

# <sup>1</sup> Origins of fractional control in regulated cell death

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## <sup>17</sup> Abstract

<sup>18</sup> Individual cells in clonal populations often respond differently to environmental changes; for binary phenotypes, such as cell death, this can be measured as a fractional response. These types of responses have been attributed to cell-intrinsic stochastic processes and variable abundances of biochemical constituents, such as proteins, but the influence of organelles has yet to be determined. We use the response to TNF-related apoptosis inducing ligand (TRAIL) and a new statistical framework for determining parameter influence on cell-to-cell variability through the inference of variance explained, DEPICTIVE, to demonstrate that variable mitochondria abundance correlates with cell survival and determines the fractional cell death response. By quantitative data analysis and modeling we attribute this effect to variable effective concentrations at the mitochondria surface of the pro-apoptotic protein Bax. Further, we demonstrate that inhibitors of anti-apoptotic Bcl-2 family proteins, used in cancer treatment, may increase the

32 diversity of cellular responses, enhancing resistance to treatment.

33 Isogenic populations of cells in homogeneous environments have the seemingly paradoxical  
34 capacity to generate many unique cell states. This ability is found in many, if not all, types of single  
35 celled organisms and in the distinct cell types of multicellular organisms. For example, *B. subtilis*  
36 cells were shown to independently and transiently switch between vegetative and competent states  
37 [1], hematopoietic progenitor cells can differentiate into either erythroid or myeloid lineages [2],  
38 and cancerous tissue maintain distinct sub-populations throughout the course of disease [3]. In  
39 all such cases, a cell's propensity for a particular state is attributed to the intrinsic stochasticity  
40 of low-copy number biomolecular reactions [4–6], or extrinsic variations in the abundances of its  
41 components [7–9]. Taken together it is clear that stochastic transitions of cell state that are driven  
42 by non-genetic sources of cell-to-cell variability (CCV) are fundamental to the maintenance of  
43 single cell populations, the function of distinct tissues, and structure of clinical lesions in diseases  
44 such as cancer.

45 One commonly studied source of CCV is protein abundance. Its premier status as a dominant  
46 source of non-genetic CCV is due to its stochastic production [6, 10], and the sensitivity of cellular  
47 decision-making machinery to variations in their components. For example, in biological signal  
48 transduction, information regarding the cell's environment is processed by a cascade of biomolec-  
49 ular reactions. Variation from one cell to another in any one of the corresponding biomolecules  
50 varies the signal magnitude across the population, making unique the cell's perception of environ-  
51 mental conditions and its corresponding response [11–14]. While it has been definitively shown  
52 that CCV in protein abundance influences cellular decisions, little attention has been given to other  
53 non-genetic sources of CCV.

54 There are numerous examples in which non-genetic and non-protein sources of CCV are con-  
55 jected to impact biological phenomena. For example, centrosome abundance [15], the size of  
56 the Golgi apparatus [16], and mitochondria abundance [17–20] all have been shown to vary from  
57 cell-to-cell. To determine if diversity in cell behaviors may be attributed to CCV in organelle abun-  
58 dance, our study focuses on the role of mitochondria in the context of TRAIL induced apoptosis.

59     Indeed, the abundance of mitochondria per cell has been shown to positively correlate with a  
60    cell's propensity for apoptosis [20]. The mechanism of this phenomena was attributed to CCV in  
61    protein abundances, which were previously shown to correlate with mitochondria abundance [21].  
62    However, this correlation is unlikely to be the entire story as a well known study demonstrated that  
63    the time to TRAIL-induced cell death of individual sister HeLa cells concomitantly treated with  
64    a potent inhibitor of protein translation, cyclohexamide, became less correlated with time [12].  
65    As protein translation is inhibited, the cause for the depreciation of this correlation is unlikely to  
66    come from temporal fluctuations in protein abundance and may be attributed to the fluctuations in  
67    mitochondria abundances.

## 68     **Results**

### 69     **Mitochondria density correlates with resistance to TRAIL**

70    To assess whether mitochondria abundance correlated with single cell sensitivity to TRAIL in-  
71    duced apoptosis (Figure 1A) we measured the binary life-or-death status and the abundance of  
72    mitochondria of individual cells by flow cytometry. During extrinsic apoptosis, TRAIL stimulates  
73    cell death by binding to its cognate death receptors on the cell surface forming a complex that  
74    activates Caspase 8 (Figure 1A), the so-called initiator caspase (IC). Active IC in turn causes Bax  
75    accumulation and polymerization on the outer membrane of mitochondria, forming pores [22, 23]  
76    which allow for the diffusion of pro-apoptotic molecules from the inter-membrane space of the mi-  
77    tochondria into the cytosol [24, 25]. These molecules activate a cascade which ultimately induces  
78    the activity of Caspase 3, the so-called executioner (EC) caspase [24, 25], which is responsible for  
79    triggering cell death. In effect, these molecules dynamically regulate each other's activity so that  
80    the continuous values of TRAIL concentration can be converted to a binary dead-or-alive response.

81       The human T-lymphoblastoid derived cells (Jurkat), a human breast adenocarcinoma cell line  
82    (MDA-MB-231), and HeLa cells were exposed to different doses of TRAIL for four hours, a time  
83    frame in which cells died readily but the single cell abundances per mitochondria remained largely  
84    unchanged (Supplementary Figures 1 and 2). For each dose of TRAIL we measured the abundance

85 of mitochondria and the cell state in single cells by concomitant labeling with a fluorescent An-  
86 nexin V and MitoTracker Deep Red in flow cytometry measurements (FCM). Living cells, Annexin  
87 V negative and MitoTracker high, are well separated from the dead cells, Annexin V positive and  
88 MitoTracker low and medium (Figure 1B, see Supplementary Figure 1 for complete gating strat-  
89 egy). Importantly, the fact that the living and apoptotic cell populations shared no MitoTracker  
90 population lead us to conclude that the apoptosis process corrupted MitoTracker signal. Conse-  
91 quently, the apoptosis process precludes assessment of mitochondria abundance by MitoTracker in  
92 Annexin V positive cells.

93 From the FCM and our live cell gate we confirmed that Jurkat and MDA-MB-231 cell lines  
94 were sensitive to TRAIL (Figures 1C,F) but HeLa cells were not as responsive (see Supplementary  
95 Figure 9). Furthermore, from fitting the Hill model to each dose response we found that these  
96 cell lines had vastly different sensitivities ( $IC_{50}$ ) to TRAIL,  $3.81 \pm 0.26$  ng/mL for Jurkat cells,  
97  $76.4 \pm 8.77$  ng/mL for MDA-MAB-231 cells and more than 300 ng/mL for HeLa cells. Because of  
98 this observation, we color-coded the effective abundance of TRAIL dose so that we may track the  
99 mitochondria abundance with the effective, as opposed to the actual, dose of TRAIL (Figures 1C-H  
100 and Supplementary Figure 9).

101 Next we found that mitochondria abundance of living cells is correlated with cell size, as mea-  
102 sured by forward scatter (Figures 1D,G). To eliminate analyzing effects due to cell size, as opposed  
103 to mitochondria, we focus our attention to the mitochondria density,  $\rho$ , defined as the MitoTracker  
104 signal normalized to FSC signal. With these data we estimated the probability density of single  
105 cell mitochondria density in live cells for each dose of TRAIL. Here we find that with successively  
106 increasing doses of TRAIL the probability distribution  $\rho$  becomes increasingly enriched for cells  
107 with high mitochondria density (Figures 1E,H). Moreover, we find that the degree of the enrich-  
108 ment is unique to each cell line - Jurkat cells are more readily biased in their mitochondria density  
109 than were the MDA-MB-231 and HeLa cells (for all HeLa cell analysis see Supplementary Note 6  
110 and Supplementary Figure 9).

111 We hypothesize that the observed enrichment of cells with high mitochondria density is es-

112 established by a differential sensitivity of single-cells to TRAIL. An intuitive result considering that  
113 the sensitivity of a signaling pathway to its cognate ligand is tuned by the abundances of its com-  
114 ponents. In apoptosis for example, we would expect that the number of TRAIL receptors on a  
115 cell's surface, the number of pro-caspase molecules, the number of Bax molecules, the number of  
116 mitochondria, etc contribute to that cell's response to a single dose of TRAIL. If each one of these  
117 molecules varied from one cell to the next, the so-called cell-to-cell variability (CCV), we should  
118 expect that the individual response of cells to TRAIL are unique.

119 Indeed, the probability density of  $\rho$  shows that the endogenous density of mitochondria vary  
120 from cell-to-cell (Figures 1E,H). If each cell's sensitivity to TRAIL were anti-correlated with mi-  
121 tochondria abundance we would expect an enrichment of high mitochondria density cells with  
122 TRAIL stimulation. Such an effect can be quantitatively studied by using the rule of probability.  
123 By applying Bayes' theorem we may associate the changes in the probability density  $\rho$  with the  
124 quantitative change of the fraction of living cells. From this simple property of probability, we  
125 were able to develop a quantitative strategy to gauge whether the observed endogenous variability  
126 of biological components are responsible for functional population diversity.

## 127 **Variability in all-or-none biological responses**

128 As found in other biological systems, e.g. MAPK and NF $\kappa$ B [26, 27], the conversion of a con-  
129 tinuous input to a binary response limits the influence of CCV in cellular components to CCV in  
130 sensitivity to perturbations. In apoptosis, each cell, with its unique concentrations of molecular  
131 components, should require a specific concentration of TRAIL to induce cell death. At the popu-  
132 lation level the diversity in single-cell sensitivities to TRAIL gives rise to the fractional control of  
133 cell death.

134 As an example, consider two separate ensembles of cells, one with near identical biomolecu-  
135 lar composition (low CCV) and the other with variable numbers of its components (high CCV).  
136 In the scenario where all components are near equal, the individuals will undergo the life-death  
137 transition at nearly the same dose of ligand (Figure 2A). In contrast, when CCV is relatively high,

138 the individual cells of the ensemble will transition from live to dead at diverse doses of TRAIL  
139 (Figure 2B). The resulting fractional control of the population response to TRAIL would then take  
140 a steep or gradual sigmoid shape, respectively.

141 This interpretation of the empirical dose response curve represents the cumulative distribution  
142 of single-cell sensitivities. From which, we may derive the corresponding probability density of  
143 single cell sensitivities. Indeed, from this simple interpretation, the empirical dose response curve  
144 of binary biological responses contains a complete statistical description of the functional diversity  
145 in the population. Fitting this dose response to a Hill function, we find that the mean sensitivity  
146 of single cells to a perturbation is simply the logarithm of the  $IC_{50}$ , and the variance of single cell  
147 sensitivities to be inversely proportional to the squared Hill coefficient (Figure 2C).

148 Matching the dose response parameters to statistical quantities is useful, because now we may  
149 use the tools of probability theory to analyze our data such as taking conditional moments. In  
150 context of TRAIL induced apoptosis we may ask what is the average sensitivity of cells given a  
151 specific mitochondria density. This statistical question is equivalent then to asking how does the  
152  $IC_{50}$  of individual cells change with the mitochondria density. Or we may ask, what is the vari-  
153 ance of single cells sensitivities given that we measured mitochondria density. Which, intuitively,  
154 quantitatively measures the remaining diversity in the population once we remove the contribution  
155 of mitochondria density. With this information we may then compute the fraction of the functional  
156 relevant population diversity attributable to a measured component.

## 157 **Decomposing sources of cell-to-cell variability**

158 Lets assume that the sensitivity of cells to TRAIL is wholly dependent on the biological compo-  
159 nents of the apoptotic signaling pathway. For simplicity lets designate the mitochondria density  
160  $\rho$  to be  $x_0$  and all other contributing components as  $x_1, x_2, \dots, x_m$ . *A priori* any mathematical  
161 function that describes the intricate relationships of these components and the dose of TRAIL to  
162 the single cell sensitivity ( $\kappa$ ) is unknown, however we may expand this *a priori* unknown function

163 to an arbitrary order by,

$$\kappa = \log(\text{IC}_{50}) + \sum_{i=0}^m k_i \delta \log(x_i) + \dots \quad (1)$$

164 where  $k_i = \partial \kappa / \partial \log(x_i)|_{\langle x_i \rangle}$  and  $\delta \log(x_i) = \log(x_i) - \log(\langle x_i \rangle)$  (see Supplementary Note 3  
 165 for details). The order in which we expand to will dictate the degree of complexity we wish to  
 166 understand. If we limit our understanding to first order, then the details of the specific pathway are  
 167 bundled into phenomenological parameters  $k_i$ . If then, we infer  $k_i$  from data, we can estimate the  
 168 extent in which each component contributes to a cell's sensitivity to TRAIL.

169 Indeed, Eq. 1 provides a framework for constructing a single cell interpretation of the Hill  
 170 model, which incorporates the abundance of biological components with the stimulation strength.  
 171 The biological species are introduced into the Hill model parameters by their influence on the  
 172 first and second statistical moments of single cell sensitivities,  $\kappa$ . For example, incorporating our  
 173 measurements of mitochondria density  $\rho$  to the  $\text{IC}_{50}$  amounts to computing the average sensitivity  
 174 conditioned on mitochondria density,

$$\log(\text{IC}_{50}(\rho)) = \log(\text{IC}_{50}) + k_\rho \delta \log(\rho). \quad (2)$$

175 Then, in like fashion, the resulting Hill coefficient comes from estimating the variance of sensitiv-  
 176 ities conditioned on mitochondria density,

$$n_\rho = \frac{\pi}{\sqrt{3 \sum_{i=1}^m \sigma_{\kappa|i}^2}} \quad \text{with} \quad \sigma_{\kappa|i}^2 = k_i^2 \sigma_i^2 \quad (3)$$

177 and  $\sigma_i^2$  representing the variance of the  $i^{th}$  biological component. If we apply the moments from  
 178 our first-order expansion (Eqs. 2,3) to the Hill model we arrive at our single cell Hill model,

$$P(\text{alive}|\rho, T) = \frac{(\rho / \langle \rho \rangle)^{k_\rho n_\rho}}{(\rho / \langle \rho \rangle)^{k_\rho n_\rho} + ([T]/\text{IC}_{50})^{n_\rho}}. \quad (4)$$

179 Eq. 4 gives us a detailed understanding on the influence of mitochondria density, or in general  
 180 any measured components. If, for example, mitochondria density does not contribute to the cell's  
 181 sensitivity to TRAIL then  $k_\rho = 0$  and Eq. 4 reduces to the standard dose response Hill function. If

182 however  $k_\rho$  is not zero and positive, then mitochondria density effectively promotes cell survival,  
183 and if  $k_\rho$  is negative then it increases the effectiveness of TRAIL. Together we can probe the influ-  
184 ence of each measured component at unprecedented resolution. We call this strategy DEPICTIVE,  
185 which is an acronym for DEtermining Parameter Influence on Cell-to-cell variability Through the  
186 Inference of Variance Explained.

187 To see this in detail, lets consider an example of an arbitrary pathway consisting of three com-  
188 ponents that takes  $s$  as input and provides a binary output  $y$  (Figure 3A). We then make a synthetic  
189 data set representing virtual single cell flow cytometry measurements for different doses of  $s$  (Fig-  
190 ure 3B). Using these data, we can compute the populations response to the stimulation, and due to  
191 the single cell nature of the data can interrogate the influence of each molecular constituent. The  
192 distribution of biological species  $x$  does not change whether we subset single cells upon their state  
193  $y$  (Figure 3C). Consequently,  $x$  must not contribute to each cells sensitivity to  $s$ , a fact corrobo-  
194 rated by  $P(y = 1|x, s)$  being invariant to the abundance of  $x$ . Unlike species  $x$ , species  $z$  and  $q$   
195 do influence the cell's behavior, which is apparent in analyzing the single cell data. Intuitively, the  
196 changes of the distribution of molecular components conditioned by cell state is the signal required  
197 for inferring each parameter  $k_i$  from (Eq.1).

198 Inferring each of the  $k_i$  in the simulation data is trivial, because we have measurements of  
199 each biological component for each cell state  $y$ . Uniquely, our experimental data consists of Mito-  
200 Tracker measurements from live cells exclusively. This was because MitoTracker Deep Red signal  
201 is dependent on the electro-chemical properties of the mitochondria, which are different for live  
202 and dead cells. To infer the values of  $k$  from such data we developed a new inference strategy  
203 for semi-supervised logistic regression and embed it as module within the DEPICTIVE statistical  
204 framework (see Supplementary Note 3.3 for details). We apply our method to the synthetic data  
205 that is analogous to our measurements, that is the measurements associated with each virtual cell  
206 with a binary label  $y = 1$ . The filled regions of the curves in  $P(y = 1|u, s)$  for  $u = x, z$ , or  $q$  (Fig-  
207 ure 3C) represent the model predictions from inferred  $k_u \pm 3$  standard deviations. These inferred  
208 parameters were then used to infer the single cell dose functions (Figure 3D) with qualitatively

209 excellent agreement. Quantitatively, we see that we can infer the conditional Hill coefficients (Figure  
210 3E), the corresponding variances explained (Figure 3F), and lastly the dependence of the single  
211 cell sensitivities on each biological component (Figure 3G).

## 212 **Mitochondria density is a source of cell-to-cell variability**

213 We apply our new statistical framework, DEPICTIVE, to quantitatively dissect the dependence  
214 of single cell sensitivities to TRAIL with mitochondria density (Figures 1E,H). We see that the  
215 fractional response of the Jurkat cells to each dose of TRAIL,  $P(\text{alive}|\rho, T)$ , is strongly dependent  
216 on mitochondria density (Figure 4A, see Supplementary Figures 3-5 for goodness-of-fit analy-  
217 sis). Moreover, we see that the single cell dose response curve translates from low TRAIL to  
218 high TRAIL doses with increasing mitochondria density (Figure 4B). The MDA-MB-231 cells  
219 fractional response (Figures 4C,D) is less steep than that of Jurkat, indicating that the single cell  
220 sensitivities of MDA-MB-231 cells to TRAIL are not as sensitive to CCV in mitochondria density  
221 as Jurkat (see Supplementary Figures 6-8 for goodness-of-fit analysis). A result that can be sum-  
222 marized by plotting the  $IC_{50}(\rho)$  for each cell line (Figure 4E). Moreover, we find that 30% and  
223 2% of the diversity in single-cell sensitivities to TRAIL may be attributed to mitochondria density  
224 in Jurkat and MDA-MB-231 cells, respectively (Figure 4F).

## 225 **Bax concentration dependence on mitochondria surface area**

226 To gain mechanistic insight in the functional role of mitochondria density in the cell death decision,  
227 we developed a coarse-grained dynamic model of apoptosis (Figure 5A). Our description aims to  
228 reproduce the dominant dynamical features of initiator caspase reporter protein (IC-RP) first mea-  
229 sured and published by [24]. These being a slow but accelerating initial increase of IC followed by  
230 a fast increase in both IC and EC. To such end our model includes: i) a slow auto-catalytic increase  
231 in IC activation, ii) a quasi-steady-state approximation for Bax pore formation dynamics and mi-  
232 toochondrial outer membrane permeabilization (MOMP), and iii) the strong positive feedback from  
233 EC to IC (see Supplementary Note 5 for details).

234 We conjectured that TRAIL induced activation of IC in Jurkat and MDA-MB-231 cells match

235 the biphasic increase of IC-RP measured in HeLa cells (Albeck et al. 2008b), but differ in their  
236 propensity to form Bax pores (Figures 5B,C). Specifically, we consider unique susceptibilities of  
237 Bax pore formation to Bcl-2 mediated inhibition for each cell line. As Bax pores reside in the mi-  
238 toochondria, the effective Bax concentration for a given amount of Bax decreases with mitochondria  
239 density. Implementing this insight into the model equations we see that the influence of mitochon-  
240 dria density can be understood through the corresponding bifurcation diagrams (Figures 5D,E).

241 The dynamic properties of IC in MDA-MB-231 cells in the absence of TRAIL are either  
242 bistable or monostable depending on mitochondria density. In these diagrams, the high IC fixed  
243 point corresponds to cells that have integrated sufficient signal for MOMP and consequently repre-  
244 sent apoptotic cells. Cells with relatively low mitochondria density are bistable and may undergo  
245 apoptosis only if their IC abundance exceeds a critical amount designated by the dashed line (Fig-  
246 ure 5D). This bistable region does not preclude cell death - cells may acquire sufficient abundances  
247 of IC for death by fluctuations in biomolecular reactions. Indeed, the likelihood of such an event  
248 decreases with the difference of IC abundance between the unstable fixed point (dashed line) and  
249 low IC stable fixed point (solid line). Meanwhile, cells with relatively high mitochondria den-  
250 sity only have a single fixed point of low IC, indicating that these cells will never spontaneously  
251 undergo apoptosis in the absence of TRAIL.

252 In contrast, the bifurcation diagram representing Jurkat cells shows three distinct regions (Fig-  
253 ure 5E). These being cells with: 1) low density of mitochondria having a single fixed point of  
254 high IC and consequently all die; 2) medium density of mitochondria are bistable, for which, the  
255 fractional response to TRAIL decreases with the concomitant increase in the IC unstable fixed  
256 point and mitochondria density; and 3) high density of mitochondria are monostable with low IC  
257 abundances, hence all cells survive. Next, we extend these analyses to the full range of TRAIL  
258 doses.

259 The influence of increasing TRAIL dose in each cell type specific parameterized model is ev-  
260 ident in their bifurcation diagrams. MDA-MB-231 cells respond to TRAIL by increasing the IC  
261 abundance of the lower fixed point (Figure 5F). In doing so, cells with mitochondria density in the

262 bistable region equally increase their susceptibility to cell death from fluctuations in IC abundance.  
263 The Jurkat model's response to TRAIL exhibits an increase of the density of mitochondria that sep-  
264 arates the monostable high and bistable IC abundance regions (Figure 5G). Therefore, an individual  
265 cell's mitochondria density determines its sensitivity to TRAIL induced cell death. Together, these  
266 model-based observations propose an explanation for how CCV in mitochondria density influences  
267 the response of Jurkat but to a lesser extent MDA-MB-231 cells to TRAIL (Figures 5H,I).

## 268 **Sensitizing MDA-MB-231 cells to CCV in mitochondria density**

269 In inspecting the model parameters associated with each cell type, we noticed that MDA-MB-231  
270 cells were more susceptible to Bcl-2 mediated inhibition of Bax pore formation than Jurkat. We  
271 hypothesized that this effect would be abated by incorporating a small molecule inhibitor to Bcl-2  
272 in MDA-MB-231 cells (Figure 6A, see Supplementary Note 5.1 for derivation). By incorporating  
273 Bcl-2 inhibition, we found that the sensitivity of the fractional response of the cell population to  
274 TRAIL increases (Figure 6B). Furthermore, and as intuited, Bcl-2 inhibition increased the depen-  
275 dence of single-cell sensitivities to TRAIL on mitochondria density (Figure 6D). We corroborated  
276 these theoretical predictions by measuring the influence of the clinically relevant small molecule  
277 inhibitor of Bcl-2 family proteins ABT-263 [28] (Figures 6C,E, see Supplementary Figures 6-8 for  
278 goodness-of-fit analysis). Remarkably, Bcl-2 inhibition alone increased the variance of sensitivi-  
279 ties attributable to mitochondria density from 0% to 40% (Figure 6F).

## 280 **Discussion**

281 We have unveiled a connection in the cell-to-cell variability of mitochondria density to the frac-  
282 tional control of TRAIL induced cell death. Importantly, we find that the dependency of single  
283 cell sensitivities to CCV in mitochondria abundance is cell line dependent. Presumably this depen-  
284 dence originates in the unique composition of components across cell lines. In that, the functional  
285 manifestation of CCV in mitochondria on the sensitivity of single cells to TRAIL induced apop-  
286 tosis is dependent on the relative abundance and diversity of mitochondria in relation to the other

287 biological constituents in the apoptosis pathway. Indeed, Jurkat cells readily responded to TRAIL  
288 and its  $IC_{50}$  scaled with mitochondria abundance, MDA-MB-231 cells showed scaling and re-  
289 sponded readily to TRAIL only in the presence of a pan-Bcl-2 inhibitor, while scaling was never  
290 observed and only a minority of HeLa cells responded to TRAIL even during Bcl-2 inhibition.  
291 Consequently, the seemingly contradictory results of our study and that of Márquez-Jurado [20]  
292 are manifestations of the unique biological systems being studied. In particular, we think that  
293 our observations are highlighting a different phenomenon than Márquez-Jurado et al. who are  
294 measuring a mitochondrial dependence of cell death in HeLa cells regardless of TRAIL dose (see  
295 Supplementary Note 6 and Supplementary Figure 9).

296 Our findings were established by a new statistical framework, DEtermining Parameter Influ-  
297 ence on Cell-to-cell variability Through the Inference of Variance Explained, namely DEPICTIVE,  
298 we developed to measure the impact of CCV on the binary response of cells to perturbation. It is  
299 composed of two parts, the first part is to infer the parameters of the logistic regression model when  
300 data from one or both of the binary cell state labels are available. While the second part provides  
301 the mathematical bases for interpreting the logistic regression model parameters to compute useful  
302 quantities.

303 Indeed, inferring the parameters of a logistic regression model from data is commonplace.  
304 However, it is only commonplace when data representative of both of the corresponding binary  
305 states is well established. To our knowledge, there is no method to infer these parameters from  
306 data where only one of the binary classes is readily available. In our study data from live and dead  
307 cells were unavailable because our experimental label of mitochondria abundance, MitoTracker  
308 DeepRed, was not reliable for dead cells.

309 The second part of DEPICTIVE statistical framework is to use the logistic model parameters to  
310 estimate the contribution of the measured biological component(s) to the variable binary response  
311 of single cells. Applying this tool, we found that mitochondria density accounts for nearly 30% of  
312 the variable response to TRAIL in Jurkat cells and varies from 2% to up to 40% in MDA-MB-231  
313 cells when Bcl-2 is inhibited. Conversely HeLa cells showed no mitochondrial density dependence.

314 Together, the two parts of the DEPICTIVE statistical framework can extract quantitative insights  
315 to sources of cell-to-cell variability.

316 We attribute the measured connection of TRAIL sensitivity and mitochondria density to the di-  
317 lution of Bax on the outer mitochondrial membrane in cells by mathematical modeling. From the  
318 quantitative insights of DEPICTIVE, we found that the functional manifestation of mitochondrial  
319 CCV is plastic - readily and predictably tunable by small molecule inhibitors of Bcl-2. It is plau-  
320 sible that this plasticity is a tool accessible to cells, and therefore may be co-opted by pathological  
321 cellular populations. For example, high mitochondria abundance can be a non-genetic mechanism  
322 of resistance to pro-apoptotic therapeutics. Incorporation of such knowledge may be an important  
323 consideration in developing therapeutic strategies.

324 The observed advantage of cells with high mitochondria densities may manifest in time-scales  
325 much longer than the life span of a single cell or the disease in a human, but propagate to the long  
326 time-scales of evolution. To date, the evolutionary hypothesis of mitochondria is as a symbiotic  
327 bacterium inside a proto-eukaryotic cell [29], exchanging safety for energy. However, another  
328 such evolutionary advantage may be expected, that this symbiosis would create a survival advan-  
329 tage such as the one described here. These results suggest that environmental constraints can  
330 select subpopulations not only based on genetic composition, protein abundances, but also CCV in  
331 organelle abundances.

## 332 Methods

### 333 Cell culture

334 **Jurkat** E6-1 cells originate from a male human acute T cell Leukemia and were purchased from  
335 ATCC (TIP-152). Cells were cultured in RPMI-1640 medium (Corning cat. 10-040-CV) sup-  
336 plemented with 10% heat inactivated fetal bovine serum (Corning cat. 35-011-CV), 2mM L-  
337 Glutamine (Corning cat. 25-005-CI) and 1mM sodium pyruvate (Corning cat. 25-000-CI). Cells  
338 were cultured at 37° C in 5% CO<sub>2</sub> in a humidified incubator and maintained at cell density not  
339 exceeding 3 x 10<sup>6</sup> by addition of fresh medium, or by centrifugation with subsequent resuspension  
340 at 1 x 10<sup>5</sup> cells/mL.

341 **MDA-MB-231** cells originate from a human female adenocarcinoma that were harvested from a  
342 metastatic site in the breast. Cells were cultured in DMEM medium (Corning cat. 10-017-CV)  
343 supplemented with 10% fetal bovine serum and 2mM L-Glutamine (Corning cat. 25-005-CI). Cell  
344 were cultured at 37° C in 5% CO<sub>2</sub> in a humidified incubator and subcultured every 2-3 days with  
345 0.25% trypsin (Corning cat. 25-053-CI) to maintain sub-confluent density.

346 **HeLa** cells were purchased from ATCC (ATCC CCL2). Cells were cultured in DMEM medium  
347 (Corning cat. 10-017-CV) supplemented with 10% fetal bovine serum and 2mM L-Glutamine  
348 (Corning cat. 25-005-CI). Cell were cultured at 37° C in 5% CO<sub>2</sub> in a humidified incubator and  
349 subcultured every 2-3 days with 0.25% trypsin (Corning cat. 25-053-CI) to maintain sub-confluent  
350 density.

### 351 Apoptosis assay and Data acquisition

352 **Jurkat** cells were pelleted by centrifugation for 5 minutes at 100 x g, and then resuspended in 1x  
353 PBS and stained with 200 nM MitoTracker Deep Red (Life Technologies, cat. M22426) for 10  
354 minutes at 37° C. MitoTracker staining was quenched with full cell culture medium, followed by  
355 centrifugation for 5 minutes at 100 x g. Cells were resuspended in cell culture media at a density  
356 of 1 x 10<sup>6</sup> per mL, in which 1 x 10<sup>5</sup> were transferred to each experimental well of a flat-bottom  
357 96-well plate. Cells were then incubated at 37° C for 4 hours with different doses of Superkiller

358 TRAIL (Enzo Life Sciences cat. ALX-201-115) and/or ABT263 (ApexBio cat. A3007). After  
359 drug treatment, cells were transferred to a v-bottom 96-well plate, pelleted by centrifugation at  
360 1,000 x g, stained with FITC-conjugated Annexin V (Biolegend cat. 640945), and then measured  
361 by flow cytometry.

362 **MDA-MB-231 or HeLa** cells were seeded on 12-well plates at  $5 \times 10^5$  cells per well in 400  $\mu\text{L}$ ,  
363 incubated overnight at 37 C in 5% CO<sub>2</sub> in a humidified incubator until 80% confluent. Cells  
364 were then washed once with PBS and stained with 200 nM MitoTracker Deep Red (Life Tech-  
365 nologies, cat. M22426) for 10 minutes at 37 C. MitoTracker staining was quenched with full cell  
366 culture medium, and then incubated at 37 C for 4 hours with different doses of Superkiller TRAIL  
367 (Enzo Life Sciences cat. ALX-201-115) and/or ABT263 (ApexBio cat. A3007). After drug treat-  
368 ment, supernatant containing floating cells was collected, and the remaining adherent cells were  
369 trypsinized, pooled with the supernatant, and pelleted by centrifugation for 5 minutes at 1,000 x  
370 g. Cells were then stained with FITC-conjugated Annexin V (Biolegend cat. 640945), and then  
371 measured by flow cytometry.

372 Flow cytometry measurements were conducted on a BD LSRII maintained by the Icahn School of  
373 Medicine at Mount Sinai flow cytometry core facility.

### 374 **FCM gating**

375 FCM measurements were gated as follows: to exclude debris (Supplementary Figure 1A), then  
376 gated for singlets (Supplementary Figure 1B), MitoTracker Deep Red positive (Supplementary  
377 Figure 1C), and lastly for living cells by Annexin V (Supplementary Figure 1D). The fraction of  
378 cells alive was computed by dividing the number of cells in the Annexin-V-negative gate by the  
379 number of cells of the MitoTracker Deep Red positive gate. Subsequent single cell analysis was  
380 then conducted exclusively using cells from the Annexin-V-negative gate.

### 381 **Code availability**

382 **DEPICTIVE**: Detailed derivation of the DEPICTIVE strategy can be found in Supplementary  
383 Note 3. We developed a user friendly Python package to run the DEPICTIVE analysis strat-

384 egy. The code is freely available as a GitHub repository, <https://github.com/robert-vogel/depictive>.

385 Along with these tools we provide two tutorials that demonstrates how to generate synthetic data

386 and to apply DEPICTIVE analysis. These tutorials can be found on the repositories wiki pages,

387 <https://github.com/robert-vogel/depictive/wiki>.

388 **Dynamics Simulations:** Detailed derivations and parameter values of model equations for simu-

389 lation can be found in Supplementary Note 5. We developed a user friendly Python package to

390 run, plot, and perform basic analysis of our model. The code is freely available as a GitHub repos-

391 itory, [https://github.com/robert-vogel/mito\\_sims](https://github.com/robert-vogel/mito_sims). Along with these tools we provide a a series of

392 tutorials that demonstrates the use of our tools by examples. These tutorials can be found on the

393 repositories wiki pages, [https://github.com/robert-vogel/mito\\_sims/wiki](https://github.com/robert-vogel/mito_sims/wiki).

## 394 **Data availability**

395 The data presented in the main-text of this paper can be found on Mendeley data [30–35].

## 396 **Modeling and Statistical analysis**

397 Detailed derivations of our DEPICTIVE statistical framework, application of DEPICTIVE to data,

398 dynamics models, and inference of dynamic model parameters can be found in Supplementary

399 Notes 3, 4, 5, and 5.4, respectively.

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## 481 **Author contributions**

482 Conceptualization, L.C.S., R.V., M.R.B., G.S., and P.M.; Methodology, R.V., G.S., and P.M.; Soft-  
483 ware, R.V., and P.M.; Formal Analysis, R.V., and G.S.; Investigation, L.C.S., R.V., and P.M.;  
484 Resources, J.E.C., M.R.B., and G.S.; Writing - Original Draft, L.C.S., R.V., and P.M.; Writing -  
485 Review & Editing, L.C.S., R.V., M.R.B., G.S., and P.M.; Visualization, R.V.; Supervision, M.R.B.,  
486 G.S., and P.M.

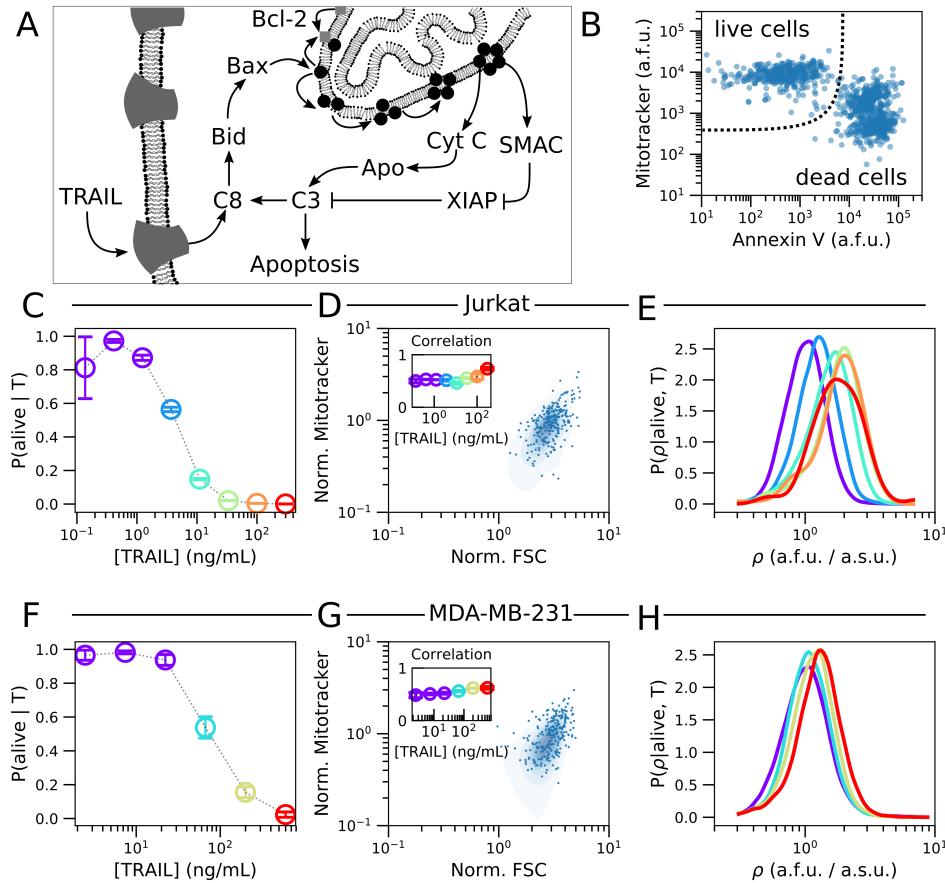
## 487 **Competing interests**

488 The authors declare no competing financial interests.

## 489 **Materials and Correspondence**

490 Requests for data, resources, and or reagents should be directed to Pablo Meyer (pmeyerr@us.ibm.com).

491 **Figures**



**Figure 1: TRAIL administration enriches for cells with high density of mitochondria** (A) An overview of TRAIL induced apoptosis. (B) Flow cytometry measurements (FCM) of mitochondria (MitoTracker Deep Red) and phosphatidylserine (FITC conjugated Annexin V) in Jurkat cells. Complete flow cytometry gating strategy can be seen in Supplementary Figure 1. The fractional response of Jurkat cells (C) to TRAIL. Each color corresponds to a unique fractional response to a specific TRAIL dose. Cell size measurements (FSC-A) in Jurkat cells (D) are correlated with mitochondria abundance (MitoTracker Deep Red). The inset shows that the Pearson correlation marginally changes for each TRAIL dose. The probability density of mitochondria density ( $\rho$ ) for each dose of TRAIL that elicits a unique response in Jurkat cells (E). The fractional response of MDA-MB-231 cells to TRAIL (F). Cell size measurements (FSC-A) in MDA-MB-231 cell (G) are correlated with mitochondria abundance (MitoTracker Deep Red). The inset shows that the Pearson correlation marginally changes for each TRAIL dose. The probability density of mitochondria density ( $\rho$ ) for each dose of TRAIL that elicits a unique response in MDA-MB-231 cells (H). In (E) and (H) the single cell measurements from each of the lowest three doses of TRAIL are aggregated prior to probability density estimation (Violet). Visual inspection of the respective dose response curves suggest that these three doses of TRAIL are effectively identical. Data presented with errorbars represent the mean  $\pm$  one standard error of the mean over triplicate experiments.

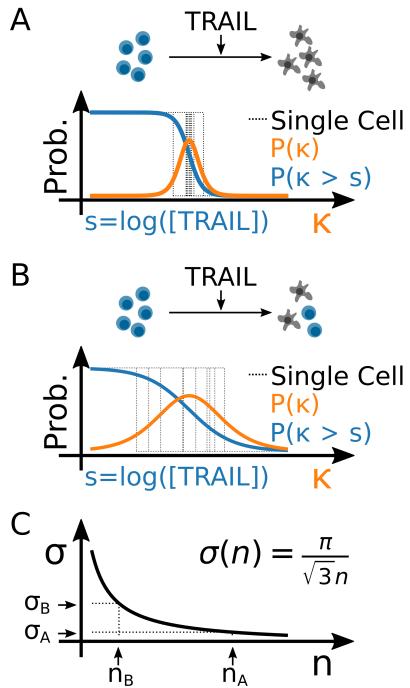
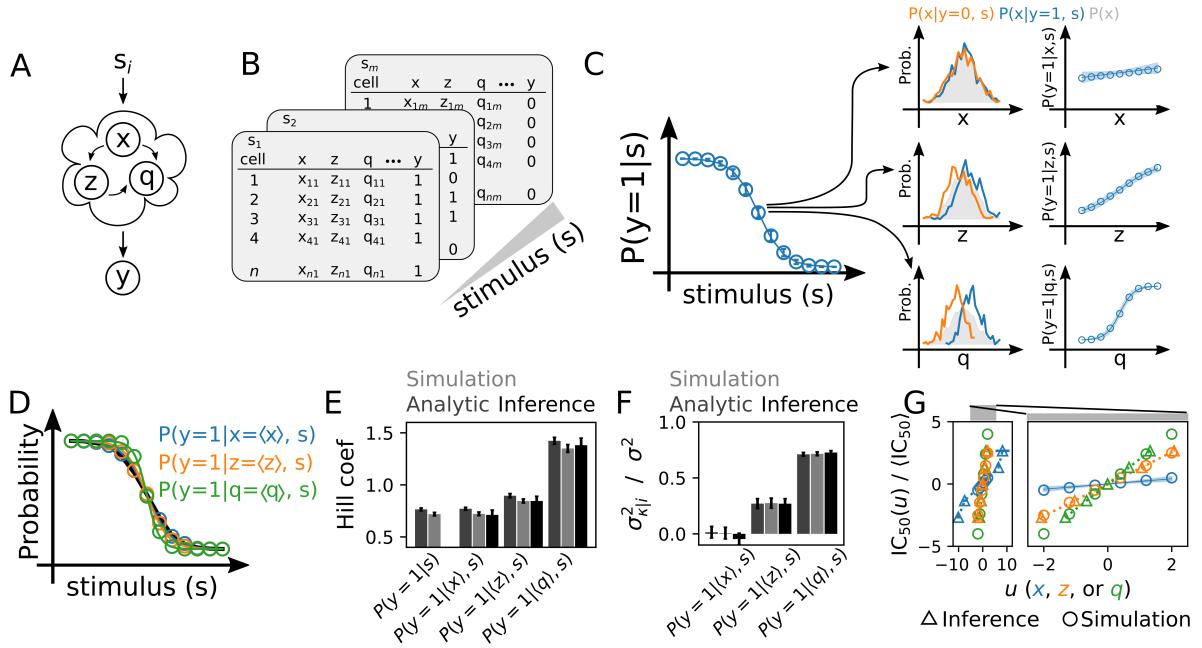
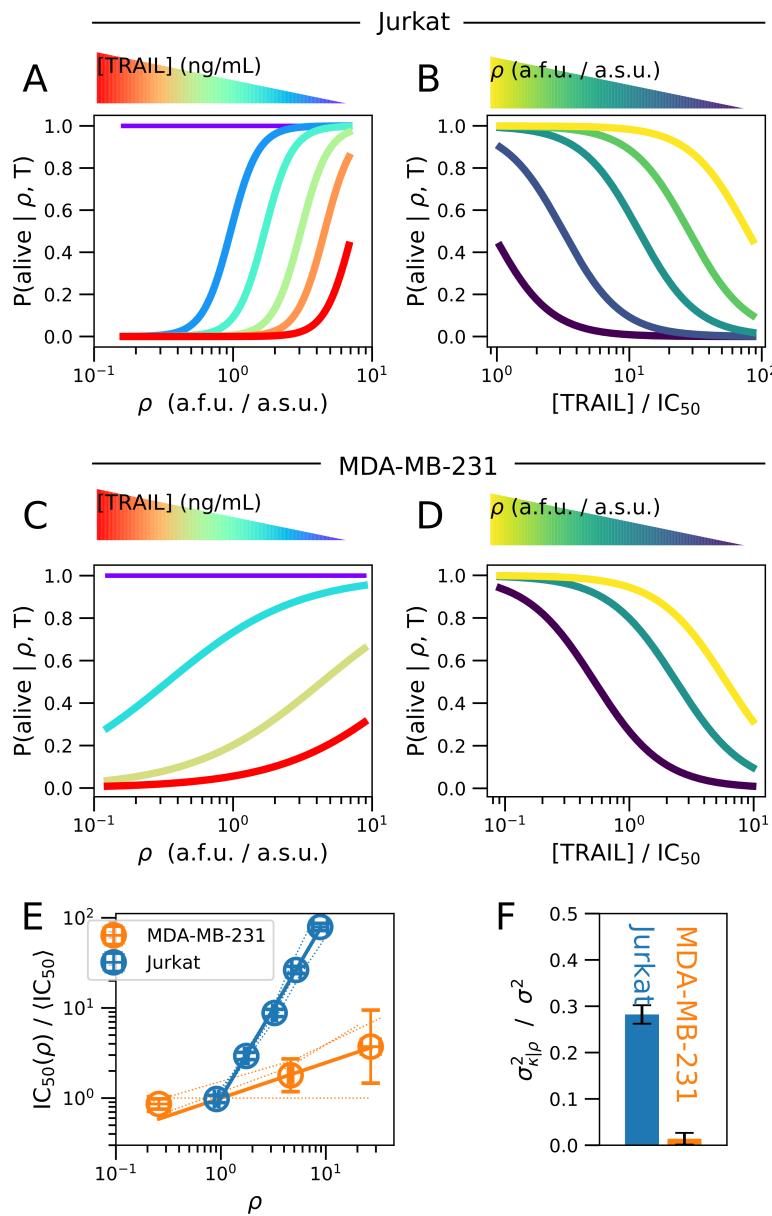


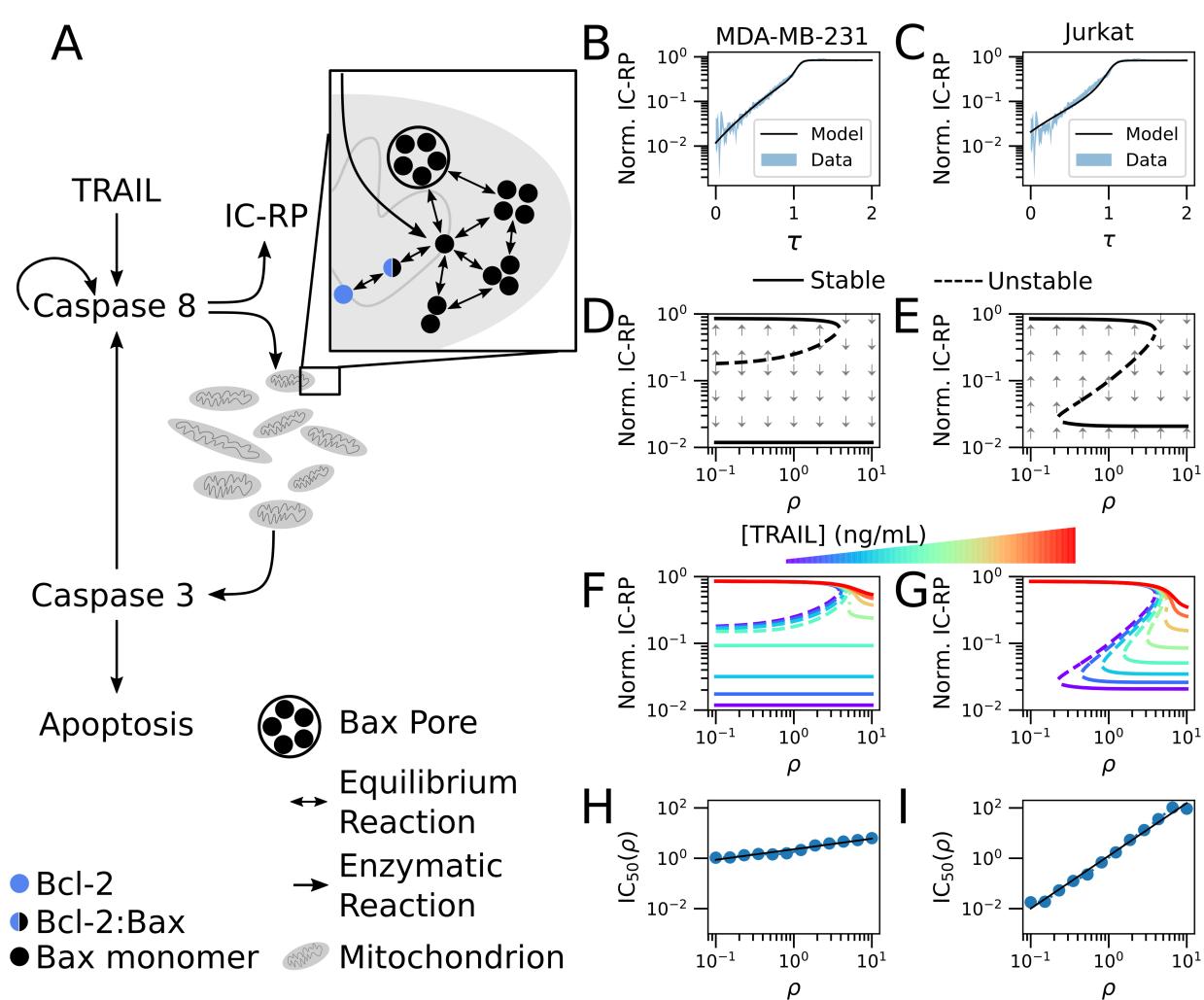
Figure 2: **Cell-to-cell variability in the binary response to TRAIL** Hill response function with respect to TRAIL dose (blue) and the corresponding probability density of the single-cell sensitivities (orange) for populations with (A) low CCV and (B) high CCV. (C) The theoretical correspondence between the variance of single-cell sensitivities to TRAIL ( $\sigma$ ) and the Hill coefficient  $n$ . Here,  $(n_A, \sigma_A)$  and  $(n_B, \sigma_B)$  represent the Hill coefficient and corresponding single-cell variances from (A) and (B), respectively.



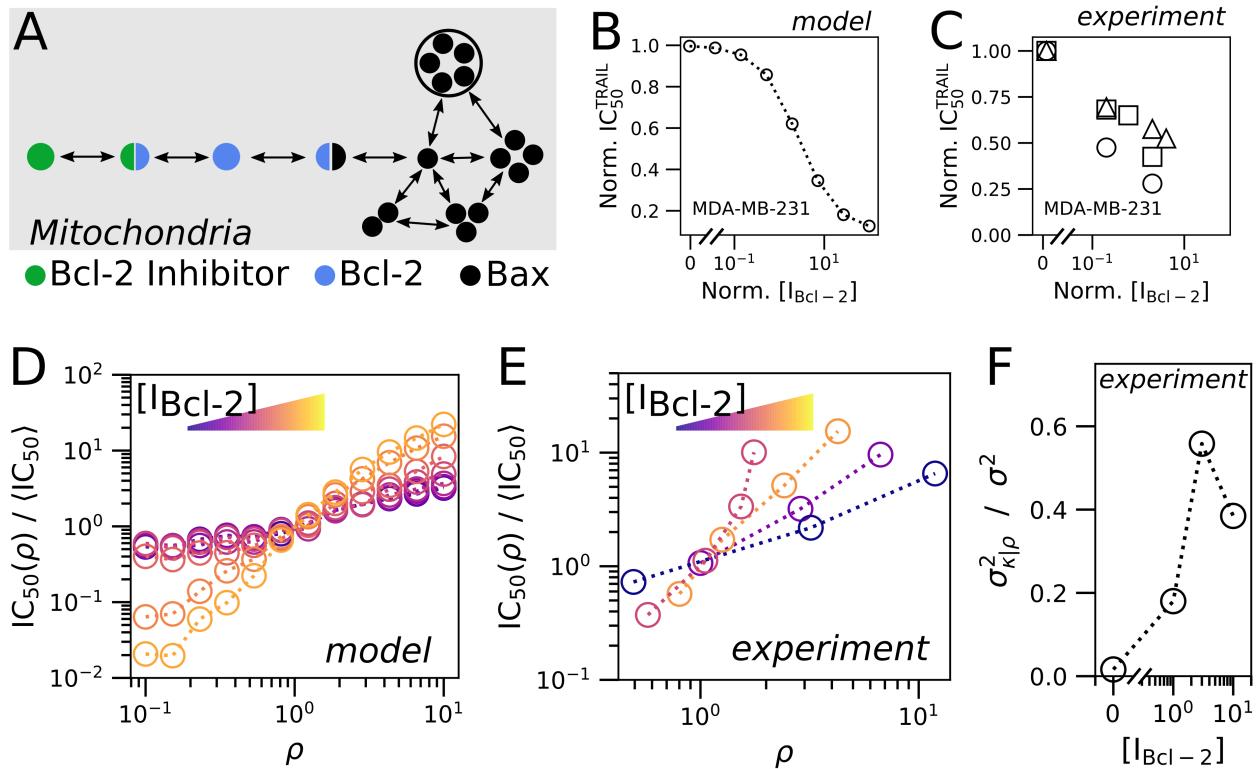
**Figure 3: Decomposing sources of cell-to-cell variability** (A) Schema for a simple cellular response,  $y \in \{0, 1\}$ , to the activation of pathway components  $x, y, q$  subject to the  $i^{th}$  dose of a stimulus  $s_i$ . (B) Single cell data were simulated to demonstrate the feasibility of CCV decomposition by sampling virtual cells (see Supplementary Note 3.2.3 for details). (C) The dose response of  $N = 1000$  simulated cells and  $n = 100$  replicate experiments in which  $k_x = 0.25$ ,  $k_z = 1.25$ , and  $k_q = 2$ . Error bars represent  $\pm$  three standard deviations about the mean. The histograms normalized by cell count of live or dead cells reveals how each biological entity correlates with cell state (left column). We may make the dependence of cell survival to TRAIL by examining the probability of the cell state,  $y = 1$ , given the dose and abundance of each biological component (right column). In the right column, the circles represent the true conditional probability, while the blue line and shaded region represents the DEPICTIVE inferred dependence  $\pm$  three standard deviations. (D) If we eliminate each individual source of CCV, the dose response is less uncertain. A phenomena that is well parameterized by the Hill coefficient (E), and the corresponding variance explained (F). Error bars represent  $\pm$  one standard deviation. (G) The scaling of the  $IC_{50}(u)$  with  $u$ .



**Figure 4: CCV in mitochondria density influences fractional response to TRAIL.** The inferred fractional response of Jurkat cells (A) or an MDA-MB-231 cells (C) as a function of  $\rho$  given TRAIL dose. The inferred fractional response of Jurkat cells (B) or an MDA-MB-231 cells (D) as a function of TRAIL dose given  $\rho$ . (E) The dose of TRAIL normalized by the population  $IC_{50}$  (y-axis) and the inferred density of mitochondria ( $\rho$ ) in which the fractional response is 0.5 (x-axis). The blue markers represent triplicate averages in Jurkat cells while the error bars represent  $\pm$  the standard error of the mean. The orange markers represent duplicate averages in MDA-MB-231 cells and standard error of the mean, while the y-axis represents triplicate statistics. We report duplicate statistic in MDA-MB-231, because in one replicate experiment there is no correlation between the  $IC_{50}$  and  $\rho$ , including these values of  $\rho$  would lead to misleadingly large error bars. Lastly, dashed blue and orange lines represent the inferred values of  $\rho$  for each replicate data set for Jurkat and MDA-MB-231 cells, respectively. (F) The fraction of the variance in single cell TRAIL sensitivities ( $\sigma$ ) explained by CCV in mitochondria density from  $(\sigma_{\kappa|\rho})$ . Error bars represent standard error of the mean of experimental triplicates. Detailed analysis of each replicate set are presented in Supplementary Figures 3-5.



**Figure 5: Mechanism of  $IC_{50}$  dependence on mitochondria density.** (A) Simple model of apoptosis. The dynamics of initiator caspase reporter protein (IC-RP) from [24] and the model-inferred dynamics corresponding to (B) MDA-MB-231 and (C) Jurkat cell lines. The model bifurcation diagrams for  $[TRAIL] = 0$  ng/mL in (D) MDA-MB-231 and (E) Jurkat cells. The influence of TRAIL dose on the model fixed points for (F) MDA-MB-231 and (G) Jurkat cells. The dependence of single cell sensitivities to TRAIL on  $\rho$  for (H) MDA-MB-231 and (I) Jurkat cells. The  $IC_{50}$  was estimated from Hill function fits of simulated data (blue circles), and which were then fit to a power law (black line). Simulations consisted of 100 cells per each of the 20 doses of TRAIL and 12 densities of mitochondria considered.



**Figure 6: Plasticity in fractional response to TRAIL.** (A) Bcl-2 inhibitor reduces the effective abundance of Bcl-2 by formation of Bcl-2:Bcl-2 inhibitor complex. (B) Simulation results of the population  $IC_{50}^{TRAIL}$  response to Bcl-2 inhibition in MDA-MB-231 cells. (C) Experimental measurement sets - uniquely represented by a square, circle or triangle marker - of the population  $IC_{50}^{TRAIL}$  response to Bcl-2 inhibition for MDA-MB-231 cells. (D) Estimated  $IC_{50}$  for changing  $\rho$  from MDA-MB-231 parameterized model simulations. (E) The experimental dependence of  $IC_{50}$  on  $\rho$ , from a single representative experiment of three replicate experiments (Supplementary Figures 6-8), as computed in Figure 4E for  $[0, 1, 3, 10] \mu M$  doses of the Bcl-2 Inhibitor ABT-263. (F) The fraction of variance in single-cell sensitivities ( $\sigma$ ) explained by mitochondria density CCV in E ( $\sigma_{k|\rho}$ ). Note that all simulations were conducted with 100 cells for each of the 20 doses of TRAIL, 12 densities of mitochondria, and 9 doses of inhibitor. Detailed analysis of each replicate data set are presented in Supplementary Figures 6-8.