1   Energy Coupling and Stoichiometry of Zn^{2+}/H^+ Antiport by the Cation Diffusion Facilitator YiiP

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8   ABSTRACT

9   YiiP is a prokaryotic Zn^{2+}/H^+ antiporter that serves as a model for the Cation Diffusion Facilitator
10   (CDF) superfamily, members of which are generally responsible for homeostasis of transition
11   metal ions. Previous studies of YiiP as well as related CDF transporters have established a
12   homodimeric architecture and the presence of three distinct Zn^{2+} binding sites named A, B, and
13   C. In this study, we use cryo-EM, microscale thermophoresis and molecular dynamics
14   simulations to address the structural and functional roles of individual sites as well as the
15   interplay between Zn^{2+} binding and protonation. Structural studies indicate that site C in the
16   cytoplasmic domain is primarily responsible for stabilizing the dimer and that site B at the
17   cytoplasmic membrane surface controls the structural transition from an inward facing
18   conformation to an occluded conformation. Binding data show that intramembrane site A, which
19   is directly responsible for transport, has a dramatic pH dependence consistent with coupling to
20   the proton motive force. A comprehensive thermodynamic model encompassing Zn^{2+} binding
21   and protonation states of individual residues indicates a transport stoichiometry of 1 Zn^{2+} to 2-3
22   H^+ depending on the external pH. This stoichiometry would be favorable in a physiological
23   context, allowing the cell to use the proton gradient as well as the membrane potential to drive
24   the export of Zn^{2+}.

25

26 ## INTRODUCTION

27   YiiP is a bacterial Zn^{2+}/H^+ antiporter and a well characterized representative of the
28 Cation Diffusion Facilitator (CDF) superfamily. Members of this family play important roles in
29 homeostasis of transition metal ions such as Zn^{2+}, Mn^{2+}, Co^{2+}, and Fe^{2+} (Montanini et al., 2007).
30 Mn^{2+} transporters from this superfamily are prevalent in plants, where this metal ion is essential
31 for oxygen generation by photosystem II as well as for a variety of other enzymatic functions
32 (Alejandro et al., 2020). Zn^{2+} CDF transporters are widespread in organisms from all kingdoms
33 of life reflecting a large influence of this ion on cell biology. An estimated 10% of proteins
34 employ Zn^{2+} either as a catalytic co-factor (e.g., carbonic anhydrase and cytochrome C oxidase)
35 or as a structural element (e.g., Zn-finger transcription factors and steroid receptors) (Maret,
36 2013). In mammals, high concentrations are found in a variety of intracellular vesicles that are
37 key players in the immune system, synaptic transmission, insulin trafficking, and fertilization
38 (Kambe et al., 2015). Zn^{2+} figures in host-pathogen interactions, with the host attempting to
39 either deprive or poison pathogens residing in endosomes (Lonergan and Skaar, 2019). Despite
40 its prevalence, the bulk of intracellular Zn^{2+} is bound to protein, with vanishingly small ($<10^{-12}$ M)
41 concentrations of free Zn^{2+} in the cytoplasm (Liang et al., 2016; Outten and O'Halloran, 2001).
42 Homeostasis is maintained by CDF transporters, which generally export Zn^{2+} from the
43 cytoplasm, as well as members of the Zinc-regulated or Iron-regulated transport Proteins (ZIP),
44 P-type ATPase and ATP-binding cassette (ABC) superfamilies (Yin et al., 2022).

45   YiiP serves as a model for studying structural and mechanistic properties of CDF
46 transporters. Structures of homologs from both *E. coli* and *S. oneidensis* in different
47 conformational states provide a framework for describing the archetypal alternating access
48 mechanism (Lopez-Redondo et al., 2021; Lopez-Redondo et al., 2018; Lu et al., 2009; Lu and
49 Fu, 2007). Molecular Dynamics has been used to study dynamics (Sala et al., 2019), to define
50 the transport pathway (Sharma and Merz, 2022) and, together with in vitro binding assays, to
51 characterize the K_d and pKa of Zn binding sites. Our understanding of CDF transporters is
52 amplified by recent MD simulations of Znt2 (Golan et al., 2018; Golan et al., 2019), cryo-EM
53 structures of Znt8 (Daniels et al., 2020; Xue et al., 2020; Zhang et al., 2023) and Znt7 (Han et
54 al., 2022), as well as X-ray structures of isolated cytoplasmic domains from a number of
55 different species (Udagedara et al., 2020). Together, these studies establish characteristics of
56 Zn^{2+} binding sites, a conserved homodimeric architecture, and the nature of inward-facing (IF)
57 and outward-facing (OF) states that presumably characterize all CDF transporters.

58   Despite this extensive work, there is uncertainty about key mechanistic questions that
59 we have sought to address in the current work. Our primary goal was to obtain experimental
60 evidence for the individual roles of the three Zn^{2+} binding sites found on each YiiP protomer
61 (Cotrim et al., 2019). Site A is within the transmembrane domain (TMD) and features three Asp
62 and one His residues; it is alternately exposed to the cytoplasm or to the periplasm in IF and OF
63 states, respectively, and is thus directly responsible for transport of ions across the membrane.
64 Although each molecule composing the dimer appears to have an independent transport
65 pathway, there is unresolved potential for cooperativity. Site C within the C-terminal domain
66 (CTD) is a binuclear site featuring four His and two Asp residues; one of these sites (C1) is well
67 conserved whereas the other (C2) is not (Parsons et al., 2018). Site B is on the loop between
68 transmembrane helices 2 and 3 (TM2-TM3) featuring two His and one Asp residue. Despite a
69 lack of sequence homology for sites B and C2, the structure of Znt8 showed Zn ions at similar
70 locations of the tertiary fold, but bound at different locations in the linear sequence, suggesting
71 that these non-conserved, auxiliary sites may have functional significance (Xue et al., 2020).

72   Another goal was to address the role of protons in the transport process. There is ample
73   evidence supporting Zn^{2+}/H^+ antiport. In vitro assays with Znt1, Znt2, ZitB and CzcD showed pH
74   dependence of transport (Chao and Fu, 2004a; Cotrim et al., 2021; Guffanti et al., 2002;
75   Shusterman et al., 2014). Binding studies with Znt8 (Zhang et al., 2023) as well as
76   computational studies with Znt2 (Golan et al., 2019) and YiiP (Sharma and Merz, 2022) showed
77   an interplay between Zn^{2+} and H^+ binding at site A. However, there are discrepancies in
78   stoichiometry, with work on ZitB (Chao and Fu, 2004a) and YiiP (Chao and Fu, 2004b)
79   supporting a 1:1 exchange of Zn^{2+} and H^+, whereas studies of CzcD (Guffanti et al., 2002) and
80   Znt2 suggest 1:2 (Golan et al., 2019). There is also recent evidence for Zn^{2+}/Ca^{2+} antiport by
81   Znt1 in neurons (Gottesman et al., 2022).

82   For the current study, we have generated mutants of YiiP and have used cryo-EM and
83   microscale thermophoresis (MST) to measure the pH dependence and structural effects of Zn^{2+}
84   binding at each of the three sites. In addition, we have used molecular dynamics (MD)
85   simulations together with the experimental MST data to deduce the pKa of residues at these
86   sites and to address the stoichiometry of transport. From these data, we conclude that Zn^{2+}
87   binding at site C is responsible for the integrity of the homodimer. Release of Zn^{2+} from site B
88   triggers a conformational change in which the transport site A becomes occluded, suggesting a
89   potential relay of Zn^{2+} between these two sites. Occlusion of only one protomer breaks the
90   symmetry of the dimer and suggests that the transport process is not cooperative. In addition,
91   binding affinity at site A displays a dramatic pH dependence, which can be explained by the
92   protonation of 2 or 3 of the residues comprising this site. A corresponding Zn^{2+}/H^+ antiport
93   stoichiometry of 1:2 or 1:3, depending on pH, is consistent with energetic coupling of Zn^{2+} export
94   to the proton-motive force in a physiological setting.

95

RESULTS

Mutants used to study the structural effects of Zn^{2+} binding

In order to study effects of Zn^{2+} binding at individual sites, we produced mutants of YiiP from *Shewanella oneidensis*. The D51A mutation was introduced to preclude binding at site A and D70A to preclude binding at site B. For site C we mutated Asp287, because it bridges the two Zn^{2+} ions at that site and we anticipated that D287A would therefore eliminate both ions. The wild-type (WT) protein studied in previous work (Coudray et al., 2013; Lopez-Redondo et al., 2021; Lopez-Redondo et al., 2018) served as a positive control. For each of these constructs, protein was expressed in *E. coli*, solubilized in decyl-β-D-maltoside and purified by affinity chromatography. To ensure binding of Zn^{2+} rather than other metal ions picked up during growth and initial purification (e.g., Ni^{2+}), we incubated the protein overnight with chelators and then added 250 μM Zn_2SO_4 prior to the final purification step. As in previous work (Lopez-Redondo et al., 2021), we used an Fab antibody fragment to produce a larger complex amenable to cryo-EM analysis: 165 kDa comprising the YiiP homodimer (65 kDa) bound to two Fab's (50 kDa each).

Site A: D51A mutation

The structure of the D51A complex was solved at 3.6 Å resolution (Fig. 1b, Suppl. Fig. 1, Table 1) revealing an architecture very similar to untreated, WT YiiP (PDB code 7KZZ) that represents the IF, holo state (Lopez-Redondo et al., 2021). Specifically, YiiP formed a two-fold symmetric homodimer with Fab molecules bound near the C-terminus of each CTD. Density for Zn^{2+} ions is clearly visible at sites B and C (Suppl. Fig. 2e and f). At site A, however, this structure lacked density (Suppl. Fig. 2d), confirming that the D51A mutation effectively eliminated binding at this site.

For comparison, we solved the structure from the WT construct that was similarly loaded with Zn^{2+}. As expected, this 3.8 Å resolution structure (Fig. 1a, Suppl. Fig. 1) is indistinguishable from 7KZZ, which is also from the WT construct but not treated with chelators or explicitly loaded with Zn^{2+} (RMSD 1.07 Å for all 562 Cα atoms), Despite overall similarity, comparison with the D51A structure showed movements of TM1, TM4 and TM5 (Fig. 2a), which resulted in a notably elevated RMSD for this region: 4.7 Å based on the corresponding 200 Cα atoms compared to 0.69 Å for the 352 residues composing the rest of the YiiP dimer. The cytoplasmic end of TM5 had the largest differences. Specifically, a kink is introduced near His155 and the TM4-TM5 loop is disordered (Suppl. Fig. 2d), suggesting a flexibility of this region in the absence of Zn^{2+} at site A.

Site B: D70A mutation

An initial structure of the D70A construct revealed a global conformational change reminiscent of the previously solved WT, apo state (PDB 7KZX) produced by removal of Zn^{2+} with chelators (Lopez-Redondo et al., 2021). The most salient feature of this conformation is a kink between TMD and CTD, which disrupts the overall two-fold symmetry of the complex. During image processing, it became evident that there were in fact multiple conformations in the dataset from D70A, which ultimately generated two distinct structures at 4.0 and 3.9 Å resolution (Fig. 1c, Suppl. Fig. 3). Unlike the WT, apo structure (7KZX), both of these new structures revealed densities at sites A and C (Suppl. Fig. 2g,i,j, and l), consistent with Zn^{2+} binding to intact sites. However, the two structures differed both in the conformation of the TMD and in the orientation of the CTD. One of these structures, termed D70A_sym, has a TMD

140   displaying local two-fold symmetry, in which both protomers adopt the IF state (Fig. 2b). Like the
141   WT, apo structure, the TM2/TM3 loops, which harbor Asp70 and site B, are disordered. In the
142   other structure, termed D70A_asym, one TMD adopts the IF state with a disordered TM2/TM3
143   loop, whereas the other TMD adopts a novel conformation in which the TM2/TM3 loop extends
144   ~17 Å away from the membrane to interact with H1 and β1 elements of the CTD from the
145   opposing protomer (Fig. 2c, Suppl. Fig. 5b). In addition to reconfiguring this loop, there are
146   movements in TM1,2,4,5 (Fig. 2d) that close off site A from the cytoplasm. This occlusion is
147   documented by the considerably smaller radius of the cavity leading to this site (Suppl. Fig. 13).

148   Despite these changes, local dimeric elements from the D70A structures superimpose
149   closely onto the corresponding elements from the WT, holo structure. In particular, alignment of
150   CTD's produces low RMSD's of 0.82 Å and 1.08 Å relative to D70A_sym and D70A_asym,
151   respectively (168 Cα atoms). The core helices mediating the TMD dimer interface (TM3/6) also
152   align closely with WT with RMSD's of 0.79 Å and 1.22 Å for D70A_sym and D70A_asym (106
153   Cα atoms, Fig. 2b, d). For D70A_sym, the entire TMD is generally consistent with the WT, holo
154   structure (Fig. 2b), though slight displacement of TM1,4,5 and bending of the cytoplasmic end of
155   TM2 lead to a somewhat elevated RMSD of 2.1 Å for 366 Cα atoms from both protomers after
156   alignment based on TM3/6. For D70A_asym, the TMD in the IF conformation has a similar
157   RMSD of 2.6 Å relative to WT, holo (183 Cα atoms from protomer B, Fig. 2d), whereas the
158   occluded TMD has an elevated RMSD of 5.8 Å (197 Cα atoms from protomer A after aligning
159   TM3/6) due to large differences in the cytoplasmic ends of TM1,2,4,5.

160   The observed structural effects of the D70A mutation are broadly consistent with MD
161   simulations based on the WT structure. In particular, when site B was empty, the TM2/TM3 loop
162   exhibited greatly increased mobility documented by >2-fold increase in root mean square
163   fluctuations (RMSF, Fig. 3a); this result is consistent with disorder of this loop in D70A cryo-EM
164   structures. The CTD also exhibited increased mobility as documented both by the broader
165   distribution of the angles relative to the TMD (Fig. 3d) and by per residue RMSF, in particular
166   when the TMD was used as reference for alignment (Fig. 3b), indicating that the CTD moved as
167   a fairly rigid body relative to the TMD. In structures with Zn^{2+} bound at site B, the TM2/TM3 loop
168   from one protomer is close to the linker between TM6 and the CTD of the opposing protomer
169   (Fig. 3e,f, Suppl. Fig. 2b,e, and n). We therefore used the distance between Cα atoms of Asp72
170   in the TM2/TM3 loop and Arg210 in the TM6/CTD linker from the opposing chain as a collective
171   variable for tracking CTD movement. The corresponding distance distributions (Fig. 3c) are
172   broader and extend to larger values when site B is empty. In simulations of the D72A mutant
173   with Zn^{2+} bound at site B there is a marked increase in CTD/TMD angle (Fig. 4d) as well as a
174   more modest increase in the distance distribution (Fig. 4c). These results, together with
175   structures of D70A_sym and WT, apo, suggest that a salt bridge between Asp72-Arg210 helps
176   maintain the symmetry seen in the holo state. Release of Zn^{2+} from site B causes disordering of
177   the TM2/TM3 loops leading to loss of the salt bridge and thus greater mobility of the CTD.
178   However, the D70A_asym structure indicates that this disordering is transient, as the loop
179   adopts the extended conformation and associates with different elements of the CTD (Fig. 2c).
180   Interestingly, this novel change in the TM2/TM3 loop is coupled with movements of TM1,2,4,5
181   that close site A off from the cytoplasm (Fig. 3i-j, Suppl. Fig. 13). Mapping of electrostatic
182   charge shows that whereas the access channel to site A in the IF protomer is negatively
183   charged, positive charge dominates the cytoplasmic surface of the protomer in the occluded
184   conformation (Fig. 3k,l).

Site C: D287A and D287A/H263A mutations

The D287A mutant was chosen to disrupt site C since it coordinates both Zn^{2+} ions at this site. However, the corresponding structure (3.7 Å resolution, Fig 1d, Suppl. Fig. 4) shows no structural changes relative to the WT structure (1.18 Ä RMSD for all 562 Cα atoms) and Zn^{2+}-related densities are still clearly visible at site C (Suppl. Fig. 2o). We therefore introduced a second mutation, D287A/H263A, and the corresponding particles had an unusual appearance consistent with formation of higher order oligomers (Suppl. Fig. 4b). This observation suggested that site C may be responsible for the integrity of the homodimer. Indeed, SEC elution profiles of the YiiP-Fab complex show that the main peak from D287A/H263A is shifted relative to the other mutants (from 11.1 to 10.1 ml, c.f., Suppl. Figs. 1a,b, 3a, 4a,b). Elution profiles from complexes formed with D70A and D287A also have an earlier peak at ~10 ml and, in both cases, image processing revealed a relatively small subpopulation of particles forming a dimer of dimers (Suppl. Fig. 3c & 4e). However, for D287A/H263A, this dimer of dimers represents the main peak and the only class of particles that could be refined to high resolution (3.5 Å) (Suppl. Fig. 4h). For D287A/H263A, higher order oligomers are apparent during 2D and 3D classification (Suppl. Fig. 4d & f) and are likely to explain the earlier elution peak at 8-9 ml.

The dimer of dimers from D287A/H263A is stabilized by an unprecedented domain swap in which CTD's and TMD's affiliate with different protomers (Fig. 2g). This domain swap is enabled by a structural transition of the linker between the TMD and the CTD. In particular, the normally unstructured loop between TM6 and the first helix of the CTD (H1) is reconfigured into a very long, continuous α-helix extending from the N-terminus of M6 (Trp178) to the C-terminus of H1 (Glu226). Site C itself is completely disordered and the CTD's are splayed apart (Figs. 2g & Suppl. Fig. 5c): i.e., the distance between Cα atoms of Arg237 and Glu281 is 22.7 Å compared to ~12 Å in structures with an intact site C (Lopez-Redondo et al., 2021). This domain swap was not observed in the dimer-of-dimers formed by D70A and D287A, where the CTD and site C were unperturbed and Fab molecules were uniquely responsible for inter-dimer interactions. Although it was not possible to refine a structure from the higher-order oligomers from D287A/H263A, due to heterogeneity and preferred orientation, they appeared to comprise a linear chain of molecules propagated via this domain swap. These surprising changes in the CTD indicate that site C is indeed crucial in maintaining the integrity of the native homo-dimer. Despite the domain swap, however, TMD's from the D287A/H263A complex are quite congruent with the WT structure (RMSD 1.35 Å for 346 Cα atoms excluding the TM2/TM3 loop) and density for Zn^{2+} ions is clearly visible at site A (Suppl. Fig. 2p). Weak density is visible for the TM2/TM3 loops, indicating that they adopt an extended configuration that disrupts site B and allows them to interact with the CTD; it does not appear that Zn^{2+} is bound at site B in this domain-swapped complex (Suppl. Figs. 2q and 5c,d).

Zn^{2+} binding affinity

To assess the binding affinity of individual Zn^{2+} binding sites, we used MST to analyze a series of mutants designed to isolate the individual sites (Fig. 4 and Suppl. Fig. 6). Specifically, the triple mutant D70A/D287A/H263A was used to study site A, D51A/D287A/H263A to study site B, and D51A/D70A to study site C. To maintain accurate and reproducible Zn^{2+} concentrations ranging from nanomolar to micromolar, we used nitrilotriacic acid (NTA, K_d = 14 nM) to buffer Zn^{2+} for sites with high affinity, and citrate (K_d = 12 μM) for sites with lower affinity. At pH 7, sites A and C displayed relatively high affinity (K_d = 16 and 33 nM, respectively, Table 2, Fig. 4), whereas site B had considerably lower affinity (K_d = 1.2 μM). Site C is

230 binuclear, and the apparent affinity was reduced when further mutations were introduced to
231 isolate individual C1 (D51A/D70A/H263A with K_d = 153 nM) and C2 (D51A/D70A/H234A with K_d
232 = 223 nM) sites, suggesting cooperative binding of ions at C1 and C2 as implied by the
233 coordination geometry of this site (Fig. 1d inset).

234   To explore the basis for coupling of Zn^{2+} transport to the proton-motive force, we
235 measured Zn^{2+} binding affinity at pH values from 5.6 - 7.4. We found that affinity at site A
236 changed by five orders of magnitude: K_d ranging from 1 nM at pH 7.4 - consistent with the
237 cytosol - to 302 μM at pH 5.6 (Fig. 4a, Table 2). Site B had only modest pH dependence ranging
238 from 1-16.6 μM, whereas Site C changed by two orders of magnitude from 0.033 - 6.7 μM.
239 Cooperativity at site C is consistent with a high Hill coefficient at pH 7 (n=2.9), which fell below 1
240 at lower pH's. However, Hill coefficients obtained for other sites were quite variable (Table 3),
241 including those for sites C1 and C2, making conclusions about cooperativity inconclusive.

242   The domain swap seen in cryo-EM structures of D287A/H263A raises concern that site
243 C mutations might affect affinity measured at other sites. However, in the absence of Fab, all of
244 the mutants used for MST studies eluted from SEC columns at the same volume as WT (Suppl.
245 Fig. 6a-d) indicating that they all adopted the native dimeric structure. This observation suggests
246 that the domain-swapping seen in the structure of D287A/H263A was induced by the Fab
247 molecules. This conclusion is supported by direct comparison of preparations with site C
248 mutations before and after addition of Fab (Suppl. Fig. 6 h & i). In the absence of Fab, they both
249 elute from SEC as a single peak at the expected volume of 12 ml. In the presence of Fab, there
250 is a shift of the main peak consistent with formation of a higher molecular weight complex and,
251 additionally, appearance of a second peak. In the case of D287A-Fab, the main peak at 11.1 ml
252 is consistent with the YiiP-Fab complex seen for the other mutants (Suppl. Fig. 1 & 3) and the
253 second peak at 9.9 ml is consistent with the dimer of native homodimers seen during image
254 processing. In the case of D287A/H263A, the main peak in the presence of Fab is at 10.1 ml
255 and thus consistent with a dimer of domain-swapped dimers and the secondary peak at 8.6 ml
256 is consistent with higher order oligomers seen during cryo-EM processing (Suppl. Fig. 4). In
257 addition, we performed MST analysis with the D70A/D287A mutation as an alternative for
258 measuring affinity at site A. The cryo-EM structure of D287A shows that the native homodimeric
259 assembly is retained and although Zn^{2+} was observed at site C, we expect it will bind at lower
260 affinity and thus not overlap with higher affinity binding at site A. Indeed, this construct produced
261 Kd= ~1 nM at pH 7 and ~6 μM at pH 6, which is consistent with results from
262 D70A/D287A/H263A (Table 2), thus confirming the pH dependence of site A.

263   We also used MD simulations in conjunction with the experimental MST data to address
264 pH dependence of Zn^{2+} binding and to evaluate the contribution of individual residues. To start,
265 we estimated pKa values for each titratable residue at site A (Asp47, Asp51, His155 and
266 Asp159) and site B (Asp70, His73 and His 77) using constant pH MD (CpHMD) simulations with
267 pH replica exchange (Huang et al., 2021) in the absence of Zn^{2+}. It was not possible obtain data
268 for site C because the Zn^{2+}-free CTD proved unstable in CpHMD simulations. These simulations
269 generated probabilities for each protonation state as a function of pH; these probabilities were fit
270 with the Hill-Langmuir equation to derive per-residue pK_a's (Suppl. Figs. 7-9, Table 4). For site A
271 residues, His155 had the highest predicted pK_a (8.0), followed by Asp159 (4.9), Asp47 (3.8) and
272 Asp51 (2.9). Predicted populations of the individual microstates (s0-s15, Suppl. Figs. 10a & b)
273 indicated that two residues are likely protonated at pH 5.5 with His155 getting protonated first
274 followed by Asp159. Although these simulations were conducted with the IF conformation, we

275   do not expect significant differences for the OF state, given the similarity of site A seen in the X-
276   ray structure (Lu et al., 2009) of the OF state (RMSD of 0.49 Å for 17 Cα atoms on TM2 and
277   TM5 and 1.01 Å for all atoms composing the four residues that coordinate the Zn^{2+} ion). For site
278   B, His73 and His77 have almost identical pK_a's of 8.1, and the dominant state at neutral pH
279   consists of both His73 and His77 protonated (Suppl. Figs. 11a & b).

280   We went on to use a thermodynamic model incorporating both protonated and Zn^{2+}-
281   bound states to assess the stoichiometry of transport (Fig. 4h). We used this model to generate
282   Zn^{2+} binding curves based on pK_a's of individual residues and binding free energies for Zn^2
283   derived from the experimental MST data (Table 2). Initially, pK_a's of each residue in the absence
284   of Zn^{2+} were taken from the Hill-Langmuir fits to the CpHMD data (Table 4, Suppl. Fig. 9).
285   However, this CpHMD-based model did not agree with the experimental data (Figs. 4d & e),
286   likely due to inaccuracy in microstate pK_a values. We therefore employed a novel modeling
287   method based on the inverse *Multibind* approach (see Methods) to iteratively refine the CpHMD
288   pK_a's and the MST Zn^{2+} binding free energies using the MST data points as a target for Monte
289   Carlo (MC) minimization. This analysis, referred to henceforth as *MST inference*, allowed us to
290   estimate probabilities of all the microstates as a function of pH and Zn^{2+} concentration (Suppl.
291   Figs. 10 & 11). After refinement of parameters by MST inference, the predicted Zn^{2+} binding
292   curves closely reproduced the observed pH-dependence of Zn^{2+} binding at both sites A and B
293   (Figs. 4f & g). The dramatically improved agreement is a consequence of substantial changes in
294   the pK_a's of individual residues based on the MST inference algorithm (Table 4).

295   A more detailed look at the population of microstates predicted by MST inference allows
296   us to explore the interplay of Zn^{2+} and H^+ binding under physiological conditions. For site A in
297   the absence of Zn^{2+}, the dominant state at cytosolic pH of 7.5 consists of 2 protons bound by
298   His155 and Asp159 (Suppl. Figs. 10c & d). Based on the microscopic pK_a values, we calculated
299   the "coupling energy" (Ullmann, 2003) and thus deduced that these two residues form a coupled
300   system (see Methods). As a result, protonation of His155 and Asp159 is highly cooperative and
301   produces a very steep binding curve (Suppl. Fig. 10e); the singly protonated state is strongly
302   suppressed and the effective pK_a is 7.8 for both residues (Suppl. Fig 10d). At the lower pH of
303   the periplasm, a third proton is recruited by Asp51, whose pK_a increased to 6.5 during
304   refinement by MST inference (Table 4). Regardless of the pH, as Zn^{2+} binds at site A, all the
305   residues are deprotonated (Suppl. Fig. 10f), supporting the idea that Zn^{2+} transport can be
306   coupled with a proton gradient across the plasma membrane. For site B, the dominant state at
307   cytosolic pH in the absence of Zn^{2+} has one protonated residue: either His73 or His77 (Suppl.
308   Fig. 11c & d). Although the microstate pK_a's are equivalent, these site B residues behave quite
309   differently from Site A residues and generate an anti-cooperative binding curve with effective
310   pK_a's of 5.6 and 12.4 (Suppl. Figs. 11e & f). Zn^{2+} binding at cytosolic pH displaces all protons
311   (Suppl. Fig. 11g). Even though protons may co-exist with Zn^{2+} at lower pH's, this is not a
312   physiologically relevant condition given that site B is uniquely exposed to the cytoplasm.

313

DISCUSSION

314   In this study, we have focused on the properties of individual Zn^{2+} binding sites of YiiP
315   from *S. oneidensis*. Previous studies have shown that this protein forms a homodimer in the IF
316   state with Zn^{2+} ions constitutively bound at three sites (Lopez-Redondo et al., 2018). Treatment
317   with EDTA to remove Zn^{2+} from all three sites induced a conformational change to produce an
318   occluded state, a necessary precursor to the OF state (Lopez-Redondo et al., 2021). For the
319   current work, we generated mutations at each site to measure their binding affinities and to
320   assess their respective roles in generating conformational change. We found that site A,
321   considered to be the transport site in the middle of the TMD, has nanomolar affinity at a
322   cytoplasmic pH of 7.4, which is reduced 10^5-fold at the more acidic pH of 5.6. Release of Zn^{2+}
323   from site A induces only modest movement of the peripheral transmembrane helices, but has no
324   global effect on the architecture of the homodimer. Site B, on the short loop between TM2 and
325   TM3, has much lower affinity in the micromolar range with relatively little pH dependence. When
326   site B lacks Zn^{2+}, the loop becomes disordered and the protein undergoes a global
327   conformational change leading to an occluded conformation in one of the protomers. Site C, a
328   binuclear site in the CTD that engages residues from both protomers, has relatively high affinity
329   and intermediate pH dependence. When site C was fully disrupted with a double mutation, the
330   homodimer became destabilized such that the Fab molecules used for cryo-EM imaging
331   induced a domain swap of the CTD leading to higher order oligomers.

Elements stabilizing the homodimer

333   Dimerization appears to be a universal feature of Cation Diffusion Facilitators. All
334   structures so far show similar elements contributing to a common dimer interface (Suppl. Fig.
335   12). In particular, a conserved salt bridge exists at the cytoplasmic surface of the membrane
336   (Lys79-Asp209 for soYiiP); the cytoplasmic end of the CTD generally includes one or more Zn^{2+}
337   sites, and extensive hydrophobic interactions involving TM3 helices mediate TMD interactions
338   (Lopez-Redondo et al., 2021). In early work, the salt bridge was proposed to act as a fulcrum for
339   alternating, scissor-like movements in TMD and CTD driven by relay of Zn^{2+} between sites A
340   and C (Lu et al., 2009). Furthermore, the original X-ray structure of ecYiiP featured a V-shaped
341   architecture in which TMD's were completely disengaged (Lu et al., 2009; Lu and Fu, 2007).
342   However, subsequent work showed that stabilization of TMD interactions by cysteine
343   crosslinking did not inhibit transport activity (Lopez-Redondo et al., 2018) and compact dimeric
344   TMD interfaces were observed in cryo-EM structures of soYiiP, Znt8 and Znt7 (Han et al., 2022;
345   Lopez-Redondo et al., 2018; Xue et al., 2020). Indeed, the TMD interface is a remarkably
346   conserved feature in our new structures of D70A and D287A/H263A mutants, despite large-
347   scale conformational changes involving the TM2/TM3 loop and domain swapping of the CTD.
348   We therefore conclude it to be unlikely that the TMD's undergo large-scale scissoring
349   movements as part of the transport cycle.

351   For isolated CTD's, metal ion dependent scissor-like movements have been well
352   documented using truncated constructs from a variety of species (Cherezov et al., 2008;
353   Udagedara et al., 2020; Zeytuni et al., 2014). We observed similar movements in full-length
354   soYiiP: i.e., the CTD's move apart when Zn^{2+} is removed from site C either by chelation or
355   mutation. However, other elements must contribute, given that isolated CTD's dimerize even in
356   the absence of metal ions and Zn^{2+} ions were not observed at all in the CTD of Znt7 (Han et al.,
357   2022). Nevertheless, the Fab-induced domain swap seen in D287A/H263A indicates that, for
358   soYiiP, CTD interactions are weakened in the absence of Zn^{2+}. Conversely, it seems likely that

359   dimer stabilization, via TMD and salt-bridge interactions, lead to enhanced Zn^{2+} binding in the
360   CTD, as evidenced by the considerably higher Zn^{2+} affinity at site C of full-length soYiiP (K_d of
361   33 nM at pH 7) compared to those measured from isolated CTD's (K_d in micromolar range
362   (Udagedara et al., 2020; Zeytuni et al., 2014)). In any case, the relatively high affinity of site C at
363   pH 7 suggests that this site will remain occupied and will serve to ensure dimer stability under
364   physiological conditions.

Role of the site B

366   Structural effects of the D70A mutation support our previous hypothesis that site B is
367   responsible for inducing a global conformational change. The most conspicuous change is the
368   kink between TMD and CTD, which breaks the global two-fold symmetry of structures that retain
369   Zn^{2+} binding at site B, in which local two-fold axes of CTD and TMD are aligned (Suppl. Fig. 12).
370   Although stable, kinked conformations were not achieved over the time-scale of MD simulations,
371   increased movement of the CTD relative to the TMD is seen both in the previously reported apo
372   state simulations (Lopez-Redondo et al., 2021) and with an empty site B (Fig. 3), indicating a
373   role of the Zn^{2+}-bound TM2/TM3 loop in stabilizing the position of the CTD. Indeed, van der
374   Waals interactions are observed between the structured loop from one protomer and the TM6-
375   CTD linker of the opposing protomer on both sides of the dimer (Fig. 3e,f), and MD simulations
376   indicate that a salt bridge between Asp72 and Arg210 may reinforce these interactions (Fig. 3d,
377   c.f., site B in Suppl. Fig. 2).

378   Both cryo-EM structures and MD simulations show that the TM2/TM3 loop becomes
379   disordered when Zn^{2+} is released from site B and this is a likely explanation for increased
380   mobility of the CTD. Two structures were obtained from the D70A mutation in which the CTD
381   becomes progressively more tilted and twisted. In one structure, the TMD's are symmetrical and
382   retain the IF conformation (D70A_sym), whereas in the other structure with more extreme CTD
383   movement (D70A_asym), the TMD transitions to an occluded state. We speculate that these
384   structures represent a sequence of conformational change leading to the occluded state.
385   Although both TM2/TM3 loops are disordered in the D70A_sym structure, one of these loops
386   reforms into an extended conformation in the occluded protomer of the D70A_asym structure
387   (Suppl. Fig. 5). This change results in a novel interaction between the loop and the CTD, which
388   may drive the displacement and bending of membrane helices thus leading to occlusion of the
389   transport site A (Suppl. Fig. 13). This interaction would also prevent the TM2/TM3 loop from
390   rebinding Zn^{2+} until the protein returned to the IF state. On the other side of the dimer, the CTD
391   has lost contact with the TMD, allowing the TM2/TM3 loop to remain disordered and the TMD to
392   remain in the IF state. Interestingly, the TM2/TM3 loops are also extended in the D287A/H263A
393   domain-swapped structure (Suppl. Fig. 5), but in this case, the interactions of this loop with the
394   reconfigured CTD's are quite different and the TMD's remain in the IF state, indicating that a
395   specific structural constraint is required to instigate occlusion.

396   Occlusion of the transport site A is a result of bending of TM5 and tilting of TM1 and 4,
397   thus narrowing the gap between these helices and closing off access to the cytosol. These
398   movements also generate a dramatic difference in the electrostatic surface at the cytoplasmic
399   side of the TMD. In the IF state, the open cavity leading toward site A is negatively charged, as
400   also shown for Znt7 (Han et al., 2022), thus serving to attract Zn^{2+} toward this site. After
401   transition to the occluded state, not only is the cavity closed (Suppl. Fig. 13), but the surface
402   becomes positively charged thus repelling Zn^{2+} (Fig. 3k,l). Previous work has identified a
403   "hydrophobic gate" consisting of two residues at the cytoplasmic ends of TM5 and TM6: Leu154

404   and Leu199 in soYiiP (Gupta et al., 2014). Our previous comparison of holo and apo states
405   showed that these two residues do come closer together in the occluded state (Lopez-Redondo
406   et al., 2021) and homologous residues in Znt7 are close in the OF state and separated in the IF
407   state (Han et al., 2022). Interaction of Leu154 and Leu199 is also seen in the occluded protomer
408   in the D70A_asym structure (Fig. 2d), but these residues are at the periphery of the cavity
409   leading to site A. This observation suggests that interaction of these residues may play an
410   important role in stabilizing the occluded state, but that bending at the cytoplasmic end of TM5
411   (Val148-Ala151) and tilting of TM1 and TM4 may be more directly responsible for blocking
412   access to the transport site.

413   For soYiiP, the IF state appears to be a low-energy, ground state when Zn^{2+} is present at
414   all three sites. Indeed, the IF state has been seen for WT protein both in lipid-based helical
415   crystals (Lopez-Redondo et al., 2018) and detergent micelles (Lopez-Redondo et al., 2021), as
416   well as in D287A and D287A/H263A mutant structures, all with RMSD's <1.5 Å. Removal of
417   Zn^{2+} from site B can be viewed as a source of energy for inducing conformational change and
418   likely leading to transport. Interestingly, the occlusion only occurs in one protomer, suggesting a
419   lack of synchrony across the dimer axis. A mixture of conformational states was also observed
420   for Znt8, in which one protomer adopted the OF state while the other was in the IF state. These
421   observations imply that a given protomer may be able to undergo transport while the other
422   remains inactive, as illustrated in Fig. 5.

423   The proposed sequence of conformational change is consistent with the notion that Zn^{2+}
424   is initially recruited to site B and that transfer to site A would act as a trigger for the first step of
425   the transport cycle. Such a two-step mechanism might be necessary if Zn^{2+} were delivered to
426   YiiP as a chelate – e.g., with metallothionein or glutathione – that would not have direct access
427   to site A. In the case of Cu^+, metallochaperones are thought to play a role in delivery (Robinson
428   and Winge, 2010), but so far there is very limited evidence for Zn^{2+} metallochaperones
429   (Chandrangsu et al., 2019). Nevertheless, essentially all of the Zn^{2+} in the cytoplasm exists in
430   chelated form with vanishingly small concentrations of free Zn^{2+} available for direct binding
431   (Choi and Koh, 1998; Outten and O'Halloran, 2001). The accessibility of site B makes it a
432   plausible acceptor as an initial recruitment site. We postulate that site B would only be available
433   for binding Zn^{2+} in the IF apo state (Fig. 5d). Once bound, two features would facilitate transfer
434   to site A: the drastic difference in affinity between sites A and B would generate a large free-
435   energy gradient and the negative charge of the cavity leading to site A, which lies almost directly
436   below site B in the WT, holo structures, would direct the ion toward the transport site. Although
437   the amino acid sequence of site B is not conserved amongst CDF transporters, a Zn^{2+} ion was
438   observed in an analogous juxtamembrane position on Znt8 (Xue et al., 2020) and many CDF
439   transporters have histidine-rich loops, typically between TM4 and TM5, which might fulfill a
440   similar role in recruiting Zn^{2+} and orchestrating conformational change. Indeed, for Znt7 this His-
441   rich loop was shown to bind two Zn^{2+} ions leading these authors also to speculate that it plays a
442   role in recruitment and shuttling to the transport site (Han et al., 2022).

Stoichiometry of transport and energy coupling

444   The proton-motive force is generally postulated to drive the antiport mechanism utilized
445   by CDF transporters. In the case of YiiP, this antiport involves exchange of Zn^{2+} from the
446   cytoplasm for H^+ in the periplasm and the stoichiometry of this process is key to energy
447   coupling. In previous work, the Zn^{2+}:stoichiometry has been measured to be 1:1 for ZitB (Chao
448   and Fu, 2004a) and deduced by cellular or computational studies to be 1:2 for CzcD (Guffanti et

449 al., 2002) and Znt2 (Golan et al., 2019), respectively. In addition, isothermal calorimetry was
450 used to deduce a binding stoichiometry for Cd^{2+} of 1:1 for ecYiiP (Chao and Fu, 2004b). For the
451 current work, we refined CpHMD simulation data with experimental MST data using the inverse
452 *Multibind* approach (Kenney and Beckstein, 2023) to infer the prevalent protonation states for
453 site A and thus to address stoichiometry. Our analysis is consistent with Zn^{2+} binding to a fully
454 unprotonated site A regardless of the pH. After Zn^{2+} release, the transport site becomes either
455 doubly or triply protonated, depending on the pH. Due to strong coupling between His155 and
456 Asp159, the singly protonated state is essentially not seen. Thus, this model is consistent with a
457 stoichiometry of at least 1:2, possibly 1:3 in more acidic environments (pH < 6).

458 Our analysis predicts significant shifts in pK_a for Zn-binding residues. Such shifts reflect
459 strong Coulomb interactions due to both the low dielectric of the membrane and the clustering of
460 several titratable residues at the binding site. Effects of the membrane environment have been
461 studied both by experimental (Gayen et al., 2016; Isom et al., 2010; Morrison et al., 2015) and
462 computational (Henderson et al., 2020; Panahi and Brooks, 2015) methods, showing pK_a values
463 up to 9 for acidic residues. Coupling between nearby residues has also been shown to shift pK_a
464 values (Yue et al., 2017), with estimated pK_a values of 3 and 11 for a di-aspartyl pH sensor in a
465 pH-sensitive calcium channel serving as a dramatic example (Chang et al., 2014). Together with
466 the current work, these examples illustrate the importance of tuning the local environment to
467 harness the energy of the proton motive force.

468 The $Zn^{2+}:H^+$ stoichiometry has crucial physiological consequences for the energetics of
469 transport, which are governed by the Nernst equation describing electrochemical potential. The
470 overall transport cycle can be described as

471 $$mH_o + nZn_i \rightleftharpoons mH_i + nZn_o$$
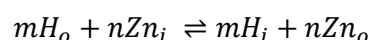
472 with the free energy calculated as

473 $$\Delta G = RT\ln\frac{[H_i]^m}{[H_o]^m} + RT\ln\frac{[Zn_o]^n}{[Zn_i]^n} + zFV_m$$

474 where *m* is the number of protons, *n* is the number of Zn^{2+} ions, *z* is the net charge for the
475 reaction and V_m is the membrane potential. Based on this equation, the higher stoichiometries
476 of 1:2 or 1:3 provide the cell with increased leverage over Zn^{2+} transport. In the absence of
477 membrane potential, for example, a 10-fold proton gradient (ΔpH of 1) can produce Zn^{2+}
478 gradients at equilibrium of up to 10^2 or 10^3, respectively, instead of simply 10 for a 1:1
479 stoichiometry (more generally, $10^{m/n}$). Membrane potential represents an important component
480 of the proton motive force that will influence electrogenic transport, where *z* is non-zero. In
481 particular, a stoichiometry of 1:1 would produce net positive charge transfer out of the cell and
482 thus would require working against this membrane potential. Given a potential of -80 mV,
483 relatively normal in *E. coli* (Felle et al., 1980), a 1:1 stoichiometry would produce an unfavorable
484 energy term that would overcome a chemical gradient of one pH unit. In contrast, a 1:2
485 stoichiometry would be electroneutral and would therefore be unaffected by membrane potential
486 thus generating a Zn^{2+} gradient of 10^2 as described above. Finally, a stoichiometry of 1:3 would
487 benefit both from the membrane potential as well as from the increased number of protons to
488 theoretically generate a gradient of $10^{4.4}$.

489 These calculations are based on equilibrium thermodynamics, but the pH dependence of
490 Zn^{2+} binding also has implications for the kinetics of transport. In particular, the dramatic

491 difference in K_d at cytoplasmic pH of 7.4 (1 nM) compared to more acidic pH's in the periplasm
492 (e.g., 6 μM at pH 6) implies that the on-rate of Zn^{2+} is dominant in the cytoplasm but that the off-
493 rate is enhanced in the periplasm, assuming that the binding site in the OF state has similar pH
494 dependence. This assumption seems plausible given the similarity of transport site geometry of
495 YiiP in the OF state (Lu et al., 2009). Thus, although the final equilibrium concentrations of Zn^{2+}
496 are not affected by the pH dependence of the transport site, the rate of transport and the rate of
497 equilibration will be greatly enhanced (Tanford, 1983).

498 YiiP has three aspartates and one histidine at site A, whereas many CDF transporters
499 including the mammalian Znt's substitute Asp47 for a second histidine. Previous work has
500 focused on changes in ion specificity associated with this change (Hoch et al., 2012), but it also
501 seems likely to affect stoichiometry. At a minimum, two histidines would make the 1:2
502 stoichiometry almost certain and a 1:3 stoichiometry highly plausible. The resulting
503 electrogenicity could be desirable for eukaryotic cells in which these transporters operate
504 predominantly in intracellular organelles such as insulin secreting granules, synaptosomes,
505 golgi or zinc-o-somes that are responsible for the dramatic Zn^{2+} sparks during oocyte fertilization
506 (Chu, 2018; Hara et al., 2017). Since the pH gradient of these organelles is modest, additional
507 driving force from the membrane potential might be key in producing the high internal
508 concentrations that are sometimes required for function.

509

MATERIALS and METHODS

Protein expression and purification

YiiP was expressed in *E. coli* (BL21(DE3)-CodonPlus-RIPL) from a pET vector that included an N-terminal decahistidine tag. Cells were grown in LB media supplemented with 30 µg/ml kanamycin at 37°C until they reached an OD_{600} of 0.8. After cooling the media to 20°C, expression was induced by addition of 0.5 mM isopropyl-β-D-thiogalactoside followed by overnight incubation at 20°C. Cells were harvested by centrifugation at 4,000xg for 1 h, resuspended in lysis buffer (20mM HEPES, pH 7.5, 100mM NaCl, 10% glycerol, and 500 µM tris(2-carboxyethyl)phosphine) - 100 ml of buffer per 20 g of cells - and then lysed with a high-pressure homogenizer (Emulsiflex-C3; Avestin, Inc. Ottawa Canada). Protein was extracted from the membrane by adding 1.5 g dodecyl-β-D-maltoside per 100 ml of cell lysate followed by 2h of incubation at 4°C. Insoluble material was removed by centrifugation at 100,000xg for 30 min. The supernatant was loaded onto a Ni-NTA affinity column pre-equilibrated in buffer A (20 mM HEPES, pH 7.5, 100 mM NaCl, 10% glycerol, and 0.05% dodecyl-β-D-maltoside). The column was washed by addition of buffer A supplemented with 20 mM imidazole and protein was then eluted using a gradient of imidazole ranging from 20 to 500 mM. Peak fractions were combined, supplemented with tobacco etch virus (TEV) protease (1:10 weight ratio of TEV:YiiP) to cleave the decahistidine tag, and dialyzed overnight at 4°C against buffer A. TEV protease was removed by loading the dialysate onto an Ni-NTA column and collecting the flow-through fractions. After concentration, a final purification was done with a Superdex 200 size-exclusion chromatography (SEC) column (GE Healthcare, Chicago, Illinois) equilibrated with SEC buffer (20 mM HEPES, pH 7.5,150 mM NaCl, 0.2% n-decyl-β-D-maltoside, and 1 mM tris(2-carboxyethyl)phosphine).

Fab selection, modification, expression, and purification has been described previously (Lopez-Redondo et al., 2021). Briefly, the construct designated Fab2r was expressed in *E. coli* strain 55244 from a freshly prepared transformation. Cells were cultured for ~24 h at 30°C with constitutive expression behind an innately leaky T4 promoter. Cell pellets were harvested by centrifugation, lysed with a high-pressure homogenizer and Fab was purified with a 5-ml HiTrap Protein G HP column (GE Healthcare). Pooled fractions were dialyzed against sodium carbonate buffer (pH 5.0) overnight at 4°C and further purified with Resource-S cation exchange column (GE Healthcare). Finally, pure Fab protein was pooled and dialyzed against SEC buffer.

Cryo-EM sample preparation and structural analyses

To ensure that YiiP was fully loaded with Zn^{2+}, the purified protein was initially incubated with metal ion chelators (0.5 mM EDTA and 0.5 mM N,N,N′,N′-tetrakis(2-pyridinylmethyl)-1,2-ethanediamine [TPEN]) for 24hrs at 4°C to remove ions that co-purified with the protein, as seen in previous work (Lopez-Redondo et al., 2021). The sample was then dialyzed against YiiP SEC buffer containing 0.5 mM EDTA for 10 h to eliminate chelator-metal complexes. Finally, YiiP was loaded with Zn^{2+} by dialysis (10 h with four buffer exchanges) against SEC buffer supplemented with 0.25 mM $ZnSO_4$. YiiP was then incubated with Fab2r at a 1:1 molar ratio for 1 h at 20°C to form the YiiP-Fab2r complex. This complex was purified by SEC using a Superdex 200 column equilibrated with SEC buffer supplemented with 0.25 mM $ZnSO_4$. Peak fractions at 3-5 mg/ml were used immediately for preparation of cryo-EM samples. Specifically, 3–4 µl were added to glow-discharged grids (C-Flat 1.2/1.3-4Cu-50; Protochips, Inc.) that were blotted under 100% humidity at 4°C and plunged into liquid ethane using a Vitrobot (Thermo Fisher Scientific, Inc. Bridgewater NJ).

555   The YiiP-Fab2r complex was imaged with a Titan Krios G3i electron microscope
556   (Thermo Fisher Scientific, Inc) equipped a Bioquantum energy filter and K2 or K3 direct electron
557   detector (Gatan, Inc. Pleasanton CA) with a pixel size of ~1 Å and a total dose of ~50
558   electrons/Å^2. Micrographs containing crystalline ice, excessive contamination, or imaging
559   artifacts were removed and the resulting micrographs were imported into cryoSPARC v2.15
560   (Punjani et al., 2017) for analysis. Particles were picked based on templates generated in
561   previous work and an initial set of particles were subjected to two rounds of 2-D classification to
562   remove false positives. The resulting particles were then subjected to successive rounds of ab
563   initio reconstruction with C1 symmetry and a resolution cutoff starting at 12 Å and declining to 8
564   Å; at each step, the best of two output classes was carried forward to the next round. The
565   resulting particles were used for heterogeneous refinement against two or three reference
566   structures derived from the ab initio jobs, still with C1 symmetry. A final selection of particles
567   was then used for non-uniform refinement using both C1 and C2 symmetry. Postprocessing
568   steps included calculation of local resolution and evaluation of 3-D variability (Punjani and Fleet,
569   2020). For the D70A construct, RELION was used to process a class of particles corresponding
570   to a dimer of dimers (Suppl. Fig. 3). After exporting these particles from cryoSPARC, steps of
571   2D classification and ab initio reconstruction were repeated in RELION, followed by 3D
572   refinement of ~117,000 dimer-of-dimer particles with C2 symmetry. A mask encapsulating one
573   dimer was created with Chimera (Pettersen et al., 2004) and symmetry expansion followed by
574   signal subtraction was used to generate a new set with ~234,000 dimeric particles. This
575   expanded particle set was imported back into cryoSPARC and combined with the class of
576   isolated dimer particles. This combined particle set was used for hetero-refinement to segregate
577   dimer complexes with symmetrical and asymmetrical TMD's. These segregated particle sets
578   were then used for final non-uniform refinement.

579   For model building of symmetrical structures from WT, D287A, D51A, we started with
580   the deposited coordinates from wild type (PDB, 7KZZ). This model was docked as a rigid body
581   to the map and adjusted manually in Coot (Emsley et al., 2010) as a starting structure for
582   refinement using PHENIX (Adams et al., 2010). For D70A and D287A/H263A mutants, the CTD
583   and the TMD from either 7KZZ or 7KZX were separately docked to the map. After adjustment
584   and crude rebuilding in Coot, these models were submitted to NAMDINATOR for Molecular
585   Dynamics Flexible Fitting (Kidmose et al., 2019). The resulting models were used as starting
586   points for PHENIX refinement. This refinement consisted of multiple rounds that alternated
587   between real-space refinement and manual adjustment using Coot. Atomic models were then
588   displayed using CHIMERA (Pettersen et al., 2004) and the PyMOL Molecular Graphics System
589   (Schrödinger, LLC, New York NY).

590   For characterization of cavities running from site A to the cytoplasm, we used Caver
591   Analyst 2.0 Beta (Jurcik et al., 2018). The starting point was defined set near D51 in models for
592   WT and D70A_asym and we selected the shortest tunnel that ran to the cytoplasm. Settings
593   used for the calculations were as follows. Approximation: 12, Minimum probe radius: 0.9,
594   Clustering threshold: 3.5, Shell depth: 2.0, Shell radius: 3.0. Zn^{2+} ions were excluded from the
595   calculation.

596   MST experiments
597   YiiP mutants were labelled with Alexa fluor 488 fluorescent dye (Invitrogen life
598   Technologies, Carlsbad CA) by adding 2.5 μL of dye from a 16 mM stock solution in DMSO to
599   200 μL of protein at 1-2 mg/ml in SEC buffer supplemented with 10% glycerol at pH 7. The

600 reactive group of this dye was N-hydroxysuccinimide, which at pH 7 preferentially targets the N-
601 terminus of the polypeptide. Although labeling of lysine residues is also possible, we believe this
602 was minimal due to the low labeling stoichiometries of ~1:1 used for our experiments. Zn^{2+} was
603 removed by adding 0.5 mM EDTA and 0.5 mM TPEN followed by overnight incubation at 4°C.
604 Excess dye and chelated Zn^{2+} were removed using several cycles of dilution with SEC buffer
605 and concentration with a 50 kDa cutoff concentrator (AMICON, Millipore Sigma, Burlington MA).
606 For titration, Zn^{2+} was buffered either by 0.5 mM sodium citrate or 0.2 mM NTA; the total amount
607 of added $ZnSO_4$ was varied to achieve the desired concentration of free Zn^{2+}, according to the
608 program MAXCHELATOR (Bers et al., 1994). Protein concentration during the titration varied
609 from 8 to 100 nM. After 1:1 mixing of protein and Zn^{2+} solutions, samples were centrifuged for 5
610 min at 2000xg, then loaded into standard treated capillaries for measurement with a Monolith
611 NT.115 MST instrument (NanoTemper Technologies, South San Francisco, CA);
612 measurements were taken at 37 °C with LED power ranges from 20-60% and medium MST
613 power. Data from three independent titrations were analyzed with the MO.Affinity Analysis
614 software v2.3 using MST on-time of 15 s. For determination of K_d, data was fitted with a curve
615 based on the law of mass action,

616

617
$$F(C_{Zn}) = F_u + \frac{(F_b - F_u) * \left(C_{Zn} + C_P + K_d - \sqrt{(C_{Zn} + C_P + K_d)^2 - 4 * C_P * C_{Zn}} \right)}{2 * C_P}$$

618
619 where $F(C_{Zn})$ is the fraction bound, C_{Zn} is concentration of free zinc, C_P is the concentration of
620 YiiP protein, F_b and F_u refer to the normalized fluorescence in the bound and unbound state,
621 and K_d is the affinity constant. Alternatively, the data was fit with the Hill equation to assess
622 cooperativity,

623
$$F(C_{Zn}) = F_u + \frac{(F_b - F_u)}{1 + \left(\frac{EC_{50}}{C_{Zn}}\right)^n}$$

624 where EC_{50} is the half-maximal effective concentration (akin to K_d) and n is the Hill coefficient.

625 Overview of MD simulations
626   Two types of all-atom, explicit solvent MD simulations were conducted to assess the
627 effects of proton and zinc binding on the structure of the YiiP dimer in a lipid bilayer. We used
628 fixed charge equilibrium MD simulations (using a force field with unchanging parameters) to
629 investigate the interactions between Zn^{2+} ions and YiiP. We also carried out replica exchange
630 constant pH MD (CpHMD) simulations to calculate the pK_a values of all titratable residues and
631 assess the microscopic protonation states of the ion binding sites in the absence of Zn^{2+}. Unlike
632 CpHMD simulations, fixed charge simulations do not allow for dynamic protonation or
633 deprotonation of residues. Despite this limitation, they are our preferred approach to study
634 protein-zinc ion interactions and conformational changes because they can be run more
635 efficiently than CpHMD and were thus used to quantify the effect of zinc ions on the structure of
636 YiiP (see Table 5 for a summary of these simulations). The zinc ions in the system were
637 simulated with the non-bonded dummy model described in our previous work (Lopez-Redondo
638 et al., 2021); parameter files are available as package 2934 in the Ligandbook repository
639 (Domański et al., 2017) (https://ligandbook.org/package/2934). Briefly, parameters governing
640 this model were refined based on experimental hydration free energy, ion-oxygen distance and
641 coordination number of the water in the first hydration shell, ultimately reproducing these values

642 with errors of 1% and 0.3%, respectively. The model was further validated using simulations of
643 known zinc-binding proteins, in which stability of the protein and the geometry of the binding
644 complexes were well maintained, though coordination distances were slightly longer than
645 experimental values, especially for sulfur atoms from cysteine residues (Lopez-Redondo et al.,
646 2021). Given that YiiP employs aspartate or histidine residues for Zn^{2+} coordination, the model
647 is well-suited for the current work.

Fixed charge equilibrium MD simulations

649 MD simulations in the *holo* (with Zn^{2+} in A, B, and C sites) and *apo* (no Zn^{2+}) state were
650 taken from our previous study (Lopez-Redondo et al., 2021). To investigate the influence of the
651 binding site B, we generated an "*empty site B"* structure by removing the Zn^{2+} ions from site B in
652 both protomers of PDB ID 5VRF, the same starting structure used previously. In order to study
653 the influence of the salt-bridge D72-R210, simulations were also conducted after applying the
654 D72A mutation to the holo structure (PDB ID 5VRF). In these D72A simulations, Zn^{2+} ions were
655 bound in all sites (A, B, C1, C2), i.e., D72A simulations differed from the holo simulations only in
656 the mutation.

657 The membrane-protein systems were modeled by embedding the YiiP dimer into a 4:1
658 palmitoyloleoylphosphatidylethanolamine:palmitoyloleoylphosphatidylglycerol (POPE:POPG)
659 lipid bilayer, which approximates the composition of the plasma membrane from *E. coli* (Raetz,
660 1986), and solvating the system with water as well as sodium and chloride ions corresponding
661 to a concentration of 100 mM using CHARMM-GUI v1.7 (Jo et al., 2008; Jo et al., 2009; Lee et
662 al., 2016). We used GROMACS 2021.1 (Abraham et al., 2015) with the CHARMM36 force field,
663 the CMAP correction for proteins (MacKerell et al., 1998; Mackerell et al., 2004), CHARMM36
664 lipids (Klauda et al., 2010), and the CHARMM TIP3P water model. The *empty site B* system
665 contained 117,512 atoms, the apo system contained 117,394 atoms, and the D72A system
666 contained 117,418 atoms. All systems were constructed in a hexagonal simulation cell with
667 initial dimensions 101 Å × 101 Å × 135 Å. Default protonation states of all ionizable residues
668 were used based on the experimental pH of 7. The neutral HSD tautomer (proton on the N_δ)
669 was selected to model all histidines except H73 and H155, which were modeled with HSE
670 (proton on the N_ϵ) based on their orientation relative to Zn^{2+} ions in the cryo-EM structure PDB
671 ID 5VRF.

672 The systems were first energy minimized and underwent a 3.75-ns six-stage
673 equilibration procedure with position restraints on protein and lipids, following the CHARMM-
674 GUI protocol (Jo et al., 2008). Three copies of 1-μs production simulations were carried out with
675 *empty site B*, starting from the same initial system conformation but with different initial
676 velocities. All simulations were performed under periodic boundary conditions at constant
677 temperature (T = 303.15 K) and pressure (P = 1 bar). The velocity rescaling thermostat (Bussi
678 et al., 2007) was used to maintain the temperature with a time constant of 1 ps and separate
679 temperature-coupling groups for protein, lipids, and solvent. A semi-isotropic pressure coupling
680 scheme was implemented using the Parrinello-Rahman barostat (Parrinello and Rahman, 1981)
681 with a time constant of 5 ps, a compressibility of 4.6×10^{-5} bar^{-1}. Long-range electrostatics were
682 calculated with the smooth particle mesh Ewald method (Essmann et al., 1995) under tinfoil
683 boundary conditions with an initial cutoff of 1.2 nm, which was optimized during the simulation,
684 and interactions beyond the cutoff were calculated in reciprocal space with a fast-Fourier
685 transform on a grid with spacing 0.12-nm and fourth-order spline interpolation. The van der
686 Waals interactions were switched smoothly to 0 between 1.0 nm and 1.2 nm, and the

687   interactions were shifted over the whole range and reduced to 0 at the cutoff. The Verlet
688   neighbor list was updated dynamically by GROMACS for optimized performance with a buffer
689   tolerance of 0.005 kJ/mol/ps. Bonds to hydrogen atoms were treated as rigid holonomic
690   constraints with the P-LINCS algorithm (Hess, 2008) with an expansion order of four and two
691   LINCS iterations; alternatively, SETTLE (Miyamoto and Kollman, 1992) was used for water
692   molecules. The classical equations of motion were integrated with the leapfrog algorithm with a
693   time step of 2 fs.

694   ### CpHMD simulations with pH replica exchange

695   In conventional MD simulations, the protonation states of titratable groups in the system
696   are fixed. To investigate the role of protons in the Zn^{2+} transport of YiiP, we performed
697   membrane-enabled hybrid-solvent continuous constant pH MD simulations (Huang et al., 2021).
698   The currently available implementation of the membrane-enabled CpHMD method does not
699   take into account the direct effect of ions on the titration of nearby residues so we only ran
700   CpHMD simulations for the apo system.

701   CpHMD simulations were initialized with the apo model (PDB ID 5VRF with Zn^{2+} ions
702   removed). An initial 250-ns production simulation was run for the CpHMD apo system to fully
703   relax the membrane, using the same GROMACS 2021.1 protocol described above for fixed
704   charge equilibrium simulations.

705   The membrane-enabled hybrid-solvent continuous CpHMD simulations were performed
706   using the CHARMM program version c42a2 (Brooks et al., 2009) with the PHMD module
707   (Khandogin and Brooks, 2005; Lee et al., 2004) and the pH replica-exchange (REPDSTR)
708   module (Wallace and Shen, 2011). The conformations of YiiP were sampled using conventional
709   all-atom simulations with the CHARMM22/CMAP all-atom force field (MacKerell et al., 1998;
710   Mackerell et al., 2004), the CHARMM36 lipid force field (Klauda et al., 2010), and the CHARMM
711   modified TIP3P water model. The titration coordinates were propagated using the membrane
712   GBSW implicit-solvent model (Im et al., 2003) with the GBSW input radii for the protein taken
713   from Chen et al. (Chen et al., 2006). Based on the average distance between the C2 atoms of
714   the lipids in the cytoplasmic- and periplasmic-facing leaflets, the thickness of the implicit bilayer
715   was set to 40 Å with a switching distance of 5 Å for the transition between the low dielectric slab
716   and bulk solvent. The implicit membrane was excluded by two cylinders with a radius of 14 Å
717   placed at the center of mass of each protomer of YiiP. The radius was selected to maximize the
718   coverage of the interior of the protein with minimal overlapping of the implicit membrane.

719   The final snapshot of the equilibrium simulation was used as the initial structure for the
720   CpHMD simulation. Dummy hydrogen atoms were added to the carboxylate groups of acidic
721   residues following the documentation of the PHMD module (Wallace and Shen, 2011) in
722   CHARMM (Brooks et al., 2009) using the HBUILD facility. The system was then equilibrated
723   with energy minimization using 50 steps of steepest descent followed by 50 steps of adopted
724   basis Newton-Raphson algorithms and CpHMD at pH 7 for 1 ns, whereby the harmonic
725   restraints on the protein heavy atoms were reduced from 1 $kcal \cdot mol^{-1} Å^{-1}$ to zero.

726   The production simulation was then performed using hybrid-solvent CpHMD with the pH
727   replica-exchange protocol (Huang et al., 2021; Wallace and Shen, 2011), using 30 replicas with
728   pH ranging from 1.5 to 11.5. The specific pH conditions were 1.5, 1.75, 2, 2.5, 2.75, 3, 3.25, 3.5,
729   3.75, 4, 4.25, 4.5, 4.75, 5, 5.25, 5.5, 6, 6.5, 7, 7.5, 8, 8.5, 8.75, 9, 9.5, 10, 10.25, 10.5, 11, 11.5,

730 chosen to ensure that the exchange rate between the nearby replicas was higher than 0.2. Each
731 replica was simulated under periodic boundary conditions at constant temperature (T = 303.15
732 K), pressure (P = 1 bar), and specified pH. A modified Hoover thermostat method (Hoover,
733 1985) was used to maintain the temperature, while pressure was maintained using the Langevin
734 piston coupling method (Feller et al., 1995) with a piston mass of 2500 amu. Long-range
735 electrostatics were evaluated with the particle mesh Ewald method (Darden et al., 1993) with a
736 real-space cutoff of 1.2 nm, and interactions beyond the cutoff were calculated in reciprocal
737 space with a fast-Fourier transform on a grid with 0.09-nm spacing and sixth-order spline
738 interpolation. The Lennard–Jones forces were switched smoothly to 0 between 1.0 and 1.2 nm,
739 and the potential was shifted over the whole range and reduced to 0 at the cutoff. Bonds to
740 hydrogen atoms were constrained with the SHAKE algorithm to allow a 2 fs time step. To avoid
741 a spike in potential energy due to a lack of solvent relaxation (Wallace and Shen, 2011), a
742 GBSW calculation was executed every 5 MD steps to update the titration coordinates. An
743 attempt to exchange adjacent pH replicas was made every 1000 MD steps (corresponding to 2
744 ps). Each replica simulation lasted 12 ns for a total aggregate sampling time of 360 ns. Many
745 replicas exchanged across a large fraction of available pH space (Supplementary Figure 7),
746 indicating that 12 ns per replica were sufficient for sampling the degrees of freedom near the
747 protonation sites.

748 ## Analysis of fixed charge MD simulations
749 Analysis of the trajectories was carried out with Python scripts based on MDAnalysis
750 (Gowers et al., 2016). RMSDs of C_α atoms of the whole protein, TMD, and CTD were calculated
751 using the qcprot algorithm (Liu et al., 2010) after optimally superimposing the structure on the
752 same C_α atoms of the cryo-EM structure. Similarly, root mean square fluctuation (RMSF) of C_α
753 atoms of the whole protein, TMD, and CTD were calculated. To assess the relative motion
754 between the two domains, a CTD-TMD rotation angle was calculated from the rotation matrix
755 which minimized the RMSD of the CTD after superimposing the protein on the TMD domain of
756 the reference structure (PDB ID 5VRF), as in our previous work (Lopez-Redondo et al., 2021).
757 The existence of the salt-bridge Asp72-Arg210 was quantified using the shortest distance
758 between O_δ atoms of Asp72 and hydrogen atoms on the side chain of Arg210.

759 ## Analysis of CpHMD simulations
760 The titration coordinates were extracted from CpHMD output files as time series $S(t)$
761 (Supplementary Figure 8) with the CpHMD-Analysis scripts
762 (https://github.com/Hendejac/CpHMD-Analysis). The primary purpose of these simulations is to
763 obtain microscopic pK_a values for titratable residues. We first describe the conventional
764 approach to obtain per-residue pK_a values using the heuristic generalized Hill equation and then
765 in the next section demonstrate an alternative inference approach based directly on statistical
766 mechanics.

767 The deprotonation fraction S of a titratable site was calculated from the titration time
768 series (Supplementary Figure 8) as the number of trajectory frames N of the residue in the
769 deprotonated and protonated states as

770
$$S = \frac{N_{\text{deprot}}}{N_{\text{deprot}} + N_{\text{prot}}}$$

771 where the site is identified as deprotonated when the CpHMD titration coordinate λ is greater
772 than 0.8 and protonated when the titration coordinate is less than 0.2. Individual residue pK_a's
773 were obtained from a fit to the generalized Henderson-Hasselbalch equation (Hill equation)
774 (Henderson et al., 2020; Huang et al., 2016; Huang et al., 2021) for the deprotonated fraction S
775 as a function of pH,

776
$$S(\mathrm{pH}) = \frac{1}{1 + 10^{n(\mathrm{p}K_a - \mathrm{pH})}}$$

777 where n is the Hill coefficient, which represents the slope of the response curve (Supplementary
778 Figure 9). The mean pK_a of a residue was calculated for each pair of equivalent residues in
779 protomer A and protomer B because these residues were sampled independently in the CpHMD
780 simulation. The statistical error was estimated as the absolute difference between the pK_a's of
781 protomer A and B residues and their mean value.

782   The CpHMD simulations track the protonation of every single titratable residue and thus
783 provide detailed microscopic information on the exact protonation state for each binding site.
784 The distribution of these microscopic states named S0 to S15 for site A (Supplementary Figure
785 10, inset table) and S0 to S7 for site B (Supplementary Figure 11, inset table) forms the basis
786 for our alternative calculation of microscopic pK_a values. In order to obtain these CpHMD
787 protonation state distributions, we treated titration coordinate data $S(t)$ from protomer A and B
788 as independent; thus, by concatenating them we effectively doubled our sampling. Using the
789 same criterion for bound/unbound protons and the definition of microstates for site A
790 (Supplementary Figure 10) and site B (Supplementary Figure 11) we generated separate
791 microstate time series for sites A and B. These time series were then histogrammed to derive
792 the distributions of the microscopic protonation states of site A (Supplementary Figure 10a) and
793 B (Supplementary Figure 11a).

794 Calculation of microscopic, state-dependent pK_a values with the *Multibind* method
795   The *Multibind* method generates thermodynamically consistent models for systems of
796 coupled reactions by using a maximum likelihood approach to combine kinetic or
797 thermodynamic measurements from different sources (Kenney and Beckstein, 2023). Given free
798 energy differences between states (either from simulations or experiments), *Multibind* generates
799 a complete set of free energies for all states in the form of a potential graph that obeys path-
800 independence of free energies and detailed balance while being maximally consistent with the
801 input data. From this set of free energies, all macroscopic thermodynamic observables can be
802 calculated. Without such an approach, thermodynamically inconsistent models arise due to
803 random errors in the input measurements. For Zn^{2+} and proton binding, the free energy
804 differences in the potential graph are calculated as functions of the external parameters, namely
805 the free Zn^{2+} concentration [X] and the pH, and with pK_a and Zn^{2+} standard state binding free
806 energy values as input. The binding free energy of a reaction $A + X \rightleftharpoons A{:}X$ is calculated as

807
$$\beta\Delta G_{\mathrm{bind}}\left([X]\right) = \ln\left(\frac{K_{\mathrm{D}}}{[X]}\right) = \ln\left(\frac{K_{\mathrm{D}}}{c_0}\right) - \ln\left(\frac{[X]}{c_0}\right) = \beta\Delta G_{\mathrm{bind}}^0 - \ln\left(\frac{[X]}{c_0}\right)$$

808 where $\beta = \frac{1}{k_B T}$ (k_B is Boltzmann's constant), K_{D} is the dissociation constant, and the binding free
809 energy is written as a sum of $\Delta G^0_{\mathrm{bind}}$, the binding free energy at the standard state concentration
810 c_0=1 M, and a term depending on the ligand concentration [X]. For proton binding, the free
811 energy difference is expressed equivalently as

812
$$\beta\Delta G_{\text{prot}}\,(\text{pH}) = \ln(10)\,(\text{pH} - \text{p}K_a),$$

813 where $\text{p}K_a$ is the acid dissociation constant.

814 We used the Python implementation of *Multibind*
815 (https://github.com/Becksteinlab/multibind) to construct thermodynamic models for binding sites
816 A and B, with the assumption that all binding sites across both protomers are independent.
817 Each model describes the transitions between all possible states as either binding of a proton or
818 binding of a Zn^{2+} ion. With four titratable residues, site A has $M=2^4=16$ Zn^{2+}-free protonation
819 microstates (states S0 to S15 in Supplementary Figure 10, inset table) and 16 Zn^{2+}-bound
820 protonation microstates for a model with 32 states in total (Fig. 4h). Site B has three titratable
821 residues and thus $M=8$ for a model with 16 states in total (states S0 to S7 in Supplementary
822 Figure 11, inset table). Because only free energy differences between states are measurable,
823 we can arbitrarily specify one state as a reference with zero free energy. Here we chose the 0-
824 proton unbound state S0 as the reference state with $G_0=0$, but calculated observables are
825 independent of this particular choice. The probability of observing the system in the microstate i
826 is

827
$$P_i(\text{pH}, [\text{Zn}^{2+}]) = \frac{1}{Z}e^{-\beta G_i}$$

828 where G_i is the free energy of any state i and Z is the partition function

829
$$Z(\text{pH}, [\text{Zn}^{2+}]) = \sum_{k=1}^{M} e^{-\beta G_{k,\text{unbound}}} + \sum_{k=1}^{M} e^{-\beta G_{k,\text{Zn}}}$$

830 which contains the partition functions of the unbound and bound states. We note that the
831 microstate probabilities P_i can also be directly obtained from the CpHMD simulations, which
832 enables us to use *Multibind* as an inverse method to infer microscopic $\text{p}K_a$ from CpHMD data
833 (without resorting to the generalized Hill equation fit), as described below.

834 The fraction of YiiP protomers that have a Zn^{2+} ion bound to the binding site in question,
835 the *bound fraction*, is

836
$$\langle X \rangle = Z^{-1} \sum_{k=1}^{M} e^{-\beta G_{k,\text{Zn}}}$$

837 The bound fraction can be obtained experimentally from MST measurements.

838 With the ability to calculate microstate probability or bound fraction at specific pH or Zn^{2+}
839 concentration, we devised an inverse approach to *infer* microscopic, state-dependent $\text{p}K_a$'s and
840 standard binding free energies (ΔG^0_{bind}) from either CpHMD data (to avoid using the Hill
841 equation with the deprotonated fractions, which are aggregated over multiple states and may
842 therefore mask coupling between residues) or from experimental MST measurements.

843 The inverse *Multibind* approach generates successive microscopic models with a Monte
844 Carlo (MC) scheme and compares the calculated observables to the target values. Observables
845 correspond to microstate probability distributions $P_i(\text{pH})$ for CpHMD or bound fraction <X> as a
846 function of pH and Zn^{2+} concentration for MST. Once convergence is reached, the microscopic
847 model contains the inferred microscopic state-dependent $\text{p}K_a$ values and Zn^{2+} binding free

848 energies. We implemented a simple finite-temperature MC algorithm that minimizes the RMSD
849 between the given and computed macroscopic features. The model was initialized with pK_a
850 values from CpHMD (obtained with the Hill equation) or ΔG^0_{bind} binding free energies calculated
851 from the experimental K_d from the MST analysis. For each MC step, the target observable was
852 calculated for a range of pH values and Zn^{2+} concentrations. For as long as the RMSD between
853 the computed and the target observable remained above a cutoff (see Table 6), a new set of
854 pK_a or ΔG^0_{bind} was generated by adding a random value drawn from a uniform distribution
855 ranging from –0.2 to 0.2 pK_a units (for pK_a) or –0.2 to 0.2 $k_B T$ (for binding free energies) to all
856 microscopic parameters. A new set of changes was accepted with probability (Metropolis
857 criterion)

858
$$P(pK_a, \Delta G^0_{bind} \rightarrow pK_a{}', \Delta G^0_{bind}{}') = \min(1, e^{-\frac{\Delta RMSD}{r}})$$

859 where $\Delta RMSD$ is the difference between the RMSDs between the target and the computed
860 observable for the old set of pK_a's or ΔG^0_{bind}'s and the new set

861
$$\Delta RMSD = RMSD(pK_a{}', \Delta G^0_{bind}{}') - RMSD(pK_a, \Delta G^0_{bind})$$

862   The fictional temperature in the Metropolis criterion, r, was set to 0.0001 to be on the
863 order of typical per-step changes. The RMSD cutoffs (Table 6) were chosen from initial runs
864 using a zero-temperature MC algorithm, which accepted a new set of changes only when
865 $\Delta RMSD$ < 0. These initial runs were stopped after 2000 steps and after no changes had been
866 accepted in the last 100 or more steps. The zero-temperature MC ensured that the final set
867 generated the smallest RMSD, while the finite-temperature MC used in the production runs
868 allowed larger parameter space to be sampled. Fifty runs were performed for each target.
869 Averaged pK_a values and corresponding standard deviations were calculated from the 50
870 independent MC runs. Although these standard variations of our parameter estimates weakly
871 depend on the somewhat arbitrary choice of r, we chose to report them instead of a rigorous
872 statistical error (which is unavailable with the current approach) to provide a sense of variability
873 of the estimates.

874   For site B, the CpHMD simulations suggested that H73 and H77 behaved identically and
875 had almost the same microscopic pK_a values. We calculated the "coupling energy" (Ullmann,
876 2003) between H73 and H77,

877
$$W = pK_a(S0 \rightarrow S2) - pK_a(S1 \rightarrow S3) = pK_a(S0 \rightarrow S1) - pK_a(S2 \rightarrow S3)$$

878 (expressed in pK_a units, i.e. energy divided by $k_B T \ln10$), from the microscopic CpHMD state
879 pK_a's (see Supplementary Data). The coupling energy measures how the protonation of a
880 specific residue (e.g. H73) depends on the protonation of another residue (here, H77). The
881 coupling energy is the difference in pK_a when H77 remains deprotonated while H73 binds a
882 proton (S0→S2, see Supplementary Figure 11) compared to the situation when H77 is already
883 protonated (S1→S3). The H73-H77 coupling energy for the CpHMD simulation was W=+1.0 for
884 D70 deprotonated and W=+0.2 for D70 protonated. Because W>0, binding of a proton to one of
885 the histidines decreases the pK_a of the other, thus decreasing proton binding via anti-
886 cooperative coupling. Preliminary calculations with the MST data, however, showed that small
887 initial differences in the starting values could lead to large pK_a shifts in H73 and H77, with the
888 directions determined by the initial ordering of pK_a values. Because we had no specific evidence
889 that the two histidines should behave differently, we considered the behavior of the initial

890   unconstrained MST inference calculations to be problematic. This problem indicated that the
891   inverse approach can be sensitive to initial values and that there may not always be sufficient
892   target data to constrain the microscopic model. We therefore treated the two residues as
893   symmetrical, i.e., both should be behaving in the same way, and imposed a constraint in the
894   *Multibind* approach so that both were assigned the same pK_a at each step, thus effectively
895   imposing the coupling observed in the CpHMD simulations. The interaction energies between
896   H73 and H77 for the MST-inference data are W=+6.2 (D70 deprotonated) and W=–0.70 (D70
897   protonated). The dominant state is the one with D70 deprotonated due to the low pK_a of D70
898   and hence the overall behavior of H73 and H77 remains strongly anti-cooperative in the MST-
899   inference model.

900   For Site A, the initial CpHMD simulations did not indicate any degeneracy in pK_a values
901   such as the one for H73/H77 and so no additional constraints were applied for any of the Site A
902   MST-inference calculations. We also calculated the coupling energy for H155 and D159 in site
903   A from the microscopic pK_a values (see Supplementary Data) for the CpHMD and the MST-
904   inference models for (1) no protons bound to D51 and D47 (W_{MST}=–5.05, W_{CpHMD}=+1.26), (2)
905   D51 protonated (W_{MST}=–7.39, W_{CpHMD}=+0.59), (3) D51 protonated (W_{MST}=–5.26, W_{CpHMD}=+1.02),
906   and (4) both D47 and D51 protonated (W_{MST}=–2.39, W_{CpHMD}=+1.79).Thus, refinement against
907   the experimental MST data changes the model based on the CpHMD results from anti-
908   cooperative binding (W>0) to strong cooperative binding (W<0).

909   The *inverse* Multibind approach has some limitations when applied to binding curves
910   such as the MST data. The binding isotherms, even when covering a range of pH values, do not
911   contain enough data to determine the microscopic model fully. Therefore, it was necessary to
912   use the CpHMD pK_a values to initialize the model instead of arbitrary starting values. Thus, in
913   the current implementation, the MST inference approach should be viewed as a refinement
914   process for the simulation-derived parameters, restricted or guided by the experimental data.
915   The resulting thermodynamic model allows the calculation of state probabilities (and any other
916   properties) at pH values outside the experimental range but it should be noted that these
917   calculated quantities are extrapolations that may not be accurate due to the lack of experimental
918   data to constrain the model; for instance, conformational changes may occur that could
919   drastically alter the interactions but these changes would not have been captured in a pure
920   binding model such as the one in Fig. 4h.

921   An effective pK_a under the Zn^{2+}-free condition was estimated for each residue by fitting
922   the deprotonation fractions (generated from the microscopic *Multibind* model) to the Hill-
923   Langmuir equation. The deprotonation fraction of a specific residue was calculated by summing
924   up the probabilities of microscopic states where the residue was deprotonated. The Zn^{2+}
925   concentration was set to 10^{-20} M to approximate the Zn^{2+}-free condition. For the symmetrized
926   residues H73 and H77, the Hill-Langmuir equation did not produce a satisfactory fit. In order to
927   compute macroscopic pK_a's for such a coupled system, we followed previous work (Henderson
928   et al., 2020; Ullmann, 2003) and fitted the total number of protons bound to the two residues to
929   the so-called "coupled titration model"

930
$$N_{prot} = 2 - [S_1(\mathrm{pH}) + S_2(\mathrm{pH})] = \frac{10^{(\mathrm{p}K_2 - \mathrm{pH})} + 2 \times 10^{(\mathrm{p}K_1 + \mathrm{p}K_2 - 2\mathrm{pH})}}{1 + 10^{(\mathrm{p}K_1 - \mathrm{pH})} + 10^{(\mathrm{p}K_1 + \mathrm{p}K_2 - 2\mathrm{pH})}}$$

931   where N_{prot} is the total number of protons, S_1 and S_2 are the deprotonation fractions of the two
932   residues, and pK_1 and pK_2 are the two coupled pK_a's describing the binding of the first proton

933   and the second proton to the coupled titrating sites. These two pK_a's can be interpreted as
934   effective pK_a values of two uncoupled residues.

935

936

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Competing Interests

None.

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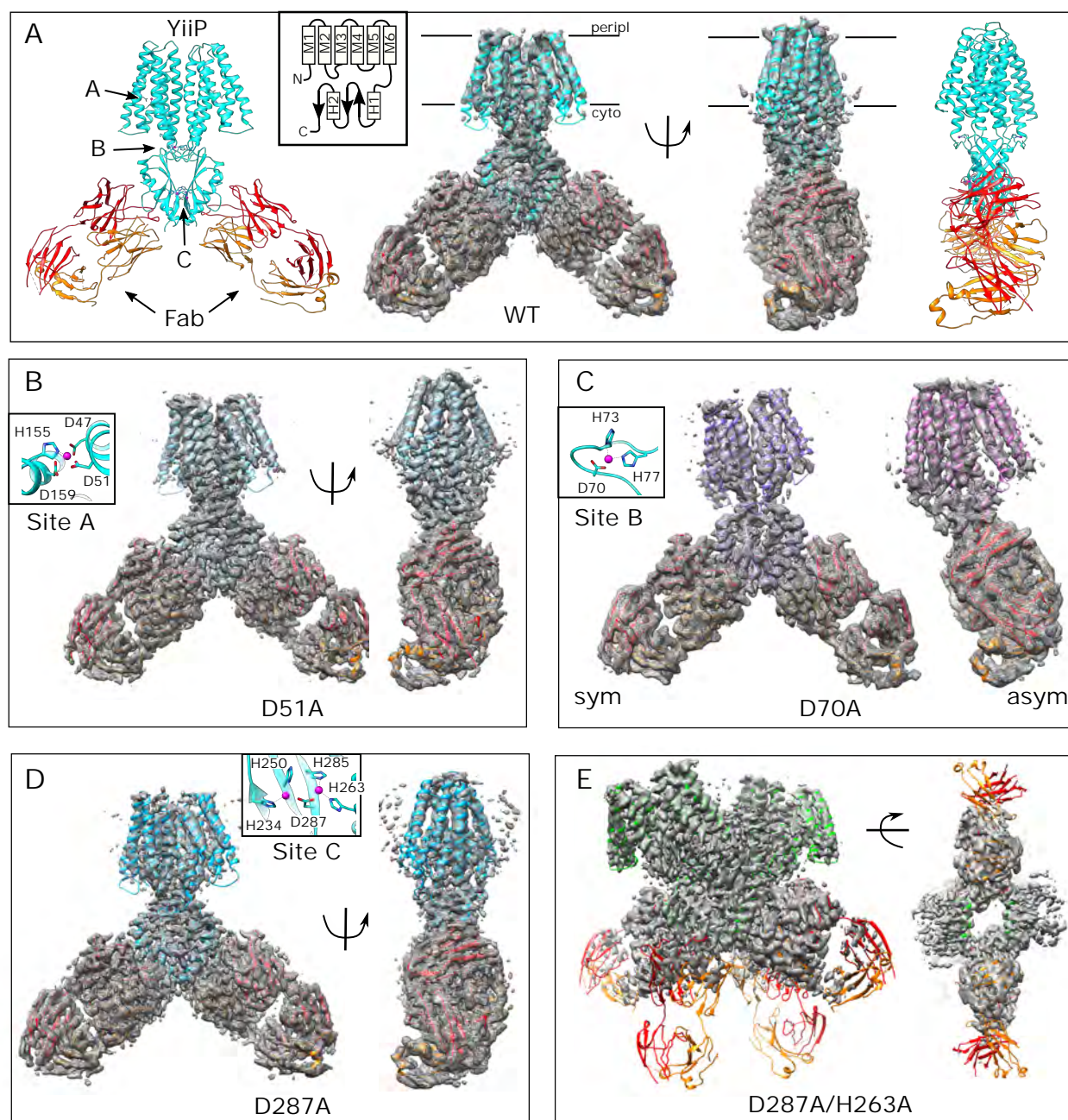
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Figure 1

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1204   Figure 1. Overview of the cryo-EM structures.

1205   Density maps and corresponding atomic models are shown for each mutant. Fab molecules are

1206   colored orange (light chain) and red (heavy chain) with YiiP colored in cyan, blue, purple and

1207   green, depending on the mutant. The homo-dimers adopt C2 symmetry for WT (A), D51A (B)

1208   and D287A (D) mutants, but a bend between TMD and CTD break this symmetry for D70A (C).

1209   The D287A/H263A mutant (E) forms a dimer of dimers in which the Fab molecules are rather

1210   disordered. Two conformations were observed for D70A, both of which are shown in panel C:

1211   D70A_sym on the left and D70A_asym on the right. Location Zn^{2+} binding sites, membrane

1212   boundaries as well as the topology of the YiiP protomer (inset) are shown in panel A; rectangles

1213   and arrows represent α-helices and β-sheets, respectively. Insets in panels B-D show the

1214   coordination geometry at the individual sites. Although the resolution was not always sufficient

1215   to uniquely define the side chain orientations, the maps are fully consistent with coordination

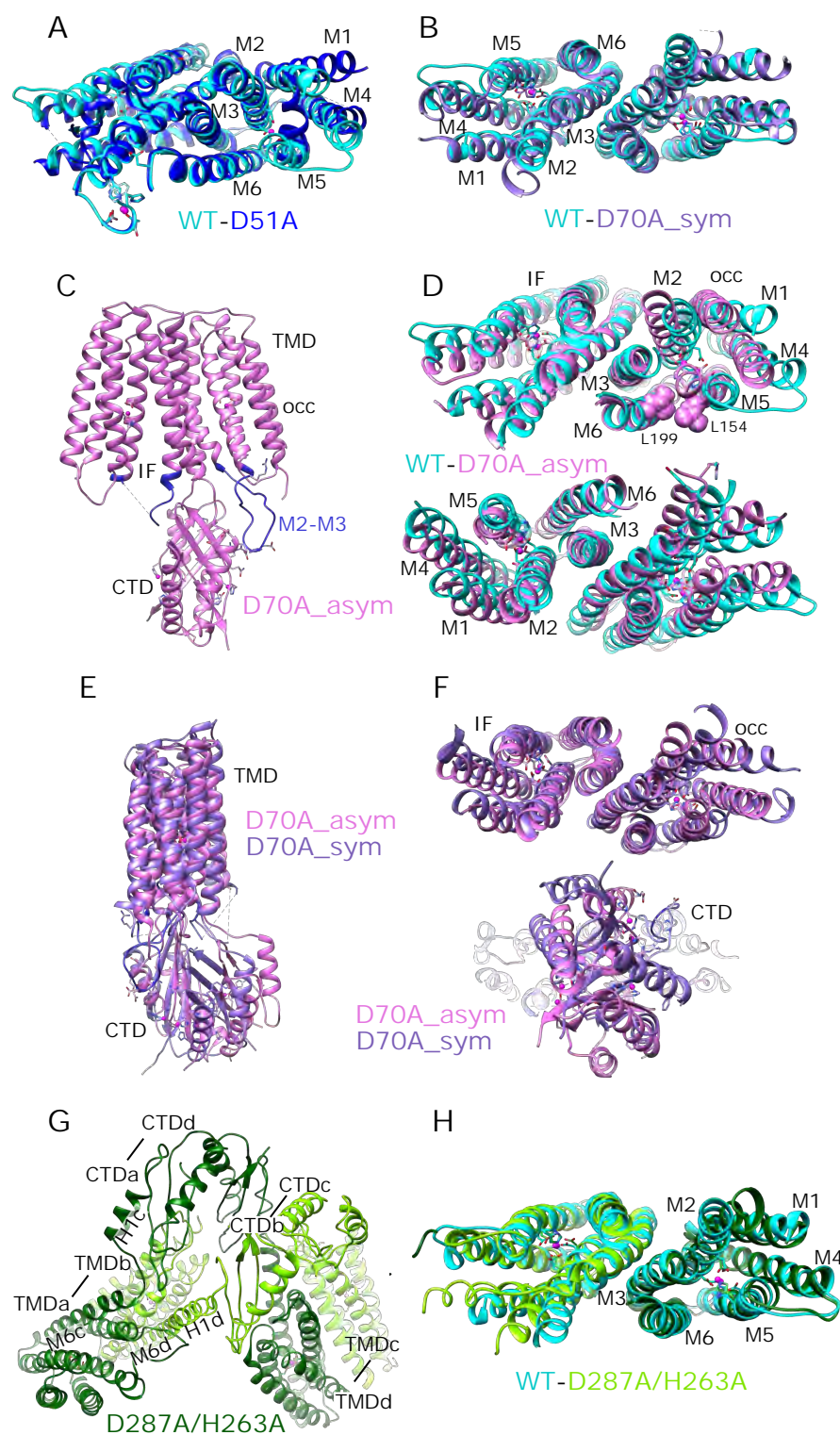1216   geometry originally defined in the higher resolution X-ray structure (Lu et al., 2009).

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Figure 2

Figure 2. Comparisons of atomic models.

(A) Overlay of the TMD for WT (cyan) and D51A (blue) structures. This view is from the cytoplasmic side of the membrane, tilted slightly to show site A in protomer A. Core helices (M2, M3, M6) are well aligned, but there are substantial displacements of the peripheral helices (M1, M4, M5), presumably due to lack of Zn^{2+} binding at site A serving to bridge M2 and M5. (B) Overlay of the TMD for WT (cyan) and D70A_sym (purple) shows a very similar configuration of helices and an intact dimeric interface. This view is directly along the two-fold axis from the cytoplasmic side of the membrane. (C) Structure of D70A_asym viewed along the membrane plane showing the asymmetry between the two TMD's. The protomer on the left (chain B) adopts an IF conformation, whereas the protomer on the right (chain A) adopts a novel occluded conformation that includes a reconfigured TM2/TM3 loop (blue) making a novel interaction with the CTD. (D) Overlay of the TMD for WT (cyan) and D70A_asym (plum) showing the occluded conformation adopted by protomer A (top) and the IF conformation adopted by protomer B (bottom). L199 and L154 (spheres) make van der Waals interactions that appear to stabilize the occluded conformation. These views are from the cytoplasmic side of the membrane, slightly tilted to show the respective protomers. (E-F) Overlays of D70A_asym (plum) and D70A_sym (purple) structures after alignment of core helices TM3 and TM6. Structures are viewed parallel to the membrane plane in E and along the two-fold axis from the cytoplasmic side of the membrane in F. A significant shift in the position of the CTD is apparent in E and bottom panel in F. Despite this shift and substantial conformational changes in the occluded protomer A, the dimer interface in the TMD (TM3 and TM6) is well aligned (F, top panel). (G) Domain swapped dimer of dimers adopted by the D287A/H263A construct. Dimerization of TMD's involves interaction between one dark-green and one light-green molecule (e.g., TMDa and TMDb, where "a" and "b" refer to chain ID), whereas dimerization of CTD's involves interaction between either two dark-green or two light-green molecules (e.g., CTDa and CTDd). The linker between M6 and the CTD adopts a long straight helix in chains b and d, but remains an unstructured loop in chains a and c. This view is from the cytoplasm looking toward the membrane surface. (H) Overlay of the TMD for WT (cyan) and D287A/H263A structures viewed along the dimer axis from the cytoplasmic side of the membrane shows a good match, indicating that disruption of site C affects mainly the configuration of the CTD.
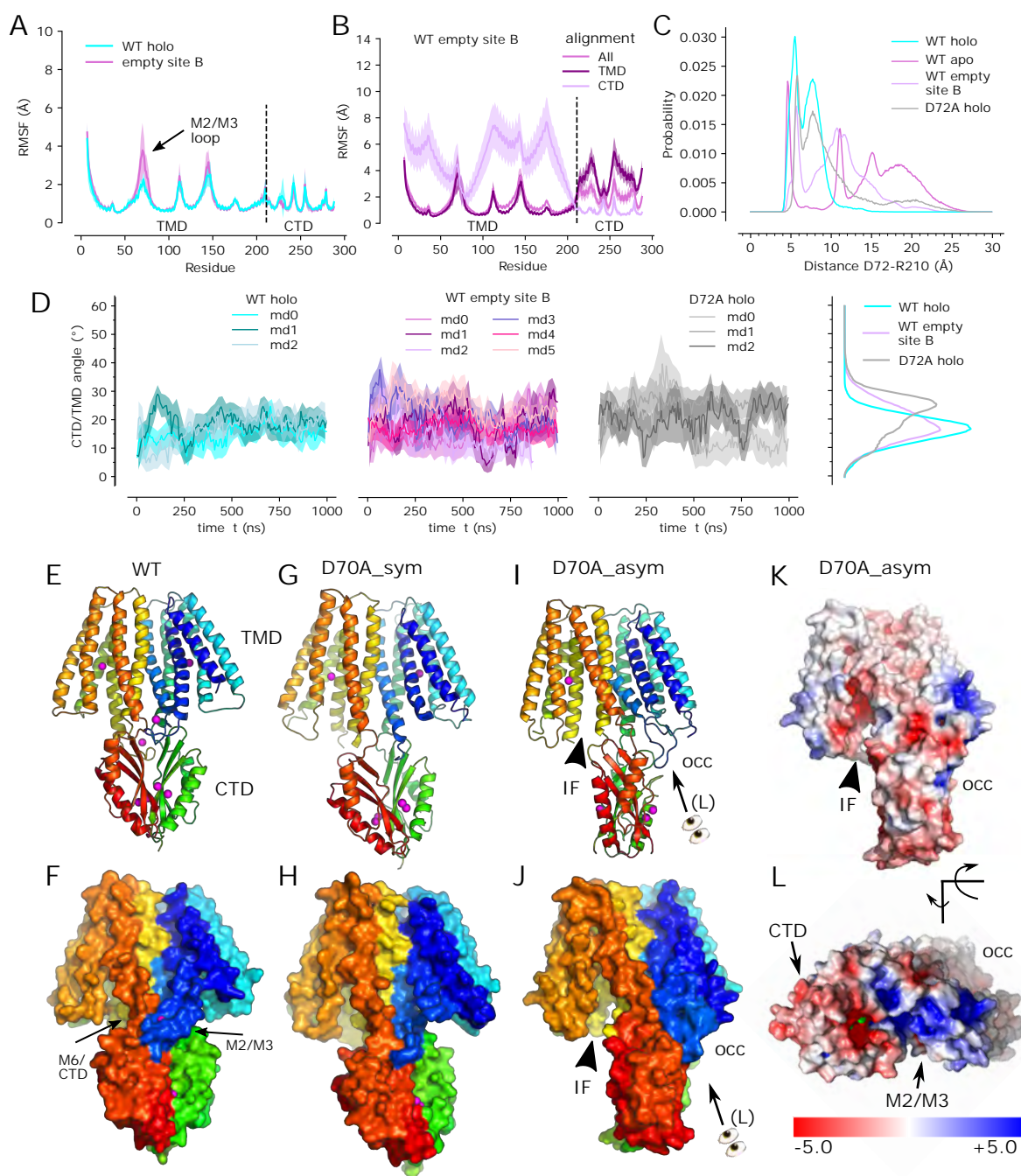
Figure 3

Figure 3. Zn^{2+} removal from site B in the TM2/TM3 loop.

(A) Per-residue RMSF of the WT, holo structure with Zn^{2+} present (cyan) and absent (purple) at site B demonstrates a notable increase in fluctuations in the TM2/TM3 loop. The dashed line indicates the boundary between TMD and CTD. (B) Per-residue RMSF for simulations with empty site B using three different alignment schemes: the entire molecule ("All"), transmembrane domain ("TMD"), or C-terminal domain ("CTD"). Analogous data for the WT, holo structure have previously been published (Fig. 3i in Lopez-Redondo et al., 2021). (C) Distributions of distance between Cα atoms from Asp72 in one chain and Arg210 in the opposite chain during simulations of the WT, holo structure, WT apo structure with Zn^{2+} absent from all sites, WT structure with site B empty, and the D72A mutant with Zn^{2+} present at all three sites. The sharp peak at ~5 Å from the holo structure suggests a salt bridge that is less stable in the D72A mutant and disrupted when Zn^{2+} is absent from site B. (D) Angle between the TMD and CTD in simulations in the presence (cyan) and absence (purple) of Zn^{2+} at site B; the D72A mutant in the holo state is also shown on the right. The distribution of angles, on the right, highlight greater mobility either with site B is empty or with the D72A mutation. (E,F) Structure of the WT, holo YiiP dimer showing global C2 symmetry about a vertical axis and juxtaposition of the TM2/3 loop (blue) with the TM6/CTD linker from the opposing protomer (orange-to-red). Rainbow colors progress from blue to red moving from the N-terminus of one protomer to the C-terminus of the other protomer. (G,H) D70A_sym structure shows a kink between TMD and CTD and disordering of the TM2/3 loop. Both protomers are in the IF state. (I,J) D70A_asym structure showing further twisting of the CTD and asymmetry of the TMD's. The TM2/3 loop is disordered in the protomer on the left (chain B), but adopts a novel interaction with the CTD in the protomer on the right (chain A). (K,L). Electrostatic surface of D70A_asym showing a negatively charged cavity leading to site A on the left, but an occluded cavity with positive charge on the right. Note that L is at an oblique angle looking down on the M2-M3 loop.
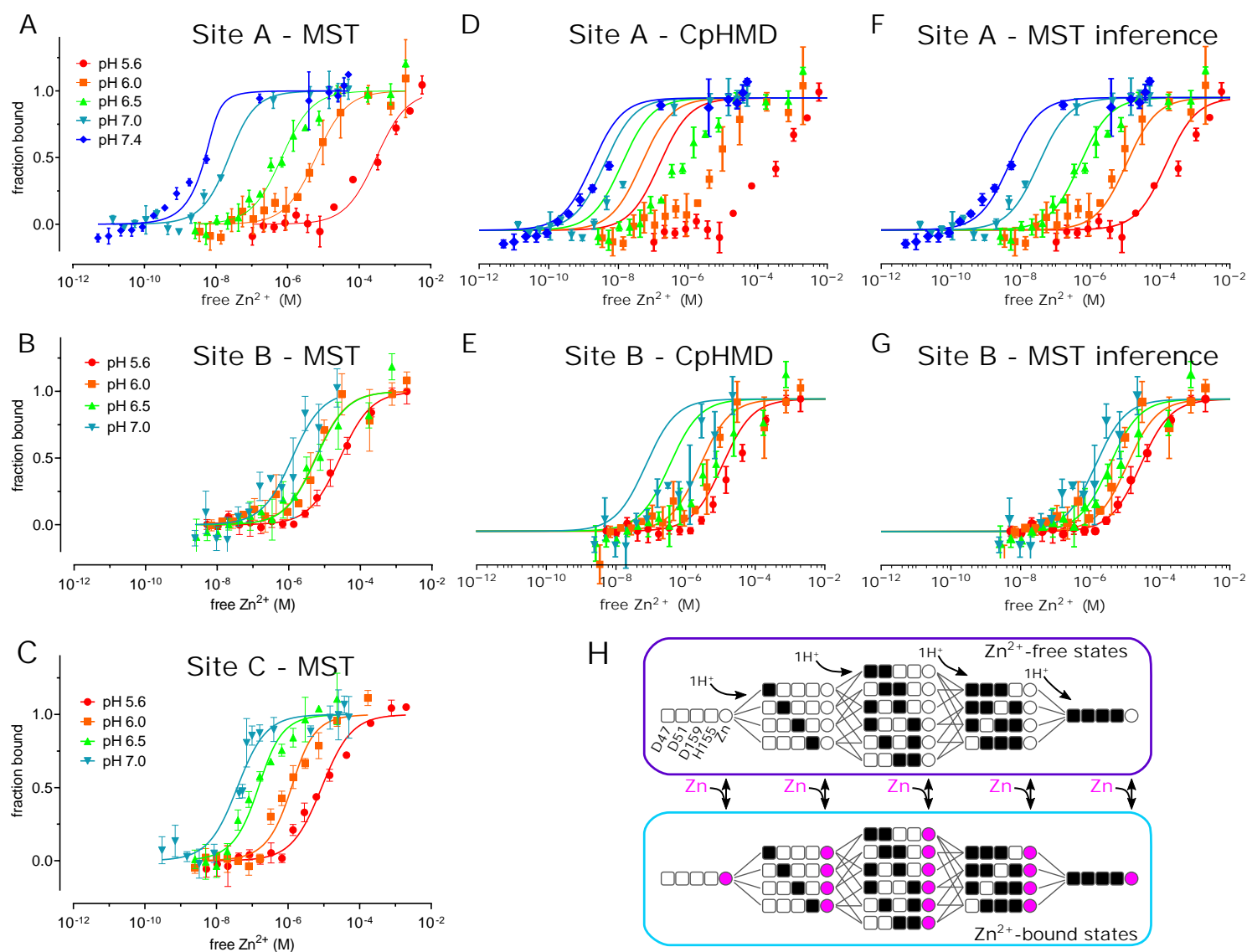
Figure 4

1275   Figure 4. pH dependence of Zn²⁺ binding.

1276   MST was used to experimentally measure Zn^{2+} binding affinity at each site (panels A, B and C).
1277   These data were combined with a thermodynamic model, represented in panel H, with
1278   parameters derived either from CpHMD (panels D and E) or MST inference (panels F and G).
1279   (A) For MST studies of site A, the D70A/D287A/H263A construct was used with Zn^{2+} buffered
1280   either with NTA (pH 7.0 and 7.4) or with citrate (pH 5.6, 6.0 and 6.5). Curves represent the law
1281   of mass action with K_d values listed in Table 2. The relatively poor fit at pH 7.4 may reflect the
1282   fact that the K_d (1 nM) is lower than the minimum protein concentration (8 nM) supported by the
1283   assay, thus moving the system from the binding to the titration regime (Jarmoskaite et al.,
1284   2020). (B). For MST studies of site B, the D51A/D287A/H263A construct was used and Zn^{2+}
1285   was buffered with citrate. (C) For MST studies of site C, the D51A/D70A construct was used
1286   and Zn^{2+} was buffered with NTA at pH 7 or with citrate at the other pH's. (D,E) Curves represent
1287   predictions of a thermodynamic model with pK_a values for either site A residues (Asp47, Asp51,
1288   His153, Asp157) or site B residues (D70, H73, H77) taken from CpHMD simulations. These pK_a
1289   values are listed in Table 4 and the distributions of protonation states are shown in Suppl. Figs.
1290   10 and 11. Symbols represent experimental MST data as in A and illustrate a poor fit using
1291   these parameters. Thermodynamic modeling was not possible for site C because of instability of
1292   the CTD in CpHMD simulations in the absence of Zn^{2+}. (F,G). Curves represent predictions of
1293   the MST inference algorithm with corresponding pK_a values listed in Table 4. Again, symbols
1294   represent experimental MST data and show the excellent fit using these refined parameters. (H)
1295   Schematic representation of the microscopic thermodynamic model for site A. Titratable
1296   residues (D47, D51, D159, H155) are represented either as black squares for the protonated
1297   state, or white squares for the deprotonated state. Binding of one Zn^{2+} ion to the site is indicated
1298   by a filled magenta circle. Transitions are only possible between states connected by lines
1299   (protonation/deprotonation) or corresponding states connected by double-sided arrows (Zn^{2+}
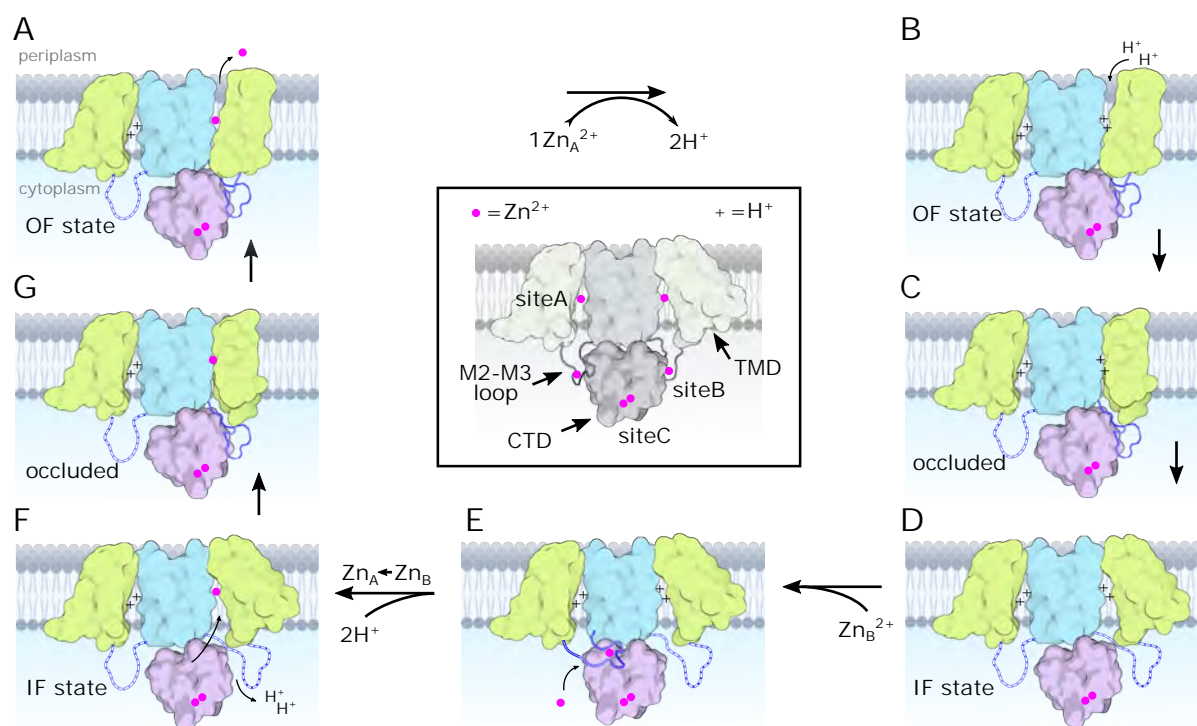1300   binding/release). An analogous model for site B comprised D70, H73 and H77 (not depicted).

1301

Figure 5

1302 **Figure 5. Transport cycle for YiiP.**

1303 According to the alternating access paradigm, YiiP toggles between the OF and IF states via an
1304 intermediate occluded state. We assume that these changes occur independently in each
1305 protomer based on asymmetry seen in structures of soYiiP and Znt8 (Xue et al., 2020). Thus,
1306 our model depicts changes in the right-hand protomer while the left-hand protomer remains in a
1307 resting IF state. Although these intermediate states are informed by current and past structural
1308 work, they do not precisely conform to solved structures but represent hypothetical states that
1309 we believe to exist under physiological conditions. (A) Zn^{2+} is released to the periplasm. The
1310 TM2/TM3 loop is depicted interacting with the CTD in a Zn^{2+}-free, extended conformation, as
1311 seen in our D70A_asym structure. (B) The release of Zn^{2+} is promoted by the low pH of the
1312 periplasm and results in protonation of two residues in site A, or potentially three residues at
1313 lower pH. (C-D) The protonated form transitions to the IF state via an occluded state. In the IF
1314 state, the Zn^{2+}-free TM2/TM3 loop is released by the CTD and becomes disordered. (E) Zn^{2+} is
1315 recruited to site B, inducing an ordered conformation of the TM2/TM3 loop that folds onto the
1316 CTD enabling interaction of Asp72 and Arg210. (F) Zn^{2+} is transferred from a relatively low
1317 affinity site B to the much higher affinity site A via a negatively charged access channel, thus
1318 displacing two protons. (G) This transfer induces a Zn^{2+}-bound, occluded conformation in which
1319 the CTD tilts toward the occluded protomer and interacts with the TM2/TM3 loop in its Zn^{2+}-free,
1320 extended conformation. Features of the model are illustrated in the middle, boxed panel with
1321 desaturated colors. Zn^{2+} ions are depicted as magenta spheres and protons with a "+". The CTD
1322 is pink with two Zn^{2+} ions constitutively bound at site C. The scaffolding membrane helices (TM3
1323 and TM6) are blue and the transport domain (TM1,2,4,5) is yellow. The TM2/TM3 loop is blue
1324 and depicted with dashed lines in the disordered state. Created with biorender.com.

1325

Tables

Table 1. Structure determination of YiiP mutants

Data set	WT	Site A D51A	Site B[1] D70A asymTMD	Site B[1] D70A symTMD	Site C D287A	Site C[2] D287A/ H263A
Deposition						
PDB	8F6E	8F6F	8F6H	8F6I	8F6J	8F6K
EMDB	EMD-28881	EMD-28882	EMD-28883	EMD-28884	EMD-28885	EMD-28886
Data collection and processing						
Magnification	81,000	81,000	81,000	81,000	81,000	81,000
Voltage (kV)	300	300	300	300	300	300
Electron exposure (e^-/$Å^2$)	50	50	50	50	50	50
Defocus range (µm)	1.0-3.0	0.75-2.75	0.7-3.0	0.7-3.0	0.7-3.0	0.7-2.5
Pixel size (Å)	1.068	1.079	1.079	1.079	1.079	1.079
Symmetry imposed	C2	C2	C1	C1	C2	C2
Initial particle images (no.)	3,058,414	3,672,562	1,702,119	1,702,119	1,664,097	2,982,749
Final particle images (no.)	536,206	196,484	188,414	182,413	252,599	300,844
Map resolution	3.78	3.63	3.93	4.03	3.68	3.46
FSC threshold (Å)	0.143	0.143	0.143	0.143	0.143	0.143
B factor ($Å^2$)	200.5	151.0	146.1	126.0	150.9	135.2
Resolution range (Å)	3.0-5.5	3.0-5.2	3.4-5.8	3.4-6.9	3.0-5.5	3.0-5.2
Model Refinement						
Model composition						
Non-hydrogen atoms	10478	10348	10421	10377	10472	8714
Protein residues	1366	1344	1358	1351	1366	1132
Ligands	8	6	6	6	8	4
RMS deviations						
Bond lengths (Å)	0.003	0.003	0.002	0.002	0.003	0.002
Bond angles (°)	0.557	0.535	0.509	0.517	0.536	0.499
Validation						
MolProbity score	1.70	1.68	1.72	1.75	1.77	1.96
Clashscore	5.44	6.31	5.78	7.11	6.37	10.28
Rotamer outliers (%)	0.00	0.09	0.00	0.00	0.00	0.00
CaBLAM outliers (%)	2.66	3.05	2.60	3.40	3.64	4.21
Rama-Z score	-0.77	-0.37	-0.05	0.20	-0.50	-0.45
Ramachandran plot						
Favored (%)	94.19	95.27	93.99	94.86	93.59	93.51
Allowed (%)	5.44	4.57	5.86	4.99	6.04	5.96
Disallowed (%)	0.37	0.15	0.15	0.15	0.37	0.53
Model vs. Data CC (mask)	0.75	0.83	0.79	0.80	0.81	0.73

[1] Both D70A structures arose from the same set of micrographs and initial particle picks.

[2] Fab molecules were not included for the refinement of D287A/H263A due to poor density in this region of the map

Table 2. Binding affinity for individual Zn^{2+} sites measured by MST* or deduced by the MST inference algorithm[§]

	site A D70A/ D287A/H263A (µM)	site A/C D70A/D287A (µM)	site B D51A/ D287A/H263A (µM)	site C D51A/D70A (µM)	site C1 D51A/ D70A/H263A (µM)	site C2 D51A/ D70A/H234A (µM)
pH 5.6	302 ± 107 (149)		27.1 ± 2.8 (19.5)	8.10 ± 1.55		
pH 6.0	6.11 ± 1.32 (10.8)	6.30 ± 1.94	5.54 ± 2.0 (5.38)	0.692 ± 0.28		
pH 6.5	0.654 ± 0.173 (0.503)		5.73 ± 1.75 (1.36)	0.088 ± 0.032		
pH 7.0	0.0163 ± 0.0041 (0.0325)	0.0012 ± 0.0018	1.18 ± 0.6 (0.503)	0.033 ± 0.0087	0.153 ± 0.048	0.223 ± 0.039
pH 7.4	0.001 ± 0.001 (0.0048)					

* Values correspond to K_d as determined by applying the law of mass action to the data.
[§] Values deduced by MST inference are shown in parentheses

Table 3. Binding affinity and Hill coefficients derived from MST data*

	site A D70A/ D287A/H263A (µM)	site B D51A /D287A/H263A (µM)	site C D51A/D70A (µM)	site C1 D51A/ D70A/H263A (µM)	site C2 D51A /D70A/H234A (µM)
pH 5.6	1490 ± 2460 n=0.46	28.4 ± 3.54 n=0.94	7.50 ± 2.20 n=0.9		
pH 6.0	6.34 ± 1.67 n=0.81	5.68 ± 1.57 n=1.60	1.39 ± 0.382 n=0.78		
pH 6.5	0.622 ± 0.198 n=0.54	27.9 ± 34.3 n=0.38	0.133 ± 0.0359 n=0.66		
pH 7.0	0.0247 ± 0.0057 n=1.0	4.23 ± 13.0 n=0.45	0.0486 ± 0.0038 n=2.9	0.116 ± 0.0119 n=2.96	0.212 ± 0.0328 n=1.2
pH 7.4	0.0039 ± 0.0009 n=0.56				

* Values correspond to EC_{50} and the Hill coefficient (n) as determined by fitting the Hill equation to the data.

Table 4. pK_a values of residues determined by CpHMD simulations (Hill-Langmuir) and MST inference

		CpHMD (Hill-Langmuir)	MST inference
Site A	Asp47	3.84 ± 0.18	-0.20 ± 0.51
	Asp51	2.92 ± 0.12	6.51 ± 0.21
	His155	7.97 ± 0.15	7.82 ± 0.15
	Asp159	4.87 ± 0.18	7.83 ± 0.15
Site B	Asp70	2.06 ± 0.46	1.12 ± 0.57
	His73*	8.08 ± 0.46	12.37 ± 0.61*
	His77*	8.12 ± 0.13	5.26 ± 0.47*

* Titration curves for His73 and His77 from the MST inference model cannot be fit individually with a simple Hill equation (c.f. Suppl. Figs. 11e & f). We therefore consider these two residues as a coupled system with two effective pK_a values as shown.

Table 5. MD simulations

Simulation	length	N of replicas	Total simulation time	software
Fixed charge *apo**	1000 ns	3	3000 ns	GROMACS
Fixed charge *holo**	1000 ns	3	3000 ns	GROMACS
Fixed charge *empty site B*	1000 ns	6	6000 ns	GROMACS
Fixed charge D72A	1000 ns	3	3000 ns	GROMACS
CpHMD apo	12 ns	30 (pHREX)	360 ns	CHARMM

"Fixed charge" simulations were repeated three times. The CpHMD simulations were performed as coupled pH-replica exchange simulations.

*Simulations for apo and holo YiiP were taken from our previous work (Lopez-Redondo et al., 2021)

Table 6. MST convergence criteria

Target	Binding site	RMSD cutoff
CpHMD microstate probability distributions	Site A	0.0382
CpHMD microstate probability distributions	Site B	0.0447
MST bound fraction	Site A	0.0760
MST bound fraction	Site B	0.0995