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3 **Emergence of Non-Linear Mixed Selectivity in Prefrontal Cortex after Training**

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35 **ABSTRACT**

36

37 Neurons in the prefrontal cortex (PFC) are typically activated by different cognitive  
38 tasks, and also by different stimuli and abstract variables within these tasks. A single  
39 neuron's selectivity for a given stimulus dimension often changes depending on its  
40 context, a phenomenon known as nonlinear mixed selectivity (NMS). It has previously  
41 been hypothesized that NMS emerges as a result of training to perform tasks in different  
42 contexts. We tested this hypothesis directly by examining the neuronal responses of  
43 different PFC areas before and after monkeys were trained to perform different working  
44 memory tasks involving visual stimulus locations and/or shapes. We found that training  
45 induces a modest increase in the proportion of PFC neurons with NMS exclusively for  
46 spatial working memory, but not shape working memory tasks, with area 9/46  
47 undergoing the most significant increase in NMS cell proportion. We also found that  
48 increased working memory task complexity, in the form of simultaneously storing  
49 location and shape combinations, does not increase the degree of NMS for stimulus shape  
50 with other task variables. Lastly, in contrast to the previous studies, we did not find  
51 evidence that NMS is predictive of task performance. Our results thus provide critical  
52 insights on the representation of stimuli and task information in neuronal populations,  
53 which may pave the way to a greater understanding of neural selectivity in working  
54 memory.

55

56 **SIGNIFICANCE STATEMENT**

57

58 How multiple types of information are represented in working memory remains a  
59 complex computational problem. It has been hypothesized that nonlinear mixed  
60 selectivity allows neurons to efficiently encode multiple stimuli in different contexts,  
61 after subjects have been trained in complex tasks. Our analysis of prefrontal recordings  
62 obtained before and after training monkeys to perform working memory tasks only  
63 partially agreed with this prediction, in that nonlinear mixed selectivity emerged for  
64 spatial but not shape information, and mostly in mid-dorsal PFC. Nonlinear mixed  
65 selectivity also displayed little modulation across either task complexity or correct  
66 performance. These results point to other mechanisms, in addition to nonlinear mixed  
67 selectivity, to represent complex information about stimulus and context in neuronal  
68 activity.

69 **INTRODUCTION**

70

71 Working memory (WM) is broadly defined as the ability to encode, maintain, and  
72 manipulate information in the conscious mind over a period of seconds without the  
73 presence of any sensory inputs. As a core component of complex cognitive abilities such  
74 as planning and reasoning, the true importance of WM ultimately depends on whether it  
75 can maintain and manipulate task relevant information in a task relevant manner  
76 (Baddeley, 2012). Multiple variables, including external sensory inputs and internal task  
77 requirements, must be encoded in order to achieve the level of adaptability in WM that is  
78 necessary for complex tasks. The mechanisms that underlie this encoding process across  
79 time and neuronal population is one of the most important questions in current WM  
80 research.

81 When individuals are required to maintain objects in their WM, neurons from a  
82 network of brain regions may exhibit selective and sustained increases or decreases in  
83 their activity in order to represent the remembered objects through these unique patterns  
84 of activity (Constantinidis and Procyk, 2004). The prefrontal cortex (PFC) plays a leading  
85 role in this network, and by extension, in the use of WM (Riley and Constantinidis,  
86 2016). For example, when the PFC is damaged or degraded, whether through trauma,  
87 illness, or experimental lesions, performance in WM tasks seems to decrease dramatically  
88 (Curtis and D'Esposito, 2004; Morris and Baddeley, 1988; Rossi et al., 2007).

89 Individual PFC neurons typically encode more than one variables, and the exact  
90 variables encoded are task dependent (Asaad et al., 2000; Machens et al., 2010; Mansouri  
91 et al., 2006; Qi et al., 2015; Warden and Miller, 2010). More interestingly, a portion of

92 neurons exhibit nonlinear mixed selectivity (NMS) for different variables, which means  
93 that their response to the combination of variables cannot be predicted by the linear  
94 summation of their responses to single variables (Johnston et al., 2020; Parthasarathy et  
95 al., 2017; Rigotti et al., 2013). Theoretical studies have shown that NMS is useful for  
96 linear readouts of flexible, arbitrary combinations of variables (Buonomano and Maass,  
97 2009; Fusi et al., 2016; Rigotti et al., 2010), and may also control the trade-off between  
98 discrimination and generalization (Barak et al., 2013; Johnston et al., 2020).

99 Despite the proposed importance of NMS on theoretical grounds, some  
100 experimental studies have failed to detect neurons with NMS (Cavanagh et al., 2018). It  
101 is therefore possible that NMS may manifest exclusively in a limited set of PFC  
102 subdivisions or alternatively, that NMS emerges exclusively after training to perform  
103 specific types of cognitive tasks. Moreover, the implications of NMS on other aspects of  
104 neural encoding, such as code stability, have not yet been investigated. We were therefore  
105 motivated to analyze and compare neural data from rhesus macaque monkeys before and  
106 after training. Here we report results of NMS as a function of task training, performance  
107 of different types of working memory tasks, and correct and error trials, across different  
108 prefrontal areas.

109 **METHODS**

110

111 Animals: Data obtained from six male rhesus monkeys (*Macaca mulatta*), age 5–9 years  
112 old, weighing 5–12 kg, as previously documented (Riley et al., 2018), were analyzed in  
113 this study. None of the animals had any prior experimentation experience at the onset of  
114 our study. Monkeys were either single-housed or pair-housed in communal rooms with  
115 sensory interactions with other monkeys. All experimental procedures followed  
116 guidelines set by the U.S. Public Health Service Policy on Humane Care and Use of  
117 Laboratory Animals and the National Research Council’s Guide for the Care and Use of  
118 Laboratory Animals and were reviewed and approved by the Wake Forest University  
119 Institutional Animal Care and Use Committee.

120

121 Experimental setup: Monkeys sat with their head fixed in a primate chair while viewing a  
122 monitor positioned 68 cm away from their eyes with dim ambient illumination. Animals  
123 were required to fixate on a 0.2° white square appearing in the center of the screen.  
124 During each trial, the animals maintained fixation on the square while visual stimuli were  
125 presented either at a peripheral location or over the fovea in order to receive a juice  
126 reward. Any break of fixation immediately terminated the trial and no reward was given.  
127 Eye position was monitored throughout the trial using a non-invasive, infrared eye  
128 position scanning system (model RK-716; ISCAN, Burlington, MA). The system  
129 achieved a < 0.3° resolution around the center of vision. Eye position was sampled at 240  
130 Hz, digitized and recorded. Visual stimuli display, monitoring of eye position, and the  
131 synchronization of stimuli with neurophysiological data were performed with in-house

132 software implemented on the MATLAB environment (Mathworks, Natick, MA), and  
133 utilizing the Psychophysics Toolbox (Meyer and Constantinidis, 2005).

134

135 Pre-training task: Following a brief period of fixation training and acclimation to the  
136 stimuli, monkeys were required to fixate on a center position while stimuli were  
137 displayed on the screen. The monkeys were rewarded for maintaining fixation during the  
138 trial with a liquid reward (fruit juice). The stimuli shown in the pre-training passive  
139 spatial task were white 2° squares, presented in one of nine possible locations arranged in  
140 a  $3 \times 3$  grid with 10° distance between adjacent stimuli. The stimuli shown in the pre-  
141 training passive feature task were white 2° circles, diamonds, H-letters, hashtags, plus  
142 signs, squares, triangles, or inverted Y-letters, also presented in one of nine possible  
143 locations arranged in a  $3 \times 3$  grid with 10° distance between adjacent stimuli.

144 Presentation began with a fixation interval of 1 s where only the fixation point  
145 was displayed, followed by a 500 ms of stimulus presentation (referred to hereafter as  
146 cue), followed by a 1.5 s “delay” interval (referred to hereafter as delay1) where, again,  
147 only the fixation point was displayed. A second stimulus (referred to hereafter as sample)  
148 was subsequently shown for 500 ms. In the spatial task, this second stimulus would be  
149 either identical in location to the initial stimulus, or diametrically opposite the first  
150 stimulus. In the feature task, this second stimulus would always be identical in location to  
151 the initial stimulus and would either be an identical shape or the corresponding non-  
152 match shape (each shape was paired with one non-match shape).

153

154 In both the spatial and feature task, this second stimulus display was followed by another  
155 “delay” period (referred to hereafter as delay2) of 1.5 s where only the fixation point was  
156 displayed. The location and identity of stimuli was of no behavioral relevance to the  
157 monkeys during the “pre-training” phase, as fixation was the only necessary action for  
158 obtaining reward.

159

160 Post-training task: Four of the six monkeys were trained to complete active spatial,  
161 feature and conjunction WM tasks. These active spatial and feature tasks were identical  
162 to the passive spatial and feature tasks that were applied during the “pre-training” phase,  
163 except that these tasks now required the monkeys to remember the spatial location or the  
164 shape feature of the first presented stimulus, and report whether the second stimulus  
165 matched the spatial location or shape feature of the first stimulus, respectively, via  
166 saccading to one of two target stimuli (green for match, blue for non-match). Each target  
167 stimulus could appear at one of two locations orthogonal to the cue/sample stimuli,  
168 pseudo-randomized in each trial.

169 The conjunction task combined the active spatial and feature tasks, and the stimuli  
170 shown were a white 2° circle, diamond, H-letter, hashtag, plus sign, square, triangle, or  
171 inverted Y-letter shapes, presented in one of nine possible locations arranged in a  $3 \times 3$   
172 grid with 10° distance between adjacent stimuli. Each trial consisted of a fixation interval  
173 of 1 s where only the fixation point was displayed, followed by 500 ms of the first  
174 stimulus presentation, followed by a 1.5 s delay interval where, again, only the fixation  
175 point was displayed. A second stimulus was subsequently shown for 500 ms, and after a  
176 second, 1.5 s delay period the monkeys would report whether the second stimulus

177 matched both the spatial location and shape feature of the first stimulus, via saccading to  
178 one of the two target stimuli. The conjunction task was therefore the most complex task,  
179 as the monkeys were required to simultaneously store two different items—location and  
180 shape—in their WM.

181

182 Surgery and neurophysiology: A 20 mm diameter craniotomy was performed over the  
183 PFC and a recording cylinder was implanted over the site. The location of the cylinder  
184 was visualized through anatomical magnetic resonance imaging (MRI) and stereotaxic  
185 coordinates post-surgery. For two of the four monkeys the recording cylinder was moved  
186 after an initial round of recordings in the post-training phase to sample an additional  
187 surface of the PFC.

188

189 Anatomical localization. Each monkey underwent an MRI scan prior to  
190 neurophysiological recordings. Electrode penetrations were mapped onto the cortical  
191 surface. We identified 6 lateral PFC regions: a posterior-dorsal region that included area  
192 8A, a mid-dorsal region that included area 8B and area 9/ 46, an anterior-dorsal region  
193 that included area 9 and area 46, a posterior-ventral region that included area 45, an  
194 anterior-ventral region that included area 47/12, and a frontopolar region that included  
195 area 10. However, the frontopolar region was not sampled sufficiently to be included in  
196 the present analyses.

197

198 In addition to comparisons between brain areas segmented in this fashion, other analyses  
199 were performed to account for the position of each neuron along the AP axis. For the

200 purposes of our analysis, we defined the AP axis as the line connecting the genu of the  
201 arcuate sulcus to the frontal pole. The recording coordinates of each neuron were  
202 projected onto this line, with position expressed as a proportion of the line's length.

203

204 Neuronal recordings: Neural recordings were carried out in areas 8, 9, 9/46, 45, 46, and  
205 47/12 of the PFC both before and after training in each WM task. Subsets of the data  
206 presented here were previously used to determine the collective properties of neurons in  
207 the dorsal and ventral PFC, as well as the properties of neurons before and after training  
208 in the posterior-dorsal, mid-dorsal, anterior-dorsal, posterior-ventral, and anterior-ventral  
209 PFC subdivisions. Extracellular recordings were performed with multiple  
210 microelectrodes that were either glass- or epoxylite-coated tungsten, with a 250  $\mu$ m  
211 diameter and 1–4 M $\Omega$  impedance at 1 kHz (Alpha-Omega Engineering, Nazareth, Israel).  
212 A Microdrive system (EPS drive, Alpha- Omega Engineering) advanced arrays of up to  
213 8-microelectrodes, spaced 0.2–1.5 mm apart, through the dura and into the PFC. The  
214 signal from each electrode was amplified and band-pass filtered between 500 Hz and 8  
215 kHz while being recorded with a modular data acquisition system (APM system, FHC,  
216 Bowdoin, ME). Waveforms that exceeded a user-defined threshold were sampled at 25  $\mu$ s  
217 resolution, digitized, and stored for off-line analysis. Neurons were sampled in an  
218 unbiased fashion, collecting data from all units isolated from our electrodes, with no  
219 regard to the response properties of the isolated neurons. A semi-automated cluster  
220 analysis relied on the KlustaKwik algorithm, which applied principal component analysis  
221 of the waveforms, to sort recorded spike waveforms into separate units. To ensure a  
222 stable firing rate in the analyzed recordings, we identified recordings in which a

223 significant effect of trial sequence was evident at the baseline firing rate (ANOVA,  $p <$   
224 0.05), e.g., due to a neuron disappearing or appearing during a run, as we were collecting  
225 data from multiple electrodes. Data from these sessions were truncated so that analysis  
226 was only performed on a range of trials with stable firing rate. Less than 10% of neurons  
227 were corrected in this way. Identical data collection procedures, recording equipment,  
228 and spike sorting algorithms were used before and after training in order to prevent any  
229 analytical confounds.

230

231 Data analysis: Data analysis was implemented with the MATLAB computational  
232 environment (Mathworks, Natick, MA), with additional statistic tests implemented  
233 through Originlab (OriginLab Corporation, Northampton, MA) and StatsDirect  
234 (StatsDirect Ltd. England). Peristimulus time histograms (PSTHs) for illustrations were  
235 calculated through the moving window average method with a Gaussian window that had  
236 a 200 ms standard deviation, with the shaded area indicating two times standard error  
237 cross trials. For all tasks, only cells with at least 12 correct trials for each cue-sample  
238 location/shape pairs were included in the analysis. To classify neurons of the spatial task  
239 into different categories of selectivity, we performed two-way ANOVAs on the spike  
240 count between either the stimuli location x matching status in for the trial, or between  
241 stimuli location x task epoch (first or second stimulus presentation). Neurons with classic  
242 selectivity (CS) exhibited a main effect of only one factor without significant interaction  
243 term. Neurons with linear mixed selectivity (LMS) exhibited main effects of both factors  
244 without significant interaction term. Neurons with NMS exhibited a significant  
245 interactions term. Finally, non-selective (NS) neurons exhibited no significant term for

246 both the main effects and the interaction term. Similarly, the two factors for feature task  
247 ANOVA analysis were stimuli shape x matching status, and stimuli shape x task epoch  
248 for the trial.

249 A method based on singular value decomposition (SVD) and cross validation was  
250 used to calculate population dimensionality for the spatial and feature tasks (Ahlheim and  
251 Love, 2018). The dimensionality of a matrix is defined as its number of non-zero singular  
252 values, identified by SVD. Under this condition however, the noise in the recorded neural  
253 data could potentially inflate the number of non-zero singular values, even if the true  
254 dimensionality were low. Reconstruction from components with cross-validation could  
255 be used to estimate dimensionality with noise, under the assumption that only true  
256 underlying dimensionality can contribute to the reconstruction performance in the cross-  
257 validation dataset. In short, data from  $j$  trials were randomly assigned to training the  
258 dataset with  $j-2$  trials, using one of the remaining trials for validation and the other for  
259 testing. SVD was then applied to the averaged training data to obtain all of the possible  
260 low-dimensional reconstructions, which were then correlated through a validation run.  
261 The dimensionality that produced the highest average correlation across  $j-1$  runs was  
262 selected as dimensionality estimate  $k$  for this fold, and a  $k$ -dimensional reconstruction  
263 was correlated with the held-out test data, resulting in the final reconstruction correlation.  
264 A similar method had also been recently used to estimate the dimensionality over time for  
265 neural data (Cueva et al., 2020). The dimensionality of the sample and delay2 period in  
266 the spatial and feature task was calculated on 50 resamples of a 200-cell pseudo-  
267 population in the corresponding datasets.

268 Only PFC areas with more than 50 cells in both pre- and post-training time points  
269 were included in the subdivision mixed selectivity comparison analysis. Thus, for the  
270 feature task, only data from the mid-dorsal, posterior-dorsal and posterior-ventral PFC  
271 were analyzed, while the spatial task analyzed data from the mid-dorsal, posterior-dorsal,  
272 posterior-ventral, anterior-dorsal and anterior-ventral PFC.

273 Neural data from tasks that applied the exact same visual stimuli were used to  
274 compare mixed selectivity between feature/spatial and conjunction tasks. For example, to  
275 compare the feature and the conjunction tasks, we started by selecting a subset of  
276 conjunction trials, in which both visual stimuli appeared at the same location as the  
277 corresponding feature task trials. Then, since all eight shapes were used in a single  
278 recording session for the feature task, a subset of trials, in which same shape pairs were  
279 used as the corresponding conjunction task, could be chosen as the feature dataset. Our  
280 prior methods of ANOVA analyses could thus be applied for comparison across these  
281 datasets.

282 For comparing mixed selectivity in success and error trials from the spatial task,  
283 we first examined two task variables—the stimuli location and matching status. In this  
284 analysis, we utilized neurons that had at least 3 match and non-match trials for both the  
285 correct and error dataset, in at least 3 stimuli locations. The number of minimum trials  
286 and stimuli locations were chosen to maximize the average trial number for each cell  
287 included into the analysis, while still retaining a sufficiently large sample (i.e. >150  
288 cells). The same number of trials from each stimuli location were randomly chosen in the  
289 correct and error dataset. This randomized trial selection process was repeated 50 times in  
290 order to make the best use of the uneven number of available trials in two datasets. We

291 also analyzed factors of stimuli location and task epoch. For this analysis, we used neural  
292 data from match trials only, and from neurons that had at least 4 correct and error trials,  
293 in at least 4 stimuli locations.

294 For decoding analysis, spiking responses from 1 second before cue onset to 5  
295 seconds after cue onset were first binned using a 400 ms wide window and 100 ms steps  
296 to create a spike count vector with a length of 57 elements. A pseudo-population was then  
297 constructed using the spike count vectors from all the available neurons of all the  
298 available animals, thus resulting in a dataset with 96 trials, as if they were recorded  
299 simultaneously. The population response matrix was z-score normalized before being  
300 used to train the decoder. A linear Support Vector Machine (SVM) decoding algorithm  
301 was implemented using the MATLAB fitcecoc function to decode stimuli location,  
302 stimuli shape, or the match/non-match status of trials. A 10-fold cross validation method  
303 was used to estimate the decoder performance and 20 random samplings were  
304 implemented to calculate a 95% confidence interval. For the location and feature task, the  
305 decoding baseline for sensory information was 12.5%, since there were 8 different  
306 options, and 50% for the matching status, since there were only 2 different options. In the  
307 pre-training vs post-training decoding analysis (Fig. 8), linear (CS and LMS) and  
308 nonlinear (NMS) neurons are first defined by their pre and post training responses in the  
309 sample or delay2 period. Each classified population was then applied to decode sensory  
310 information (location and shape) and matching status. A randomization test was used to  
311 determine the time points at which decoding performance was significantly different  
312 between different selectivity categories. In short, we constructed the null distribution by  
313 randomly reassigning the cell selectivity labels under comparison, and re-computing the

314 maximum absolute difference across all time points of the data in each iteration. This  
315 procedure was repeated for 5000 times. A difference was deemed to be significant if the  
316 true response difference occurred at the extremes of this null distribution ( $p < 0.05$ , two-  
317 tailed). Since every point in the null distribution is the maximum of all time points, this  
318 method already corrected for the multiple comparisons.

319 Only informative neurons (CS, LMS, and NMS neurons) in the delay2 period  
320 were used for the cross temporal decoding analysis (Fig. 7), since we wanted to explore  
321 the decoding dynamics during the delay period. The linear SVM decoder was trained on  
322 individual time points and thus had 57 linear decision boundaries. The same dataset was  
323 then classified by every decision boundary in the vector to produce a 57x57 matrix—a  
324 process that was repeated 20 times in order to eliminate the noise. The decoding  
325 performance matrix for each condition was normalized individually to highlight the  
326 coding dynamics rather than absolute performance.

327 Data availability: All relevant data and code will be available from the  
328 corresponding author on reasonable request. Matlab decoder code for figure 8 and 9 is  
329 available at <https://github.com/dwhzlh87/mixed-selectivity>

330 **RESULTS**

331

332 Extracellular neurophysiological recordings were collected from the lateral PFC of six  
333 monkeys before and after they were trained to perform the match/nonmatch WM tasks  
334 (Meyer et al., 2011; Riley et al., 2018). The task required them to view two stimuli  
335 appearing in sequence, with delay periods intervening between them, and to report  
336 whether or not the second stimulus was identical to the first. The two stimuli could differ  
337 in terms of their location (spatial task, Fig. 1A), shape (feature task, Fig. 1B), or both  
338 (conjunction task, Fig. 1C). If the second stimulus matched with the first, monkeys would  
339 saccade towards a green target during a subsequent interval, otherwise to a blue target at  
340 a diametrical location. A total of 1617 cells from six monkeys and 1495 cells from five  
341 monkeys were recorded while the animals were performing the passive spatial and  
342 feature tasks, respectively, which were mutually dubbed “pre-training.” A total of 1104  
343 cells from three monkeys and 1116 cells from two monkeys were collected while the  
344 animals were performing the active spatial and feature tasks, respectively, which were  
345 mutually dubbed “post-training”. We also collected neural data from 247 neurons for the  
346 passive spatial task from two monkeys after they were trained in the active spatial task.  
347 An additional 975 cells from two monkeys were collected while they were performing  
348 the active “post-training” conjunction task.

349

350 **Types of selectivity in individual neuronal responses**

351 In our tasks, the context of a given stimulus depends upon the task interval and sequence  
352 in which it is presented. We first considered how selectivity for stimulus location and

353 shape in the spatial, feature and conjunction WM tasks may vary when the same sample  
354 stimulus appears as a match (it is preceded by a cue at the same location/shape) or a  
355 nonmatch (i.e. is preceded by a cue stimulus of a different location/shape). The neuronal  
356 firing rate is therefore a function of the stimulus location/shape (eight shapes, eight  
357 locations arranged on a 3x3 grid with 10 degrees distance between stimuli, excluding the  
358 center location) and whether this sample stimulus matched the cue stimulus. We used a 2-  
359 way ANOVA with the factors of stimulus location/shape and match/nonmatch status to  
360 classify neurons into four categories of selectivity. CS neurons exhibited a significant  
361 main effect to only one of the factors (stimulus identity or matching status) and had no  
362 significant interaction term. In Fig. 2, the first exemplar displays a cell selective  
363 exclusively for the location of the stimuli, which does not respond differently regardless  
364 of whether the stimulus appeared as a match or nonmatch. The second exemplar of Fig. 2  
365 displays a cell not selective for the location of the stimuli but demonstrates higher mean  
366 response when the stimulus appeared as a non-match. LMS neurons exhibited a  
367 significant main effect for both factors but had no significant interaction term. The third  
368 exemplar of Fig. 2 displays a neuron demonstrating a higher mean response when stimuli  
369 appear as non-match, while simultaneously displaying the same rank order preference for  
370 location. NMS neurons exhibited a significant interaction effect, as shown in the last  
371 exemplar in Fig. 2, a neuron demonstrating different selectivity pattern for locations  
372 under match vs. non-match conditions. Finally, NS indicated the neurons with no  
373 selectivity to any factors or their interaction under consideration. These analyses were  
374 performed using the firing rate recorded during the stimulus presentation period, and  
375 again, using the firing rate recorded during the delay period that followed it.

376 A second type of NMS was identified in terms of selectivity for stimulus  
377 sequence, that is, whether the same stimulus appeared first (cue) or second (sample). To  
378 avoid the confound of the match or nonmatch status of the second stimulus, we relied  
379 exclusively on match stimuli. This form of NMS was also evaluated through a 2-way  
380 ANOVA model, identifying CS, LMS, NMS, and NS neurons in terms of how the  
381 neurons represented the exact same stimulus when it appeared as a cue and as a match  
382 stimulus.

383

384 **Effects of training on NMS**

385 When we used the factors of stimulus location/shape and match/nonmatch status for our  
386 two-way ANOVA, we found that training in the spatial WM task increased the proportion  
387 of NMS cells in both the sample period and the delay period that followed the sample  
388 (sample period: pre-training proportion=6.2%, post-training proportion=12.3%, two-  
389 sample proportion test,  $z=5.31$ ,  $p=1.13\times10^{-7}$ ; delay2 period: pre-training proportion=  
390 2.8%, post-training proportion=6.2%, two-sample proportion test,  $z=4.62$ ,  $p=4.86\times10^{-5}$ ).

391 However, this increase in selectivity was not exclusive to NMS cells. The proportion of  
392 CS cells also increased in the delay period following the sample (pre-training proportion=  
393 10.6%, post-training proportion=14.8%, two-sample proportion test,  $z=3.19$ ,  $p=0.0014$ ).

394 The increase in NMS cells was not evident for all types of training. When we  
395 looked at the proportion of change across the pre-training and post-training feature task,  
396 we only found an increase of proportion for CS cells (sample period: pre-training  
397 proportion= 12.0%, post-training proportion=15.7%, two-sample proportion test,  $z=2.65$ ,  
398  $p=0.0081$ ; delay2 period: pre-training proportion= 9.0%, post-training proportion=22.6%,

399 two-sample proportion test,  $z=9.37$ ,  $p=0$ ). No significant increase in the proportion of  
400 NMS cells was observed (sample period: pre-training proportion=5.8%, post-training  
401 proportion=6.7%, two-sample proportion test,  $z=1.01$ ,  $p=0.314$ ; delay2 period: pre-  
402 training proportion= 4.2%, post-training proportion=4.6%, two-sample proportion test,  
403  $z=0.522$ ,  $p=0.602$ ) (Fig. 3 A,B).

404 Similar results were observed when we used the factors of stimulus location/shape  
405 and task epoch (cue vs. match) for the two-way ANOVA instead (Fig. 3 C,D). For the  
406 spatial task, training increased the proportion of NMS cells, at least in the delay period  
407 (stimulus period: pre-training proportion= 5.7%, post-training proportion=7.4%, two-  
408 sample proportion test,  $z=1.78$ ,  $p=0.075$ ; delay period: pre-training proportion= 2.1%,  
409 post-training proportion=6.2%, two-sample proportion test,  $z=5.03$ ,  $p=4.94\times10^{-7}$ ). A  
410 similar increase was observed for the CS cells (stimulus period: pre-training proportion=  
411 21.3%, post-training proportion=25.3%, two-sample proportion test,  $z=2.37$ ,  $p=0.018$ ;  
412 delay period: pre-training proportion= 24.2%, post-training proportion=31.1%, two-  
413 sample proportion test,  $z=3.93$ ,  $p=8.53\times10^{-5}$ ). In the feature task, once again, only the  
414 proportion of CS cells changed (stimulus period: pre-training proportion= 21.9%, post-  
415 training proportion=32.6%, two-sample proportion test,  $z=6.05$ ,  $p=1.45\times10^{-9}$ ; delay  
416 period: pre-training proportion= 27.6%, post-training proportion=41%, two-sample  
417 proportion test,  $z=7.16$ ,  $p=8.32\times10^{-13}$ ). The proportion of NMS cells with an effect in the  
418 stimulus period remained relatively unchanged for the cue/match period (pre-training  
419 proportion= 3.4%, post-training proportion=4.7%, two-sample proportion test,  $z=1.59$ ,  
420  $p=0.112$ ), as well as the delay period (pre-training proportion= 2.4%, post-training  
421 proportion=3.8%, two-sample proportion test,  $z=1.95$ ,  $p=0.051$ ).

422 To further validate our proportional measure for NMS and compare our results to  
423 previous research on NMS in the PFC, we plotted the F scores for the interaction term  
424 (i.e. stimulus identity  $\times$  matching status) in both the spatial and the feature task (Fig. 4  
425 A). We found that this measure of NMS for individual cells increased specifically for the  
426 spatial task, indicated by much higher F score values after training for the spatial task.  
427 We also measured the dimensionality of population responses in the sample and delay2  
428 period for the spatial and feature task. Again, this analysis confirmed the results of our  
429 cell proportion measure (Fig. 4 B). For the spatial task, there was a significant increase of  
430 dimensionality after training (sample period: pre-training dimensionality= 5.72, post-  
431 training dimensionality=10.33, two-sample t test,  $t(98)=12.21$ ,  $p=2.18\times10^{-21}$ ; sample  
432 period: pre-training dimensionality= 3.25, post-training dimensionality=6.29, two-sample  
433 t test,  $t(98)=9.39$ ,  $p=2.51\times10^{-15}$ ). For the feature task however, no significance increase  
434 was observed in mean F score (Fig. 4A) or dimensionality (Fig 4B; sample period: pre-  
435 training dimensionality= 2.72, post-training dimensionality=2.73, two-sample t test,  
436  $t(98)=0.027$ ,  $p=0.978$ ; sample period: pre-training dimensionality= 2.43, post-training  
437 dimensionality=2.11, two-sample t test,  $t(98)=3.49$ ,  $p=7.29\times10^{-4}$ ).  
438

### 439 **Regional localization of NMS**

440 To assess whether specific sub-regions of the PFC may be specialized for NMS, we  
441 divided the lateral PFC into six regions (Fig. 5 A) and analyzed the respective  
442 neurophysiological data from five of these regions in order to determine the different  
443 areas' proportional contributions to the observed changes in NMS. We examined NMS  
444 defined by location/shape and match/nonmatch status in the sample period and ultimately

445 found that the mid-dorsal subdivision underwent the greatest proportional change in  
446 NMS cells for the spatial task after training (Fig. 5 C), without a comparable increase in  
447 the proportion of CS neurons (Mid-dorsal: CS 21.7% pre-training to 19.0% post- training,  
448 NMS 8.2% pre-training to 21.8% post-training). For the feature task however, the  
449 proportional change in NMS cells was relatively small, with moderate increases in CS  
450 and LMS observed in all three analyzed areas (Fig. 5 B).

451

#### 452 **NMS in task context**

453 Previous theoretical studies linked NMS with more flexible readouts of multiple task  
454 variables, thus leading to the hypothesis that task complexity may modulate NMS. To test  
455 this hypothesis, we compared the neural responses to different shapes at the same  
456 location when the stimuli appeared as match or nonmatch in the conjunction task, to the  
457 same neurons' responses to the same stimuli when they appeared in the feature task. In  
458 the conjunction task, animals needed to simultaneously remember both location and  
459 shape of visual stimuli, while in the feature task, they were only required to remember  
460 shape. Although the hypothesis predicted that the conjunction task would result in greater  
461 NMS than the feature task when the sensory stimuli was the same, this was not what we  
462 observed. No significant differences were observed for either CS cells (feature task  
463 sample proportion= 11.9%, conjunction task sample proportion=9.9%, exact matched  
464 pair sample proportion test , $F=1.229$ ,  $p=0.197$ , feature task delay2 proportion= 10.8%,  
465 conjunction task delay2 proportion=11.6%, exact matched pair delay2 proportion test  
466 , $F=1.069$ ,  $p=0.681$ ) or NMS cells (feature task sample proportion= 4.1%, conjunction  
467 task sample proportion=4.4%, exact matched pair sample proportion test,  $F=1.031$ ,

468 p=0.901, feature task delay2 proportion= 4.6%, conjunction task delay2  
469 proportion=5.9%, exact matched pair delay2 proportion test, F=1.278, p=0.266) (Fig. 6  
470 A) in the sample period or the delay2 period that followed. We also examined changes in  
471 individual cells' selectivity across the feature and conjunction tasks. Although this  
472 analysis was limited by the relatively low proportion of NMS cells in both tasks, we  
473 found an unstable mapping between tasks in the selectivity categories for both CS and  
474 NMS cells (Fig. 6 B), evidenced by the observation that most cells in CS and NMS  
475 category in the feature task changed their selectivity category in the conjunction task.  
476 There is a possibility, however, that the majority of the informative cells were simply due  
477 to chance (p=0.05 was used as threshold for detecting significant terms), which is  
478 enforced by the observation that NMS cells with larger degree of interaction in one task  
479 tend to also fall into the NMS category in the other task (Fig. 6 C). No significant  
480 difference was observed in the proportion of NMS cells when we performed a similar  
481 comparison between the spatial and conjunction task with a relatively small sample size  
482 (Fig. S1).

483 The comparison of the naïve and trained conditions allowed us to test the overall  
484 incidence of NMS in different populations of PFC neurons, sampled randomly before and  
485 after training, which was carried out over the course of several months. If NMS were  
486 critical for the representation of task-relevant information, we would expect a difference  
487 in the observed proportion of neurons with NMS, when animals are passively viewing  
488 stimuli vs. when they are actively performing the task and storing representations of the  
489 stimuli in their WM. We therefore applied a two-way ANOVA to compare the neural  
490 responses of neurons between the active and passive spatial tasks after the monkeys had

491 been trained to perform the active spatial task. We ultimately observed an increase in the  
492 proportion of cells that coded matching status during the sample period, as well as an  
493 increase in the proportion of cells coding sensory information in the delay1 period when  
494 the animal was prompted to report the matching decision. However, the observed  
495 increase in the proportion of NMS cells was not significant (passive proportion= 9.3%,  
496 active proportion=11.7%, exact matched pair proportion test,  $F=1.385$ ,  $p=0.362$ ) (Fig. 7  
497 A). Interestingly, a large proportion of cells changed their selectivity category across  
498 tasks, especially for CS cells (Fig. 7 B), and the degree of NMS does not seem to be  
499 predictive of whether a given neuron would fall in the same selectivity category in both  
500 tasks (Fig. 7 C).

501

## 502 **Information encoding by NMS neurons**

503 It is known that training leads to increased incorporation of task relevant information in  
504 neural populations, with relatively little change to stimulus information (confirmed in our  
505 dataset, Fig. S2). However, the relative contribution by NMS is not clear. To quantify the  
506 amount of task relevant information contained in linear (CS and LMS) and NMS cells,  
507 we used a linear SVM decoder to decode sensory information (location and shape) and  
508 match/or nonmatch status information. Since the cell selectivity category could be  
509 defined by their response in either sample or delay2 period, we randomly selected equal  
510 numbers of linear and nonlinear cells in both task epochs for each comparison. The  
511 random selecting process was repeated multiple times to obtain a confidence interval. We  
512 ultimately found that linear and nonlinear cells contain comparable amounts of linearly  
513 decodable information in regard to both sensory information and task relevant

514 information. The only observed difference between the decodable information in the  
515 linear and nonlinear cells occurred in the post training feature task, where linear cells  
516 were observed to contain more stimulus information in the sample period.

517 We also applied cross temporal decoding to compare classic and linear mixed  
518 cells in regard to population coding dynamics during the delay period. If information  
519 were represented by a stable pattern of activity, the classifier trained at one timepoint  
520 would be expected to work equally effectively at other time points where the information  
521 is present. Conversely, if information were represented by dynamic patterns of activity,  
522 then the decision boundary at one time point would not contribute to decoding  
523 information at other time points. The most prominent result from this analysis is that  
524 NMS cells produced significantly more stable code for matching spatial task information,  
525 compared to CS and LMS cells, as indicated by higher performance off the diagonal  
526 during the delay2 period (Fig. 9).

527

### 528 **NMS in correct and error trials**

529 The presence of decodable information in the PFC does not necessarily imply the  
530 presence of information in the conscious mind, and the representation of task relevant  
531 information is ultimately revealed by the ability to conduct the task successfully. In order  
532 to decipher the role of NMS, we examined the F score of the main effects and their  
533 interaction in the ANOVA test in correct vs. error trials for the spatial task (Fig. 10),  
534 which displayed higher NMS levels than the feature or conjunction tasks. Similar to the  
535 pre- vs. post training comparisons, we examined two types of mixed selectivity: stimulus  
536 location vs. matching status and stimulus identity vs. task epoch. The number of trials

537 and task variables were matched for each cell to avoid confounds in the comparison. The  
538 mean F score in correct trials for the location variable in the stimulus epochs for the  
539 location  $\times$  epoch comparison was equal to 1.86, while for the error trials the mean was  
540 2.59 (paired t test,  $t(147)=3.38$ ,  $p=9.42 \times 10^{-4}$  ). The effect extended into the delay  
541 epochs, where the average F score for location in correct trials was 1.43, and that of error  
542 trials was 1.79 (paired t test,  $t(150)=2.61$ ,  $p=0.010$  ). However, we did not find any  
543 differences in the F score for the interaction terms in any comparison. The results indicate  
544 that NMS may not be necessary in representing task relevant information in WM.

545 **DISCUSSION**

546

547 Selectivity for different types of information is critical in representing the plethora of  
548 stimuli and task contexts that can be maintained in WM. NMS is thought to be critical in  
549 that respect, as it allows efficient representation of flexible, arbitrary combinations of  
550 variables (Barak et al., 2013; Buonomano and Maass, 2009; Fusi et al., 2016; Johnston et  
551 al., 2020; Rigotti et al., 2010). Consistent with this idea, increased dimensionality in  
552 NMS has been highlighted as a potential means of increasing the efficiency of WM task  
553 performance (Johnston et al., 2020; Rigotti et al., 2013) and dimensional collapse  
554 characterizes task errors (Rigotti et al., 2013). Moreover, all task relevant information  
555 could be decoded from NMS neurons alone, despite their relative scarcity, with decoder  
556 accuracy actually increasing as the task became more complex (Rigotti et al., 2013).  
557 NMS is assumed to emerge with training in complex tasks that combine multiple types of  
558 information, or in multiple tasks, even without an explicit requirement to combine such  
559 information (Johnston et al., 2020; Lindsay et al., 2017). However, this idea has not been  
560 tested experimentally until now. Our study, by virtue of analyzing neural recordings  
561 before and after training in a series of cognitive tasks, directly tested these postulates. We  
562 found that NMS resulted in a modest increase with training, but only for some tasks, and  
563 furthermore, task complexity was not a predictor of NMS emergence. A causal  
564 relationship between success and dimensionality—and by extension, NMS—was also not  
565 supported by our results, as we did not observe any significant changes in NMS between  
566 error and success trials. These insights refine and qualify the role NMS plays in WM, and  
567 identify a number of open questions.

568

569 **Effects of training on neural responses**

570 WM is considerably plastic and at least some aspects of it, such as mental processing  
571 speed and the ability to multitask, can be improved with training (Bherer et al., 2008;  
572 Dux et al., 2009; Jaeggi et al., 2008; Klingberg et al., 2005; Klingberg et al., 2002). WM  
573 training has been proven particularly beneficial for clinical populations, e.g. in the case of  
574 traumatic brain injury, attention deficit hyperactivity disorder (ADHD), and  
575 schizophrenia (Klingberg et al., 2002; Subramaniam et al., 2012; Westerberg et al.,  
576 2007). However, the verdict of whether WM training confers tangible benefits on normal  
577 adults and whether these benefits transfer to untrained domains, remains a matter of  
578 heated debate. (Constantinidis and Klingberg, 2016; Cortese et al., 2015; Fukuda et al.,  
579 2010; Owen et al., 2010; Peijnenborgh et al., 2015; Schwaighofer et al., 2015).

580       This malleability of cognitive performance is thought to be mediated by the  
581 underlying plasticity in neural responses, most importantly within the PFC  
582 (Constantinidis and Klingberg, 2016). In a series of prior studies, we have investigated  
583 changes in PFC responsiveness and selectivity (Meyer et al., 2011; Meyers et al., 2012;  
584 Qi et al., 2011; Riley et al., 2018), as well as other aspects of neuronal discharges such as  
585 trial-to-trial variability and correlation between neurons (Qi and Constantinidis, 2012a,  
586 2012b). This led to our present analysis where—guided by experimental and theoretical  
587 predictions (Rigotti et al., 2013)—we examined NMS as another potential source of  
588 enhanced ability to represent WM information after training.

589

590           In agreement with our hypothesis, we found that training increased the proportion  
591           of neurons that exhibit NMS. However, training does not seem to be a prerequisite, as  
592           NMS was also observed in animals that were naïve to any cognitive training. Prior  
593           research has established that the human and primate PFC represent stimuli in memory  
594           even when not prompted to do so (Foster et al., 2017), or without training in WM tasks  
595           (Meyer et al., 2007). Our finding of NMS neurons in naïve monkeys provides another  
596           exemplar of that principle. However, NMS only increased for certain types of task  
597           information and not for others, thus suggesting that its role in the simultaneous  
598           representation of multiple types of information is not universal across tasks. These results  
599           stand in agreement with some prior studies, which have failed to uncover substantial  
600           NMS in the tasks they employed (Cavanagh et al., 2018). Examining where NMS failed  
601           to appear—and where WM representations fail to spontaneously appear—will be an  
602           important area of future investigation for NMS.

603           The greatest increase in the proportion of neurons that exhibited NMS for the  
604           spatial working memory task was observed at the mid-dorsal region during the sample  
605           presentation period (Fig. 5). This disproportionate increase in NMS neurons was  
606           associated with a modest decrease in neurons that exhibit CS, as predicted by theoretical  
607           studies (Lindsay et al., 2017). However, this finding, too did not generalize across  
608           conditions. During the delay periods of the spatial task, we saw an across-the-board  
609           increase in neurons with CS, which were much more abundant in the trained than the  
610           naïve PFC (Fig. 3). In fact, the increase in feature selectivity after training was driven  
611           almost exclusively by CS cells, suggesting a potential division of labor between NMS  
612           and CS in the PFC for different types of information.

613

614 **Task Complexity and Difficulty**

615 Another potential factor that determines the emergence of NMS is task complexity. NMS  
616 may arise exclusively in highly complex tasks that require subjects to maintain and  
617 combine multiple types of information in their WM, simplifying the involved neural  
618 circuits to achieve greater efficiency (Rigotti et al., 2013). We thus tested this concept by  
619 applying a dataset that relied on three tasks which differed in complexity (and overall  
620 difficulty). The spatial and feature tasks each required maintenance of a single stimulus  
621 property in memory (location or shape). The conjunction task required both. Surprisingly  
622 however, we did not observe a higher incidence of NMS in the conjunction task when  
623 compared to the feature task. Moreover, we observed a much lower incidence of NMS in  
624 the feature task compared to the spatial task despite the fact that the latter was no more  
625 complex or difficult for the monkeys to perform (Meyer et al., 2011; Riley et al., 2018).  
626 This implies that NMS in the PFC may not be necessary for certain types of information,  
627 like object shape, even when the task complexity is high. Alternatively, we may also  
628 consider the possibility that the increased NMS that results from training may be  
629 sufficient for the majority of behavioral requirements, without any additional increases  
630 required. Future research is therefore necessary to assess and examine all of these  
631 possibilities, and more.

632

633 **Regional Specialization**

634 Different types of information are represented across the dorso-ventral and anterior-  
635 posterior axes of the PFC (Constantinidis and Qi, 2018), and examining the regional

636 distribution of NMS neurons within the PFC therefore bears a clear importance. We  
637 found that NMS was most strongly demonstrated in the mid-dorsal area for the spatial  
638 task and the posterior dorsal area for the feature task. This pattern was generally  
639 consistent with the known distribution of neuronal selectivity for stimuli in the PFC  
640 (Riley et al., 2018).

641

#### 642 **Information Content and Task Performance**

643 A critical issue regarding the role of Mixed Selectivity is whether nonlinear match  
644 selectivity, by virtue of representing information more efficiently, is also more necessary  
645 for effective task performance (Rigotti et al., 2013). We relied on a linear SVM decoder  
646 to decipher the specific information that may be represented by NMS cells, compared to  
647 CS cells. In the current study, we found similar quantities of information could be  
648 decoded from (equal-sized) populations of CS and NMS neurons, though the coding  
649 dynamics for some types of information were significantly different between CS and  
650 NMS cells. Similarly, when we compared the NMS levels of successful and failed task  
651 trials, we were surprised to find that there was no appreciable difference. This suggests  
652 that loss of information encoded in a nonlinear manner is not the primary factor of  
653 successfully maintaining information in the conscious mind. An important caveat for this  
654 conclusion is that the combination of small and unbalanced number of error trials in  
655 match vs. nonmatch conditions make the detection power for the interaction fairly small  
656 in our analysis. Moreover, with very little NMS presented even in success trials after  
657 matching the trial number for the error condition, a floor effect may have prevented a  
658 further decline from becoming apparent. Nonetheless, our result reinforces the idea that

659 NMS is not necessary in all tasks, without which performance fails. An interesting  
660 observation in this analysis was that the proportion of cells tuned to spatial location was  
661 elevated in error trials. The result may imply that task success also depends on the task  
662 relevance of the represented information, with error trials incorporating greater quantities  
663 of task irrelevant spatial information and therefore unnecessarily drawing away WM  
664 resources without benefit. Ultimately, by comparing and evaluating the conditions in  
665 which NMS emerges, we may decipher its true role in WM and other cognitive functions.

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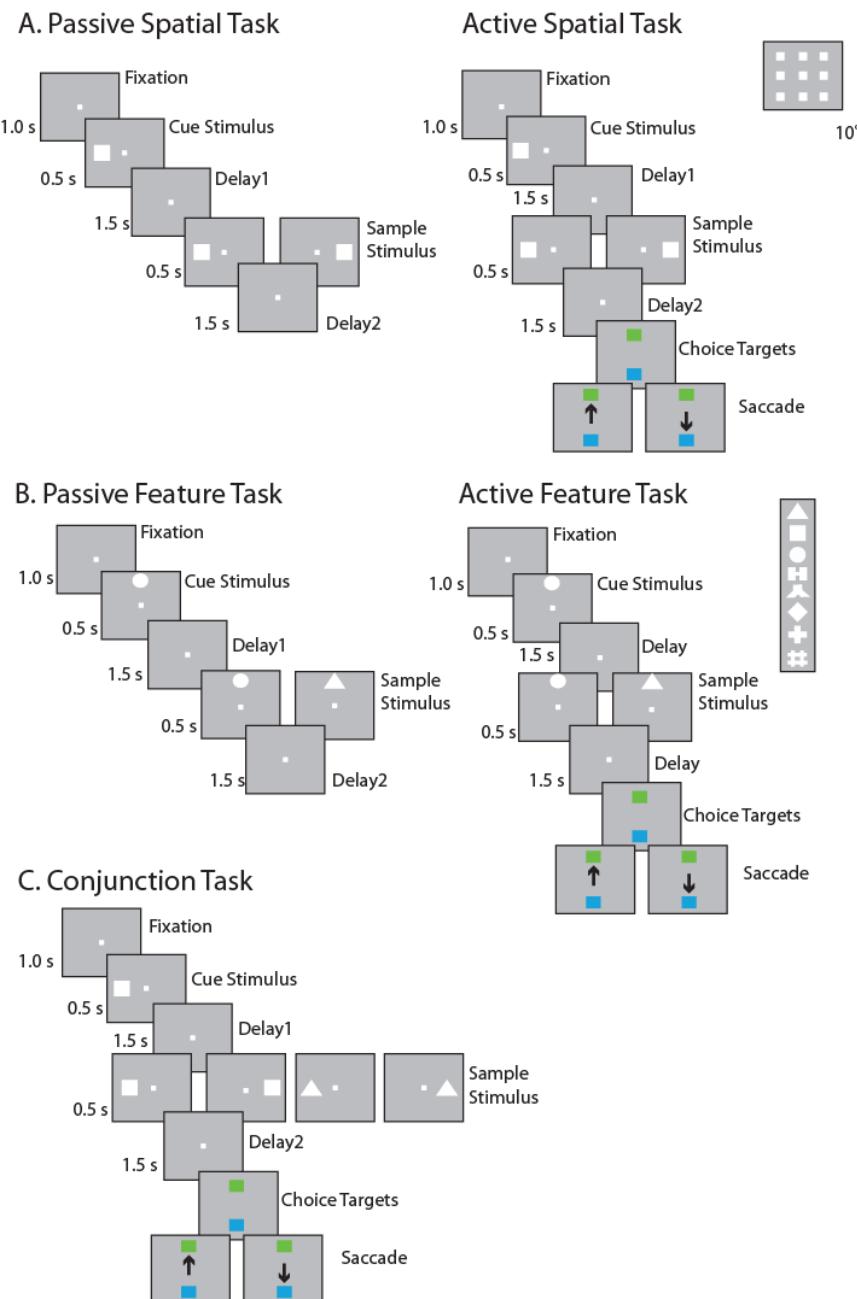
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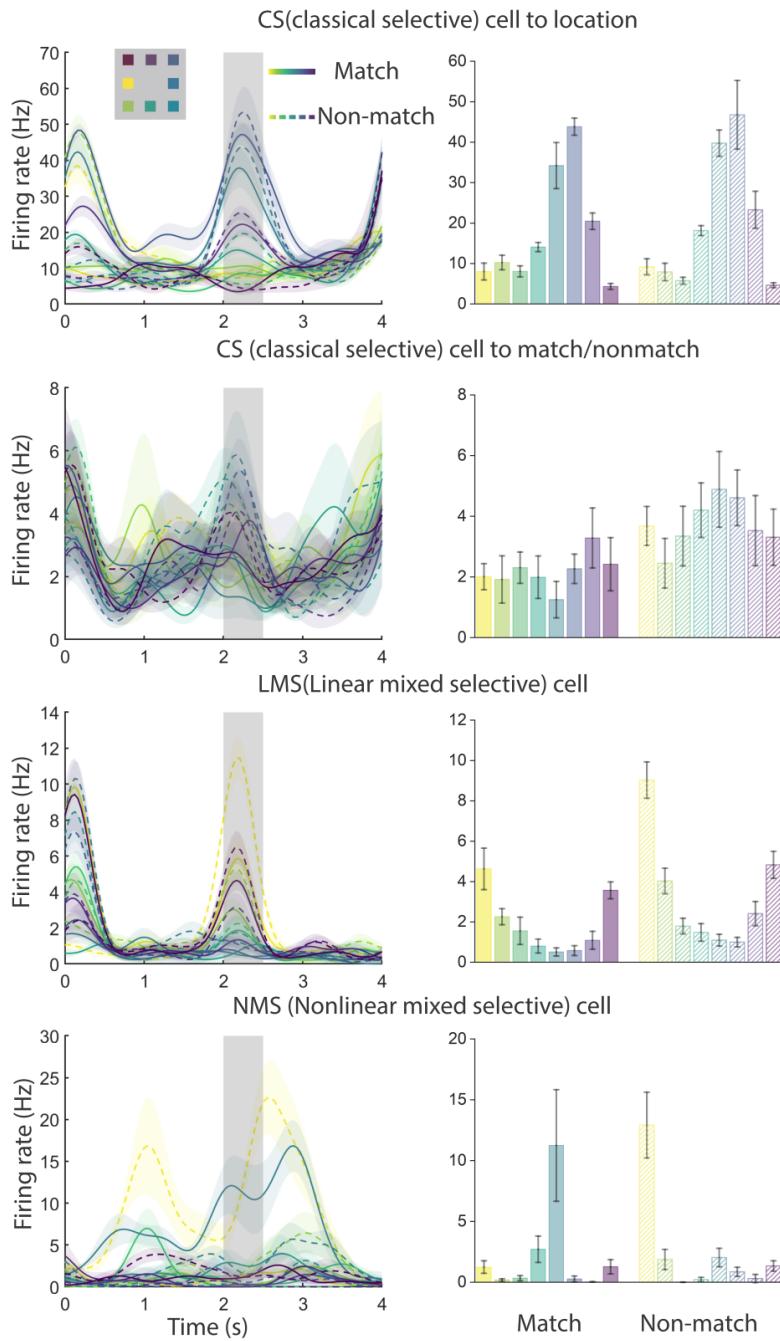
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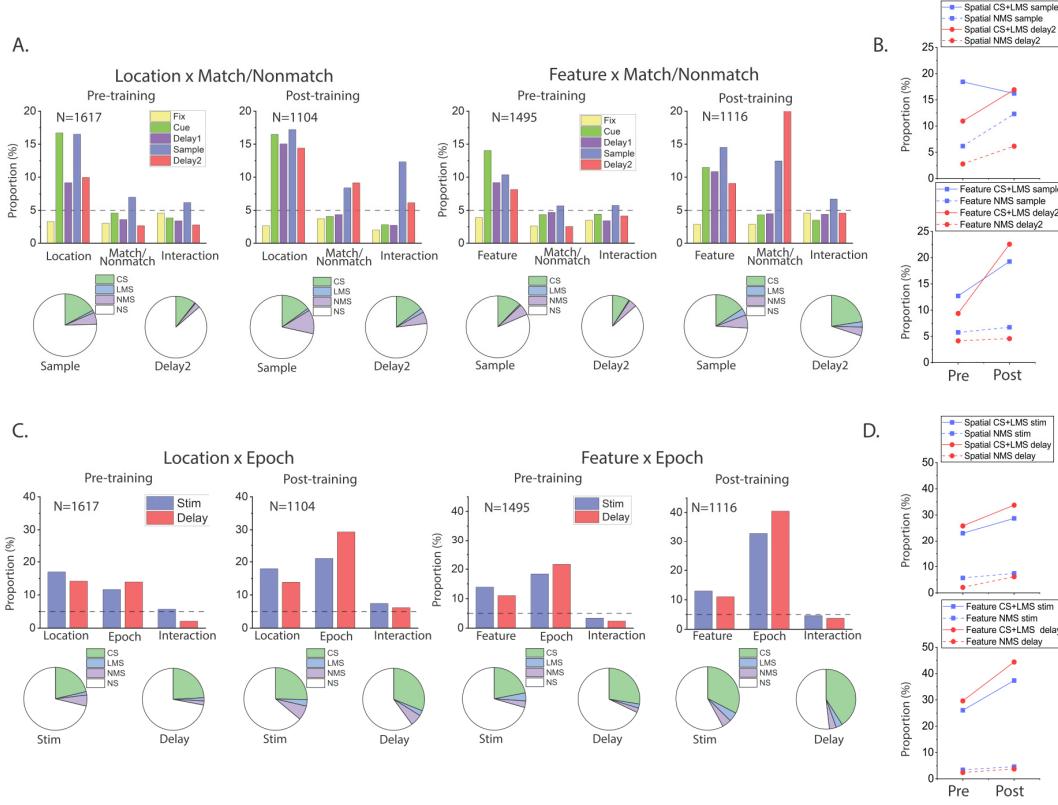
Figure 1. Task structure and stimuli used. The animals were required to maintain center fixation throughout both active and passive task trials. At the end of active tasks trials however, monkeys were required to make a saccade to a green target if the stimuli matched or to a blue target if the stimuli did not match. (A) Spatial location match-to-sample task, nine possible cue locations in a session shown in the inset. (B) Shape feature match-to-sample task, 8 possible shapes in a session shown in the inset. (C) Spatial-shape conjunction task, up to two locations and two stimuli shapes were used for any single particular session. Stimuli in all tasks extended 2 degree of visual angle.



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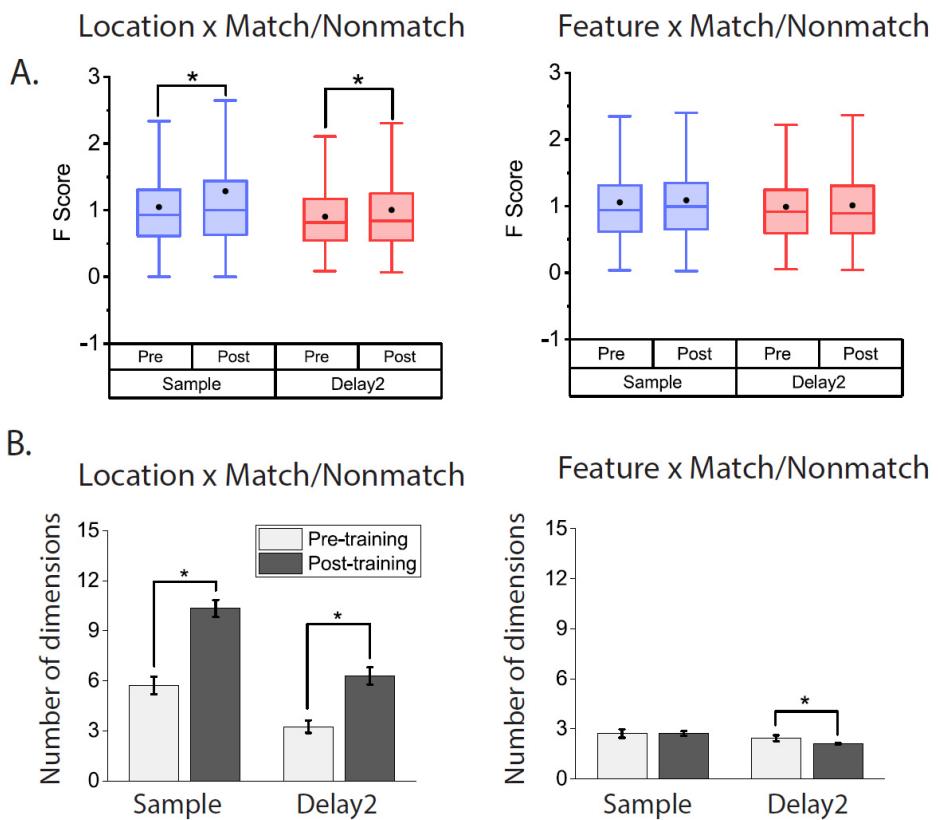
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795 Figure 2. Exemplar neural responses from the spatial task for CS (classical  
796 selective), LMS (linear mixed selective) and NMS (nonlinear mixed selective)  
797 cells, defined by the task variables of stimulus location and match status.  
798 Selectivity classification were based on the spike responses of the 500 ms  
799 sample period. The locations the stimuli were color coded, with a solid line/bar  
800 representing when the stimulus was a match with the cue, and a dash line/bar  
801 representing when the stimulus was a nonmatch with the cue. Shaded regions  
802 and error bar indicate 2 times SE of firing rate.



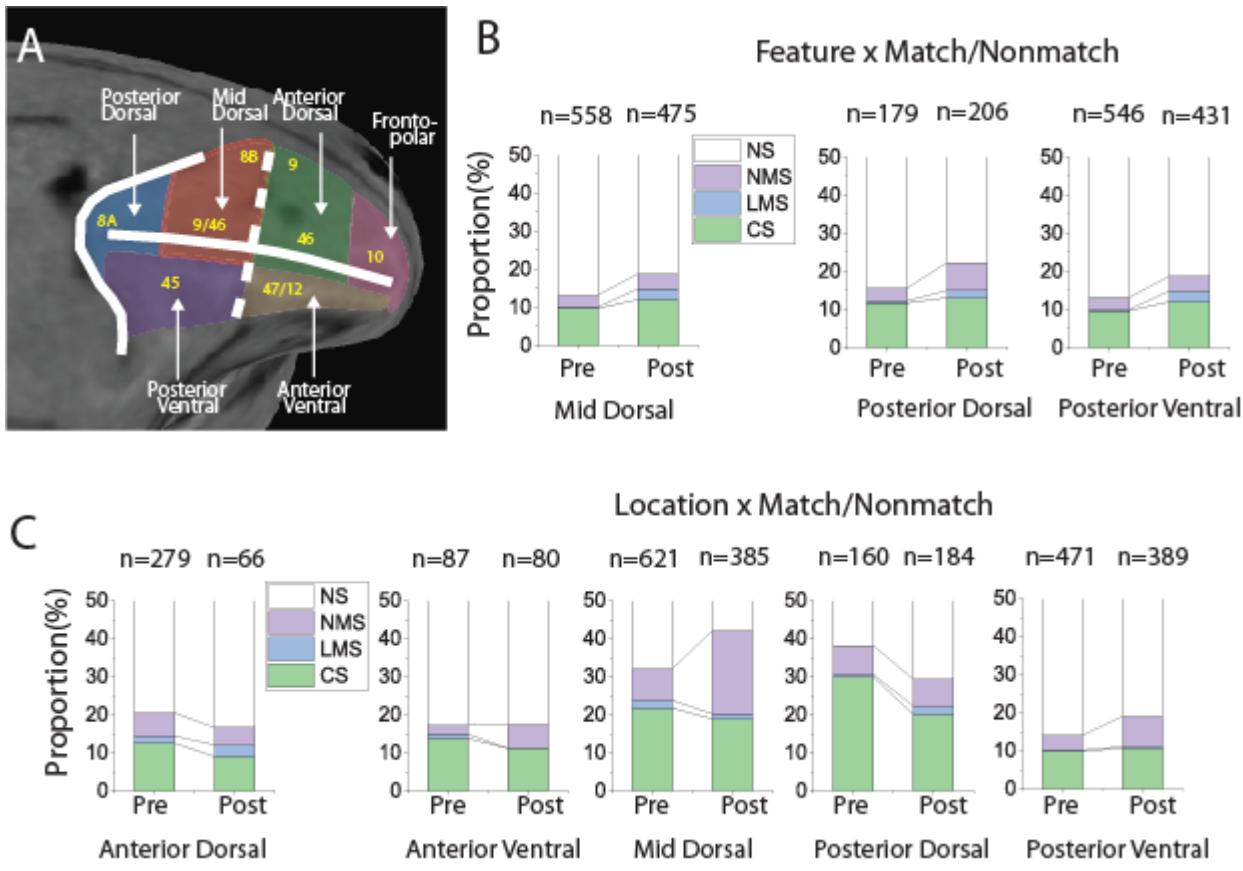
803  
804 **Figure 3. Training increased mixed selectivity preferentially in the spatial task. (A)**  
805 Bar graphs show the proportions of cells tuned to stimuli identities  
806 (Location/Shape), matching status and their interaction (i.e. NMS) in different  
807 stages of the task trials, both before and after the animals were trained for the  
808 active tasks. Pie charts show the proportion of different selectivity categories  
809 (NS, CS, LMS and NMS) in the sample and delay2 periods of both tasks, both  
810 before and after the animals were trained for the active tasks. (B) Plots of  
811 corresponding proportion changes. (C) Same as (A) but examining the  
812 interaction between stimuli identities (Location/Shape), and task epoch  
813 (cue/delay1 vs sample/delay2 period), instead of trials matching status. (D) Plots  
814 of corresponding proportion changes.  
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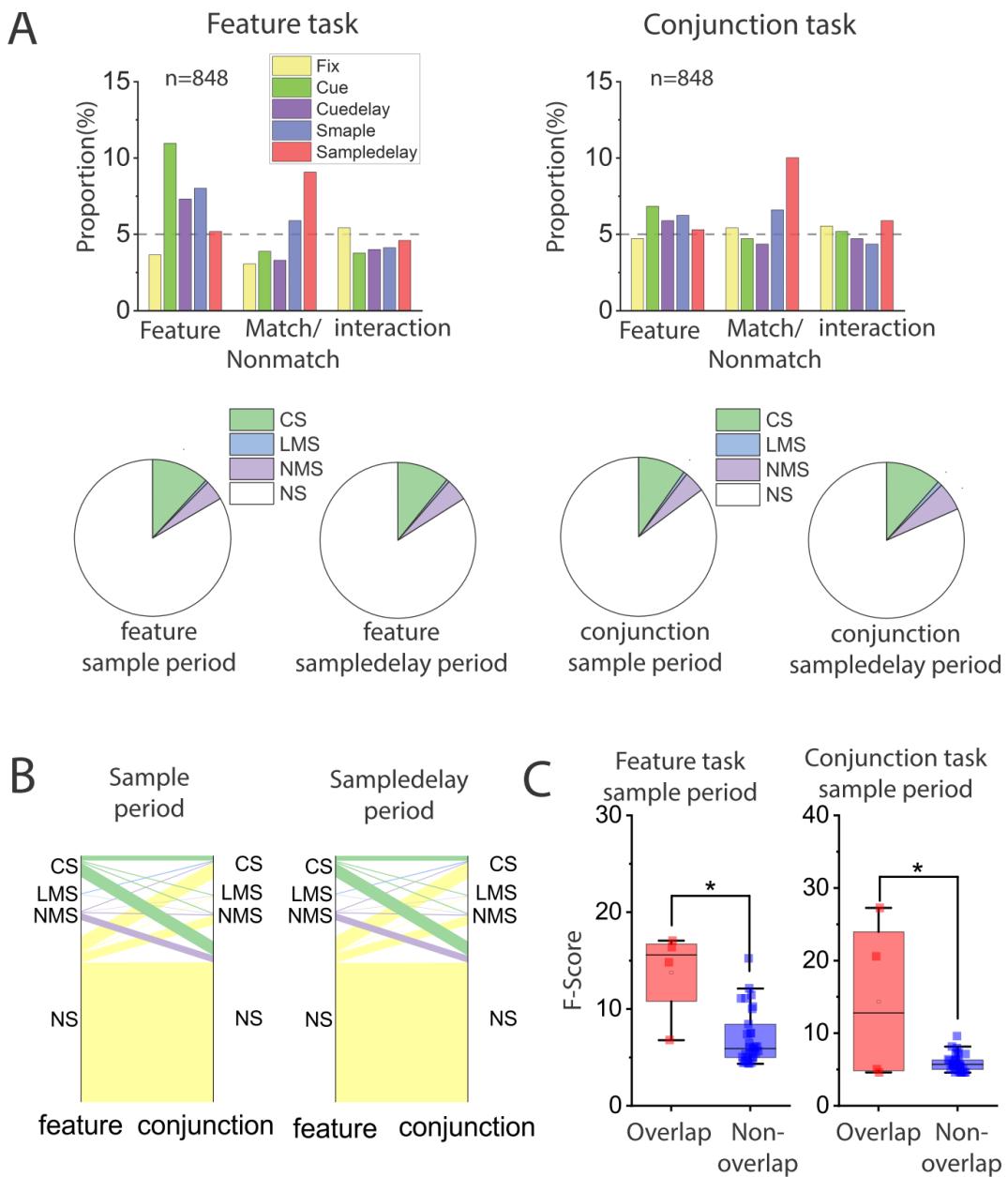
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819 Figure 4. (A) Analysis of F score for the interaction term (stimuli identity ×  
820 match/nonmatch) shows that the degree of mixed selectivity increased after  
821 training for the spatial task only. Black dots in the box represent mean, box  
822 boundaries indicate 25%-75% range, and whiskers represents 1.5 IQR. (B)  
823 Dimensionality measure of neural responses in the spatial (left) and feature  
824 (right) task, before and after training in the active tasks.



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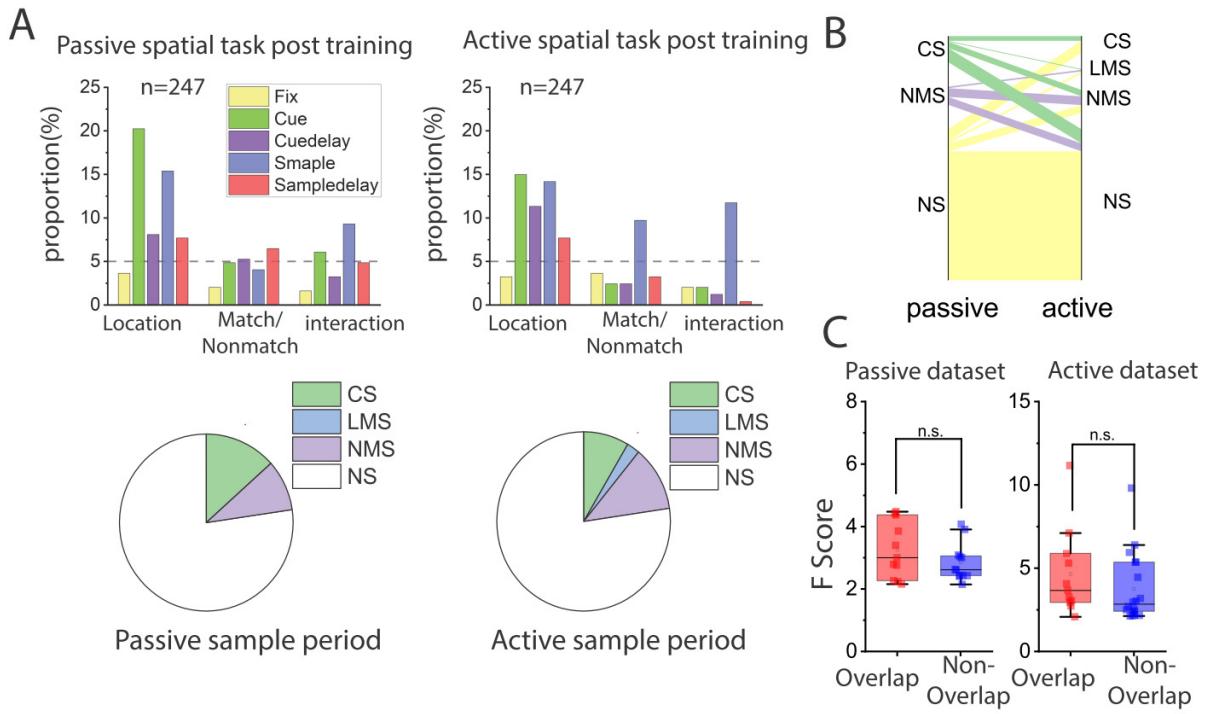
827 Figure 5. Cell selectivity changes by brain regions. (A) PFC subdivisions that  
828 were utilized for recording in the current study. (B) The effects of training in for  
829 the active feature task on the proportion of different selectivity categories (NS,  
830 CS, LMS and NMS) in the sample period. There were significant increases in the  
831 proportion of LMS cells in all three PFC regions included for analysis, but  
832 relatively low increases in the proportion of NMS cells. (C) The effects of training  
833 in the active spatial task on the proportion of different selectivity categories (NS,  
834 CS, LMS and NMS) in the sample period. The greatest increase in NMS  
835 occurred at the mid-dorsal region.



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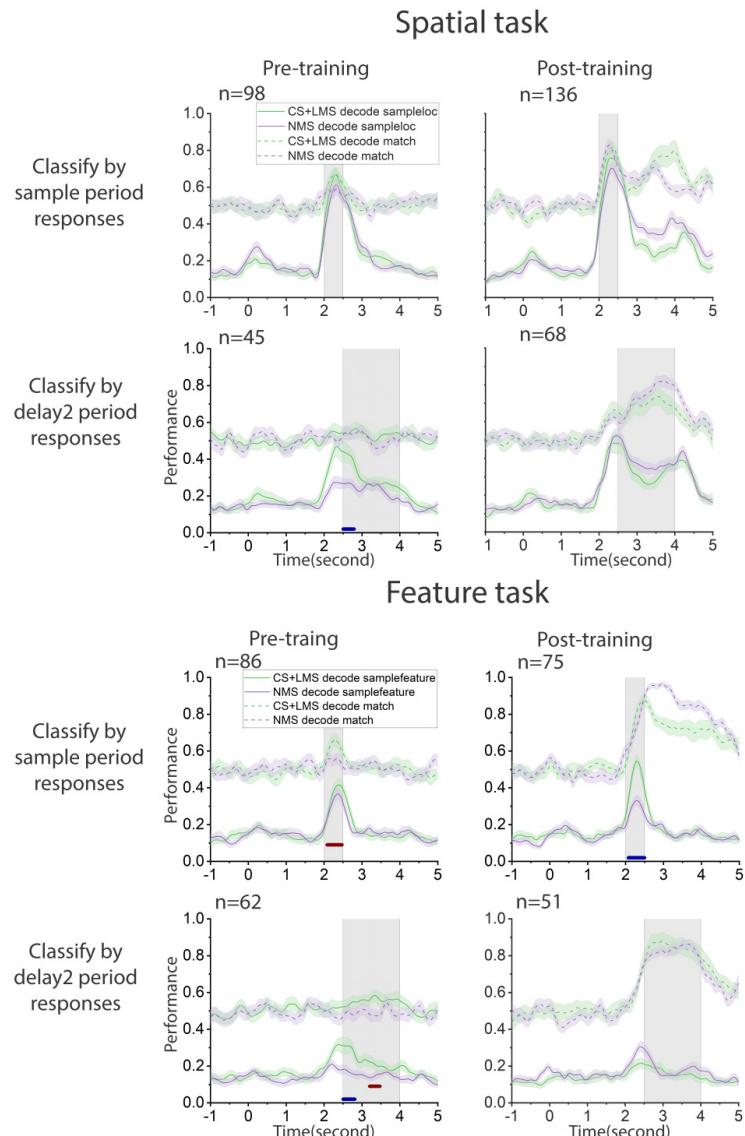
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Figure 6. Cell selectivity in tasks with different task complexity. Analyses were performed on neural data from the same population of cells, with matching numbers of trials in the feature and the conjunction tasks. Only trials with the same stimuli were included in this analysis. (A) Examining interaction (NMS) across stimulus preference and matching status. Bar graphs show the proportions of cells tuned to stimuli shape, trials matching status and their interaction in different stages of both the feature and conjunction tasks. Pie charts display the proportion of different selectivity categories (NS, CS, LMS and NMS) in corresponding sample and delay2 periods. (B) Cell selectivity category mapping cross tasks. (C) F scores of the interaction term in the ANOVA were compared between cells that were classified as NMS cell in both tasks (overlapping cells), and those only classified as NMS in one of the tasks (non-overlapping cells).

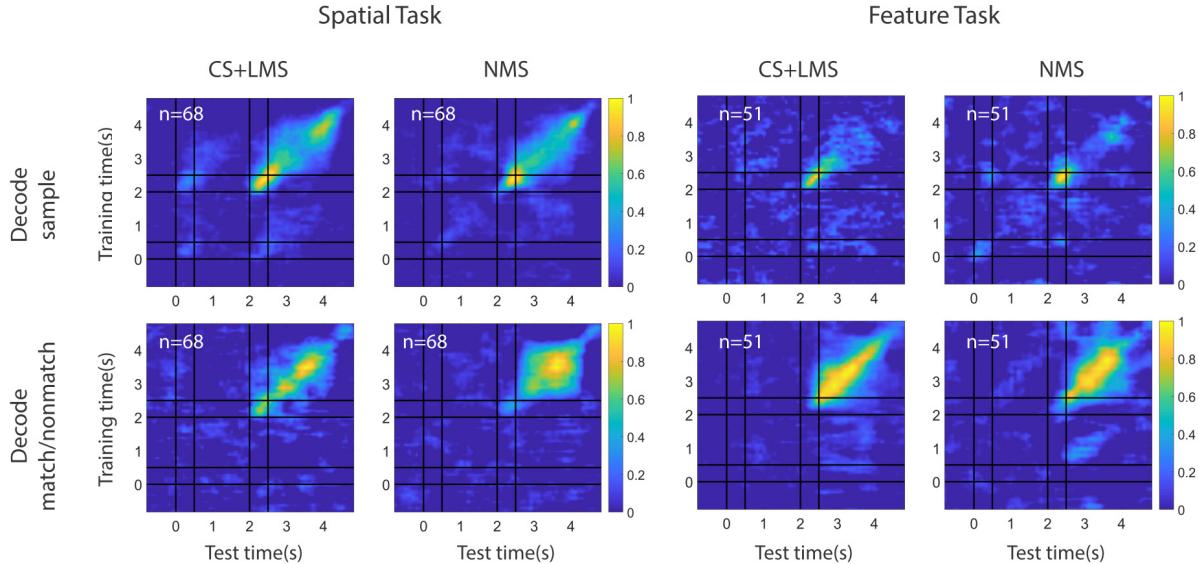


850

851 Figure 7. Cell selectivity in tasks with the same sensory input but different  
 852 behavioral requirements. Analyses were performed on neural data from the same  
 853 population of cells, with matching number of trials in the passive and active  
 854 spatial tasks. Only trials that had the exact same stimuli pairs in both tasks were  
 855 included in this analysis. (A) Examining interaction (NMS) between stimulus  
 856 preference and matching status. Bar graphs show the proportions of cells tuned  
 857 to stimuli location, trials matching status and their interaction in different stages of  
 858 the tasks. Pie charts display the proportion of different selectivity categories (NS,  
 859 CS, LMS and NMS) in the sample period. (B) Cell selectivity category mapping  
 860 across tasks in the sample period. (C) F scores of the interaction term in the  
 861 ANOVA were compared between cells that were classified as NMS cell in both  
 862 tasks (overlapping cells), and those only classified as NMS in one of the tasks  
 863 (non-overlapping cells).



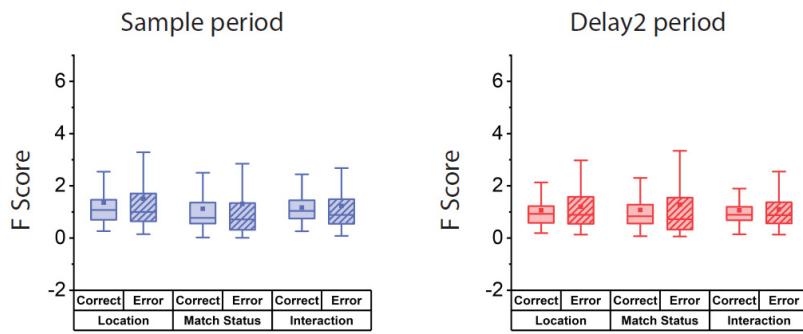
864  
865 Figure 8. Comparing linear SVM decoder information between pure and linear  
866 selective cells (CS and LMS) vs. NMS cells. An equal number of linear (CS and  
867 LMS) and NMS cells were randomly selected from the sample or delay2 period.  
868 The selectivity categories were defined by spiking count in corresponding periods  
869 with reference to stimuli identity (stimuli location or shape) and matching status.  
870 The decoders were trained to classify either stimuli identity or match/nonmatch  
871 status with z-score normalized pseudo-population response. (A) Decoding  
872 performance in the spatial task before and after training. (B) Decoding  
873 performance in the feature task before and after training. Red and blue bars  
874 indicate time points when the performance for NMS and linear cells differs  
875 significantly within the shaded regions.



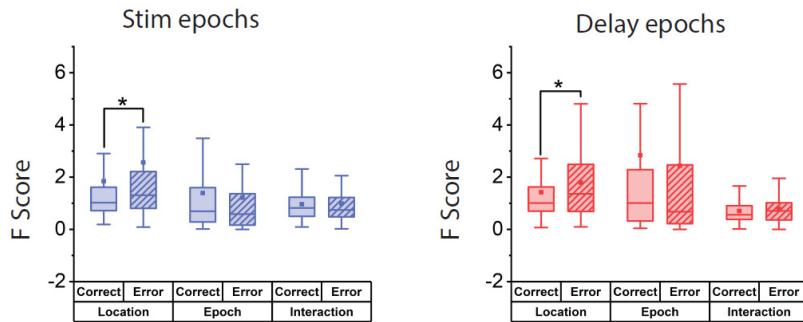
876  
877 Figure 9. Coding dynamics of pure and linearly selective cells (CS and LMS) vs.  
878 NMS cells. Linear kernel SVM decoders were trained to perform cross-temporal  
879 decoding with different selectivity populations in the delay2 period, for both  
880 spatial and feature tasks, as indicated by the Y-axis. The decoder was then  
881 required to predict whether a match or non-match occurred at each time point  
882 based on a different test set of data, as indicated by the X-axis. Normalized  
883 decoding accuracy is indicated in the color bar, demonstrating how spatial and  
884 feature WM representations can be decoded from specific patterns of neural  
885 activity. Coding of matching information for NMS cells is more stable across time  
886 for the spatial task.

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### Location x Match/Nonmatch

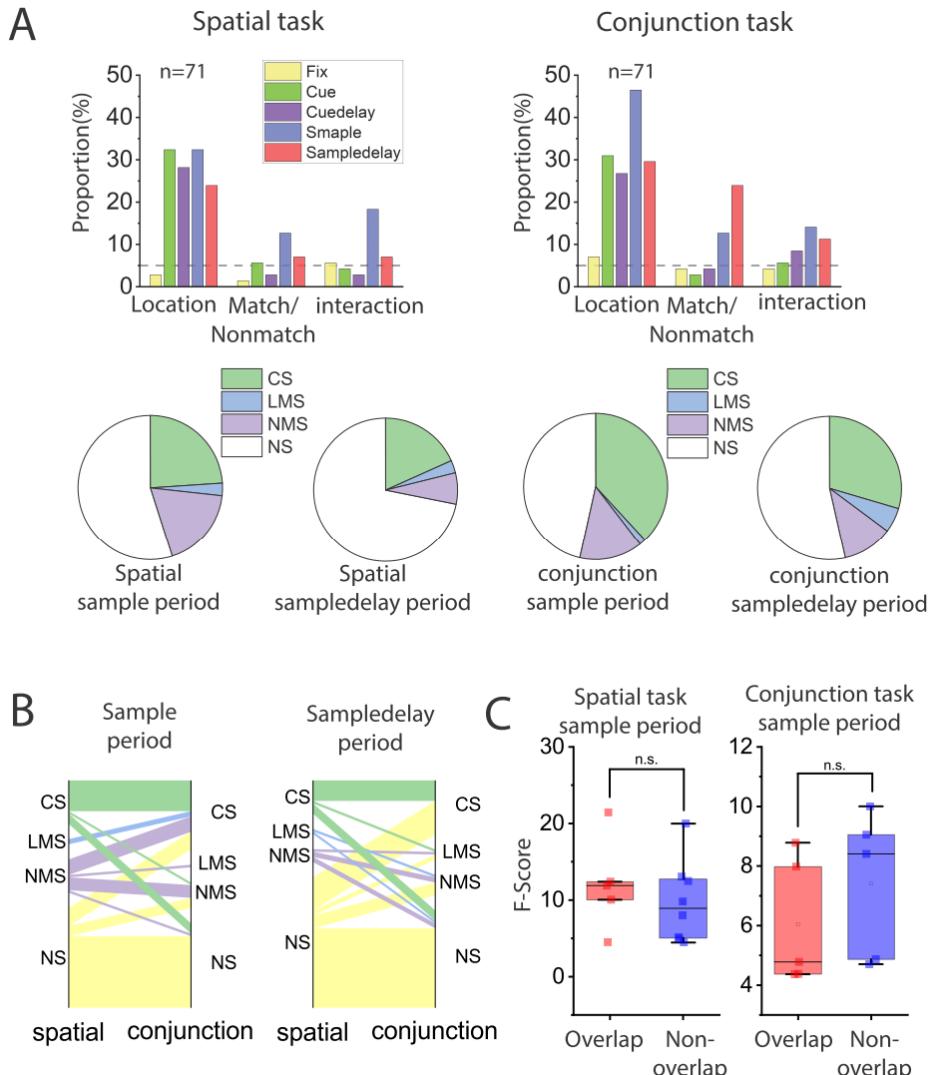


### Location x Epoch



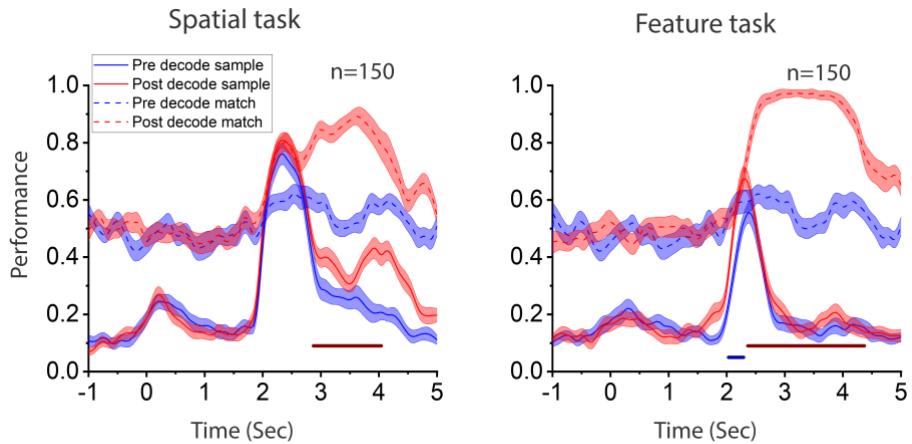
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889 Figure 10. Comparison of cell selectivity in correct and error trials in the same  
890 population for the spatial task, after controlling for trial number and location pairs  
891 used. Two forms of mixed selectivity were examined (location x matching,  
892 location x task epoch). No change (location x matching delay2 period) or  
893 increase (location x task stim and delay epochs, location x matching sample  
894 period) in the F score of the interaction term of ANOVA results were observed in  
895 cells with significant interaction (NMS) terms. Higher F score for the variable of  
896 stimuli location was observed in error trials in the location x Epoch comparison.  
897 Box boundaries represent 25%-75% data range, whiskers indicate 1.5 IQR and  
898 squares indicates means across cells.



899

900 Fig. S1. Plotting conventions same as Fig. 6. Comparing cell selectivity between  
 901 the spatial and the conjunction tasks. The analysis was performed on neural data  
 902 from the same population of cells, with matching numbers of trials in the spatial  
 903 and the conjunction tasks. Only trials with the same stimuli were included in this  
 904 analysis. (A) Examining interaction (NMS) between stimulus preference and  
 905 matching status. Bar graphs display the proportions of cells tuned to stimuli  
 906 shape, trials matching status and their interaction in different stages of the tasks,  
 907 in both the feature and conjunction task. Pie charts display the proportion of  
 908 different selectivity categories (NS, CS, LMS and NMS) in corresponding sample  
 909 and delay2 periods. (B) Cell selectivity category mapping across tasks. (C) F  
 910 scores of the interaction term in the ANOVA were compared between cells that  
 911 were classified as NMS cells in both tasks (overlapping cells), and those only  
 912 classified as NMS in one of the tasks (non-overlapping cells). Similar to the  
 913 comparison between the feature and the conjunction tasks, no change in the  
 914 proportion of NMS was observed.



915  
916 Fig. S2. Incorporation of new information after training for the spatial and the  
917 feature tasks. Linear SVM decoders were trained to classify either stimuli identity  
918 or match/nonmatch status with z-score normalized pseudo-population response.  
919 Color bars indicate time points when the performance for NMS and linear cells  
920 differs significantly. Red bar for decoding matching status, blue bar for decoding  
921 stimuli identity.