

FL-QSAR: a federated learning based QSAR prototype for collaborative drug discovery

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Abstract

Motivation: Quantitative structure-activity relationship (QSAR) analysis is commonly used in drug discovery. Collaborations among pharmaceutical institutions can lead to a better performance in QSAR prediction, however, intellectual property and related financial interests remain substantially hindering inter-institutional collaborations in QSAR modeling for drug discovery.

Results: For the first time, we verified the feasibility of applying the horizontal federated learning (HFL), which is a recently developed collaborative and privacy-preserving learning framework to perform QSAR analysis. A prototype platform of federated-learning-based QSAR modeling for collaborative drug discovery, i.e, FL-QSAR, is presented accordingly. We first compared the HFL framework with a classic privacy-preserving computation framework, i.e., secure multiparty computation (MPC) to indicate its difference from various perspective. Then we compared FL-QSAR with the public collaboration in terms of QSAR

modeling. Our extensive experiments demonstrated that (1) collaboration by FL-QSAR outperforms a single client using only its private data, and (2) collaboration by FL-QSAR achieves almost the same performance as that of collaboration via cleartext learning algorithms using all shared information. Taking together, our results indicate that FL-QSAR under the HFL framework provides an efficient solution to break the barriers between pharmaceutical institutions in QSAR modeling, therefore promote the development of collaborative and privacy-preserving drug discovery with extendable ability to other privacy-related biomedical areas.

Availability and implementation: The source codes of the federated learning simulation and FL-QSAR are available on the GitHub: <https://github.com/bm2-lab/FL-QSAR>

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1 Introduction

During the drug discovery process, predicting and prioritizing the properties of large numbers of compounds is an essential step in the early stage of drug discovery (Vamathevan, et al., 2019). In the pharmaceutical industry, QSAR is a commonly used in-silico technique to predict and investigate various properties of compounds, such as the compound affinity towards a target and the absorption, distribution, metabolism and excretion (ADME), etc, which can substantially reduce the experimental work needed here (Ma, et al., 2015).

Machine learning (ML) approaches provide powerful tools that can promote the data-driven decision making, speed up the process and reduce failure rates with abundant, high-quality data in drug discovery and development (Cohen, et al., 2018; Cruz-Roa, et al., 2017; Ding, et al., 2018; Rahman, et al., 2017; Wang and Gu, 2018). Generally speaking, increasing the training data can improve the performance of ML approaches. In the pharmaceutical industry, generating more data generally means more time and money costs (Ma, et al., 2020), however, the structure of the lead compounds in the development pipelines will not be exposed before marketing, which prevents the compound data sharing from one institute to each other. Therefore, although collaboration and data sharing between individual entities is expected to serve as a good strategy to save cost and promote drug discovery, such forms of collaboration have been limited by concerns on compound intellectual property and other related financial interests (Hie, et al., 2018).

Modern cryptography has provided partial solutions to this issue. Secure multiparty computation (MPC) is an increasing popular while classical encryption method that allow multiple entities to compute over their private datasets without revealing any information about pharmacological data (Aho, 1987; Yao, 1982). A quick while thorough survey indicates that MPC has been applied for genomic diagnosis (Jagadeesh, et al., 2017), Drug-target interaction (DTI) prediction (Hie, et al., 2018; Ma, et al., 2020) and genome-wide association study (GWAS) (Cho, et al., 2018). In the MPC framework, all participants must submit their data securely to the third party with encryptions (Bogdanov, et al., 2008). However, participants may not

want to share data with the third party, even though the data is encrypted. Meanwhile, other ethic and political issues remain under the MPC framework since countries around the world are strengthening laws to protect data privacy and security by prohibition of certain data transition across countries or organizations, even though the data is encrypted. Such regulations includes the GDPR implemented by the European Union (Voigt and Von dem Bussche, 2017) and CCPA enacted by California, U.S. (de la Torre, 2018) et c. Therefore, the traditional MPC framework remains facing the challenges under the constantly emerging new data laws and regulations.

Federated learning (FL) is a recently proposed collaborative paradigm to enable the data owners collaboratively train a model while any data owner does not expose its data to others (Kairouz, et al., 2019). FL was first proposed by Google (Konečný, et al., 2016; Konečný, et al., 2016; McMahan, et al., 2016), and then extended by Yang et al (Yang, et al., 2019). FL can be categorized into horizontal federated learning (HFL), vertical federated learning(VFL) and federated transfer learning(FTL) (Yang, et al., 2019) . HFL is applicable to the scenarios that data sets share the same feature space but differ in samples. VFL applies to the scenarios that data sets share the same sample space but differ in feature space. FTL is introduced in the scenarios that the two data sets differ not only in samples but also in feature space with only a small portion of the feature space and sample space overlapped (Yang, et al., 2019) (**Fig. 1**). In the pharmaceutical industry, the most common scenario is that different institutions often have the same type of data, i.e., the lead compounds in their

pipelines, which can be encoded with the same feature representations. The difference is that the compounds held by different institutions are different. Compared to VFL and FTL, HFL is obviously more suitable for the collaborations among pharmaceutical industry. Essentially, HFL is based on the traditional MPC framework with advantages that it passes encrypted model parameters to the server instead of encrypted raw pharmacological data, which provides a workable solution to the facing issues aforementioned.

In this study, we verified the feasibility of applying HFL to collaborative drug discovery, with the commonly faced QSAR modeling as a demonstration study. To the best of our knowledge, this is the first study to apply FL framework for collaborative drug discovery compared to traditional MPC ones. In our study, we simulated the scenario that parties have their private data, respectively, and trained a routine ML model with and without HFL. Comprehensive experiments indicated that in most cases, collaboration via HFL achieves almost the same performance as that of collaboration via the corresponding cleartext algorithm and significantly outperforms a single client via the corresponding cleartext algorithm. The FL-QSAR platform, which is designed as a prototype system for QSAR modeling under HFL is presented, served as a pioneer study to call for more attention and devoting in this area. To sum up, for the first time, our study demonstrated the effectiveness of applying HFL in QSAR modeling and proposed a prototype framework FL-QSAR with extendable ability. The FL framework and FL-QSAR developed in our study can be applied or extended to various drug-related learning problems involving collaboration and

privacy-preserving, promoting the development of collaborative drug discovery and privacy-related computing in pharmaceutical community.

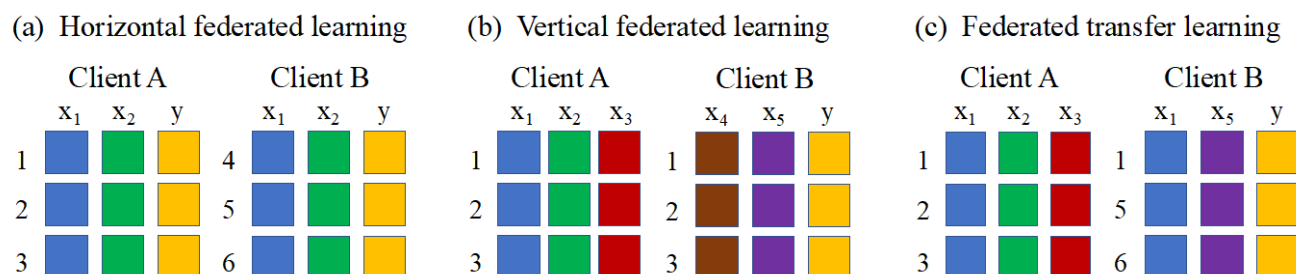


Fig. 1. Categorization of Federated Learning. (a) Horizontal federated learning. (b) Vertical federated learning. (c) Federated transfer learning. The term x_n donates the n_{th} feature of the feature descriptions of the sample, y is the sample label and n donates sample ID.

2 Methods

2.1 Traditional Secure MPC

Secure MPC is a designed protocol that allows multiple parties to compute a function on encrypted data and access only their own data and data that all parties agree to reveal. In secure MPC, the data owner encrypts its data by splitting it using random masks into n random shares that can be combined to reconstruct the original data. These n shares are then distributed between n parties. This process is called secret sharing (Ben-Or and Wigderson, 1988). We use a concrete example to better illustrate the secret sharing concept. Suppose that an integer x is the private data and Q is a big random integer. Then this client sends a random integer a between $-Q$ and Q to party S_1 and $(x - a \bmod Q)$ to party S_2 respectively, a and $(x - a \bmod Q)$ are called the two shares of x respectively. Then the parties can compute functions on the data by

operating on the secret shares and they can decrypt the final result by communicating the resulting shares among each other (Ma, et al., 2020).

2.2 Horizontal federated learning applied in FL-QSAR

We then introduced the HFL framework applied in FL-QSAR, as an alternative strategy for collaborative and privacy-preserving QSAR modeling compared to MPC.

The formal description of HFL is given as follows:

Define N data owners $\{F_1, \dots, F_N\}$. All of them would like to train a model by consolidating their respective data $\{D_1, \dots, D_N\}$. A conventional method, such as using the traditional MPC, is to put their data together and use $D = D_1 \cup \dots \cup D_N$ to train a model. A FL system is a process in which the data owners collaboratively train a model and no data owner F_i expose its data D_i to others. HFL is applicable when data sets share the same feature space while different samples. We denote the features space of the sample as X , the label space of the sample as Y and the sample ID space as I , all of whom constitute the complete training dataset (I, X, Y) . HFL can be represented as:

$$X_i = X_j, Y_i = Y_j, I_i \neq I_j, \forall D_i, D_j, i \neq j \quad (1)$$

A HFL system commonly assumes *honest* participants and security against an *honest-but-curious* server. An honest client means the client will not send fake or false data to the server. An honest-but-curious server means the server will not send fake or false data to clients, but is curious about information of clients and will mine sensitive information from the data (Yang, et al., 2019).

As shown in **Fig. 2**, in HFL system, participants with the same data structure learn a ML model collaboratively with the help of a server. To train a model to predict QSAR with HFL, our training process of such a system can be divided into the following four steps (Yang, et al., 2019):

- Step 1: Each participant trains its model on its own data, encrypts model parameters with secure MPC techniques, and sends encrypted results to server;
- Step 2: Server performs secure aggregation without obtaining information from any participant;
- Step 3: Server sends back the aggregated results to participants;
- Step 4: Participants update their models with the decrypted parameters.

In our implementation of FL-QSAR, we use the Crypten, which is a ML framework built on PyTorch (Paszke, et al., 2019) by applying secure MPC as its cryptographic part, to implement encryption of model parameters and their operations in secure aggregation.

It should be noted that traditional MPC allows the encrypted parameters to compute in a secure manner, and a solution is needed to aggregate these parameters to form the parameters in a federated learning model. One of the most common solutions to aggregation for FL is the Federated Averaging algorithm (McMahan, et al., 2016) (Algorithm S1). In our study, the basic idea of the algorithm is to average the parameters w and b of the neural network models applied in FL-QSAR for aggregating different clients.

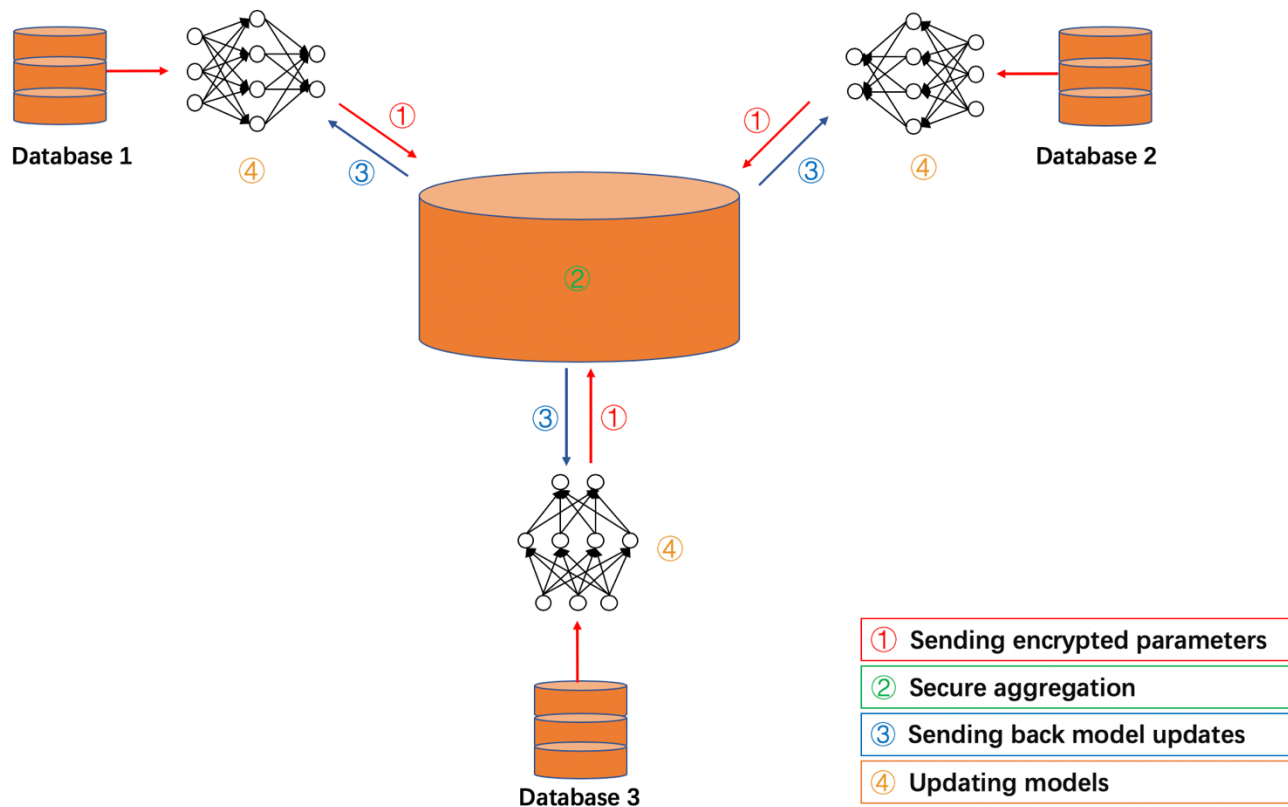


Fig. 2. The workflow of HFL. Each client trains its model on its private data, encrypts model parameter, and sends them to the server. The server performs secure aggregation and sends back the aggregated results to clients. At last, clients update their models with the decrypted parameters.

Algorithm S1 Federated Averaging. The K clients are indexed by k , T is total communication rounds, M is the number of local epochs, and η is the learning rate.

Server executes:

initialize w_0

for each round $t = 1, 2, \dots, T$ do

$S_t \leftarrow$ (random set of M clients)

for each client $i \in S_t$ in parallel do

$$w_{t+1}^i \leftarrow \text{ClientUpdate}(i, w_t)$$

$$w_{t+1} \leftarrow \sum_{k=1}^M \frac{1}{M} M_{t+1}^k$$

ClientUpdate(i, w):

for local step $j = 1, \dots, K$ do

$$w \leftarrow w - \eta \nabla f(w; z) \text{ for } z \sim P_i$$

return w to server

2.3 Benchmark data collection and federated learning simulation for FL-QSAR

In our study, we simulated the scenarios of two clients, three clients and four clients with and without HFL, respectively, to demonstrate the effectiveness of FL-QSAR in QSAR modeling. We take the simulation for 3 clients with and without HFL as an illustration example to demonstrate the process of simulation (**Fig. 3**). We use 15 benchmark datasets public available in Kaggle competition (Ma, et al., 2015) to validate our study. Each dataset is curated for a type of ADME assays or a target, and the detailed description of the datasets are listed in Table 1. Since the performance of the HIVPROT dataset in 15 datasets is extremely outrageous and unstable, it is excluded in the subsequent analysis. We randomly separated all available data into subsets and distributed them to clients, which were then regarded as the private data. Clients have the same amount of training data and testing data, with the chemical structure descriptors (Ma, et al., 2015) as feature descriptions and bioactivities as the

labels for the training data. Suppose that there are n instances in all available training data. Then a client owns a random subset of training data with $1/x \cdot n$ instances, where x stands for the number of clients.

Table 1. Benchmark data sets tested in FL-QSAR

Data sets	Data type	Description	Number of molecules	Number of feature descriptors
3A4	ADME	CYP P450 3A4 inhibition $-\log(\text{IC}_{50})$ M	50000	9491
CB1	Target	Binding to cannabinoid receptor 1 $-\log(\text{IC}_{50})$ M	11640	5877
DPP4	Target	Inhibition of dipeptidyl peptidase 4 $-\log(\text{IC}_{50})$ M	8327	5203
HIVINT	Target	Inhibition of HIV integrase in a cell based assay $-\log(\text{IC}_{50})$ M	2421	4306
HIVPROT	Target	Inhibition of HIV protease $-\log(\text{IC}_{50})$ M	4311	6274
LOGD	ADME	LogD measured by HPLC method	50000	8921
METAB	ADME	Percent remaining after 30 min microsomal incubation	2092	4595
NK1	Target	Inhibition of neurokinin1 (substance P) receptor binding $-\log(\text{IC}_{50})$ M	13482	5803
OX1	Target	Inhibition of orexin 1 receptor $-\log(\text{K}_i)$ M	7135	4730
OX2	Target	Inhibition of orexin 2 receptor $-\log(\text{K}_i)$ M	14875	5790
PGP	ADME	Transport by p-glycoprotein $\log(\text{BA}/\text{AB})$	8603	5135
PPB	ADME	Human plasma protein binding $\log(\text{bound}/\text{unbound})$	11622	5470

RAT_F	ADME	Log(rat bioavailability) at 2 mg/kg	7821	5698
TDI	ADME	Time dependent 3A4 inhibitions log(IC50 without NADPH/IC50 with NADPH)	5559	5945
THROMBIN	Target	human thrombin inhibition $-\log(\text{IC}_{50})$ M	6924	5552

Since the deep neural network has been extensively applied in QSAR modeling and proven to outperform other traditional ML methods (Preuer, et al., 2018), in our study, we just introduced a routine neural network for QSAR model and use parameter setting of DNN recommended by previous study as our hyperparameters in all experiments (Ma, et al., 2015). We consider chemical structure descriptors as the feature descriptions here and the numerical bioactivities are taken as the labels in FL-QSAR, therefore the whole QSAR modeling is taken as a regression problem. In order to improve the numeric stability, logarithmic transformation is applied to transform the features while Min-Max Normalization is performed to scale the labels. The number of training epochs is set to 180 at most and early stopping is adopted to prevent overfitting. In our experiments, we trained the neural networks ten times and averaged their predicted scores as the final results. It should be noted that basically the core ML model applied in FL-QSAR and model selection procedure are not our focus here, and users can try other ML models with different parameter settings and different compound feature descriptors in the future.

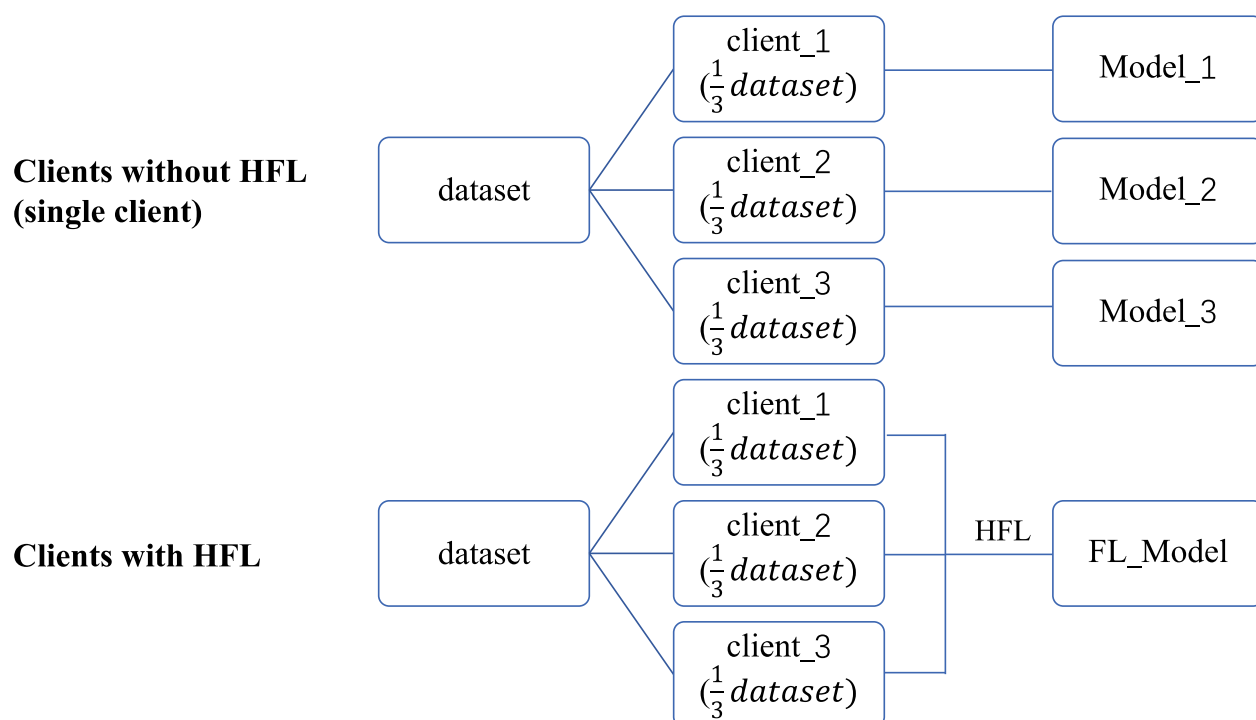


Fig. 3. The simulation for 3 clients with and without HFL as a demonstration example

3 Result

3.1 Comparisons between HFL and MPC

We made a comprehensive comparison between HFL and MPC, as MPC was also previously proposed for QSAR modeling (Ma, et al., 2020) (**Table 2**). First, HFL is a framework developed based on MPC and MPC is used to implement the encryption of model parameters as well as their operations in secure aggregation in the workflow of HFL. Second, MPC combines encrypted raw data of all clients together to train a model while HFL aggregates encrypted model parameters for all clients to train a model. Third, in terms of prediction performance, MPC is just identical to the

corresponding cleartext neural network since it essentially trains the model by combining all the training data from individual client, while HFL is expected to be a little bit lower, keep a tradeoff between model efficiency and data private-preserving. Therefore, the upper-bound of the performance of FL-QSAR is the performance of cleartext QSAR modeling by combining all the training data from individual client. Taking together, HFL can solve the issues or concerns by facing the increasing emerged data laws and regulations to prohibit data transmission, where MPC is not able to, and at the same time, reach relatively the same performance as those of combining individual client together for model training.

Table 2. A comprehensive comparison between MPC and HFL

	MPC	HFL
Framework relationship	/	Applying MPC for model parameters encryption
Content passed to the server	Encrypted raw data	Encrypted model parameters
Performance compared to cleartext learning algorithms with data sharing	Identical	Upper-bound
Applicable to data transmission regulations	No	Yes

3.2 Comparisons between public and HFL collaborations

In this section, we examined whether collaboration via HFL will cause the loss of the prediction accuracy and to what degree it will cause when compared to the collaboration via cleartext learning algorithms using all shared information. We used

the coefficient of determination (R^2) as the criterion to evaluate the performance for this regression task of QSAR modeling. As shown in Fig. 4a, it indicated that the loss of the prediction accuracy is increasing as the number of clients increases, and HFL for 4 clients is more unstable as 2 outliers appeared. This is expected, since increasing the number of clients will not increase the whole training data, while it increases the model instability because the errors occurred in every single client will influence the final aggregation results in QSAR modeling. Nevertheless, in most cases, HFL can achieve almost the same performance as collaboration via cleartext learning algorithms using all shared information. This can be seen in Fig. 4a that the loss for all scenarios are nearly zero. More details can be found in the Supplementary Table 1.

3.3 Comparison between HFL collaborations and a single client using private data

We also compared the prediction performance between a single client and that of HFL for 2 clients, 3 clients and 4 clients respectively. We found that collaboration by HFL achieved a significant improvement in R^2 and outperformed a single client using its private data (**Fig. 4b-4d**). This result demonstrated the effectiveness of HFL. Collaboration by HFL gained a substantially performance improvement than that of one client by using only its private data. More details can be found in the Supplementary Table 1.

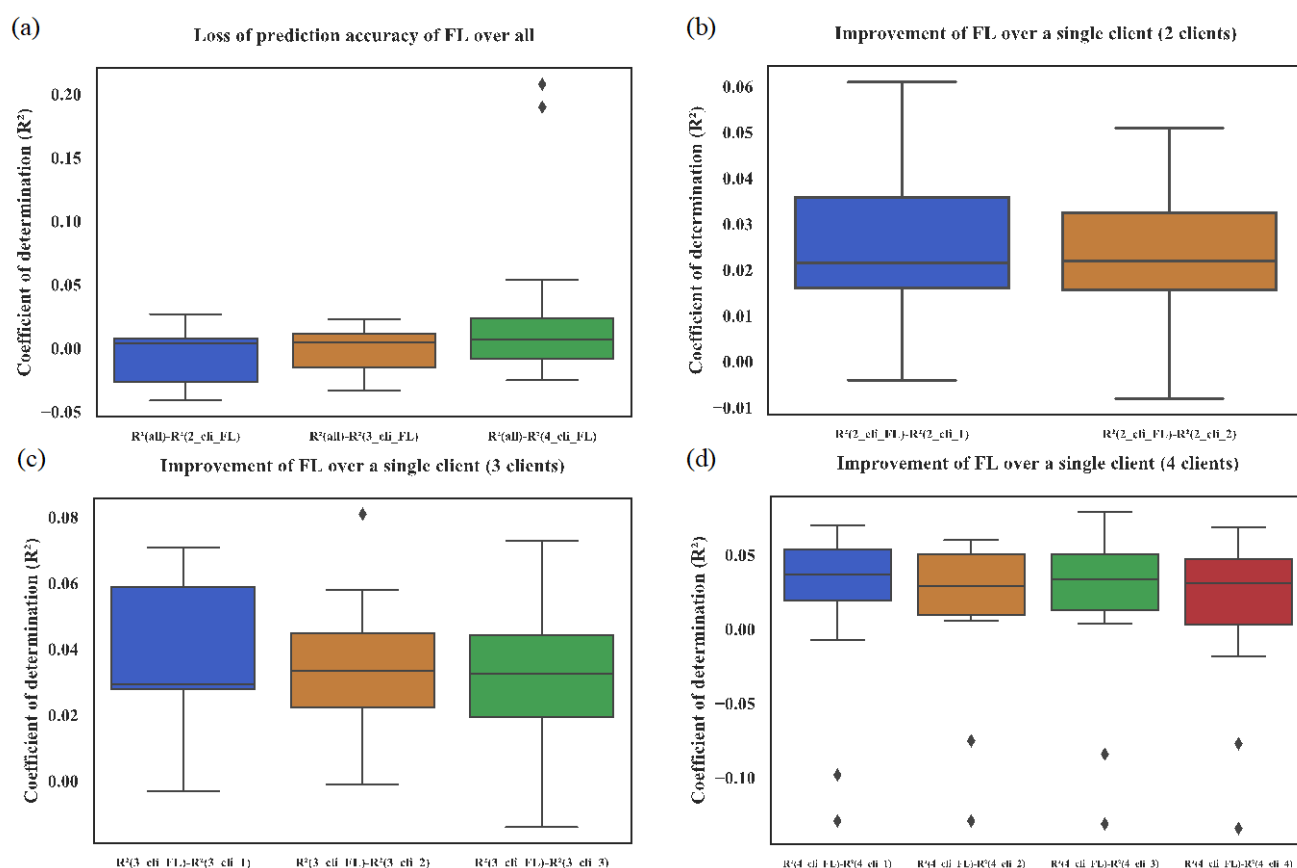


Fig. 4. The prediction performance of HFL. The term ‘all’ means that collaboration via cleartext learning algorithms using all shared information. The term ‘ n_cli_FL ’ means that collaboration of n clients via HFL and so on. The term ‘ n_cli_p ’ means that the p_{th} client of n clients and so on. (a) The loss of prediction accuracy of FL over all. (b) The improvement of HFL for 2 clients over a single client. (c) The improvement of HFL for 3 clients over a single client. (d) The improvement of HFL for 4 clients over a single client.

3.4 Implementation of FL-QSAR as a prototype for collective QSAR modeling

In this study, we proposed the FL-QSAR prototype under a HFL framework for collective QSAR modeling. FL-QSAR is designed as an user-friendly prototype for predicting QSAR under HFL with pyTorch implementation. Users just need to specify the training data, test data and the client number, and then the model training,

prediction and the final performance reports for each individual client as well as their collaborated one via HFL will be showed in the results files. FL-QSAR aims to help users with a better understanding of the workflow and the underline mechanism of applying HFL for QSAR modeling. FL-QSAR can be easily extended to apply other ML models for solving various drug-related learning tasks. Taking together, FL-QSAR is expected to provide great promotion for the development of collaborative drug discovery and privacy-related computing in pharmaceutical community.

4 Discussion

Several frameworks are presented for FL, such as FATE (<https://github.com/FederatedAI/FATE>), PySyft (Ryffel, et al., 2018), PaddleFL (<https://github.com/PaddlePaddle/PaddleFL>), etc. To the best of our knowledge, FATE is the only industrial-grade framework while other frameworks are more of theoretical value. Recently, OpenMined, which belongs to PySyft's development community, and the PyTorch partner, have announced a plan to develop a combined platform by integrating PyTorch, PySyft and CrypTen to accelerate privacy-preserving ML. However, a FL-based collective drug discovery platform is still lacking and FL-QSAR is served as a pioneer and prototype study to inspire the related community to further investigating FL for pharmaceutical applications.

Besides HFL, VFL and FTL are also expected to have potential utilities in collaborative drug discovery. For example, different pharmaceutical companies may

have their unique assay for leads discovery, therefore the distinct in-house data for the same compound in the development pipelines in different company can be generated. Integrating this information together from different institutes for the same set of compounds by VFL and FTL will accelerate the drug discovery procedure substantially, which is waiting to be explored in the future.

Another future improvement is that Federated Averaging Algorithm may be improved by aggregating parameters with a client-oriented way. Weighted average of parameters based on the training performance contributed by individual client may be an improvement direction of the Federated Averaging Algorithm, and this can be regarded as a fair way to evaluate the contribution of individual client. HFL may also be attacked by a malicious participant training a GAN (Hitaj, et al.). A malicious participant has the ability to reconstruct the training data of a given label. Therefore, how to guide the participants to make their own contributions properly and evaluate or reward their contributions fairly is important while challenging, waiting to be further explored.

In summary, biomedical community is expected to be beneficial from FL. Bio-medical data such as disease symptoms, gene sequences are very sensitive, private, and difficult to collect. If bio-medical data are collected together, the performance of ML models trained on the large scale bio-medical dataset are expected to be significantly improved, however, the collaborative and privacy-preserving learning framework applied here are needed to be carefully designed and investigated to address the facing challenges.

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Conflict of interest.

None declared.

Author contribution

Q.L. and Q.Y. conceived the study, S.Q.C., D.Y.S., G.H.C. implemented FL-QSAR.

Q.L., S.Q.C. and Q.Y. wrote the manuscript with assistance from other authors.

References

Aho, A.V. (1987) Proceedings of the Nineteenth Annual ACM Symposium on Theory of Computing. *Association for Computing Machinery*.

Ben-Or, M. and Wigderson, A. (1988). Completeness theorems for non-cryptographic fault-tolerant distributed computation. pages 1-10.

Bogdanov, D., *et al.* (2008). Sharemind: A framework for fast privacy-preserving computations. pages 192-206. *Springer*.

Cho, H., *et al.* (2018) Secure genome-wide association analysis using multiparty computation. *Nat Biotechnol*, **36**, 547-551.

Cohen, O., *et al.* (2018) MR fingerprinting Deep RecOnstruction NETwork (DRONE). *Magn Reson Med*, **80**, 885-894.

Cruz-Roa, A., *et al.* (2017) Accurate and reproducible invasive breast cancer detection in whole-slide images: A Deep Learning approach for quantifying tumor extent. *Sci Rep*, **7**, 46450.

de la Torre, L. (2018) A guide to the california consumer privacy act of 2018. *Available at SSRN 3275571*.

Ding, J., *et al.* (2018) Interpretable dimensionality reduction of single cell transcriptome data with deep generative models. *Nat Commun*, **9**, 2002.

Hie, B., *et al.* (2018) Realizing private and practical pharmacological collaboration. *Science*, **362**, 347-350.

Hitaj, B., *et al.* Deep Models Under the GAN: Information Leakage from Collaborative Deep Learning.

Jagadeesh, K.A., *et al.* (2017) Deriving genomic diagnoses without revealing patient genomes. *Science*, **357**, 692-695.

Kairouz, P., *et al.* (2019) Advances and open problems in federated learning. *arXiv preprint arXiv:1912.04977*.

Konečný, J., *et al.* (2016) Federated optimization: Distributed machine learning for on-device intelligence. *arXiv preprint arXiv:1610.02527*.

Konečný, J., *et al.* (2016) Federated learning: Strategies for improving communication efficiency. *arXiv preprint arXiv:1610.05492*.

Ma, J., *et al.* (2015) Deep neural nets as a method for quantitative structure-activity relationships. *J Chem Inf Model*, **55**, 263-274.

Ma, R., *et al.* (2020) Secure multiparty computation for privacy-preserving drug discovery. *Bioinformatics*.

McMahan, H.B., *et al.* (2016) Communication-efficient learning of deep networks from decentralized data. *arXiv preprint arXiv:1602.05629*.

McMahan, H.B., *et al.* (2016) Federated learning of deep networks using model averaging.

Paszke, A., *et al.* (2019). PyTorch: An imperative style, high-performance deep learning library. pages 8024-8035.

Preuer, K., *et al.* (2018) Fréchet ChemNet distance: a metric for generative models for molecules in drug discovery. *Journal of chemical information and modeling*, **58**, 1736-1741.

Rahman, R., *et al.* (2017) IntegratedMRF: random forest-based framework for integrating prediction from different data types. *Bioinformatics*, **33**, 1407-1410.

Ryffel, T., *et al.* (2018) A generic framework for privacy preserving deep learning.

arXiv preprint arXiv:1811.04017.

Vamathevan, J., *et al.* (2019) Applications of machine learning in drug discovery and development. *Nat Rev Drug Discov*, **18**, 463-477.

Voigt, P. and Von dem Bussche, A. (2017) The eu general data protection regulation (gdpr). *A Practical Guide, 1st Ed., Cham: Springer International Publishing.*

Wang, D. and Gu, J. (2018) VASC: Dimension Reduction and Visualization of Single-cell RNA-seq Data by Deep Variational Autoencoder. *Genomics Proteomics Bioinformatics*, **16**, 320-331.

Yang, Q., *et al.* (2019) Federated machine learning: Concept and applications. *ACM Transactions on Intelligent Systems and Technology (TIST)*, **10**, 1-19.

Yao, A.C. (1982). Protocols for secure computations. pages 160-164. *IEEE*.