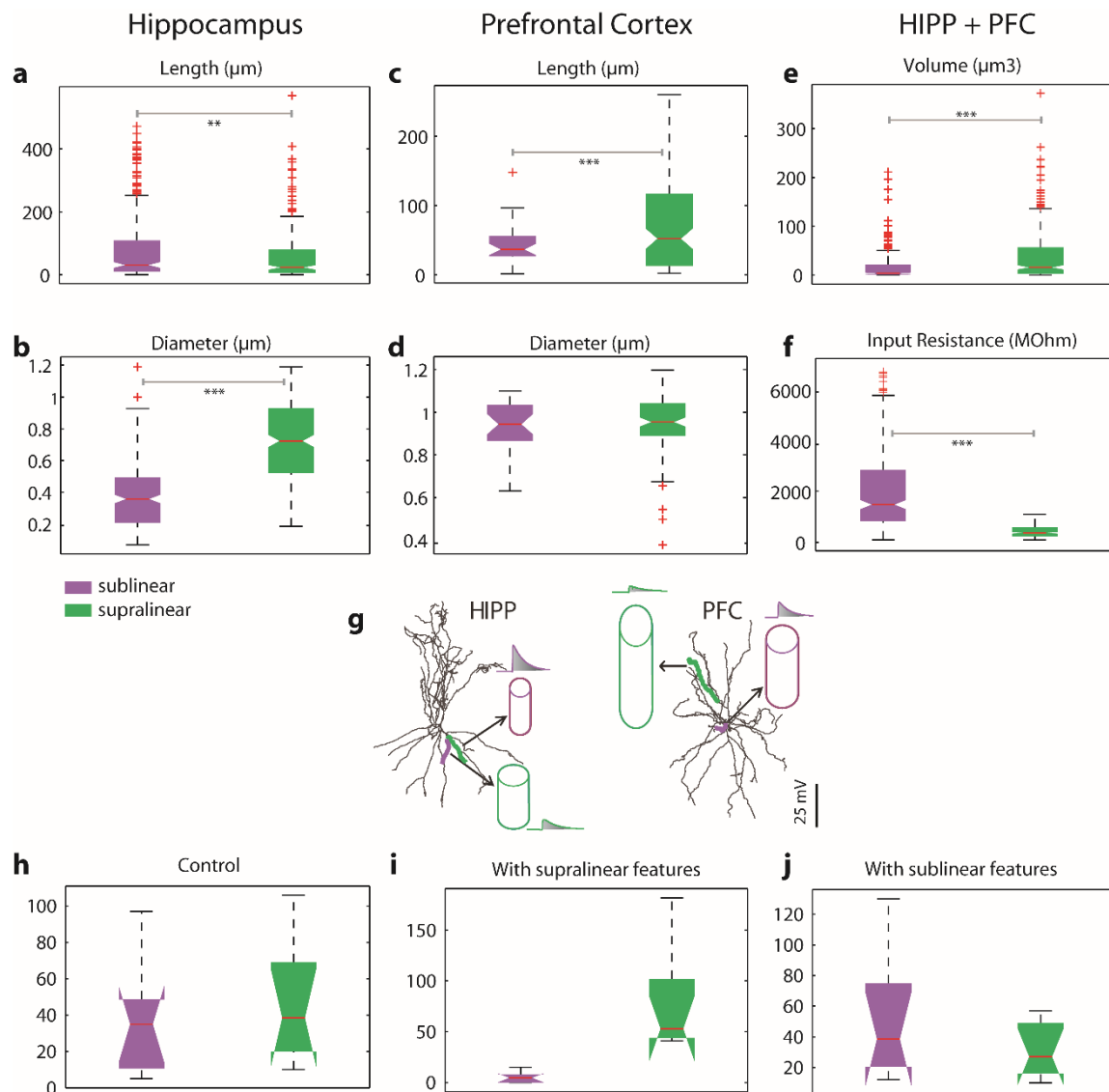
of dendritic integration remained unaffected by the presence of *in vivo* like activity fluctuations (**Supplementary Figure 9**).

Taken together, the above simulations establish the robustness of bi-modal dendritic integration and suggest that under physiological conditions, FS BCs are likely to express both types of dendritic integration modes.

## **Determinants of dendritic integration modes**

Next, we searched for biophysical and/or anatomical determinants of the two integration modes. Blockade of sodium conductances in the dendrites eliminated the supralinear integration mode in all morphologies tested (**Supplementary Figure 7**), but this was not the case for blockade of cp-AMPA, NMDA, VGCCs or A-type potassium channels. (**Supplementary Figure 6a**). These simulations indicate that sodium channels are the key ionic mechanism underlying the supralinear mode. What remains unclear is why these model cells also have sublinear dendrites, when the distribution and conductance values of sodium channels is the same in all dendrites.

Since morphological features of dendrites were previously shown to influence synaptic integration profiles<sup>36</sup>, we investigated whether anatomical features correlate with the expression of each integration mode. We found that the mean dendritic diameter was highly statistically different (p-value=2.6041e-60) among sub-(thinner) and supra-linear (thicker) dendrites in the hippocampus (**Figure 3b**) while in the PFC the dendritic length was a better determinant of sub- (shorter) vs. supra-linearity (longer) (p-value=4.1768e-04) (**Figure 3c**). Length was less, yet, important in the hippocampus (p-value=0.0040) (**Figure 3a**) while diameter was not different among sub- and supralinear dendrites in the PFC (p-value=0.9458) (**Figure 3d**). Dendritic volume and input resistance consider both of the above anatomical features and serve as robust morphological / electrophysiological determinants for all dendrites in both areas (p-value=9.8516e-11, 3.9457e-45 respectively), (**Figure 3e,3f**).



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**Figure 3: Morphological determinants of dendritic integration mode.** **a, c:** Total length distributions of supralinear vs. sublinear dendrites in the hippocampus (**a**) and the PFC (**c**). Statistically significant differences are observed for both sub- and supra-linear dendrites, in both areas. (p-value<0.0001 for Hippocampus and p-value<0.01 for PFC). **b, d:** Same as in **a, b**, for mean dendritic diameter. Statistically significant differences are observed in Hippocampal (p-value<0.0001) but not in PFC FS BCs. **e-f.** Dendritic Volume and dendritic Input Resistance are common discriminating characteristics among supralinear (larger, with low input resistance) and sublinear (smaller, with high input resistance) dendrites, for both areas (p-value<0.0001 for Hippocampus and PFC, for volume and Input Resistance respectively). **g.** Schematic illustration of morphological features for supralinear and sublinear dendrites in Hippocampus (left) and PFC (right). Traces indicate first EPSP in supralinear and sublinear dendrites. **h-j.** Distributions of the number of supralinear and sublinear dendrites in both areas, under control conditions (**h**), with the mean diameter and length



196 of all dendrites set to the mean values of the supralinear class (i) and with mean diameter and length  
197 of all dendrites set to the mean values of the sublinear class (j).

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199 Overall, we found that supralinear dendrites have high volume and low input resistance  
200 while sublinear dendrites have smaller volume and high input resistance (**Figure 3e, 3f**).  
201 This can be explained by considering the fast kinetics of cp-AMPA receptors and A-type  
202 potassium channels in the dendrites of FS BCs. In sublinear dendrites, where the input  
203 resistance is high (small volume), coincident synaptic input induces a large, fast rising EPSP  
204 which in turn strongly activates the A-type potassium channels that rapidly repolarize the  
205 membrane, thus preventing the branch from spiking<sup>12</sup>. The opposite is true for supralinear  
206 dendrites, where the low input resistance results in smaller depolarizations that drive smaller  
207 A-type potassium currents, enabling the branch to reach the sodium spike threshold. This  
208 explanation is consistent with prior findings<sup>2,6,42,12</sup>.

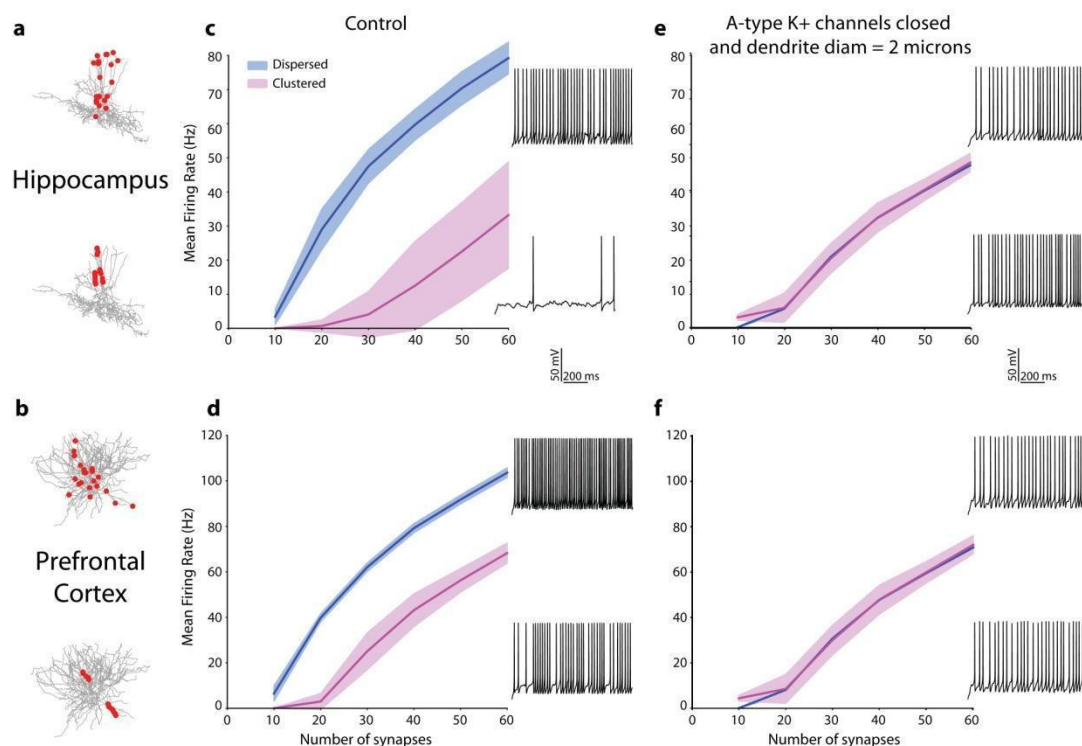
209 To test the above proposition, we performed causal manipulations whereby we fixed the  
210 diameter and length of all dendrites to the mean values of first the supralinear and then the  
211 sublinear class and assessed the effect on integration mode. We found that setting the  
212 dendritic anatomy to that of a given class also dictated the integration mode (**Figure 3h-j**).  
213 These findings suggest that, under the experimentally constrained conductance values for  
214 sodium channels, morphology plays a crucial role in the ability of a given dendrite to  
215 support local sodium spikes and express the supralinear integration mode.

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## 217 **Effect of bimodal dendritic integration on neuronal firing**

218 To assess the impact of bi-modal dendritic integration on neuronal output, we simulated a  
219 large variety of different spatial patterns of synaptic activation and measured the resulting  
220 firing rates. Specifically, we generated over 10,000 synaptic stimulus patterns, which  
221 comprised of increasing numbers of excitatory synapses. Synapses were either placed  
222 within a few, strongly activated branches (clustered) or they were randomly distributed  
223 within the entire dendritic tree (dispersed). In all cases, synapses were activated with  
224 random Poisson spike trains at 50 Hz (see **Online Methods**). Dendrites were selected at  
225 random and inputs were distributed uniformly within selected dendrites. For the dispersed  
226 case, we allocated 2, 5, or 10 synapses in randomly selected dendrites, one at a time, while

for the clustered case we allocated 10,15,20,30,60 synapses within an increasing number of branches. In all cases, the number of activated synapses increased gradually up to a maximum of 60, as this number was sufficient to induce spiking at gamma frequencies (30-100 Hz). This process was repeated  $k$  times ( $k$  = number of dendrites in each cell) to ensure full coverage of the entire tree. As expected given the two modes of dendritic integration, the localization of activated inputs affected neuronal firing. For a given number of activated synapses, dispersed activation led to *higher* somatic firing rates than clustered activation, particularly during gamma related frequencies (30-100 Hz) both in Hippocampal (**Figure 4c**) as well as in PFC FS basket cells (**Figure 4d**). Interestingly, this finding is opposite to what has been reported for pyramidal neurons, in which synapse clustering increases firing rates<sup>33</sup>.



**Figure 4:** Effect of bimodal dendritic integration on neuronal firing. Firing rate responses (in Hz) from one Hippocampal (a,c) and one PFC (b,d) model cell, in response to stimulation of increasing numbers of synapses (10 to 60) that are either randomly distributed throughout the entire dendritic tree (blue) or clustered within a few dendritic branches (pink). Synapses are stimulated with a 50 Hz Poisson spike train. In both cases, dispersed activation leads to higher firing rates. e,f: Same as in c,d with dendritic diameter set to 2 microns and removal of A-type dendritic channels. Firing rates are indistinguishable between clustered and dispersed activation patterns. Insets depict representative traces from dispersed (top) and clustered (bottom) activation of 30 synapses. Red dots in show the synaptic allocation motif in a, b.

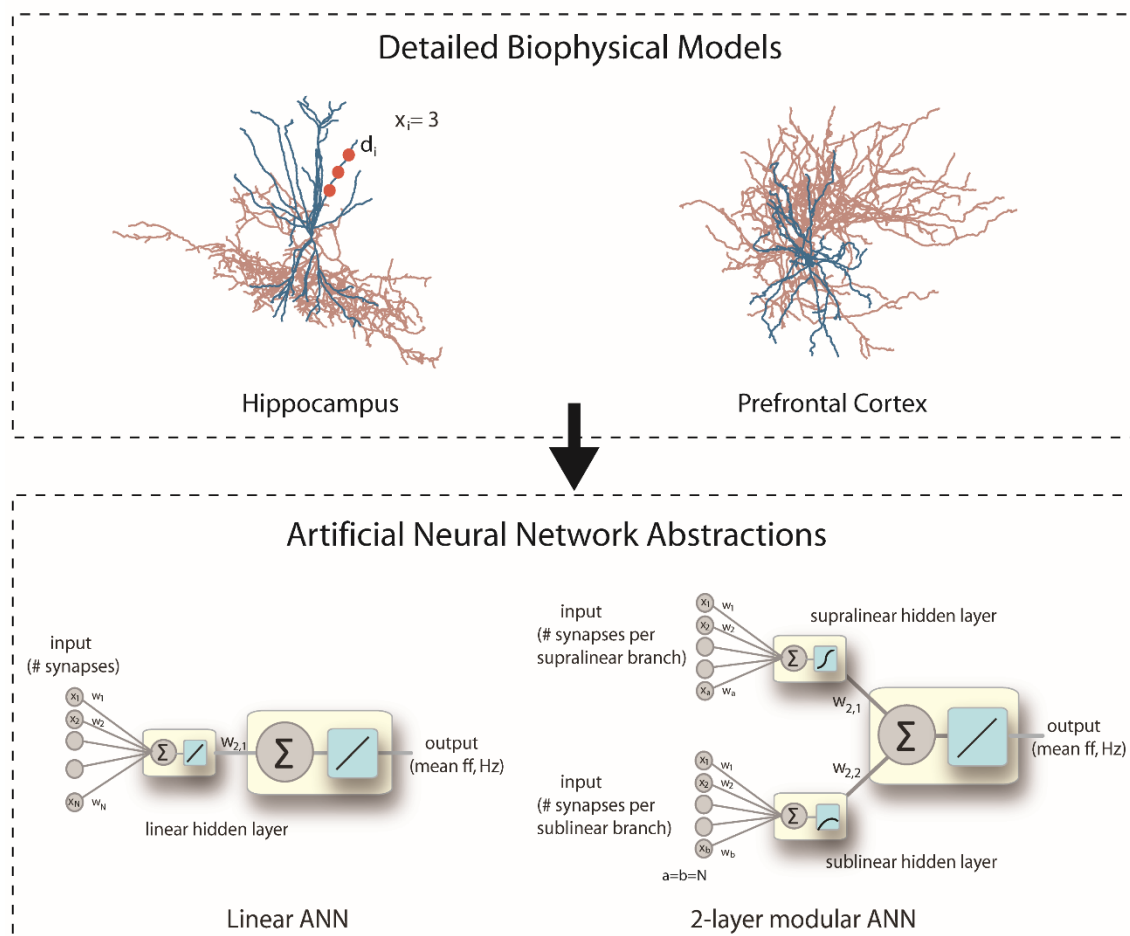
249 It was previously proposed that the combination of a small diameter with an increased  
250 conductance of A-type potassium channels in FS BCs underlies the preference for dispersed  
251 synaptic allocationions<sup>6</sup>. To tests this hypothesis, we repeated the above experiment after  
252 increasing the diameter (to 2 microns) and blocking the A-type potassium conductance in  
253 all dendrites. As shown in **Figure 4e-f**, this manipulation resulted in very similar firing rates  
254 irrespectively of the spatial arrangement of synapses, thus eliminating the preference for  
255 dispersed allocation of excitatory inputs.

256 **Supplementary Figure 12** shows the relative contributions of these two mechanisms in our  
257 model cells. Disperse synaptic arrangements benefit mostly from the dendritic morphology  
258 of FS BCs, as setting the dendritic diameter to 2 microns sharply decreases this preference  
259 (**Suppl. Fig. 12 a, b**). This is likely because small diameters prevent signal loss, enabling  
260 the small depolarizations produced by dispersed inputs to reach and excite the soma.  
261 Clustered arrangements on the other hand, are severely hampered by the high conductance  
262 of the A-type potassium channels<sup>24</sup>, as blockade of these currents enhances somatic output  
263 (**Suppl. Fig. 12 c, d**). This is because clustered -but not disperse- inputs induce large  
264 dendritic depolarizations which strongly activate A-type channels. Since NMDA currents<sup>7</sup>,  
265 which would further boost and prolong the cluster-induced EPSPs, are very small in these  
266 neurons, the hyperpolarizing effects of the A-type currents are larger than the depolarizing  
267 effects of clustered activation.

268 Another factor that contributes to disperse preference, is dendritic integration. Unlike  
269 pyramidal neurons where dendrites are mostly supralinear and benefit from clustered inputs  
270 via the induction of dendritic spikes<sup>31,35,40</sup>, these neurons also have sublinear dendrites  
271 which dampen the abovementioned benefit. The higher the percentage of sublinear  
272 dendrites, the larger the dampening, as: 1) the probability of allocating clustered inputs in  
273 the few supralinear dendrites is much smaller and 2) activating sublinear dendrites with  
274 clustered inputs offers little/no advantage as dendritic spikes don't occur in these branches.  
275 As shown in **Supplementary Table 7** the more sublinear dendrites a FS BC model has, the  
276 weaker the response to clustered input.

277 Taken together, this analysis reveals that the combination of a high conductance of A-type  
278 channels (which penalizes clustering), the specific morphological features of FS BCs  
279 (which favor dispersed inputs), and the presence of multiple sublinear dendrites underlie

the preference of these cells for disperse rather than clustered activation of their inputs,  
contrary to pyramidal neurons<sup>40</sup>.



**Figure 5:** Reduction of multi-compartmental models into ANN abstractions. Two types of abstractions are examined: **a)** a Linear ANN, in which the input from all dendrites ( $x_i$ =number of synapses in dendrite  $i$ ,  $N$ =number of dendrites) is linearly combined at the cell body and **b)** a 2-layer modular ANN, in which the input is fed into two parallel, separated hidden layers. The supralinear-layer receives the number of inputs landing onto supralinear branches ( $a$ =number of supralinear dendrites) while the sublinear layer receives the number of inputs landing onto sublinear dendrites ( $b$ =number of sublinear dendrites). Neurons in both hidden layers are equipped with nonlinear transfer functions, a logistic sigmoid in the supralinear layer and a sublinear function in the sublinear layer. The somatic transfer functions of both ANNs are linear.

### FS basket cells as 2-layer artificial neural networks

The non-linear synaptic integration taking place within the dendrites of cortical<sup>48</sup> and CA1<sup>35,44</sup> pyramidal neurons was previously described as a sigmoidal transfer function<sup>49</sup>. Based on this reduction, a single pyramidal neuron was proposed to integrate its synaptic

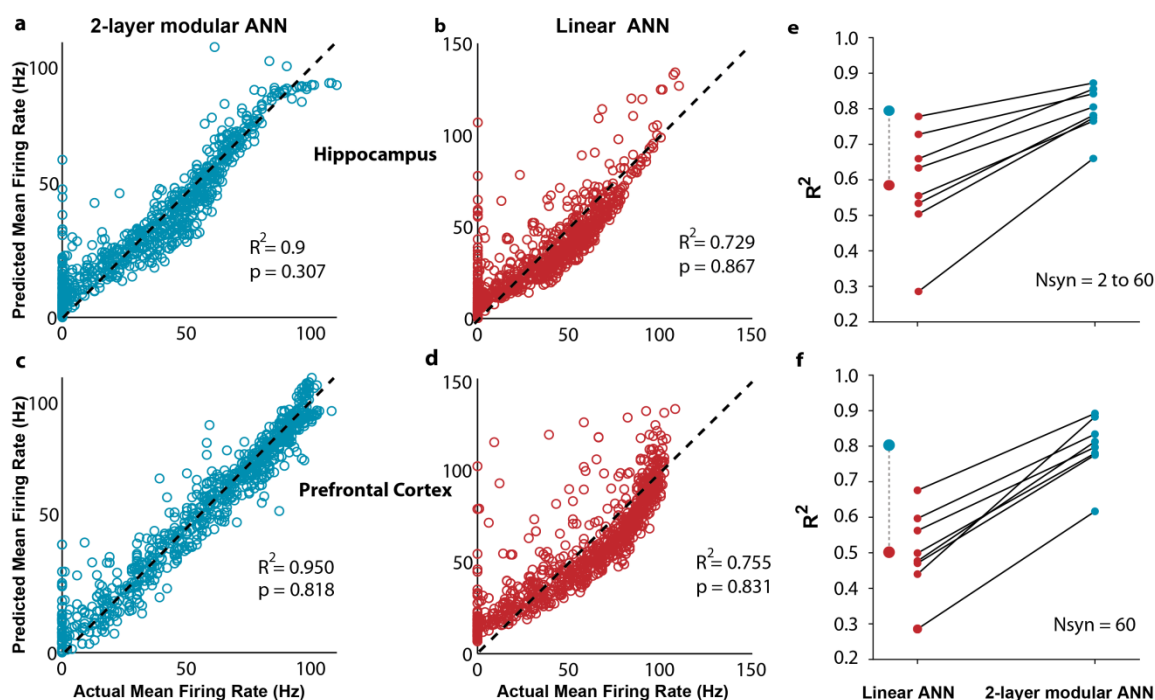
inputs like a 2-layer artificial neural network, where dendrites provide the hidden layer and the soma/axon the output layer<sup>40</sup>. To assess whether a similar mathematical formalism could be ascribed to FS BC models, we constructed linear and non-linear artificial neural networks (as graphically illustrated in **Figure 5**) and asked which of them can better capture the firing rate variability in the biophysical models.

Specifically, four types of feedforward, backpropagation Artificial Neural Networks (ANNs) were constructed (see **Online Methods**). In the *2-layer modular ANN*, supralinear and sublinear dendrites were simulated as 2 parallel hidden layers consisting of a logistic sigmoid and a sublinear activation function  $y(x) = (x+2)^{0.7}-2$ , respectively<sup>49</sup> (**Figure 5**). The number of activated synapses allocated to supralinear vs. sublinear dendrites in the biophysical models was used as input to the respective hidden layers. The output layer represented the soma/axon of the biophysical model and consisted of a linear activation function. In the *linear ANN*, there was only a single hidden layer receiving input from all dendrites and consisting of linear activation functions (**Figure 5**). We also constructed two ANNs with the exact same architecture as the linear one, but with either a) a logistic sigmoidal (*2-layer supralinear ANN*) or b) a sublinear  $y(x) = (x+2)^{0.7}-2$  (*2-layer sublinear ANN*) activation function in the hidden layer neurons (**Supplementary Figure 10**). These ANNs represent FS BCs with just one type of non-linear dendrites.

For all 8 FS BC model neurons the *linear* and *2-layer modular ANNs* were trained using the number of synapses to supra-/sublinear dendrites as inputs to the respective hidden layers and the mean firing rate of the soma as target output. A randomly selected 80% of our synaptic activation data set was used to train the model and the rest 20% to test its generalization performance (see **Online Methods**). Performance accuracy was estimated based on regression analysis between the ANN-generated firing rates and those produced by the biophysical models. Fits for two representative model cells are shown in **Figure 6a-d**, while the overall performance for all 8 model cells is shown in **Figure 6e**. **Figure 6f** demonstrates the performance of both ANN types for a dataset of the same power (number of inputs = 60), whereby the location of the inputs varies. As evident from the results, the *2-layer modular ANN* outperformed the *linear ANN* in all cases tested.

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**Figure 6:** Challenging the point neuron dogma: FS basket cells as 2-stage nonlinear integrators. Linear regression analysis for 2-layer modular (a, c) and linear (b, d) ANNs for one indicative Hippocampal (top) and one indicative PFC (bottom) model cell. Actual Mean Firing Rates (Hz) correspond to the responses of the compartmental model when stimulating with 50Hz Poisson spike trains- varying numbers of synapses (1 to 60), distributed in several ways (clustered or dispersed) within both sub- and supra-linear dendrites. Expected Mean Firing Rates (Hz) are those produced by the respective ANN abstraction when receiving the same input (number of stimulated synapses) in its respective sub-/supra- or linear input layer nodes. e) Regression performance (measured as  $R^2$ ) for 2-layer modular (right) and Linear (left) ANNs for all 8 FS BC model cells respectively. In all cases the 2-layer modular ANNs is superior to the Linear ANNs. Mean  $R^2$  values over all cells for the Linear (red) and 2-layer modular (cyan) ANNs are shown in the right. f) Same as e), applied to datasets comprised of 60 input synapses. The difference in performance of the two ANN types is higher in this challenging task.

However, the performance of the *linear ANN* was relatively good. This can be attributed to the wide range of activated synapses (2 to 60) which resulted in large differences in the somatic firing, irrespectively of synapse location, and can thus be captured by any linear model (also see the work of Poirazi et al 2003b)<sup>40</sup>. Therefore, we also assessed the performance accuracy of *linear* and *2-layer modular ANNs* to the more challenging task of discriminating between input distributions corresponding to the exact same number of



synapses. To do so, we subdivided the data into input categories corresponding to 20, 40 and 60 synapses, respectively. In these more challenging conditions, the *2-layer modular ANN* clearly outperformed the respective *linear ANN*, which failed to explain the variance produced by differences in input location. This result was consistent for all model cells as shown in **Table 1**. Performance for the 60-synapse case is shown in **figure 6f**.

<b>Table 1. ANN regression performance (<math>R^2</math>) for individual sets of synapses in the 8 model cells</b>			
ANN type	20 synapses	40 synapses	60 synapses
2-layer modular ANN	0.8224	0.7432	0.6167
	0.8228	0.9060	0.8339
	0.8048	0.8709	0.7971
	0.7951	0.8563	0.8127
	0.8242	0.8352	0.7752
	0.9098	0.8857	0.8921
	0.8879	0.8975	0.8827
	0.8415	0.8600	0.7801
Linear ANN	0.4541	0.3484	0.2856
	0.6814	0.7462	0.5966
	0.6436	0.5201	0.5625
	0.5636	0.4475	0.4768
	0.5550	0.4919	0.4707
	0.7832	0.7242	0.6758
	0.6263	0.5463	0.4400
	0.6179	0.7039	0.4991

**Table 1:** Comparison of ANN prediction accuracy (measured as the  $R^2$ ) for linear and 2-layer modular ANN reductions across all 8 FS BC models, tested on three sets of synaptic inputs consisting of 20, 40 or 60 activated synapses, respectively. Synapses were randomly distributed in various ways/locations in the biophysical model cells and resulting firing rates were used as target vectors for the ANNs. The 2-layer modular ANN is clearly superior to the Linear ANN when it comes to capturing location-induced firing-rate variability.

Taken together, this analysis suggests that a 2-layer artificial neural network that considers both types of dendritic non-linearities is a much better mathematical abstraction for FS basket cells than the currently assumed linear point neuron.

### **Bimodal nonlinear integration of FS basket cells enhances memory encoding**

In order to investigate the functional implications of our findings, we built a canonical microcircuit network model<sup>41</sup> composed of simplified 2-stage excitatory neurons, FS BCs and dendrite targeting (SOM+) interneurons (**Figures 1d and Supplementary Table 6**). The model includes inhibitory feedback connectivity, multi-dendrite and perisomatic interneurons. It implements plasticity-related processes which act on multiple temporal and

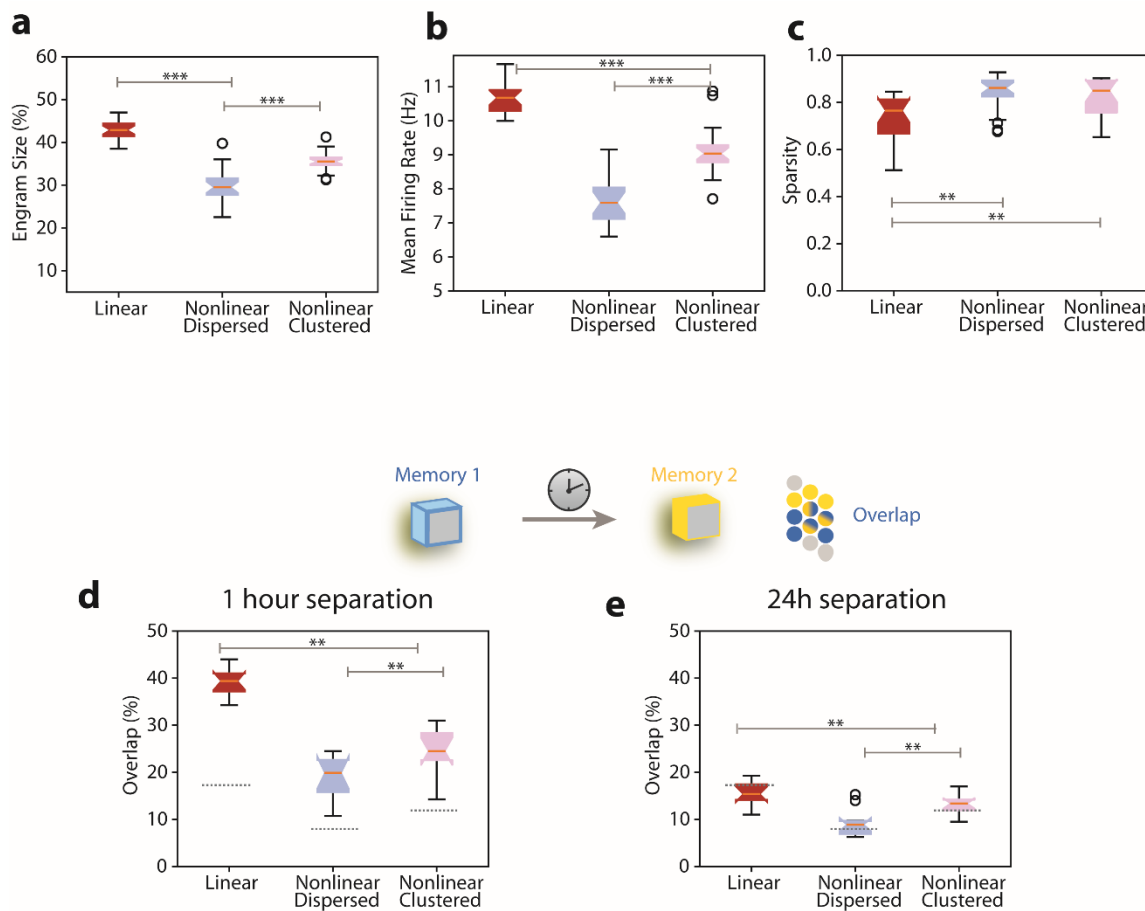


369 spatial scales: two-stage dendritic integration, dendritic calcium dynamics, synaptic tagging  
370 and capture (STC), CREB-dependent excitability and homeostasis (see **Online Methods**).

371 The network model was first trained to encode a single memory<sup>41</sup> (see **Online Methods**)  
372 using FS BCs with either a) purely linear or b) bi-modal (sublinear and supralinear)  
373 dendritic subunits, as predicted by the compartmental modeling analysis (**Figure 2**). SOM+  
374 interneurons were modeled as having either sublinear, linear, supralinear, or bi-modal  
375 dendritic subunits (**Supplementary Figure 11**). In these simulations, synaptic inputs to the  
376 FS BCs cells were either a) randomly distributed in all dendrites (Dispersed) or b) clustered  
377 within 33% of all dendrites (Clustered) (see **Online Methods**). The properties of the  
378 resulting memory engram (*i.e.* the population of active excitatory neurons during recall)  
379 were assessed by analyzing the activity of excitatory neurons during recall 24 hours after  
380 the learning event (**Figure 7e**).

381 Our results indicate that, compared to linear dendrites, bi-modal FS BCs dendrites lead to  
382 significant reductions in the size of the resulting memory engram (p-value=5.8e-15), and  
383 the mean engram firing rates (p-value=3.1e-18 linear-dispersed, p-value=7.2e-10 linear-  
384 clustered) (**Figure 7a,b**) while they also increase the network firing sparsity (p-  
385 value=0.00095 linear-disperse, p-value =0.00338 linear-clustered) (**Figure 7c**). All of the  
386 above suggest that dendritic bi-modality in FS BCs promotes resource savings in the

387 encoding of new memories.



388

389 **Figure 7:** Properties of memory engram encoding under different dendritic nonlinearity  
390 configurations, using the circuit model depicted in Figure 1d. **a)** Size of memory engram (percentage  
391 of excitatory neurons that respond with  $ff > 10\text{Hz}$  during memory recall) for Linear/Bi-modal FS-BC  
392 dendritic subunits receiving dispersed (blue) or clustered (pink) synaptic inputs. **b)** Mean firing rate  
393 of the excitatory population under the conditions enumerated in **(a)**. **c)** Treves-Rolls sparsity metric  
394 of the excitatory population firing rates under the conditions enumerated in **(a)**. **d)** Percentage of  
395 overlap between two memory engrams when 2 memories are separated by 1 hour, under the  
396 conditions enumerated in **(B)**. Dashed lines indicate the chance level of overlap for the engram sizes  
397 of the dispersed case shown in **(a)**. **e)** As in **(d)** for 24 hours separation. Box plots indicate data from  
398 20 simulation trials for A-D, and 10 trials for E-F. \*\*:  $p < 0.05$ , \*\*\*  $p < 0.005$ .

399 As predicted by our multi-compartmental models (**Figure 4**), we found that dispersed  
400 synaptic activation is beneficial to engram properties by further reducing the engram size  
401 ( $p\text{-value}=4.0\text{e-}6$ ) and the mean firing rate ( $p\text{-value}=1.7\text{e-}7$ ) (**Figure 7a-b**). Summarizing,  
402 the memory engram properties indicate that bi-modal FS BC dendrites receiving dispersed  
403 inputs confer resource consumption advantages to memory encoding by a) increasing the  
404 sparsity of the population, b) recruiting fewer engram neurons and c) reducing the overall

network excitability. The above findings were unaffected by the presence of either linear, supralinear or bi-modal SOM+ model dendrites (**Supplementary Figure 11**).

Finally, we also assessed the role of FS-BC nonlinearities in memory linking, by encoding two memories separated by 1 or 24 hours in the same network model and measuring the population overlap of the resulting memory engrams. According to previous work<sup>33,41,50</sup>, memories learned in close temporal proximity (e.g. 1 hour apart) display increased engram overlap compared to distant memories (24 hours apart). Overlapping storage is also associated with behavioral binding of the two memories and has been proposed to underlie the linking of memories across time<sup>51</sup>. We found that linear FS BC dendrites result in substantially larger engram overlaps in the circuit model compared to bi-modal dendrites (**Figure 7d**), for the 1-hour case. These overlaps are in fact significantly larger than the experimentally reported ones<sup>50</sup> (~20%), suggesting that the two memories may interfere with one another. Taken together, our network modeling analysis suggests a beneficial role of nonlinear dendrites in FS BCs with respect to memory encoding, storage capacity as well as the binding of memories over time.

## DISCUSSION

The role of dendrites in interneuron computations is a rapidly emerging and debatable subject<sup>52</sup>. Several recent reports present exciting findings according to which dendrites may serve as key players<sup>2,11,37,38,53</sup>. For example, sodium spikes and supralinear calcium accumulation have recently been reported in the dendrites of FS BCs<sup>2</sup>, yet the consensus still favors the linear point neuron dogma<sup>6,45,52</sup>. The present study provides new insight into this ongoing debate by systematically analyzing the dendritic integration mode of FS BCs in two brain areas: The Hippocampus and the PFC. We do so using an extensive set of computational tools that extends from detailed biophysical single cell models, to reduced integrate-and-fire single cell and circuit models as well as artificial neural network models (**Figure 1**). We predict that dendrites of both cortical and hippocampal FS BCs operate in one of two modes of synaptic integration: supralinear or sublinear (**Figure 2**). Supralinearity is due to the generation of dendritic sodium spikes (**Supplementary Figures 7**), which are in turn gated by the morphology (**Figure 3**) of dendrites. Moreover, we find that somatic output is influenced by the spatial distribution of activated synapses, with dispersed input inducing higher firing rates than clustered activation. This feature is opposite to pyramidal

neurons<sup>40</sup> and is attributed to a) the presence of sublinear dendrites in FS BCs and b) the small dendritic diameter, increased A-type current and fast EPSP kinetics of cp-AMPA receptors found in these cells<sup>6</sup> (**Figure 4, Supplementary Figure 12**). Due to these properties, a 2-layer modular Artificial Neural Network abstraction with both sub- and supra-linear hidden neurons (**Figure 5**) captures the spiking profile of biophysical neurons with much higher accuracy than a linear ANN, analogous to a point neuron. This is true for all of the 8 morphological reconstructions of FS BCs tested and is more evident for datasets in which the number of inputs is fixed but their location varies (**Figure 6, Table 1**). This is because discriminating the effect of input location as opposed to input strength is a much more challenging task and pushed the linear ANN to its performance limits. Finally, we show that such a 2-stage integration model facilitates the efficient encoding, storage and discriminability of memories in a biologically relevant circuit model across time (**Figure 7**).

450

#### 451 **Mediators of supralinear and sublinear dendritic integration in FS basket cells**

A bimodal dendritic integration is predicted for all hippocampal and PFC morphologies analyzed. Supralinearity was found to be due to the occurrence of dendritic sodium spikes (**Supplementary Figure 7**). Several mechanisms can influence the generation of such dendritic spikes: ionic conductances (primarily of sodium currents but also potassium currents) and morphological features. In our models, biophysical mechanisms are constrained by existing experimental data and dendritic sodium conductances are kept to a minimum (10 times smaller than the soma<sup>6</sup>), so as to minimize the probability of non-physiological dendritic spiking. Sensitivity analysis further demonstrates that results are robust to physiological variations in a wide range of active dendritic conductances (**Supplementary Figure 6**). These findings strongly suggest that dendritic spiking in certain dendrites of FS basket cells are highly likely to occur under physiological conditions, in line with recent experimental reports<sup>2</sup>.

Apart from sodium currents as a universal enabling mechanism, we find a key role of morphology in gating local dendritic spikes. A combination of dendritic length and mean diameter, or otherwise the dendritic volume and input resistance, is statistically different between sub- (smaller) and supralinear (larger) dendrites across all morphologies tested (**Figure 3**). The inability of small-volume dendrites (**Figure 3F**) to support sodium spikes

is attributed to their high input resistance (**Figure 3F**), fast kinetics of calcium permeable AMPA receptors and the high density of A-type potassium channels<sup>6,12</sup>. This combination results in large, fast EPSPs that are very efficient in activating  $I_A$  currents, which in turn repolarize the membrane<sup>6,12</sup>. This mechanism has been previously proposed by others<sup>6,12,42</sup>, is supported by our morphology and  $I_A$  manipulation experiments (**Figure 4**) and is in line with other studies reporting a similar effect of morphology on the ability of dendrites to generate local spikes<sup>36</sup>.

#### **Functional coexistence of sub- and supra-linear dendrites within FS basket cells**

Our simulations predict the co-existence of both sublinear and supralinear dendrites in all FS BCs models (**Figure 2, Supplementary Figures 4-9**). Similar bimodal dendritic integration has been reported in hippocampal CA1 pyramidal neurons<sup>35,44</sup> and predicted in PFC pyramidal neurons<sup>48</sup>.

The existence of sublinear dendritic branches supports the idea of inhibitory neurons acting as coincidence detectors by aggregating spatially disperse and nearly synchronous synaptic inputs<sup>6</sup>. Moreover, sublinear dendrites can compute complex non-linear functions similar to those computed by sigmoidal dendrites<sup>49</sup>, thus substantially extending the processing capacity of these neurons compared to a linear integrator. Why have two types of nonlinearity then?

Our network modeling predicts that the presence of both types of nonlinearities confer substantial benefits to network computations and especially to memory encoding. We find that bimodal nonlinearities in the dendrites of FS BCs, enables the encoding of new memories within a smaller neuronal population, thus increasing sparsity and storage capacity. These nonlinearities also facilitate the interaction of memories over time, via decreasing the possibility of interference (**Figure 7**).

#### **Not that Simple: FS basket cells as 2-layer modular ANNs**

Artificial Neural Network analysis demonstrates that a FS basket cell is better described by a 2-stage abstraction that incorporates both modes of dendritic integration (**Figure 5,6**). This work, along the lines of the 2-stage model proposed for pyramidal neurons<sup>40</sup>, strongly challenges the prevailing point neuron dogma. The 2-stage abstraction is supported by

experimental reports of dendritic sodium spikes and supralinear calcium accumulations<sup>2</sup> while it also explains sublinear dendritic integration<sup>6,11,29,55</sup>, providing a unifying framework for interneuron processing.

Possible limitations of our work include the imprecise modeling of ionic and synaptic mechanisms given the shortage of sufficient information for FS BCs models. This limitation is counteracted by the sensitivity analysis of the mechanisms that mostly influence our findings and their consistency across several cortical and hippocampal morphologies. Another limitation is the lack of inhibitory inputs (except from the autaptic GABA<sub>A</sub> current that is incorporated in all models). Inhibitory inputs consist of just 6% of all incoming contacts in Fast Spiking interneurons<sup>6,56,57</sup>. Thus, our results are unlikely to be affected by inhibitory inputs. FS basket cells in the hippocampus and the neocortex are highly interconnected by gap junctions<sup>6</sup>, that can speed the EPSP time course, boost the efficacy of distal inputs and increase the average action potential frequency after repetitive synaptic activation<sup>6</sup>. All of these effects would contribute to stronger responses but unless gap junctions are spatially specific to certain branches and not others, they are unlikely to influence the non-linear integration modes of dendrites.

## Conclusion

This work provides a novel view of dendritic integration in FS basket cells, that extends in hippocampal and cortical areas<sup>41</sup>. Here we suggest new reductionist models for interneuron processing, in which dendrites play a crucial role. Experimental validation of these new models is likely to change the way we think about interneuron processing, attribute new and exciting roles to FS basket cells and open new avenues for understanding interneuron contributions to brain function.

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530

## 531 **AUTHOR CONTRIBUTIONS**

532 AT and PP designed the experiments. AT and GK performed the simulations and analyzed  
533 the data. AT and PP wrote the manuscript. All authors edited the manuscript. PP supervised  
534 the work.

## 535 **COMPETING FINANCIAL INTERESTS**

536 The authors declare no competing financial interests.

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## 539 References

- 540 1. Buzsáki, G., Geisler, C., Henze, D. A. & Wang, X.-J. Interneuron Diversity series:  
541 Circuit complexity and axon wiring economy of cortical interneurons. *Trends*  
542 *Neurosci.* **27**, 186–193 (2004).
- 543 2. Chiovini, B. *et al.* Marti. *Neuron* **82**, 908–924 (2014).
- 544 3. Freund, T. F. Interneuron Diversity series: Rhythm and mood in perisomatic  
545 inhibition. *Trends in Neurosciences* (2003). doi:10.1016/S0166-2236(03)00227-3
- 546 4. Kann, O. The interneuron energy hypothesis: Implications for brain disease.  
547 *Neurobiol. Dis.* **90**, 75–85 (2016).
- 548 5. Tremblay, R., Lee, S. & Rudy, B. GABAergic Interneurons in the Neocortex:  
549 From Cellular Properties to Circuits. *Neuron* **91**, 260–292 (2016).
- 550 6. Hu, H., Gan, J. & Jonas, P. Interneurons. Fast-spiking, parvalbumin<sup>+</sup> GABAergic  
551 interneurons: from cellular design to microcircuit function. *Science* **345**, 1255263  
552 (2014).
- 553 7. Klausberger, T. & Somogyi, P. Neuronal Diversity and Temporal Dynamics: The  
554 Unity of Hippocampal Circuit Operations. *Science (80-. ).* **321**, (2008).
- 555 8. Van Aerde, K. I. *et al.* Flexible spike timing of layer 5 neurons during dynamic  
556 beta oscillation shifts in rat prefrontal cortex. *J. Physiol.* **587**, 5177–5196 (2009).
- 557 9. Averkin, R. G., Szemenyei, V., Bordé, S. & Tamás, G. Identified Cellular  
558 Correlates of Neocortical Ripple and High-Gamma Oscillations during Spindles  
559 of Natural Sleep. *Neuron* (2016). doi:10.1016/j.neuron.2016.09.032
- 560 10. Somogyi, P. & Klausberger, T. Defined types of cortical interneurone structure  
561 space and spike timing in the hippocampus. *J. Physiol.* **562**, 9–26 (2005).
- 562 11. Abrahamsson, T., Cathala, L., Matsui, K., Shigemoto, R. & DiGregorio, D. A.  
563 Thin Dendrites of Cerebellar Interneurons Confer Sublinear Synaptic Integration  
564 and a Gradient of Short-Term Plasticity. *Neuron* **73**, 1159–1172 (2012).
- 565 12. Nörenberg, A., Hu, H., Vida, I., Bartos, M. & Jonas, P. Distinct nonuniform cable  
566 properties optimize rapid and efficient activation of fast-spiking GABAergic

- interneurons. *Proc. Natl. Acad. Sci. U. S. A.* **107**, 894–9 (2010).
13. Freund, T. F. & Katona, I. Perisomatic Inhibition. *Neuron* (2007).  
doi:10.1016/j.neuron.2007.09.012
14. Lee, S.-H. *et al.* Parvalbumin-Positive Basket Cells Differentiate among  
Hippocampal Pyramidal Cells. *Neuron* **82**, 1129–1144 (2014).
15. Povysheva, N. V *et al.* Parvalbumin-positive basket interneurons in monkey and  
rat prefrontal cortex. *J. Neurophysiol.* **100**, 2348–60 (2008).
16. Hioki, H. *et al.* Cell type-specific inhibitory inputs to dendritic and somatic  
compartments of parvalbumin-expressing neocortical interneuron. *J. Neurosci.* **33**,  
544–55 (2013).
17. Hainmüller, T., Kriegstein, K., Kulik, A. & Bartos, M. Joint CP-AMPA and  
group I mGlu receptor activation is required for synaptic plasticity in dentate  
gyrus fast-spiking interneurons. *Proc. Natl. Acad. Sci. U. S. A.* **111**, 13211–6  
(2014).
18. Geiger, J. R. P. *et al.* Relative abundance of subunit mRNAs determines gating  
and Ca<sup>2+</sup> permeability of AMPA receptors in principal neurons and interneurons  
in rat CNS. *Neuron* **15**, 193–204 (1995).
19. Goldberg, J. H. *et al.* Calcium Microdomains in Aspiny Dendrites. *Neuron* **40**,  
807–821 (2003).
20. Wang, H.-X. & Gao, W.-J. Cell type-specific development of NMDA receptors in  
the interneurons of rat prefrontal cortex. *Neuropsychopharmacology* **34**, 2028–40  
(2009).
21. Goldberg, J. H., Yuste, R. & Tamas, G. Ca<sup>2+</sup> imaging of mouse neocortical  
interneurone dendrites: contribution of Ca<sup>2+</sup>-permeable AMPA and NMDA  
receptors to subthreshold Ca<sup>2+</sup>-dynamics. *J. Physiol.* **551**, 67–78 (2003).
22. Bacci, A., Rudolph, U., Huguenard, J. R. & Prince, D. A. Cellular/Molecular  
Major Differences in Inhibitory Synaptic Transmission onto Two Neocortical  
Interneuron Subclasses.

- 595 23. Goldberg, E. M. *et al.* K<sup>+</sup> channels at the axon initial segment dampen near-  
596 threshold excitability of neocortical fast-spiking GABAergic interneurons. *Neuron*  
597 **58**, 387–400 (2008).
- 598 24. Rudy, B. & McBain, C. J. Kv3 channels: voltage-gated K<sup>+</sup> channels designed for  
599 high-frequency repetitive firing. *Trends Neurosci.* **24**, 517–526 (2001).
- 600 25. Kim, D. *et al.* Distinct Roles of Parvalbumin- and Somatostatin-Expressing  
601 Interneurons in Working Memory. *Neuron* **92**, 902–915 (2016).
- 602 26. Kim, H., Ährlund-Richter, S., Wang, X., Deisseroth, K. & Carlén, M. Prefrontal  
603 Parvalbumin Neurons in Control of Attention. *Cell* **164**, 208–218 (2016).
- 604 27. Povysheva, N. V, Zaitsev, A. V, Gonzalez-Burgos, G. & Lewis, D. A.  
605 Electrophysiological heterogeneity of fast-spiking interneurons: chandelier versus  
606 basket cells. *PLoS One* **8**, e70553 (2013).
- 607 28. Martina, M. & Jonas, P. Functional differences in Na<sup>+</sup> channel gating between  
608 fast-spiking interneurons and principal neurons of rat hippocampus. *J. Physiol.*  
609 **505**, 593–603 (1997).
- 610 29. Hu, H., Martina, M. & Jonas, P. Dendritic mechanisms underlying rapid synaptic  
611 activation of fast-spiking hippocampal interneurons. *Science (80-. )*. **327**, 52–58  
612 (2010).
- 613 30. Silver, R. A. Neuronal arithmetic. *Nat. Rev. Neurosci.* **11**, 474–489 (2010).
- 614 31. Polsky, A., Mel, B. W. & Schiller, J. Computational subunits in thin dendrites of  
615 pyramidal cells. *Nat. Neurosci.* **7**, 621–7 (2004).
- 616 32. Häusser, M. & Mel, B. Dendrites: bug or feature? *Curr. Opin. Neurobiol.* **13**,  
617 372–383 (2003).
- 618 33. Kastellakis, G., Cai, D. J., Mednick, S. C., Silva, A. J. & Poirazi, P. Synaptic  
619 clustering within dendrites: An emerging theory of memory formation. *Prog.*  
620 *Neurobiol.* **126**, 19–35 (2015).
- 621 34. Poirazi, P. & Mel, B. W. Impact of Active Dendrites and Structural Plasticity on  
622 the Memory Capacity of Neural Tissue. *Neuron* **29**, 779–796 (2001).

- 623 35. Losonczy, A. & Magee, J. C. Integrative Properties of Radial Oblique Dendrites  
624 in Hippocampal CA1 Pyramidal Neurons. *Neuron* **50**, 291–307 (2006).
- 625 36. Tran-Van-Minh, A. *et al.* Contribution of sublinear and supralinear dendritic  
626 integration to neuronal computations. *Front. Cell. Neurosci.* **9**, 67 (2015).
- 627 37. Tran-Van-Minh, A., Abrahamsson, T., Cathala, L. & DiGregorio, D. A.  
628 Differential Dendritic Integration of Synaptic Potentials and Calcium in  
629 Cerebellar Interneurons. *Neuron* **91**, 837–850 (2016).
- 630 38. Katona, G. *et al.* Roller Coaster Scanning reveals spontaneous triggering of  
631 dendritic spikes in CA1 interneurons. *Proc. Natl. Acad. Sci. U. S. A.* **108**, 2148–  
632 2153 (2011).
- 633 39. Cornford, J. H. *et al.* Dendritic NMDA receptors in parvalbumin neurons enable  
634 strong and stable neuronal assemblies. *bioRxiv* 279505 (2018).  
635 doi:10.1101/279505
- 636 40. Poirazi, P., Brannon, T. & Mel, B. W. Pyramidal Neuron as Two-Layered Neural  
637 Network. *Neuron* **37**, 989–999 (2003).
- 638 41. Kastellakis, G., Silva, A. J. & Poirazi, P. Linking Memories across Time via  
639 Neuronal and Dendritic Overlaps in Model Neurons with Active Dendrites. *Cell*  
640 *Rep.* **17**, 1491–1504 (2016).
- 641 42. Goldberg, J. H., Tamas, G. & Yuste, R. Ca<sup>2+</sup> imaging of mouse neocortical  
642 interneurone dendrites: Ia-type K<sup>+</sup> channels control action potential  
643 backpropagation. *J. Physiol.* **551**, 49–65 (2003).
- 644 43. Goldberg, J. H. & Yuste, R. Space matters: Local and global dendritic Ca<sup>2+</sup>  
645 compartmentalization in cortical interneurons. *Trends Neurosci.* **28**, 158–167  
646 (2005).
- 647 44. Poirazi, P., Brannon, T. & Mel, B. W. Arithmetic of Subthreshold Synaptic  
648 Summation in a Model CA1 Pyramidal Cell. *Neuron* **37**, 977–987 (2003).
- 649 45. Hu, H., Martina, M. & Jonas, P. Dendritic Mechanisms Underlying Rapid  
650 Synaptic Activation of Fast-Spiking Hippocampal Interneurons. *Science* (80-. ).  
651 **327**, 52–58 (2010).

- 652 46. Tamas, G., Buhl, E., Lorincz, A. & Somogyi, P. Proximally targetd GABAergic  
653 synapses and gap junctions synchronise cortical interneurons. *Nat. Neurosci.* **3**,  
654 366–371 (2000).
- 655 47. Gentet, L. J., Avermann, M., Matyas, F., Staiger, J. F. & Petersen, C. C. H.  
656 Membrane Potential Dynamics of GABAergic Neurons in the Barrel Cortex of  
657 Behaving Mice. *Neuron* **65**, 422–435 (2010).
- 658 48. Larkum, M. E., Nevian, T., Sandler, M., Polsky, A. & Schiller, J. Synaptic  
659 Integration in Tuft Dendrites of Layer 5 Pyramidal Neurons: A New Unifying  
660 Principle. *Science (80-. )*. **325**, (2009).
- 661 49. Cazé, R. D., Humphries, M. & Gutkin, B. Passive dendrites enable single neurons  
662 to compute linearly non-separable functions. *PLoS Comput. Biol.* **9**, e1002867  
663 (2013).
- 664 50. Cai, D. J. *et al.* A shared neural ensemble links distinct contextual memories  
665 encoded close in time. *Nature* **534**, 115–8 (2016).
- 666 51. Zhou, M. *et al.* CCR5 is a suppressor for cortical plasticity and hippocampal  
667 learning and memory. *Elife* **5**, (2016).
- 668 52. Hu, H. & Vervaeke, K. Synaptic Integration in Cortical Inhibitory Neuron  
669 Dendrites. *Neuroscience* **368**, 115–131 (2018).
- 670 53. Topolnik, L. Dendritic calcium mechanisms and long-term potentiation in cortical  
671 inhibitory interneurons. *Eur. J. Neurosci.* **35**, 496–506 (2012).
- 672 54. Camire, O. & Topolnik, L. Dendritic Calcium Nonlinearities Switch the Direction  
673 of Synaptic Plasticity in Fast-Spiking Interneurons. *J. Neurosci.* **34**, 3864–3877  
674 (2014).
- 675 55. Martina, M. Distal Initiation and Active Propagation of Action Potentials in  
676 Interneuron Dendrites. *Science (80-. )*. **287**, 295–300 (2000).
- 677 56. Gulyás, A. I., Megías, M., Emri, Z. & Freund, T. F. Total Number and Ratio of  
678 Excitatory and Inhibitory Synapses Converging onto Single Interneurons of  
679 Different Types in the CA1 Area of the Rat Hippocampus. *J. Neurosci.* **19**,  
680 (1999).

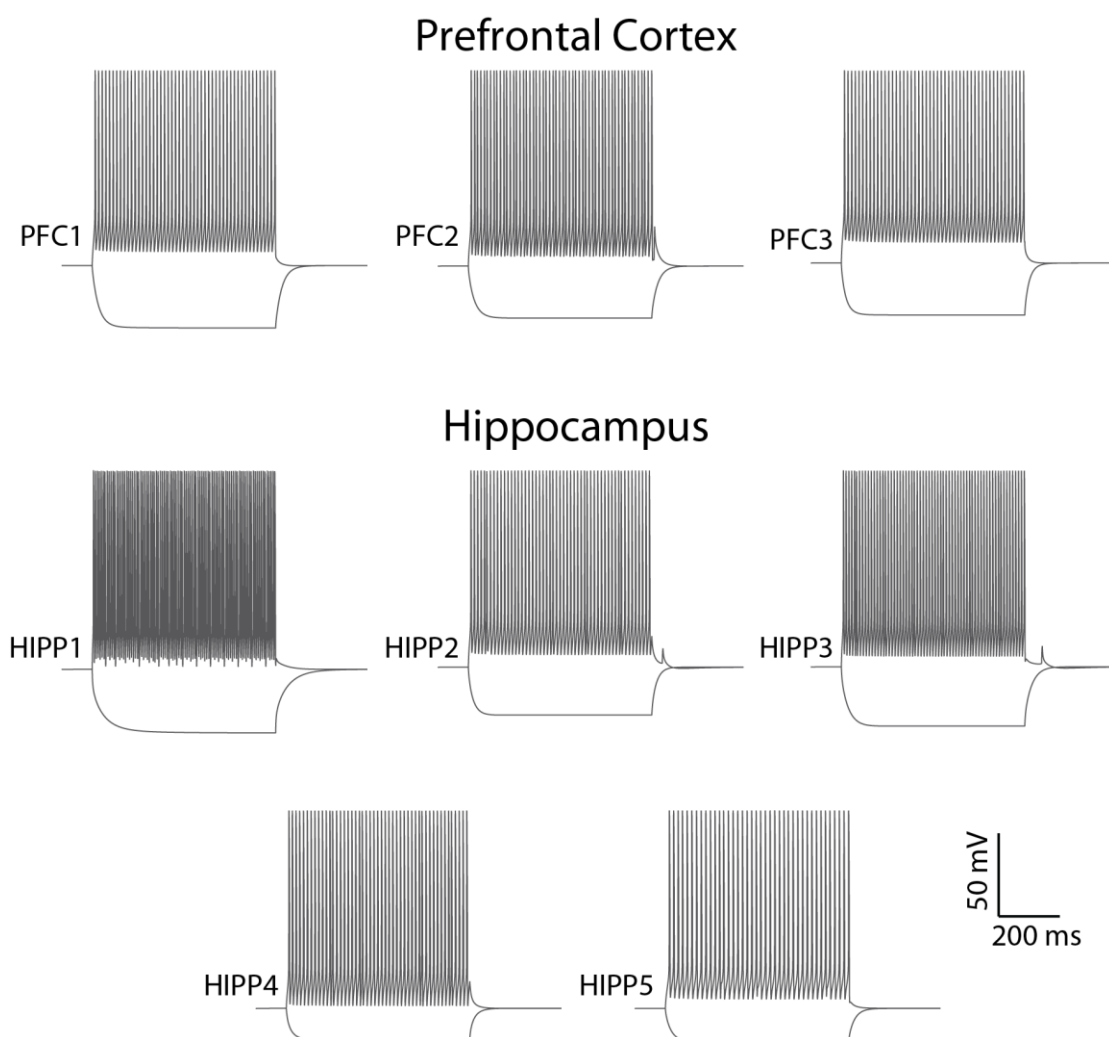
681 57. Tukker, J. J. *et al.* Distinct Dendritic Arborization and In Vivo Firing Patterns of  
682 Parvalbumin-Expressing Basket Cells in the Hippocampal Area CA3. *J. Neurosci.*  
683 **33**, (2013).

684

685

686

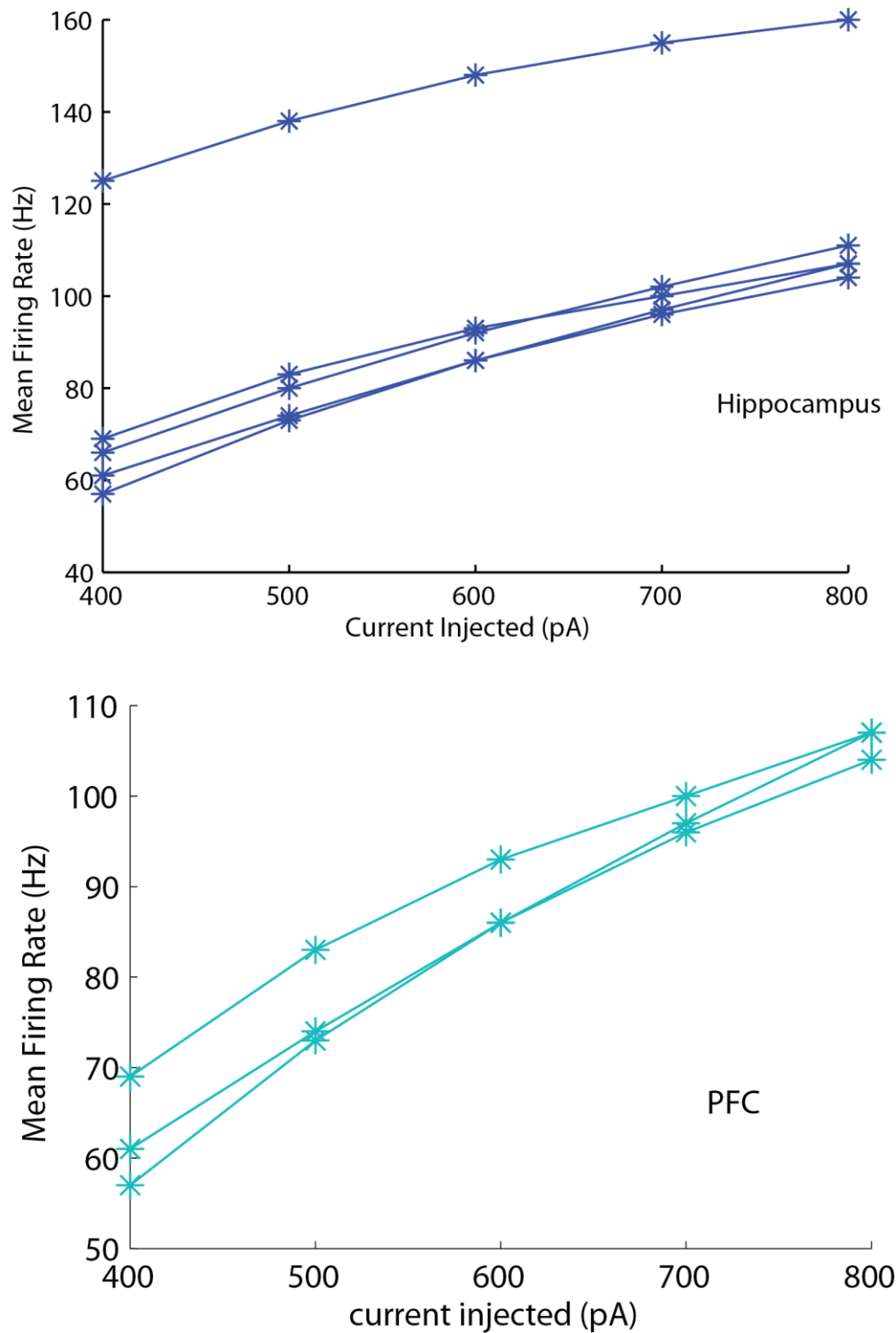
687 **Supplementary Figures.**



688

689 **Supplementary Figure 1.** Model cell firing profiles. Somatic Current-clamp traces of  
690 Hippocampal (A) and PFC (B) model cells, after a depolarizing current injection in somata  
691 (500 pA; 1000 ms) evoked a high-frequency firing pattern. A hyperpolarizing current  
692 injection in somata (-300pA, 1000ms) induced a realistic hyperpolarizing response.

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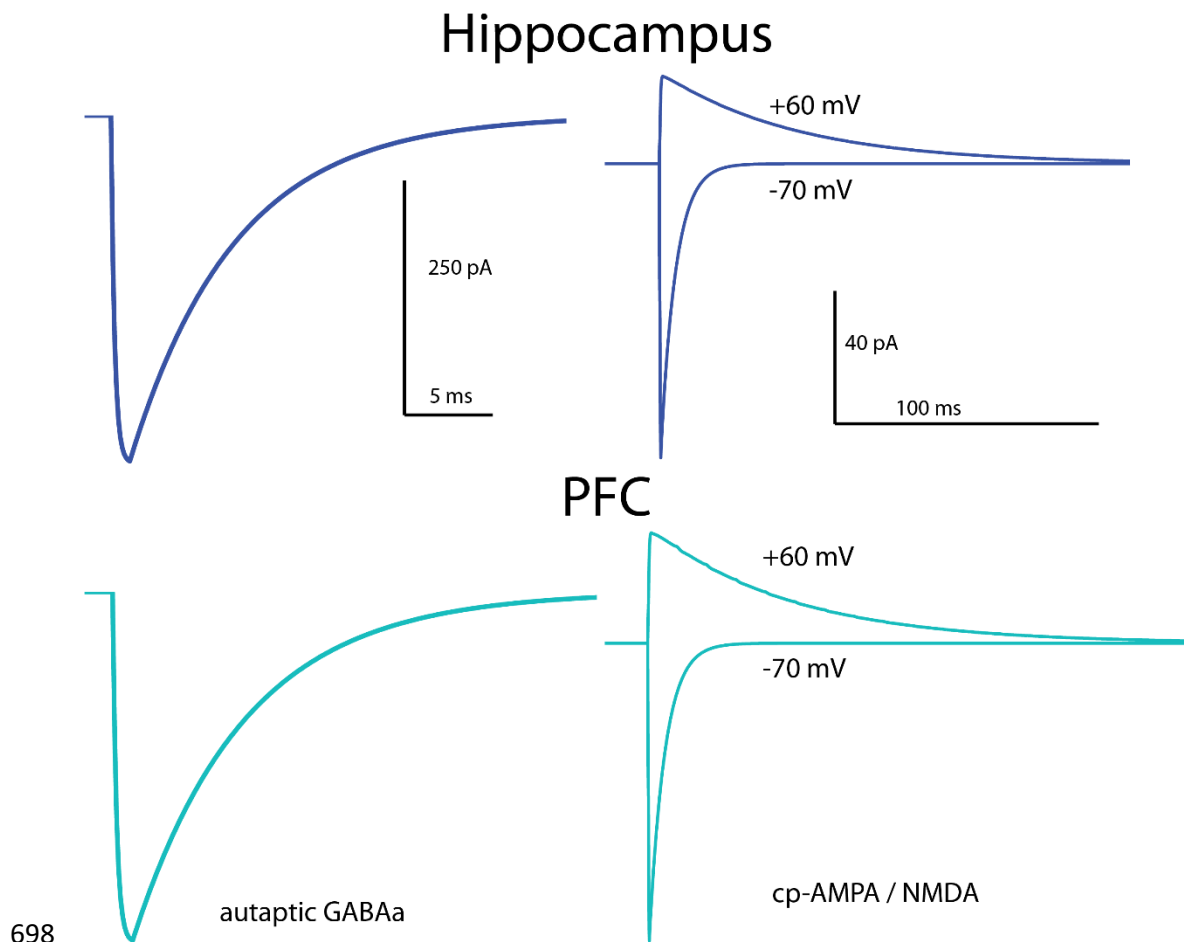


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695 **Supplementary Figure 2:** Mean firing frequencies in response to injected currents of  
696 different amplitudes (600 ms duration) in Hippocampal (up) and PFC (down) model cells.

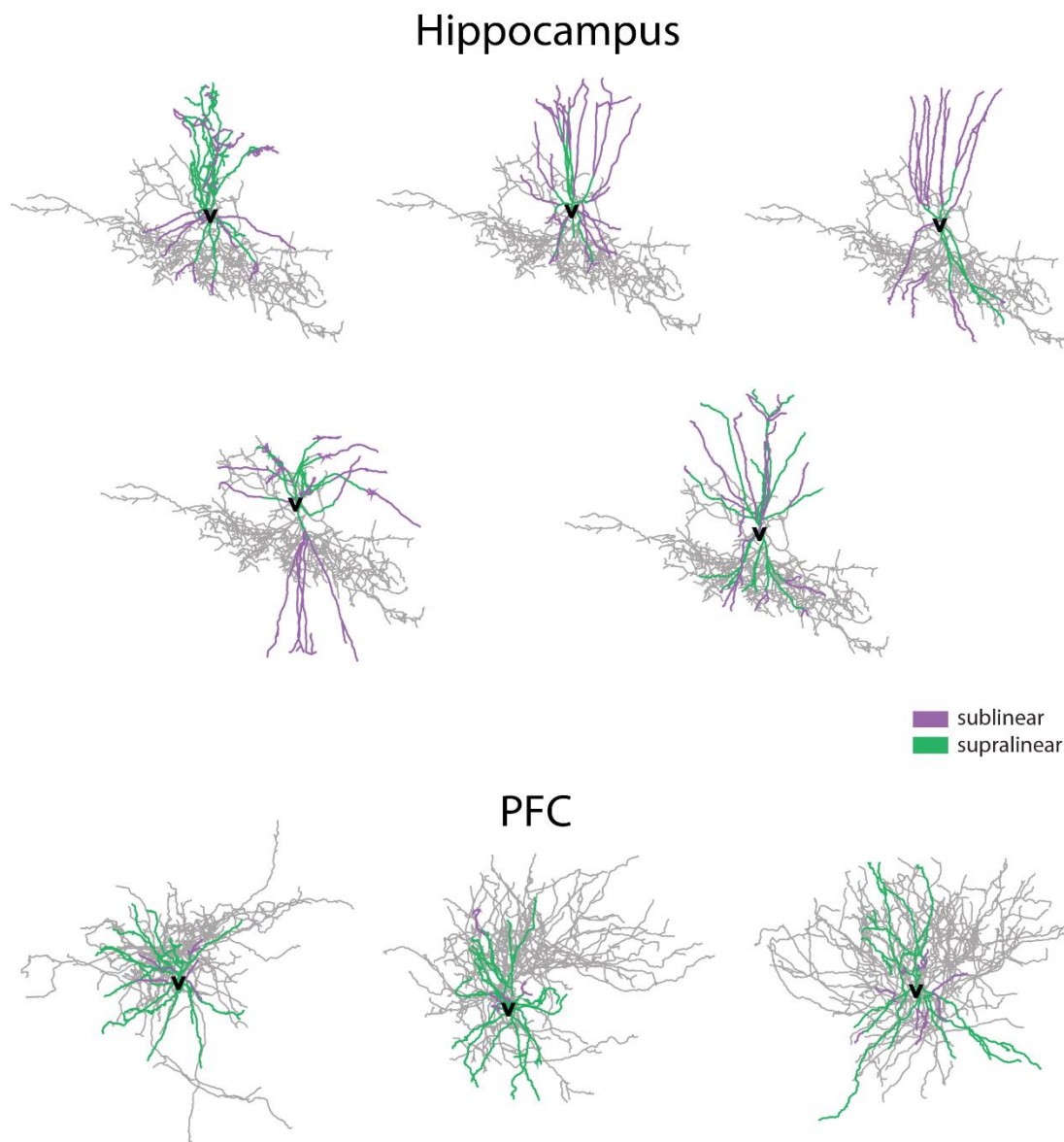
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**Supplementary Figure 3:** Validation of synaptic currents in Fast Spiking basket cells.

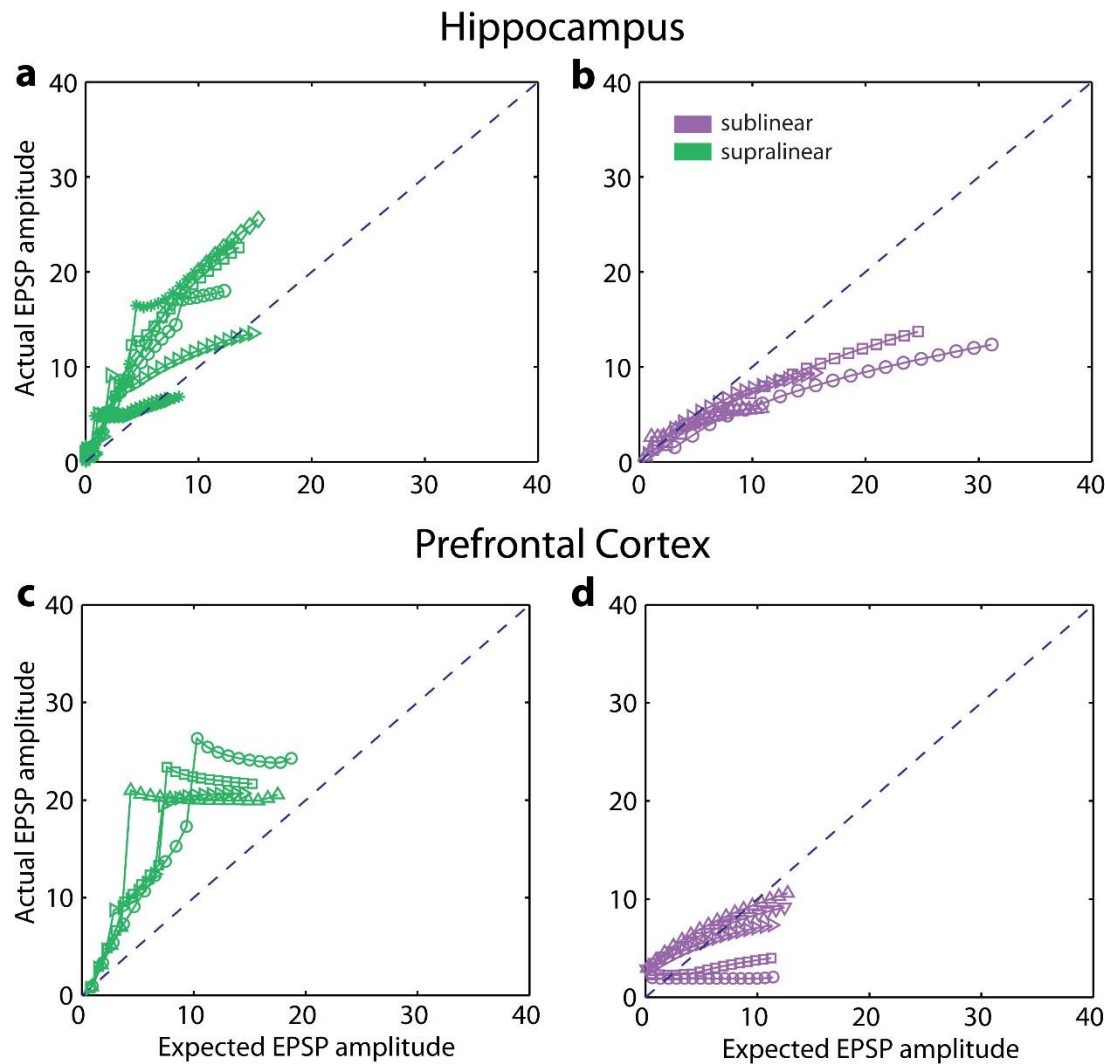
Left. A three-step voltage clamp of voltage changes from  $-70$  mV to  $10$  mV (duration  $1$  ms) and back to  $-70$  mV was used to produce a self-inhibitory (autaptic) current. During the validation of this current, the reversal potential of  $\text{Cl}^-$  was adjusted from  $-80$  to  $-16$  mV, in order to reproduce the experimental set up of Bacci et al., 2003. However, a physiological reverse potential ( $-80$  mV) was used for all other simulations. Right. Model reproduction of cp-AMPA ( $-70$  mV) and NMDA ( $+60$  mV) currents in response to stimulation of 2 synapses as per Wang et al., 2009. \* each trace represents the mean of all Hippocampal and PFC cells respectively.



709

710 **Supplementary Figure 4:** Related to **Figure 2**. Bimodal non-linear integration in Fast  
 711 Spiking basket cells. Supralinear (blue) and sublinear (magenta) dendrites shown in each  
 712 model cell.

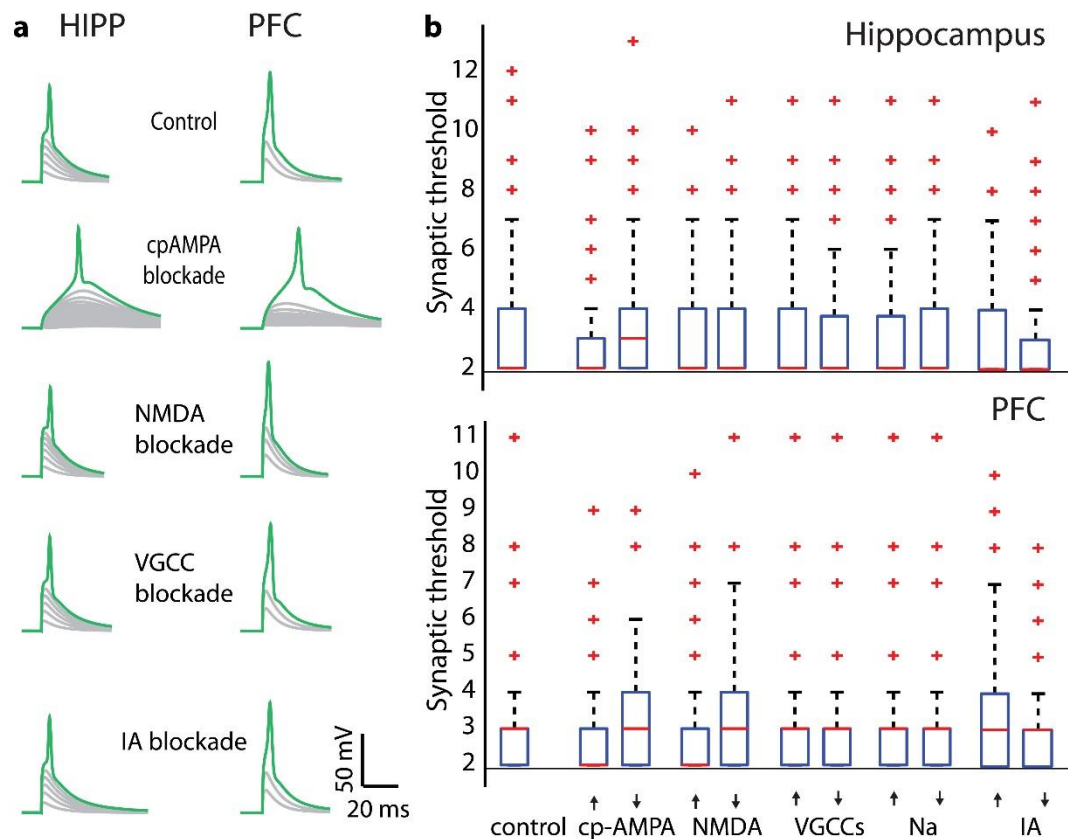
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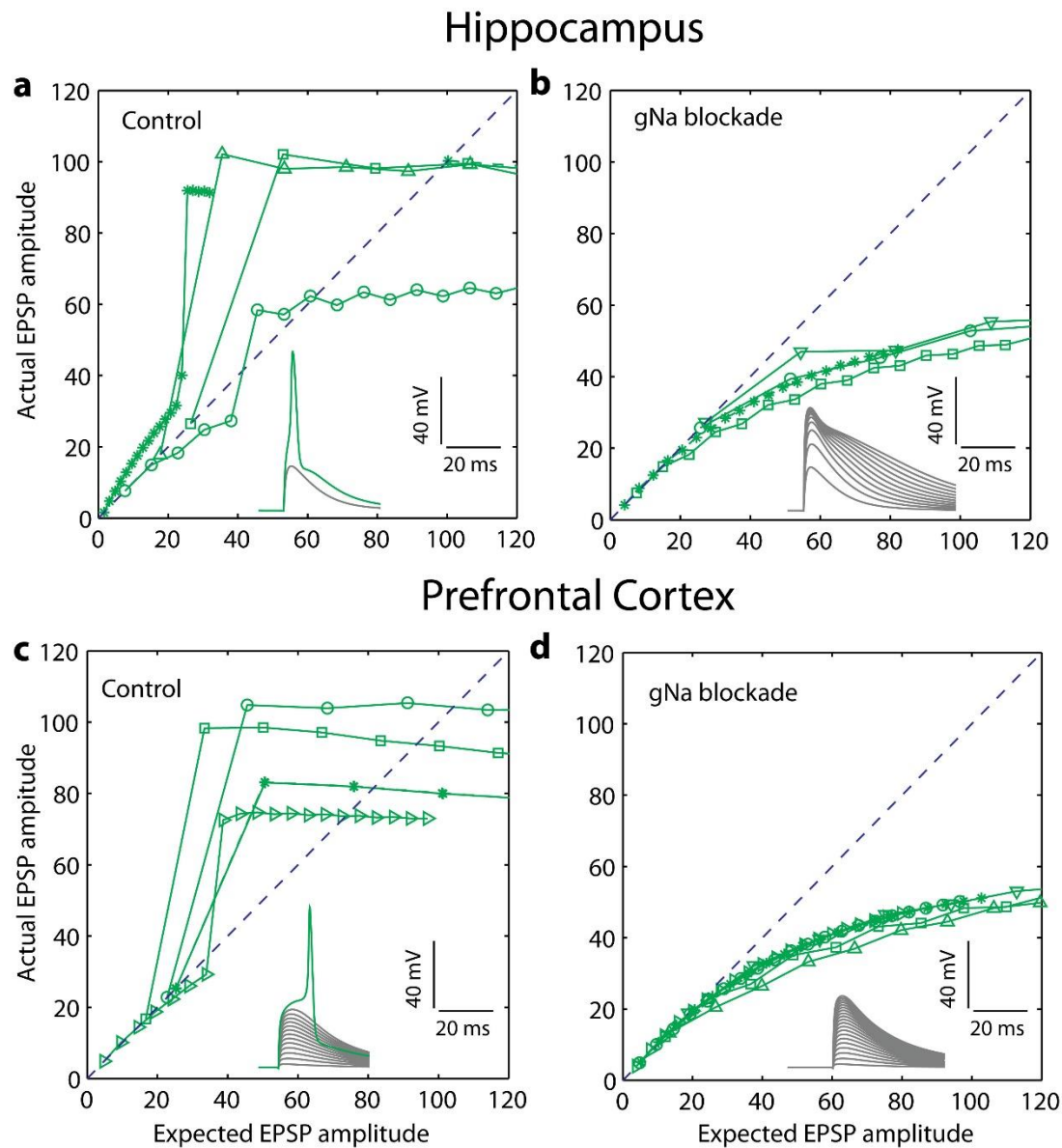
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715 **Supplementary Figure 5:** Related to **Figure 2**. Bimodal non-linear integration in Fast  
716 Spiking basket cells. Representative Somatic EPSPs after stimulation (single pulse) of an  
717 increasing number of synapses (1:1:20), uniformly distributed within dendrites.

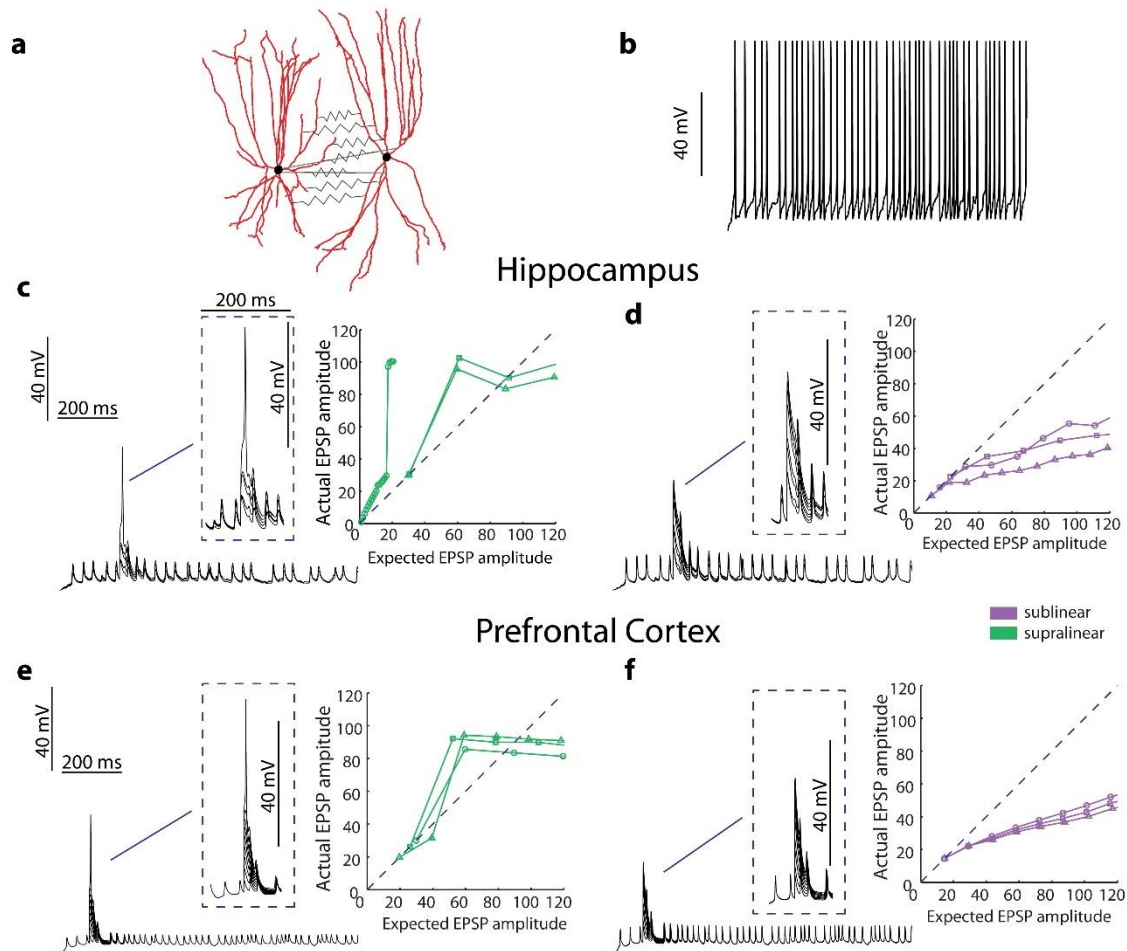
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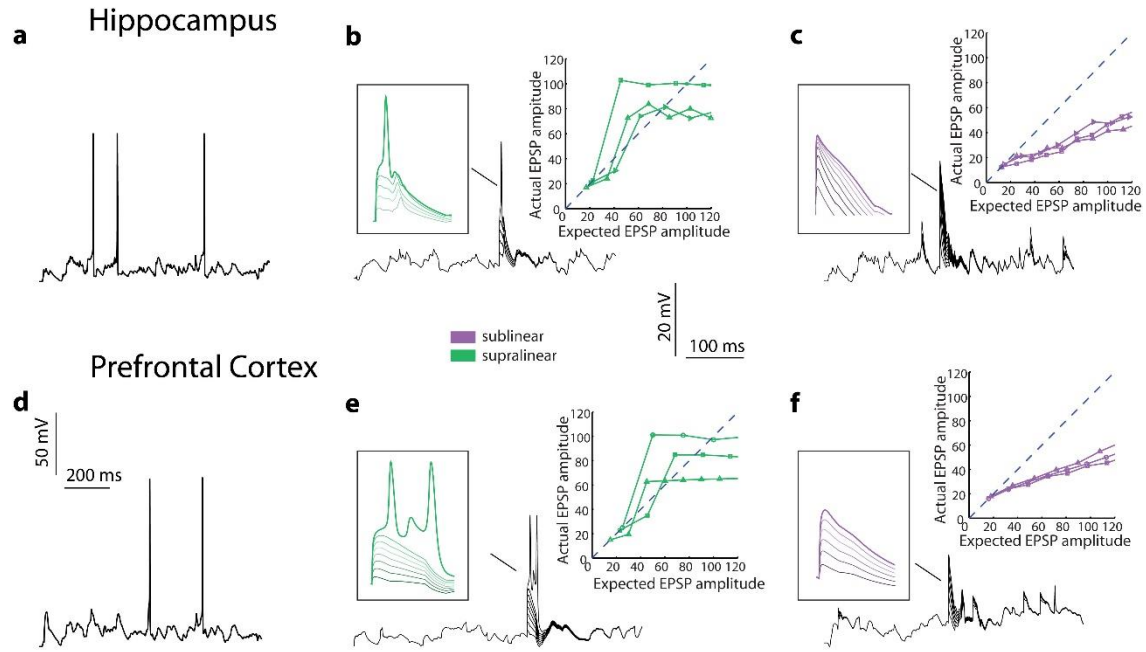
**Supplementary Figure 6:** Related to Figure 1. **a.** Presence of supralinear summation in dendrites of FS BCs after blockade of multiple active currents respectively in Hippocampus (left) and PFC (right). **b.** Sensitivity analysis of biophysical dendritic mechanisms reveals minor changes in the synaptic threshold for spike generation in supralinear dendrites across Hippocampus and PFC.



**Supplementary Figure 7.** Related to Figure 1. Blockade of active sodium conductances in the dendrites of FS BCs, totally eliminates the supralinear operation mode. Hippocampal (a) and PFC (c) representative supralinear responses of dendrites under physiological conditions. Dendritic spikes are eliminated both in Hippocampal (b) and PFC (d) FS BCs dendrites EPSP responses after blockade of sodium conductances. Linear line represents linear summation.



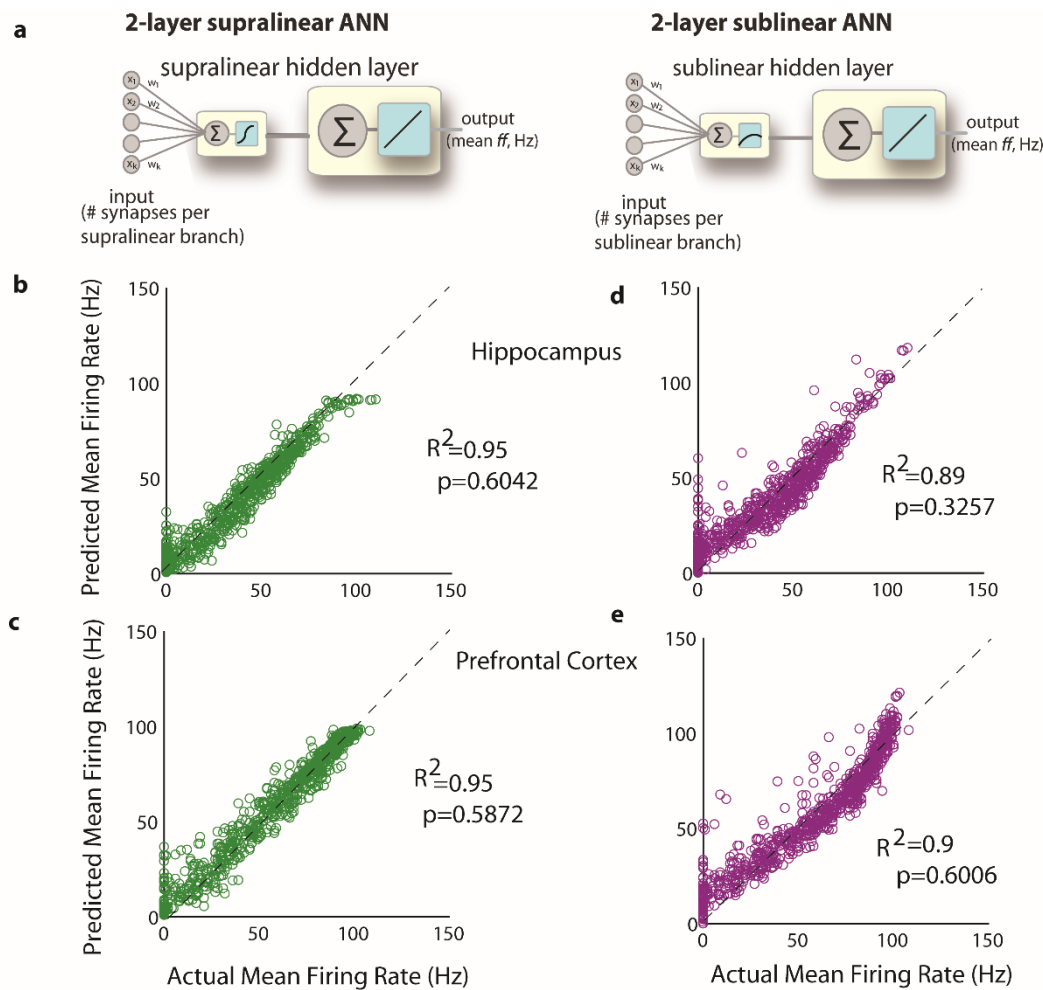
**Supplementary Figure 8.** FS BCs exhibit supralinear and sublinear dendritic responses in the presence of Gap Junctions. A) Illustrated dendritic trees that are interconnected with Gap Junctions. B) Presynaptic firing rate (~30 Hz). Supralinear (C,E) and sublinear (D,F) dendrites co-exist in Hippocampal (up) and PFC (down) Fast spiking basket cells models.



740

741 **Supplementary Figure 9.** FS BCs exhibit supralinear and sublinear dendritic responses in  
742 the presence of *in vivo*- like fluctuations. Somatic firing rate of  $3 \pm 1$  Hz induced in  
743 Hippocampal (A) and PFC (D) models of FS BCs after synaptic activation of randomly  
744 selected dendrites with 10Hz Poisson spike trains. Supralinear (B,E) and sublinear (C,F)  
745 dendrites co-exist in FS BCs of Hippocampus (up) and PFC (down).

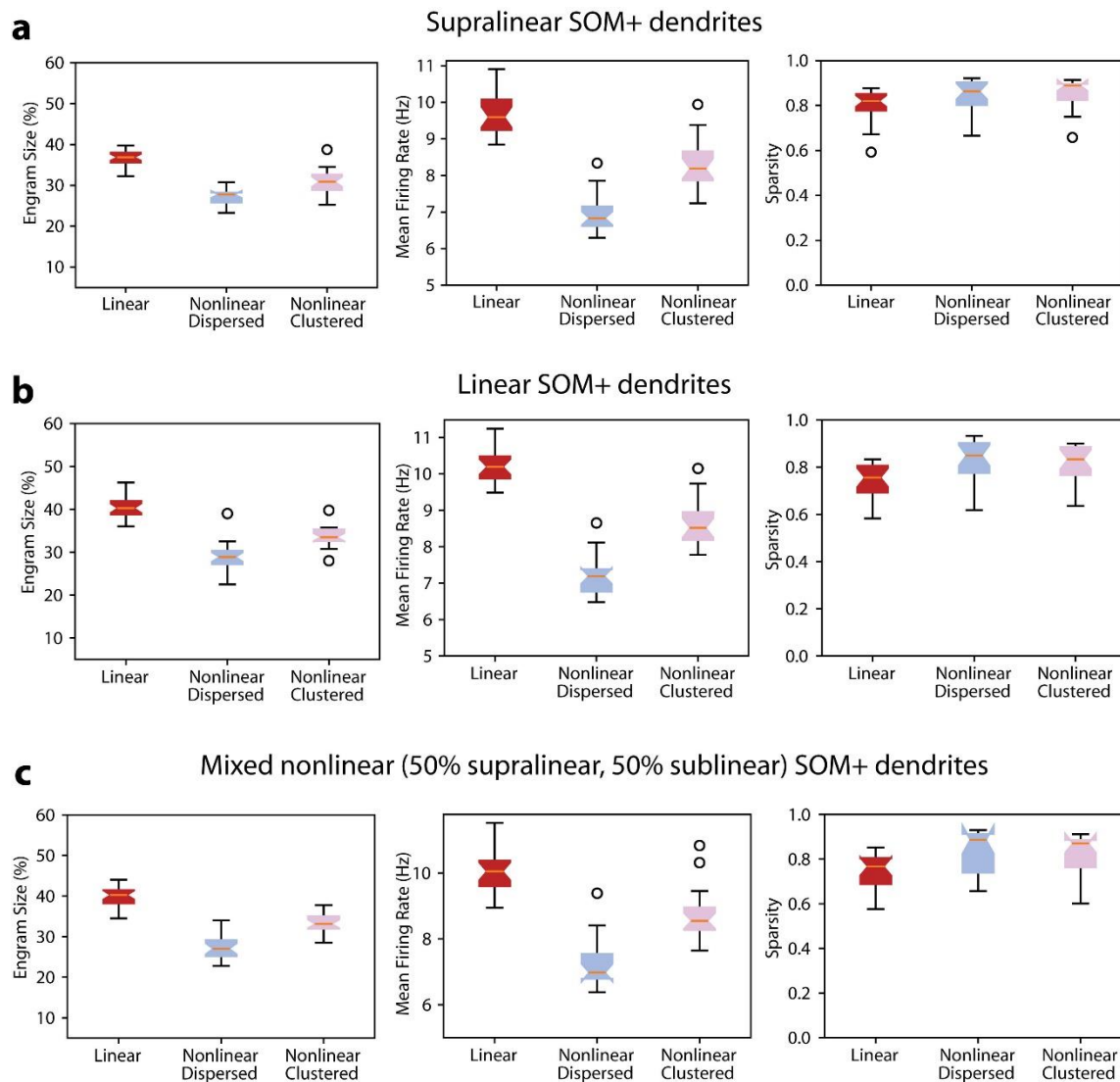




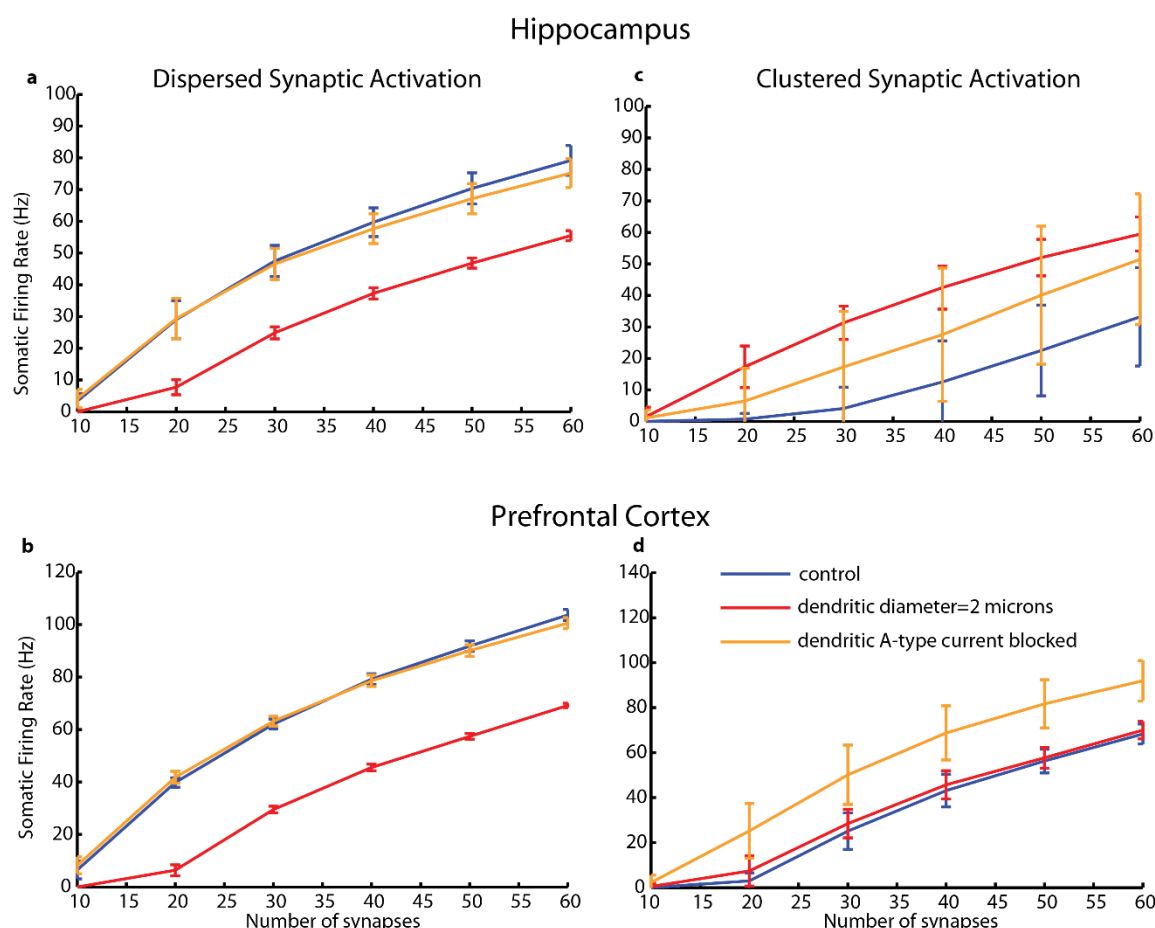
746

747 **Supplementary Figure 10.** Related to **Figure 6**. Linear regression analysis for one hidden  
748 layer supralinear (**b,c**) and one hidden layer sublinear (**d,e**) ANNs for one indicative  
749 Hippocampal (top) and one indicative PFC (bottom) model cell. Actual Mean Firing Rates  
750 (Hz) correspond to the responses of the compartmental model when stimulating -with 50Hz  
751 Poisson spike trains- varying numbers of synapses (1 to 60), distributed in several ways  
752 (clustered or dispersed) within both sub- and supra-linear dendrites. Expected Mean Firing  
753 Rates (Hz) are those produced by the respective ANN abstraction when receiving the same  
754 input (number of stimulated synapses) in its respective sub-/supra- or linear input layer  
755 nodes.

756



**Supplementary Figure 11.** Related to **Figure 7**. Manipulation of SOM+ models dendritic transfer function results in almost identical responses of multiple properties of the canonical microcircuit. Modeled SOM+ dendrites A) Supralinear B) Linear C) Supralinear and sublinear (50% of each mode)



763

764 **Supplementary Figure 12.** Related to **Figure 4**: Firing rate responses (in Hz) from one  
765 Hippocampal (**a, c**) and one PFC (**b, d**) model cell, in response to stimulation of increasing numbers  
766 of synapses (10 to 60) that are either randomly distributed throughout the entire dendritic tree or  
767 clustered within a few dendritic branches. Effect of dendritic diameter (red, setting the diameter of  
768 all dendrites to 2 microns) and A-type current (orange, setting the conductance of dendritic A-type  
769 currents to zero) on somatic firing rates in response to synaptic stimulation under dispersed and  
770 clustered spatial arrangements. As shown in panels **a, c** disperse synaptic arrangements benefit  
771 mostly from the dendritic morphology of FS BCs, as setting the diameter to 2 microns sharply  
772 decreases this preference. Clustered arrangements on the other hand (panels **b, d**) are severely  
773 hampered by the high conductance of the A-type potassium channels in these cells, as blockade of  
774 these currents enhances somatic output. This potassium current does not penalize disperse inputs as  
775 much, simply because it is not as strongly activated as in the case of clustered activation (which  
776 induces much higher local depolarizations and thus stronger A-type channel activation). (p-values  
777 for the various comparisons: hippocampus, disperse: diameter vs. control =0.0018, IA vs. control,  
778 non-significant; hippocampus, clustered: diameter vs. control=0.0048, IA vs. control=0.0087; PFC,  
779 disperse diameter vs. control =0.0014, IA vs. control, non-significant; PFC, clustered diameter vs.  
780 control =0.0102, IA vs. control=0.0026)