

1    **Evolutionary and ontogenetic changes of the anatomical organization and modularity in the**  
2    **skull of archosaurs**

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4    **Short title: Evolution of network anatomy in archosaurian skulls**

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16 **Abstract**

17 Comparative anatomy studies of the skull of archosaurs provide insights on the mechanisms of  
18 evolution for the morphologically and functionally diverse species of crocodiles and birds. One of  
19 the key attributes of skull evolution is the anatomical changes associated with the physical  
20 arrangement of cranial bones. Here, we compare the changes in anatomical organization and  
21 modularity of the skull of extinct and extant archosaurs using an Anatomical Network Analysis  
22 approach. We show that the number of bones, their topological arrangement, and modular  
23 organization can discriminate birds from non-avian dinosaurs, and crurotarsans. We could also  
24 discriminate extant taxa from extinct species when adult birds were included. By comparing  
25 within the same framework, juveniles and adults for crown birds and alligator (*Alligator*  
26 *mississippiensis*), we find that adult and juvenile alligator skulls are topologically similar,  
27 whereas juvenile bird skulls have a morphological complexity and anisomerism more similar to  
28 those of non-avian dinosaurs and crurotarsans than of their own adult forms. Clade-specific  
29 ontogenetic differences in skull organization, such as extensive postnatal fusion of cranial bones  
30 in crown birds, can explain this pattern. The fact that juvenile and adult skulls in birds do share a  
31 similar anatomical integration suggests the presence of a specific constraint to their ontogenetic  
32 growth.

33

34 **Keywords:** Comparative Anatomy; Cranium; Anatomical Network Analysis; Birds; Crocodiles;  
35 craniofacial evolution, Archosauria

36 **INTRODUCTION**

37 The skulls of archosaurs are morphologically and functionally diverse, with clade-specific  
38 specialized features that set apart crurotarsans (extant crocodilians and their stem lineage) from  
39 avemetatarsalians (birds and non-avian dinosaurs)<sup>1-7</sup>, as reviewed by Brusatte and colleagues<sup>8</sup>.  
40 The evolution and diversification of the skull of archosaurs have been associated with changes in  
41 the patterns of phenotypic integration and modularity<sup>9-13</sup>. For more information on integration  
42 and modularity in shape, see the review by Klingenberg<sup>14</sup>. Different regions of the skull may act  
43 as anatomical modules that can evolve, function, and develop semi-independently from one  
44 another. Bones within a same module tend to co-vary in shape and size more with each other than  
45 with bones from other such variational modules<sup>15-18</sup>. In addition, the bones of the skull can also  
46 modify their physical articulations so that some groups of bones are more structurally integrated  
47 than others, and, hence, we can recognize them as distinct anatomical-network modules, which  
48 had been defined by Eble as a type of organizational modules<sup>15,19,20</sup>. The relationship between  
49 anatomical-network modules and variational modules is not yet fully understood, but it is thought  
50 that network anatomy constrain growth patterns and shape variation<sup>21-23</sup>.

51

52 Changes in the anatomical organization of the skull in archosaurs have been concomitant with a  
53 broader evolutionary trend in tetrapods toward a reduction in the number of skull bones due to  
54 loses and fusions, a phenomenon known as the Williston's law<sup>24-26</sup>. Understanding how the bones  
55 are globally arranged to each other allows us to measure the anatomical complexity and  
56 organization of body parts, and explain how structural constraints might have influenced the  
57 direction of evolution<sup>25-28</sup>. Werneburg and colleagues compared the skull network-anatomy of a  
58 highly derived *Tyrannosaurus rex*, *Alligator mississippiensis* and *Gallus gallus* with that of an  
59 opossum, a tuatara, and a turtle<sup>29</sup>. They found that the tyrannosaur has the most modular skull  
60 organization among these amniotes, with a modular separation of the snout in upper and lower  
61 sub-modules and the presence of a lower adductor chamber module. However, the specific

62 anatomical changes in the organization of the archosaur skull during their evolutionary transitions  
63 more generally have never been characterized. More recently, Plateau and Foth used anatomical  
64 network analysis to study postnatal ontogenetic changes in the skulls of crown bird and non-avian  
65 theropods<sup>30</sup>. They found that early juvenile crown birds have skulls that are less integrated and  
66 more modular than those of more derived birds, resembling their non-avian theropod ancestors.

67

68 Here, we compared the anatomical organization and modularity of the skull of archosaurs using  
69 Anatomical Network Analysis (AnNA)<sup>31</sup> to highlight how skull topology has changed in  
70 evolutionary and developmental scales. We chose AnNA over more conventional methods, such  
71 as geometric morphometrics, to understand how major re-organizations of the skull (i.e., loss and  
72 fusion of bones) affect the overall anatomy regardless of shape. We created network models of  
73 the skull for 21 species of archosaurs, including taxa representing key evolutionary transitions  
74 from early pseudosuchians to crocodiles, from non-avian theropods to modern birds, and from  
75 paleognath birds to neognaths (Fig. 2). Our dataset also includes a representative ornithischian, a  
76 sauropodomorph, and a basal saurischian (Supplementary Information 1) for comparison. To  
77 understand the significance of the ontogenetic transitions in archosaur skulls, we provided our  
78 dataset with juvenile skulls for extant birds and alligator. Network models of the skull were built  
79 by coding individual cranial bones and their articulations with other bones as the nodes and links  
80 of a network, respectively (Fig. 1). Network modules, defined as a group of bones with more  
81 articulations among them than to other bones outside the module, were identified heuristically  
82 using a community detection algorithm. We compared skull architectures using topological  
83 variables (i.e. network parameters) that capture whole-skull anatomical feature (modelling and  
84 analysis of anatomical networks were detailed previously<sup>20,25,31</sup>).

85

86 Networks and network modules and their respective complexity, integration, modularity, and  
87 anisomerism could be quantified by these network parameters: density of connections, clustering

88 coefficient, path length, heterogeneity of connections, and parcellation<sup>20,23,31,32</sup>. Here, complexity  
89 is defined as the relationship of bones in a skull and is associated with how abundant are the  
90 interactions that bones have with each other (i.e. density of connections), how interdependent or  
91 integrated the bones are (i.e. clustering coefficient), and proximity between nodes (i.e. path  
92 length). A more complex network would have higher density, higher clustering coefficient, and  
93 shorter path length. Anisomerism is defined as a deviation among anatomical parts<sup>33</sup> and could be  
94 observed by the specialization of bones and measured by heterogeneity of connections, i.e. how  
95 each bone has a different number of connection<sup>25</sup>. Modularity is measured by parcellation, which  
96 is the number of modules and the consistency in the number of bones per module.

97

98

## 99 MATERIAL AND METHODS

100

### 101 Sampling

102 We sampled extinct and extant species, and for some forms included both adults and juveniles to  
103 account for ontogenetic trends within archosaurs. Namely, adults *Aetosaurus ferratus*,  
104 *Archaeopteryx lithographica*, *Citipati osmolskae*, *Coelophysis bauri*, *Compsognathus longipes*,  
105 *Dakosaurus andiniensis*, *Desmatosuchus haplocerus*, *Dibothrosuchus elaphros*, *Dilophosaurus*  
106 *wetherilli*, *Eoraptor lunensis*, *Ichthyornis dispar*, *Plateosaurus engelhardti*, *Psittacosaurus*  
107 *lujiautunensis*, *Riojasuchus tenuisceps*, *Sphenosuchus acutus*, *Velociraptor mongoliensis*, *Gallus*  
108 *gallus*, *Geospiza fortis* and *Nothura maculosa*; and juveniles *Gallus gallus*, *Geospiza fortis*,  
109 *Nothura maculosa* and *Alligator mississippiensis*. Within our sample set, eight species represent  
110 the transition from crurotarsan archosaur ancestor to modern crocodilians and 13 species  
111 represent the transition from non-avian theropods to modern birds as described previously<sup>34-43</sup>.  
112 Due to the sample size limitation for extinct taxa, reconstructed and type forms were used to  
113 represent each taxon and intraspecific variation could not be accounted for.

114

115 **Phylogenetic Context**

116 We created a phylogenetic tree (Figure 2) based on the previous studies<sup>34–37,39–44</sup>. The tree was  
117 calibrated using the R package paleotree<sup>45</sup> by the conservative “equal” method<sup>46,47</sup>; branching  
118 events were constrained using the minimum dates for known internal nodes based on fossil data  
119 from Benton and Donoghue<sup>48</sup> (listed in Table S3) and the first and last occurrences of all 21  
120 species from the Paleobiology Database using the paleobioDB package<sup>49</sup> in R. Because there  
121 were two extinct *Nothura* species in the Paleobiology Database, the last occurrence for extant  
122 *Nothura* species was adjusted to 0 (Table S2).

123

124 **Network Modelling**

125 We built anatomical network models for each archosaur skull in our sample set based on detailed  
126 literature descriptions and CT scans of complete skulls (see Supplementary Information 1). Skull  
127 bones were represented as the nodes of the network model and their pair-wise articulations (e.g.  
128 sutures and synchondroses) were represented as links between pairs of nodes (Figure 1). Skull  
129 network models were formalized as binary adjacency matrices, in which a 1 codes for two bones  
130 articulating and a 0 codes for absence of articulation. Bones that were fused together without  
131 trace of a suture in the specimens examined were formalized as a single individual bone.

132

133 **Network Analysis**

134 Following Esteve-Altava et al<sup>28</sup>, we quantified the following topological variables for each  
135 network model: the number of nodes (N), the number of links (K), the density of connections (D),  
136 the mean clustering coefficient (C), the mean path length (L), the heterogeneity of connections  
137 (H), the assortativity of connections (A), and the parcellation (P). The morphological  
138 interpretation of these topological variables has been detailed elsewhere<sup>28</sup>. A summary is  
139 provided here. N and K represent the direct count of the number of individual bones and

140 articulations observed in the skull. D is the number of connections divided by the maximum  
141 number of possible connections (it ranges from 0 to 1); D is a proxy measure for morphological  
142 complexity. C is the average number of neighboring bones that connect to one another in a  
143 network (i.e., actual triangles of nodes compared to the maximum possible): a value close to 1  
144 shows all neighboring bones connect to each other while a value close to 0 shows neighboring  
145 bones do not connect to each other; C is a proxy measure for anatomical integration derived from  
146 co-dependency between bones. L measures average number of links separating two nodes (it  
147 ranges from 1 to N-1); L is a proxy measure of anatomical integration derived from the effective  
148 proximity between bones. H measures how heterogeneous connections are in a network: skulls  
149 composed of bones with a different number of articulations have higher H values. If all bones had  
150 the same number of connections (i.e., H = 0), it means that all bones were connected in the same  
151 way and the skull had a regular shape. A measures whether nodes with the same number of  
152 connections connect to each other (it ranges from -1 to 1); H and A are a proxy measure for  
153 anisomerism or diversification of bones. P measures the number of modules and the uniformity in  
154 the number of bones they group (it ranges from 0 to 1); P is a proxy for the degree of modularity  
155 in the skull. Calculating P requires a given partition of the network into modules (see next below).

156

157 Network parameters were quantified in R<sup>50</sup> using the igraph package<sup>51</sup>. Networks visualization  
158 was made using the visNetwork package<sup>52</sup> and Cytoscape<sup>53</sup>.

159

## 160 Principal Component Analysis

161 We performed a Principal Component Analysis (PCA) of the eight topological variables with a  
162 singular value decomposition of the centered and scaled measures. On the resulting PCs, we used  
163 a PERMANOVA (10,000 iterations) to test whether topological variables discriminate between:  
164 (1) Avialae and non-Avialae; (2) adults and juveniles; (3) extinct and extant; (4) Crurotarsi and  
165 Avemetatarsalia; (5) Neornithes and non-Neornithes; (6) early flight, can do soaring flight, can do

166 flapping flight, gliding, and flightless (details in Table S5); (7) Crurotarsi, non-avian Dinosauria,  
167 and Aves; and (8) carnivorous, omnivorous, and herbivorous (dietary information in  
168 Supplementary Information 4). First, we performed the tests listed above for all archosaurs. Then,  
169 we repeated these tests for a sub-sample that included all archosaurs, except for all modern birds.  
170 Next, we repeated these tests for a sub-sample that included all archosaurs, except for adult birds.

171

172

### 173 **Modularity Analysis**

174 To find the optimal partition into network modules we used a node-based informed modularity  
175 strategy<sup>54</sup>. This method starting with the local modularity around every individual node, using  
176 cluster\_spinglass function in igraph<sup>51</sup>, then it returns the modular organization of the network by  
177 merging non-redundant modules and assessing their intersection statistically using combinatorial  
178 theory<sup>55</sup>.

179

## 180 **RESULTS**

181

### 182 **Topological discrimination of skull bones**

183 A Principal Component Analysis (PCA) of the eight topological variables measured in skull  
184 network models discriminates skulls with different anatomical organizations (Figs. S1-S3). When  
185 all sampled skulls are compared together, the first three principal components (PCs) explain 89.4%  
186 of the total variation of the sample. PC1 (57.5%) discriminates skulls by number of their bones  
187 (N), density of connections (D), and degree of modularity (P). PC2 (21.3%) discriminates skulls  
188 by their degree of integration (C) and anisomerism (H). Finally, PC3 (10.6%) discriminates skulls  
189 by whether bones with similar number of articulations connect with each other (A).

190

191 PERMANOVA tests confirm that different skull anatomies map onto different regions of the  
192 morphospace. Thus, we can discriminate: Avialae (Aves plus *Ichthyornis* and *Archaeopteryx*)  
193 versus non-Avialae ( $F_{1,23} = 4.124, p = 0.006699$ ; Fig. 3B); Neornithes plus toothless archosaurs  
194 versus archosaurs with teeth ( $F_{1,23} = 6.99, p = 0.0005999$ ; Fig. 3C); Aves (include all modern  
195 birds) versus Crurotarsi versus non-avian Dinosauria ( $F_{2,22} = 3.837, p = 0.000699$ ; Fig. 3D); and  
196 extant and extinct species ( $F_{1,23} = 4.304, p = 0.0017$ ; Fig. S1C). However, we find no statistically  
197 significant difference in morphospace occupation between crurotarsans and avemetatarsalians  
198 ( $F_{1,23} = 1.46, p = 0.2002$ , Fig. S1D).

199  
200 When all avians are excluded from the comparison, the first three PCs now explain 80.6% of the  
201 total variation (Figs. S4-6). PC1 (38.6%) discriminates skulls by the density of their inter-bone  
202 connections (D) and effective proximity (L). PC2 (22.6%) discriminates skulls by the number of  
203 bones and their articulations (N and K). Finally, PC3 (19.5%) now discriminates skulls by their  
204 anisomerism (H) and whether bones with the same number of connections connect to each (A).  
205 PERMANOVA tests could not discriminate between Crurotarsi and non-avian Dinosauria ( $F_{1,17} =$   
206  $1.235, p = 0.3022$ ; Fig. S4D), and between extant and extinct species ( $F_{1,17} = 2.274, p = 0.06399$ ;  
207 Fig. S4C).

208  
209 When only adult birds are excluded, the first three PCs explain 79.7% of the topological variation  
210 (Figs. S7-9). PC1 (35.8%), PC2 (24.5%), and PC3 (19.5%) discriminate skull similarly as when  
211 all birds are excluded (see above). PERMANOVA tests also could not discriminate between  
212 juvenile birds, crurotarsans, and non-avian dinosaurs ( $F_{2,19} = 1.682, p = 0.09649$ ; Fig. S7D), and  
213 between extant and extinct species ( $F_{1,20} = 2.119, p = 0.06169$ ; Fig. S7C).

214  
215 Regardless of the sub-sample compared, we found no statistically significant difference in  
216 morphospace occupation between taxa stratified by flying ability and diet (Fig. S1E, see

217      Supplementary Information 4 for details). This suggests that at least for the given sample set  
218      changes in cranial network-anatomy (i.e. how bones connect to each other) are independent of  
219      both dietary adaptations and the ability to fly.

220

221      **Number of network modules**

222      The number of network modules identified in archosaur skulls ranged from one (i.e. fully  
223      integrated skull) in adult birds *Nothura maculosa* (the spotted tinamou) and *Geospiza fortis*  
224      (medium ground finch) to eight in the non-avian dinosaur *Citipati* (Table S10). The number of  
225      network modules within the studied taxa decreases during evolution of both major archosaurian  
226      clades: from 6 (*Riojasuchus*) to 4 (*Desmatosuchus*), and from 6 (*Dibothrosuchus*) to 4  
227      (*Dakosaurus* and all adult crocodilians) modules in Crurotarsi; from 6 (*Coelophysis*) to 4  
228      (*Dilophosaurus* and *Compsognathus*), and from 8 (*Citipati*) to 4 (*Velociraptor*, *Archaeopteryx*,  
229      *Ichthyornis*, and juvenile modern birds) modules in theropod-juvenile bird transition (Fig. 4A and  
230      4B, Table S10). We found no modular division of the skull in adult *Nothura* and *Geospiza*. This  
231      is most likely because these skulls are highly integrated due to the extensive cranial bone fusion  
232      in adults, which, in turn, results in a network with very few nodes. In general, skull networks are  
233      partitioned into overlapping modules.

234

235

236

237      **DISCUSSION**

238

239      **Occupation of morphospace and evolution of skull architecture**

240      The two major groups of archosaurs (Crurotarsi and Avemetatarsalia) show an analogous trend  
241      towards a reduction in the number of skull bones (Table S8; Supplementary Information 3), in  
242      line with the Williston's Law, which states that vertebrate skulls tend to become more specialized

243 with fewer bones as a result of fusions of neighboring bones during evolution<sup>25,56,57</sup>. This  
244 reduction in the number of bones and articulations, together with an increase in density, is also  
245 observed within aetosaurs and sphenosuchians (Table S8). Likewise, we observed fusion of  
246 paired bones into new unpaired ones: for example, left and right frontals, parietals, and palatines  
247 are fused through their midline suture in the more derived taxa, such as the crocodilians (Table  
248 S6). Bone fusion in extant species produced skulls that are more densely connected than the  
249 skulls of extinct species (Fig. S1C). It was previously suggested that the more connected skulls  
250 would have more developmental and functional inter-dependences among bones, and, hence, they  
251 would be more evolutionarily constrained<sup>22,23</sup>. Similarly, avian cranium with its strongly  
252 correlated traits has lower evolutionary rates and bird skulls are less diverse overall<sup>12</sup>.

253

254 Bhullar et al. pointed out that avian kinesis relies on their loosely integrated skulls with less  
255 contact and, thus, skulls with highly overlapping bones would be akinetic<sup>58</sup>. This contradicts our  
256 observations here in that kinetic crown birds have more complex and integrated skulls than the  
257 akinetic crurotarsans and the partially kinetic *Riojasuchus*<sup>59</sup>. The reason could be that Bhullar et  
258 al. factored in how much connective tissue and number of contact points each bone has, but not  
259 the total number of connections possible from the number of bones in these taxa. The total  
260 number of articulations possible is the denominator used to calculate density. More recently,  
261 Werneburg and colleagues showed *Tyrannosaurus*, suspected to have kinesis, also has a higher  
262 density when compared to akinetic *Alligator* but lower density when compared to the more  
263 derived and clearly kinetic *Gallus* skull<sup>29</sup>.

264

265 When compared with modules identified by Felice et al.<sup>60</sup>, the node-based modules, such as the  
266 rostral and neurocranial modules (shown as blue and red modules in Fig. 4), are composed of  
267 elements essentially similar to those described as variational modules (more details in  
268 Supplementary Information 2). The supraoccipital and basioccipital bones were part of the same

269 topology-defined (Supplementary Information 2, Fig. 4) and shape-defined module in most taxa,  
270 likely due to its functional importance in connecting the vertebral column with the skull<sup>60</sup>.

271

## 272 **Crurotarsi**

273 The aetosaurs, *Aetosaurus* and *Desmatosuchus*, and the sphenosuchians, *Sphenosuchus* and  
274 *Dibothrosuchus*, show an increase in complexity within their lineages. The more derived aetosaur  
275 *Desmatosuchus* has a fused skull roof (parietal fused with supraoccipital, laterosphenoid, prootic  
276 and opisthotic) and toothless premaxilla that are absent in the less derived aetosaur *Aetosaurus*<sup>61–</sup>  
277 <sup>63</sup>. In contrast, basal and derived sphenosuchian are more topologically similar. Their main  
278 difference is that basipterygoid and epiotic are separate in *Sphenosuchus* but are fused with other  
279 bones in the more derived *Dibothrosuchus*<sup>64,65</sup>. When we compared aetosaurs and sphenosuchians,  
280 we found that sphenosuchians have a skull roof intermediately fused condition between  
281 *Aetosaurus* and *Dibothrosuchus*: interparietal sutures in both sphenosuchians are fused while  
282 supraoccipital, laterosphenoid, opisthotic, and prootic remain separate.

283

284 To understand cranial topology in Thalattosuchia, a clade with adaptations specialized for marine  
285 life, we included *Dakosaurus andiniensis*. These adaptations comprise nasal salt glands<sup>66</sup>,  
286 hypocercal tail, paddle-like forelimbs, ziphodont dentition, fusion of the inter-premaxillary suture,  
287 a fused vomer, and a short and high snout<sup>67,68</sup>. Despite these adaptations, *Dakosaurus* has a  
288 cranial complexity closer to that of extant crocodylians by similarly having inter-frontal and inter-  
289 parietal fusions<sup>67,68</sup>. In addition to the fused frontals and parietals, both *Crocodylus* and *Alligator*  
290 have a fused palate and a fused pterygoid bones.

291

292 In turn, crurotarsans first fuse the skull roof and skull base, followed by the fusion of the face  
293 (more details on Table S6). Interestingly, this resonates with the pattern of sutural fusion in  
294 alligator ontogeny, which cranial (i.e. frontoparietal) has the highest degree of suture closure

295 followed by skull base (i.e. basioccipital-exoccipital) and then the face (i.e. internasal)<sup>69</sup>  
296 suggesting that the same mechanism may control topological changes in both ontogeny and  
297 evolution.

298

299 **Avemetatarsalia**

300 Avemetatarsalian transition is marked with a faster ontogenetic bone growth in more derived taxa,  
301 indicated by higher degree of vascularization, growth marks, and vascular canal arrangement  
302 (reviewed by Bailleul<sup>70</sup>), more pneumatized skulls (reviewed by Gold<sup>71</sup>), and an increase in  
303 complexity reminiscent of what is observed in crurotarsans. The basal ornithischian *Psittacosaurus*  
304 *luijiautunensis* and basal saurischian *Eoraptor lunensis* are relatively close to each other on the  
305 morphospace (Fig. 3), with the *Psittacosaurus* skull showing slightly more density because of  
306 fused palatines, a trait which is also observed in extant crocodilians and some birds, and its extra  
307 rostral bone as observed in other ceratopsians<sup>72</sup>.

308

309 The basal sauropodomorph *Plateosaurus engelhardti* has the lowest clustering coefficient (i.e.  
310 lower integration) of archosaurs, suggesting that skulls of sauropodomorphs are less integrated  
311 than those of saurischians<sup>31</sup>, accompanied by poorly connected bones (as seen in the network in  
312 Fig. 4C). Poorly connected bones, for example epipterygoid, and some connections, such as the  
313 ectopterygoid-jugal articulation, are later lost in neosauropods<sup>43,73</sup>.

314

315 Within theropods, the ceratosaurian *Coelophysis* is more derived and has a slightly more complex  
316 and specialized skull than the ceratosaurian *Dilophosaurus*<sup>42</sup>. Their positions on the morphospace  
317 suggest that ceratosaurians occupy a region characterized by a higher mean path length (L), when  
318 compared to other archosaurs (Fig. 3). *Compsognathus* is close to *Riojasuchus* on the  
319 morphospace with a similar mean path length (Figs 3 and S4, Table S8), its facial bones are also  
320 unfused, and it has a similar composition for its facial modules (see facial modules in

321 *Compsognathus* and nasal modules in *Riojasuchus* on Table S4 and Figure S10). These  
322 observations suggest an ancestral facial topology (see Table S6 and S8 for more details) is  
323 concomitant to the magnitude of shape change reported for compsognathids<sup>34</sup>. *Compsognathus*  
324 possesses an independent postorbital that is absent from *Ichthyornis* to modern birds. It also has  
325 an independent prefrontal that is absent in most Oviraptorsauria and Paraves<sup>74</sup>, including *Citipati*,  
326 *Velociraptor*, and from *Ichthyornis* to modern birds. Despite its ancestral features, the back of the  
327 skull and the skull base of *Compsognathus* are fused, similarly to other Paravians and modern  
328 birds.

329

330 The oviraptorid *Citipati* has a skull topology that occupies a morphospace within non-avian  
331 theropods, despite its unique vertically-oriented premaxilla and short beak<sup>34,75</sup>. *Citipati* has an  
332 independent epipyterygoid that is also present in some non-avian theropods and ancestral  
333 archosaurs, such as *Plateosaurus erlenbergiensis*, but which is absent in extant archosaurs<sup>75-78</sup>.  
334 *Citipati* also has fused skull roof (with fused interparietals), skull base, and face, marked with  
335 fused internasal and the avian-like inter-premaxillary sutures.

336

337 Like other dromaeosaurids, *Velociraptor*'s eyes are positioned lateral to the rostrum. Its prefrontal  
338 bone is either absent or fused with the lacrimal while it remains separate in other  
339 dromaeosaurids<sup>79-81</sup>. We observed a loss of the prefrontals from *Citipati* to modern birds, but not  
340 in more ancestral archosaurs or crurotarsans. Bones forming the *Velociraptor* basicranium, such  
341 as basioccipital, and basisphenoid are fused with other members of the basicranium (listed in  
342 Table S6). Despite having a similar number of bones and articulations to *Citipati*, the cranial  
343 bones in *Velociraptor* are more integrated with each other and are more likely to connect to bones  
344 with a different number of articulations (i.e. more disparity) (Table S8). Like *Compsognathus* and  
345 other primitive non-avian dinosaurs, *Velociraptor* has an ancestral facial topology with separate  
346 premaxilla, maxilla, and nasal bones.

347

348 ***Archaeopteryx* and *Ichthyornis* as intermediates between non-avian theropods and modern  
349 birds**

350 The skull of *Archaeopteryx* occupied a region of the morphospace closer to non-avian dinosaurs  
351 and crurotarsans than to juvenile birds (Fig. 3). The distance of *Archaeopteryx* from crown birds  
352 and its proximity in the morphospace to *Velociraptor* and *Citipati* along the PC1 axis (Fig. 3)  
353 may reflect the evolving relationship between cranial topology and endocranial volume. In fact,  
354 *Archaeopteryx* has an endocranial volume which is intermediate between the ancestral non-avian  
355 dinosaurs and crown birds<sup>82,83</sup> and it is within the plesiomorphic range of other non-avian  
356 Paraves<sup>84</sup>. This makes *Archaeopteryx* closer to dromaeosaurid *Velociraptor* than to oviraptor  
357 *Citipati*, for both its skull anatomy and its endocranial volume<sup>84</sup>. Modifications related to the  
358 smaller endocranial volume in *Archaeopteryx* include the unfused bones in the braincase, the  
359 independent reappearance of a separate prefrontal after the loss in Paraves<sup>74</sup>, a separate left and  
360 right premaxilla as observed in crocodilian snouts and ancestral dinosaurs, and the presence of  
361 separate postorbitals, which might restrict the fitting for a larger brain<sup>34</sup>.

362

363 Compared to *Archaeopteryx*, *Ichthyornis* is phylogenetically closer to modern birds and occupies  
364 a region of the morphospace near the juvenile birds and extant crocodilians when adult birds are  
365 included in the analysis (Fig. 3), but closer to extant crocodilians when all birds or when adult  
366 birds are removed (Figs. S4-9). The proximity between *Ichthyornis* and juvenile birds may be  
367 explained by the similar modular division (as observed in Figs. 4B and 4D; Table S4, Fig. S10),  
368 presence of anatomical features characteristic of modern birds, such as the loss of the postorbital  
369 bones, the fusion of the left and right premaxilla to form the beak, a bicondylar quadrate that form  
370 a joint with the braincase, and the arrangement of the rostrum, jugal, and quadratojugal required  
371 for a functional cranial kinetic system<sup>58,85-88</sup>. The proximity between *Ichthyornis* and extant

372 crocodilians in terms of complexity (Figs. S4-9, Table S8) may be explained by the fused frontal  
373 and fused parietal, and separate maxilla, nasal, pectoral and laterosphenoid (Table S6).

374

375 **Paleognath and neognath birds**

376 Juvenile birds have a skull roof with relatively less fused bones with the interfrontal, interparietal,  
377 and frontoparietal sutures open, and a more fused skull base. Postorbital is already fused in all  
378 juvenile birds (i.e. after hatching). Collectively, juvenile neognaths show a skull anatomy with a  
379 fused cranial base, relatively less fused roof, and unfused face that resembles the anatomy of  
380 ancestral non-avian theropods. Unlike what is observed in non-avian theropods, frontal, parietal,  
381 nasal, premaxilla, and maxilla eventually fuse with the rest of the skull in adult modern birds.  
382 However, in the palatal region not all the sutures are completely closed: the caudal ends of the  
383 vomers remained unfused in adult *Nothura*, which is a characteristic common in Tinamidae<sup>89</sup>. A  
384 similar pattern of suture closure has been described in another paleognath, the emu, in which the  
385 sutures of the base of the skull close first and then the cranial and facial sutures close while  
386 palatal sutures remain open<sup>69</sup>. The only difference is that in *Nothura*, where closure of major  
387 cranial sutures (frontoparietal, interfrontal, and interparietal) happens after the facial sutures  
388 closure. In summary, when compared with neognaths, the skull of the paleognath *Nothura* is  
389 more homogeneous and complex in both juvenile and adult stages. As the skull grows, its bones  
390 fuse and both its complexity and heterogeneity increase.

391

392 Within the neognaths, the skull of *Geospiza fortis* is more complex and more homogenous than  
393 *Gallus gallus* in both juvenile and adult stages: bones in *Geospiza* skull are more likely to connect  
394 with bones with the same number of connections than *Gallus*. These two trajectories illustrate  
395 how the connectivity of each bone diversifies and becomes more specialized within a skull as  
396 sutures fuse together, as predicted by the Williston's law.

397

398 As in crurotarsans, major transitions in Avemetatarsalia are associated with the fusion first of the  
399 skull base, then the skull roof, and, finally, with the face (more details on Table S6). This is more  
400 similar to the temporal pattern of sutural closure during ontogeny in the emu (skull base first,  
401 skull roof second, facial third) than to the one observed in the alligator (cranial first, skull base  
402 second, facial third)<sup>69</sup>, thus suggesting that the same mechanism for ontogeny may have been co-  
403 opted in Avemetatarsalia evolution.

404

#### 405 **Ontogenetic differences in topology between birds and crocodilians**

406 Our comparisons on network anatomy found that juvenile birds occupy a region of the  
407 morphospace that is closer to the less derived archosaurs and crurotarsans than to that occupied  
408 by adult modern birds (Fig. S1B). Juvenile birds have a degree of anisomerism of skull bones and  
409 skull anatomical complexity closer to that in crurotarsans and non-avian dinosaurs, while their  
410 pattern of integration overlaps with that of adult birds, crurotarsans, and non-avian dinosaurs.

411 These similarities in complexity and heterogeneity may be explained by the comparably higher  
412 number and symmetrical spatial arrangements of circumorbital ossification centres in early  
413 embryonic stages<sup>74</sup>. For example, both crown avians and *A. mississippiensis* have two ossification  
414 centres that fuse into one for lacrimals<sup>74,90</sup>. Meanwhile, ossification centres that form the  
415 prefrontal and postorbital, fuse in prenatal birds but remain separate in adult non-avian  
416 dinosaurs<sup>74,90,91</sup>. These ossification centres later develop into different, but overlapping, number of  
417 bones and their arrangement in juvenile birds (27 – 34 bones) and adult non-avian theropods (32  
418 – 44 bones) with discrepancies explained by the heterochronic fusion of the ossification centres  
419 (Table S8).

420

421 Following postnatal fusions and growth, modern bird skulls become more heterogeneous and  
422 their bones more connected and topologically closer to each other (Figs. 3C and 5; Table S8).  
423 This makes avian skull bones more diverse and functionally integrated. Simultaneously, skull

424 topology in birds diversifies with ontogeny within their lineage, as shown by the ontogenetic  
425 trajectories of *Gallus*, *Nothura*, and *Geospiza* (Figs. 3C and 5). Thus, bones (1) develop from  
426 ossification centres shared among crurotarsans and avemetatarsalians, (2) interact as modules  
427 with heterogeneity and complexity similar to basal members at juvenile stage, and (3) then fuse  
428 and diversify to produce skulls of adult birds.

429

430 The skulls of birds, crocodilians, and dinosaurs develop from ossification centres with  
431 comparable spatial locations in the embryonic head<sup>74</sup>. When both evolutionary and ontogenetic  
432 cranial shape variation was compared among crocodilians, Morris and colleagues showed that at  
433 mid- to late embryonic stages, cranial shapes originated from a conserved region of skull shape  
434 morphospace<sup>92</sup>. They suggested that crocodilian skull morphogenesis at early and late embryonic  
435 stages are controlled by signaling molecules that are important in other amniotes as well, such as  
436 *Bmp4*, *calmodulin*, *Sonic hedgehog* (*Shh*); and *Indian hedgehog*<sup>92–99</sup>. Then, from late prenatal  
437 stages onward, snout of crocodilians narrows<sup>100</sup> and elongates following different ontogenetic  
438 trajectories to give the full spectrum of crocodilian cranial diversity<sup>92</sup>.

439

440 Another major transformation in archosaurian evolution is the origin of skulls of early and  
441 modern birds from the snouted theropods. This transition involved two significant heterochronic  
442 shifts<sup>34,101</sup>. First, avians evolved highly paedomorphic skull shapes compared to their ancestors by  
443 developmental truncation<sup>34</sup>. This was followed, by a peramorphic shift where primitively paired  
444 premaxillary bones fused and the resulting beak bone elongated to occupy much of the new avian  
445 face<sup>101</sup>. By comparison, the skull of *Alligator* undergoes extensive morphological change and  
446 closing of the interfrontal and interparietal sutures during embryogenesis is followed by the  
447 prolonged postnatal and maturation periods, with the lack of suture closure and even widening of  
448 some sutures<sup>102,103</sup>. Bailleul and colleagues suggested that mechanisms that inhibit suture closure,  
449 rather than bone resorption, cause the alligator sutures to remain open during ontogeny<sup>103</sup>.

450 Nevertheless, juvenile and adult alligators share the same cranial topology featuring similar  
451 module compositions and both occupy a region of morphospace close to *Crocodylus* (Figs. 4D  
452 and S10; Table S4 and S8). Such topological arrangement suggests that conserved molecular,  
453 cellular, and developmental genetic processes underlie skull composition and topology observed  
454 across crocodilians. Likewise, oviraptorid dinosaurs, as represented by *Citipati*, display their own  
455 unique skull shape and ontogenetic transformation<sup>34</sup>, while retaining a topology conserved with  
456 other theropods. Combined, this evidence suggests that developmental mechanisms controlling  
457 skull composition and interaction among skull elements are conserved among theropods.

458

459 The process of osteogenesis underlies the shape and topology of the bony skull. In chicken  
460 embryo, inhibition of FGF and WNT signaling pathways prevented fusion of the suture that  
461 separates the left and right premaxilla, disconnected the premaxilla-palatine articulation and  
462 changed their shapes giving the distal face a primitive snout-like appearance<sup>101</sup>. The site of bone  
463 fusion in experimental unfused, snout-like chicken premaxillae showed reduced expression of  
464 skeletal markers *Runx2*, *Osteopontin*, and the osteogenic marker *Col I*<sup>101</sup>, implying localized  
465 molecular mechanisms regulating suture closure and shape of individual cranial bones. Thus,  
466 changes in gene expression during craniofacial patterning in avians<sup>95,96,98,104–106</sup>, non-avian  
467 dinosaurs, and crocodilians<sup>92,101</sup> contribute to the clade-specific differences in skull anatomical  
468 organization resulting from the similar patterns of bone fusion of bones.

469

470 Finally, we observe some network modules where some bones within the same modules in  
471 juveniles will later fuse in adult birds, but not in *A. mississippiensis* (Supplementary Information  
472 5; Figs. 4E and S10, Table S4). For example, in *Nothura*, premaxilla, nasal, parasphenoid,  
473 pterygoid, vomer, and maxilla grouped in the same juvenile module will later fuse during  
474 formation of the upper beak in the adult. In *A. mississippiensis*, premaxilla, maxilla, nasal,  
475 lacrimal, prefrontal, jugal, frontal, and ectopterygoid are also in the same juvenile module, but

476 remain separate structures in adult. These findings suggest that bones within the same module  
477 may be more likely to fuse together in ontogeny but doing so is a lineage-specific feature.

478

479 Comparisons of juveniles and adults for extant birds and the alligator revealed ontogenetic  
480 changes linked to the evolution of the skull organization in archosaurs. Whereas the anatomical  
481 organization of the skull of juvenile alligators resembles that of adults, the anatomy of juvenile  
482 modern birds is closer to that of non-avian dinosaurs than to that of adult avians of the same  
483 species in terms of morphological complexity and anisomerism, probably due to the spatial  
484 arrangements of ossification centres at embryonic stages<sup>74,90,91</sup>. More specifically, the differences  
485 in skull organization between crown birds and non-avian dinosaurs could be explained by  
486 postnatal fusion of bones.

487

488

## 489 CONCLUSION

490

491 A network-based comparison of the cranial anatomy of archosaurs shows that differences within  
492 and among archosaurian clades are associated with an increase of anatomical complexity, a  
493 reduction in number of bones (as predicted by the Williston's Law), and an increase of  
494 anisomerism marked by bone fusion, for both crurotarsans and avemetatarsalians. Our findings  
495 indicate that the anatomical organization of the skull is controlled by developmental mechanisms  
496 that diversified across and within each lineage: heterotopic changes in craniofacial patterning  
497 genes, heterochronic prenatal fusion of ossification centres<sup>74,90,91</sup>, and lineage-specific postnatal  
498 fusion of sutures. Some of these mechanisms have been shown to be conserved in other tetrapods.  
499 For example, heterotopy of craniofacial patterning genes also took place between chick and mice  
500 embryos<sup>95,96,106</sup>. Hu and Marcucio showed that mouse frontonasal ectodermal zone could alter the  
501 development of the avian frontonasal process, suggesting a conserved mechanism for frontonasal

502 development in vertebrates<sup>96</sup>. Our findings illustrate how a comparative analysis of the  
503 anatomical organization of the skull can reveal both common and disparate patterns and processes  
504 determining skull evolution in vertebrates.

505

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516

## 517 **AUTHOR CONTRIBUTION**

518

519 HWL, BE-A, AA designed the study.

520 HWL coded network models.

521 HWL and BE-A wrote the R scripts and performed the analyses.

522 All authors discussed the results and wrote the manuscript.

523 **Conflict of Interest:** The authors declare no conflict of interest.

524

## 525 **Data Availability**

526 Data and R code are available at <https://figshare.com/s/80714fb9a06e886cd412>.

527

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788 **SUPPLEMENTARY MATERIALS**

789 Table S1. Variance distribution across principal components

790 Table S2. First and last occurrence dates used to calibrate phylogenetic tree

791 Table S3. Internal nodes used for the phylogenetic tree

792 Table S4. Composition of modules for each taxon

793 Table S5. Categories of archosaurs based on capabilities of flight

794 Table S6. List of major fusion of bones with other bones in archosaurs

795 Table S7. Variation explained by each parameter

796 Table S8. Topological network parameters measured for each taxon

797 Table S9. Network parameters categorized by diet

798 Table S10. Number of modules.

799 Fig. S1. First two PC of topological parameters for all taxa.

800 Fig. S2. Second and third PC of topological parameters for all taxa.

801 Fig. S3. First and third PC of topological parameters for all taxa.

802 Fig. S4. First two PC of topological parameters for all taxa excluding avians.

803 Fig. S5. Second and third PC of topological parameters for all taxa excluding avians.

804 Fig. S6. First and third PC of topological parameters for all taxa excluding avians.

805 Fig. S7. First two PC of topological parameters for all taxa excluding adult avians.

806 Fig. S8. Second and third PC of topological parameters for all taxa excluding adult avians.

807 Fig. S9. First and third PC of topological parameters for all taxa excluding adult avians.

808 Fig. S10. Node-based modules of archosaurs based on details listed on Table S4.

809 Supplementary Information 1 References and notes about the specimens used.

810 Supplementary Information 2 Comparison between network-modules and variational modules in

811 archosaurs.

812 Supplementary Information 3 Comparison of network parameters among Aves, Crurotarsi, and

813 non-avian Dinosauria.

814      Supplementary Information 4 Comparison based on diet.

815      Supplementary Information 5 Comparison of juvenile avian modules with adult avian bones.

816      Supplementary Information 6 Supplementary Reference

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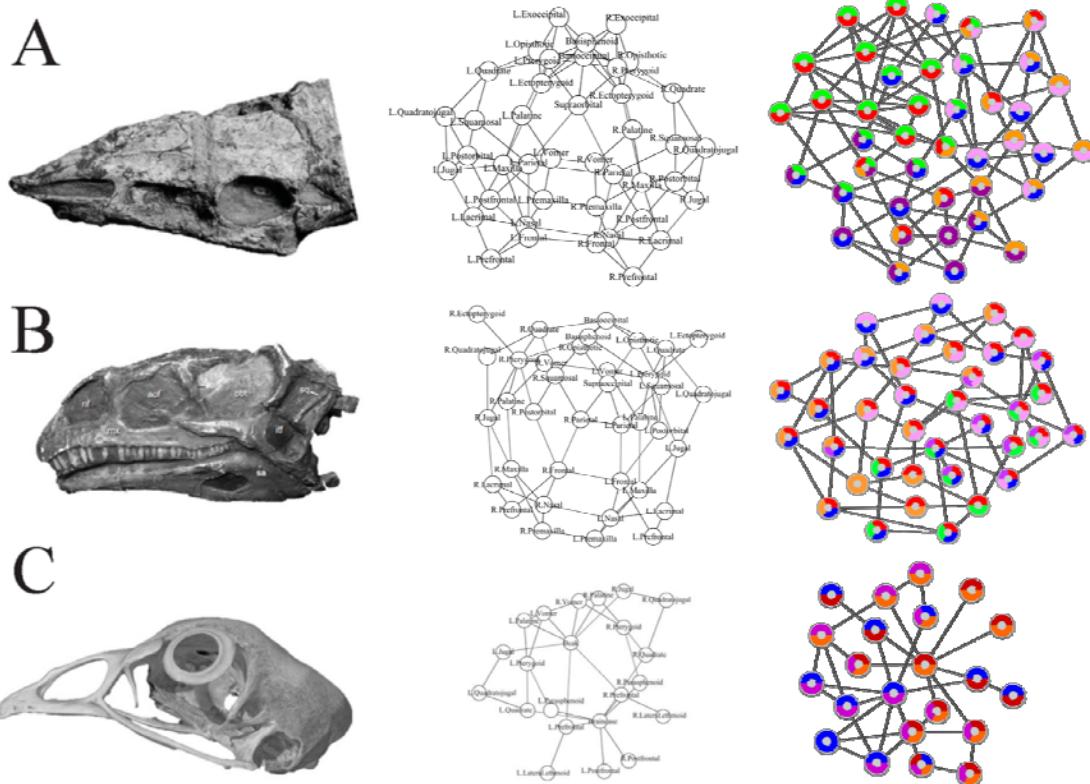
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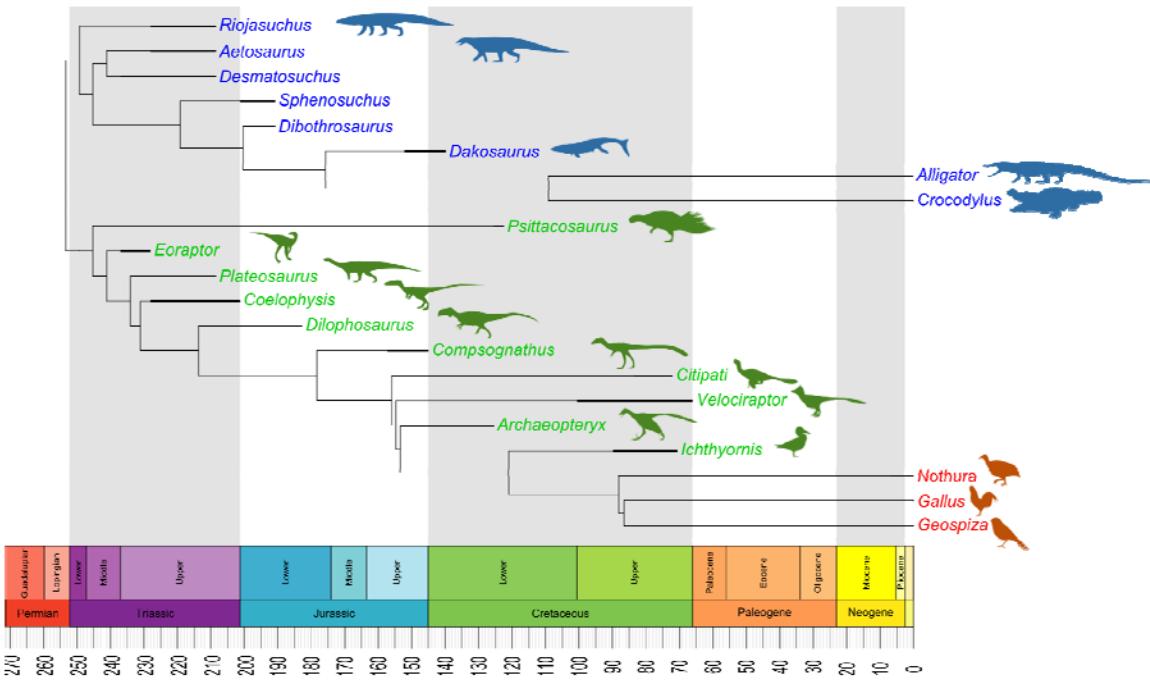
822 **FIGURE LEGENDS**



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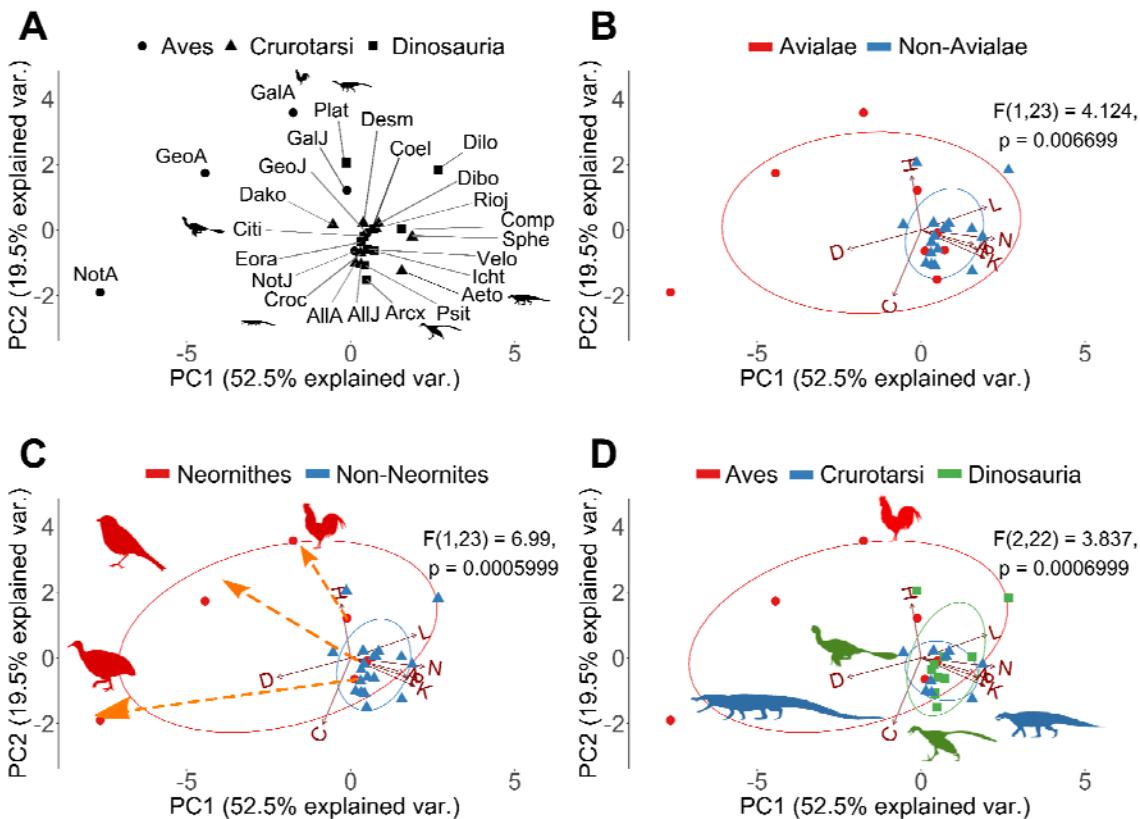
824 **Figure 1. Anatomical network models.** Example of the network models for three archosaurian  
825 skulls: (A) *Aetosaurus* from Schoch (2007)<sup>63</sup>; (B) *Plateosaurus* from Prieto-Marquez & Norell  
826 (2011)<sup>107</sup>; (C) *Gallus* from Digimorph. The pair-wise articulations among the bones of skulls (left)  
827 are formalized as network models (middle) and later analyzed, for example, to identify the skull  
828 anatomical node-based modules (right). See methods for details.

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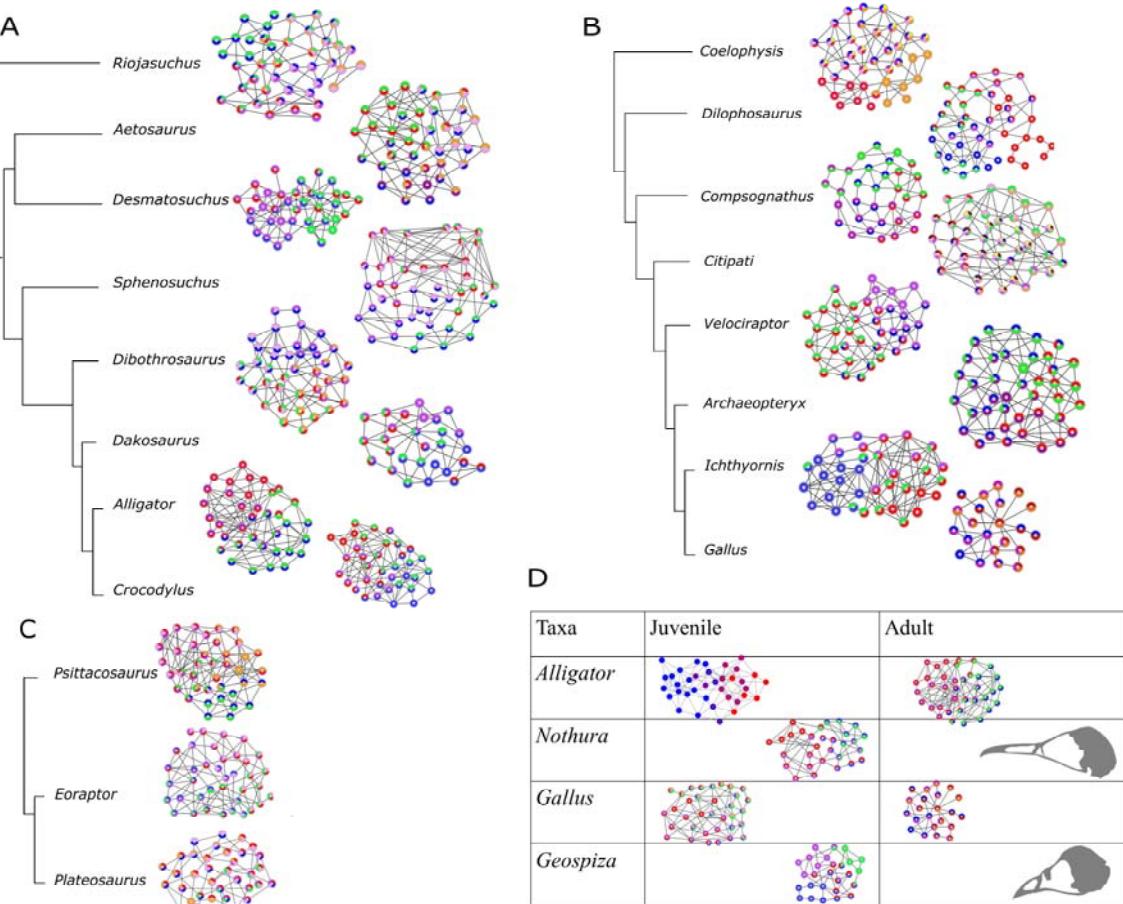
831 **Figure 2. Phylogenetic framework.** A phylogenetic tree was created based on the evolutionary  
832 relations among taxa as detailed in previous work<sup>34–43</sup>. Bifurcation times were calibrated based  
833 on fossil dates from Benton and Donoghue<sup>48</sup> using the equal method in the paleotree package<sup>45–47</sup>.  
834 First and last occurrences were from Paleobiology Database (details listed in Table S2).  
835 Silhouettes were from Phylopic.org. See methods for details.



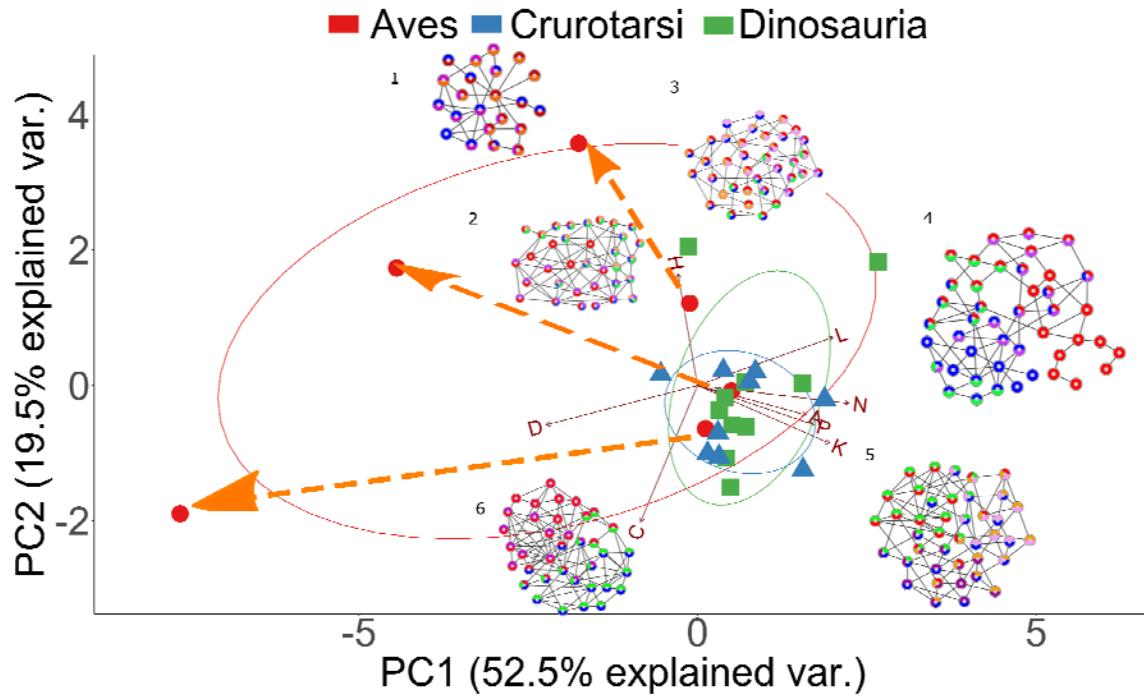
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837 **Figure 3. Principal components decomposition of topological variables.** (A) Skull distribution  
 838 for each taxon (see labels below). (B) Comparison of Avialae versus non-Avialae shows that non-  
 839 Avialae occupy part of the Avialae morphospace. (C) Comparison of Neornithes versus non-  
 840 Neornithes shows that non-Neornithes overlap with part of the Neornithes morphospace. Orange  
 841 dotted arrows show the ontogenetic change in modern birds from juvenile stage to adult stage. (D)  
 842 Comparison of Aves, Crurotarsi, and Dinosauria shows that they occupied different morphospace.  
 843 Ellipses show a normal distribution confidence interval around groups for comparison. Labels: N,  
 844 Number of nodes; K, Number of links; D, Density of Connection; C, Mean clustering coefficient;  
 845 H, Heterogeneity of connection; L, Mean path length; A, Assortativity of connection; P,  
 846 Parcellation. Aeto, *Aetosaurus*; AllA, adult *Alligator*; AllJ, juvenile *Alligator*; Arcx,  
 847 *Archaeopteryx*; Citi, *Citipati*; Coel, *Coelophysis*; Comp, *Compsognathus*; Croc, *Crocodylus*;  
 848 Dako, *Dakosaurus*; Desm, *Desmatosuchus*; Dibo, *Dibothrosuchus*; Dilo, *Dilophosaurus*; Eora,

849 *Eoraptor*; GalA, adult *Gallus*; GalJ, juvenile *Gallus*; GeoA, adult *Geospiza*; GeoJ, juvenile  
850 *Geospiza*; Icht, *Ichthyornis*; NotA, adult *Nothura*; NotJ, juvenile *Nothura*; Plat, *Plateosaurus*;  
851 Psit, *Psittacosaurus*; Rioj, *Riojasuchus*; Sphe, *Sphenosuchus*; Velo, *Velociraptor*. Silhouettes  
852 were from Phylopic.org.



853  
854 **Figure 4. Visualizations of the module composition changes across phylogeny.** The number of  
855 node-based modules ranged from 1 to 8. (C) shows the difference in module composition among  
856 the ornithischian *Psittacosaurus*, the basal saurischian *Eoraptor*, and the sauropodomorph  
857 *Plateosaurus*. (D) Comparisons of the adult and juvenile stages of extant species. Adult *Nothura*  
858 and *Geospiza* are shaded in grey as one module was identified because of the small number of  
859 nodes and links due to a highly fused skull. Nodes were colored based on their modules.  
860 Composition of each module is listed in Supplementary Table 4.



861

862 **Figure 5. Overview of the evolution of archosaurian skull topology:** Modern birds and few  
863 non-avian dinosaurs have more heterogeneous connections than crurotarsans; extant taxa have  
864 fewer bones and articulations than the extinct ones; bones in juvenile modern birds fuse and  
865 produce a more densely connected adult skull. Modules and networks of the following taxa are  
866 shown: (1) *Gallus*, (2) juvenile *Gallus*, (3) *Plateosaurus*, (4) *Dilophosaurus*, (5) *Aetosaurus*, (6)  
867 adult *Alligator*. Morphospace of Aves is significantly different from Crurotarsi and Dinosauria  
868 when adult birds are included. Orange arrows show the ontogenetic changes from juvenile to  
869 adult stages in neornithes. Taxa on the left side of the biplot have higher density and fewer bones,  
870 such as *Gallus* and *Alligator*, than taxa on the right, such as *Aetosaurus* and *Dilophosaurus*.

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