

1 **Invariances in a combinatorial olfactory receptor code**

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12 **Abstract**

13

14 **Animals can identify an odorant type across a wide range of concentrations, as well as**  
15 **detect changes in concentration for individual odorant type. How olfactory**  
16 **representations are structured to support these functions remains poorly understood.**  
17 **Here, we studied how a full complement of ORNs in the *Drosophila* larva encodes a**  
18 **broad input space of odorant types and concentrations. We find that dose-response**  
19 **relationships across odorants and ORN types follow the Hill function with shared**  
20 **cooperativity but different activation thresholds. These activation thresholds are drawn**  
21 **from a power law statistical distribution. A fixed activation function and power law**  
22 **distribution of activation thresholds underlie invariances in the encoding of odorant**  
23 **identity and intensity. Moreover, we find similar temporal response filters of ORNs**  
24 **across odorant types and concentrations. Such uniformity in the temporal filter may**  
25 **allow identity invariant coding in fluctuating or turbulent odor environments. Common**  
26 **patterns in ligand-receptor binding and sensory transduction across olfactory receptors**  
27 **may give rise to these observed invariances in the olfactory combinatorial code.**  
28 **Invariant patterns in the activity responses of individual ORNs and the ORN ensemble**  
29 **may simplify decoding by downstream circuits.**

30

31 **Introduction**

32 The abilities to identify odorants across a wide range of concentrations and detect changes in  
33 odorant concentration are essential for olfactory perception and behavior. Olfactory systems use  
34 combinatorial codes to encode large numbers of odors with smaller numbers of olfactory  
35 receptor neurons (ORNs) (Malnic et al., 1999). Each ORN typically expresses one of a large  
36 repertoire of olfactory receptors (Ors) (Buck and Axel, 1991). A single Or can be activated by  
37 many different odorants, and a single odorant can activate many different Ors (Friedrich and  
38 Korschning, 1997). Different odorants can be discriminated by distinct activity patterns across an  
39 ensemble of olfactory neurons (Hallem and Carlson, 2006; Kreher et al., 2005; Nara et al.,  
40 2011). The olfactory code also conveys information about odorant intensity as higher odorant  
41 concentrations tend to activate more ORNs (Kajiya et al., 2001; Wang et al., 2003). Different  
42 odorants may also evoke different temporal patterns in neuronal activity, augmenting  
43 information coding using time (Friedrich and Laurent, 2001; Laurent et al., 2001; Junek et al.,  
44 2010; Smear et al., 2011).

45

46 Recent studies have uncovered coding properties at the single cell and population levels that  
47 may allow for scale-invariant representation of olfactory information such as odorant type and  
48 intensity. At the individual ORN level, ORN responses to temporal patterns in odorant  
49 presentation may be converted into predictable activity patterns by stereotyped filters (Nagel  
50 and Wilson, 2011; Martelli et al., 2013). At the population level, inputs to the olfactory bulb may  
51 encode odorants in concentration invariant spatial representations (Wachowiak et al., 2002;  
52 Cleland et al., 2007). At the statistical level, the firing rates of *Drosophila* ORNs appear to be  
53 drawn from an odor invariant probability distribution (Stevens, 2016). However, a quantitative  
54 characterization of such invariances in olfactory representation by a complete ORN ensemble is  
55 still missing.

56

57 In this study, we characterized the ORN ensemble of the *Drosophila* larva to a panel of odorant  
58 types and concentrations that spanned the selectivity of all olfactory sensory neurons. The  
59 *Drosophila* larva offers the advantage of numerical simplicity for dissecting an olfactory circuit  
60 that shares glomerular organization with adult insects and vertebrates (Vosshall and Stocker,  
61 2007; Su et al., 2009). We find that ORN-odorant pairs share the same activation function: ORN  
62 activity increases with concentration along the same Hill curve for any odorant type but with  
63 odorant-specific thresholds. We find that the statistical distribution of these ORN sensitivities to  
64 odorants across olfactory space follows a power-law. Furthermore, ORNs share a stereotyped

65 temporal filter shape such that ensemble level responses may be concentration-invariant in a  
66 fluctuating environment. Our systems-level characterization of an entire olfactory periphery  
67 across a wide range of odorant types and concentrations has revealed individual and ensemble  
68 level ORN patterns that allow for invariant representation of olfactory information, with  
69 significance for downstream processing.

70

### 71 **A microfluidic setup for *in vivo* calcium imaging of larval ORNs**

72 Small size and optical transparency make the larva's olfactory system – like that of *C. elegans* –  
73 suitable for *in vivo* multineuronal calcium imaging with precise and flexible microfluidic control of  
74 olfactory inputs (Chronis et al., 2007). We developed a microfluidic device for an intact, un-  
75 anesthetized larva with up to 16 fluid delivery channels, allowing us to image olfactory  
76 processing in single animals exposed to a broad input space (**Fig 1A-D, Supp Fig 1**). Fluid  
77 delivery allows for precise control of odorant concentration, timing between stimulus delivery,  
78 and stimulus waveform (Andersson et al., 2012). Furthermore, with the microfluidics setup we  
79 can record from ensembles of olfactory neurons with single cell resolution while delivering  
80 inputs that span odorant types and concentrations. Calcium imaging and genetic labeling allow  
81 us to record the activity of any individual ORN alone or the activity of all ORNs simultaneously,  
82 by expressing the calcium indicator GCaMP6m (Chen et al., 2013) under the control of either a  
83 specific ORN *Gal4* driver or the *Orco-Gal4* driver, respectively.

84

### 85 **Anatomical and functional identification of individual ORNs**

86 The larva has 21 ORNs located in each bilaterally symmetric dorsal organ ganglion (DOG). The  
87 layout of ORN dendrites aids in segmenting and identifying all cells during multineuronal  
88 calcium imaging. The 21 ORN sensory dendrites are organized into seven parallel bundles,  
89 each containing three sensory dendrites, that project from an ORN soma to the dorsal organ, a  
90 perforated dome on the animal's head (Singh and Singh, 1984). When a larva is immobilized in  
91 the microfluidic device, four ventral and three dorsal dendritic bundles are easily distinguished  
92 (**Fig 1E**). We mapped individual ORNs to each bundle by expressing RFP in all ORNs and GFP  
93 in a selected ORN using a cell specific Gal4 driver (**Supp Fig 2**). We found that the three ORN  
94 dendrites located in each bundle were stereotyped (confirmed in  $n \geq 5$  animals for each cell  
95 type). Thus, by following the activation of any cell body in the DOG to its corresponding dendritic  
96 bundle, its possible identity is narrowed to one of three ORNs.

97

98 To further aid in the identification of individual ORNs, we used a set of odorants, termed private  
99 odorants, that activate single ORNs at low concentrations. Mathew et al. (2013) assembled a  
100 panel of 18 private odorants for each larval ORN by expressing a single functional larval  
101 olfactory receptor (Or) in a mutant adult ORN devoid of the endogenous Ors, and recorded its  
102 electrical activity in response to olfactory cues. We delivered these private odorants to larvae in  
103 our microfluidic setup and found that 18 of the 21 ORNs, in each DOG, are responsive to these  
104 odorants: none of the private odorants in the panel activate the Or33a or Or63a ORNs and the  
105 Or49a ORN is only activated by a wasp pheromone (Ebrahim et al., 2015). We found that 13 of  
106 the private odorants are sufficient to identify all ORNs when examined in conjunction with  
107 dendritic bundle location (**Fig 1F**). Together, the anatomical map and functional responses to  
108 this subset of private odorants provides a comprehensive means of identifying and segmenting  
109 the ORNs responsive to any olfactory input during multineuronal imaging.

110

### 111 **ORN ensemble responses across odorant identities and intensities**

112 The panel of 18 private odorants provides a maximally decorrelated set of stimuli that spans the  
113 larval olfactory system. To characterize the olfactory representation of these stimuli, we  
114 exposed larvae to all 18 private odorants across the concentration range of olfactory sensitivity.  
115 We measured the response amplitude of every cell to step stimuli across five orders of  
116 magnitude in concentration, from  $10^{-8}$  dilution (where all private odorants were at or below  
117 threshold of ORN detection) to  $10^{-4}$  dilution (where many ORNs had reached saturation). We  
118 used five second step pulses interleaved with 20-60 seconds of water, a protocol that allowed  
119 us to measure peak responses and allowed for full recovery of neural activity (**Supp Fig 3**).

120

121 We verified that all private odorants were highly selective for their target ORNs at low  
122 concentrations, with activity expanding to additional ORNs at higher concentrations. For  
123 example, 1-pentanol was identified as a private odorant for the Or35a-expressing ORN. At  $10^{-7}$   
124 dilution, 1-pentanol slightly evoked activity specifically in the Or35a-ORN. Higher concentrations  
125 of 1-pentanol gradually saturated the Or35a-ORN, while also activating four other ORNs  
126 expressing either Or67b, Or85c, O13a, or Or1a (**Movie 1**). Interestingly, each additional ORN  
127 recruited by 1-pentanol corresponded to a private odorant that is also a long chain alcohol  
128 (Mathew et al., 2013). We next examined the ensemble-wide dose-response curves for these  
129 additional private alcohol odorants. Low concentrations of each private alcohol specifically  
130 activated its target ORN. Higher concentrations reliably activated the Or35a-ORN, Or13a-ORN,  
131 Or67b-ORN, and Or85c-ORNs to varying degrees (**Supp Fig 4**). Furthermore, we performed

132 the dose-response analysis across the entire ORN ensemble for all 18 private odorants (**Fig.**  
133 **2A**). We found a similar pattern of overlapping activation for ORNs sharing an odorant with a  
134 similar molecular structure. Thus, as odorant concentration increases, a family of molecules with  
135 similar structure will cross-activate the subgroup of ORNs that are particularly selective for  
136 molecules within the same family.

137

138 As in other animals, the olfactory code changes with increasing odorant intensity (Malnic et al.,  
139 1999), but with a pattern of ORN recruitment that is correlated with molecular selectivity. To  
140 discern this pattern, we used principal component analysis (PCA) of the responses of all ORNs  
141 measured against all private odorants across all concentrations. We visualized the data by  
142 projecting the ORN activity responses in the space of the first three principal components (PCs)  
143 (**Fig 2B**), which account for 60% of the variance in the data (**Supp Fig 5A**). At the lowest  
144 concentrations, olfactory representations at or below the detection threshold across odorants  
145 were tightly clustered at a central point in the PCA space. At higher concentrations, olfactory  
146 representations diverged, increasing distance monotonically from the central point (**Fig 2B**,  
147 **Supp Fig 5B**). Interestingly, the trajectory of each odorant tended to follow its own direction in  
148 PCA space. This pattern is particularly clear for aliphatic and aromatic odorants. Aliphatic  
149 odorants with long carbon chains form trajectories projecting in a similar direction of PCA space,  
150 since higher concentrations of these odorants tend to selectively recruit the other ORNs with  
151 aliphatic private odorants. The same was true for aromatic odorants and the corresponding  
152 group of ORNs with private odorants of this type (**Fig 2B**). The vectors corresponding to  
153 structurally similar molecules were separated by small angles (**Fig 2B, Supp Fig 5C**). Thus,  
154 visualization of ORN responses in PCA space reveals structure in the ensemble representation  
155 of odorant identity over a large range of intensities. The population wide response maintains a  
156 fixed direction in the representation of each odorant as concentration rises.

157

158 **Dose-response curves share the same steepness but vary in threshold concentrations**

159 We uncovered additional invariant structure when we analyzed the dose-response relationship  
160 of individual odorant-ORN pairs. We found that the subset of all pairs that reached saturation  
161 (n= 21 of 324 pairs) were well described by a Hill function:

$$162 \quad y = y_{max} \frac{c^n}{c^n + EC_{50}^n},$$

163 where  $y_{max}$  is the maximum response amplitude measured by the calcium indicator,  $c$  is the  
164 odorant concentration,  $n$  is the Hill coefficient or steepness of the linear portion of the curve, and

165  $EC_{50}$  is the half-maximal effective concentration. The Hill function canonically describes binding  
166 affinities in ligand-receptor interactions such as that between odorants and olfactory receptors.  
167 Here, we find that the Hill equation describes a common concentration dependent nonlinearity in  
168 each dose-response relationship. After normalizing each dose-response curve by  $y_{max}$  and  
169 aligning by the  $EC_{50}$ , all 21 dose-response curves collapsed onto a single Hill function with  $n =$   
170  $1.5 \pm 0.1$  (**Fig 3A**). This common Hill coefficient suggests a similar degree of cooperativity in  
171 odorant binding and signal transduction across the ORN repertoire. Assuming the same  
172 cooperativity applies to the other odorant-ORN pairs, we estimated the  $EC_{50}$  value for all  
173 remaining pairs. The complete  $EC_{50}$  matrix reveals the distribution of sensitivities across the  
174 ORN ensemble to each odorant (**Fig 3B**).  
175

176 A simple coding scheme emerges. A common Hill function, with the  $EC_{50}$  value as the only free  
177 parameter, describes the dose-response relationship for any odorant-ORN interaction. This  
178 model, using the complete matrix of estimated  $EC_{50}$  values, accounts for 98% of the variance in  
179 the original dataset (**Supp Fig 6A**). For each odorant, the vector of  $EC_{50}$  values (a row in the  
180 matrix in **Fig 3B**) specifies the identity and threshold of each activated ORN with increasing  
181 odorant concentration. A corollary of having a unique  $EC_{50}$  vector for each odorant is having a  
182 unique direction for the trajectory of population responses across concentrations (**Fig 2B**).  
183

184 To study structure in the distribution of ORN sensitivities, we applied PCA to the matrix of  
185  $\ln(1/EC_{50})$  (see **Methods**). We found that the first principal component (PC) explains a  
186 significant portion of the variance (**Supp Fig 6B**). We projected the vector of  $\ln(1/EC_{50})$  values  
187 associated with each private odorant onto this first PC, and found that this projection strongly  
188 correlated with aromaticity index (**Supp Fig 6C**), one of the major quantitative metrics of odorant  
189 molecular structure that has been linked to olfactory discrimination across animals (Haddad et  
190 al., 2008). This observation explains why the trajectories of aromatic and aliphatic odorant  
191 representations point in opposite directions in **Fig. 2B**.  
192

### 193 **Power law distribution of ORN ensemble sensitivities**

194 Next, we examined the properties of the  $EC_{50}$  values themselves. We extracted all measured  
195 elements from the  $EC_{50}$  matrix and constructed a cumulative density function (**Fig. 3C**). The  
196 data closely follows a line in the log-log plot, indicating a power law:  $P(\frac{1}{EC_{50}}) \propto (\frac{1}{EC_{50}})^{-\lambda-1}$ ,  $\lambda =$   
197 0.35.

198

199 A power law distribution of olfactory sensitivities means that a relative change of concentration  
200 will trigger the same mean relative change in the number of activated ORNs, irrespective of  
201 odorant type. A power law distribution of olfactory sensitivities, together with a common Hill  
202 function, should give rise to ensemble-wide activity that follows a power law relationship with  
203 respect to concentration and has an exponent  $\lambda$  (See **Methods**). We confirmed this prediction in  
204 our experimental data (**Fig 3D**). The mean activity of the olfactory ensemble grows with odorant  
205 concentration following a power law with an exponent of  $0.38 \pm 0.06$ , which is close to the 0.35  
206 exponent found from fitting the  $EC_{50}$  matrix (**Fig 3C**). Thus, on average, activity expands across  
207 the ORN ensemble at the same rate with increasing relative concentration, irrespective of  
208 odorant type (as shown in **Fig. 2**).  
209

## 210 **ORN-odorant responses share similar temporal characteristics**

211 An additional challenge to olfactory coding of a wide variety of odorant types across  
212 concentrations arises from complex temporal dynamics due to physical fluctuations, such as  
213 turbulence or convection, in the stimulus itself. To examine how such fluctuations affect ORN  
214 responses, we compared the conversion of temporal patterns of olfactory input for different  
215 odorant-ORN pairs across odorant intensities. To do this, we used reverse-correlation analysis,  
216 subjecting larvae to “white noise” olfactory input by stochastically switching between odorant  
217 and water delivery and seeking the temporal filter that best maps olfactory inputs into calcium  
218 dynamics (Geffen et al., 2009; Kato et al., 2014). We found that random olfactory input could  
219 evoke fluctuating calcium activity in an ORN, and repeated presentation of the same input  
220 pattern would evoke consistent responses from trial to trial (**Supp Fig 7A**). The systematic  
221 conversion of the stimulus to response waveform is well characterized by a linear-nonlinear (LN)  
222 model. A linear transfer function estimates the relative weight of each time point in stimulus  
223 history to determine the time-varying response amplitude (**Supp Fig 7B**). The convolution of the  
224 linear transfer function with stimulus history is then passed through a static nonlinearity to  
225 correct for saturation (**Supp Fig 7C**). We verified the LN model by predicting the response to a  
226 novel random input using a filter calculated from different random inputs (**Supp Fig 7D**).  
227

228 We measured the linear transfer function for 3-octanol, the private odorant for the Or85c-ORN,  
229 across the concentration range used to characterize the  $EC_{50}$  matrix. At the lowest  
230 concentrations of 3-octanol, a filter describing ORN activity only emerges for the Or85c-ORN  
231 (**Fig 4A**). At higher concentrations, filters begin to emerge for additional ORNs. These filters for

232 each ORN, when normalized for response amplitude, were virtually identical in their temporal  
233 response profiles as single lobed functions with similar peak and decay times (**Fig 4B, Supp**  
234 **Fig 8B-C**). The shapes of the filters for different odorants activating the same ORN are also  
235 virtually indistinguishable, on the order of ~100 ms (**Fig 4C, Supp Fig 8A-C**). This result is  
236 constrained by the calcium indicator, which has a time constant associated with calcium binding  
237 to GCaMP6m, making it difficult to resolve differences in ORN temporal filters on a shorter time  
238 scale. Nonetheless, recent electrophysiological measurements of odorant-evoked activity in the  
239 ORNs of adult *Drosophila*, under the same LN model, also report remarkable similarity in the  
240 temporal pattern of filters across odorant-receptor pairs, within ~10-20 ms (Martelli et al., 2013).  
241  
242 A common temporal filter across ORNs could simplify the olfactory code in an environment with  
243 fluctuating odorant concentrations. A constant filter in conjunction with uniform scaling of ORN  
244 activity over concentration could allow the ensemble of responsive neurons to maintain the  
245 same relative amplitudes of activation over time. These relative amplitudes would be correlated  
246 with the ORN ensemble  $EC_{50}$  values for any odorant, regardless of whether an animal is in a  
247 static or fluctuating odorant environment.  
248

## 249 **Discussion**

250 Previous efforts at a systems-level characterization of ORNs necessarily focused analysis on  
251 particular cell types, odorants, or odorant concentrations (Hallem and Carlson, 2006; Mathew et  
252 al., 2013; Nagel and Wilson, 2013; Martelli et al., 2013; Asahina et al., 2009). The small size of  
253 the *Drosophila* larva, combined with multineuronal imaging and new microfluidic tools, has  
254 allowed us to characterize the responses of a complete ORN ensemble to a panel of odorant  
255 types and concentrations that spans the selectivity of olfactory sensory neurons. This broad  
256 characterization has uncovered regular patterns in the response of individual ORNs and of the  
257 ORN ensemble. First, each ORN response to odorants exhibits the same activation function  
258 shape with variant sensitivity levels. Furthermore, consistent temporal filters that convert  
259 different stimulus waveforms into ORN calcium activity patterns will make the relative activities  
260 of different ORNs robust despite fluctuating inputs. Second, the ORN ensemble across all  
261 tested odorants exhibits a constant rate of increase in activity with increasing concentration.  
262 Underlying this effect, we have identified a power-law distribution in the sensitivities of odorant-  
263 ORN interactions. The power law distribution may allow downstream circuits to estimate the  
264 relative concentrations of any odorant by the relative extent of ORN activity using the same  
265 quantitative relationship for any odorant. Invariant quantitative patterns in single and ensemble-

266 level ORN activities could allow shared mechanisms to extract olfactory features, even in  
267 fluctuating environments, across olfactory space.

268

269 Different neurons are required to sense odorants in different regimes of odorant concentration  
270 needed for long-range chemotaxis in the *Drosophila* larva (Asahina et al., 2009). Encoding a  
271 broad concentration range requires a distribution of ORNs with varying sensitivities. Our  
272 analysis reveals that olfactory sensitivities follow an invariant statistical distribution across  
273 odorants and ORN types. This power law distribution implies a fixed ratio between the relative  
274 change in ORN ensemble activity for a fixed change in odorant concentration. Detection of  
275 relative change in stimulus intensities has been observed in psychophysical studies of diverse  
276 sensory modalities. A notable example is Stevens's Law in human psychophysics, where  
277 response magnitudes have been shown to scale with the logarithm of stimulus intensities across  
278 sensory modalities including olfaction (Stevens, 1957). Our results reveal that a phenomenon  
279 analogous to Stevens's Law can be attributed to the olfactory sensory periphery itself, a direct  
280 outcome of the statistical distribution of response sensitivities across an ensemble.

281

282 A combinatorial olfactory code will arise from a distribution of ORN sensitivities to different  
283 odorant molecules. Changes in concentration necessarily lead to changes in the combinatorial  
284 code, but with correlated changes depending on the odorant. The basis of this correlation is a  
285 unique vector of sensitivities across ORNs for each odorant. This constraint allows each  
286 odorant's identity to be coded in a concentration-independent manner as a direction in an  
287 olfactory coding space. It has been suggested that extracting relative glomerulus activity across  
288 odorant concentrations may allow the concentration-invariant coding of different odorant types  
289 (Wachowiak et al., 2002; Cleland et al., 2007). For animals that sniff, the change in  
290 concentration through inhalation generates a reliable temporal sequence of ORN activity that  
291 could represent the vector of ORN sensitivity (Smear et al., 2011). As we have found in  
292 *Drosophila*, a common activation function and temporal filter – which may arise from  
293 stereotyped receptor cooperativities and shared transduction dynamics among ORNs – would  
294 facilitate the decoding that takes place by such mechanisms to extract concentration invariant  
295 representations of odorant identity.

296

297 To our knowledge, a power law distribution of olfactory sensitivities has not yet been described  
298 in any animal. One possibility for the power law in olfactory sensitivity is to match the  
299 distributions of odorant concentrations found in natural olfactory environments. Natural odors

300 are mixed by convection and turbulence, physical processes that are rich in power law  
301 dynamics (Catrakis and Dimotakis, 1996). Power laws appear in the statistics of other natural  
302 stimuli as well. Natural visual scenes exhibit a power law relationship between spectral power  
303 and spatial frequency (Field, 1987; Simoncelli and Olshausen, 2001). The loudness of natural  
304 sounds across frequencies are distributed by power laws (Theunissen and Elie, 2014). Sensory  
305 systems, in general, may adapt the statistical distribution of their sensitivities to their natural  
306 environments.

307

308 Another possibility is that the observed power law distribution represents an optimization of the  
309 olfactory code. It has recently been proposed that the olfactory code maximizes informational  
310 entropy (Stevens, 2015). Given the constraint of fixed mean firing rates among ORNs, this  
311 model leads to an exponential distribution of ORN firing rates evoked by odorants measured in  
312 the adult *Drosophila* antenna (Stevens, 2016). Interestingly, another prediction of this  
313 optimization is that the overall activity of the olfactory ensemble should increase as a power law  
314 of odor concentration, as we have also experimentally observed in the *Drosophila* larva and, in  
315 our case, connected to the statistical distribution of olfactory sensitivities across ORNs.

316

317 Finally, the molecular recognition mechanism of olfactory receptors may themselves give rise to  
318 a power law distribution in ORN sensitivities. Lancet et al., 1993 proposed a molecular  
319 recognition system in which a receptor has multiple selective binding sites. Each binding site  
320 contributes in a combinatorial manner to the binding strength between a receptor and molecule.  
321 This simple quantitative model generates a power law sensitivity distribution for receptors with  
322 random sets of binding sites. The statistics of an olfactory code using such a molecular  
323 recognition system would be robust to expansion of the ORN periphery, as occurs with  
324 *Drosophila* in which the adult has nearly triple the number of receptor types as that found in the  
325 larva. Furthermore, a conserved statistical structure in the olfactory code would allow  
326 downstream circuitry to employ similar decoding mechanisms across an animal's lifetime.

327

## 328 **Acknowledgment**

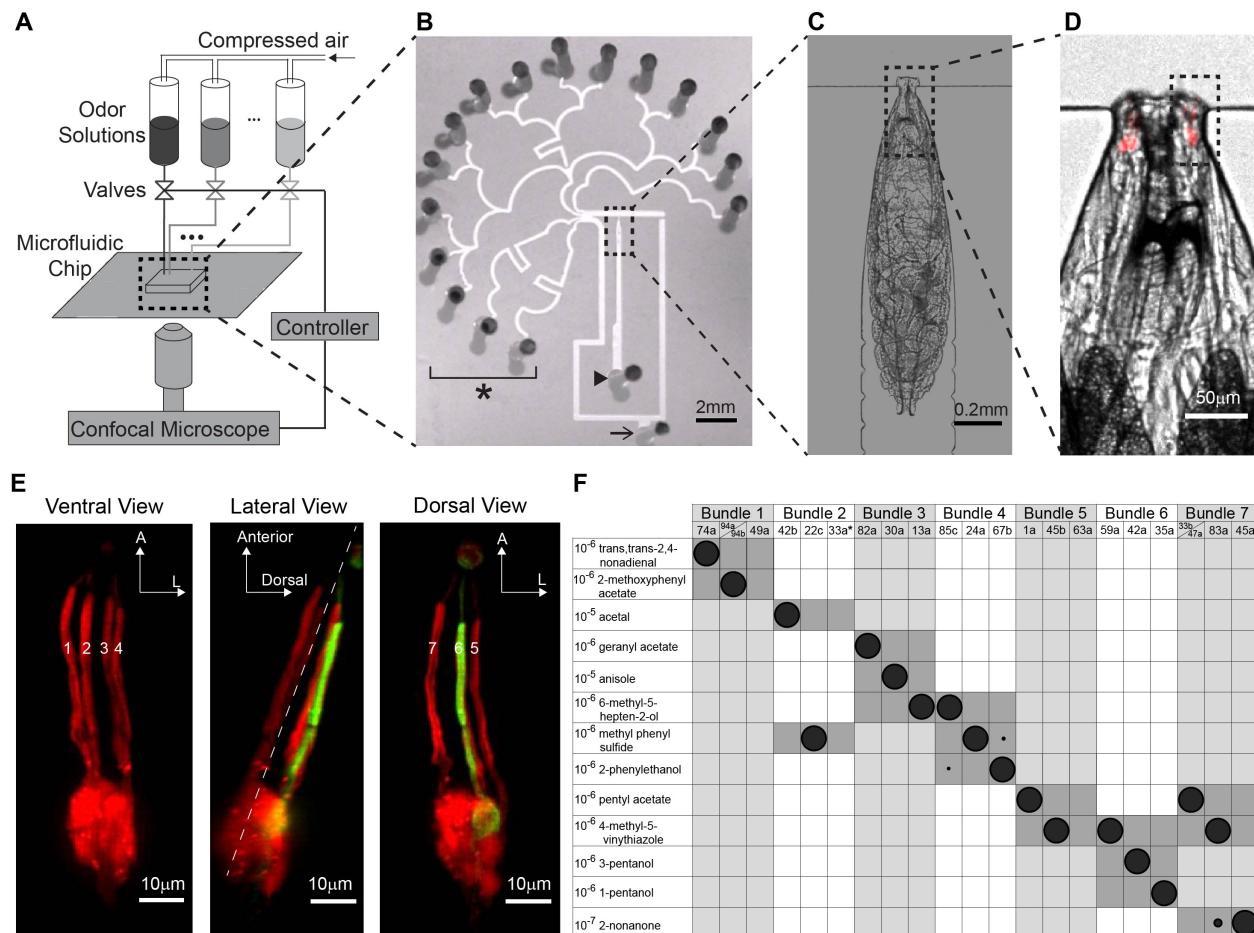
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337

338 **Figures:**

339



340

341

342 **Figure 1. Anatomical and functional identification of individual ORNs within the ORN**

343 **population.** A. Schematic of the setup for confocal imaging of a larva in a microfluidic device

344 during odorant delivery. B. 16 channel microfluidic device (\* indicates stimulus delivery channels,

345 arrowhead marks larva loading inlet, arrow marks fluid outlet). C and D. Zoomed-in view of an

346 immobilized larva in the loading channel. Red indicates RFP labeling of ORN dendrites and cell

347 bodies. E. Larval ORN sensory dendrites are organized into seven parallel bundles (numbered).

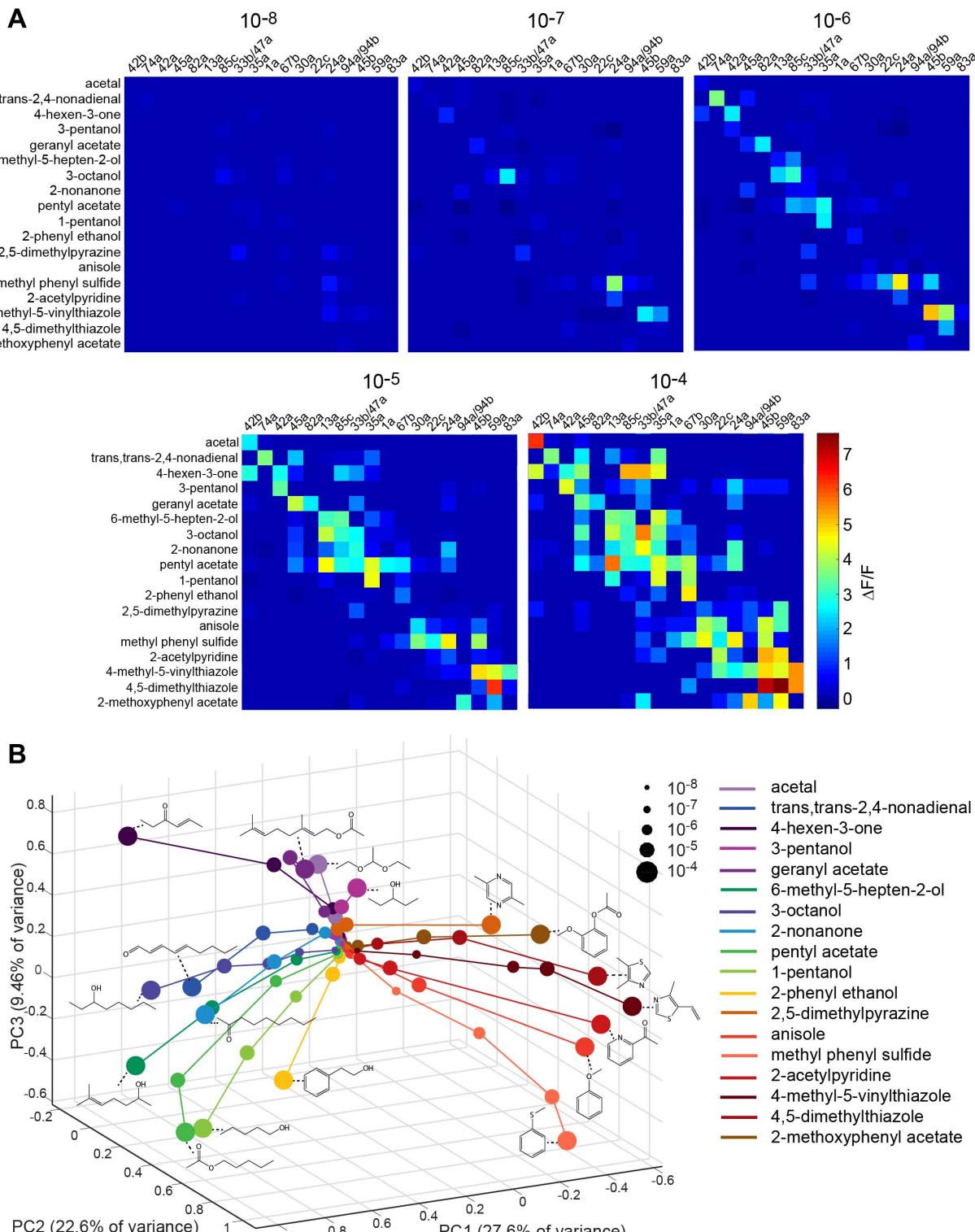
348 All ORNs shown in red, Or35-ORN shown in green, using *Or35a>GFP*; *Orco>RFP* genotype.

349 Dashed line in lateral view marks separation between ventral and dorsal bundles. F. Each of 13

350 odorants at low concentrations primarily activates only one ORN within each bundle. Size of

351 shaded circles indicates normalized neural activity ( $\Delta F/F$ ) of the specified ORN to an odorant. \*

352 indicates that location of Or33a-ORN was inferred from vacancy in bundle 2 (**Supp Fig 2**).



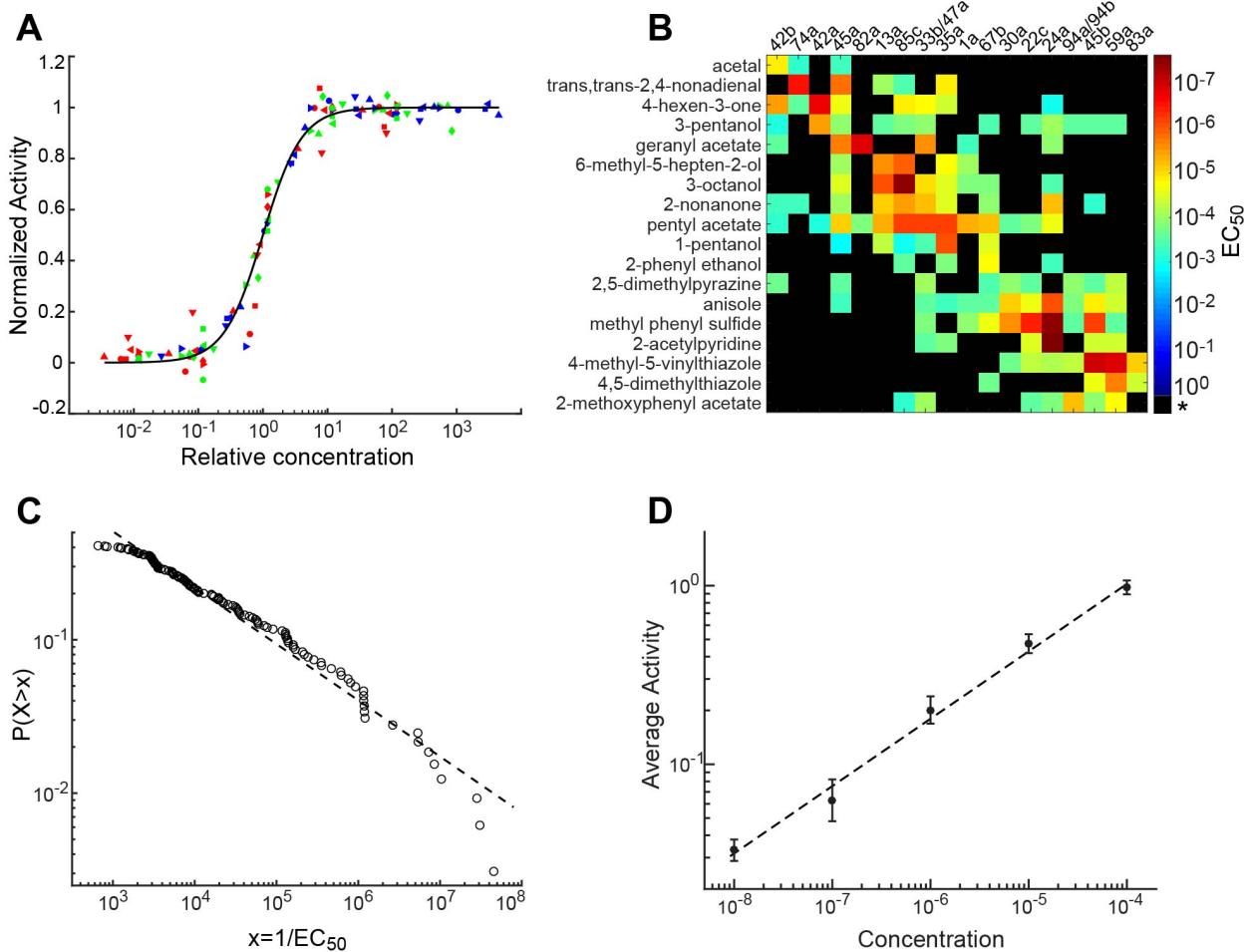
353

354 **Figure 2. ORN population responses to different odorants and concentrations. A.**

355 Averaged peak responses of 18 ORNs to a panel of 18 odorants, each delivered at five

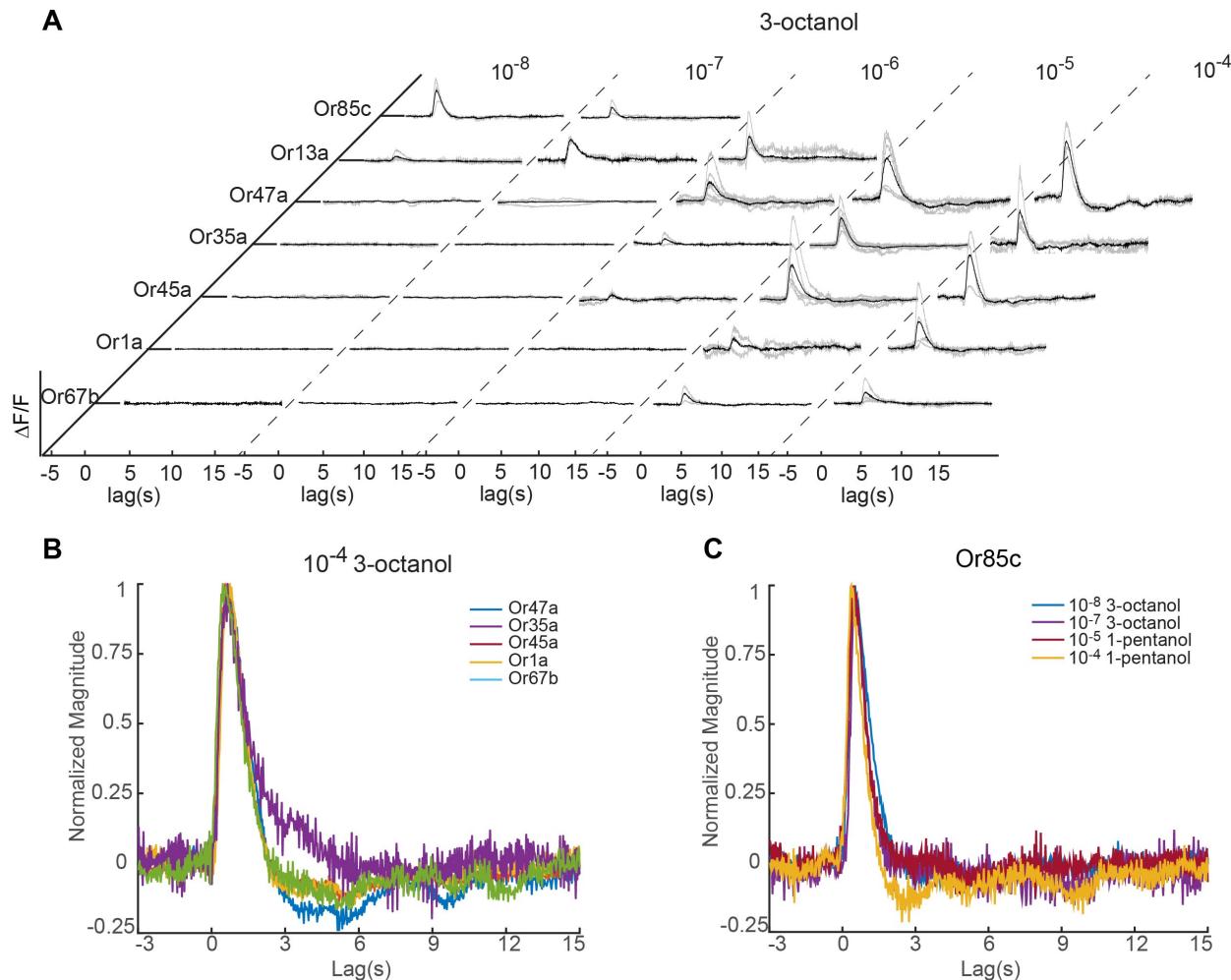
356 concentrations ( $n \geq 5$  for each odorant type and concentration; odorant pulse = 5 s). B. ORN

357 population responses visualized in PCA space. Each dot represents the projection of ORN  
358 population activity onto the first three principal components. Size and color of dots correspond  
359 to odorant concentration and type, respectively. Dots from the same odorant are linked and the  
360 molecular structure of the odorant is shown adjacent to each trajectory. Aromatic versus  
361 aliphatic odorants cluster in separate regions of PCA space.



362

363 **Figure 3. Scaling laws for individual and ensemble ORN activity.** A. Normalized ORN  
 364 responses for various odorant-ORN pairs across relative odorant concentration (actual  
 365 concentration divided by  $EC_{50}$ ). Individual curves for plotted odorant-ORN pairs collapse onto a  
 366 single curve described by a Hill equation with a shared Hill coefficient of 1.45. Black line  
 367 indicates the fitted Hill equation, different colored and shaped points represent data from unique  
 368 odorant-ORN pairs. B. Matrix of  $EC_{50}$  values fit to dose-response data from each odorant-ORN  
 369 pair (\* for black squares indicates that odorant-ORN pair had no response within the tested  
 370 concentration range). C. Log-log plot of the cumulative distribution function of  $1/EC_{50}$  values.  
 371 The dashed line is a linear fit to the data and has a slope of -0.35. D. Log-log plot of average  
 372 neuron activity across all odorant-ORN pairs for each concentration. The error bars represent  
 373 the standard error. Least-squares fit line has a slope of  $0.38 \pm 0.06$  ( $R^2 = 0.99$ ).



375 **Figure 4. Temporal filters of ORN response.** A. Linear filters of 7 ORNs responding to 3-  
376 octanol across five concentrations. Black curve indicates the averaged filter from data across  
377 multiple animals (individual filters shown in gray). B and C. Comparison of filter waveforms for  
378 the same odorant ( $10^{-4}$  dilution of 3-octanol) activating different ORNs (B), and the same ORN  
379 (Or85c-ORN) responding to different odorants and concentrations (C). All filters were  
380 normalized by their peak amplitude.

381 **References:**

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468 **Methods**

469 **Fly stocks**

470 Flies were reared at 22°C under a 12:12 hour light/dark cycle in vials containing conventional  
471 yeast agar medium. Adult flies were transferred to a larvae collection cage (Genesee Scientific)  
472 containing a grape juice agar plate and a dime-sized amount of fresh yeast paste. Flies could  
473 lay eggs on the grape juice agar plate for two days and then the plate was removed for  
474 collection of first instar larvae. The following fly lines were used in this study: *UAS-*  
475 *mCherry.NLS*; *UAS-GCaMP6m*, *UAS-mCD8::GFP*; *Orco::RFP*, *Orco-Ga4* (BL23292), *Or1a-*  
476 *Gal4* (BL9949), *Or13a-Ga4* (BL9945), *Or22c-Ga4* (BL9953), *Or24a-Ga4* (BL9958), *Or30a-*  
477 *Gal4* (BL9960), *Or33b-Ga4* (BL9963), *Or35a-Ga4* (BL9968), *Or42a-Ga4* (BL9970), *Or42b-*  
478 *Gal4* (BL9971), *Or45a-Ga4* (BL9976), *Or45b-Ga4* (BL9977), *Or47a-Ga4* (BL9982), *Or49a-*  
479 *Gal4/Cyo*; *Dr/TM3* (gift from John Carlson lab), *Or59a-Ga4* (BL9990), *Or63a-Ga4* (BL9992),  
480 *Or67b-Ga4* (BL9995), *Or74a-Ga4* (BL23123), *Or82a-Ga4* (BL23125), *Or83a-Ga4* (BL23128),  
481 *Or85c-Ga4* (BL23913), *Or94b-Ga4* (BL23916).

482

483 **Microfluidic device design, fabrication, and calibration**

484 Odorant stimuli were delivered using a microfluidic device (**Fig 1A**) designed with a 300 µm  
485 wide and 70 µm high larva loading channel. The channel tapered to a width of 60 µm in order to  
486 immobilize the larva. The tapered end was positioned perpendicular to a stimulus delivery  
487 channel to allow for odorant flow past larval ORNs. The device was designed with a “shifting-  
488 flow strategy”, similar to that described in Chronis et al, 2007. The 16-channel device included  
489 two control channels located at the periphery, 13 odorant channels in the middle, and one water  
490 channel to remove odorant residue. Each channel was of equal length to ensure equal  
491 resistance. During an experiment, a combination of three channels was always open: the water  
492 channel, one of the 13 odorant delivery channels, and one of the control channels. The 13  
493 odorant channels could be sequentially opened to deliver any odorant. Switching between the  
494 two control channels directed either water or an odorant to flow past the larva’s ORNs, as  
495 demonstrated in **Supp Fig 1**.

496

497 Fluorescein dye was used to measure the switching time between water and odorants as well  
498 as to verify the spatial odorant profile in the device during stimulus delivery. Our standard air  
499 pressure for stimulus delivery was 6 psi, which led to a flow rate of 0.5 mL/min in the microfluidic  
500 device. With these conditions, the switching time between water and odorant was ~20 ms  
501 (**Supp Fig 1A**).

502 The microfluidic device pattern was designed using AutoCAD. The design pattern was then  
503 transferred onto a silicon wafer using photolithography. The wafer was used to fabricate  
504 microfluidic devices using polydimethylsiloxane (PDMS) and following the standard soft  
505 lithography approach (Anderson et al, 2000). The resulting PDMS molds were cut and bonded  
506 to glass cover slips. Each microfluidic device was used for only a single panel of odorants in  
507 order to prevent contamination.

508

### 509 **Odorant delivery setup**

510 Odorants were obtained from Sigma-Aldrich, diluted in deionized (DI) water (Millipore) and  
511 stored for no more than 2 days. To prevent contamination, each odorant concentration was  
512 stored in a separate glass bottle and delivered through its own syringe and tubing set. Panels of  
513 odorants were delivered using a 16-channel pinch valve perfusion system (AutoMate Scientific,  
514 Inc.). Each syringe and tubing set contained a 30 mL luer lock glass syringe (VWR) connected  
515 to Tygon FEP-lined tubing (Cole-Parmer), which in turn was connected to silicone tubing  
516 (AutoMate Scientific. Inc.). The silicone tubing was placed through the pinch valve region of the  
517 perfusion system as its flexibility could allow for the passage or blockage of fluid flow to the  
518 microfluidics device. The silicone tubing was then connected to PTFE tubing (Cole-Parmer),  
519 which was then inserted into the microfluidic device. A microcontroller and custom written  
520 Matlab code were used to control the on/off sequence of the valves and to synchronize valve  
521 control with the onset of recording in the imaging software (NIS Elements).

522

523 During the entire recording, the larva experienced continuous fluid flow, with a flow rate of  
524 0.5mL/min or 0.2m/s. In the dose-response experiments, the stimuli sequences consisted of five  
525 seconds of odorant pulses followed by a washout period using water. The duration of odorant  
526 pulses was chosen such that ORN responses reached maximum amplitude. The washout time  
527 was adjusted to allow for ORN recovery back to baseline activity levels, and thus ensured that  
528 measurements of ORN responses were independent of stimulus sequence (**Supp Fig 3** and  
529 **Movie 1**). For the white noise experiments, a 1024-step m-sequence of odorant stimulus and  
530 water was delivered with a time step of 0.2 s (**Movie 2**).

531

### 532 **Calcium imaging**

533 A first instar larva was loaded into a microfluidic device using a 1 mL syringe filled with 0.1%  
534 triton-water solution. Using the syringe, a larva was pushed towards the end of the channel,  
535 where the 60  $\mu$ m wide opening mechanically trapped further larval movement. Each larva was

536 positioned such that its dorsal organ (nose) was exposed to the stimulus delivery channel and  
537 its dorsal side (where ORN cell bodies are located) was closest to the objective. Larvae were  
538 imaged using an inverted Nikon Ti-e spinning disk confocal microscope with a 60X water  
539 immersion objective (NA 1.2). A charged-coupled device (CCD) microscope camera (Andor  
540 iXon EMCCD) captured images at 30 frames/sec. ORN cell bodies were recorded by scanning  
541 the entire volume (~20 slices with a step size of 1.5  $\mu$ m) of the dorsal organ ganglion (**Movie 1**),  
542 while ORN axon terminals were recorded from a single slice of the antennal lobe (**Movie 2**).  
543 Dose-response experiments (data shown in **Fig 1-2, Supp Fig 3-4** and **Movie 1**) were  
544 performed using larvae of the *Orco>GCaMP6m*, *Orco>mCherry.NLS* genotype and recording  
545 from ORN cell bodies. White noise experiments (data shown in **Fig 4, Supp Fig 7-8** and **Movie**  
546 **2**) were performed using larvae expressing GCaMP6m in a single ORN (e.g. *Or42a>GCaMP6m*  
547 used in **Supp Fig 7**) and recording from ORN axon terminals.

548

549 **Dose response analysis**

550 Custom code written in ImageJ was used to track and identify each ORN as well as its  
551 responses to odorant stimuli. Slight movement artifacts were corrected by aligning frames using  
552 mCherry NLS labeling of ORN cell bodies and the ImageJ TurboReg plugin (Thevenaz et al,  
553 1998). Each ORN activated in response to an odorant stimulus was visually identified using both  
554 the anatomical location of its dendritic bundle and the functional map of cognate odorant to  
555 ORN activation (**Fig 1 E, F, Supp Fig 2**). ORN identification was performed independently by  
556 two experimenters to ensure accuracy. Changes in fluorescence were then quantified  
557 as  $(F_{peak} - F_0)/F_0$ , where  $F_0$  was the average ORN intensity sampled from the frames  
558 immediately preceding odorant delivery and  $F_{peak}$  was the highest intensity in ORN  
559 fluorescence during odorant delivery. Each odorant stimulus was repeated with at least 5 trials.  
560 The raw response data is summarized in **Supp Table 1**.

561

562 The heatmap in **Fig 2A** was generated by directly averaging the peak responses across trials.  
563 Simulated annealing was used to optimize the order of ORNs and odorants presented in this  
564 heatmap, such that it minimized a loss function in which cost increased linearly with the distance  
565 that activated odorant-ORN pairs were from the matrix diagonal. The response data was  
566 normalized by the highest response level within each trial, averaged across trials, and then Z-  
567 scored prior to performing PCA. The distance and direction of vectors shown in **Supp Fig 5**  
568 were calculated for each data point in **Fig 2B** using the standard formulae for cartesian to polar  
569 coordinate transformation.

570

571 **Dose-response curve fitting**

572 A Hill equation with a unique set of parameter values was fit to the dose-response curve for  
573 each odorant-ORN pair in our data set. The general form of the Hill equation is as follows:

574 
$$y = y_{max} \frac{c^n}{c^n + EC_{50}^n}$$
 Equation 1

575 where  $y_{max}$  is the maximum ORN response level across concentrations,  $c$  is the odorant  
576 concentration,  $EC_{50}$  is the half-maximal effective concentration, and  $n$  is the Hill coefficient.  
577 In the calcium imaging experiment, the maximum fluorescence intensity  $y_{max}$  could be affected  
578 by the detailed experimental settings and it is differently fitted for the curve of each odorant-  
579 ORN pair. Here, the absolute value of  $y_{max}$  is not considered a coding feature, so in the  
580 following analysis, we normalized the responses using  $y_{max}$ .

581

582 There were 21 odorant-ORN pairs saturated within the concentration range we studied. We  
583 started by fitting these 21 curves using the Hill equation. We normalized the responses using  
584 the  $y_{max}$  for each odorant-ORN pair and shifted the x-axis using its  $EC_{50}$ . A scatter plot of the  
585 normalized and shifted dose-response data for the 21 odorant-ORN pairs is shown in **Fig 3A**.

586

587 Next, we used a Hill equation function with  $y_{max} = 1$  and  $EC_{50} = 0$  to fit all 105 data points from  
588 the 21 different odorant-ORN pairs. The resulting equation had a Hill coefficient  $n = 1.45$ , with  
589  $R^2 > 0.99$ . Next, we applied this Hill coefficient to fit odorant-ORN data pairs that did not  
590 saturate in the concentration range we had tested. There were 19 additional odorant-ORN pairs  
591 that were close to saturation and we could therefore estimate their  $y_{max}$  and  $EC_{50}$  values well.

592

593 After fitting the 21 odorant-ORN pairs that had saturated as well as the 19 that were close to  
594 saturation, we had at least one parametrized Hill equation for each odorant. To fit the remaining  
595 odorant-ORN pairs that were not close to saturation within our tested concentration range, we  
596 first assumed that each odorant had approximately the same  $y_{max}$  for each odorant (this was  
597 calculated by averaging the  $y_{max}$  of all ORNs that shared an odorant with a parameterized  
598 logistic curve). Given the known  $y_{max}$  for each odorant and the fixed Hill coefficient, we could  
599 estimate the  $EC_{50}$  for the remaining 100 weakly responding odorant-ORN pairs.

600

601 The  $EC_{50}$  of all odorant-ORN pairs is summarized in **Fig 3B**. The black elements in the matrix  
602 indicate that the corresponding ORN showed no activity within the tested concentration range;

603 we were unable to fit an  $EC_{50}$  value for these odorant-ORN pairs. We used the Hill equation and  
604 fitted parameters for each odorant-ORN pair to generate the activity response data and found  
605 that it was similar to the actual data (**Supp Fig 6A**).

606

#### 607 **Analysis of the $EC_{50}$ Matrix**

608 To perform PCA on the  $EC_{50}$  matrix, we first transformed the values to the  $-\ln(EC_{50})$ , such that  
609 odorant-ORN pairs with a high sensitivity (small  $EC_{50}$ ) were now represented by large values  
610 and those that were less sensitive (large  $EC_{50}$ ) had small values. The remaining pairs that that  
611 did not have an  $EC_{50}$  value (the missing data, represented by black squares in **Fig 3B**),  
612 represent pairs with a much lower sensitivity and were set to zero. **Supp Fig 6B** shows the  
613 percentage of variance explained by each principal component (PC) once PCA was performed  
614 on the  $-\ln(EC_{50})$  matrix. In comparison to a shuffled matrix (in which each row is randomly  
615 permuted), we found that only the first PC was significantly different ( $p < 0.0001$  for 1000  
616 instances of shuffled data).

617

618 We compared 32 descriptors of molecular structure from the E-Dragon software, which were  
619 found in Haddad et al., 2008 to be relevant for olfactory coding across animals. We found that  
620 one metric, aromaticity index of a molecule, had the highest correlation with the first PC of the  
621  $EC_{50}$  matrix with a coefficient of 0.8 (**Supp Fig 6C**).

622

623 We fit the power law distribution using code from (Clauset et al., 2009). The resulting fitting  
624 index of 0.22 (large values mean better fit to the power law for this metric) is larger than the  
625 threshold (0.1) needed to accept the power law hypothesis (Clauset et al., 2009).

626

#### 627 **Derivation of power law scaling of ORN ensemble responses from $EC_{50}$ distribution**

628 Here, we explain analytically the power law relation between odorant concentration and the  
629 ensemble response of ORNs. Under the same Hill equation we used to fit individual dose-  
630 response curves (Eq. 1, here we set  $y_{max} = 1$  for simplicity), assume that (i)  $EC_{50}$  follows a  
631 power law distribution  $P(1/EC_{50}) \propto (1/EC_{50})^{-\lambda-1}$  (or equivalently an exponential distribution for  
632  $k = -\ln(EC_{50})$ :  $P(k) = \lambda e^{-\lambda(k-k_0)}$ ,  $k \geq k_0$ ) (ii) the Hill coefficient  $n$  for all odorant-ORN pairs are  
633 the same and greater than  $\lambda$  (satisfied in the data as 1.45 vs. 0.35). If so, the ensemble  
634 response follows an approximate power law form  $r(c) \propto c^\lambda$  for concentrations  $c \leq e^{-k_0}$  (which  
635 means the weakest response pair in the ensemble has not reached the half level). For

636 convenience, we use the log scale of concentration and  $EC_{50}$ :  $x = \ln(c)$ ,  $k = -\ln(EC_{50})$  and the  
637 logistic function in place of the Hill equation:  $y(x) = \frac{1}{1 + \exp(-n(x+k))}$ .

638

639 This result can be intuitively obtained by considering the limiting case where the logistic function  
640 is infinitely steep (large Hill coefficient) and is thus replaced by a step function. The ensemble  
641 response combining a large number of odorant-ORN pairs can be expressed as an integral:

642  $r(x) = \int_{k_0}^{\infty} y(x, k) \lambda e^{-\lambda(k-k_0)} dk$ ,  $y(x, k) = \frac{1}{1 + \exp(-n(x+k))}$  is the log-concentration. When  $y(x, k)$  is  
643 a step function, the integral becomes  $P(k \geq -x)$ , which is essentially the cumulative density  
644 function for  $k$ . Given the distribution of  $k$ , this is exactly an exponential function  $r(x) = e^{\lambda(x+k_0)}$   
645 (or a power law function of  $c$ ) for  $x \leq -k_0$ , and saturates at larger concentrations.

646

647 For the general case of logistic activation, the integral does not have a simple form expression  
648 but involves hyper-geometric functions. However, we can derive a simple closed form  
649 approximation by approximating the logistic function  $f(x) = 1/(1 + e^{-nx})$  using piecewise  
650 exponential functions:

651

$$f(x) \approx \begin{cases} e^{nx} - \frac{e^{2nx}}{2}, & x \leq 0 \\ 1 - e^{-nx} + \frac{e^{-2nx}}{2}, & x > 0 \end{cases}$$

652 Such an approximation becomes asymptotically exact when the steepness  $n$  goes to infinity, or  
653 when the absolute value of  $x$  goes to infinity. Substituting  $y(x, k)$  with this approximation, the  
654 integral splits into segments, over which the integrand are sums of exponential functions, and  
655 therefore can be easily integrated. This gives the closed form approximation of  $r(x)$ :

656

$$r(x) = \begin{cases} \left(1 + \frac{2\lambda^2}{n^2 - \lambda^2} - \frac{\lambda^2}{4n^2 - \lambda^2}\right) e^{\lambda(x+k_0)} - \frac{\lambda}{n-\lambda} e^{n(x+k_0)} + \frac{\lambda}{2(2n-\lambda)} e^{2n(x+k_0)}, & x \leq -k_0 \\ 1 - \frac{\lambda}{n+\lambda} e^{-n(x+k_0)} + \frac{\lambda}{2(2n+\lambda)} e^{-2n(x+k_0)}, & x > -k_0 \end{cases}$$

657 For small concentrations,  $x \leq -k_0$ , the leading term in the above expression is  $e^{\lambda(x+k_0)}$ , since  
658  $\lambda < n$ . This explains that the ensemble response is approximated by an exponential function  
659 with exponent  $\lambda$ . Furthermore, the theory also predicts the magnitude (vertical shift in the log-log  
660 plot of ensemble response as in **Fig 3C**), that is,  $r(x) \approx (1 + \frac{7\lambda^2}{4n^2}) e^{\lambda(x+k_0)}$ , which explains how  
661 the Hill coefficient affect the ensemble response.

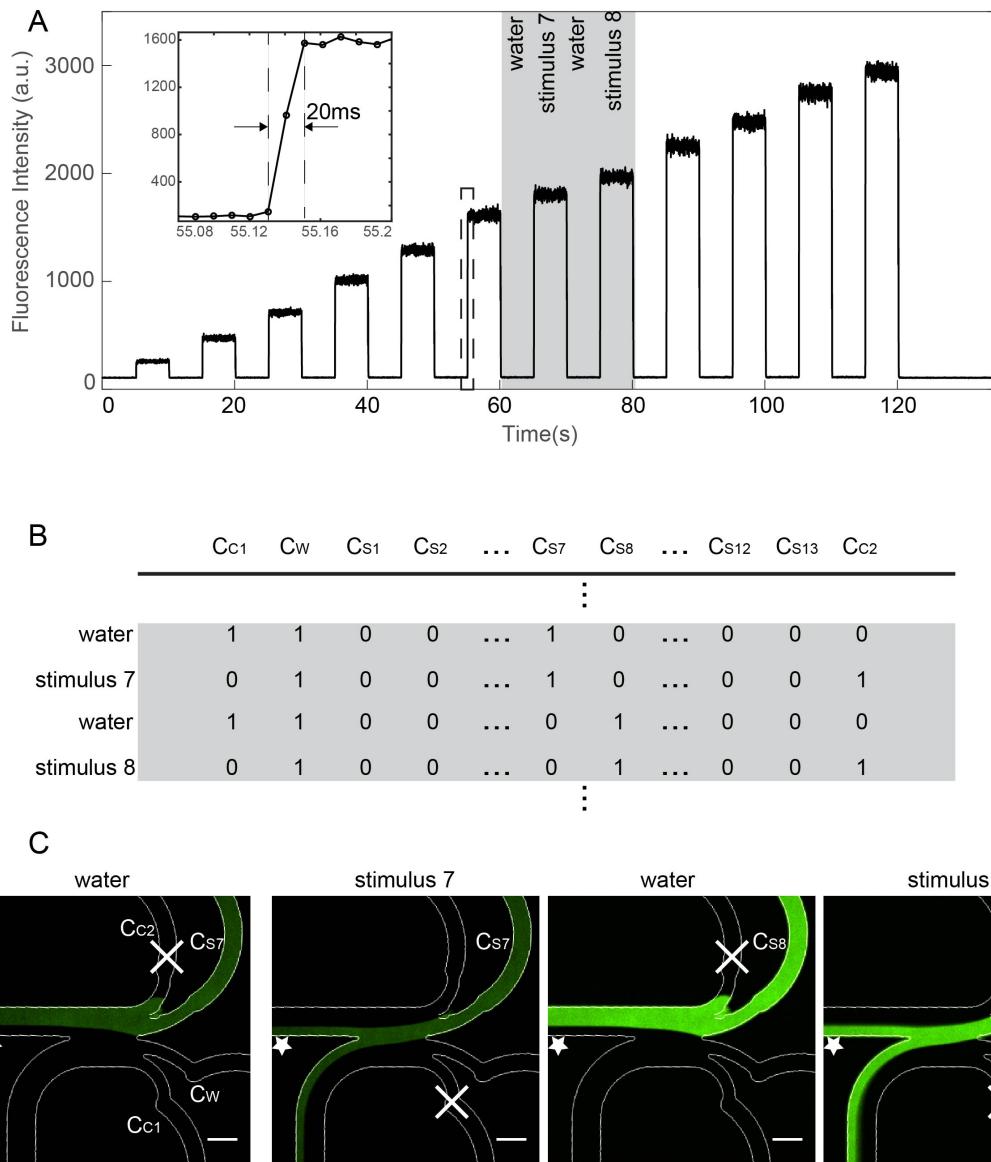
662

663 **Reverse-correlation analysis**

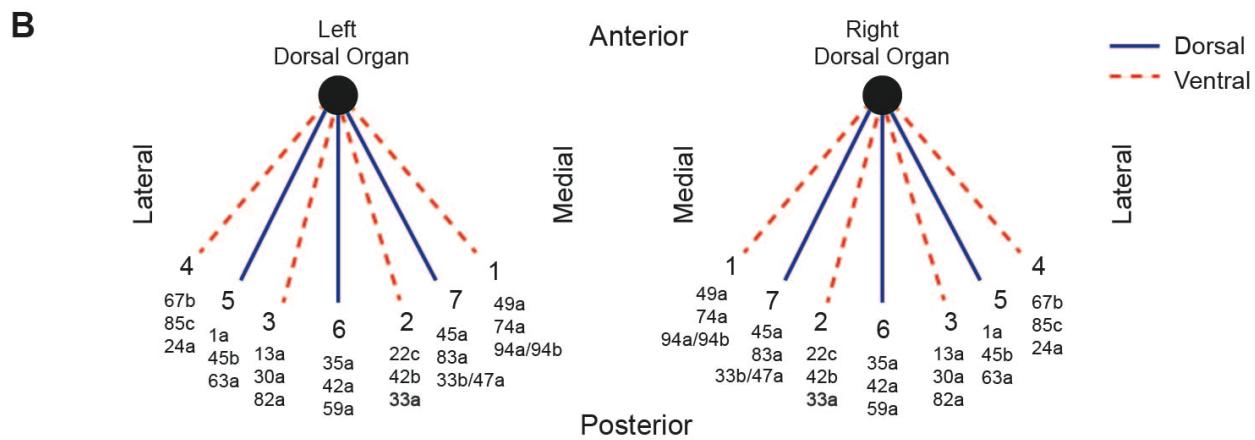
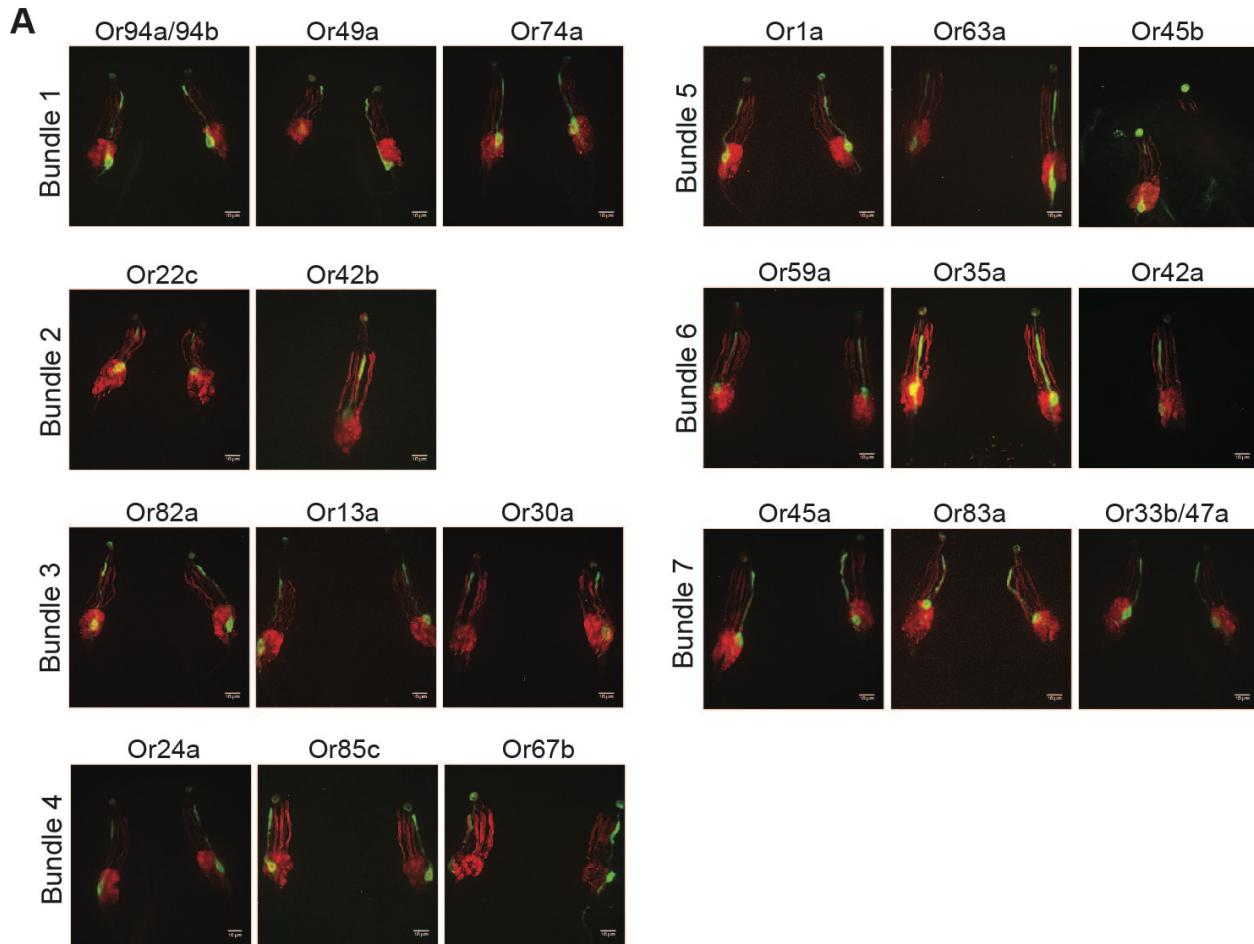
664 White noise experiments were performed in a manner similar to those described in Kato, et. al,  
665 (2014). Briefly, we used custom code written in MATLAB to control odorant and water switching  
666 such that it followed an m-sequence. Calcium imaging was performed on the axon terminal of  
667 individual ORNs at ~30 frames per second. Calibration and an example of such a recording is  
668 shown in **Movie 2**. We then used a linear-nonlinear model to compare the m-sequence input to  
669 ORN responses during a 150second interval (from 60 - 210 sec). An 18 second time window  
670 was used for the linear filter, of which 15 seconds represented stimulus history in order to  
671 ensure extraction of the full filter dynamics (**Supp Fig 7B**). Next, we applied the linear filter to  
672 the data and compared this to the output in order to capture the nonlinear function. We found  
673 that a sigmoidal function fits the nonlinear function well (**Supp Fig 7C**). We applied novel m-  
674 sequences to validate the linear-nonlinear model (**Supp Fig 7D**) and found that they fit the data  
675 well. Peak and decay times for each filter were found by extracting the time points  
676 corresponding to the maximum amplitude and half maximum amplitude of the decay phase,  
677 respectively. 454 filters were calculated from the recording of 138 larvae responding to various  
678 m-sequence stimuli. Each of the 31 filters quantified in **Supp Fig 7**, are averaged across 10  
679 trials.

680

681 Data, code and software can be found at: [https://github.com/samuellab/larval\\_olfaction](https://github.com/samuellab/larval_olfaction)  
682 Microfluidic device pattern design can be found at:  
683 [https://metafluidics.org/devices/larval\\_olfaction/](https://metafluidics.org/devices/larval_olfaction/)

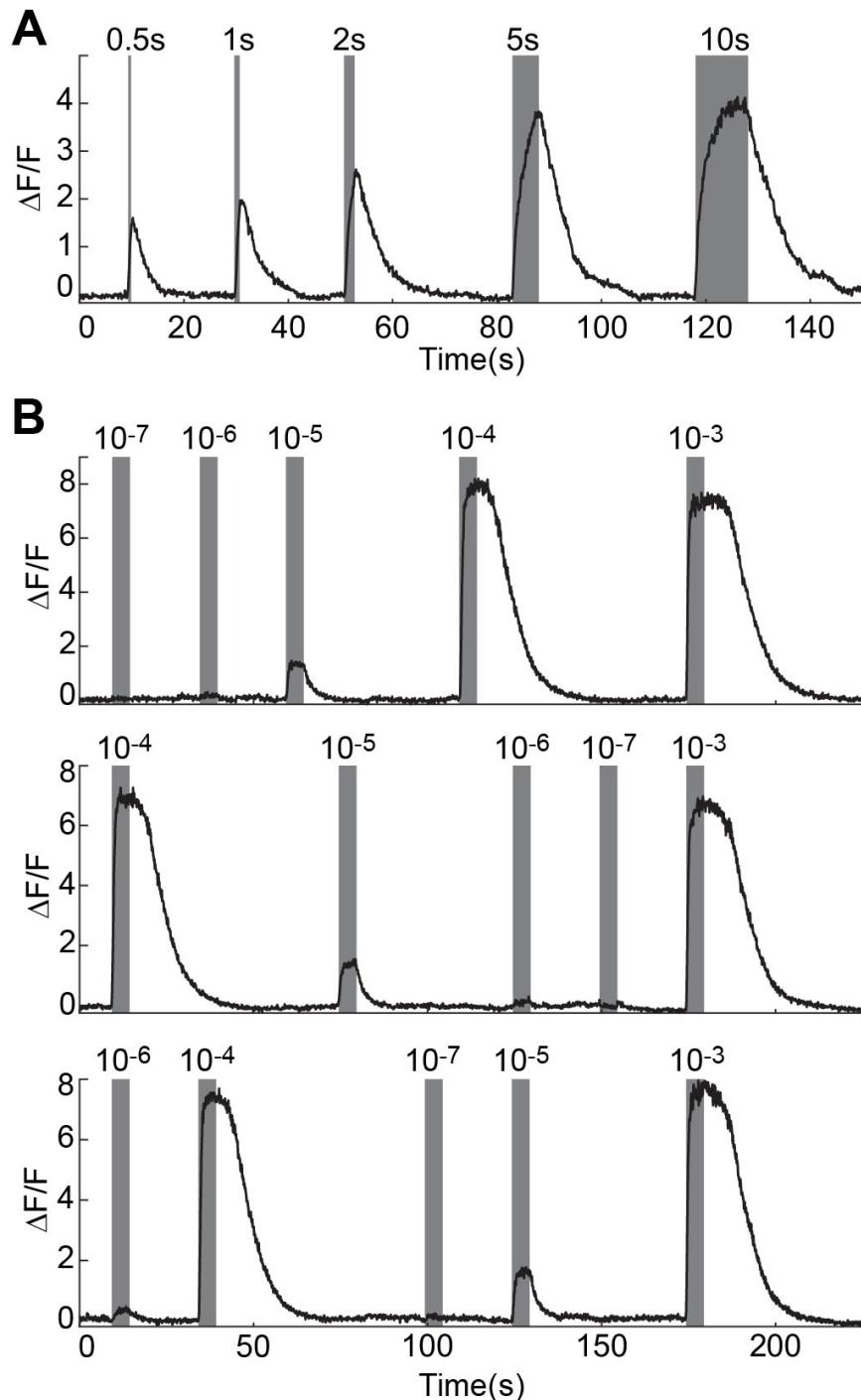


685 **Supplementary Figure 1. Validation of temporal and spatial odorant profiles in**  
686 **microfluidics device, using a fluorescent dye.** A. Change in fluorescence intensity during  
687 delivery of 5 sec step pulses of increasing concentration of fluorescein dye, each followed by 5  
688 second of water. Inset shows zoom-in of dashed box, indicating stimulus transition time is ~20  
689 ms. B. Combination of valve states required to generate the stimulation sequence in shaded  
690 area of panel A; 1 and 0 indicate valve is open or closed, respectively.  $C_w$  represents water  
691 channel,  $C_{c1}$  and  $C_{c2}$  represent control channels that allow stimulus switching, and  $C_7$  and  $C_8$   
692 represent odorant delivery channels and only open prior to and during stimulus delivery. C.  
693 Images of fluorescein dye, representing an odorant stimulus, in the microfluidics device during  
694 each state shown in panel B (water, stimulus 7, stimulus 8). Cross mark indicates closed  
695 channels, star marks the location of the larva's "nose". Scale bar is 300  $\mu$ m.



696

697 **Supplementary Figure 2. Anatomical map of ORN dendritic organization.** A. Image of each  
698 ORN's dendritic location using GFP to label a specific ORN and RFP to label all ORNs. Larvae  
699 expressing *OrX>GFP*, *Orco>RFP*, where *OrX* is a specific olfactory receptor. We infer the  
700 vacancy in bundle 2 is *Or33a*. During functional imaging, there were no strong signals from this  
701 neuron. No expression of *Or2a* and *Or7a* were observed in first instar larvae. B. Summary  
702 schematic of stereotyped ORN position in each dendritic bundle for left and right dorsal organs.



703

704 **Supplementary Figure 3. Effect of stimulus duration and sequence on ORN response. A.**

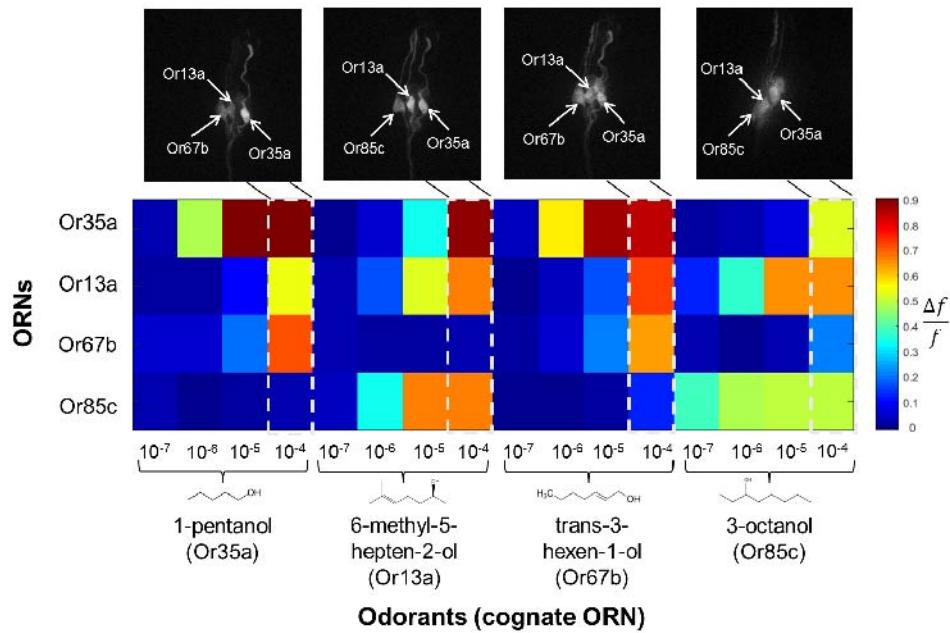
705 Or35a-ORN responses to 0.5, 1, 2, 5 and 10 seconds of  $10^{-5}$  dilution of 3-octanol. The

706 maximum response saturates when odorant pulse is longer than 5 seconds. B. Or35a-ORN

707 response to increasing (top panel), primarily decreasing (middle panel), and random (bottom

708 panel) concentration sequences of 3-octanol pulses, delivered at 5 seconds each. The response

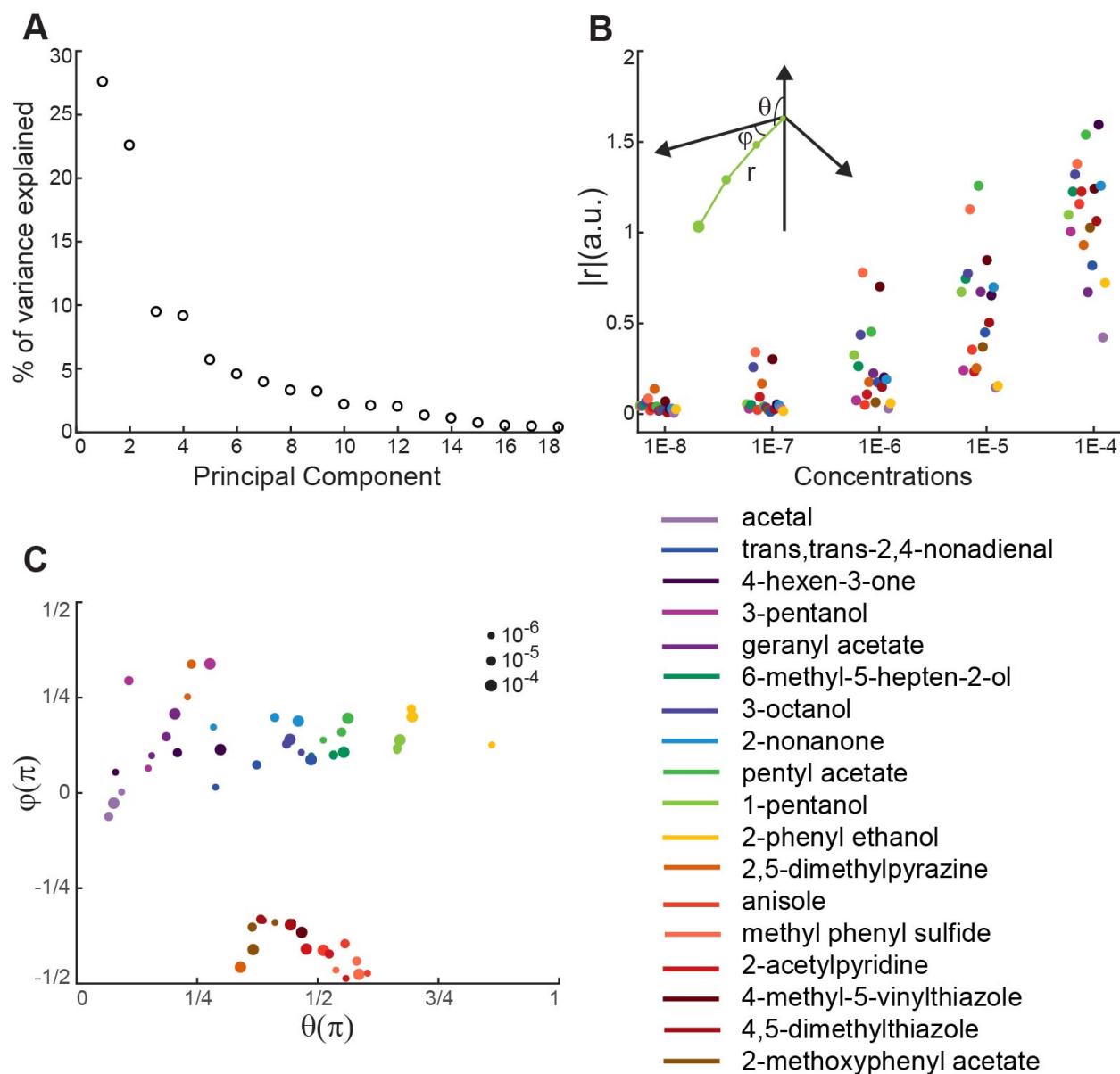
709 amplitude to each concentration level is history independent.



710

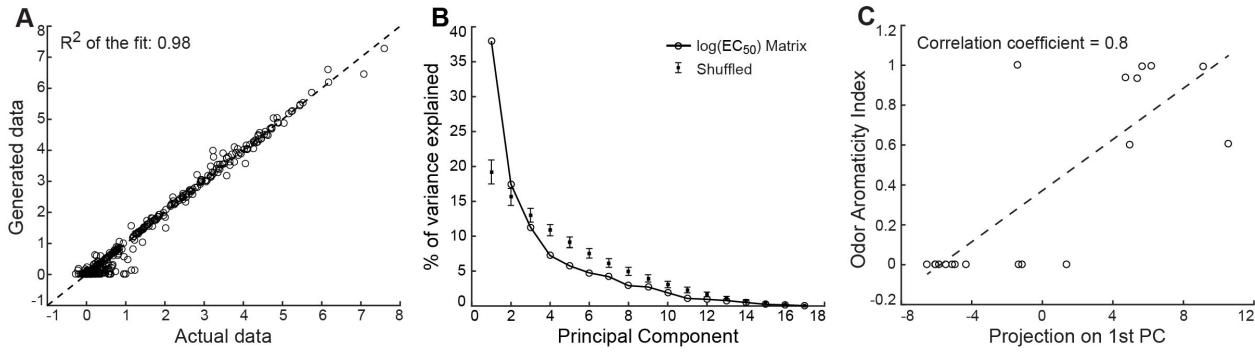
711 **Supplementary Figure 4. Coactivation of ORNs with similar cognate odorants at high**  
712 **concentrations.** Heatmap of peak responses of four ORNs to four alcohol odorants, across  
713 four concentrations of each odorant. Activities normalized by maximum response amplitude.  
714 Neural images show responsive ORNs in dorsal organ ganglion during calcium imaging at the  
715 highest odorant concentrations.

716



717

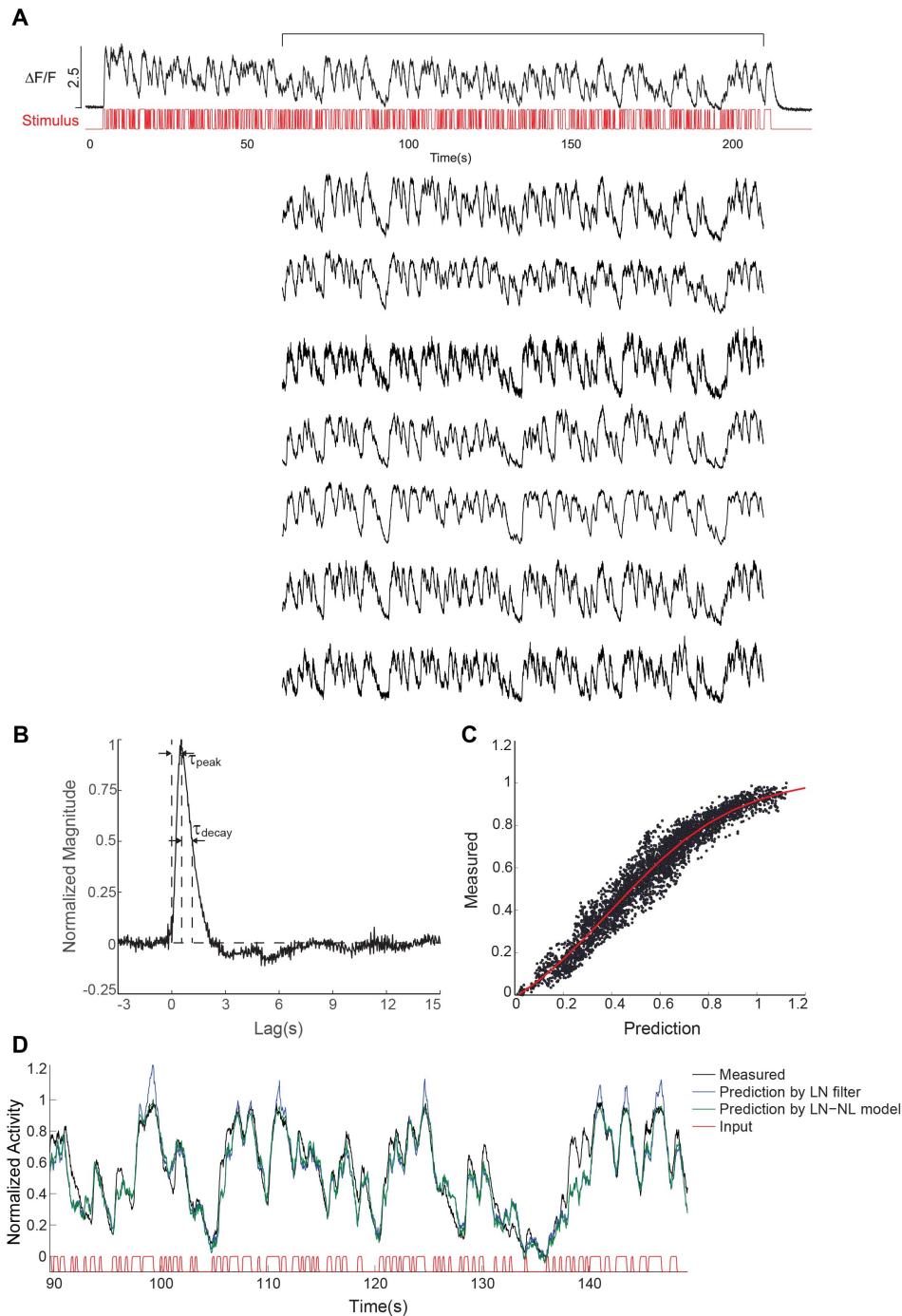
718 **Supplementary Figure 5. PCA analysis of ORN dose-response data.** A. Percentage of  
 719 variance explained by each principal component. B. and C. Transform of odorant vectors in  
 720 PCA space (Fig 2B) to spherical coordinates (inset of B). Odorant vector length increases  
 721 monotonically with increasing concentration. Angular direction of different odorants (represented  
 722 by dot color) separate, but aggregate for direction of different concentrations of the same  
 723 odorant (dot size).

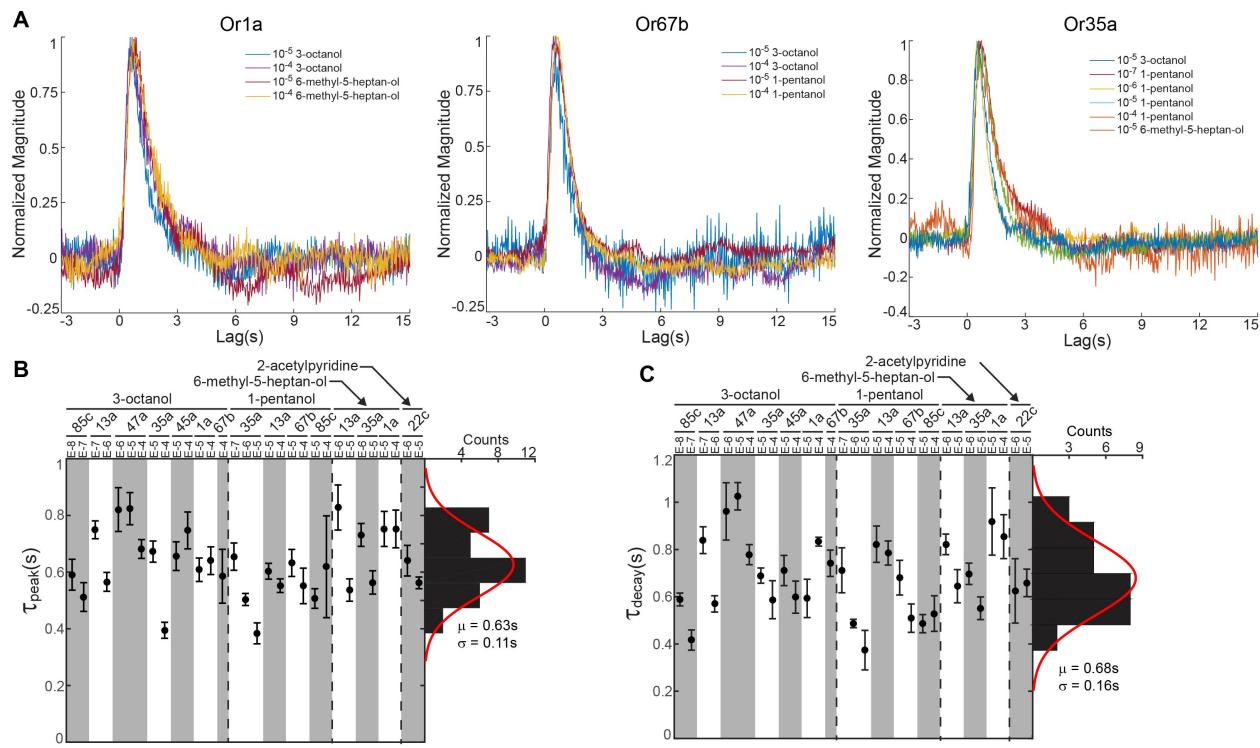


724

725 **Supplementary Figure 6. Aromaticity index highly correlated to major PC of EC<sub>50</sub> matrix.**

726 A. Actual neural activity data is highly correlated with simulated data generated using the Hill  
727 equation and fitted parameters. Scatter plot includes all non-zero data in **Fig 2A**. Dashed line  
728 indicates  $y = x.R^2$  is 0.98. B. Percentage of variance explained by each PC of the PCA on the  
729  $-\ln (EC_{50})$ . Data compared with the corresponding results from 1000 randomly shuffled data. C.  
730 Correlation plot between each odorants projection on the 1<sup>st</sup> PC of  $-\ln (EC_{50})$  matrix and its  
731 aromaticity index.





739

740 **Supplementary Figure 8. Comparison of ORN temporal filters.** A. Normalized filters of three  
 741 ORNs responding to various odorant stimuli. B. and C. Distribution of peak time (B.) and decay  
 742 time (C.) of 31 filters measured from various ORN and odorant stimuli. Distributions of peak and  
 743 decay times were fit to Gaussian distributions with mean and variance labeled below histogram.  
 744

745 **Movie 1. Dose-dependent activation of ORNs.** Left: Calcium imaging of 21 pairs of larval  
 746 ORNs in response to increasing concentrations of the 1-pentanol odorant, from  $10^{-7}$  to  $10^{-3}$   
 747 dilutions. Movie starts by scanning through the imaging volume to identify ORNs activated at the  
 748 highest concentration level. Three ORNs are responsive on the left side and five on the right  
 749 side. ORN identity was confirmed from the dendrite location and response to panel of 13  
 750 cognate odorants (not shown in the movie). Right: Responses of ORNs to step pulses of  
 751 odorant stimuli.

752

753 **Movie 2. ORN responses to pseudorandom white noise stimulus.** Top left, stimulus delivery  
 754 marked by fluorescence. Bottom left, axon terminal of Or45a-ORN responding to the white noise  
 755 stimulus using  $10^{-7}$  dilution of 2-nonenone. Top and bottom right, real time plots of the input  
 756 stimulus and ORN response during an experiment.

757

758 **Supplementary Table 1.** Raw activity data of 21 ORNs responding to 19 odorants at five  
759 concentration levels collected from 122 recordings.

760 **Additional references:**

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