

1 Title:

2 The relationship between eDNA particle concentration and organism abundance in nature is
3 strengthened by allometric scaling

4

5 Running title:

6 Abundance and allometric scaling in eDNA production

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16

17 **Abstract**

18 *Organism abundance is a critical parameter in ecology, but its estimation is often challenging.*

19 *Approaches utilizing eDNA to indirectly estimate abundance have recently generated substantial*

20 *interest. However, preliminary correlations observed between eDNA concentration and*

21 *abundance in nature are typically moderate in strength with significant unexplained variation.*

22 *Here we apply a novel approach to integrate allometric scaling coefficients into models of eDNA*

23 *concentration and organism abundance. We hypothesize that eDNA particle production scales*

24 *non-linearly with mass, with scaling coefficients < 1. Wild populations often exhibit substantial*

25 *variation in individual body size distributions; we therefore predict that the distribution of mass*

26 *across individuals within a population will influence population-level eDNA production rates. To*

27 *test our hypothesis, we collected standardized body size distribution and mark-recapture*

28 *abundance data using whole-lake experiments involving nine populations of brook trout. We*

29 *correlated eDNA concentration with three metrics of abundance: density (individuals/ha),*

30 *biomass (kg/ha), and allometrically scaled mass (ASM) ($\sum(\text{individual mass}^{0.73})/\text{ha}$). Density and*

31 *biomass were both significantly positively correlated with eDNA concentration (adj. $R^2 = 0.59$*

32 *and 0.63, respectively), but ASM exhibited improved model fit (adj. $R^2 = 0.78$). We also*

33 *demonstrate how estimates of ASM derived from eDNA samples in ‘unknown’ systems can be*

34 *converted to biomass or density estimates with additional size structure data. Future experiments*

35 *should empirically validate allometric scaling coefficients for eDNA production, particularly*

36 *where substantial intraspecific size distribution variation exists. Incorporating allometric scaling*

37 *may improve predictive models to the extent that eDNA concentration may become a reliable*

38 *indicator of abundance in nature.*

39

40 Keywords:

41 environmental DNA, eDNA, Abundance, Density, Biomass, Allometry, Allometric scaling

42 **Introduction**

43 Developing methods to estimate animal abundance in nature has attracted the attention of
44 researchers and managers alike for over a century (Schwarz & Seber, 1999). Abundance is a
45 fundamental population parameter in ecology, conservation, and natural resource management
46 (Luikart, Ryman, Tallmon, Schwartz, & Allendorf, 2010), with direct impacts on ecological
47 interactions (Krebs, 2009), ecosystem functioning (Schaus et al., 2010), population persistence
48 and adaptability (Jamieson & Allendorf, 2012), as well as ecosystem services/resources (Immell
49 & Anthony, 2008; Schwarz & Seber, 1999). Methodologies to estimate animal abundance
50 represent a well-developed field of empirical research in ecology that has progressed remarkably
51 (Schwarz & Seber, 1999; Seber, 1986). Yet despite this success, the estimation of abundance in
52 nature is often challenging; obtaining robust estimates in natural populations using traditional
53 methods can be time-consuming, costly, labor intensive, or even impossible to obtain for some
54 populations (Luikart et al., 2010; Ovenden et al., 2016; Yates, Bernos, & Fraser, 2017).

55 The recent development of novel molecular tools has renewed interest in utilizing genetic
56 information to indirectly estimate abundance in difficult-to-sample natural populations
57 (Goldberg, Strickler, & Pilliod, 2015; Luikart et al., 2010). Molecular techniques that quantify
58 the concentration of environmental DNA (eDNA) particles represent a promising tool, with
59 recent studies demonstrating support for a correlation between eDNA concentration and
60 abundance (Pilliod, Goldberg, Arkle, & Waits, 2013; Takahara, Minamoto, Yamanaka, Doi, &
61 Kawabata, 2012; Thomsen et al., 2012). In addition to monitoring of species of conservation
62 concern, eDNA represents a potential indirect-but-accurate means to quantify abundance that has
63 broad implications for species harvesting, invasive species control, and monitoring of key
64 indicator species used to assess ecosystem health (Barnes & Turner, 2016).

65 Laboratory studies have demonstrated a strong correlation between eDNA concentration
66 and abundance (Eichmiller, Miller, & Sorensen, 2016; Klymus, Richter, Chapman, & Paukert,
67 2015), exhibiting a mean correlation coefficient of 0.9 ($R^2 = 0.81$) (Yates, Fraser, & Derry,
68 2019). Studies in nature, however, have generally found weaker correlations than laboratory
69 studies, with a mean correlation coefficient of 0.71-0.75 ($R^2 = 0.51-0.57$) (Yates et al., 2019).
70 Although correlations remain moderately strong in nature, much of the variation in eDNA
71 particle concentration across environments often remains unexplained. As a result, the extent to
72 which eDNA could be used to reliably infer abundance in nature remains limited without
73 significant improvements in modelling or technology.

74 In nature, organismal abundance is typically quantified by evaluating individual density
75 (i.e. individuals/unit area) or biomass density (i.e. kg/unit area). While both metrics of abundance
76 appear to correlate equally well with species-specific eDNA particle concentration in the wild,
77 processes involved in the production of eDNA particles in natural environments are unlikely to
78 scale linearly with either biomass or density. Although eDNA production tends to increase with
79 individual mass (Maruyama, Nakamura, Yamanaka, Kondoh, & Minamoto, 2014), individuals
80 with a large biomass often produce fewer eDNA particles than equivalent biomass of smaller
81 conspecifics (Maruyama et al., 2014; Mizumoto, Urabe, Kanbe, Fukushima, & Araki, 2018;
82 Takeuchi, Iijima, Kakuzen, Watanab, & Yamada, 2019). As such, eDNA particle concentration
83 would be expected to vary, for example, between environments that contain equal densities of
84 individuals but with varying biomass. Similarly, environments with equal biomass but varying
85 densities would also be likely to vary in observed eDNA particle concentration. Wild populations
86 often exhibit substantial inter-population variation in the distribution of individual biomass
87 (Donald, Anderson, Mayhood, Anderson, & Correlations, 1980; Guernon, Yates, Fraser, &

88 Derry, 2018; Millien et al., 2006; Sebens, 1987), which may in turn scale to affect overall
89 population-level rates of eDNA production (Maruyama et al., 2014) and partially account for the
90 substantial unexplained variation observed between eDNA concentration and traditional metrics
91 of abundance (e.g. density and biomass) in nature (Yates et al., 2019).

92 Here, we extend models of physiological allometric scaling to organismal eDNA particle
93 production to provide a framework through which differences in density, total biomass, and the
94 distribution of individual biomass can be integrated into models of eDNA production in natural
95 populations. Allometry refers to changes in organisms (e.g. physiological rates, morphology,
96 etc.) that occur in relation to proportional changes in body size (Gittleman, 2011). Excretory
97 processes (urine, fecal matter, etc.) and shedding (from scales, skin, mucous, etc.) are thought to
98 be the two major physiological processes that contribute to the production of eDNA particles (Jo,
99 Murakami, Yamamoto, Masuda, & Minamoto, 2019; Stewart, 2019). The metabolic theory of
100 ecology (MTE) provides a robust, empirically validated framework through which allometry in
101 metabolic processes (including excretion) can be modelled (Brown, Gillooly, Allen, Savage, &
102 West, 2004). The MTE posits that metabolic processes scale non-linearly with body size
103 according to the power function:

$$I = I_0 * M^b$$

104 where I = metabolic rate, I_0 = a normalization constant, M = organism body mass, and b = an
105 allometric scaling coefficient (Allegier, Wenger, Rosemond, Schindler, & Layman, 2015; Brown
106 et al., 2004; Vanni & McIntyre, 2016). The value of b varies depending on the physiological
107 process; metabolic rates typically scale to the power of 0.75 (Brown et al., 2004; Isaac &
108 Carbone, 2010), whereas values for consumptive or excretory rates are often lower (Post,
109 Parkinson, & Johnston, 1999; Vanni & McIntyre, 2016). Nevertheless, metabolic theory predicts

111 that larger organisms tend to exhibit disproportionately lower rates (relative to their mass) for
112 metabolically linked processes such as excretion (Allen & Gillooly, 2009; Vanni & McIntyre,
113 2016). While shedding from mucous, scales, or skin may also be linked to metabolic rates,
114 shedding rates are also likely a function of the surface area of an organism. In many aquatic
115 organisms (particularly fish) the allometric relationship between body mass and surface area
116 follows a similar mathematical form as metabolic processes; salmonids, for example, exhibit
117 mass-scaling coefficients for surface area between 0.59 and 0.65 (Shea, Fryer, Pert, & Bricknell,
118 2006).

119 Metabolic rates, excretory rates, and surface area (via shedding) are likely to collectively
120 impact eDNA production, yet all follow a similar allometric form. As a result, we hypothesize
121 that eDNA production can also be modelled as an approximate power function of individual
122 mass and an exponential scaling coefficient with a value less than 1. That is, the rate at which
123 eDNA production increases with body mass will decline (Figure 1a) such that, on a per-gram
124 basis (e.g. mass-specific rate), large individuals will tend to excrete fewer eDNA particles
125 relative to smaller conspecifics (Figure 1b). This hypothesis has important consequences for
126 ecosystem-level processes; the utility of integrating allometric scaling in ecosystem-level models
127 of ecological stoichiometry (Allen & Gillooly, 2009), animal excretion (Vanni & McIntyre,
128 2016), consumption (Post et al., 1999), and nutrient cycling (Schaus et al., 2010; Schindler &
129 Eby, 1997), for example, has long been acknowledged with broad empirical support. We
130 therefore further hypothesize that, when scaled to the level of an entire population, allometric
131 scaling in eDNA production will also have a substantial effect on overall population-level
132 production of eDNA. We consequently predict that the incorporation of mass scaling coefficients
133 to account for inter-population variation in density, biomass, and the distribution of biomass

134 across individuals will improve modelling efforts linking eDNA particle concentration and
135 abundance across natural ecosystems.

136 To test our hypothesis, we collected standardized individual biomass data and used
137 common mark-recapture experiments to enumerate abundance in nine populations of brook trout
138 (*Salvelinus fontinalis*) in the Rocky Mountains of Canada while simultaneously collecting eDNA
139 samples in each lake. Study populations exhibited substantial variation in individual density (63 -
140 1177 individuals/ha), biomass density (12.6 - 52.4 kg/ha), and mean body size (43.0 - 405.9
141 g/individual). We applied these data to specifically test two key predictions: i) brook trout eDNA
142 particle concentration will correlate with traditional metrics of abundance (density and biomass)
143 across the nine study lakes; and ii) incorporating allometric scaling coefficients to estimates of
144 brook trout abundance (e.g. $\sum(\text{individual biomass}^{0.73})/\text{ha}$, or “allometrically scaled mass”
145 (ASM)) will substantially improve models of abundance and eDNA particle concentration.

146 ASM estimates derived from known eDNA concentrations in novel systems lacking
147 abundance data cannot be directly converted to traditional metrics of abundance (e.g. density and
148 biomass) because multiple density/biomass configurations (e.g. many small fish or a small
149 number of large fish) can produce equivalent ASM values. However, using a real-world
150 example, we also demonstrate how ASM estimates derived from known eDNA concentrations
151 for systems that lack abundance data on a target species can be converted into traditional
152 estimates of abundance with additional size structure data.

153 **Materials and Methods**

154 *Study species and system*

155 Nine brook trout populations introduced in the early 20th century to lakes located in
156 Kootenay, Banff, and Yoho national parks (Figure S1) were monitored to determine population
157 size and individual biomass distributions. Brook trout represent ideal populations to study
158 allometry in eDNA production and its impact on the relationship between eDNA particle
159 concentration and abundance. Several studies have already demonstrated significant correlations
160 between abundance and eDNA concentration for brook trout in lotic systems (Baldigo, Sporn,
161 George, & Ball, 2017; Wilcox et al., 2016). Brook trout populations also often exhibit substantial
162 variation in size structure (Donald et al., 1980; Guernon et al., 2018), providing the opportunity
163 to study populations that represent a gradient of small-to-large bodied individuals. Additionally,
164 our study populations experience little recreational fishing pressure due to no-take policies
165 implemented within the National Parks.

166

167 *Mark-recapture surveys and size structure estimates*

168 Mark-recapture studies were conducted in 2018 between May 27th and June 30th, except
169 for Cobb lake where isolated marking events occurred until September 12th (Figure S2). Fish
170 were captured using a combination of fyke nets, angling, and backpack electrofishing (Table 1).
171 Large (1 m hoop diameter, 2 cm mesh) and small (0.7 m hoop diameter and 0.8 cm mesh) fyke
172 nets were distributed around the perimeter of lakes with the lead attached to shore and the end of
173 the trap facing the center of the lake. Nets were checked daily to reduce stress to fish and
174 possible cannibalism. Angling was used to supplement fish capture efforts at sites where fyke
175 catchability was low (predominantly Cobb). Marks were also assigned to fish captured by

176 electrofishing the shore and inlets/outlets of lakes with a backpack electrofisher (Smith-Root,
177 Vancouver, Washington, USA)

178 Captured fish were anesthetized using clove oil and measured for fork length ($\pm 1\text{mm}$)
179 and mass ($\pm 0.1\text{g}$). Any unmarked fish were gastrically tagged with a BioMark HPT8 pre-loaded
180 Passive Integrated Transponder (PIT) tag (Boise, Idaho, USA). Only fish greater than or equal to
181 80 mm were tagged to reduce tagging mortality. The tag number of any recaptured fish was
182 recorded. All fish were processed in the shade with aerators to avoid unnecessary stress.

183 Recovered fish were released in the center of the lake to standardize release location and
184 promote mixing (e.g. if released near shore, fish may have been recaptured in an adjacent net,
185 biasing mark recapture data). Marking ceased once recapture ratios approached twenty five
186 percent for several consecutive days in order to standardize marking efforts across
187 all populations and to ensure that enough fish were tagged to facilitate census size (N_c) estimates
188 have confidence intervals within 10% to 25% of true values, following general methodologies
189 reviewed in (Krebs, 2009).

190 Size structure estimates aimed to obtain a representative snapshot of the size structure of
191 each population and were conducted between July 27th and September 1st, with the exception of
192 Cobb where size structure assessments continued to October 12th (Figure S2). Fyke-nets were
193 deployed in littoral zone areas extending to the centre of the lake and, as a result, size-structure
194 assessments may be more biased towards small-medium bodied individuals (who prefer littoral
195 habitats) (Tiberti et al., 2017). To obtain a relatively unbiased estimate of population size
196 structure, fish were captured in large and small sinking mixed mesh gillnets with clear
197 monofilament distributed throughout the lake. Large mixed-mesh gillnets were 15.6 m long, 1.8
198 m deep and had an equal area of 64-51-89-38-76 mm mesh panels. Small mixed-mesh gillnets

199 were 12.5 meters long, 1.8 meters deep, and consisted of an equal area of 32-19-38-13-25 mm
200 mesh panels. Index nets are widely used in North America for size structure assessments (Bonar,
201 Hubert, & Willis, 2009; Hubert, Pope, & Dettmers, 2012; Johnson, 1983; Post et al., 1999; Ward,
202 Askey, Post, Varkey, & Mcallister, 2012) as these attempt to capture a representative size/age
203 structure of the population (Morgan, 2002). Nets were checked daily and moved to different
204 locations across the lake if reset in order to capture a representative sample of fish in each lake.
205 Sampling ceased when approximately five to ten percent of the population was captured, apart
206 from Cobb lake where size structure assessment captured approximately 71% of individuals
207 (Table 1). Captured fish were euthanized with clove oil, PIT tags were recorded, and length/mass
208 data were collected as described for the marking period.

209

210 *Population size estimation*

211 Schnabel population size estimates, which utilize sequential marking/recapture events,
212 were used to determine the number of fish in a lake (Schnabel, 1938). All size structure
213 assessment removals were pooled together into one final sampling event for the population
214 estimates which controlled for the removal of marks at large. Note that population estimates only
215 account for fish greater than the minimum tagging size (80 mm fork length). All population
216 estimates were conducted in R (R Development Core Team, 2017) with the *mrClosed* function
217 from the Fisheries Stock Assessment package FSA (Ogle, 2016). Confidence intervals for
218 Schnabel population estimates followed recommendations from (Seber, 2002) as implemented in
219 the FSA package.

220 *Density calculation*

221 To link eDNA particle concentration with fish abundance, three metrics of density were
222 calculated: (i) individual density (individuals/ha); (ii) biomass density (biomass/ha); (iii) and
223 allometrically scaled mass (ASM/ha). Individual density was estimated by dividing the
224 population size estimate by lake size (ha). Biomass density was calculated according to the
225 following formula:

$$\text{biomass per ha} = \frac{\sum_{i=1}^{N_{SA}} \text{mass}_{SAi} \cdot \hat{N}}{N_{SA} \text{ area (ha.)}}$$

226 Where $\sum_{i=1}^{N_{SA}} \text{Mass}_{SAi}$ is the sum of the masses captured in the index net during size structure
227 assessment, N_{SA} is the number of fish captured in the index nets, \hat{N} is the estimated population
228 size. This methodology assumes that the size structure assessment was representative of the
229 population.

230 ASM was calculated by replacing the mass measure with $\text{mass}^{0.73}$ according to the
231 formula:

$$\text{ASM per ha} = \frac{\sum_{i=1}^{N_{SA}} (\text{mass}_{SAi}^b) \cdot \hat{N}}{N_{SA} \text{ area (ha.)}}$$

232
233 This density metric was included to account for the relative decline in mass-specific eDNA
234 production or excretion rates typically observed as individual organismal mass increases
235 (Maruyama et al., 2014; Takeuchi et al., 2019; Vanni & McIntyre, 2016). Scaling coefficients
236 (the value of b) can vary substantially depending on the physiological process, taxonomy or
237 environment (Allegier et al., 2015; Glazier, 2005). In the absence of data on allometric scaling in
238 eDNA production, data on allometric scaling in metabolic or excretory rates for the same study

239 species can represent useful starting points. Data on allometry in excretory rates were
240 unavailable for brook trout. However, in laboratory experiments (Hartman & Cox, 2008) found
241 that mass-specific metabolism scaled as a power law of mass with an exponent of -0.265. The
242 scaling exponent for absolute metabolism would therefore be $1 - 0.265 = 0.735$, which we used
243 as the value of b in our ASM model.

244 In difficult to sample populations, estimates of relative abundance are often obtained
245 using catch-per-unit-effort (CPUE) metrics. As a result, most previous studies examining eDNA
246 particle concentration and abundance utilize similar metrics (Yates et al., 2019). To evaluate the
247 utility of CPUE as a ‘proxy’ metric of abundance in our study system, CPUE for each lake was
248 quantified as the mean catch per-unit effort of a large and small index gillnet.

249

250 *eDNA sample collection*

251 eDNA samples were collected between June 30 and July 13th, 2018. Sampling was
252 equidistantly distributed around each lake and included four littoral and four pelagic samples.
253 Littoral samples were collected approximately 1-3 m from shore at a depth of least 30 cm but 15
254 cm above the bottom to avoid the unintentional collection of sediments, which can contain
255 concentrated eDNA but also inhibit PCR reactions (Turner, Uy, & Everhart, 2015). Surface
256 pelagic samples were collected from each lake along a vertical line through its center (identified
257 as the midpoint of its longest axis); samples were collected along this axis at equidistant intervals
258 within the first meter of depth (approximately 0.5m). eDNA for most fish species tends to be
259 uniformly distributed throughout the water column of deep lakes (Hanfling et al., 2016) and
260 shallow ponds (Evans et al., 2017). A thermal profile of the lake (e.g. temperature reading every
261 0.5 m using a YSI professional series sonde (model 10102030) (Yellow Springs Inc., Ohio,

262 USA)) at the deepest point was taken immediately after sample collection. To avoid between-
263 lake contamination all eDNA samples were collected either from an inflatable kayak that was
264 decontaminated 48h prior in a 2% regular strength household bleach solution for 15 minutes
265 (including paddle and life-jacket) or from a canoe assigned to sample a single specific lake.
266 Water samples were collected using sterile Whirl-PakTM bags (Uline, Ontario, Canada).

267 Samples were immediately filtered on the lakeshore using two chlorophyll filtering
268 manifolds (Wildco, Florida, USA) bleached in a 30% household bleach solution for ten minutes
269 2-12h prior to collection. All samples were stored in the shade prior to filtration in plastic
270 washbasins bleached with a 30% solution for ten minutes, and all filtering was conducted in the
271 shade under a tarp. Manifolds were transported in a Polar BearTM backpack cooler (Polar Bear
272 Coolers, Georgia, USA) whose interior was wiped with a 30% household bleach solution for ten
273 minutes. Manifold components were stored after bleaching and transported individually in sealed
274 plastic zippered bags to limit contamination. Pencils and markers were also wiped with a 30%
275 bleach solution.

276 One L of sample water from each site was filtered through a 0.7 μ m-pore glass fibre filter
277 (GE Healthcare Life Sciences, Ontario, Canada) using a vacuum hand pump (Soil Moisture,
278 California, USA); each vacuum pump was decontaminated between lakes by wiping with a 30%
279 household bleach solution and resting for ten minutes. All littoral samples were filtered on one
280 manifold and all pelagic samples were filtered on the other. Prior to filtering lake water samples,
281 1 L of distilled water was filtered through each manifold as a negative control. Filters were
282 handled using two metal forceps bleached in a 30% solution for ten minutes and transported in
283 individual bags; one forceps was used for littoral samples and another forceps was used for
284 pelagic samples. After filtering, filters were folded and placed directly in a sterile 2 ml

285 microcentrifuge tube filled with 700 μ l AL buffer (Qiagen, Maryland, USA) which was then
286 labelled and individually sealed in a plastic zippered bag and placed in a second cooler that was
287 decontaminated by wiping with a 30% household bleach solution and resting for ten minutes.
288 This cooler contained two frozen freezer-gel packs decontaminated in a 30% bleach solution for
289 ten minutes. If a filter became clogged (i.e. < 1 L of water was filtered) the final volume of water
290 filtered was recorded and the sample was stored in buffer. Filters were immediately transported
291 to, and stored in, a -20 $^{\circ}$ freezer (wiped with 30% household bleach and soaked for ten minutes)
292 at Kootenay Crossing. Filters were stored on dry ice for transportation to Montreal (driven
293 approximately two and a half days) where they were stored in a -80 $^{\circ}$ freezer.

294 *eDNA extraction and analysis*

295 Each filter was extracted using a Qiagen DNeasy Blood and Tissue TM kit and
296 QiashdredderTM spin column following a modified extraction protocol (see Appendix S1 for
297 details). Final DNA product was eluted into 130 μ l of AE buffer and stored in a clean -20 $^{\circ}$
298 freezer dedicated to the sole storage of eDNA samples. To avoid contamination between lakes,
299 extractions were conducted on batches from a single lake with a single extraction blank of 700
300 μ L AL buffer included as an extraction control. Decontamination procedures were identical for
301 both manifolds, so only a single negative control was extracted per lake. All extractions were
302 conducted in an extraction room dedicated to the handling of sensitive eDNA samples. This
303 room receives weekly cleaning with a 10% household bleach solution and is free of PCR
304 products or high-concentration DNA. All individuals entering the extraction room were required
305 to wear nitrile gloves, hair nets, shoe covers, and dedicated, clean lab coats. All lab surfaces were
306 soaked with a 20% household bleach solution for ten minutes before and after extractions. PCR

307 Clean WipesTM (Thermo Scientific, Massachusetts, USA) were also used to decontaminate all
308 lab surfaces and pipettes prior to and after extracting or handling eDNA samples.

309 The concentration of brook trout eDNA was quantified using the TaqMan minor groove
310 assay published in (Wilcox et al., 2013), which targets a region of the brook trout cytochrome *b*
311 mitochondrial gene. All samples were run in triplicate at a 20 μ l final reaction volume on a
312 Stratagene MX 3000P thermal cycler using Environmental Master Mix 2.0 and 5 μ l of template
313 DNA. Forward and reverse primers were included at a final concentration of 900 nM, with the
314 probe at a final concentration of 250 nM. Each replicate was spiked with an internal positive
315 control to test for inhibition; any replicate that exhibited inhibition ($C_t > 1$ in the internal positive
316 control) was reanalyzed with diluted template DNA at 60% concentration (3 μ l template + 2 μ l
317 of ultrapure water); this was sufficient to relieve inhibition in all cases. Standard curve template
318 DNA was composed of a synthetic GblockTM gene fragment (IDT, Iowa, USA) of the targeted
319 sequence. A triplicate no template control and triplicate five-point standard curve (1250
320 copies/ μ l, 250 copies/ μ l, 50 copies/ μ l, 5 copies/ μ l, 2 copies/ μ l template concentration) were
321 included on each 96-well plate. All qPCR reaction reagents were aliquoted into single-use
322 volumes adequate for a single plate and reactions were prepared in the dedicated eDNA room,
323 with the exception of the standard curve replicates due to the presence of high concentration
324 synthetic DNA fragments. Reactions were cycled with an initial hold at 95 \square for ten minutes
325 followed by 45 cycles of 30 seconds at 95 \square and 1 min at 60 \square . eDNA particle concentration at
326 each site was determined by averaging site-specific replicates. Final mean copy number values
327 were converted (based on total volume of water filtered per sample) to total eDNA particle
328 concentration per 1 L of sampled water (copies/L).

329 *Data Analysis*

330 Mean eDNA particle concentration (copies/L) for each lake was calculated by first
331 averaging eDNA particle concentrations of the four littoral and four pelagic samples to obtain
332 mean littoral eDNA concentration and mean pelagic eDNA concentration. A weighted-mean
333 eDNA concentration for each lake was calculated by weighing the littoral and pelagic eDNA
334 concentrations based on the fraction of total lake area each zone represented. Our study lakes
335 varied substantially in size (1.7 to 18.5 ha); total pelagic and littoral areas were calculated for
336 each lake using polygons on Google Earth. In the absence of detailed bathymetry data, the total
337 area of the littoral zone (where sunlight can reach the lake bottom to support submerged
338 macrophyte and benthic primary production (Kalff, 2001)) was calculated by including all lake
339 surface area up to 20m from the shore, with the remaining area assigned to the pelagic zone. A
340 distance of 20 m was chosen because, based on personal observation, we estimate that the littoral
341 zone of the lakes extended an average of approximately 10-15 m from the shore. The
342 concentration of eDNA near points of high concentration (i.e. high fish density or areas where
343 fish feed) decreases rapidly, with concentrations dropping rapidly after 5-10 m (Ghosal,
344 Eichmiller, Witthuhn, & Sorensen, 2018). A littoral zone of 20 m reflects these processes (10-15
345 m littoral zone + 5-10 m for diffusion). Given these assumptions, the area of the pelagic zone
346 expressed as a fraction of the total area of a lake increases with lake size. The relative
347 contribution of the littoral and pelagic zones to the overall mean concentration of eDNA per lake
348 should therefore be increasingly weighted towards the pelagic eDNA concentration as lake
349 surface area increases.

350 Mean lake eDNA particle concentration (copies/L) was modelled separately as a function
351 of the three metrics of brook trout density calculated above: individual density (individuals/ha);

352 biomass density (kg/ha); and allometrically scaled mass (ASM) ($\sum(\text{individual mass}^{0.73})/\text{ha}$).

353 eDNA particle concentration was included as a dependent variable in a linear regression and a

354 separate model for each abundance metric was fitted to the observed data. Wald F -tests were

355 used to evaluate the significance of fixed-effect terms, with model log-likelihood values were

356 values used to compare model fit using the AIC criterion (Akaike, 1974) as in (Lacoursière-

357 Roussel, Côté, Leclerc, Bernatchez, & Cadotte, 2016), assuming that models with $\Delta\text{AIC} > 2$

358 exhibit significantly reduced explanatory power (Burnham & Anderson, 2002). All analyses

359 were conducted in R (v.3.3.3) (R Development Core Team, 2017). To assess the performance of

360 CPUE as a ‘proxy’ metric of abundance, we also examined the relationship between density and

361 CPUE, as well as eDNA particle concentration and CPUE, using linear regression. To assess the

362 sensitivity of the final results to the relative size of the area of the littoral zone, we ran an

363 additional set of models in which we halved the estimated littoral area of each lake.

364

365

366 *Estimating density and biomass from predicted allometrically scaled mass: a case study for*

367 *population management*

368 Predicting abundance in unknown systems from known eDNA particle concentrations

369 would require an inversion of the modelling relationship described above: abundance would be

370 modelled as a function of eDNA particle concentration. Predicted estimates of ASM obtained

371 from eDNA samples for systems lacking abundance data cannot be directly converted to

372 traditional metrics of abundance (e.g. individual density or biomass density) because multiple

373 density/biomass configurations (e.g. many small fish or a small number of large fish) can

374 produce equivalent ASM values. However, with additional individual mass distribution data

375 from standardized size structure data any predicted ASM point-estimates can be converted to
376 traditional metrics. Size structure data could be exponentiated to the power of b (the allometric
377 scaling coefficient) and the resulting scaled mass values nonparametrically bootstrapped until the
378 cumulative sum of the bootstrapped values surpass the predicted ASM. Individual density could
379 then be estimated by totalling the number of bootstrap “samples” required to surpass the
380 predicted ASM; biomass density could then be estimated by multiplying the predicted density
381 value by the untransformed mean of the size distribution.

382 As a case study, this technique was applied to data collected from Hidden Lake (Banff,
383 Alberta, Canada). The brook trout population of Hidden Lake was targeted as part of rotenone-
384 based removal program by Parks Canada. eDNA samples from Hidden Lake were collected in
385 July 2018 and extracted/analyzed using the same methodology as described above. The
386 estimated “ASM/unit area” of the lake (including 95% prediction intervals) was calculated from
387 the linear relationship obtained from our nine study lakes. Unfortunately, standardized size
388 structure data were unavailable; rotenone removal efforts began in August 2018 and no brook
389 trout remain in the system. However, prior to the use of rotenone mechanical gill netting efforts
390 were employed during brook trout removal efforts between 2011 and August 2017 (Stitt, *pers.*
391 *comm.*). By 2016 netting efforts had removed most large fish from the population, and fish older
392 than age 0+ were between 90-140mm in length (Sullivan, 2017), although it should be noted that
393 standardized size distribution data was unavailable. Of our nine study lakes, fish from Olive lake
394 exhibited the smallest body mass, so size structure data from this lake was utilized as a “proxy”
395 to calculate an approximate pre-rotenone individual density and biomass density of brook trout
396 inhabiting Hidden Lake in 2018. Bootstrap simulations to quantify individual density and

397 biomass density utilizing the Olive size distribution and predicted ASM of Hidden Lake were run
398 for 1000 iterations. All analyses were performed in R (R Development Core Team, 2017).

399 *Predicting allometric scaling coefficient for eDNA production in brook trout*

400 Allometric scaling coefficients are likely to fall between a value of 0 and 1; notably, (\sum
401 individual mass^{0.0})/ha is equivalent to individual density (fish/ha) and (\sum individual mass^{1.0})/ha is
402 equivalent to biomass density (kg/ha). Although we employed an allometric scaling coefficient
403 of 0.73 in our model (based on metabolic data from brook trout), the “true” allometric scaling
404 coefficient for eDNA production in our system was unknown. We used our data to predict the
405 optimal value for the scaling coefficient given the observed eDNA particle concentration and
406 biomass distribution data observed across our study lakes. To achieve this, we iteratively
407 generated ASM values from our data using scaling coefficients ranging from 0 to 1 (increasing
408 by intervals of 0.01) and sequentially modelled eDNA particle concentration data as a function
409 of each ASM value. AIC values for each model were then used to evaluate model fit. If eDNA
410 production scales allometrically according to a power function, we predict that the AIC values
411 across models with scaling coefficients between 0 and 1 will exhibit an approximately upward
412 parabolic distribution with a minimum best-fit value that corresponds to an “optimal” allometric
413 scaling coefficient. According to the general rule described in (Burnham & Anderson, 2002),
414 models within $2 \Delta\text{AIC}$ also exhibit substantial support; we predict that the ‘true’ allometric
415 scaling coefficient for brook trout eDNA production in nature will fall between the range of
416 scaling coefficients that produce models within 2 AIC of the ‘best-fit’ scaling coefficient,
417 although future experiments will be necessary to validate our predictions. To assess the
418 sensitivity of this analysis to the estimated size of the littoral zone, this analysis was repeated for

419 models in which we halved the estimated littoral area of each lake. All analyses were performed
420 in R (R Development Core Team, 2017).

421

422 **Results**

423 *Population size estimates and density*

424 Population size estimates ranged from 145 to 3266 individuals, individual density ranged
425 from 63 to 1131 fish/ha, biomass density ranged from 12.6 to 52.5 kg/ha, and ASM ranged from
426 3707 to 18600 ASM/ha (Table 2, see Figure 2 for population size structure). Estimates of catch-
427 per-unit-effort (CPUE) did not exhibit a significant correlation with individual density ($F_{1,7} =$
428 0.53, $p = 0.491$, Figure S3).

429

430 *eDNA concentrations and correlations with density metrics among lakes*

431 Brook trout eDNA was successfully amplified from all samples in all lakes. No
432 amplification was observed in any negative controls or extraction blanks. The R^2 values for
433 standard curves ranged from 0.984 to 0.995, with an estimated efficiency ranging from 84.2 to
434 95.1%. Littoral and pelagic eDNA concentrations varied substantially by lake (Table 3). After
435 weighing for lake zone area, mean eDNA concentrations ranged from 592 copies/L in Cobb to
436 7805 copies/L in Olive.

437 Linear models for each density metric demonstrated positive and significant correlations
438 with eDNA particle concentration (Table 4, Figure 3). Individual density, biomass density, and
439 ASM accounted for 59%, 63%, and 78% of the variation in observed eDNA particle
440 concentration (adjusted R^2), respectively. AIC values indicated that individual density and
441 biomass density metrics provided roughly equivalent model fit; however, the ASM metric
442 provided substantially improved model fit relative to individual density and biomass density
443 (ΔAIC of 5.7 and 4.6, respectively). Trends did not substantially change when littoral area per

444 lake was halved (Table S1). CPUE did not exhibit a significant correlation with eDNA particle
445 concentration (Table 4, Figure S4).

446 *Estimating density and biomass from predicted allometrically scaled mass: a case study for*
447 *population management*

448 The eDNA concentration of Hidden Lake littoral and pelagic eDNA samples averaged
449 2653 and 342 copies/L, respectively, with a weighted mean average eDNA particle concentration
450 of 847 copies/L (Table 3). Based on a linear model using data from the nine study lakes, Hidden
451 Lake had an estimated ASM/ha of 4279.6 (Figure 4). After 1000 iterations, the mean number of
452 individual mass values sampled from the Olive size distribution was 278.4, which represents the
453 individual density (ind/ha) point-estimate for Hidden Lake; this corresponds to a total population
454 size estimate of 3286 individuals. Predicted total biomass was 143.0 kg, with a biomass density
455 of 12.1 kg/ha. Notably, point estimates of biomass density rank Hidden Lake lower than all nine
456 study lakes, likely as a result of previous fish removal efforts between 2011 and 2017 in Hidden
457 Lake. Upper 95% prediction intervals for population size, total biomass, density, and biomass
458 density were 7629 individuals, 332.0 kg, 646.5 fish/ha, and 28.1 kg/ha, respectively. Due to the
459 overall low concentration of eDNA present in the lake, lower 95% prediction intervals
460 overlapped with zero for all four parameters.

461

462 *Predicting the allometric scaling coefficient for eDNA production in brook trout*

463 Based on model AIC values, a scaling coefficient of 0.72 best explained patterns of
464 eDNA particle concentration across the nine study lakes; models with scaling coefficients
465 between 0.47 and 0.89 generated Δ AIC values < 2 (Figure 5). The ‘optimal’ scaling coefficient
466 appeared to be slightly sensitive to the fraction of the area of each lake assigned to the littoral

467 zone: when littoral zone area within each lake was halved, a scaling coefficient of 0.63 best
468 explained patterns of eDNA particle concentration (Figure S5). However, credible intervals
469 between the two models substantially overlapped; models with scaling coefficients between 0.28
470 and 0.84 generated Δ AIC values < 2 when lake littoral area was halved.

471 **Discussion**

472 Our study provides strong support for the hypothesis that eDNA production scales non-
473 linearly with mass according to a power function. Incorporating allometric scaling coefficients to
474 account for the distribution of biomass across individuals substantially improved predictive
475 models, indicating that the distribution of biomass across individuals within a population may
476 have an important effect when scaling individual eDNA production rates to the population-level.
477 Incorporating metabolic scaling coefficients for mass into models of eDNA particle
478 concentration and organismal abundance may therefore be particularly important in species that
479 exhibit substantial inter-population variation in size distributions. Our findings contribute to a
480 broader understanding of the ecology of eDNA production and have important implications for
481 many eDNA applications. While the focus of this study was on the relationship between eDNA
482 particle concentration and abundance using qPCR techniques, allometry in species with variable
483 size structure could, for example, partially account for the variation observed in read numbers
484 across environments in metabarcoding studies.

485 This study also reaffirms previous findings that metrics of population abundance
486 correlate with species-specific eDNA particle concentration in natural environments (Klobucar,
487 Rodgers, & Budy, 2017; Nevers et al., 2018; Pilliod et al., 2013; Schmelzle & Kinziger, 2016;
488 Thomsen et al., 2012). Previous research has demonstrated a moderate correlation between
489 density and/or biomass and eDNA particle concentration in lotic systems for brook trout
490 (Baldigo et al., 2017; Wilcox et al., 2016). We found similar relationships within lentic systems,
491 but also demonstrate that they can be considerably improved by integrating allometric scaling
492 coefficients into estimates of organismal abundance. Notably, in eight of the nine study lakes the
493 mean concentration of eDNA observed in lentic zone samples was higher compared to pelagic

494 zone samples. eDNA particle concentrations generally show a strong correlation with the spatial
495 distribution of fish within a lake (Ghosal et al., 2018; Hanfling et al., 2016), and our findings
496 reflect well documented ecological preferences of brook trout, which tend to favor littoral zones
497 (Magnan & Fitzgerald, 1982; Tiberti et al., 2017). The only lake where this trend was not
498 observed was Olive, where pelagic and littoral zone eDNA concentrations were similar; this lake
499 was also the smallest (and shallowest, at 3.5 m maximum depth) lake with the highest individual
500 density of brook trout, indicating that fish are likely relatively evenly distributed across the lake.

501 The correlation coefficients we observed between eDNA concentration and all three
502 metrics of abundance were greater than most previous studies conducted in nature (Yates et al.,
503 2019). The relatively strong correlations we observed between our abundance metrics and eDNA
504 concentration could also be due to the methodology with which we assessed population size. Our
505 estimates of population size were obtained using mark-recapture studies and unbiased measures
506 of size-structuring, which provided precise and standardized estimates of individual density,
507 biomass density, and ASM. However, such estimates are rare in published eDNA/abundance
508 studies; conducting mark-recapture studies to estimate population size is time consuming and
509 requires a substantial commitment of labour and resources. To date only a handful of eDNA
510 studies in nature have specifically enumerated population size (Klobucar et al., 2017; Levi et al.,
511 2019; Tillotson et al., 2018) rather than proxies for abundance, such as CPUE (Yates et al.,
512 2019). CPUE may be appropriate if it exhibits a strong correlation with abundance, but in some
513 systems CPUE can perform poorly as a proxy for abundance (Hubert et al., 2012; Rose & Kulka,
514 1999). In our study systems CPUE did not exhibit a significant correlation with individual
515 density and, as a result, eDNA concentration. Some of the substantial unexplained variation in
516 nature between eDNA concentration and abundance observed in other systems could result from

517 reliance on CPUE as a ‘proxy’ for abundance, although we acknowledge that for many species it
518 may often be impractical or impossible to directly estimate population size.

519 It is important to note, however, that our abundance estimates may miss a small fraction
520 of the adult population and do not account for juvenile (age 0+) abundance because fish were not
521 included in the mark-recapture study until they were at least 80mm (to avoid excessive tagging
522 mortality). Population size estimates therefore represent underestimates of true population census
523 size. Discrepancies in juvenile abundance/density across lakes could account for some of the
524 remaining unexplained variation present in our model, particularly since smaller fish would be
525 expected to exhibit higher mass-specific eDNA production rates. Similarly, temperature is
526 known to have a strong effect on metabolic rates (Brown et al., 2004) and eDNA production (Jo
527 et al., 2019). Notably, bioenergetics models for a closely related species (bull trout, *Salvelinus*
528 *Confluentus*) demonstrate that both the value of the normalization constant (I_0) as well as the
529 allometric scaling coefficient (b) can change with temperature (Mesa, Weiland, Christiansen,
530 Sauter, & Beauchamp, 2013). Temple lake exhibited a substantially lower concentration of
531 eDNA than expected from its ASM estimate; at 3.5 °C, Temple lake was also substantially colder
532 than the other eight study lakes during eDNA sampling (8.9-17.2 °C). Although we lacked the
533 replication to do so, integrating other important environmental variables (e.g. temperature, pH,
534 etc.) into models of eDNA particle concentration across environments could further improve
535 predictive models.

536 Despite these caveats, we demonstrate that it is possible to predict estimates of population
537 abundance with eDNA samples and size structure data in similar ecosystems that lack abundance
538 data. We predicted traditional metrics of abundance for Hidden Lake based on a hypothetical
539 assumption that size structure in Hidden Lake closely resembled size structure in another study

540 lake (Olive lake). Although predicted density metrics for Hidden Lake based on an ‘proxy’ Olive
541 Lake size structure distribution were low and exhibited wide upper 95% prediction intervals,
542 they still provided enough information to facilitate relative comparisons to the nine study lakes;
543 we can predict with some certainty, for example, that if size structure in Hidden Lake was similar
544 to that found in Olive, it would have had a lower biomass density relative to two of the nine
545 study lakes (Dog and Olive). Furthermore, 95% prediction intervals represent a relatively
546 stringent criteria of certainty; 75% or 80% prediction intervals might still represent useful
547 information to help guide managerial or research decisions, although that would be up to
548 practitioner discretion.

549 Most significantly, our results highlight the need for further empirical studies exploring
550 and validating allometric scaling via power functions as a framework for modelling eDNA
551 particle production rates. While we demonstrate that incorporating allometric scaling coefficients
552 substantially improves models predicting abundance and eDNA concentration at the population
553 level, we have not directly quantified how eDNA production scales allometrically in brook trout
554 at the level of individual organisms. Nevertheless, recent experiments demonstrate that mass-
555 specific eDNA production rates tend to decline as individual mass increases (Maruyama et al.,
556 2014; Mizumoto et al., 2018; Takeuchi et al., 2019). We found that a scaling coefficient of 0.72
557 best described patterns of eDNA concentration for our study species across our nine study lakes;
558 this value is closely aligned with the metabolic scaling coefficient for brook trout from (Hartman
559 & Cox, 2008). Scaling coefficients between 0.51 and 0.87 produced models with ΔAIC values <
560 2; we therefore predict that the ‘true’ allometric scaling coefficient for eDNA production in
561 brook trout will likely fall within this interval, although we do note that this point estimate was
562 slightly sensitive to the area of each lake assigned to the littoral zone. If the area assigned to the

563 littoral zone of each lake is halved, the value of the ‘optimal’ scaling coefficient is reduced to
564 0.63 (models with ΔAIC values < 2 range from 0.28-0.84) which is closer to theoretically
565 expected values for excretory/consumptive/shedding allometric scaling coefficients (although
566 note that credible intervals for both values substantially overlap). In future studies, detailed
567 bathymetry data would be useful to disentangle these issues. Nevertheless, credible intervals for
568 both models overlapped substantially, indicating that allometric scaling substantially improved
569 explanatory models. To validate our findings, test our subsequent predictions, and disentangle
570 what processes are likely to most strongly affect the value of eDNA scaling coefficients (e.g.
571 metabolism vs excretion/shedding), further experiments are necessary to quantify allometric
572 scaling of eDNA production at the individual level in brook trout.

573 As a well-supported general theory in ecology, experimental designs developed to test
574 MTE hypotheses (e.g. (Allegier et al., 2015; Hartman & Cox, 2008)) can inform future
575 experiments examining the effect of allometry on eDNA production rates. Notably, previous
576 experiments investigating allometric scaling in excretion or metabolic rates quantified rates at the
577 level of *individual* organisms (Allegier et al., 2015; Hartman & Cox, 2008; Vanni & McIntyre,
578 2016). Previous laboratory experiments quantifying the effect of biomass on eDNA
579 production/shedding rates typically pooled organisms to create different biomass treatments
580 (Doi, Uchii, Takahara, & Matsuhashi, 2015; Klymus et al., 2015; Lacoursière-Roussel, Rosabal,
581 & Bernatchez, 2016; Mizumoto et al., 2018; Takahara et al., 2012). At best, such experiments
582 pool organisms from similar size-classes, in which case eDNA production/abundance
583 relationships across ‘treatments’ only reflect changes in abundance within a specific age- or size-
584 class. Such experimental designs are likely to produce a strong relationship between eDNA
585 concentration and biomass, as has been found in a meta-analytic review (Yates et al., 2019).

586 While such studies were necessary to empirically quantify a preliminary correlation between
587 eDNA particle concentration and metrics of abundance, they might obscure critical differences in
588 mass-specific eDNA production rates across size classes that could have important consequences
589 for population-level rates. Natural populations often exhibit substantial variation in the
590 distribution of body size across individuals; the failure to account for allometric scaling in the
591 relationship between biomass and eDNA production might partially explain the failure to
592 translate the strong relationships observed in laboratory experiments to nature (Sebens, 1987).
593 Notably, our eDNA/abundance models utilizing ASM exhibited correlation coefficients
594 comparable to those typically observed in laboratory environments (Yates et al., 2019).

595 It may be possible to investigate allometry in eDNA production by pooling individuals
596 that are the same size within replicates. However, we would advise against this because
597 behavioural interactions between fish at high density in confined spaces may impact eDNA
598 production; some studies have demonstrated that eDNA production per fish increases at high
599 densities (Id et al., 2019). Brook trout, for example, are known to exhibit aggressive behaviour
600 towards conspecifics (McNicol, Scherer, & Murkin, 1985), which could increase eDNA particle
601 concentration at high densities due to increased activity and/or injuries inflicted upon each other.
602 If size classes exhibit different behaviour at high densities, this could further affect estimates of
603 allometric scaling. Future studies examining allometric scaling in eDNA production should
604 therefore incorporate individuals from a gradient of age/size classes and quantify organismal
605 eDNA production at the *individual*-level, as in (Takeuchi et al., 2019). Notably, the two studies
606 to examine eDNA production rates at an individual level across age/size classes found that
607 larger, older individuals exhibited lower mass-specific eDNA production rates (Maruyama et al.,
608 2014; Takeuchi et al., 2019). There is also a critical need to conduct such experiments *in situ* at

609 field study sites on wild organisms, as in (Pilliod, Goldberg, Arkle, & Waits, 2014). Laboratory
610 experiments, while important from a validation perspective, may not reflect natural excretion
611 processes because study organisms are housed in artificial conditions, fed artificial diets, and are
612 often subject to fasting regimes (Vanni & McIntyre, 2016). Furthermore, size-scaling
613 coefficients for metabolic processes such as nutrient excretion exhibit substantial interspecific
614 variation and can even include values greater than 1 (Allegier et al., 2015; Vanni & McIntyre,
615 2016). Allometric scaling in eDNA production may therefore exhibit similar variability across
616 species and should be investigated on a case-by-case basis.

617 Finally, our experiment investigated intraspecific allometry in eDNA production.
618 Although there is substantial taxonomic variation, multiple studies have demonstrated that it is
619 possible to extend allometric power-scaling across taxonomic groups for metabolic and/or
620 excretory processes (Allegier et al., 2015; Vanni & McIntyre, 2016). Metabarcoding studies
621 exhibit a weak but positive relationship between read count and organism biomass (Lamb et al.,
622 2019). If allometric scaling in eDNA production exhibits a similar relationship across taxonomic
623 groups, the relationship between read count and organism abundance could be strengthened by
624 integrating allometry.

625

626 *Conclusions*

627 Our results provide evidence supporting the hypothesis that eDNA production scales
628 allometrically with organism mass. We have demonstrated that the incorporation of additional
629 (but straightforward to collect) size structure data to integrate key allometric scaling predictions
630 resulted in substantial improvement in models of eDNA concentration across environments. The
631 bulk of experiments examining eDNA in nature have typically focused on presence/absence

632 applications for species detection utilizing metabarcoding technologies (Goldberg et al., 2015),
633 in which the detection of rare DNA fragments is often prioritized. As a result, substantial
634 consideration in the literature has been given to factors that affect eDNA degradation and
635 dispersion (e.g. (Barnes et al., 2014; Goldberg, Strickler, & Fremier, 2018; Harrison, Sunday, &
636 Rogers, 2019; Strickler, Fremier, & Goldberg, 2015)), while relatively less attention has focused
637 on the ecology of eDNA production. Our study demonstrates that the ecology of eDNA
638 production may represent an understudied yet critically important subject, particularly when
639 attempting to infer abundance from eDNA concentrations in nature. Future studies on
640 eDNA/abundance relationships in nature should consider incorporating allometry, particularly
641 when study species exhibit substantial inter-population variation in size distributions. However,
642 there is also a need to validate this hypothesis in controlled experimental contexts at the level of
643 individual organisms. As a well-developed ecological theory validated by numerous empirical
644 studies (Vanni & McIntyre, 2016), the literature on the MTE represents a robust methodological
645 foundation that future studies can utilize to explore relationships between a variety of
646 environmental and ecological factors that might influence organismal production of eDNA. Such
647 studies could further improve predictive models estimating abundance from eDNA particle
648 concentration to the extent that, in some circumstances, species-specific eDNA particle
649 concentration might be a reliable ecological indicator of abundance.

650 Predictive models would need to be calibrated on a system- and species-specific basis.
651 The extent to which models for a particular species can be extended to different ecosystems or
652 geographical regions also remains unknown. Future studies employing the methodology
653 developed herein will likely need to construct models from population size/abundance estimates
654 combined with standardized size distribution data on an individual species/system basis. These

655 studies will also need to collect size distribution data, in addition to eDNA samples, to predict
656 the density or biomass of organisms in similar ecosystems that lack abundance data. Direct
657 estimates of allometric scaling coefficients for study species would also likely improve
658 predictive models, although metabolic or excretory allometric scaling coefficients estimated in
659 other empirical studies on the same (or closely related) species may represent useful starting
660 points. In the absence of any other empirical data, the general scaling coefficient predicted by the
661 MTE (0.75) may also suffice.

662 Depending on the species studied, obtaining robust population size estimates and
663 individual size distribution data to calibrate initial models can often be difficult, labour intensive,
664 and come with a substantial monetary cost. However, the benefits might be substantial – the idea
665 that future researchers or managers might be able to obtain reasonable estimates of abundance
666 from eight water samples and a small number of gill net sets is, from an ecologist’s perspective,
667 exciting.

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908

909 **Data Accessibility Statement:**

910 eDNA particle concentration data for each lake will be deposited in the Dryad Digital Repository
911 upon acceptance.

912 **Author contributions**

913 MCY collected eDNA samples and analyzed eDNA data. DG collected and analyzed mark-
914 recapture and size structure data. Statistical analyses were conducted by MCY. MCY wrote the
915 first draft of the manuscript, and all authors contributed substantially to subsequent drafts.

916 **Tables**

917 Table 1: Size structure gill net effort and fyking (mark-recapture) effort. SS refers to size
918 structure assessment, percent SS refers to the proportion of population harvested during size
919 structure assessment.

920

Site	SS Samples	Percent SS	SS CPUE	Mark/Recapture days	Total Marks Applied
Cobb	104	0.72	7	20	24
Mud	84	0.10	42	20	364
Olive	160	0.09	53	21	307
Ross	128	0.09	64	19	571
Temple	165	0.10	41	25	409
Dog	187	0.06	94	30	617
Helen	41	0.07	41	12	172
Margaret	171	0.08	43	23	414
McNair	27	0.13	27	14	118

921

922

923 Table 2: Density metric estimates for each population. N_c = population size, ASM =
 924 allometrically scaled mass. 95% confidence intervals for 'N' are given in brackets.

Site	N_c	Ha	Mean Individual Mass (g)			ASM/ha	eDNA (copies/L)
			Fish/ha	Kg/ha			
Cobb	145 (94, 237)	2.3	404.8	63 (41, 103)	25.7 (16.5, 41.7)	5663	592.2
Dog	3266 (2715, 4097)	11.5	184.8	284 (236, 356)	52.5 (43.6, 65.8)	13962	5131.1
Helen	557 (420, 755)	2.5	83.9	225 (168, 302)	18.8 (14.1, 25.3)	6187	2445.9
Margaret	2017 (1638, 2623)	18.0	112.3	112 (91, 146)	12.6 (10.2, 16.4)	3707	1240.4
McNair	201 (158, 276)	1.7	137.3	121 (93, 162)	16.6 (12.8, 22.3)	4736	3050.5
Mud	860 (733, 1040)	7.2	141.9	119 (102, 144)	17.0 (14.4, 20.5)	4587	1138.7
Olive	1877 (1459, 2628)	1.7	43.1	1131 (858, 1546)	48.8 (37.0, 66.6)	18601	7805.1
Ross	1392 (1211, 1635)	6.6	82.5	211 (183, 248)	17.4 (15.1, 20.4)	5559	917.4
Temple	1655 (1369, 2090)	3.3	51.1	509 (415, 633)	26.1 (21.2, 32.4)	9587	2076.5

925

926

927

928 Table 3: Lake zone area and corresponding eDNA concentrations (minimum and maximum

Site	Pelagic area (ha)	Littoral area (ha)	Mean Pelagic eDNA (copies/L)	Mean Littoral eDNA (Copies/L)	Weighted Mean eDNA (Copies/L)
Cobb	1.0	1.3	253.8 (39.6 - 557.9)	854.6 (35.9 - 2650.4)	592.2
Dog	8.5	3.1	3447.1 (683.8 - 9148.1)	9796.7 (3705.6 - 16839.3)	5131.1
Helen	1.2	1.3	1342.4 (854.3 - 1586.9)	3514.4 (2083.2 - 5060.5)	2445.9
Margaret	14.4	3.6	791.9 (706.8 - 968.1)	3034.1 (814.3 - 5689.7)	1240.4
McNair	0.7	1.0	2395.4 (2214.9 - 2495.9)	3505.0 (3181.1 - 4886.4)	3050.5
Mud	4.7	2.6	399.3 (261.7 - 580.7)	1550.6 (628.3 - 3833.3)	797.5
Olive	0.5	1.2	8084.6 (5115.9 - 11758.9)	7684.7 (1839.6 - 11829.1)	7805.1
Ross	4.6	2.0	790.5 (439.7 - 1101.9)	1209.8 (3763 - 2576.0)	917.4
Temple	1.6	1.7	1180.1 (854.3 - 1685.7)	1850.3 (1133.6 - 3887.0)	1530.6
Hidden	11.8	2.6	342.0 (149.3 - 472.4)	2652.9 (1277.2 - 5758.1)	847.2

929 observed eDNA concentrations per lake zone included in parentheses).

930

931

932 Table 4: Model results evaluating the relationship between eDNA particle concentration and
933 density (fish/ha), biomass (kg/ha), allometrically scaled mass (ASM/ha), and CPUE.

934

Model	F-value	P-value	Adj. R ²	Log Likelihood	AIC	ΔAIC
Density	12.37 _(1,7)	0.010	0.59	-77.78	161.6	5.7
Biomass	14.76 _(1,7)	0.006	0.63	-77.26	160.5	4.6
ASM	29.4 _(1,7)	0.001	0.78	-74.95	155.9	-
CPUE	1.92 _(1,7)	0.208	0.10	-81.27	168.5	12.6

935

936

937 **Figure Captions**

938

939 Figure 1: Conceptual example of allometric scaling in eDNA production rate with individual
940 mass. Figure a) demonstrates absolute eDNA production rate as mass increases, figure b)
941 demonstrates mass-specific eDNA production rate (i.e. eDNA production rate per (g) of mass).
942 Solid lines reflect an allometric process that scales linearly with body mass ($b = 1$), dashed lines
943 correspond to allometric scaling with a value of $b < 1$.

944

945 Figure 2: Lake size structure distributions (g) obtained from standardized gill net sets for the nine
946 study lakes.

947

948 Figure 3: Correlation between weighted mean lake brook trout eDNA particle concentration and
949 three metrics of abundance in the nine study lakes: (a) individual density (individuals/ha, $R^2 =$
950 0.59), (b) biomass density (kg/ha, $R^2 = 0.63$), and (c) allometrically scaled mass (ASM/ha, $R^2 =$
951 0.78) ($n = 9$). O = Olive, D = Dog, C = Cobb, T = Temple, H = Helen, MD = Mud, MG =
952 Margaret, MN = McNair, R = Ross.

953

954 Figure 4: Predicting allometrically scaled mass (ASM/ha) for Hidden Lake based on eDNA
955 particle concentration. Black dots represent values for the nine study lakes, gray circle represents
956 the ASM/ha point estimate for Hidden Lake. Error bars represent 95% prediction intervals ($n =$
957 9).

958

959 Figure 5: AIC values for models correlating brook trout eDNA and allometrically scaled mass
960 (ASM), utilizing allometric scaling coefficients ranging from 0.00 (corresponding to individual
961 density) to 1.0 (corresponding to biomass density). Horizontal black bars and dotted lines denote
962 range of models with $\Delta\text{AIC} < 2$ relative to the ‘optimal’ scaling coefficient (0.72).

963

964 Figure S1: Map of the nine study lakes located in Alberta and British Columbia, Canada.

965

966 Figure S2: Timing of sampling activities in 2018. S.A. refers to size-structure assessment.

967

968 Figure S3: Relationship between catch-per-unit-effort (CPUE) of a large and small gill net and
969 individual density (fish/ha) for the nine study lakes (adjusted $R^2 < 0$) ($n = 9$).

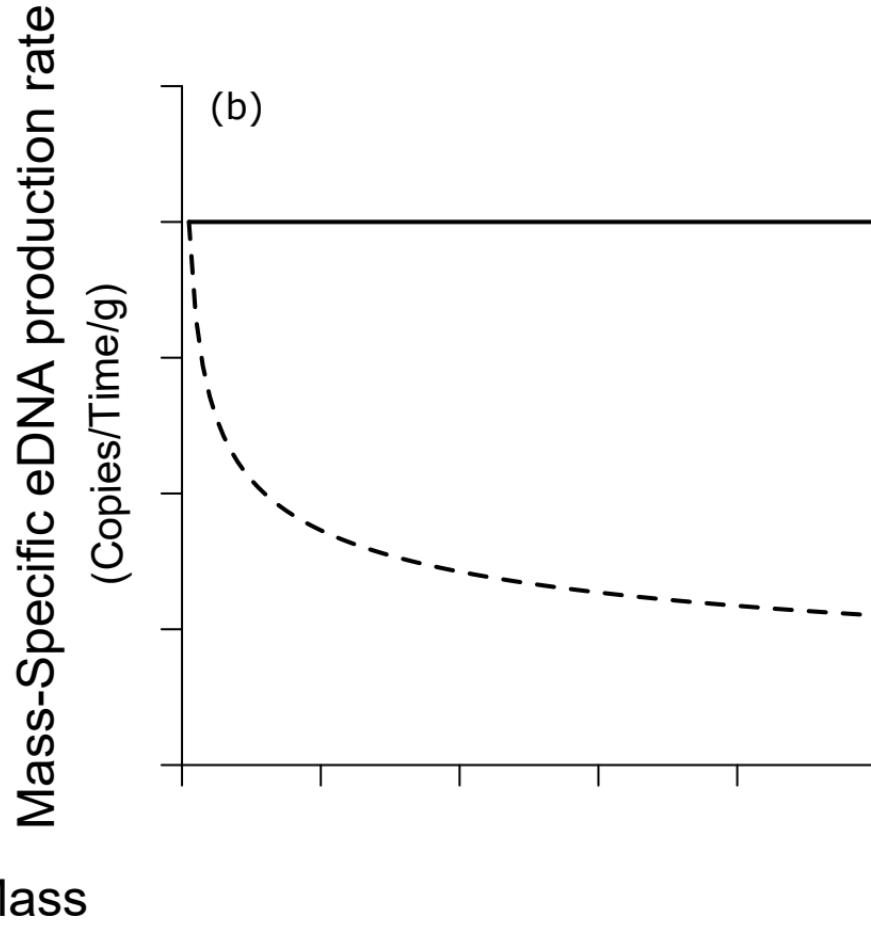
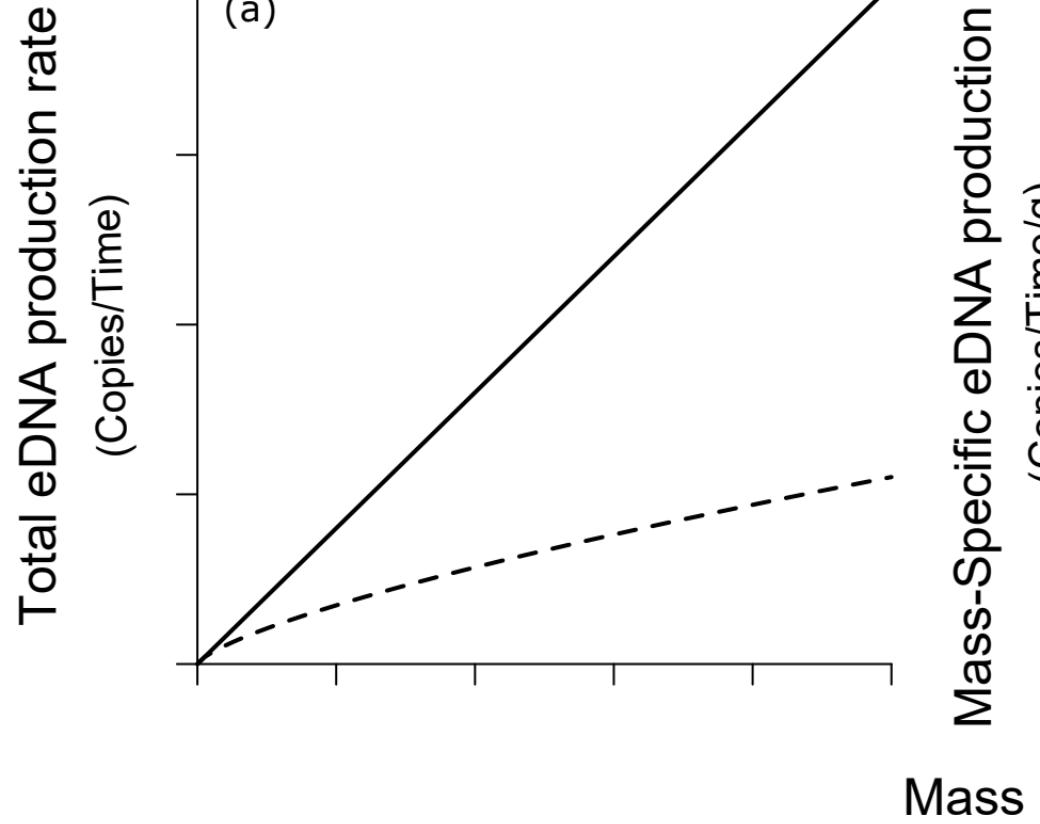
970

971 Figure S4: Relationship between brook trout eDNA particle concentration and catch-per-unit-
972 effort (CPUE) of a large and small gill net for the nine study lakes ($R^2 = 0.10$).

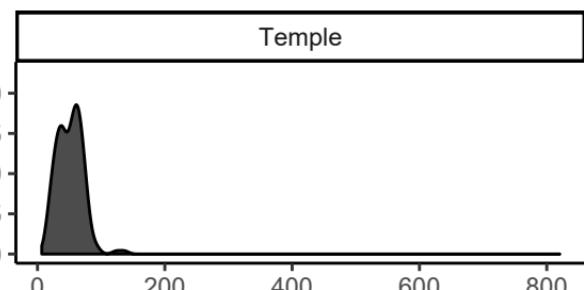
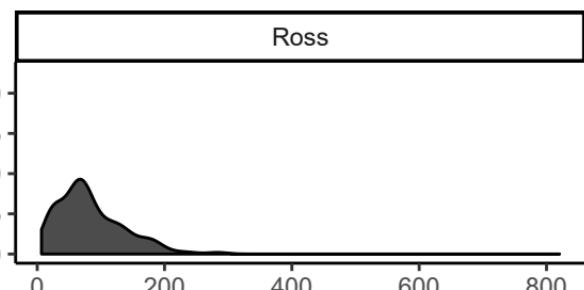
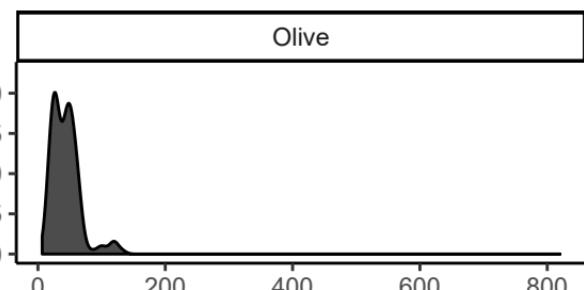
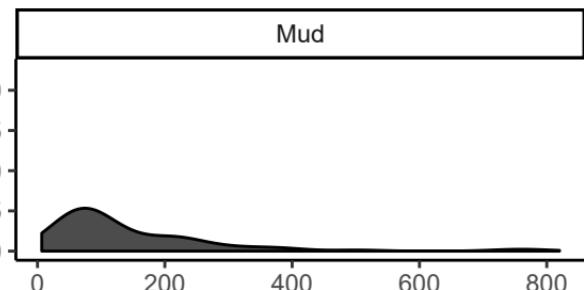
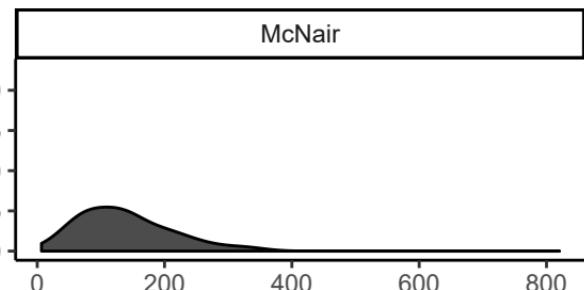
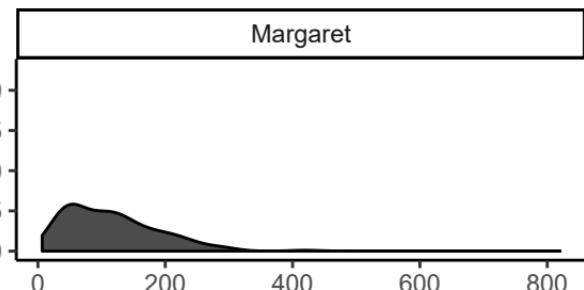
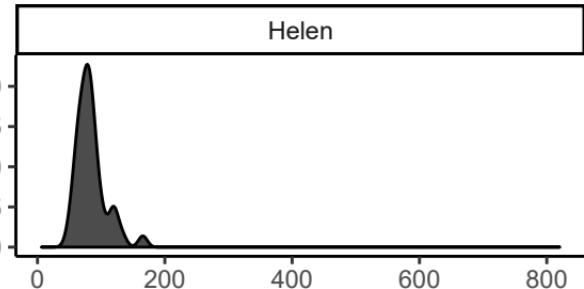
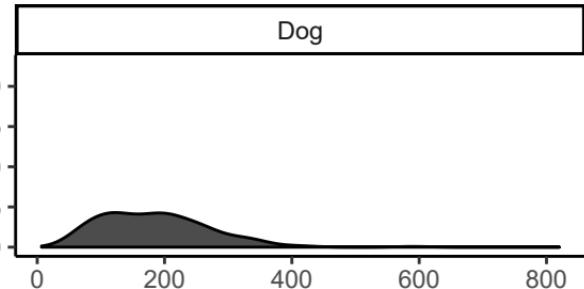
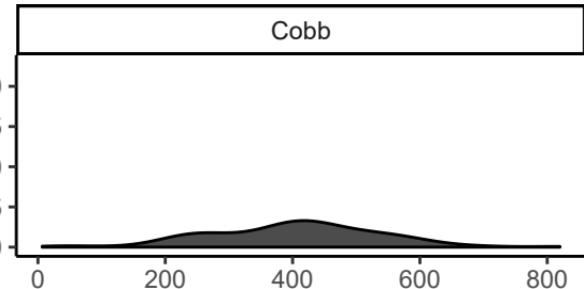
973

974 Figure S5: AIC values for models correlating brook trout eDNA with littoral lake area halved
975 and allometrically scaled mass (ASM), utilizing allometric scaling coefficients ranging from 0.00
976 (corresponding to individual density) to 1.0 (corresponding to biomass density). Horizontal black
977 bars and dotted lines denote range of models with $\Delta\text{AIC} < 2$ relative to the ‘optimal’ scaling
978 coefficient (0.72).

979



Percent catch



Mass (g)

