

Longitudinal ultrasonic dimensions and parametric solid models of the gravid uterus and cervix

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Abstract

Tissue mechanics is central to pregnancy, during which maternal anatomic structures undergo continuous remodeling to serve a dual function to first protect the fetus in utero while it develops and then facilitate its passage out. In this study of normal pregnancy using biomechanical solid modeling, we used standard clinical ultrasound images to obtain measurements of structural dimensions of the gravid uterus and cervix throughout gestation. 2-dimensional ultrasound images were acquired from the uterus and cervix in 30 pregnant subjects in supine and standing positions at four time points during pregnancy (8-14, 14-16, 22-24, and 32-34 weeks). Offline, three observers independently measured from the images of multiple anatomic regions. Statistical analysis was performed to evaluate inter-observer variance, as well as effect of gestational age, gravity, and parity on maternal geometry. A parametric solid model developed in the Solidworks computer aided design (CAD) software was used to convert ultrasonic measurements to a 3-dimensional solid computer model, from which estimates of uterine and cervical volumes were made. This parametric model was compared against previous 3-dimensional solid models derived from magnetic resonance frequency images in pregnancy. In brief, we found several anatomic measurements easily derived from standard clinical imaging are reproducible and reliable, and provide sufficient information to allow biomechanical solid modeling. This structural dataset is the first, to our knowledge, to provide key variables to enable future computational calculations of tissue stress and stretch in pregnancy, making it possible to characterize the biomechanical milieu of normal pregnancy. This vital dataset will be the foundation to understand how the uterus and cervix malfunction in pregnancy leading to adverse perinatal outcomes.

Introduction

To date, there has been a lack of clinical, translational, and basic science research in the field of reproductive biomechanics and bioengineering. To illustrate, although parturition (labor and delivery) is so common that every human has experienced it, there are currently no clinical tools to effectively predict when delivery will happen, how long pregnancy will last, and how well it will all go. This lack of understanding of fundamental pregnancy biomechanics makes it extremely challenging to understand and address abnormal pregnancy conditions such as preterm birth (PTB, delivery before 37 weeks gestation), which affects 10% of deliveries worldwide and carries short- and long-term health consequences from death in the neonatal period to lifelong disability [1].

The mechanical integrity and function of reproductive tissues is clearly critical to pregnancy outcome [2–5]. The uterus, fetal membranes, and cervix each have dynamic, biological, and mechanical roles (Fig.1); these tissues must remodel and stretch to accommodate the growing fetus while it develops *in utero*, and then do the opposite, i.e. contract, deform, or rupture, to facilitate safe delivery of the fetus. Failure and mistiming of these essentially mechanical events contribute to major obstetrical complications such as PTB [6, 7].

The vital knowledge gap in fundamental pregnancy physiology exists in part because it is challenging to obtain direct quantitative data on how the uterus, fetal membranes, and cervix change throughout pregnancy as pregnancy is a protected environment. This is why we propose a biomechanical parametric modeling approach. Our ultimate goal is to facilitate precision medicine for parturition via development of personalized computational models to characterize a patient-specific biomechanical environment in pregnancy. As a step toward that, the goal of the present work is to provide time-course maternal anatomy data and corresponding 3-dimensional computer aided design (CAD) models on a cohort of low-risk patients with normal singleton pregnancies.

Fig 1. Pregnant Anatomy Representative illustration of a sagittal view of pregnant anatomy with relevant reproductive and surrounding structures labeled.

We acquired imaging data with a standard clinical ultrasound imaging system for practical reasons because compared to other imaging modalities, ultrasound is relatively inexpensive, convenient, and low risk. Fortunately, we found it is feasible to use 2D images to obtain accurate measurements of maternal anatomy to create a CAD model for comprehensive visualization of maternal anatomy. Here, we report: 1) values of critical anatomic structures in normal gestation based on images from quick 2D ultrasound data acquisitions, 2) reproducibility and reliability of each individual measurement and its value to the overall model, 3) effect of gestational age, gravity, and parity on maternal geometry 4) corresponding simplistic and robust 3D parametric CAD models of the uterus and cervix (Solidworks, Dassault Systèmes, Vélizy-Villacoublay, France), 5) estimates of time-course uterine and cervical volumes throughout pregnancy, and 6) a comparison study of the parameterized 3D solid model to MRI-derived solid models.

The data and models generated in this study establish a quantitative foundation for computational analysis of pregnancy. Additionally, the 3D solid modeling method provides the critical foundation to understand how these reproductive tissues may malfunction in pregnancy and allow for novel avenues to design biomedical devices which can be used to prevent adverse outcomes such as PTB.

Materials and Methods

Two-dimensional (2D) ultrasound acquisitions from the uterus and cervix were taken from 30 women at four time points (8-14, 14-16, 22-24, and 32-34 weeks gestation) during pregnancy and stored for offline measurements of dimensions of the uterus and cervix. Reproducibility and reliability of each parameter and its potential contribution to the model was assessed and correlations between parity, maternal age, and gestational age were evaluated. Parameterized patient-specific models were built using Solidworks for all patients and time points using the validated dimensions. Estimates of uterine and cervical tissue volume were determined from these models. Shape parameterization effects were explored by applying the 2D ultrasound measurement protocol to, and comparing the resulting parametric model with, segmented MRI solid models.

Patients

Thirty patients ages 18-41 were recruited when they were in the 1st trimester (<14 weeks gestation) from Valley Womens Health in Provo, Utah from July to December of 2017. Exclusion criteria included history of preterm birth, prior cesarean delivery for failure to progress in labour, previous cervical surgery (including cerclage/LEEP/cone), collagen vascular disease, or known uterine malformation. This study was approved by the institutional review boards at Intermountain Healthcare and the University of Wisconsin, and each subject provided written informed consent.

The age, race, ethnicity, pregnancy history, estimated gestational age (EGA) at each visit, EGA at delivery, and delivery outcomes were recorded for each patient. Details about this cohort are published in Carlson et al. [8]. The estimated date of delivery (EDD) was confirmed by ultrasound crown-rump length at the first study visit. One patient delivered preterm (at 34 weeks 5 days) and was therefore excluded from analysis. Of the remaining 29 patients included in the final analysis, 9 were nulliparous (first pregnancy) and 20 multiparous (at least 1 previous delivery). Patient demographics are reported in Table 1.

Table 1. Patient demographics including the number of subjects, N, in each group and their average age (age range in parentheses).

	N	Age
Nulliparous	9	27 (22-30)
Multiparous	21	28 (21-37)
Total	30	28 (21-37)

Ultrasound Data Acquisition

All ultrasound examinations were done by the same sonographer (J.D.) and acquisitions overseen by the same engineer (L.C.C.). Scanning was performed using a Siemens ACUSON S3000 ultrasound system (Siemens Healthcare, Ultrasound Business Unit, Mountain View, CA, US). The designated research sonographer (J.D.) was certified for cervical length measurement through the Perinatal Quality Foundation's Cervical Length Education and Review (CLEAR) program ([url:perinatalqualityfoundation.org](http://perinatalqualityfoundation.org)). Transabdominal measurements followed the protocol established by Saul et al. 2008 [9].

Each participant underwent ultrasound an exam at four different time points: 1st trimester (8-13 weeks), early 2nd trimester (14-16 weeks), mid 2nd trimester (22-24 weeks), and 3rd trimester (32-34 weeks). The rationale for performing two evaluations during the 2nd trimester is that 16-24 weeks currently appears to be the most critical period for preterm birth-associated cervical change in pregnancy [6]. During each visit,

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six B-mode ultrasound images of the uterus and cervix were acquired (Figs.2-4), three
with the patient supine and three standing. These included transabdominal (TA)
sagittal views of the uterus and cervix, a TA axial view of the uterus, and a
transvaginal (TV) sagittal view of the cervix and lower uterine segment.

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Fig 2. Representative and actual transabdominal (TA) sagittal scan of a
pregnant patient at 32 weeks. Left: representative illustration of measurements
taken from ultrasounds of the uterus and cervix in the sagittal view. Right: actual
transabdominal (TA) sagittal view of the uterus taken as a panoramic ultrasound sweep
from uterine fundus to the cervix. Measurements taken from the TA sagittal view are:
inferior-superior (UD1) and anterior-posterior intrauterine dimensions (UD2, UD3,
UD3a, UD3b), uterine wall thickness measurements (UT1, UT2), and the distance the
inner os is offset from the inferior-superior uterine axis (PCO).

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Fig 3. Representative and actual transabdominal (TA) axial scan of a
pregnant patient at 32 weeks. Left: coronal uterine outline with the ultrasound
sweep location shown with a dashed line, and a representative illustration of
measurements taken from ultrasounds of the uterus in the axial view. Right: actual
transabdominal (TA) axial view of the uterus taken as a panoramic ultrasound sweep
from left to right at the widest section of the uterus. Measurements taken from the TA
axial view are either left or right uterine wall thickness (UT3) and left-right uterine
diameter (UD4).

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Fig 4. Representative and actual transvaginal (TV) sagittal scan of a
pregnant patient at 32 weeks. Left: representative illustration of measurements
taken from ultrasounds of the cervix and lower uterine segment in the sagittal view.
Right: actual transvaginal (TV) sagittal view of the cervix and lower uterine segment
taken by placing the transvaginal ultrasound probe on the anterior fornix and turning
the probe to view the sagittal plane. Measurements taken in the TV sagittal view are:
cervical length (CL), outer diameter (CD1), inner canal diameter (CD2), and cervical
angle with anterior wall of the uterus (AUCA).

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TA sagittal and axial scans were acquired using the SieScape panoramic imaging
feature on the ultrasound system, which automatically registers adjacent images
together as the transducer is swept across the abdomen. Examples of this panoramic
imaging in the sagittal and axial views for a participant at 32 weeks are shown in Fig. 2
and Fig. 3, respectively. For TV acquisitions, the transvaginal transducer was placed
into the anterior fornix of the vagina, the image optimized, and the landmarks identified
(internal and external ostia, canal). All measurements of the dimension parameters were
taken from deidentified ultrasound images using Fiji (ImageJ) [10]. A representative
selection of images from the first few patients was used by L.C.C. to instruct the two
research sonographers on making measurements. The 3 research team members then
independently recorded measurements on the entire dataset.

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The 16 parameters describing dimensions of the uterus and cervix were based upon
previous work [11]. From TA sagittal images, the inferior-superior intrauterine diameter
(UD1) was measured as the longest dimension from the fundus to the lower uterine
segment (Fig. 2). From the midpoint of UD1, the perpendicular distance to the anterior
(UD2) and posterior (UD3) intrauterine walls were measured. To quantify the position
of the cervix in relation to the uterus, the perpendicular cervical offset (PCO) distance
of the cervical internal os to UD1 was measured. Additional posterior dimensions
(UD3a & UD3b) perpendicular to UD1 were taken at 25% and 75% of UD1 from the

superior intrauterine wall, respectively, to describe the curvature of the posterior uterine wall due to the boundary of the spine. Uterine wall thicknesses at the fundus (UT1) and anterior uterine wall (UT2) were also measured in the TA sagittal scan. However, if UT1 and UT2 were not clear in the TA sagittal scan, additional ultrasound images were taken at the specific location of the unclear measurement.

From the TA axial images (Fig.3), left-right uterine diameter (UD4) and uterine wall thickness at either the left or right wall (UT3) were measured. The TA axial scan was done at the widest section of the uterus, where UD4 represents the largest left-right axial intrauterine diameter. Again, if UT3 was not clear in the TA axial scan, then an additional ultrasound was taken at the left or right wall to obtain the wall thickness measurement. Left and right wall thicknesses were assumed to be the same.

From the TV images, uterine wall thickness at the lower uterine segment (UT4), cervical length (CL), cervical outer diameter (CD1), cervical canal diameter (CD2), and the anterior utero-cervical angle (AUCA) were measured (Fig.4). Care was taken to exclude from the CL the isthmus (IS), where the cervical mucousa ends [12]. During the TV exam, quantitative ultrasound data were also acquired from the cervix to measure tissue softness, as published in Carlson et al [8], for future integration into our models of information about tissue microstructure.

Statistical Analysis

To assess reproducibility (interobserver variability) and reliability of the measurements, the inter-class correlation coefficient (ICC) was estimated (p-value is for testing H_0 : $ICC=0$). The quality of each parameter was categorized according to the Cicchetti (1994) Guideline as follows: poor (less than 0.40), fair (between 0.40-0.59), good (between 0.60-0.74), and excellent (between 0.75-1.00) [13].

A linear mixed effects model (LMM) was used to estimate the relationship between each parameter and gestational age (continuous variable GA in weeks), position (categorical predictor Pos ; supine = 1, standing = 0) and parity (categorical predictor Par ; nulliparous = 1, multiparous = 0) and fitted using maximum likelihood. Random effects due to multiple observers and uncorrelated random effects due to intersubject variability for slope and intercept were included. An LMM model for a measurement can be represented as follows:

$$\text{Meas}_i = a' + b' * GA + c' * Pos + d' * Par + e' * GA * Pos + f' * GA * Par \quad (1)$$

where primed (') variables include random effects. For each model, 95% confidence intervals were estimated for the fixed effects via parametric bootstrapping (10,000 iterations), and approximate p-values were subsequently found via inversion of estimated confidence intervals. Statistical analysis was performed in R version 3.3.2 (R Core Team, 2014, R Foundation for Statistical Computing, Vienna, Austria; available at: <http://www.R-project.org/>).

Parametric CAD Model

Solidworks 2018-19 (Dassault Systèmes, Vélizy-Villacoublay, France) was used to construct solid models of the uterine and cervical geometries. A *design table* approach was used to allow for automatic generation of patient specific geometries based on the list of anatomical dimensions described in Figs. 2-4. To establish a parametric build workflow, a *Default Configuration* was established where geometric relations for all subsequent models are established (Fig. 5). Detailed information of the Solidworks

workflow is presented in S1 Appendix and a video created and recorded for the 2020
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Summer Biomechanics, Bioengineering, and Biotransport Conference (SB3C), held
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online June 17-20, 2020 (available: <https://doi.org/10.7916/d8-wxem-e863>) [14].
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Fig 5. CAD model construction. (A) Inner uterine wall sagittal shape built from
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ultrasound measurements. Posterior side is built with either a spline (left) or ellipses
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and a spline (right). Red arrows indicate where tangency constraints have been applied.
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(B) Outer uterine wall sagittal shape built by adding uterine wall thickness ultrasound
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measurements to inner uterine wall sagittal shape. (C) Outer uterine loft completed
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using scaled ellipses as left and right profiles and a half ellipse as the guide curve. (D)
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Inner os is placed at a distance of of the perpendicular cervical offset (PCO) from the
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inferior-superior intrauterine diameter (UD1) on the posterior wall and a plane at an
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angle of the anterior uterocervical angle (AUCA) to the perpendicular of the posterior
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wall.(E) Cervix is added by extruding a circle with diameter of the outer cervical
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diameter (CD1) away from the outer uterine loft a length of the combined cervical and
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isthmus lengths (CL+IS) and up to the outer surface of the uterine loft. (F)
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Intrauterine cavity is made using a lofted cut and the cervical canal is added by an
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extruded cut to the end surface of the cervix and the surface of the intrauterine cavity.
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(G) Fillets are added at the inner os, outer os, exocervix, and uterocervical junction.
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Volume Measurement

The parametric solid model created in Solidworks was used to estimate uterine and
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cervical volume over the course of gestation for all patients in both the supine and
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standing positions. Because the parametric solid model creates the uterus and cervix as
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a single part, the cervical volume had to be separated from the uterine volume. CD1
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was selected as the uterocervical boundary. The sketch of the outer cervical diameter
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(CD1) was made into a surface using the *Extended Surface* tool at a distance equal to
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the cervical length, and the *Split* feature used to separate the cervix from the uterus.
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The *Mass Properties* tool in Solidworks was used to calculate the volume of the uterus
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and cervix individually.
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Validation of Parametric Model

MRI data from Joyce et al. were obtained for 8 term pregnant women prior to caesarean
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delivery [4]. Patient age ranged from 32 to 47 with a mean gestational age of $38.41 \pm$
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0.36 weeks. MRIs were taken within 0-7 days of the scheduled delivery. The MRI image
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stacks were then segmented using the commercial software package Materialise Mimics
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(Research 20.0, Materialise MV, Leuven, Belgium). The detailed protocol of model
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builds for validation and method for model comparison are in S2 Appendix.
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Results and Discussion

Overall uterine diameters and dimension measurements collected via transvaginal
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ultrasound have excellent and good agreement between observers. As expected, all
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uterine diameters increase with gestation, while lower uterine segment thickness (UT4)
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and isthmus length (IS) decrease. The anterior uterocervical angle shifts posteriorly
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with gestation. Parity influences the lower uterine segment thickness (UT4) and cervical
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length (CL) measurement trends. Multiparous patients have a greater rate of lower
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uterine segment thinning, compared to nulliparous patients, and cervical lengths that
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remain constant with gestation. Nulliparous patients' cervical length decrease
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throughout gestation. Maternal position, supine vs. standing, was not significant for lower uterine segment thickness (UT4), cervical length (CL), and isthmus length (IS). However, maternal position affected uterine diameters (UD1-UD4, UD3a, and UD3b) and anterior uterocervical angle (AUCA). The parametric solid modeling method is able to automatically generate models based on patient-specific dimension measurements in 91% of cases. All ultrasonic dimension data and corresponding solid models are available at Columbia University's Academic Commons (dimensions: [permalink DOI here when accepted], models: <https://doi.org/10.7916/d8-tchz-hs47>). 182
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Ultrasound Parameters 190

Reproducibility and Reliability 191

The majority of intrauterine diameter measurements (UD1-4, UD3a) and lower uterine wall thickness measurement (UT4) showed excellent agreement between observers (Table 2, $ICC > 0.75$). The inferior perpendicular distance from the inferior-superior axis to the posterior intrauterine wall (UD3b) showed good agreement between observers ($0.60 < ICC < 0.74$). Good agreement was also demonstrated for cervical length (CL), isthmus length (IS), and anterior uterocervical angle (AUCA). Fair agreement between observers ($0.40 < ICC < 0.59$) was noted for the outer cervical diameter (CD1) and poor agreement ($ICC < 0.40$) was seen for uterine wall thicknesses at the fundus, anterior uterine wall, and left or right uterine wall (UT1-UT3), along with the posterior cervical offset (PCO) and diameter of the mucous plug (CD2). Parameters with fair or poor agreement were removed from further analysis. The ICC values for each measurement are summarized in the last column in Table 2. 192
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Table 2. Summary of linear mixed model and ICC results for each parameter sorted by highest to lowest ICC value. LMM slope estimates (mm/week) in linear mixed effects models adjusting for parity and position (supine versus standing). The line indicates the cutoff between good and fair measurements, as prescribed in the methods section.

*Indicates measurements for which parity was significant and included in the model.

Measurement	b (LMM slope) [mm/wk]	95% CI	P-value	ICC
UD1	8.831	(8.75–8.91)	<0.001	0.990
UD4	7.912	(7.81–8.01)	<0.001	0.984
UD23	2.795	(2.74–2.85)	<0.001	0.936
UD3	1.753	(1.71–1.80)	<0.001	0.853
UD2	1.060	(1.02–1.00)	<0.001	0.827
UT4*	-0.324	(-0.35– -0.30)	<0.001	0.823
UD3a	2.013	(1.96–2.06)	<0.001	0.820
UD3b	1.353	(1.31–1.40)	<0.001	0.739
AUCA (Deg./wk)	0.369	(0.24–0.50)	<0.001	0.691
IS	-0.436	(-0.47– -0.40)	<0.001	0.677
CL*	-0.065	(-0.09– -0.04)	<0.001	0.625
CD1	0.270	(0.25–0.29)	<0.001	0.562
PCO	0.632	(0.58–0.68)	<0.001	0.365
UT1	0.029	(0.02–0.04)	<0.001	0.263
UT2	-0.013	(-0.02–0.00)	0.023	0.230
UT3	0.055	(0.04–0.07)	<0.001	0.202
CD2	0.011	(0.01–0.02)	<0.001	0.076

The intrauterine diameter measurements accounting for the posterior uterine wall at 25% and 75% along the inferior-superior axis (UD3a and UD3b) show the lowest ICC 204
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values of all intrauterine diameters, likely because of difficulty in viewing posterior features in the TA sagittal view. The inconsistency in image quality also precludes measurement of posterior uterine wall thicknesses, and in models that posterior wall thickness is assumed to be equal to the anterior wall thickness (UT2). As expected, the sum (UD23) of the perpendicular distance from the midpoint of the inferior-superior intrauterine diameter (UD1) to the anterior (UD2) and posterior (UD3) intrauterine wall shows a higher ICC value than the measurements individually, likely because it spans the entire anterior-posterior intrauterine diameter, making it independent of the placement of UD1.

The significantly higher ICC value for the lower uterine segment thickness (UT4) as compared to the other uterine wall thicknesses parameters (UT1-UT3) is undoubtedly due to the use of TV ultrasound to obtain this image. As compared to TA transducers, TV transducers provide better image resolution because they operate at a higher frequency [15], they acquire data directly from the structure instead of having several tissue layers to penetrate, and the image covers a much smaller area so the features appear larger, all of which contribute to a more precise measurement.

Besides uterine thickness measurements, several other parameters showed fair or poor agreement between observers: PCO, CD1, and CD2. The poor agreement between observers for posterior cervical offset (PCO) measurements may be attributed to variable inferior-superior intrauterine diameter (UD1) placement, as it is used as the end point for this dimension. Additionally, identification of the inner cervical os is often difficult in TA sagittal scans (this is why the clinical gold standard for measurement of the cervix is TV), further contributing to poor agreement on the PCO parameter. The fair agreement for the outer cervical diameter (CD1) is likely a result of inadequate measurement definition; the location along the cervix to measure the diameter was not specified. The poor agreement between observers for the mucous plug (CD2) can be attributed to inadequate visualization of the cervical canal in some images, and the small magnitude of the measurement (single pixel differences can have large effects on the measurement value). This finding is consistent with previous reports describing characterization of the mucous plug [16].

It has been previously reported isthmus length (IS) and anterior uterocervical angle (AUCA) are considered repeatable measurements, while cervical length (CL) repeatability varies [17], [18], [19], [20]. These reports are in accordance with the good agreement found for IS and AUCA, and the good agreement between sonographers for CL is most likely due to their uniform training and certification.

Effect of Gestation

All intrauterine diameter measurements (UD1-UD4, UD3a, UD3b) significantly increase with gestational age and cervical/lower uterine segment measurements (UT4, IS) significantly decrease with gestational age in both supine and standing positions (p-values < 0.001). The cervical length (CL) slightly decreases throughout gestation (p-value < 0.001), as has been previously described in normal pregnancy [21], and the anterior uterocervical angle (AUCA) shifts posteriorly throughout gestation (p-value < 0.001). Plots of each measurement vs. gestational age are shown for all patients in the supine position averaged across observers in S3 Appendix.

The fixed effect coefficients [a, b, c, d, e, f] for each variable [$GA, Pos, Par, GA * Pos, GA * Par$] in Eq. 1 are summarized in Table 3. In the LMMs (Eq. 1), the variables used with parity and position (Pos, Par) are binary, thus the coefficients that include parity and position are only applied if the subject was in the supine position and/or nulliparous. To illustrate, if a patient is in the supine position, $Pos = 1$ and variables c and e are included in the effective LMM (Eq. 1). However, if a patient is in the standing position, $Pos = 0$ and variables c and e will not be included in the effective

LMM (Eq. 1), as they have been multiplied by 0. The same is true for position.

Table 3. Summary of linear mixed model fixed effect coefficients from equation 1 sorted by highest to lowest ICC value (non-significant terms are dropped with coefficients indicated as –). The line indicates the cutoff between good and fair, as prescribed in the methods section. Measurements are based on ICC values in Table 2. Int.=intercept

Measurement	a	b	c	d	e	f
	Int. mm	GA mm/wk	Pos mm	Par mm	GA*Pos mm/wk	GA*Par mm/wk
UD1	-24.865	8.976	3.575	–	-0.289	–
UD4	-30.559	8.205	17.216	–	-0.585	–
UD23	34.666	2.964	-6.830	–	-0.110	–
UD3	15.344	1.809	-4.884	–	-0.338	–
UD2	18.739	1.193	-1.325	–	-0.266	–
UT4	17.356	-0.342	–	-3.427	–	0.065
UD3a	6.280	2.079	-4.703	–	-0.133	–
UD3b	18.071	1.407	-0.967	–	-0.108	–
AUCA (deg)	73.432	0.014	-5.860	–	0.709	–
IS	22.847	-0.436	–	–	–	–
CL	31.759	0.026	0.577	3.772	–	-0.325
CD1	28.281	0.210	-0.589	–	0.120	–
PCO	6.322	0.711	4.419	–	-0.158	–
UT1	6.665	0.029	-0.724	–	–	–
UT2	7.527	-0.013	-0.791	–	–	–
UT3	7.673	0.055	-0.703	–	–	–
CD2	3.169	0.011	–	–	–	–

The dramatic increase of the uterine diameter over the course of gestation is expected, as the uterine cavity must expand to accommodate the growing fetus. The decrease in the isthmus length (IS) and lower uterine segment thickness (UT4) is also an expected finding, due to normal remodeling throughout gestation [18, 22, 23].

Effect of Parity

Parity influences the lower uterine segment thickness (UT4) and cervical length (CL) measurements (Fig. 6). UT4 decreases by 0.277 mm/wk for nulliparous patients and 0.342 mm/wk for multiparous patients. CL decreases by 0.299 mm/wk for nulliparous patients, but for multiparous patients CL stays nearly constant (small increase of 0.026 mm/wk).

Fig 6. Effect of parity on ultrasonic maternal anatomy measurements across gestational age. Box and whisker plots for lower uterine segment thickness (UT4) and cervical length (CL) for nulliparous and multiparous patients.

The dependence on parity suggests possible permanent mechanical and structural changes that occur during the remodeling events of pregnancy. For a multiparous patient, the increased rate of thinning of the lower uterine segment suggests two possible mechanisms: 1) the mechanical load exerted by the contents of the amniotic sac is shifting faster towards the lower part of the uterus and/or 2) uterine tissue becomes softer in subsequent pregnancies. As for a multiparous cervix, there is not enough evidence in the literature to statistically determine if the cervix becomes mechanically

softer with each pregnancy. One study found that women with a history of previous vaginal deliveries have softer cervices than nulliparous women [24].

Effect of Position

Maternal position (supine vs. standing) also influences maternal geometric measurements. Maternal position vs. gestation age interaction (column 6 in Table 3) is significant for all intrauterine diameters (UD1-UD4, UD3a, and UD3b) and the anterior uterocervical angle (AUCA) where the LMM slopes are higher in the standing position, except for AUCA, where the angle decreases with standing. Maternal position is not significant for lower uterine segment thickness (UT4), cervical length (CL), and isthmus length (IS).

The effect of gravity has long been a curiosity in the study of pregnancy biomechanics. Bedrest has been demonstrated to be ineffective at reducing the rate of preterm birth [25]. The maternal anatomy measurements here confirm the cervix does not further deform when a woman stands from a supine position, nor does the lower uterine segment thin. Whether the cervix deforms after longer periods of standing (i.e. viscoelastic creep) remains to be determined. However, it is observed uterine shape changes with position. Specifically, the uterus becomes flatter in the anterior-posterior direction and wider in the left-right direction when in the supine position when compared to the standing position. This is quantitatively observed by comparing the ratio of the anterior-posterior intrauterine diameter (UD23) to the left-right intrauterine diameter (UD4) in the standing and supine position, where in 86% of cases the ratio is larger when standing than in supine. Therefore, gravity does have an effect on uterine axial shape.

Parametric CAD Model

The solid CAD models provide a visualization of uterine and cervical shape and size change throughout gestation (Fig. 7) and provide a structural foundation to calculate the mechanical loading environment of pregnancy. All solid models (STL files) generated from the workflow described in S1 Appendix are freely available through the Columbia University Library's permanent Academic Commons collection (url: <https://doi.org/10.7916/d8-tchz-hs47>). With 29 patients scanned at 4 time points in two positions measured by 3 sonographers, 696 sets of parametric measurements were taken and used to build models. For visits 1-3, the *spline method* better represents the posterior uterine wall, and for visit 4 the *quarter ellipse method* is a better method (see S1 Appendix for method description). Of the 696 patient-specific parametric model builds attempted, 632 usable models are generated (91% automatic build rate). Of these models, 70 require slight edits, such as altering the fillet type or radii.

Fig 7. Representative overlays of Solidworks model and ultrasound for all visits. Solidworks models aligned with corresponding ultrasound scan along the inferior-superior intrauterine diameter (UD1) for (A) patient 11 in the supine position, (B) patient 11 in the standing position, (C) patient 27 in the supine position, and (D) patient 27 in the standing position. Patients have been selected randomly from those where all models generated.

Cases failing to generate usable models have issues in four categories: an extreme anterior uterocervical angle (51 cases), a posterior cervical offset (PCO) larger than posterior intrauterine diameters (7 cases), or loft function failure (6 cases). Cases with an extreme anterior uterocervical angle (AUCA) fail because the cervical cylinder does not terminate correctly on the uterine body. Of these cases, 45% were visit 1, 23% were

visit 2, 14% were visit 3, and 18% were visit 4. As observed in ultrasound, the CL is not typically a straight line and is frequently measured using several segments, especially early in pregnancy. Therefore, in order to model these cases, the curvature of the cervix may need to be captured. For cases where the loft function failed, Solidworks is not able to complete the loft for the outer uterine body, where 66% of cases are at visit 1, 17% at visit 2, and 17% at visit 4. These models may require additional guide curves in order to loft, or may call for an inferior-superior loft instead of left-right. The cases where the PCO is greater than posterior intrauterine diameters (UD3 and UD3b) is fairly consistent across visits. In these cases, a different measurement protocol must be used to characterize the posterior wall, as discussed in model validation in S2 Appendix.

It is observed, though not quantified, that the sagittal shape of the parametric model does not always produce a good match to the TA sagittal scan. For the anterior side, this occurs when the uterine wall is not a half ellipse. For the posterior side, this occurs when the spline does not fit the actual posterior wall shape well. The spline parameters in the models are automatically fit and no attempt is made to vary them to match individual's posterior wall shapes. This could be remedied through the use of an alternate measurement method, as discussed in S2 Appendix, or a method of capturing spline parameters from ultrasound images. Future validation of the model must be done for use in rigorous analysis of the entire gravid uterine and cervical environment. However, these low fidelity models are useful for educational and visualization purposes. Additionally, the shape and size of the lower uterine segment and cervix match well in the sagittal plane between the ultrasound and MRI-derived CAD models (S2 Fig. 1), but improvement is still seen with an alternative measurement method. Hence initial structural analysis can be conducted of this critical *stress concentration* region [11] using a subsection of the CAD models reported here, though model accuracy is still unquantified.

Uterine and Cervical Volume

The uterine volume increases over the gestational ages (Fig. 8). This is observed in both the supine and standing configurations. The cervical volume does not have a clear trend of increase or decrease in volume when looking at all patients and configurations (Fig. 9). Same patient, same visit uterine volume in the standing and supine positions are frequently unequal, with an average error between supine and standing or 22.1% using eq. 2.

$$\text{Error} = \frac{\text{SupineVolume} - \text{StandingVolume}}{\text{SupineVolume}} * 100, \quad (2)$$

Fig 8. Uterine Volume with Gestation. Average of (A) standing and (B) supine uterine volume across three sonographers for all visits.

Fig 9. Cervical Volume with Gestation. Average of (A) standing and (B) supine cervical volume across three sonographers for all visits.

Uterine tissue volume tends to increase at an increasing rate over the gestational ages included in this study. This result is in accordance with previous studies, which report an S-shaped curve to describe qualitatively how uterine tissue weight changes during gestation [26]. In future work, further agreement between Gillespie and parametrically estimated uterine volume can be achieved by collection of very late gestation ultrasounds to determine if tissue volume plateaus as reported. Uterine

volume inconsistency between supine and standing may arise from a number of factors, including poor repeatability of uterine thickness measurements and uterine contractions occurring at time of ultrasound acquisition.

It is assumed, as pregnancy tissue remodeling occurs, the isthmus disappears. Due to this conclusion, it is difficult to determine if a lack cervical volume trends are a result of tissue volume changes, inconsistent cervical boundary assignment, or some combination thereof. There is currently no universally accepted method of distinguishing a boundary between the cervix and the uterus. The method used to distinguish cervical tissue from uterine tissue, described above, does not offer a rigorous delineation of tissues. While this inconsistency will not greatly influence trends in uterine volume, it has the potential to substantially skew cervical volume trends due to the smaller volume of the cervix and greater influence an equally sized error will have.

Comparing dimensions to previously published data

The choice of proportions to portray the uterus and cervix is informed by previous investigations of gravid geometry. Published in 1950, the last holistic study of pregnant uterine shape reports gestational-age trends of greater sagittal and transverse uterine dimensions measured from x-rays as well as uterine weights recorded retrospectively from hysterectomies executed at various stages of gravidity [26]. All data are reported either through qualitative description or graphical sketches [26]. This study concludes uterine weight increases until the 20th week of gestation, coinciding with the most rapid increase in the transverse measurement of the fundus [26]. At the 20th week of gestation the uterus is spherical and proceeds to elongate into a “cylindrical” shape until delivery [26]. A prior study of the gravid morphology in monkeys identified three stages of uterine development: 1. growth of the myometrium through hypertrophy accounting for the uterus’s increase in weight during early pregnancy, 2. uterine growth through some hypertrophy but predominantly hyperplasia, and 3. elongation and stretching of the uterus until term [27]. In 2010, a longitudinal anatomical and cellular investigation of the myometrium in pregnant mice supported the earlier study’s assertion, finding that growth in early gestation was due to hypertrophy while most growth after mid-gestation was due to hyperplasia of the smooth muscle myocytes [28].

Ultrasound investigations of the myometrium have developed differing analyses of gestational trends in thickness. Durnwald et al (2008) found a significant negative linear relationship between myometrial thickness and gravidity at the fundus, anterior wall, posterior wall, right and left-side walls, and lower uterine segment [29]. However, in an inquiry of the same five measurements, Degani et al (1998) reported only the lower uterine segment showed a significant negative correlation with gestational age [30]. Similarly, Degani et al discovered the myometrial dimensions were not significantly different from one another while Durnwald et al found the fundus was thinner than the upper uterine segment during second and third trimesters [29], [30]. Durnwald also showed multiparous women exhibited thicker uterine walls at five of the six measured sites [29]. Our own examination reviewed the myometrium at the fundus, anterior wall, side wall, and lower uterine segment.

Cervical dimensions are among the most scrutinized aspects of pregnancy, both clinically and academically. Various risk-scoring methods based on cervical diameter, dilation, length, position, and consistency have been developed from consistently found statistical correlation, though with low prognostic success [31]. Short cervical length has long been associated with PTB and the time since conception at which the measurement is taken impacts its predictive nature [32], [33], [34]. In the first trimester, the isthmus length correlates with PTB while cervical length does not and as gestation progresses, the cervical length measurement predicts a lower risk for the patient over all [33], [35]. Recent research has also shown uterocervical angle (UCA), describing the

angle at which the cervix connects with the lower uterus, also correlates with likelihood of PTB and indeed shows higher sensitivity to risk than cervical length [18]. The choice of UCA, cervical length, cervical dilation, cervical diameter and isthmus length as part of our study is based on these studies.

Limitations

To characterize and model maternal anatomy in normal gestation, we made several simplifications to allow for implementation in the clinical setting. 2D ultrasound images allowed for data collection from more patients than if we used more detailed imaging modalities, such as 3D ultrasound or MRI. However, the 2D ultrasound images have a lower quality than other imaging techniques and preclude vision of certain anatomic features, such as the posterior uterine wall. Additionally, though the number of patients provides compelling trends in maternal anatomy evolution with gestation, a more extensive sample set would be necessary to draw population-level conclusions. The parametric modeling method, an improvement in capturing sagittal uterine shape compared to previous parametric models, is not assumed to be the most accurate method of generating patient-specific geometry. It is instead a first attempt at including more geometric sophistication. Thus, the novelty of the presented parametric modeling method lies in the ability to quickly generate patient-specific solid models for visualization, education, and ideation on the biomechanics of the uterus and cervix throughout gestation. It is not a rigorous basis for calculating gravid mechanical loading, though future computational studies may prove it to be so. Nevertheless, this method is foundational to our future studies of calculating stretch and stress in the pregnancy, but we have not validated its quantitative accuracy at the time of publication. While we work towards this validation, we acknowledge the importance of sharing our longitudinal measurements of the uterus and cervix in pregnancy and a straightforward method to create solid models from them.

Conclusion

This work presents longitudinal 2D ultrasound dimension measurements which characterize the overall shape and position of the uterus and cervix, along with a framework to implement them into patient-specific parametric CAD models. In this study, the interobserver variability between measurements is explored, with measurements of intrauterine diameters, lower uterine segment thickness, anterior uterocervical angle, isthmus, and cervical length having the best repeatability. Measurements of cervical diameters, posterior cervical offset, and uterine thicknesses taken from transabdominal ultrasound show fair to poor agreement between observers. These findings are promising in refining a 2D ultrasound dimension measurement protocol that is easily integrated into clinical practice. They are also useful in establishing structural models to facilitate biomechanical calculations of tissue stress, stretch, growth and remodeling of the uterus and cervix for pregnancies at low-risk of preterm birth.

Linear mixed effect models (LMM) are calculated for all measurements, taking into account gestational age, parity, and position. Our results regarding growth of the intrauterine cavity with gestational age are intuitive, since intrauterine diameters increase with gestation to accommodate the growing fetus. The LMM models also provide insight to the effect of gravity on axial uterine shape, which becomes more oblong in the supine position compared to standing. Parity is shown to have an effect on changes in lower uterine segment thickness and cervical length with gestation, indicating a shift in mechanical loading of the uterus and cervix in subsequent pregnancies.

The solid modeling framework is able to automatically generate patient-specific models in 91% of cases using Solidworks, a commercially available CAD software. Additional modeling frameworks will need to be developed in order to capture all uterine and cervical shapes. Uterine and cervical volume throughout gestation is estimated using the patient-specific models. Uterine volume is shown to increase with gestational age, which is in agreement with existing literature. No clear trend in cervical volume with gestational age is deduced. The current phase of the framework produces low-fidelity models appropriate for visualization and educational purposes. In future studies, the solid models will be incorporated into a finite element analysis workflow to calculate tissue stress and strain. The model's viability for finite element analysis of mechanical loading during pregnancy will be validated and necessary refinements made such that biomechanical phenomena of pregnancy can be probed. This will aid in distinguishing maternal geometry that results in a mechanically higher risk of preterm birth.

Supporting information

S1 Appendix. Parametric Solid Model Solidworks Workflow To build the *Default Configuration*, first the sagittal intrauterine wall was defined in the front-plane. The anterior intrauterine wall was built using two equal quarter ellipses, where the inferior-superior radial value was half of the inferior-superior intrauterine diameter (UD1) and the anterior-posterior radial value was the perpendicular distance from the midpoint of UD1 to the anterior intrauterine wall (UD2) (Fig. 5a). The posterior intrauterine wall was built using either a single spline or two quarter ellipses and a spline. UD3a, UD3, and UD3b were used to define the posterior side in both cases, with UD3a placed superiorly to UD3b (Fig. 5a). In the case of the single spline, the ends of the spline were defined to be tangent where it connects to the quarter ellipses of the anterior side. For the two quarter ellipses and a spline as the posterior side, UD3a and UD3b were used as the anterior-posterior radial values, and UD3 was a connecting point for the spline between them. The spline was defined to be tangent to the quarter ellipses at the shared points of UD3a and UD3b.

Next, the outer uterine wall was defined in the front-plane. The build process from the intrauterine wall was repeated, but the sagittal uterine thicknesses were added. Thus, UT1 was added superiorly to the inferior-superior intrauterine diameter (UD1) to define the superior outer uterine wall, UT2 was added anteriorly to UD2 for the anterior outer uterine wall, UT4 was added inferiorly to UD1 for the inferior uterine wall, and UT2 was added posteriorly to UD3a, UD3, and UD3b for the posterior uterine wall, as no posterior uterine wall thickness was collected (Fig. 5b).

To construct the three-dimensional uterus, a *Lofted Boss/Base* function was used. In order to execute a *Lofted Boss/Base* function, *Profiles* and a *Guide Curve* were defined. Small ellipses were used as the *Profiles* to the right and left of the sagittal plane. The ellipse size was defined using UD2/500 as the vertical radius and half of UD1/500 as the horizontal radius (Fig. 5c). This was done to ensure the guides were similar in overall shape to the sagittal uterine wall, but small enough to not affect future finite element analysis. With respect to the sagittal plane, the ellipses were placed at the midpoint of UD1 and the midpoint of UD2 and UD3, and were placed a distance of half of UD4 plus UT3 from the front-plane to define the right and left-most walls of the uterus. The *Guide Curve* sketch plane was defined by the superior-most points of the elliptical left and right profiles and the sagittal uterine wall profile. The *Guide Curve* was then drawn as a half-ellipse connecting the superior points of the elliptical left and right profiles and the sagittal uterine wall profile (Fig. 5c).

Next, cervical placement was determined in the front-plane by finding the

intersection point of a guide line posteriorly parallel to the inferior-superior intrauterine diameter (UD1) and the inferior side of the sagittal intrauterine wall at a distance of the posterior cervical offset (PCO) (Fig. 5d). From this point, a plane was defined to be perpendicular to the inferior intrauterine wall. A second plane was placed at an angle of AUCA to the perpendicular plane (Fig. 5d). A circle was sketched on this plane with a diameter of CD1 and extruded a length of CL+IS using the *Extruded Boss/Base* feature, creating the cervical geometry (Fig. 5e). The intrauterine cavity was then generated using the *Lofted Cut* function (Fig. 5f). Having similar requirements as the *Lofted Boss/Base* function, the *End Guides* were the same ellipses, but rather placed at a distance of half of UD4 from the Front Plane on its left and right sides. The *Guide Curve* was defined in a similar fashion to the outer uterus loft *Guide Curve*. On the same plane as the definition of the gross cervical geometry, a circle with a diameter of CD2 was sketched and an *Extruded Cut* was performed at a length of CL+IS (Fig. 5f). Finally, fillets were added to the inner os, outer os, ectocervix, and outer uterocervical junction (Fig. 5g). With the completion of the *Default Configuration*, a design table was enabled and all patient-specific ultrasound measurements were input. Patient-specific parametric models were then automatically generated.

S2 Appendix. Parametric Model Validation Method The commercial software Materialise Mimics (Research 20.0, Materialise MV, Leuven, Belgium) was used to segment the MRI image stacks for 8 term pregnant women prior to caesarean delivery [4]. On average, every third image was selected for manual segmentation using the paint tool. An interpolation was performed among segmented images to create a complete segmentation. A three-dimensional geometry was then created by exporting the resulting segmentation as a stereolithography (STL) formatted surface. The STL file was then conservatively smoothed using a commercial software 3D-Coat (Pilgray, Kiev, Ukraine) to preserve the overall geometric features and eliminate minor surface imperfections. Of the 8 STL files, 5 were used for parametric model validation, as 3 geometries had large gaps in the uterine wall. These 5 STL models are available through the Columbia University Library's permanent Academic Commons collection (url:*permalink will be added upon paper acceptance*).

Segmented MRI-derived solid models were measured using the 2D ultrasound measurement protocol instead of MRI images. Each STL volume was then imported into Solidworks 2018-2019 (Dassault Systemes, Vélizy-Villacoublay, France) as a solid body. The TA sagittal plane was chosen as the section with the largest cervical canal width, and the TA axial plane as the one with the largest internal diameter. From these planes, all dimensions were taken using the 2D ultrasound measurement protocol described above.

Using the measurements taken, a parametric solid model was built from each MRI-derived solid model in order to compare the complex MRI-based model to the simplified ultrasound-based model. The similarity of the parametric models to the MRI-derived solid models was analyzed by comparing their shapes in the sagittal plane. Sagittal slices of models were aligned so the inferior-superior intrauterine diameters (UD1) were colinear. The models were also aligned using CL in the sagittal plane to compare uterocervical junction shape. The volume of the MRI-derived and parametric models was also compared. This was accomplished by using the "Mass Properties" tool in Solidworks. The volume percent error (Error) between the models was computed by finding the volume difference between the MRI-based model volume (MRI) and parametric model volume (Para), then dividing by the MRI-based model volume and multiplying by 100 (Eq. 3).

$$\text{Error} = \frac{MRI - Para}{MRI} * 100, \quad (3)$$

Validation against MRI-Derived Models The shape of the parametric and MRI-based models is compared by overlaying in the sagittal plane. The overlays are shown in S2 Fig. 1. The parametric model is also compared to the MRI-based models through volume measurements. The average error in volume between the MRI-derived solid models and parametric models is $7 \pm 7\%$. For MRI patients 1, 2, and 5, the parametric model underestimates the volume of the MRI-based model. The parametric model overestimates the volume of the MRI-based model for patients 3 and 4.

S2 Fig. 1 Comparison of Solidworks sagittal shape to MRI-based model sagittal shape Solidworks model sagittal slices overlaid on MRI-based model sagittal slices. Top row aligned using the inferior-superior intrauterine diameter (UD1), bottom row aligned using the cervical length (CL).

By visual comparison, the sagittal profiles are a good visual match for patients 1, 2, and 5. The visual match in sagittal profile shape is fair for patient 4, and patient 3 did not match well. The MRI-based solid models which had the best visual match with their associated parametric model exhibited features in accordance with assumptions made during the parametric model build, such as having a maximum anterior radial diameter close to the center of the inferior-superior axis, and local extrema of the posterior uterine wall equally spaced along it. However, the uterocervical junction shape is not well captured in the parametric models with exception in patient 3, where a similarity in shape is observed. The uterocervical junction must be accurately captured to utilize this modeling process in future computational studies. This area likely has consequential tissue stretch and stress and plays a fundamental role in late pregnancy and birthing dynamics. One possible alteration to better capture the uterocervical junction is to redefine UD3a and UD3b as local extrema of the posterior wall on the superior and inferior halves of the inferior-superior intrauterine diameter (UD1), respectively, and additional measurements taken as locator dimensions along UD1. The results of redefining UD3a and UD3b as such are shown in S2 Fig. 2. Incorporating these measurement definitions into the parametric models results in much better agreement of uterocervical junction shape between the MRI-based model and parametric model for all patients, as well as match in overall sagittal profile shape. This methodology has limited use as not all posterior walls have clear extrema, in which case the equidistant placement of posterior intrauterine wall diameters is better. The equidistant measurement definition will likely offer better results in early gestation, before the uterus has abutted against the spine. Certain geometric features should offer insights into which measurement definitions would more accurately model individual patients. Further studies are required as not all geometries can be represented using the presented processes.

S2 Fig. 2 Comparison of Solidworks sagittal shape to MRI-based model sagittal shape for alternate measurement method. Solidworks model with alternate measurement method sagittal slices overlaid on MRI-based model sagittal slices. Top row aligned using the inferior-superior intrauterine diameter (UD1), bottom row aligned using the cervical length (CL).

The coronal and axial planes are not well matched between the MRI-based models and parametric models. This is due to the use of ellipses to model the coronal and axial shape, with the largest transverse diameter assumed to be at the midpoint of the inferior-superior intrauterine diameter (UD1). The MRI-based models show the coronal

shape of the uterus in late gestation has a maximum transverse diameter occurring at approximately 60% of UD1 from the inferior uterine wall. Therefore, for late gestation models, it is not appropriate to use an ellipse as the coronal shape of the uterus and the parametric construction method must be revised to account for the tapering of the transverse uterine diameter towards the uterocervical junction, as observed in the MRI-based models. It is currently unknown how the uterine shape in the coronal and axial planes change throughout pregnancy, and additional ultrasound images are necessary to characterize the evolution of the inferior portion of the uterus throughout pregnancy. A better understanding of the shape evolution of the uterocervical junction would be of great impact in future computational studies.

S3 Appendix. Patient 2D ultrasound dimension measurements with gestational age in the supine position averaged across sonographers

S3 Fig. 1 Uterine Diameters Uterine diameters with gestational age in the supine position averaged across sonographers. Shown are inferior-superior intrauterine diameter (UD1), perpendicular distance between the midpoint of UD1 and the anterior intrauterine wall (UD2), perpendicular distance between the midpoint of UD1 and the posterior intrauterine wall (UD3), perpendicular distance between 25% and 75% of UD1 from the superior to the posterior intrauterine wall (UD3a & UD3b), and the left-right intrauterine diameter (UD4).

S3 Fig. 2 Uterine Wall Thicknesses Uterine wall thicknesses with gestational age in the supine position averaged across sonographers. Shown are fundal uterine wall thickness (UT1), anterior uterine wall thickness (UT2), left or right uterine wall thickness (UT3), and the lower uterine segment thickness (UT4).

S3 Fig. 3 Cervical Measurements Cervical measurements with gestational age in the supine position averaged across sonographers. Shown are the posterior cervical offset (PCO), anterior uterocervical angle (AUCA), cervical length (CL), isthmus length (IS), outer diameter of the cervix (CD1), and the diameter of the mucous plug (CD2).

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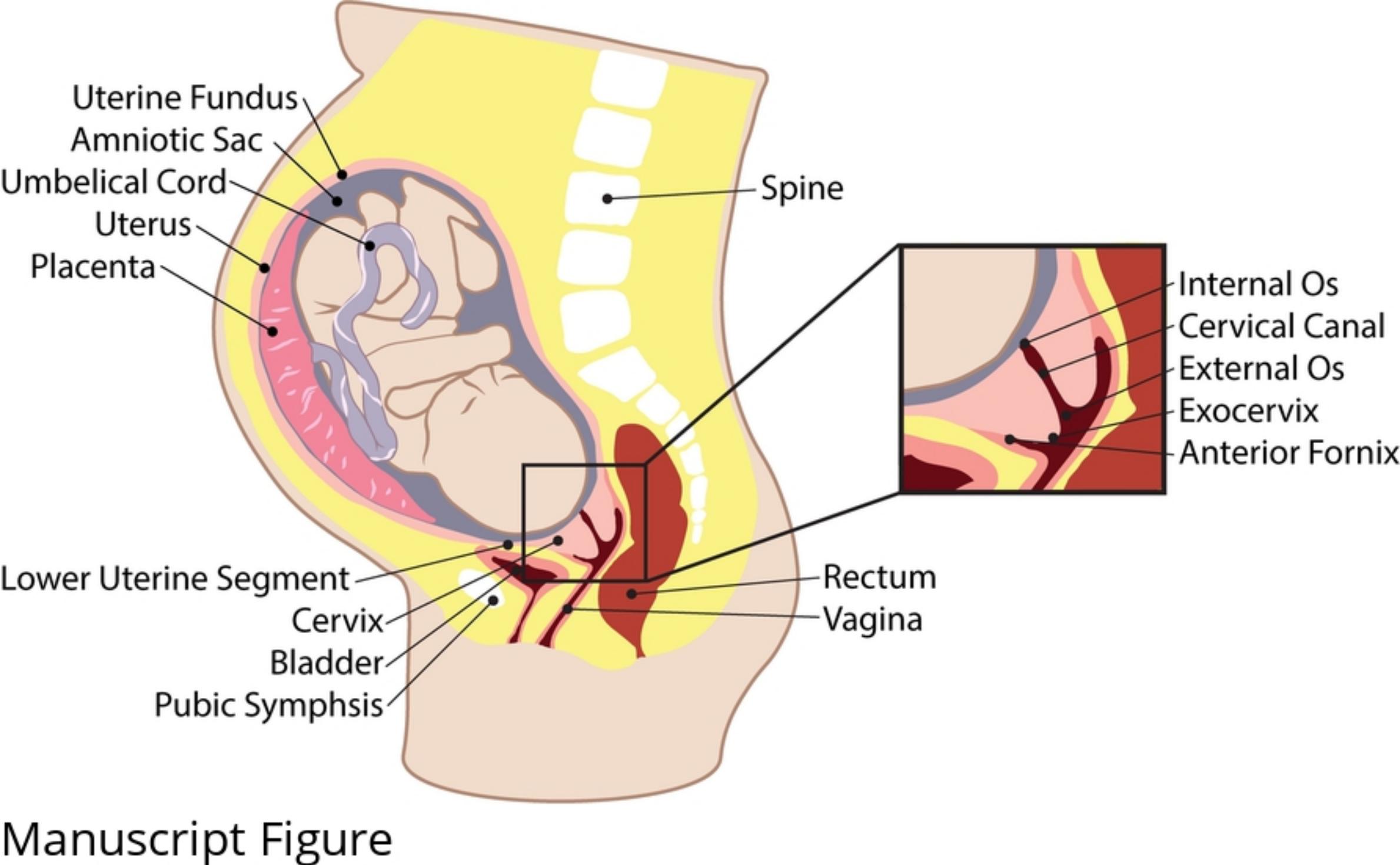
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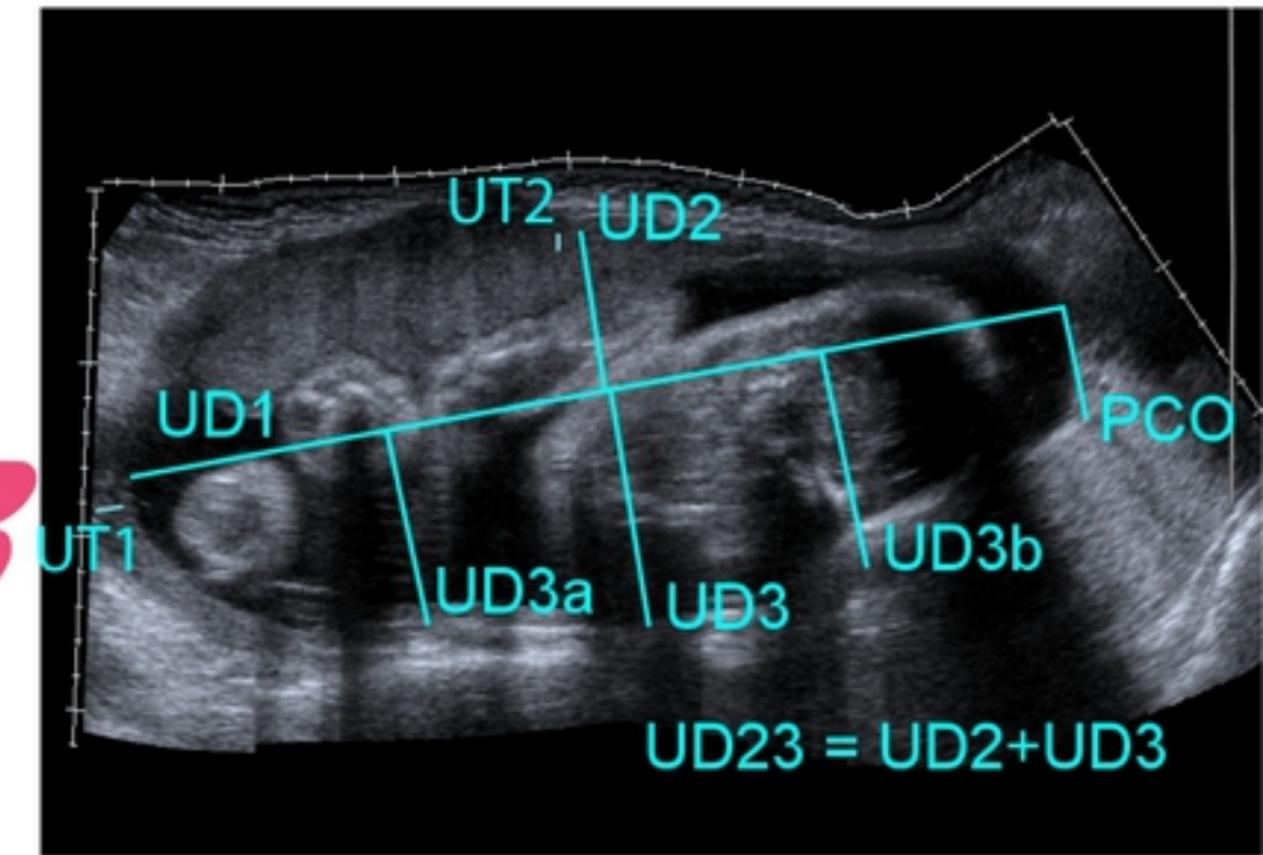
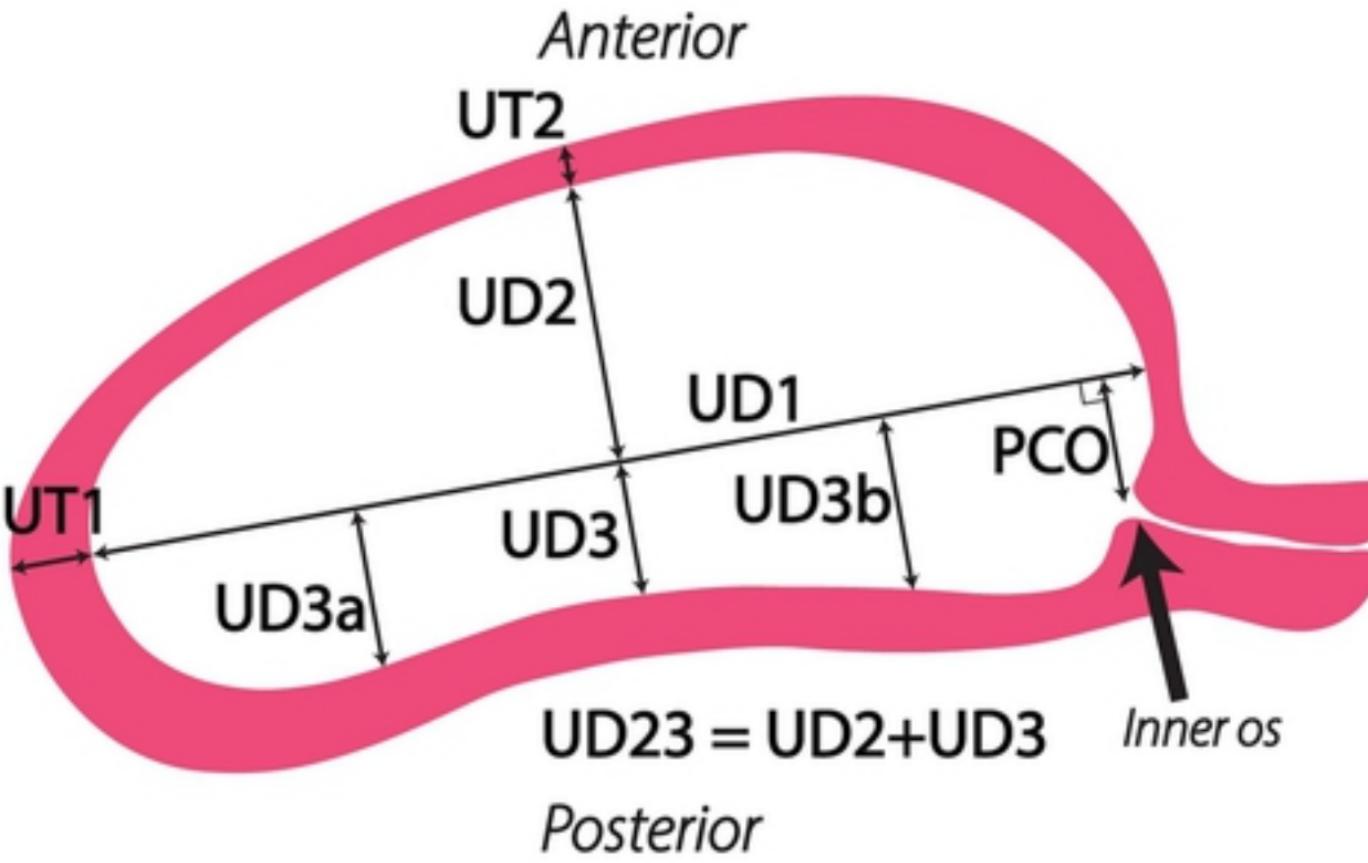
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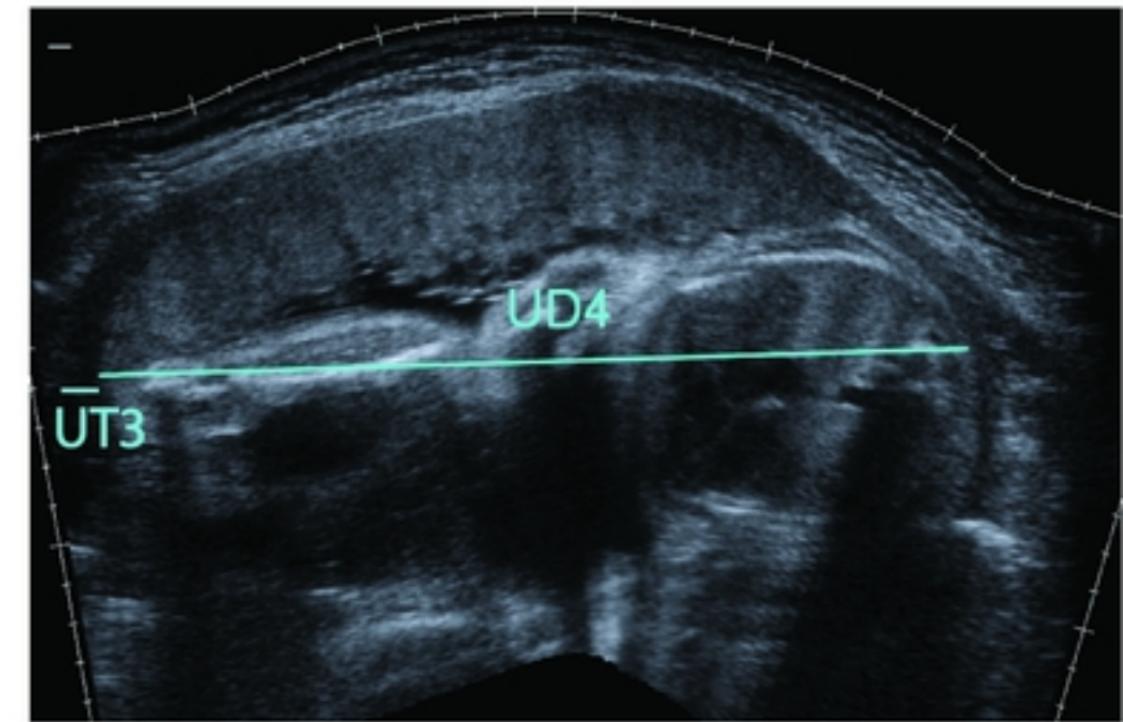
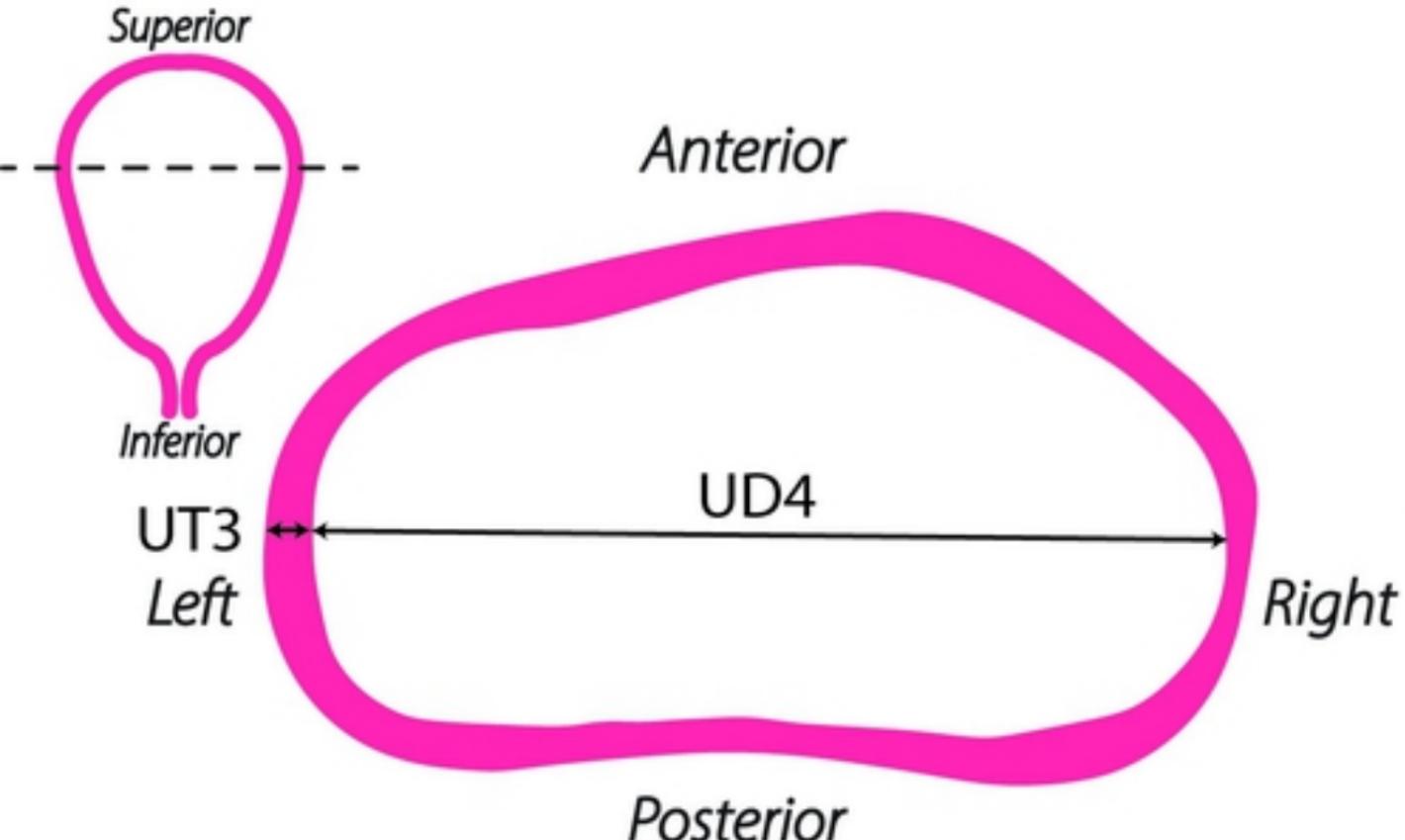
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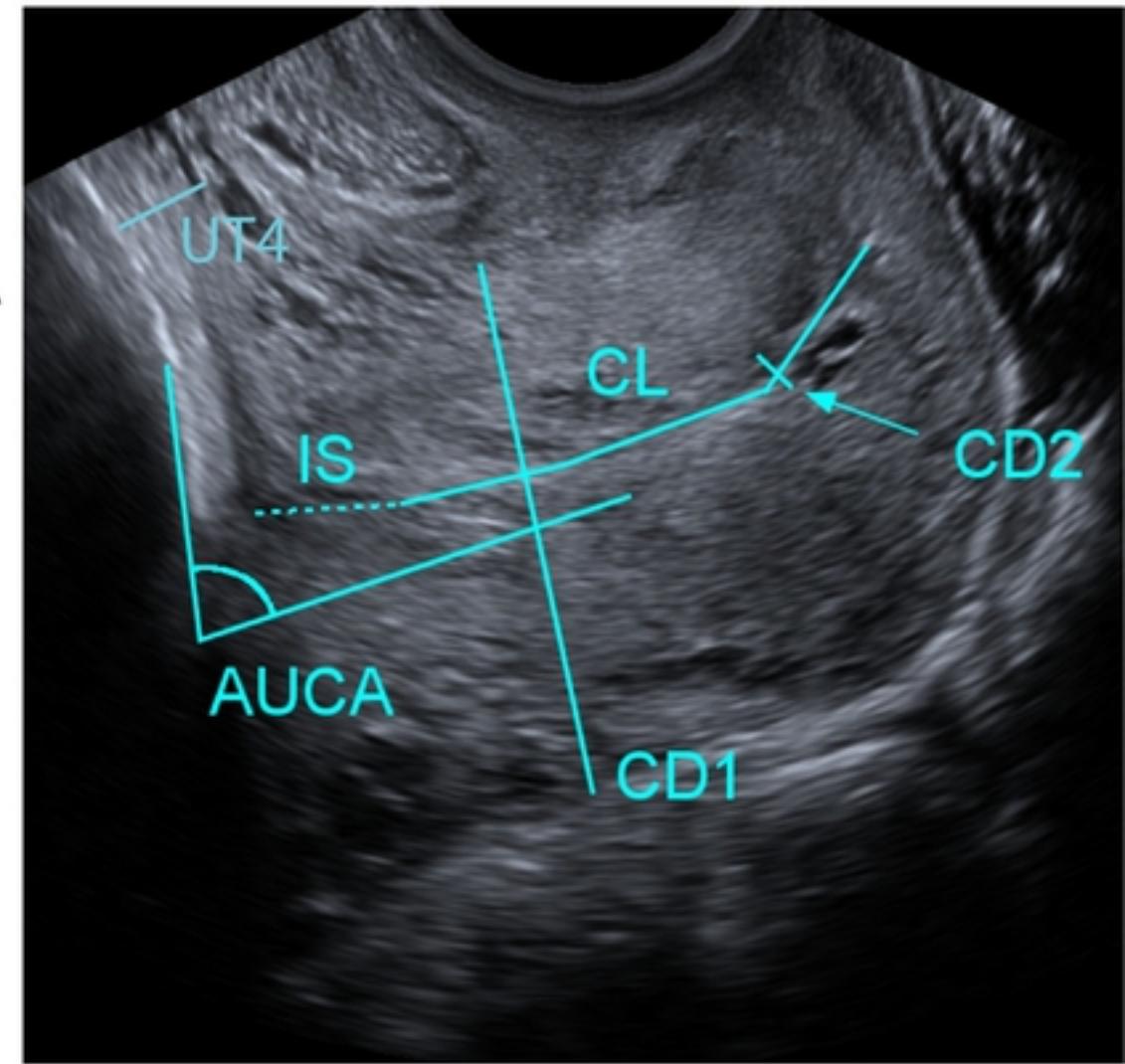
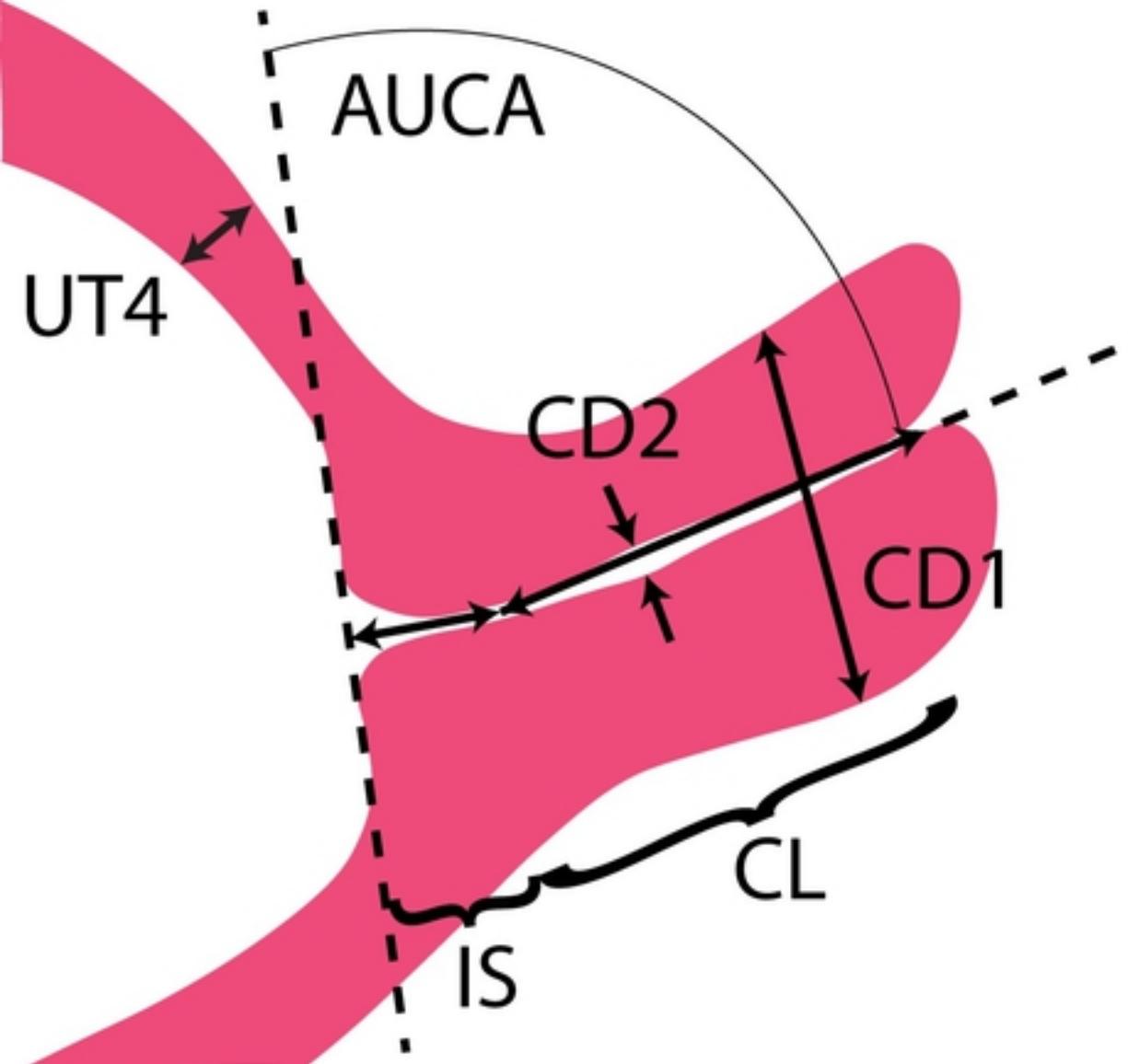




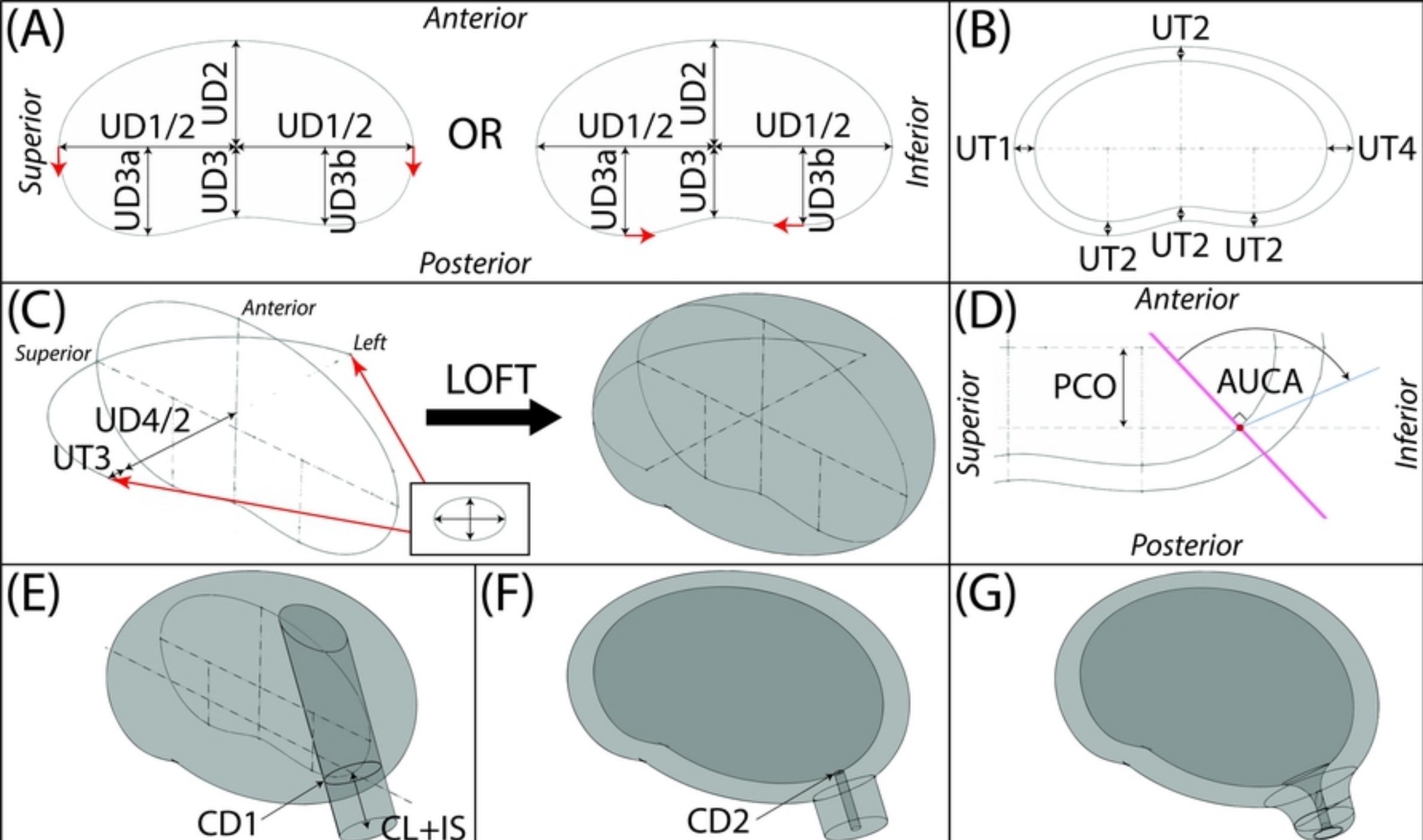
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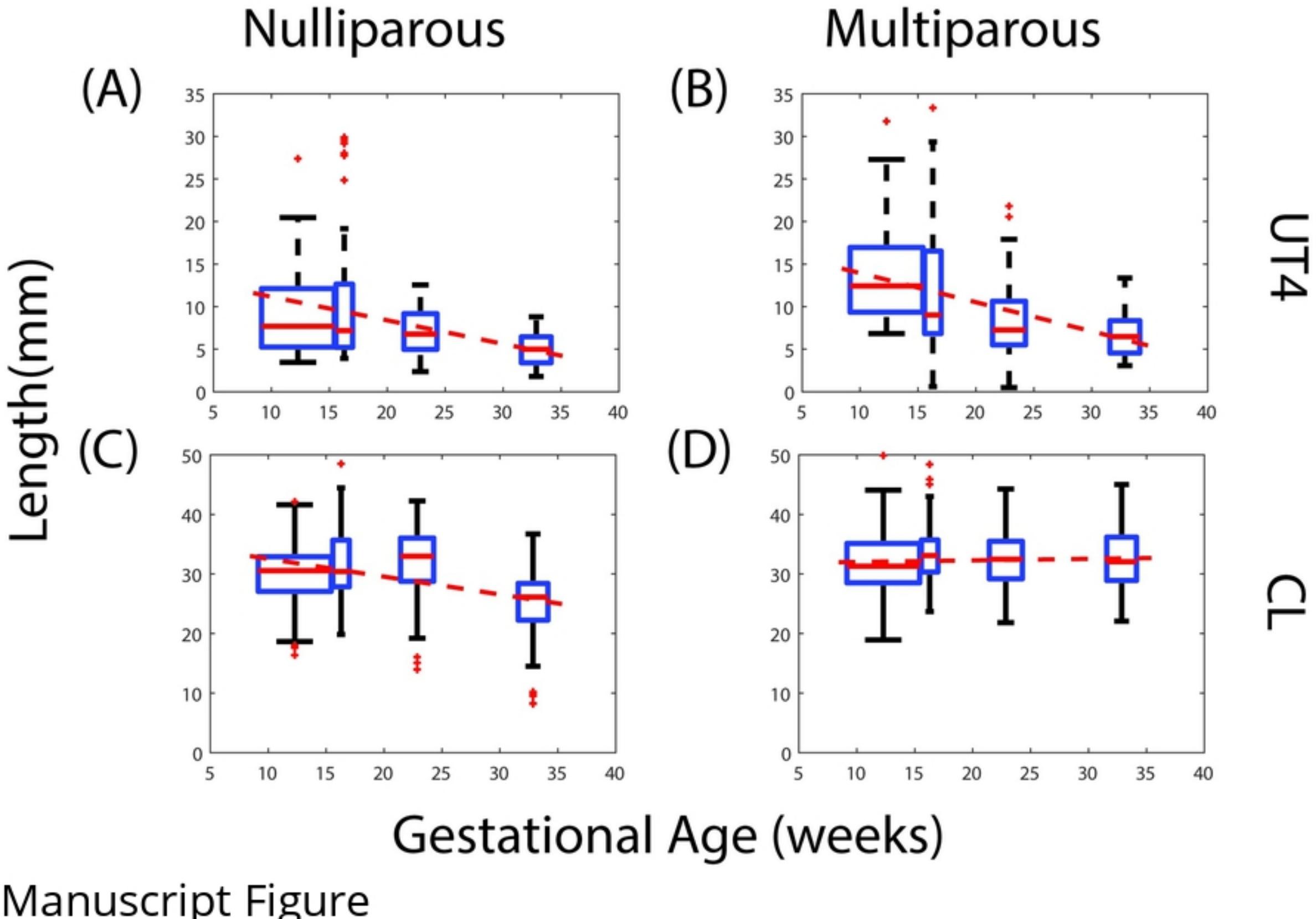
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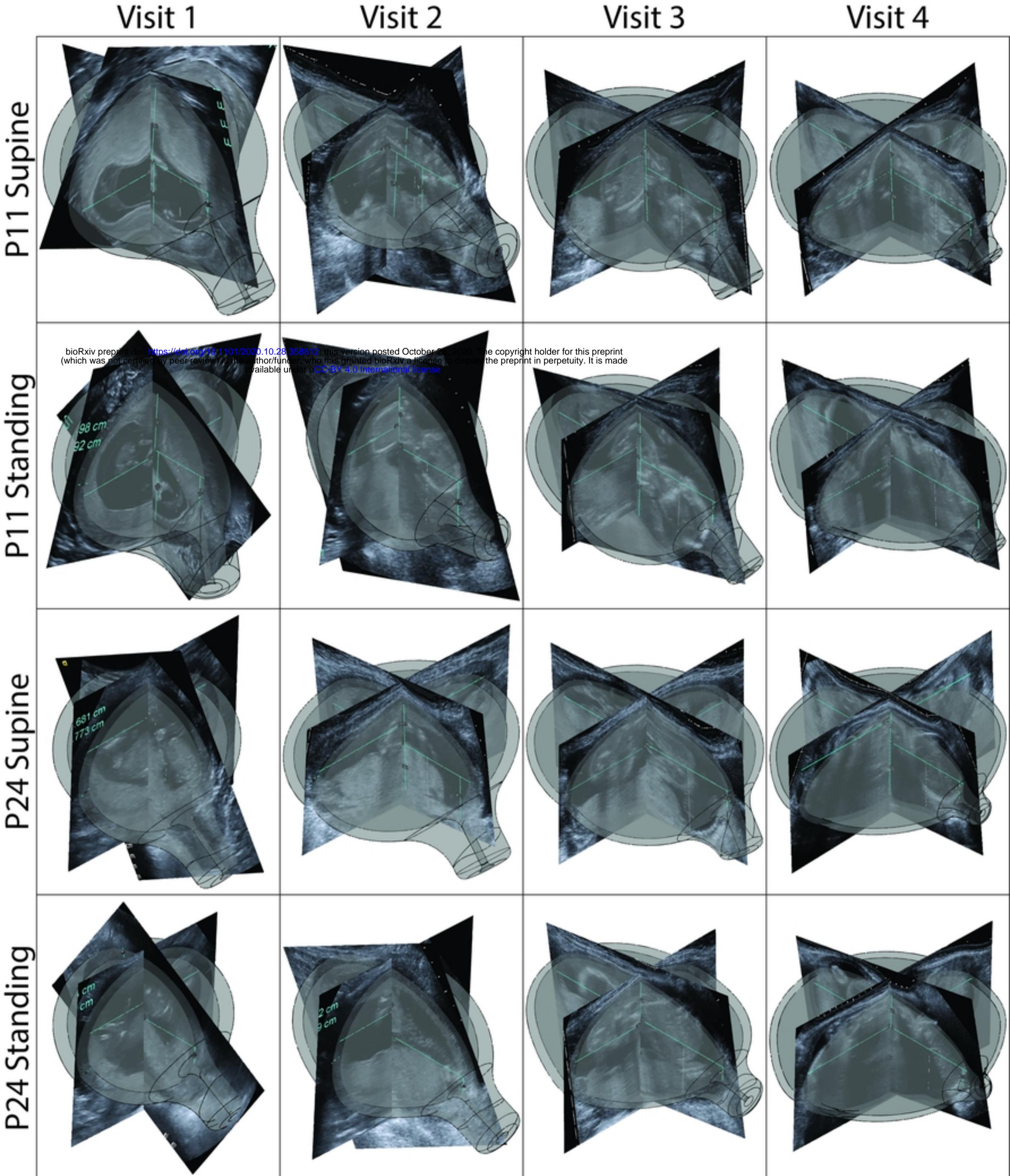


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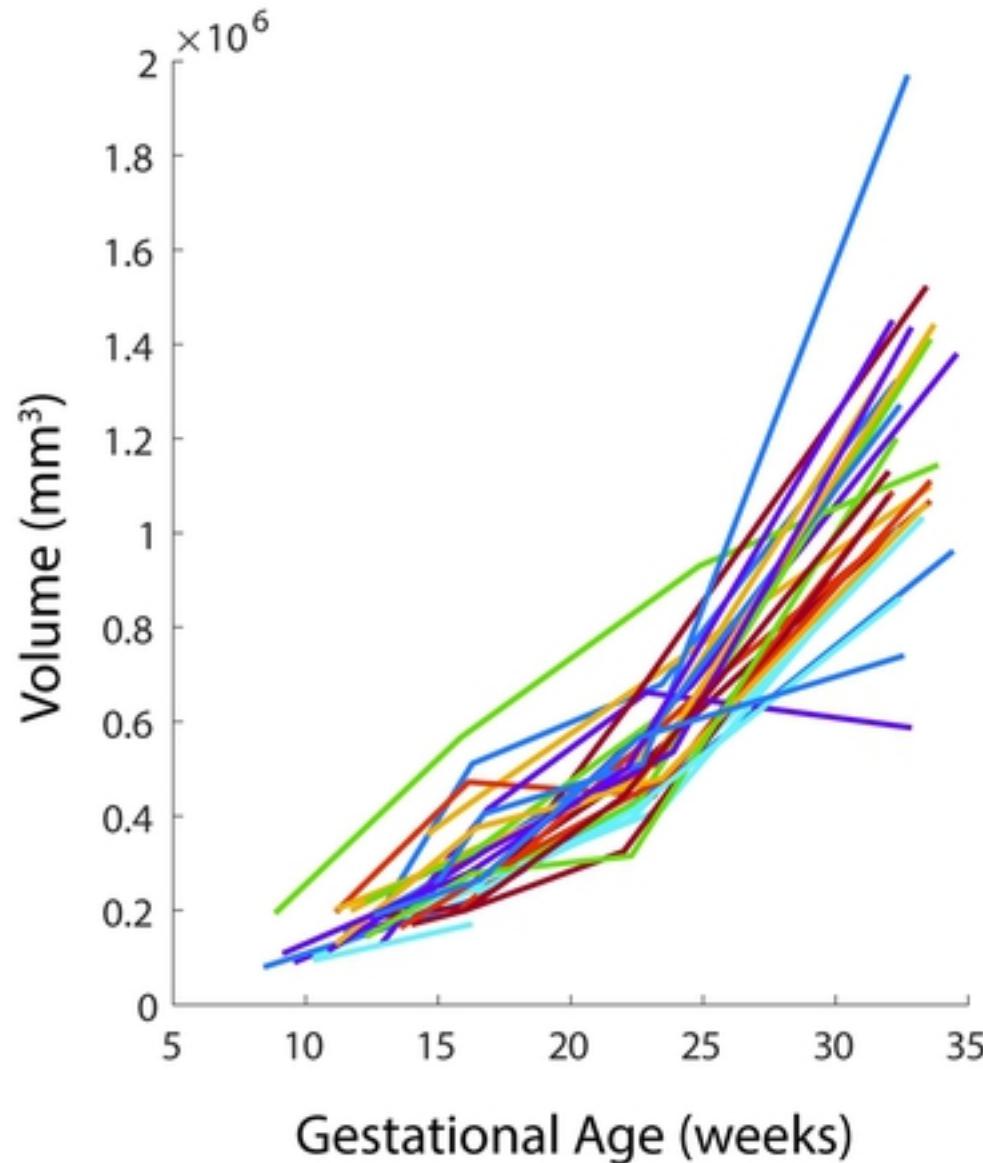
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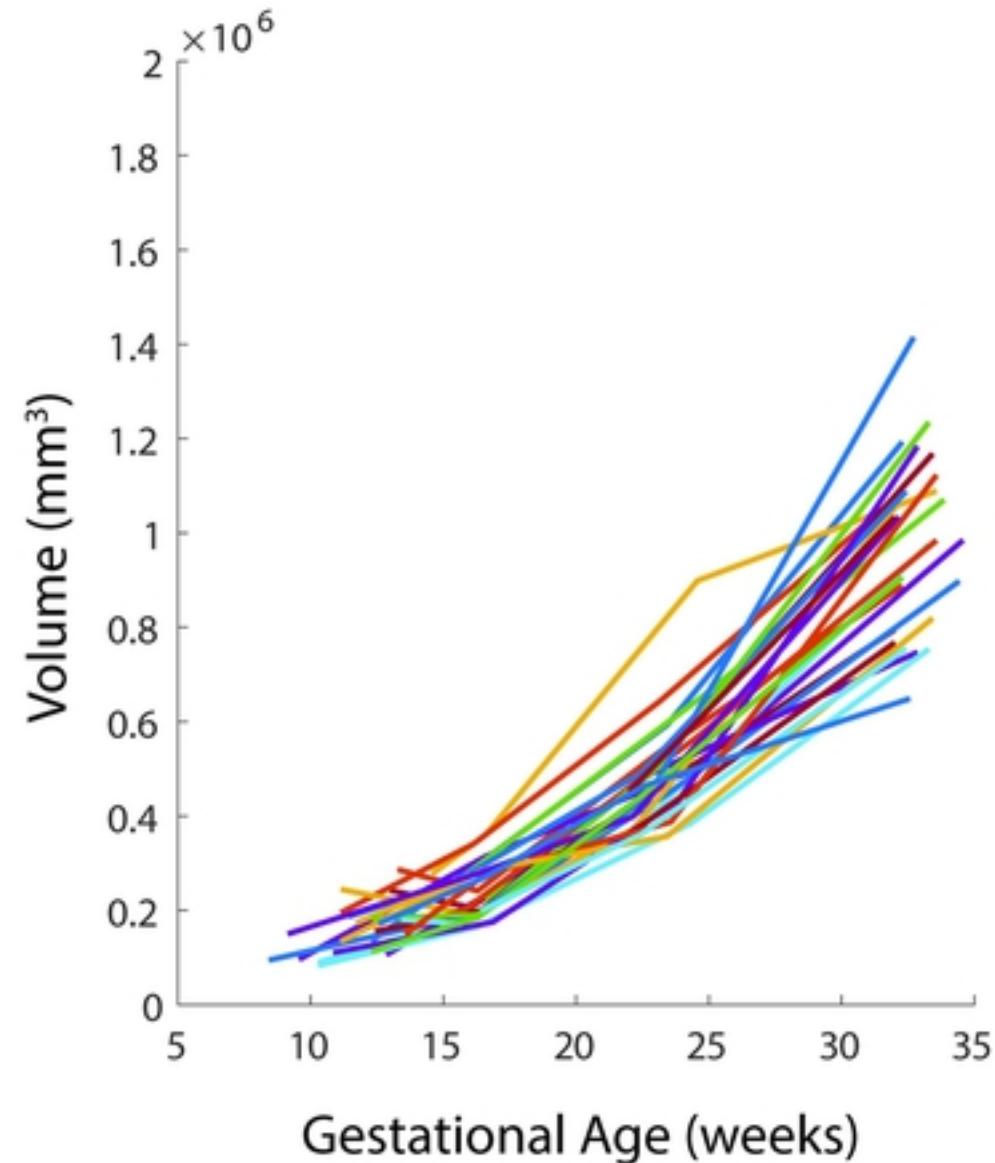


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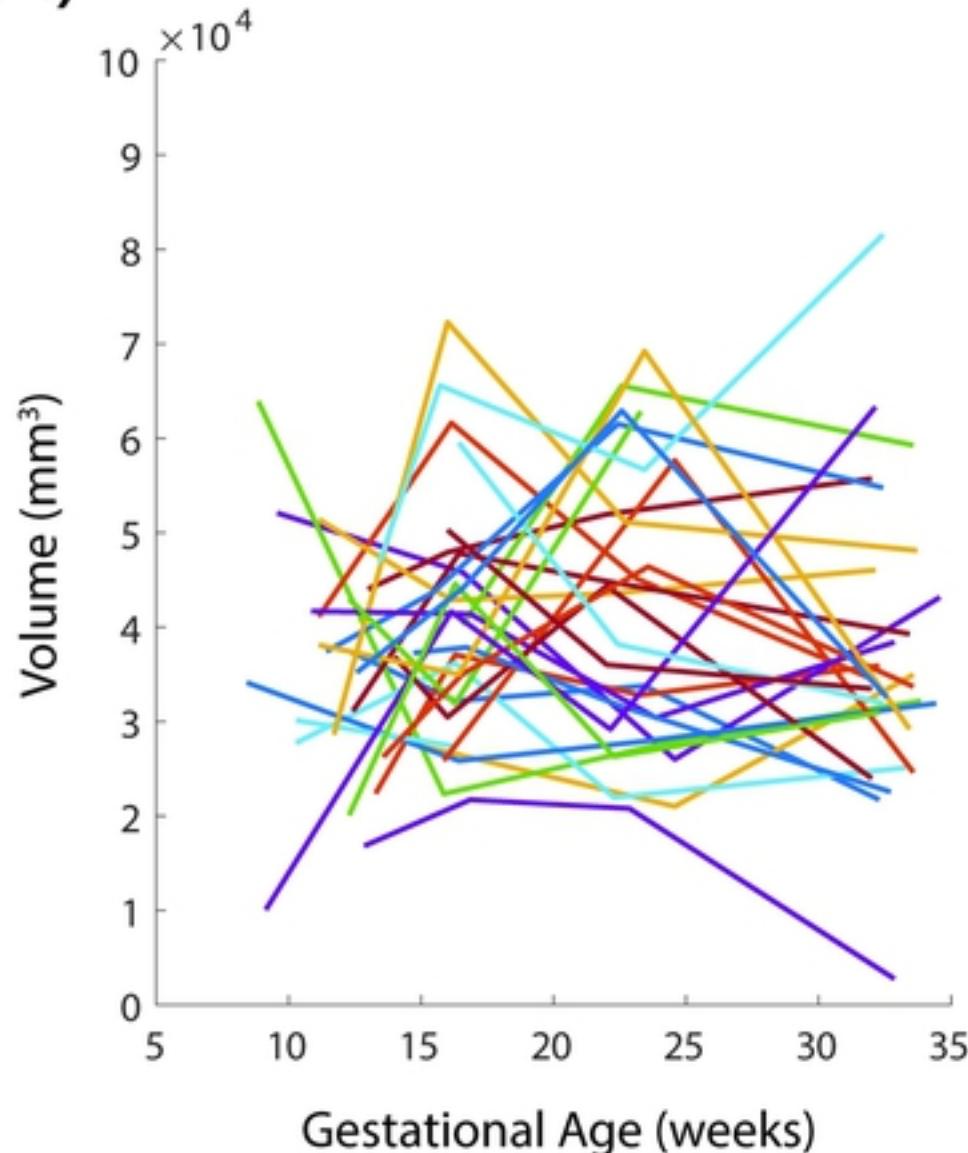


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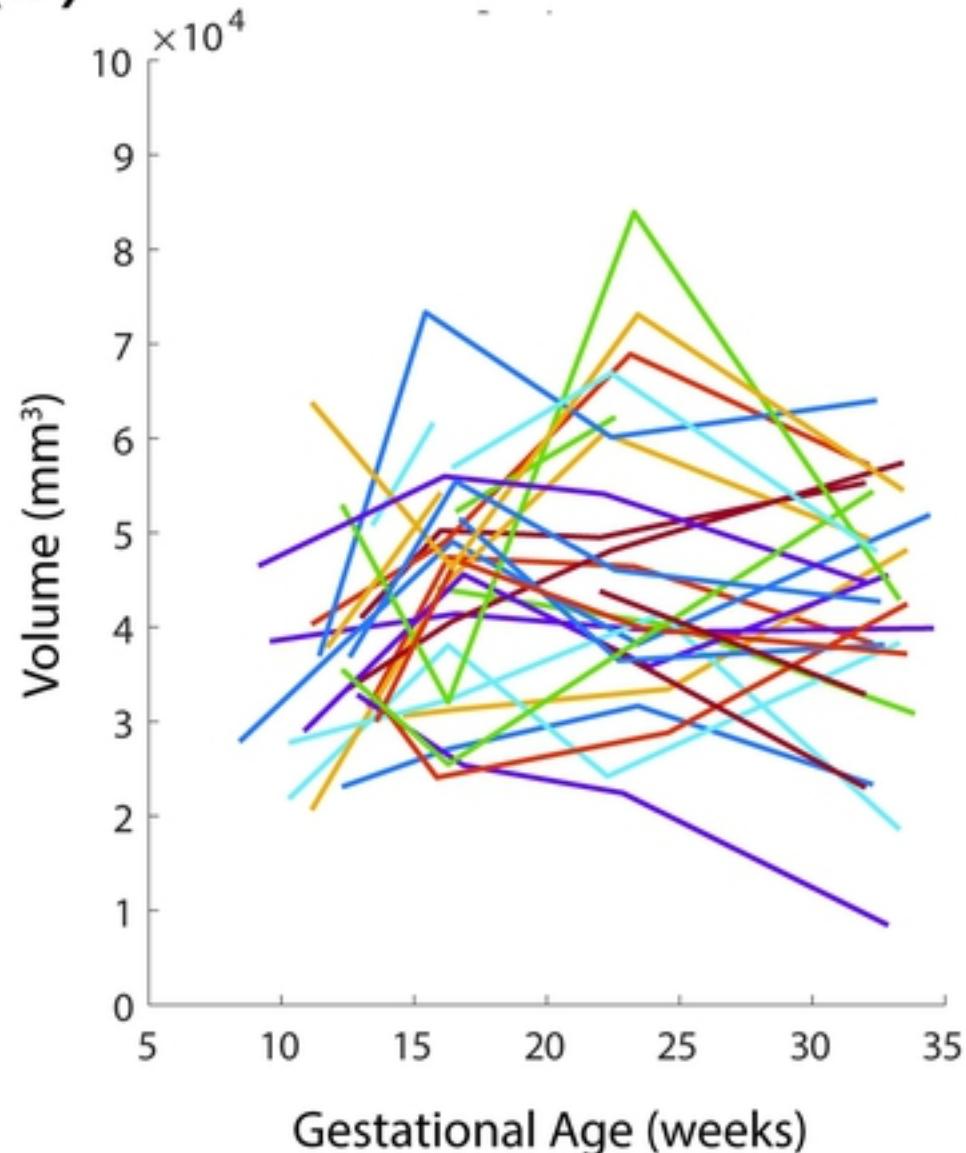


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