Spatial Variation of Microtubule Depolymerization in Large Asters Suggests Regulation by MAP Depletion

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Abstract

Microtubule plus end depolymerization rate is a potentially important target of physiological regulation, but it has been challenging to measure, so its role in spatial organization is poorly understood. Here we apply a method for tracking plus ends based on time difference imaging to measure depolymerization rates in large interphase asters growing in *Xenopus* egg extract. We observed strong spatial regulation of depolymerization rates, which were almost two-fold higher in the aster interior compared to the periphery, and much less regulation of polymerization or catastrophe rates. We interpret these data in terms of a limiting component model, where aster growth results in lower levels of soluble tubulin and MAPs in the interior cytosol compared to that at the periphery. The steady-state polymer fraction of tubulin was ~30%, so tubulin is not strongly depleted in the aster interior. We propose that the limiting component for microtubule assembly is a MAP that inhibits depolymerization, and that egg asters are tuned to low microtubule density.

Introduction

Microtubules undergo rapid polymerization dynamics in many cell types, as first revealed by polarization microscopy (Inoué and Sato 1967). Polymerization dynamics occur mostly on plus ends, and are well-approximated by a two-state dynamic model of dynamic instability (Dogterom and Leibler 1993). Plus end behavior is described by four parameters in this model: polymerization, depolymerization, catastrophe and rescue rates. For the robust organization of intracellular structures, these parameters are regulated in both space and time, which also allows for a rapid response to internal and external cues. Most recent studies on the biology and mechanisms of dynamics regulation focused on polymerization and catastrophe rates, in part because multiple factors are known to regulate these rates, and in part because they are the easiest to measure in cells. Tracking of the the plus-tip binding proteins EB1/3 allows measurement of polymerization rate with high reliability, and inference of catastrophe rate from comet lifetime with somewhat lower reliability. In contrast, depolymerization rates are harder to measure. Most studies reporting depolymerization rates focused on pure tubulin systems or on manual measurements of small numbers of microtubules at the periphery of living cells (Desai and Mitchison 1997; Brouhard and Rice 2018). As a result, we know rather little about regulation of depolymerization rates in complex microtubule structures such as the mitotic spindle or microtubule asters. Here, we apply imaging-based methods to systematically measure microtubule depolymerization rates in *Xenopus* egg extract, and report spatial regulation of depolymerization for the first time.

One important emergent property from the four dynamic instability factors, combined with nucleation, is the fraction of polymerized tubulin at steady state, which we will call the "polymer fraction". In a closed system like a cell, an increase in microtubule mass leads to depletion of soluble subunits which limits further assembly giving rise to a negative feedback of microtubule growth. When continuously supplied with GTP, the system comes to a steady state where the polymer fraction is approximately constant over time, and sufficient tubulin remains in solution to power robust polymerization of GTP-capped plus ends. The steady-state polymer fraction in interphase tissue culture cells was found to be 60-80% (Zhai and Borisy 1994; Kim, Peshkin, and Mitchison 2012). What determines this value, and its signficance for regulation, are largely unknown. Negative feedback from microtubule mass on further assembly in a closed system was conceptualized in the "component limitation" model for mitotic spindle size (Mitchison et al. 2015). A feedback of this kind is inevitable, but its precise mechanism is non-obvious. For pure tubulin, polymerization rate is a linear function of soluble dimer concentration (Desai and Mitchison 1997; Brouhard and Rice 2018). Thus, increased microtubule mass in a closed system decreases polymerization rate by subunit consumption. Catastrophe rate should increase in parallel, assuming it negatively correlates with polymerization rate as in most models (Walker et al. 1988; Gardner et al. 2008). Depolymerization is commonly considered to be a zero-order process whose rate is independent of soluble subunit concentration, though this assumption has been questioned (Gardner et al. 2011). In physiological contexts, tubulin need not be the only limiting component in a closed system. Microtubule-associated proteins (MAPs) that promote microtubule polymerization are also depleted when microtubule mass increases, which could limit further polymerization. It is unclear how MAP-limitation would regulate individual dynamic instability parameters.

76   *Xenopus* egg extract provides undiluted, metabolically-active cytoplasm that
77   reconstitutes physiological polymerization dynamics and is useful for investigating
78   regulatory mechanisms (Field and Mitchison 2018). It allows microscopy-based scoring
79   of large numbers of dynamic microtubules in a relatively homogeneous environment
80   which is ideal for quantitative analysis. Here, we focus on interphase asters, which
81   model the egg-spanning asters that position centrosomes, nuclei and cleavage furrows
82   during early divisions (Wühr et al. 2010). These asters grow to hundreds of microns in
83   radius at a rate of ~20 microns/min. EB1 tracking showed that the microtubules within
84   them are relatively short, ~16 microns on average. Their plus end dynamics are in the
85   bounded regime of dynamic instability, so they polymerize transiently, but are biased
86   towards eventual depolymerization with a half-life of ~1 min (Ishihara, Korolev, and
87   Mitchison 2016). The aster as a whole grows because each microtubule nucleates more
88   than one daughter microtubule during its lifetime by a poorly understood branching
89   process. The density of plus ends is approximately homogeneous within interphase
90   asters, and there are two interesting boundaries: the stationary MTOC and the growing
91   aster periphery. The MTOC nucleates continuously, and is thought to provide the
92   information that directs microtubule polarity. The periphery controls the rate of aster
93   expansion and whether expansion is bounded or unbounded. Plus ends at the periphery
94   polymerize into a microtubule-free environment, while those in the aster interior
95   polymerize into an environment that is dense in microtubules, and as we will show
96   below, partially depleted of soluble subunits. Many questions remain about these asters,
97   including the polymer fraction, minus end behavior, and whether dynamics differ
98   between the interior and periphery. These dynamical properties likely have important
99   implications for aster mechanics and function. Here, we unexpectedly observed that
100 plus end depolymerization rate is subject to strong spatial regulation. We interpret this
101 observation in terms of a new model for regulation of tubulin polymer fraction by MAP
102 depletion.

Results

Polymerization rate increases slightly at the aster periphery

105 We first investigated the spatial variation of plus end polymerization and catastrophe
106 rates using standard EB1 comet tracking methods (Fig. 1A, Movie 1). We found that the
107 polymerization rate remained relatively constant at 30.9 μm/min (N=9348 tracks, SD
108 5.52, SEM 0.06) as a function of distance from the center of asters (Fig. 1B). We detected
109 a ~10% increase in polymerization rate at the aster periphery 33.7 $\pm$ 10.9 μm/min
110 (mean, std) compared to the interior 30.0 $\pm$ 9.5 μm/min (mean, std). The plus end
111 density is lower at the periphery compared to the aster center (Fig. 1C), and resulted in
112 a slight anti-correlation between plus end density and polymerization rate (Fig. 1D).
113 This anti-correlation was much smaller than reported in an independent
114 study (Geisterfer et al. 2020).

115 Next, we asked if the plus end catastrophe rate showed spatiotemporal variation using
116 EB1 comet lifetimes as a proxy. The average EB1 comet persisted for 19 seconds which
117 corresponds to a catastrophe rate of 3.1 per minute. This value did not show much
118 variation as a function of location or plus end density (Fig. 1E). These measurements
119 performed with wide-field imaging were consistent with our previous measurements
120 with spinning disc confocal microscopy (Ishihara, Korolev, and Mitchison 2016).

121 Therefore, we expect our measurements to be sensitive to spatial variation in
122 catastrophe rate. In summary, our analysis of EB1 comet imaging demonstrated a
123 modest 10% increase in polymerization rate at the aster periphery, where local plus
124 end density is relatively low, and no measurable differences in catastrophe rate.

125
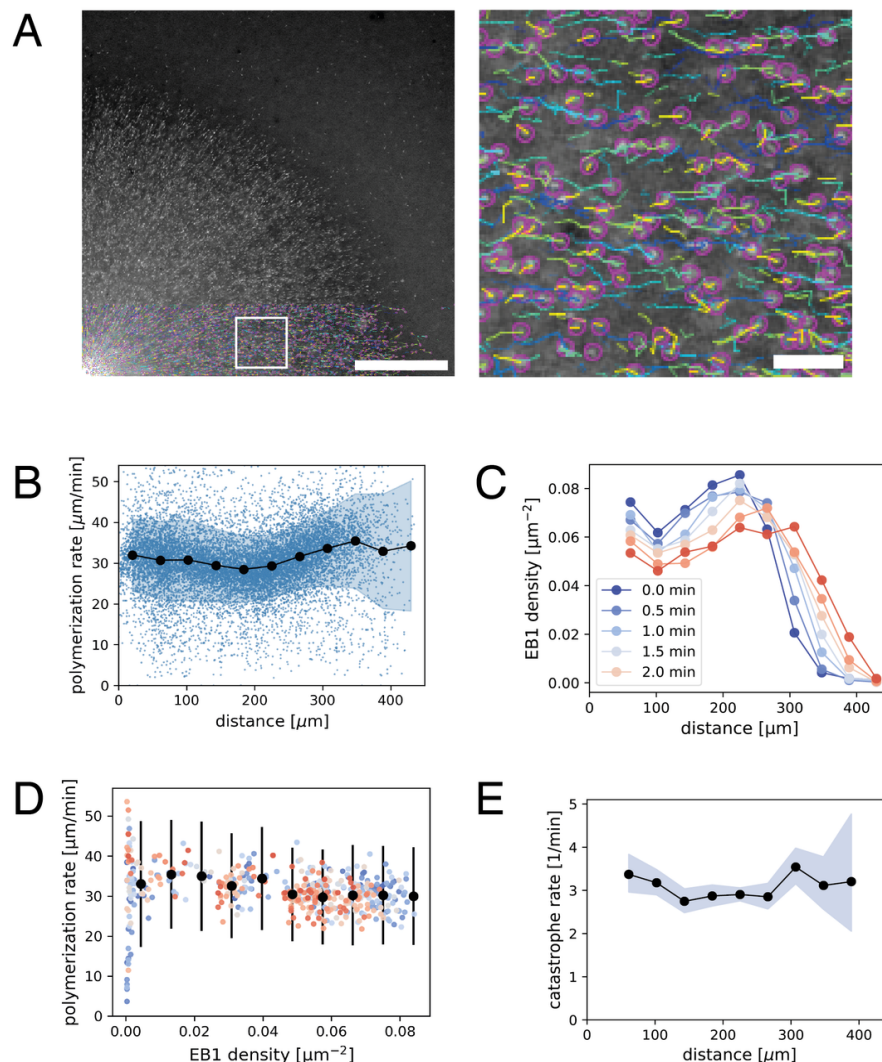
126 **Fig. 1** *EB1 tracking-based measurements of microtubule plus end polymerization rate and*
127 *catastrophe rate during aster growth. (A) Time lapse movies of EB1-GFP comets are*
128 *analyzed by particle tracking. Region in the white box is magnified on the right. Purple*
129 *spots show the location of individual EB1 comets in this frame, while the trailing lines*
130 *show the trajectory of the corresponding plus end for the preceding 10 seconds. The*
131 *velocity of EB1 comets report microtubule polymerization rate. (B) Polymerization rate as*
132 *a function radial distance from the center of the aster. N=9348 EB1 tracks are represented*
133 *as blue dots. Filled black circles and the shaded region indicate the mean and the standard*
134 *deviation of polymerization rate for each spatial bin. The estimated mean difference in the*
135 *interior (distance>300 μm) vs. periphery (50 μm<distance<280 μm) for t =1.5 min was 3.7*
136 *μm/min (95%CI=[2.4, 4.9]). (C) EB1 comet density as a function radial distance. (D)*
137 *Polymerization rate vs. EB1 comet density. Filled black circles and error bars indicate the*
138 *mean and the standard deviation of polymerization rate for each EB1 density bin. The*
139 *different colors correspond to the same time points as in the previous panel. The estimated*
140 *mean difference in the dense (0.066 1/μm^2) vs. sparse (0.022 1/μm^2) was 3.8 μm/min*

141 *(95%CI=[2.6, 5.0]). (E) Catastrophe rate is calculated from the duration of EB1 tracks and*
142 *plotted over radial distance. Filled black circles and the shaded region indicate the mean*
143 *and the corresponding 95% confidence interval for the catastrophe rate for each spatial*
144 *bin. Original data used for this analysis is Movie 1. Scale bars 100 μm and 10 μm.*

Spatial regulation of depolymerization rates

146 To measure microtubule depolymerization rates, we applied tubulin intensity
147 difference analysis. This method relies on collecting high quality tubulin images at
148 frequent intervals using TIRF microscopy, subtracting the intensity of sequential
149 frames to generate time difference images, then applying a tracking algorithm. It allows
150 tracking of polymerizing and depolymerizing ends even when most microtubules are in
151 small bundles as is the case in egg extract asters. Our previous analysis of growing and
152 shrinking ends used manual kymograph analysis of difference images and was
153 restricted to the interior of the interphase asters (Ishihara et al. 2014). Here, we applied
154 a newly developed automated workflow (Caldas et al. 2019; Caldas et al. 2020), and
155 systematically compared spatial differences in polymerization dynamics (Fig. 2A). In
156 brief, this method applies a low pass spatial filter to the difference images, followed by
157 particle based tracking to quantify many microtubule ends. Using this workflow, the
158 polymerization rate was found to have a mean of 32.0 ± 4.5 μm/min (mean, std) in
159 the aster interior, and 32.0 ± 4.0 μm/min (mean, std) in the periphery (Fig. 2B, upper
160 panel). These values of polymerization rates are consistent with EB1 comet tracking
161 (Fig. 1). Polymerization rates exhibited a sharp, unimodal histogram, which overlapped
162 for the interior and periphery with no statistical difference. In contrast, the
163 depolymerization rate showed a striking difference in the aster interior vs. periphery.
164 The depolymerization rate was 36.3 ± 7.9 μm/min (mean, std) in the aster interior,
165 compared to 29.2 ± 8.9 μm/min (mean, std) at the aster periphery. The distribution of
166 the depolymerization rates was spread out and had a positive skew in the aster interior,
167 and a negative skew in the aster periphery, with some hint of a bimodal distribution. In
168 summary, our analysis based on an improved intensity difference analysis showed that
169 polymerization rates are similar in the aster periphery relative to the interior, while
170 depolymerization rates show strong spatial variation and are faster inside asters.

171 Tubulin difference imaging revealed other useful information on polymerization
172 dynamics. Plus end polymerization and depolymerization rates were both variable, but
173 over fairly narrow ranges, so the data supported a two-state model of dynamic
174 instability over alternatives such as a biased random walk (Needleman et al. 2010). Our
175 tracking was not accurate enough to score rate fluctuations within bouts of
176 depolymerization, and we did not try to distinguish stochastic switching between states
177 from more complex dynamics. We observed very few outward-moving
178 depolymerization events, suggesting that minus ends are not depolymerizing, ie there is
179 no significant treadmilling. We also saw very few inward moving polymerization events,
180 suggesting minus ends are static, and perhaps capped.
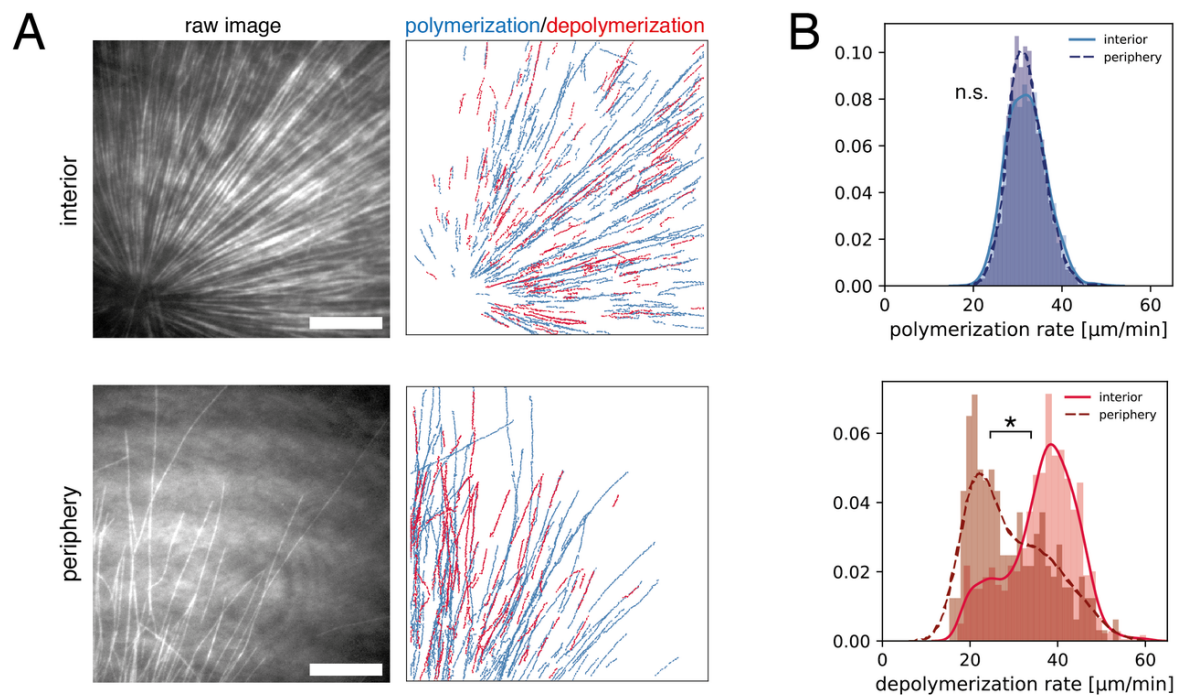
Fig. 2 *Intensity difference-based measurement of polymerization and depolymerization rates in the interior and the periphery of microtubule asters. (A) TIRF microscopy movies of fluorescent tubulin were subjected to intensity difference analysis, which revealed a spatial map of polymerization and depolymerization for the interior (less than 100 μm away from the MTOC) and peripheral (more than 200 μm from the MTOC with few microtubules) region of microtubule asters. These images correspond to Movies 2 and 3. (B) The distributions of polymerization and depolymerization rates measured from N=6 interior movies and N=6 peripheral movies. The polymerization rate (median 32.0 vs. 32.0 μm/min) showed no statistical difference in the interior vs. periphery (p-value = 0.819, t-test). The depolymerization rate (median 37.6 vs. 26.7 μm/min) was higher in the interior (p-value = 4.44e-16, two sample Kolmogorov-Smirnov test) with estimated difference of mean and median depolymerization rates of 7.1 μm/min (95% CI = [5.9, 8.3]) and 11.0 μm/min (95% CI = [8.4, 12.4]). Scale bar, 20 μm.*

Laser ablation induced depolymerization rates

In the conventional model of dynamic instability, growing plus ends lose their structural stability prior to the switch from polymerization to depolymerization. To ask if such physiological catastrophe events are required for the difference in depolymerization rates, we used femtosecond laser ablation to artificially induce depolymerization. Ablation along a line normal to the microtubule axis triggers a spatially defined, synchronous wave of depolymerization (Decker et al. 2018; Decker and Brugués 2015). Using circular patterns , we ablated microtubules at a fixed distance from the center of asters (Fig. 3A, Movie 4). Intensity difference analysis (Fig. 3B) revealed a resulting wave of depolymerization that moved inward at a constant rate (Fig. 3C). This single inward wave is consistent with the fact that (a) the majority of microtubules are oriented with plus ends outward, (b) cut plus ends immediately depolymerize, and (c) newly formed minus ends are stable. By applying this laser ablation assay to multiple asters, we measured an average depolymerization wave velocity of 33.5 ± 9.4 μm/min

210   (mean, std) with a 31.5 µm/min median value, which was comparable to the modal
211   value of the depolymerization rates in the aster interior (Fig. 2). We found no
212   correlation between the rate of depolymerization wave and the distance at which the
213   ablation was induced (15-56 µm). We were not able to reliably cut and measure at the
214   aster periphery due to the low microtubule density. Overall, these observations suggest
215   that depolymerization dynamics are similar for plus ends following a natural
216   catastrophe vs. ablation in the aster interior.

217   Laser ablation experiments offer insights into the organization of microtubule
218   structures (Brugués et al. 2012; Decker et al. 2018). We found that the strength of the
219   depolymerization wave (i.e. the area under the curves of the summed differential
220   intensities) decreased with progression (Fig. 3E). This is explained by the fact that
221   depolymerization is halted when individual plus ends reach their corresponding minus
222   ends. Thus, this observation provides evidence that minus ends exist throughout the
223   aster, and confirms our previous proposal that asters are built of short
224   microtubules (Ishihara, Korolev, and Mitchison 2016).


225
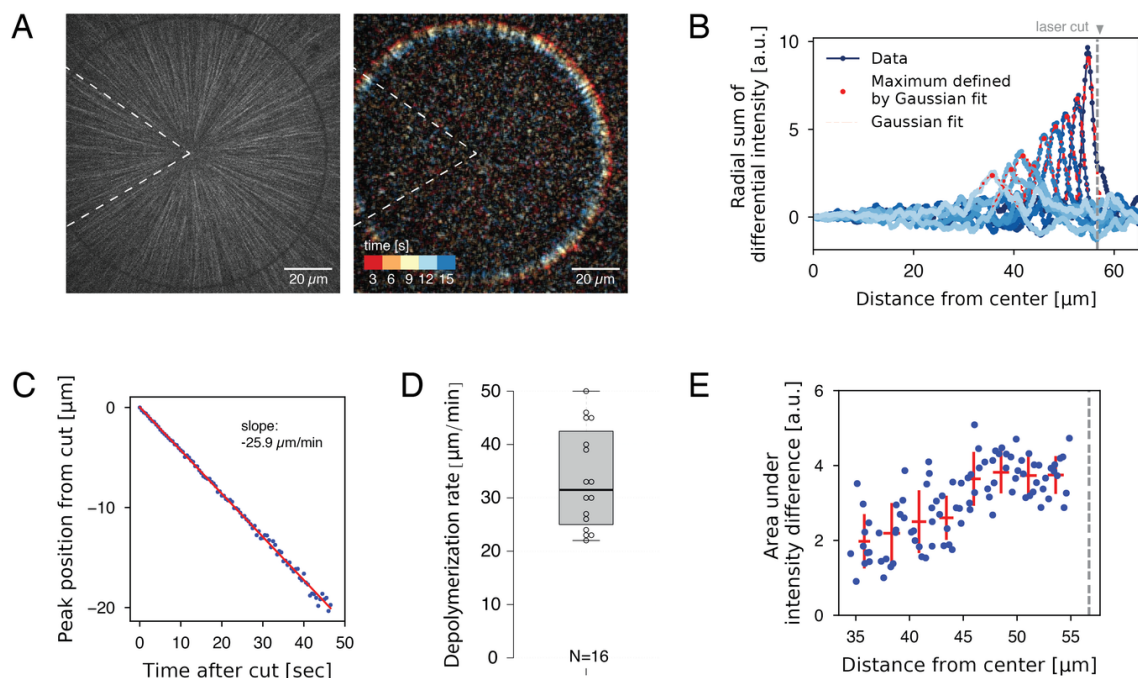
226   **Fig. 3** *Measurement of depolymerization rates following laser ablation. (A) An interphase*
227   *aster was subjected to a circular laser cut with radius 56 µm (left), which induced a wave*
228   *of microtubule depolymerization Movie 4. The resulting movie was used to construct a*
229   *differential intensity movie (right and Movie 5). Dotted wedge region indicates region*
230   *excluded from image analysis. (B) Radial sum of differential intensities at different time*
231   *points (from dark to light blue) of the same laser cut experiment. The area under each*
232   *curve equals the mass of microtubules depolymerized per time interval of 5 s. Vertical*
233   *dotted line indicates the location of the laser cut. (C) For each cut, the peak position of the*
234   *differential intensity travels at constant speed. (D) Depolymerization rates measured from*
235   *N = 16 laser cuts positioned at 15-56 µm from the center of the aster. (E) The area under*
236   *differential intensity curves decreases as the depolymerization wave travels inward. This*
237   *example corresponds to the cut depicted in panel A-C. Vertical dotted line indicates the*
238   *location of the laser cut.*

Aster growth results in spatial gradients of soluble tubulin and EB1

239   Spatial regulation of depolymerization rate could be due to complex biochemical
240   schemes, such as activation of a dynamics-regulating kinase in the aster interior. We
241   cannot rule out this kind of hypothesis, but we prefer an interpretation based on
242   component limitation, in part because this is a mechanistically simpler hypothesis, and
243   in part because component limitation is inevitable in a closed system. Component
244   limitation is a relevant consideration when comparing microtubule dynamics between
245   the inside and periphery of large asters because aster cytosol is not well mixed by
246   diffusion on relevant time and length scales. Specifically, the aster grows ballistically
247   into fresh cytosol outside the aster much faster than its interior can diffusively
248   equilibrate with that fresh cytosol. A simple Péclet number calculation serves to make
249   this point. Consider the dimensionless Péclet number: $\text{Pe} = \frac{\text{advective transport}}{\text{diffusive transport}} = \frac{Lu}{D}$. While
250   a typical protein molecule is transported in a diffusive process with cytoplasmic
251   diffusion coefficient $D = 360 \ \frac{\mu\text{m}^2}{\text{min}}$ (Salmon et al. 1984), aster growth is a ballistic or
252   advective process, i.e. radius increases linearly with time, with a velocity $u =$
253   $20 \frac{\mu\text{m}}{\text{min}}$ (Ishihara et al. 2014). Given a relevant length scale L, we evaluate the magnitude
254   of the Péclet number. The extremes are: Pe>>1, peripheral microtubules grow so fast
255   that they will always grow into fresh cytoplasm with plenty of available material. Pe<<1,
256   aster growth is limited by the diffusive transport of material to the aster periphery. At a
257   depth of $L = 200$ μm from the aster periphery, which is typical for our internal
258   measurements, Pe = 11, so diffusion makes little contribution to supplying subunits.
259   Thus, we expect the aster interior to effectively constitute a closed system, shut off from
260   fresh cytosol supplied by diffusion from the outwardly growing aster boundary.

262   To seek evidence for depletion of soluble subunits by growing asters we imaged
263   fluorescently labeled tubulin and analyzed its intensity profile as a proxy of local tubulin
264   concentration, summing both polymer and soluble forms (Fig. 4A). The center of asters
265   showed the highest signal, reflecting the highest microtubule polymer density. In
266   addition, we noticed an annular region at the aster periphery with ~4% lower value of
267   fluorescence signal relative to the background cytosol levels (Fig. 4B). We interpret this
268   as evidence for depletion of soluble tubulin by aster growth. Considering the potential
269   contribution of background signal, the 4% decrease of tubulin intensity is a lower
270   bound for the degree of depletion. The EB1-GFP intensity profile showed a similar
271   spatial pattern, suggesting that microtubule associated proteins may also be depleted to
272   some degree. Finally, we compared the relative position of tubulin/EB1 intensity
273   profiles to that of the EB1 comet density profile (Fig. 4B). This suggested that even the
274   most peripheral plus ends exist in a cytosolic environment that is 4% (or more)
275   depleted of tubulin and EB1 compared to unconsumed cytosol. The half-width of the
276   depleted zone extended ~50 microns beyond the growing aster periphery,
277   approximately consistent with our Péclet number estimate. This analysis indicated that
278   soluble protein levels may vary within growing asters due to subunit consumption.
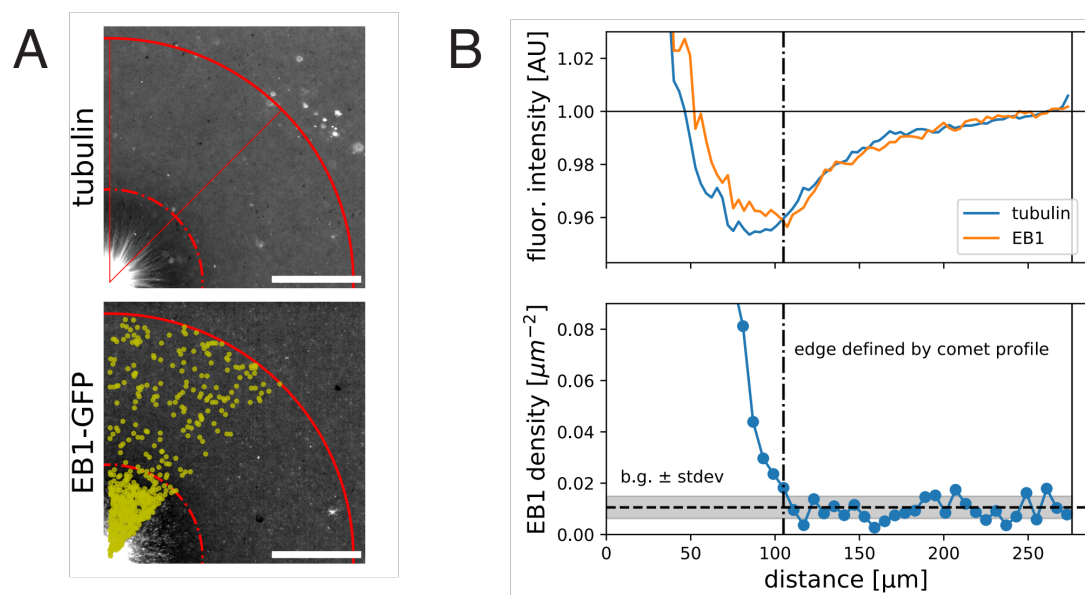
Fig. 4 *Fluorescent intensity profiles of tubulin and EB1 indicate spatial variation of these species within growing interphase asters. (A) Wide field images of a growing aster visualized with Alexa647-labelled tubulin and EB1-GFP. For both images, the contrast is adjusted to emphasize the zone of low fluorescence intensity. (B) Corresponding quantification of the fluorescence intensity profiles averaged over the quadrant and normalized to the intensity outside the aster (top) and EB1 comet density profile (bottom). We define the aster as the region that has EB1 density higher than the background level + standard deviation. Scale bar, 100 μm.*

Discussion

## Limiting component hypothesis for the spatial regulation of depolymerization rate

The initial motivation of this study was to test our previous assumption that microtubule dynamics was spatially homogenous during aster growth (Ishihara, Korolev, and Mitchison 2016). EB1 tracking experiments showed that the catastrophe rate was largely constant over hundreds of microns (Fig. 1), and the polymerization rate was ~10% higher in the periphery than the interior. Intensity difference imaging showed that the depolymerization rate varied from modal values of ~20 μm/min at the aster periphery to ~40 μm/min in the interior (Fig. 2). Average values were closer, 29 vs. 36 μm/min, but the effect size was evident. This may be the first report of systematic spatial variation in this parameter of dynamic instability.

Multiple hypotheses could be considered to account for the observed spatial regulation of depolymerization rates. We will focus on component depletion models because this is the simplest hypothesis; the growth of structures in confined cytoplasm necessarily consumes the available building blocks and limits further growth (see Introduction). Consistent with such a model, we found evidence for depletion of soluble tubulin and EB1 inside asters by imaging (Fig. 4) and a Péclet number calculation showed that the

306   cytosol inside and outside growing asters do not mix by diffusion once the distance
307   between them is larger than ∼50 microns.

308   The first candidate for a limiting component in a microtubule system is tubulin itself. As
309   tubulin concentration decreases, the literature predicts that plus ends should grow
310   more slowly and catastrophe more often (see Introduction). However, we observed
311   little spatial variation in these parameters, though EB1-measured growth rates trended
312   in the expected direction (Fig. 1). One reason for a lack of effect of depletion on
313   polymerization rate may be that the steady state polymer fraction in our system is
314   relatively low, ∼30% (Methods, Tubulin polymer fraction estimate), which is the upper
315   bound for difference in soluble tubulin concentration inside and outside asters. Given
316   this small difference and lack of literature on how soluble tubulin levels regulate
317   depolymerization, we explore alternative candidates for the limiting component that is
318   responsible for the spatial regulation of depolymerization rate.

319   Several MAPs have been shown to slow down depolymerization rates (Drechsel et al.
320   1992; Andersen and Karsenti 1997). We propose that one or mores MAPs that are
321   present at low concentrations relative to microtubule polymer binds to microtubules at
322   lower density in the interior compared to the periphery, resulting in faster
323   depolymerization in the interior (Fig. 5A). The key parameters that determines whether
324   a given MAP can cause spatial regulation in this way are concentration in cytosol and
325   affinity to the microtubule lattice, which together determine whether the MAP is
326   significantly depleted by microtubule binding. We present a toy model to illustrate how
327   these parameters may help us predict which MAPs regulate depolymerization (see
328   Method, A model of single MAP species binding to microtubule lattice). The model
329   predicts the fraction of freely diffusing MAP molecules $\frac{M_{\text{free}}}{M_{\text{total}}}$ and the site occupancy of
330   the microtubule lattice $\theta = \frac{M_{\text{bound}}}{P}$, both of which decrease with microtubule polymer
331   concentration P as expected (see Fig. 5B). For a hypothetical MAP whose abundance is
332   0.2 μM and associates with microtubules with a relatively tight dissociation constant of
333   100 nM, the fractional occupancy of the microtubule lattice decreases from 0.67 to 0.12
334   when the polymer concentration increases from 0 to 1.6 μM. We argue that such 5.6-
335   fold difference in microtubule lattice occupancy may be sufficient to cause differences in
336   depolymerization rate that account for spatial regulation. Soluble tubulin, in contrast,
337   only decreases by 0.7-fold. In Table 1, we summarize how different MAPs present in the
338   frog egg are predicted to change their lattice occupancies. Based on the predicted fold
339   change lattice occupancies, we favor EML4, MAP7 and its homologs MAP7D1 and
340   MAP7D2, and MAP1B as candidate regulators of depolymerization that are subject to
341   component limitation effects in large interphase asters, leading to faster
342   depolymerization in the interior.
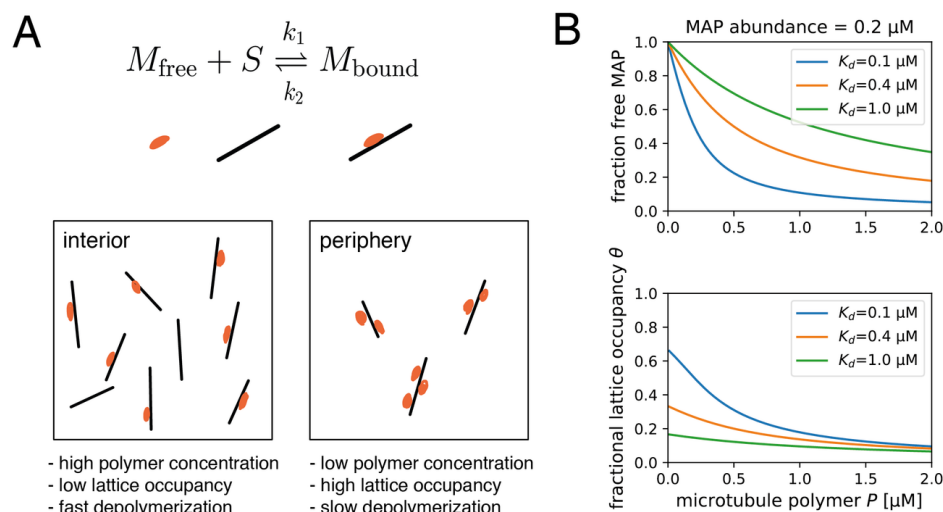
Fig. 5 *Proposed model for the regulation of depolymerization rate by a MAP species as the limiting component. (A) We consider the equilibrium of a single MAP species that associates with the microtubule lattice with dissociation constant $K_d = \frac{k_2}{k_1}$. We hypothesize that the degree at which a microtubule is bound by this MAP species slows down depolymerization rate. This effect is greater in the aster periphery, where the microtubule density is lower. (B) Fraction of free MAP and occupied microtubule lattice as a function of microtubule concentration for a hypothetical MAP present at 0.2 μM.*

Gene Symbol	Protein Description	abundance [nM]	Kd [nM]	reference	theta at low P	theta at P = 1.6 μM	theta fold change
MAP4	Microtubule-associated protein, XMAP230	964.5	300	Tokuraku et al. JBC 2003, Andersen et al. JCB 1994	0.76	0.45	1.69
EML2	Echinoderm microtubule-associated protein-like 2	578.18	?				
EML4	EML4 protein	504.2	180	Eichenmuller et al. Cytoskeleton 2001	0.74	0.27	2.74
EML1	Echinoderm microtubule-associated protein-like 1	135.67	?				
MAP7	Ensconsin	91.3	460	Monroy et al. Nat. Comm. 2018	0.17	0.04	4.25
MAP1B	Microtubule-associated protein 1B, XMAP310	84.68	200	Andersen et al. JCB 1997	0.3	0.05	6.0
MAP1S	MAP1S light chain	66.04	?				
MAP7D1	MAP7 domain-containing protein 1	46.97	?				
MAP7D2	MAP7 domain containing 2 protein varaint 2 (Fragment)	8.55	?				

Table 1 *Summary of microtubule associated proteins (MAPs) that may slow down plus end depolymerization rate. Protein abundance in the frog egg is from proteome data in (Wühr et al. 2014). For those with reported dissociation constants (Eichenmüller et al. 2001; Andersen and Karsenti 1997; Andersen et al. 1994; Monroy et al. 2018; Tokuraku et*

356   *al. 2003), we provide the estimated value of θ, the fractional occupancy of the microtubule*
357   *lattice at low (i.e. excess MAP) and high polymer concentrations (P = 1.6 μM).*

358   Our proposal that a spatially varying MAP:microtubule ratio regulates depolymerization
359   comes with several limitations. First, while a single, low-abundance, tight binding MAP
360   was considered in our model, multiple MAPs may reglated depolymerization rate in
361   eggs. The total abundance of all MAP species easily exceeds 2 μM. Thus, in a more
362   realistic scenario, multiple MAP species may compete for microtubule binding and their
363   order of association is governed by their abundances and affinities. Kinases such as
364   Cdk1, MARK, and Nek may regulate the affinity of these MAPs (Adib et al. 2018; Ookata
365   et al. 1997; Chang et al. 2001; Drewes et al. 1992; Illenberger et al. 1996; Drewes et al.
366   1997). Our current model is a useful starting point for future studies that consider
367   complex multi-species dynamics of cytoskeletal self-organization including the mitotic
368   spindle (Hazel et al. 2013; Good et al. 2013; Rieckhoff, Ishihara, and Brugués 2019;
369   Rieckhoff et al. 2020).

370   Second, while most MAPs that slow down depolymerization have been reported to
371   accelerate polymerization in minimal conditions (Drechsel et al. 1992; Andersen et al.
372   1994; Andersen and Karsenti 1997), we observed little regulation of polymerization
373   rate in our aster reactions. We speculate that, in a cellular context where the synergistic
374   effects of XMAP215 and EB1 play a prominent role in modulating plus end
375   dynamics (Kinoshita et al. 2001; Zanic et al. 2013), our hypothetical MAP may not
376   further accelerate polymerization. It will be interesting to carefully revisit
377   depolymerization rates in other cellular and reconstitution systems.

Implications of low tubulin polymer fraction for aster mechanics

379   Finally, what are the implications of our observations for the biology of interphase
380   asters in large eggs? Asters function to separate centrosomes and nuclei at the end of
381   mitosis, and to position cleavage furrows, both of which require that they grow to egg-
382   spanning size. Previously, we modeled aster growth from the interplay of
383   polymerization dynamics and autocatalytic nucleation at the periphery (Ishihara,
384   Korolev, and Mitchison 2016). To prevent the uncontrolled exponential growth
385   expected from an autocatalytic process, we had to assume negative feedback from
386   growth to further assembly, which we implemented as a logistic function that made no
387   mechanistic assumptions. Our current findings suggest that this feedback occurs mainly
388   by increased depolymerization rate in the aster interior, and that it leads to a steady
389   state with a relatively low polymer fraction, estimated as ~30% tubulin polymerized.
390   This low polymer density may be important for how dynein exert forces for aster
391   positioning (Wühr et al. 2010). Egg asters are gels comprising a network of relatively
392   short microtubules entangled with F-actin and organelles (Pelletier et al. 2020).
393   Microtubules are the stiffest component of this composite gel, so the bulk stiffness of the
394   aster is likely to depend strongly on the tubulin polymer fraction. We speculate that a
395   low polymer fraction allows the aster gel to deform in response to forces from dynein
396   and the ingressing furrow while maintaining sufficient connectivity to transmit forces
397   across large length scales.

398

Materials and Methods

Aster Reconstitution in Xenopus Egg Extract

Interphase microtubule asters were reconstituted in Xenopus egg extract with anti-AurkA coated beads as microtubule organizing centers (Field, Pelletier, and Mitchison 2017; Field et al. 2014). All reactions were supplemented with 0.04 mg/mL p150-CC1 fragment of dynactin to inhibit dynein motor activity. Fluorescently labelled tubulin or EB1-GFP was used to visualize microtubules.

Measurement of polymerization and catastrophe rates from EB1 comets

Wide-field images were acquired on a Nikon Eclipse Ni-E upright microscope equipped with a CFI Plan Apochromat Lambda 20× 0.75 N.A. objective lens (Nikon), Nikon motorized XY stage, and Hamamatsu ORCA-Flash4.0 LT scientific CMOS camera, driven by NIS-Elements. EB1-GFP was supplemented to the reactions at a final concentration of 200-400 nM. EB1 comets were imaged at 2 second intervals, and analyzed with TrackMate (Tinevez et al. 2017). For identifying spots, the LoG detector was used with with 2.0 micron spot diameter, threshold 10.0, no median filter, sub-pixel localization enabled. For linking tracks, the LAP tracker was applied with max search radius of 3 micron without gap closing. The results were further analyzed by a custom script written in Python to calculate the polymerization velocity (average of the frame-to-frame velocity for each track) and the catastrophe rate (fitting an exponential function to the comet duration distribution). The DABEST-Python package was used for statistics and effect size estimation (Ho et al. 2019).

Measurement of polymerization and depolymerization rates of microtubule ends

Physiological microtubule polymerization and depolymerization rates were measured by TIRF microscopy and tubulin intensity difference analysis. Briefly, asters labeled with Alexa647-labelled bovine tubulin were assembled under K-casein coated coverslips and imaged with TIRF microscopy (Ishihara et al. 2014). The Nikon Ti-E motorized inverted microscope was equipped with a Nikon motorized TIRF illuminator, Perfect Focus, a Prior Proscan II motorized stage, Agilent MLC400B laser launch (488 nm, 561 nm, 647 nm), and an Andor DU-897 EM-CCD camera. Alexa 647-labeled bovine tubulin was imaged with a 100× CFI Apo 1.49 N.A. TIRF objective lens (Nikon) with or without 1.5x Optovar. Stream acquisition of images at 500-ms intervals was performed using the RAM capture mode in NIS-Elements software (Nikon Instruments). We defined the aster interior as FOVs with the artificial MTOC in the corner (=center of the FOV less than 100 microns from the center of the aster), while peripheral regions were chosen as the leading edge of the growing aster with very few microtubules in the field of view (=center of the FOV at least 200 microns from the center of the aster).

To obtain spatial information regarding polymerization and depolymerization rates, we applied a recently developed workflow used to quantify treadmilling dynamics in bacterial cytoskeletal filaments (Caldas et al. 2019; Caldas et al. 2020). This method allows to track hundreds of growing and shrinking microtubule ends in an automated

441 fashion, overcoming the limitations of a standard manual kymograph analysis. We first
442 constructed differential time-lapse movies by subtracting the intensity differences
443 between each two consecutive frames. This image-processing step removes static
444 objects from the movie while regions containing intensity fluctuations give rise to either
445 a positive or negative signal (speckles), which corresponds to growth (polymerization)
446 or shrinkage (depolymerization) rates, respectively. Next, the particle-tracking software
447 for ImageJ, TrackMate (Tinevez et al. 2017), was used to automatically detect and follow
448 the resultant moving speckles to rebuild trajectories for analysis. Finally, a custom
449 python script is used to quantify densities and rates of all the detect spots along their
450 trajectories. For TrackMate, we used the LoG (Laplacian Gaussian) detector with an
451 estimated diameter of 1 μm to detect the moving spots. To discard potential false
452 positives, we considered only particles with a signal-to-noise ratio lower than 0.8 and a
453 track displacement distance larger than 1 μm. To build the final trajectories, we used
454 the "Simple LAP tracker" with a "Max Linking Distance" of 1 μm, a "Maximal gap-closing
455 distance" of 1 μm and "Max frame Gap" of 5 frames. Later, we only considered for
456 analysis trajectories longer than 5 sec. To construct the distributions in Fig. 2B, we
457 pooled the frame-to-frame velocities for each track without averaging. The DABEST-
458 Python package was used for statistics and effect size estimation (Ho et al. 2019).

459 ## Measurement of laser cutting-induced depolymerization rates

460 During the cutting experiments, interphase asters were labeled with Atto565 porcine
461 tubulin and imaged using a Nikon microscope (Ti Eclipse) with Yokogawa CSU-X1
462 confocal spinning disk, an EMCCD camera (Andor iXon DU-888), a 60x 1.2 NA water
463 immersion objective, and the software AndorIQ for image acquisition. Laser cutting and
464 image analysis were done as described in (Decker et al. 2018) with the only difference
465 that the laser pulse repetition rate was reduced by a pulse picker (APE pulseSelect)
466 from 80 MHz to 20 kHz for some of the cuts, which reduced the probability of
467 destroying the asters. In brief, the sample stage was moved according to the desired cut
468 shape in multiple z planes to reach a cut depth of ~2 μm around the focal plane. The
469 resulting inward traveling microtubule depolymerization wave was recorded at 2-5
470 frames/s. The measurement of the polymerization speed involved calculating
471 differential intensities from the raw images with a time difference of 2-3 s (see Fig. 3,
472 Movie 4, 5). These differential intensities were integrated with respect to the radius
473 leading to a Gaussian-shaped integrated intensity profile plotted over the radius for
474 each time point. Using the peak position of fitted Gaussians to these profiles, we
475 determined the distance that the depolymerization wave travelled over time. The slope
476 of this travelled distance over time plot equals the depolymerization speed of the cut
477 microtubules, which was constant over the entire time that the wave was visible (in
478 agreement with depolymerization in metaphase spindles and monopoles (Decker et al.
479 2018)).

480 ## Fluorescence intensity-based estimation of local depletion of
481 tubulin and EB1

482 Wide-field images were acquired on a Nikon Eclipse Ni-E upright microscope equipped
483 with a CFI Plan Apochromat Lambda 20× 0.75 N.A. objective lens (Nikon), Nikon
484 motorized XY stage, and Andor Zyla 4.2 Plus scientific CMOS camera, driven by NIS-
485 Elements. Alexa647-labelled bovine tubulin and EB1-GFP were supplemented to the

486 reactions. Dark current subtraction and flat field correction were applied to both
487 channels. A custom script written in Matlab was used to quantify the fluorescent
488 intensity as a function of radial distance from the MTOC (Pelletier et al. 2020). Spot
489 detection of EB1 comets was performed with TrackMate as described above.

Tubulin polymer fraction estimate

491 To estimate the fraction of tubulin that is in polymer state, we performed a simple
492 calculation based on our measurements. Specifically, we calculated the total
493 concentration of microtubule polymer in the interior of our aster reactions:

494
$$\left[\mathrm{MT_{polymer}}\right] = \frac{\rho \cdot L}{p \cdot N_A}$$

495 where

496 ρ: number of microtubules per volume [#/μm^3]

497 L: average length of a microtubule – 16 μm (Ishihara 2016)

498 p: pitch of tubulin dimers – 8 nm/13 heterodimers

499 N_A: Avogadro's number – 6*10^23 heterodimers/mole

500 By analyzing a z-stack of EB1-GFP images, we measured the thickness of a reaction
501 prepared by squashing 4 μl of extract under a 18x18 mm cover slip as ~10 micron.
502 Further, we found that a single focal plane of a 20x 0.75 NA lens captures as much as 30-
503 40% of all EB1 comets that are axially distributed in such reaction. Thus, we estimate
504 the microtubule density from $\rho = \frac{\sigma}{d\phi} \cdot \frac{f_{\mathrm{cat}} + f_{\mathrm{res}}}{f_{\mathrm{res}}}$.

505 σ: number of microtubule per area in a single focal plane – 0.08 per μm^2

506 d: Thickness of the cover slip reaction – 10 μm

507 ϕ: fraction of EB1 comet detected in a single focal plane - 0.35

508 f_{cat}: catastrophe rate - 3.3 [1/min] (Ishihara, Korolev, and Mitchison 2016)

509 f_{res}: rescue rate - 2.0 [1/min] (Ishihara, Korolev, and Mitchison 2016)

510 The ratio of catastrophe and rescue rates allow us to account for the shrinking plus
511 ends, which are not detected by EB1 comets. We estimate that asters contain [polymer]
512 = 2.65 μM of polymerized tubulin. Comparing this value to abundance of tubulin
513 heterodimers in the frog egg, 8.6 μM (Wühr et al. 2015), we estimate that ~31 % of
514 tubulin is in the polymer form.

A model of single MAP species binding to microtubule lattice

516 We consider a single MAP species M (total concentration M_{total}) that binds and unbinds
517 from the microtubule lattice (total concentration P). Let S denote the concentration of
518 free lattice sites and k_1 and k_2 denote the binding and unbinding rates, respectively.

519
$$M_{\mathrm{free}} + S \rightleftharpoons M_{\mathrm{bound}}$$
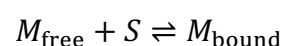
520   Conservation of MAP species: $M_{\text{total}} = M_{\text{free}} + M_{\text{bound}}$

521   Conservation of microtubule lattice sites: $P = S + M_{\text{bound}}$

522   The equation for mass action kinetics is:

523
$$\frac{dM_{\text{bound}}}{dt} = k_1 M_{\text{free}} S - k_2 M_{\text{bound}} .$$

524   Solving for the steady state solution $\frac{dM_{\text{bound}}}{dt} = 0$, we find:

525
$$M_{\text{bound}} = \frac{1}{2}\left(P + M_{\text{total}} + K_D - \sqrt{(P + M_{\text{total}} + K_D)^2 - 4 P M_{\text{total}}}\right)$$

526   This allows us to calculate, (fraction free MAP) $= \frac{M_{\text{free}}}{M_{\text{total}}} = 1 - \frac{M_{\text{bound}}}{M_{\text{total}}}$

527   and (fractional lattice occupancy) $= \theta = \frac{M_{\text{bound}}}{P}$.

Supplementary Material

529   **Movie 1.** Timelapse imaging of EB1-GFP comets during aster growth.

530   **Movie 2.** TIRF microscopy-based intensity difference imaging of the aster interior. Blue
531   correspond to positive intensity difference interpreted as polymerization, while red
532   correspond to negative intensity difference interpreted as depolymerization.

533   **Movie 3.** TIRF microscopy-based intensity difference imaging of the aster periphery.

534   **Movie 4.** A circular laser ablation induces an inward wave of depolymerization.

535   **Movie 5.** Intensity difference movie corresponding to the laser ablation in Movie 4.

Author Contributions

537   KI and TJM designed the research and wrote the manuscript with help from all
538   authors. TJM acquired the data and KI performed the analysis for EB1 comets. KI, PC,
539   and ML performed the tubulin intensity difference analysis. KI, FD, and JFB performed
540   the laser ablation experiments and analyzed the data. KI and JFP performed the analysis
541   to infer local protein depletion from wide field microscopy images. KI developed the
542   theoretical model.

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554 Competing interests

555 All the authors declare no competing interests.

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