1   **Ancestral reconstruction of polyethylene terephthalate degrading cutinases reveals a**

2   **rugged and unexplored sequence-fitness landscape**

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20   The enzymatic degradation of polyethylene terephthalate (PET) is a promising method of
21   advanced plastic recycling. Traditional protein engineering methods often fall short in
22   exploring protein sequence space for optimal enzymes due to structural and rational
23   design limitations. Our study addresses this by using multiplexed ancestral sequence
24   reconstruction (mASR) to explore the evolutionary sequence space of PET-degrading
25   cutinases. With a dataset of 397 cutinase sequences, we created a diverse library of
26   ancestral sequences. Experimental characterization of 48 ancestral sequences revealed
27   a wide range of PETase activities, highlighting the value of mASR in uncovering functional
28   variants when compared to traditional ASR. Our results showed that PETase activity in
29   cutinases evolved through diverse pathways involving distal mutations to the active site,
30   and is readily accessible within this family. Additionally, our analysis of the PETase fitness
31   landscape using one-hot encoding (OHE) and local ancestral sequence embedding
32   (LASE) highlighted the effectiveness of LASE in capturing sequence features relevant to
33   activity. This work emphasizes the utility of mASR as a protein engineering tool for
34   identifying enhanced PET-degrading enzymes, and the advantages of the LASE
35   embedding scheme in mapping the PETase fitness landscape.

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Introduction

Over 350 million tonnes of plastic are produced annually, with the majority being derived from petrochemicals[1]. However, the current global recycling rate of plastics is estimated to be less than 10%, partially due to the technological constraints of mechanical (melt-extrusion) recycling[2]. There is a pressing need to develop advanced and scalable recycling methods that will enable the transition towards a circular plastic economy. In the last decade, enzymatic depolymerization of plastics has emerged as one such advanced recycling method[3]. The enzymatic degradation of polyethylene terephthalate (PET), a versatile thermoplastic commonly found in food and beverage packaging, and polyester textiles has received particular interest[3].

PET-degrading enzymes that have been characterized to date, including those classified as cutinases[4–6] (EC 3.1.1.74), lipases[7] (EC 3.1.1.3), and carboxylesterases[8] (EC 3.1.1.1), belong to the esterase subclass (EC 3.1) and are characterized by a catalytic triad (Ser-His-Asp) typical of the α/β hydrolase fold superfamily. Cutinases have garnered significant interest due to their ability to hydrolyse both aromatic and aliphatic polyesters[9]. Cutinases of bacterial[5,9,10], fungal[7], and metagenomic[11–13] origins have been studied for their PETase activity, including Thc_Cut1 and Thc_Cut from *Thermobifida cellulosilytica*[5], TfCut2 from *Thermobifida fusca*[5], HiC from *Humicola insolens*[14], FsC from *Fusarium solani pisi*[15], and LCC from leaf-branch compost metagenome[16]. However, extant cutinases are often unsuitable for direct use in industrial processes, necessitating optimisation to improve properties such as catalytic efficiency[17], stability under harsh conditions[18,19], and to alleviate product inhibition[20]. For example, active site optimisation through rational design[6,10,21] and evolutionarily-guided engineering[20] has yielded significant improvements in PET hydrolysis across various cutinase backgrounds. While structure-guided protein engineering has been effective in improving the efficiency of extant PETases, it has provided little insight on the mechanisms by which PETase activity emerges or has been optimized by evolution.

Ancestral sequence reconstruction (ASR), which utilizes a phylogenetic tree and a statistical model of evolution to infer the sequences of extinct, ancestral proteins, can provide critical insights into molecular evolution and functional diversification within protein families[22]. ASR has been useful in studying sequence-function relationships over protein families[23,24]; such insight can shed light on the topologies of fitness landscapes that dictate the adaptive potential of proteins[25]. For example, ASR can give insight into the ruggedness (i.e. complexity) of a fitness landscape over large spans of evolutionarily accessible sequence space to reveal

74 fitness peaks that are inaccessible through stepwise mutational approaches[24]. In addition to
75 this, ASR is also frequently used to engineer enzymes with enhanced industrial properties[22,26–
76 28], making it a valuable tool in both protein engineering and understanding the mechanisms of
77 molecular evolution.
78
79 More recently, protein representation learning has become a widely used method in protein
80 engineering and evolutionary inference[29,30]. Protein language models (PLM), which are deep
81 neural networks trained to predict the identities of masked residues in a corpus of protein
82 sequences[29–32], can map information sparse and high dimensional protein sequences to fixed-
83 length vector representations. These vector representations capture the evolutionary and
84 biophysical features of protein sequences in the representation model's latent embedding
85 space[29,30]. Indeed, PLMs have been used to learn the structure of fitness landscapes[33–35], and
86 can learn evolutionary features when trained with ancestrally reconstructed sequence data[36].
87
88 In this study, we applied ASR to explore the evolutionarily accessible sequence space of PET-
89 degrading cutinases. Using a dataset of 397 extant cutinase sequences with significant
90 homology to known cutinases with PETase activity, we adopted a multiplexed ASR (mASR)
91 approach to generate a diverse library of ancestral cutinase sequences. Through experimental
92 characterization of 48 ancestral cutinases, we identified a broad range of PETase activities,
93 including between equivalent nodes on distinct yet statistically indifferent phylogenetic
94 topologies. Such findings highlight the importance of sampling diverse phylogenetic
95 backgrounds to uncover functional ancestral variants. Furthermore, our study analyzed the
96 topology of the PETase fitness landscape through two sequence embedding schemes: one-
97 hot encoding (OHE) and the more recently described local ancestral sequence embedding
98 (LASE)[36]. We found that LASE was more effective in capturing cutinase sequence features
99 pertinent to PETase activity, demonstrating a clear pattern of iterative improvement in PETase
100 functionality throughout the sequence exploration phases of our study. This comprehensive
101 approach not only highlights the utility of mASR in uncovering novel PETase variants but also
102 emphasizes the role of advanced embedding techniques in mapping PETase fitness
103 landscapes.
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109   Results

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111   **Multiplexed ASR yields functional PETases from diverse phylogenetic backgrounds.**

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113   We used ASR to explore the PETase functional sequence space of the cutinase family. To

114   maximize diversity in the local sequence space around known PETases, such as *Tf*Cut2 and

115   LCC, we employed the recently described multiplexed ASR (mASR)[36]. In brief, mASR samples

116   multiple statistically indifferent phylogenetic backgrounds from which to reconstruct ancestral

117   sequences from. This produces diverse libraries of ancestral proteins that span functional

118   sequence space over a distribution of realistic phylogenies. To achieve this, we performed 20

119   replicates of maximum likelihood (ML) phylogenetic inference and ASR on a single dataset of

120   397 extant cutinases with significant homology to *Tf*cut2 and LCC (E-value <= 1E-5).

121   Consistent with previous phylogenetic studies[37], PET hydrolytic cutinases were resolved as a

122   polyphyletic group of two monophyletic lineages: the *Thermobifida sp*. PETases, which include

123   *Tf*cut2, *T. cellulosytica* cutinase and *T. alba* esterase 1 and the LCC-like PETases that include

124   LCC and BhrPETase. This topology was resolved consistently over all 20 phylogenetic priors

125   used for mASR (**Figure 1A**). The placement of the PETase clades were supported by high

126   ultra-fast bootstrap approximations[38] (>= 0.95) and the ancestral nodes separating these

127   groups were reconstructed in CodeML from the PAML[39] suite with relatively high mean

128   posterior probability (>0.9; based on ASR statistical benchmarking studies[40]). The resulting

129   ancestral sequence library comprised approximately 1600 unique sequences that

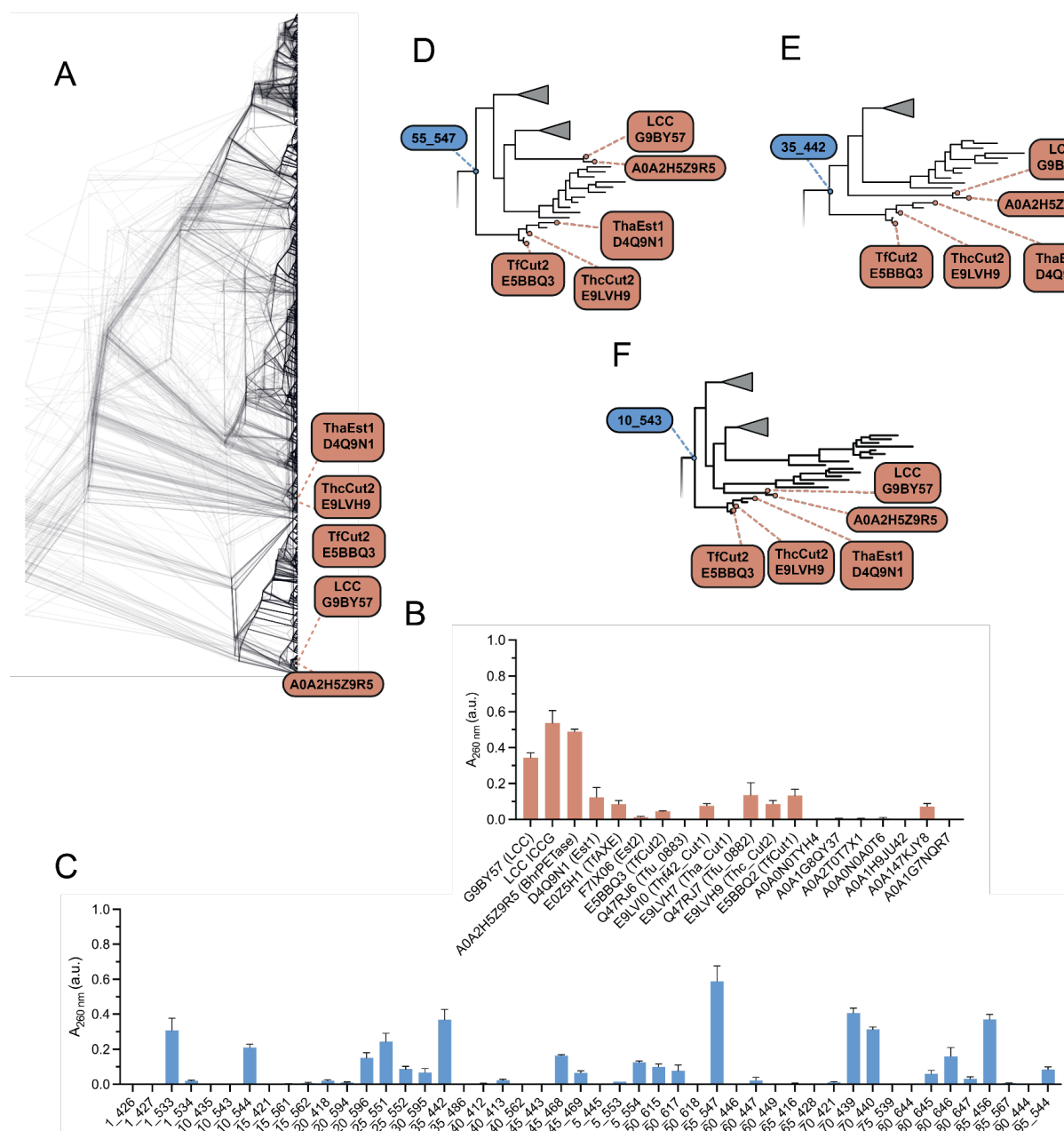130   encompassed the evolutionarily accessible sequence space of the bacterial cutinase family.

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Figure 1. Ancestral sequence reconstruction and characterization of ancestral cutinases. (**A**) 20 replicates of phylogenetic reconstruction of the cutinase family with fixed extant node locations. All 20 presented topologies failed rejection by the AU-test and are equally valid representations of the underlying sequence alignment. Extant tips of interest (*Thermobifida* cutinases, E5BBQ3, D4Q9N1, E9LVH9 and metagenomic assembled cutinases A0A2H5ZR95, G9B757 (LCC)) are labeled). Degradation of amorphous PET film by. (**B**) 20 extant and (**C**) 48 ancestral cutinases. The bulk soluble products of PET hydrolysis (TPA, MHET, BHET) are measured by absorbance at 260 nm after 16 hours incubation with the enzyme at 60 °C. Data are represented as the mean ± SEM (n = 3). (**D**) Phylogenetic tree 55, (**E**) 35 and (**F**) 10, with ancestors 35_442, 55_547 and 10_543 highlighted. Each ancestor belongs to equivalent nodes from independent phylogenetic topologies, and are the most recent common ancestor of LCC and TfCut2, extant cutinases with known PETase activity.

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144 We selected 48 ancestral nodes from 20 different trees with homology to the most recent
145 common ancestor of LCC and *Tf*Cut2 for experimental characterization and comparison to
146 extant cutinases. Specifically, these nodes were chosen from the recent ancestors of the LCC
147 and *Tf*Cut2 lineages (or the most recent common ancestor of both), with at least a single
148 sequence sampled from each of the 20 distinct phylogenetic trees. Each ancestral sequence
149 was selected as the *maximum a posteriori* (MAP) sequence that maximizes the posterior
150 probability over the full-length of the reconstructed protein. The variants were expressed,
151 purified and tested for PETase activity. The soluble expression level of each variant was
152 measured using the Bradford assay (**Supplementary Figure 1**). PETase activity against
153 amorphous PET film was measured by UV absorbance at 260 nm to detect the soluble
154 products of PET hydrolysis after the removal of undigested film, including terephthalic acid
155 (TPA), mono(2-hydroxyethyl) terephthalate (MHET), and bis(2-hydroxyethyl) terephthalate
156 (BHET) (**Supplementary Figure 2**). Among the extant cutinases, the highest PETase
157 activities were observed for LCC (A_{260} nm = 0.34 ± 0.03), BhrPETase from bacterium HR29
158 (A_{260} nm = 0.49 ± 0.01), and a previously engineered variant of LCC with the mutations
159 F243I/D238C/S283C/Y127G (LCC ICCG)[6] (A_{260} nm = 0.54 ± 0.07), with other cutinases
160 showing lower activity (**Figure 1B**). Of the 48 ancestral variants, we observed PETase activity
161 for a number of ancestral cutinases from a diverse range of trees (**Figure 1C**). Several variants
162 (1_533, 35_442, 55_547, 70_439, 70_440, and 85_456) exhibited similar activity to the most
163 active extant cutinases, LCC and BhrPETase. From this group, we selected ancestors from
164 tree 35, node 442 (35_442; A_{260} nm = 0.37 ± 0.06) and tree 55, node 547 (55_547; A_{260} nm =
165 0.59 ± 0.09), for further investigation. Notably, these two ancestors belonged to equivalent
166 positions from two independent phylogenetic trees (Figure **1D-F**), representing the most
167 recent common ancestor of LCC and TfCut2, and sharing 98.5% sequence identity to one
168 another.

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170 Within the dataset of 48 ancestral sequences, 12 represent the same phylogenetic node (the
171 most recent common ancestor of LCC and *Tf*Cut2) over 12 different phylogenetic
172 backgrounds. Of these, 9 exhibited PETase activity while 3 were inactive on PET.
173 Interestingly, the PETase ancestor 55_547 and the inactive ancestor 10_543 both represent
174 equivalent positions (the most recent common ancestor of *Tf*Cut2 and LCC) in their respective
175 phylogenetic backgrounds and differ by only 9/261 positions, yet 55_547 has activity against
176 PET and 10_543 does not. The functional differences between these sequences arise solely
177 from the topology of the phylogenetic tree used to reconstruct them and drastically alters how
178 the evolution of PETase activity could be inferred. For example, in the case of the 55_547
179 phylogeny, PETase activity appears to be a promiscuous ancestral trait that existed prior to
180 the discovery of extant PETases (such as LCC and *Thermobifida* cutinases), whereas the

181   10_543 phylogeny supports the contradictory hypothesis that PETase activity emerged
182   independently in LCC-like and *Thermobifida* PETase lineages from an ancestor without
183   PETase activity. As both topologies failed rejection by the approximately unbiased (AU)[41] test
184   and are statistically indifferent at representing the observed alignment data, it is not possible
185   to reject one of these hypotheses purely from a phylogenetic perspective. We also observe
186   no correlation between the mean posterior probability of an ancestor and its activity
187   (**Supplementary Figure 5**). This observation is somewhat counterintuitive, as the mean
188   posterior probability of a sequence, which is the statistical confidence in the identity of a
189   reconstructed ancestor, is often used to discriminate between poorly reconstructed sequences
190   (and hence likely to be less fit) and those that are likely to be functional and fit[40]. Together,
191   these results highlight the importance of sampling diverse phylogenetic backgrounds during
192   ASR when accessing the functional sequence space of a protein family as minor phylogenetic
193   incongruencies can translate into significant functional differences in (equivalent)
194   reconstructed ancestral sequences.
195
196   **Structural characterization and analysis of ancestral cutinases.**
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198   A comparative structural and sequence analysis of inactive and active ancestors suggests
199   that PET hydrolysis appears to be a trait that is evolutionarily accessible from within the
200   cutinase background. Unlike the *I. sakaiensis* PETase, which emerged through conformational
201   optimization of the first- and second-shells *via* obvious selection within the active site[42–44],
202   PETase activity in the TfCut2 and LCC PETase lineages appears to emerge through non-
203   specific and likely neutral mutations that are often distal to the active site (**Figure 2A-C**).
204   Indeed, analysis of ancestral cutinase sequences reveals virtually no differences in the PET
205   binding sites between PETase active and inactive variants (**Supplementary Figure 6**).
206   Furthermore, mutations associated with a gain-of-function vary between the different
207   phylogenetic trees used to reconstruct the ancestral sequences. For example, ancestors
208   55_547 and 35_442 are each separated by 9 unique mutations from their closest relatives
209   without PETase activity (ancestors 10_543 with A15S, A36V, T49S, T92S, N109D, R114S,
210   N145R, I180V, S226A and 75_539 with A36V, T49D, T92S, M105Q, R114S, S124N, R167T,
211   P199S, A226S, respectively). Of these loss of function mutations, 3 are shared between either
212   background, 5 are unique and one is a reversion (S226A for 55_547, A226S for 35_442).
213   Intuitively, a combination (with at least one) of these mutations are required to be fixed in
214   either respective cutinase background to impart PETase activity. Similarly, ancestor 10_543
215   is separated by 8 mutations from its closest relative with PETase activity (70_439 with E28Q,
216   S49D, S124N, R145N, V180I, P199S, S215T, A226S); of the 8 mutations associated with
217   gain-of-function in the background of 10_543, only 3 are specifically shared with gain-of-

218 function mutations in 55_547. Nearly all functionally consequential mutations across
219 backgrounds are distal to the active site and PET binding pocket. This suggests that (i) there
220 are numerous (and diverse) molecular mechanisms by which PETase activity can emerge
221 from an ancestral cutinase without PETase activity, (ii) these mechanisms are not obviously
222 associated with a restructuring of the enzyme active site and (iii) PETase activity is readily
223 evolutionarily accessible within the cutinase family, consistent with recent observations of
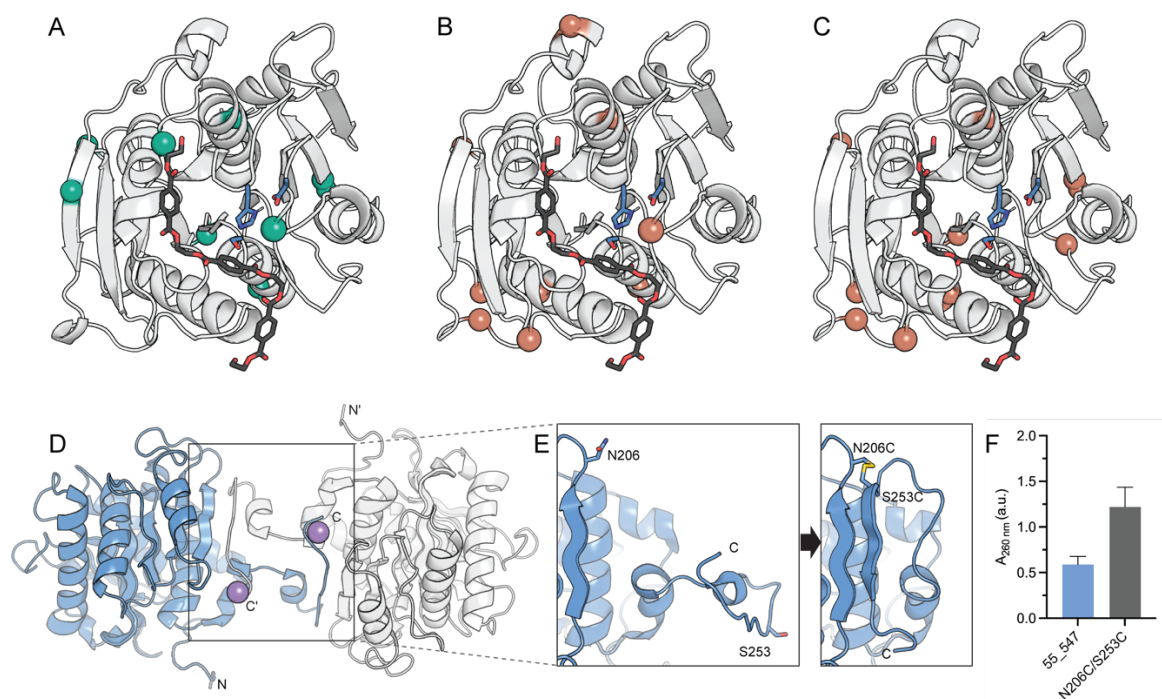224 PETases that have emerged from cutinase backgrounds[11,12].

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227 **Figure 2. Structural characterization of 55_547 and 35_442. A)** Positions of gain-of-function (GOF)
228 mutations in the inactive ancestor 10_543, and **B)** loss-of-function (LOF) mutations in the active
229 ancestors 55_547 and **C)** 35_442. GOF and LOF mutations are shown as teal and red spheres,
230 respectively. AlphaFold[45,46] was used to generate models of each ancestor. Most GOF/LOF mutations
231 are distal from the catalytic site residues (blue), and the putative PET binding site highlighted by the
232 docked 2HE-(MHET)3 ligand (black). Structural analysis of the active site residues H210, S132 and
233 D178 in ancestors 10_543, 55_547, and 35_442 shows uniform alignment, indicating that PETase
234 activity does not arise from modifications within the active sites (**SI. Figure 4**). **D)** Domain-swapped
235 homodimer observed in the crystal structure of ancestor 55_547 with two C-terminal strands swapped
236 (PDB 8ETX). The N- and C- termini of each subunit are indicated. The dimer is coordinated by sodium
237 ions (represented as purple spheres) in the crystal lattice. **E)** Positions on the flexible C-terminus of
238 ancestor 55_547 targeted for disulfide engineering, as shown in the crystal structure (left; PDB 8ETX),
239 resulting in the disulfide mutant N206C/S253C, as generated by AlphaFold[45,46] (right). The predicted
240 formation of an additional β-strand at the C-terminus, constrained by the disulfide bond, is shown. **F)**
241 PETase activity of ancestor 55_547 and the disulfide mutant N206C/S253C. The bulk soluble products
242 of PET hydrolysis (TPA, MHET, BHET) are measured by absorbance at 260 nm after 16 hours
243 incubation with the enzyme at 60 °C. Data are represented as the mean ± SEM (n = 3).

244

245 We next determined the crystal structures of two active ancestors, 35_442 (PDB 8ETY) and
246 55_547 (PDB 8ETX), and identified an additional pathway to optimizing PETase activity

247 beyond modification of the active site. Both ancestors crystallized in the C222 space group at

248 resolutions of 1.5 - 1.8 Å (**Supplementary Table 1**). Structural analysis revealed the formation

249 of domain-swapped dimers (**Figure 2D**). The observation of domain swapping, likely induced

250 by the high protein concentration in the crystallization conditions, suggests an intrinsic

251 flexibility of the C-terminus, a characteristic commonly observed in proteins previously

252 characterized to form domain-swapped dimers[47]. Given the flexible nature of the C-terminus,

253 it was hypothesized that introducing a disulfide bond to constrain this region into forming an

254 intramolecular β-sheet would enhance enzyme stability (**Figure 2E**). Furthermore, the chosen

255 site for the disulfide bond coincided with the predicted Ca^{2+}/Mg^{2+} binding site of the ancestors

256 based on homology to extant cutinases, a region previously targeted for disulfide bond

257 engineering in TfCut2 and LCC for improved thermostability and PETase activity[6,48,49]. We

258 introduced the disulfide mutation N206C/S253C to ancestor 55_547 and experimental

259 characterization of the resulting mutant demonstrated an approximately 2-fold improvement

260 in whole-cell activity ($A_{260\ nm}$ = 1.22 ± 0.22) (**Figure 2F**) and a 1.5-fold increase in soluble

261 expression levels compared to the 55_547 background determined by Bradford assay

262 (**Supplementary Figure 5**). In combination with our comparative analysis of the selected

263 inactive and active ancestors, the successful optimization of PETase activity via the

264 introduction of a disulfide bond distal to the active site illustrates that PETase activity within

265 the cutinase family can emerge and be enhanced through mechanisms that extend beyond

266 the structural reconfiguration of the active site. It is therefore likely that activity optimization is,

267 at least in part, being driven by thermodynamic and kinetic stabilization.

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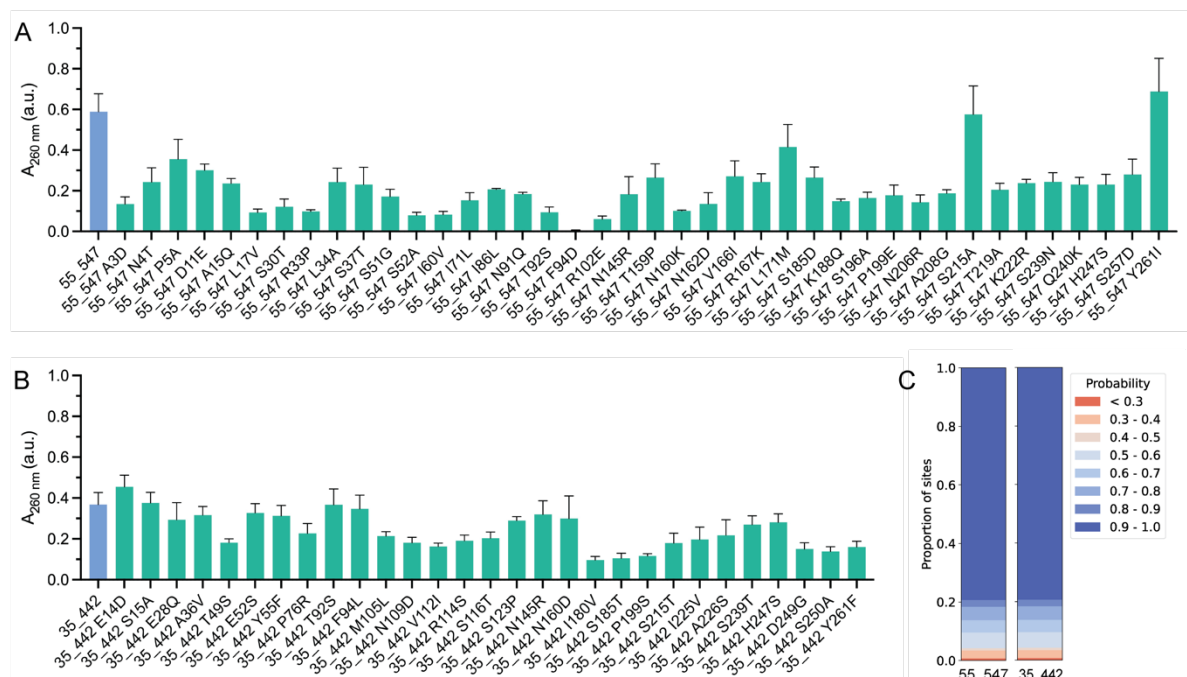**Alternate Reconstructions of Ancestral Cutinases 35_442 and 55_547.**

Figure 3. Alternate reconstructions and random recombinations of ancestral cutinases 35_442 and 55_547. Activity of alternate reconstructions of **A)** ancestor 55_547 and **B)** 35_442 against amorphous PET film. The bulk soluble products of PET hydrolysis (TPA, MHET, BHET) are measured by absorbance at 260 nm after 16 hours incubation with the enzyme at 60 °C. Data are represented as the mean ± SEM (n = 3). **C)** Posterior probability distributions for ancestors 55_547 and 35_442.

We next experimentally characterized all alternate sequences of ancestors 55_547 (40 mutants) and 35_442 (29 mutants) that individually sampled each mutation that had been ambiguously reconstructed. Here, we define ambiguity as any site where at least two amino acids are reconstructed with a posterior probability of >= 0.2. This provided a high resolution mutagenic map of the local sequence space around either of the ancestral PETase variants. Ambiguously reconstructed sites were spatially distributed over the protein and not localized to any specific functional area (**Supplementary Figure 7**). Having already established that the mean posterior probability of an ancestral sequence is a poor indicator of PETase activity (**Supplementary Figure 4B**) and that relatively minor changes in the cutinase sequence can drastically alter PETase activity, we hypothesized that the neighborhood of evolutionarily possible (albeit less probable) sequences may contain mutations that benefit PETase activity. This hypothesis was guided by recent ASR studies on the *I. sakaiensis* PETase branch of the cutinase phylogeny where PETase activity appeared to emerge transiently within ancestral lineages[50]. Experimental characterization revealed that all of the alternate reconstructions of ancestors 55_547 and 35_442 demonstrated PETase activity that was comparable (or reduced) to either respective ancestral background (**Figure 3A-B**).
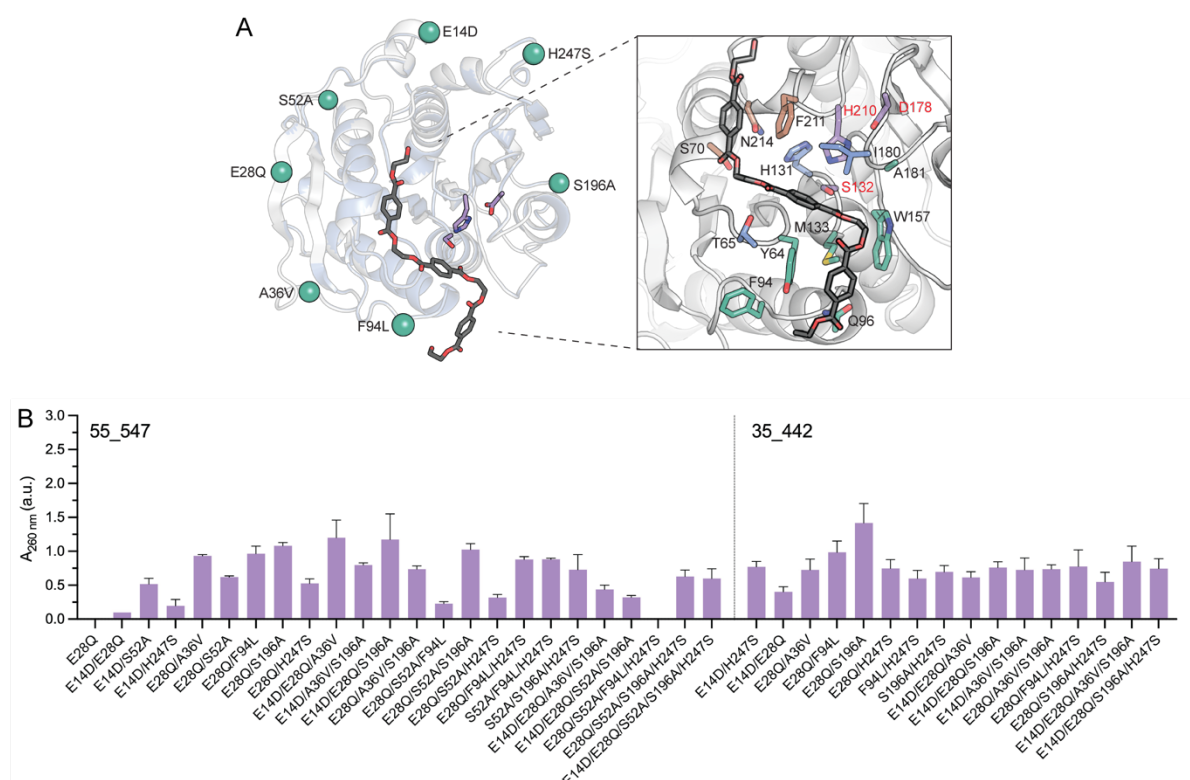
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Figure 4. PETase activities of recombined alternate reconstructions. **A)** Structure of 35_442 and 55_547 aligned. Positions selected for recombination are highlighted as spheres. The docked pose of 2HE-(MHET)$_3$ is shown in a close-up of the binding and catalytic site, and residues that form the putative PET binding site based on homology to LCC are shown. Residues comprising subsites -2 (green), -1 (blue) and +1 (brown) are highlighted. The catalytic residues Ser132-His210-Asp178 are also shown (purple; red labels). **B)** Activity of recombined mutations from alternate reconstructions of 35_442 and 55_547 against amorphous PET film. The bulk soluble products of PET hydrolysis (TPA, MHET, BHET) are measured by absorbance at 260 nm after 16 hours incubation with the enzyme at 60 °C. Data are represented as the mean ± SEM (n = 3) and grouped based on mutations recombined in the background of 55_547 (left) and 35_442 (middle).

A subset of randomly sampled combinations of single mutations from the alternate reconstructions were selected to explore potential epistatic interactions and their impact on PETase activity. The 7 selected mutations, E14D, E28Q, A36V, S52A (in 55_547), F94L, S196A, and H247S, were recombined in various combinations from 2 to 5 point mutations in the background of 35_442 and 55_547. E28Q, A36V, S52A, S196A, and H247S are surface mutations, distal from the catalytic and putative PET binding site (**Figure 4A**). In contrast, F94L is positioned within the PET binding site, as deduced from docking of 2HE-(MHET)$_3$ into both 35_442 and 55_547 (**Figure 4A**), as well as structural homology to previously predicted PET binding sites in LCC. As single mutations, E14D, E28Q, A36V, F94L and H247S were considered neutral based on PETase activity relative to the 35_442 background, while S52A and S196A exhibited decreased activity relative to 55_547. In our experimental

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characterization, we identified 24 recombined variants with increased PETase activity relative to their ancestral background (**Figure 4B**). Specifically, 10 recombined variants in the background of 55_547 showed increased PETase activity, with the most active being E14D/E28Q/A36V (A_{260} nm = 1.20 ± 0.26), E28Q/S196A (A_{260} nm = 1.08 ± 0.05), and E28Q/S52A/S196A (A_{260} nm = 1.03 ± 0.09). Similarly, 14 recombinations in the background of 35_442 demonstrated increased activity, with the most active being E28Q/S196A (A_{260} nm = 1.42 ± 0.29), E28Q/F94L (A_{260} nm = 0.99 ± 0.17), and E14D/H247S (A_{260} nm = 0.77 ± 0.08). Interestingly, we identified 17 recombined variants that exhibited improved PETase activity relative to LCC ICCG, the most active extant variant in the study, with 35_442 E28Q/S196A, displaying ~2.5-fold higher activity.

The mutational analysis of the recombined variants highlighted E28Q as a key mutation, present in 14 of the 17 variants that demonstrated enhanced activity compared to the engineered LCC ICCG variant. This suggests a positive effect of E28Q on PETase activity; however, this was only observed in the presence of other mutations from the recombinations. The context dependence of E28Q is especially significant when considering the double mutation E28Q/S196A, which was among the most active in both ancestral backgrounds. When assessed independently in the 55_547 background, the E28Q mutation adversely affected activity (A_{260} nm = 0.00 ± 0.00), and the S196A mutation similarly led to a reduction in activity relative to the ancestor (A_{260} nm = 0.16 ± 0.02). However, the combination of these mutations resulted in a significant increase in activity beyond the additive effects of the single mutations (A_{260} nm = 1.08 ± 0.05), indicative of positive epistatic interactions.

Ruggedness analysis reveals epistasis in recombined mutations.

We next analyzed the topology of the PETase fitness landscape over the 196 cutinase sequences characterized in this study. This was done both to build a holistic overview of PETase evolution and function in the cutinase family and to assess the effectiveness of this approach in exploring new-to-nature fitness peaks across functional sequence space. To achieve this, we embedded cutinase sequences as nodes in a network graph where edges connect each node to its *k* nearest (Euclidean) neighbors. The scheme used to embed sequences therefore dictates the topology of the network graph. When this is the one-hot encoding (OHE), the Euclidean distance between nodes in the network graph is proportional to the number of mutations between the sequences they represent. The OHE graph network therefore captures PETase activity as a function of the mutations between sequences when the signal over the graph is the measured PETase activity (**Figure 5A**).

12

357   Encoding protein sequences as the hidden states of a PLM can capture comparatively richer

358   features than the OHE[29,30], albeit at the cost of interpretability over the network graph[36].

359   Euclidean distances in the latent space of a representation model may share no interpretable

360   relationship with equivalent Euclidean distances in the OHE space, therefore confounding the

361   interpretation of PETase activity over the network graph to non-linear distances instead of

362   simple mutational distances.

363

364   We embedded all characterized cutinases in a OHE basis and visualized the resulting

365   landscape in 2 dimensions with t-distributed stochastic neighbor embedding (tSNE)

366   dimensionality reduction. In this space, ancestral and extant cutinases form homogenous,

367   random clusters (**Figure 5A**). The alternate reconstructions of ancestors 55_547 and 35_442

368   and their recombinations are grouped as closely connected clusters around their respective

369   ancestral backgrounds. Despite their comparable PETase activity, sequences in both

370   backgrounds are resolved as independent components that share few direct edge

371   connections, suggesting that the PETase fitness landscape is multi-modal (i.e. there are

372   multiple solution spaces to competent PETase activity) when considering only naive, residue-

373   wise OHE sequence embeddings.

374

375   We then reconstructed the PETase fitness landscape in a learned representation space. To

376   ensure that local features of the cutinase sequence space were captured by a PLM, we used

377   a recently described method of local ancestral sequence embedding (LASE)[36]. In brief, LASE

378   trains a small and family-specific deep learning model on ancestrally reconstructed sequence

379   datasets. The features learned by LASE capture the functional properties of proteins, such as

380   catalytic efficiency, in a non-linear space that is not interpretable with simple mutational

381   distances. Embedding in LASE can therefore reveal topological features of the fitness map

382   that are obfuscated in an OHE embedding.

383

384   Sequences in the LASE embedding space cluster according to their relative fitness and how

385   they were sampled (e.g. extant, ancestral, alternate or recombined; **Figure 5B**). For example,

386   all point mutations from alternate reconstructions and recombinations group together in a

387   single connected component in the LASE space, irrespective of the genetic background

388   (ancestors 55_547 or 35_442) they were introduced into. Moreso, ancestral and extant

389   sequences cluster into disconnected components, despite their often high degree of site-wise

390   sequence similarity. Indeed, the LASE representation space is highly structured relative to the

391   OHE space, where ancestral and extant sequences co-occur across distinct identity groups in

392   the network graph. This indicates that our sequence sampling strategy is highly structured and

393 systematic over an evolutionarily informative representation space, while appearing

394 somewhat random in the OHE space.

395

396 Finally, we used a graph signal processing approach to quantify ruggedness in the cutinase

397 PET fitness landscape. We define ruggedness as the non-linearity between the fitness of a

398 sequence and its neighbors in the network graph. We use the Dirichlet energy of the graph,

399 which describes the non-linearity of a signal over a graph, to measure this[36,51,52]. In order to

400 make the Dirichlet energy interpretable as a node-wise local quantity, we calculate it over each

401 subgraph in the network defined by an edge-length of exactly 1, thus reducing its interpretation

402 to the deviation from linearity a node demonstrates relative only to its immediate neighbors;

403 the fitness signal over the network graph changes as a linear function (i.e. is smooth) over

404 nodes of the graph that are characterized by low local DEs. The local Dirichlet energy is

405 therefore a descriptor of how confounded by epistasis a sequence is. This analysis revealed

406 that the fitness landscape is most rugged over the cutinase variants with the greatest PETase

407 activity. Indeed, the node with the single highest local Dirichlet energy is also the fitness peak

408 (ancestor 55_547_E28Q/S196A). Importantly, this was true for both OHE and LASE network

409 graphs (**Figure 5C**; **Supplementary Figure 9**), indicating that the combinatorial mutations

410 E28Q/S196A in the 55_547 background would be unlikely to be introduced through a stepwise

411 mutagenesis approach due to the relatively low activity of each single mutation in isolation.

412 Together, these analyses demonstrate that mASR can effectively guide protein engineering

413 by discovering evolutionary features that are not immediately apparent, and can help navigate

414 rugged regions of sequence space to find fit enzyme variants that are not rationally obvious.
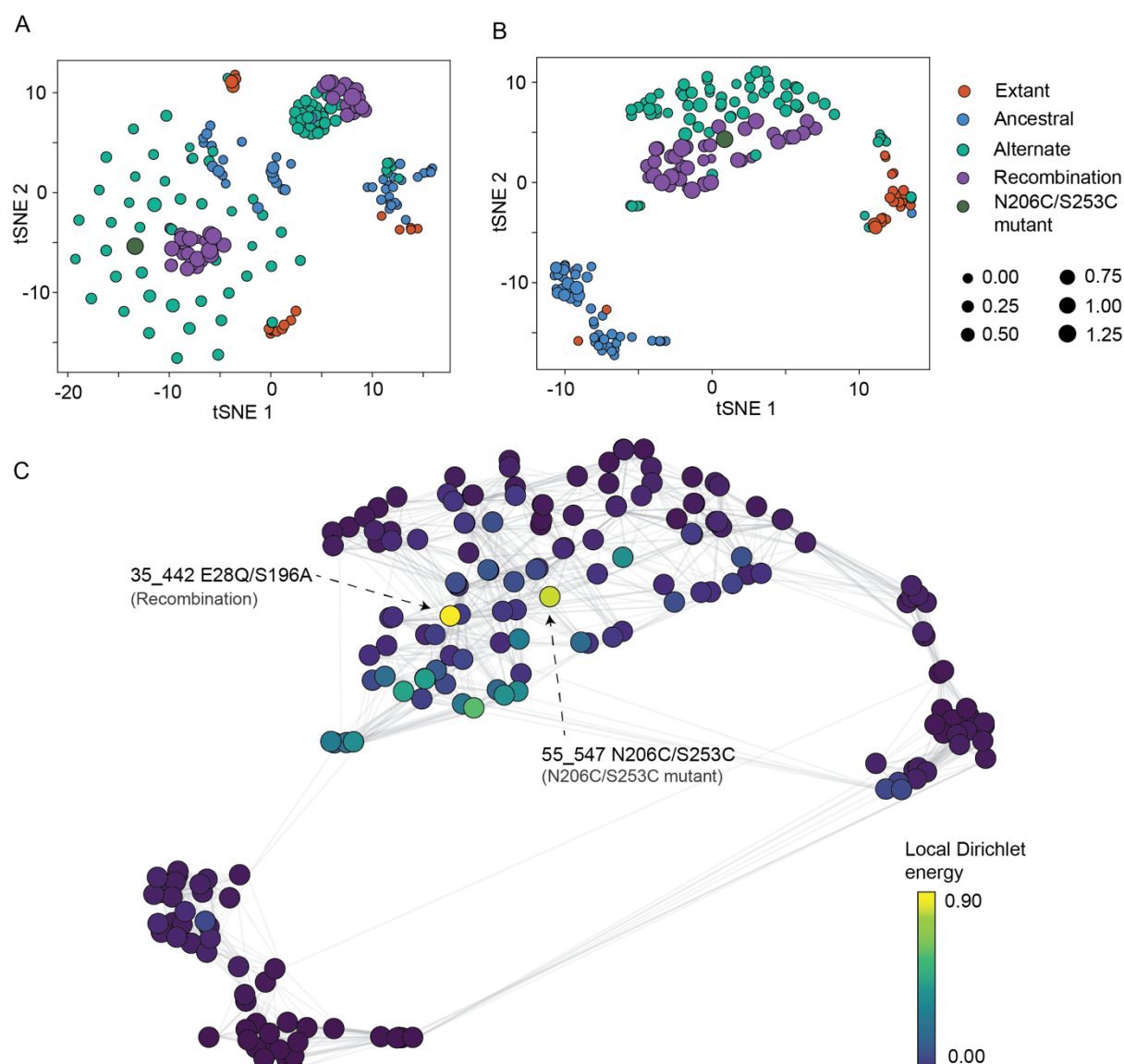
415

Figure 5. Analysis and regression on PETase sequence space. PETase sequences were represented in **A)** OHE- and **B)** LASE-forms and projected into a 2-dimensional space with tSNE. Colour represents design stage and size represents activity ($A_{260 \text{ nm}}$ (a.u.)). The OHE and LASE sequence data was then used to train regression models. **C)** The local Dirichlet energy for each variant was determined over subgraphs that include the variant's immediate neighbors as determined by kNN. Edges connect variants that were found to be neighbors and color represents the local Dirichlet energy calculated.

Discussion

In our investigation into the evolutionary sequence space of bacterial cutinases with PETase activity, we employed multiplexed ASR[36] to enhance our exploration. This method allowed us to reconstruct and analyze ancestral cutinases across 20 diverse phylogenetic topologies, moving beyond the constraints of a single-tree perspective. Our experimental characterizations of 20 extant and 48 ancestral cutinases unveiled a wide spectrum of activities against amorphous PET film (A_{260} nm = 0.00 - 0.59). Of particular interest were two ancestors, 35_442 (A_{260} nm = 0.37 ± 0.06) and 55_547 (A_{260} nm = 0.59 ± 0.09), each representing the most recent common ancestor of LCC[13] and TfCut2[5] on independent trees and exhibiting similar activity to the most active extant cutinases, LCC (A_{260} nm = A_{260} nm = 0.34 ± 0.03) and BhrPETase (A_{260} nm = 0.49 ± 0.01). Notably, the use of mASR was crucial in uncovering the variability of ancestrally reconstructed sequences, as it revealed that equivalent nodes from independent phylogenetic topologies exhibited highly varied activity despite all topologies being equally valid representations of the underlying sequence alignment based on the AU-test. While some ancestors were inactive, others showed significant PETase activity comparable to characterized extant PETases. These observations highlight the utility of the mASR method in improving both the success and robustness of ASR applications in protein engineering. By embracing a wider array of evolutionary scenarios, mASR allowed for a more comprehensive and reliable identification of functional sequences relative to a single-tree approach. Multiplexed ASR may therefore become an important component of ASR- and evolutionary-guided enzyme design strategies in the future.

Our sequence and structural analysis of active and inactive ancestral cutinases provided insights on the evolutionary emergence of PETase activity in the cutinase family. In particular, our findings suggest that PETase activity in the TfCut2 and LCC PETase lineages has emerged through neutral mutations that are distal to the active site, rather than specific changes localized to the active site itself, as observed in the evolution of *I. sakaiensis* PETase[37]. Our detailed examination of ancestors 35_442 and 55_547, along with their closest inactive counterparts, highlighted unique gain-of-function mutations leading to PETase activity from these distinct phylogenetic backgrounds. These findings imply the existence of multiple, distinct evolutionary pathways for acquiring PETase functionality and indicate that PETase activity is readily accessible within the cutinase family.

Our structural analysis also revealed the formation of domain-swapped dimers between adjacent symmetry mates in the crystal structures of the ancestral variants 35_442 and

460   55_547. While possibly an artifact of the crystallization conditions, this observation suggests
461   a certain degree of structural flexibility in the C-terminus of these ancestors even in solution.
462   Based on this observation, we introduced a disulfide bond in the C-terminus of ancestor
463   55_547 that coincided with the predicted Ca^{2+}/Mg^{2+} binding site, a strategy homologous to
464   similar successful modifications in TfCut2 and LCC that were observed to improve stability
465   and activity[6,48,49]. Indeed, the introduction of the disulfide N206C/S253C resulted in a variant
466   of 55_547 with an approximately 2-fold improvement in whole-cell activity and 1.5-fold
467   improvement in soluble expression relative to the background ancestor.

469   We deepened our exploration of the evolutionary sequence space of the cutinase family by
470   addressing ambiguously reconstructed positions in the initial mASR. Ambiguous positions
471   were identified based on a posterior probability threshold of ≥ 0.2 for the second most probable
472   residue. Introducing these 69 alternate reconstructions as single mutations into 35_442 and
473   55_547, we observed that most mutations were either neutral or decreased PETase activity
474   relative to the ancestral background. However, when we recombined a random subset of the
475   alternate reconstructions, we observed several recombinations in the background of both
476   35_442 (E28Q/S196A) and 55_547 (E14D/E28Q/A36V) that displayed increased PETase
477   activity, not only relative to the initial ancestors, but also to an engineered variant of LCC with
478   enhanced activity, LCC[ICCG] [6]. Notably, the most active recombinations exhibited activity
479   improvements that exceeded the additive effects predicted from their individual mutations,
480   highlighting positive epistatic interactions that contribute to their PETase activity.

482   To complement our experimental investigations, we modeled the sequence-fitness landscape
483   of all 196 cutinase sequences characterized in our study, employing a graph signal processing
484   approach that elucidates the complex topology of the PETase fitness landscape. This
485   methodology involved embedding cutinase sequences as nodes in a network graph, where
486   each node was connected to its *k* nearest (Euclidean) neighbors, thereby enabling a direct
487   comparison between two embedding schemes, OHE and LASE. While OHE provides a
488   straightforward mutational distance metric between sequences, it often oversimplifies the
489   nuanced relationship between sequence variation and function. In contrast, LASE, by training
490   a family-specific deep learning model on our dataset of ancestrally reconstructed sequences,
491   captures the functional properties of proteins in an abstract manner, revealing non-linear
492   sequence-activity relationships that are obscured in OHE representations.

494   Using LASE to map the sequence-fitness landscape, we highlighted iterative improvements
495   in PETase activity throughout the different phases of our sequence exploration of the cutinase
496   family. This embedding not only facilitated a deeper understanding of the functional

497   implications of sequence variation but also allowed us to identify clusters of sequences with

498   similar functional profiles, regardless of their evolutionary background. Moreover, our analysis

499   of the fitness landscape's ruggedness via LASE provided new insights into the role of epistasis

500   in PETase activity. The local Dirichlet energy calculations revealed that sequences with the

501   highest PETase activity were associated with the greatest ruggedness, suggesting that the

502   most functionally optimized variants emerge from complex interplays of multiple mutations

503   rather than from linear accumulations of beneficial single mutations. This observation

504   highlights the significance of epistatic interactions in driving the evolutionary innovation of

505   PETase activity, illustrating that successful enzyme variants often lie in regions of the fitness

506   landscape that are not readily accessed through single mutational steps, but can be accessed

507   using evolutionarily-guided approaches, such as mASR.

508

509

Materials and Methods

Ancestral sequence reconstruction. 1000 sequences were collected from the NCBI non-redundant (nr) database with blast using LCC (UniProt: G9BY57) as seed and an e-value cutoff of 1e-5. Sequence redundancy was removed to 90% ID in CD-HIT[53]. Signal peptides were deleted using SignalP4.0[54]. Alignment was performed using the GINSI protocol of MAFFT[55]. 100 replicates of independent model parameterization and tree search (default parameters) were performed using IQTREE2[56] on the NCI GADI supercomputer. The sequence evolution model was parameterized using ModelFinder[57], as implemented in IQTREE2. Branch supports were determined as the ultrafast bootstrap approximation[38] calculated to 1000 replicates, as implemented in IQTREE2. The Approximately unbiased test[41] was conducted to 10000 replicates for all ML topologies. Empirical Bayesian ASR was performed on 20 of the 100 trees that failed rejection by the AU test in CodeML[39] using the ML replacement matrix (LG)[58] with rates modeled as a discrete gamma parameterized with 4 rate categories.

Small-scale protein expression and purification. Plasmids were transformed by heat shock into chemically competent BL21(DE3) *E. coli* cells and plated onto Lysogeny broth (LB) agar supplemented with 100 µg/mL kanamycin and incubated at 37 °C overnight. A single colony was used to inoculate 1.5 mL autoinduction media supplemented with 100 µg/mL kanamycin in a 2.2 mL 96-well deep well block and grown at 1050 rpm at 37 °C for 5 hours, followed by room temperature (RT; 25 °C) for 16 hours.

Cells were harvested by centrifugation at 2000 x g for 15 minutes at RT and resuspended in Lysis Buffer (1X BugBuster® Protein Extraction Reagent (Merck-Millipore), 20 mM Tris, 300 mM NaCl, 1 U/ml Turbonuclease (Sigma) pH 8). The cell suspension was left to incubate at RT for 20 minutes with gentle shaking. The lysate was separated from the insoluble cell debris by centrifugation at 2250 x g for 1 hour at RT.

The clarified lysate was then diluted with 100 µl of Equilibration Buffer (20 mM Tris, 300 mM NaCl pH 8) and purified by nickel-charged IMAC using a 96-well HisPurTM Ni-NTA Spin Plate (ThermoFisher Scientific) equilibrated in Equilibration Buffer, washing the sample three times with 250 µl of Wash Buffer (20 mM Tris, 300 mM NaCl, 10 mM imidazole pH 8) and eluting with 250 µl of Elution Buffer (20 mM Tris, 300 mM NaCl, 150 mM imidazole pH 8). All centrifugation steps following addition of Wash or Elution Buffer were at 1000 x g for 1 minute at RT. The eluate was stored at 4 °C. Bradford assay was used to quantify the soluble expression levels post-purification (**Supplementary Figure 1**).

19

547

548   **UV absorbance assay for PET-degrading activity**. For purified protein from 96-well

549   expression and purification, 15 µl of the eluate from the 96-well Ni-NTA purification and 285

550   µl of Reaction Buffer (50 mM Bicine pH 9) was added to a clear 96-well plate. For purified

551   protein from large-scale expression and purification, 300 µl of 100 nM enzyme in Reaction

552   Buffer was added to a clear 96-well plate. A single disk of amorphous PET (Goodfellow

553   ES301445) with 4 mm diameter and 0.25 mm thickness was added to each well. The plate

554   was incubated at 60 °C for 16 hours. Following incubation, 100 µl of the reaction solution was

555   transferred to a clear UV-transparent 96-well plate and the absorbance was measured

556   between 240 to 300 nm in 10 nm steps using the Epoch Microplate Spectrophotometer

557   (BioTek) (**Supplementary Figure 2**). For comparison of activity of all variants, the absorbance

558   at 260 nm was used. Assays were repeated in triplicate for each variant.

559

560   **Assay data processing.** To correct for possible systematic error between replicate data

561   points, the mean absorbance at 260 nm for each replicate was determined. Using the mean

562   absorbance, a scaling coefficient was assigned to the replicates with the lowest and highest

563   mean values such that the mean of the scaled absorbance values equaled the mean of the

564   replicate with the mid-range mean value. To ensure scaling improved consistency between

565   replicates, correlograms of the data before (**Supplementary Figure 3**) and after

566   (**Supplementary Figure 4**) scaling were produced to confirm the monotonic (rank) correlation

567   between replicates was preserved.

568

569   **Cloning of TEV-PETase variants for crystallography studies.** Primer pairs containing the

570   DNA sequence for the TEV cleavage site (5'-GAAAACCTGTATTTTCAAAGC-3') were

571   constructed, specific to each PETase variant. PCR was performed using these primers and

572   PETase variant genes to create mutant fragments. These fragments were reassembled using

573   Gibson Assembly[59] and checked through Sanger sequencing to ensure the TEV cleavage site

574   was correctly introduced.

575

576   **Large scale protein expression and purification.** The TEV-PETase ancestral variants

577   plasmids were transformed using electroporation into electrocompetent E. cloni® cells

578   (Lucigen) and plated onto LB agar supplemented with 100 µg/mL kanamycin. The plates were

579   incubated overnight at 37 °C. A single colony was inoculated into a 10 mL solution of LB media

580   with 100 µg/mL kanamycin and incubated overnight at 37 °C and 180 rotations per minute

581   (rpm). This liquid starter culture was then added to 1 L of autoinduction media[60] (6 g Na_2HPO_4,

582   3 g KH_2PO_4, 20 g tryptone, 5 g yeast extract, 5 g NaCl, 10 mL of 60% (v/v) glycerol, 5 mL of

583   10% (w/v) glucose, and 25 mL of 8% (w/v) lactose) with 100 µg/mL kanamycin and incubated

584   for 24 hours at room temperature and 180 rpm. The cells were separated from the media by

585   centrifugation at 5000 × g for 15 minutes at 4 °C and resuspended in lysis buffer (400 mM

586   NaCl, 25 mM imidazole, 1 U/mL Turbonuclease (Sigma), and 50 mM Tris-HCl pH 8.0). The

587   resuspended cell solution was lysed using two rounds of sonication at 50% power and pulse

588   time for 5 minutes, with 5 minutes on ice between sonication steps. Next, the sample was

589   centrifuged at 32000 × g for 60 minutes at 4 °C, and the soluble cell solution was separated

590   from the insoluble cell material and filtered through a 0.45 µm pore size filter. The filtered

591   soluble cell solution was passed through an equilibrated Nickel-charged IMAC using a 5 mL

592   HisTrap HP (GE Healthcare Life Sciences) in Lysis Buffer. The protein bound to the column

593   was eluted using elution buffer (400 mM NaCl, 500 mM imidazole, and 50 mM Tris-HCl pH

594   8.0). The protein sample was buffer exchanged to TEV reaction buffer (100 mM NaCl, 0.5 mM

595   EDTA, 1 mM DTT, 1% (v/v) glycerol, and 50 mM Tris-HCl pH 8.0) using a PD-10 desalting

596   column and diluted to 50 mL in this buffer. A 1 mL solution containing 1 mg/ml of purified TEV

597   protease was added and incubated at room temperature overnight. The cleaved sample was

598   passed through an equilibrated Nickel-charged IMAC using a 5 mL HisTrap HP (GE

599   Healthcare Life Sciences), and the flowthrough was collected. This flowthrough was

600   concentrated using the 3 kDa Amicon® ultra 15 mL centrifugal filters and filtered through a

601   0.22 µm filter. Finally, the cleaved protein was purified to homogeneity using size-exclusion

602   chromatography, and the HiLoad 26/600 Superdex 200 column (GE Healthcare Life Sciences)

603   was equilibrated in size-exclusion buffer (150 mM NaCl, 25 mM HEPES pH 7.5).

604

605   **Protein crystallisation and structure determination.** Proteins were concentrated using the

606   3 kDa Amicon® ultra 15 mL centrifugal filters to 15-36 mg/ml and crystallized in 20% (w/v)

607   PEG 3350 alongside 0.2 M salt and BisTris buffer solution. Specifically, ancestor 55_547 in

608   0.2 M sodium/potassium tartrate, 0.1 M BisTris propane pH 7.5 and 20% (w/v) PEG 3350; and

609   ancestor 35_442 in 0.2 M sodium malonate, 0.1 M BisTris propane pH 6.5 and 20% (w/v) PEG

610   3350. The X-ray diffraction data were collected on the MX2 beamline at the Australian

611   Synchrotron[61]. The data was processed using XDS[62], and the phase problem was resolved

612   with molecular replacement using the PETase WT structure (PDB: 6EQE) as the search

613   model. The ligands and solvent molecules were removed and then used as the search model

614   part of Phaser (CCP4)[63]. The structure was refined using phenix.refine[64] through multiple

615   iterative steps, and rebuilt each time with Coot[65]. The structures of ancestors 55_547 and

616   35_442 were deposited in the protein data bank under the PDB ID of 8ETX and 8ETY,

617   respectively.

618

619   **Protein sequence representations.** To analyze PETase sequence space One-hot

620   embeddings (OHE) and Learned Ancestral Sequence Embeddings (LASE) were made. To

621   produce OHE, aligned PETase sequences were converted into a (20×267) vectors where

622   gaps were represented as a zero vector of length 20. The LASE embedding model was

623   implemented as a Transformer in PyTorch 2.0.1 as previously described[36], with three encoder

624   blocks with 2-headed multihead attention (64 dimensions) and a feed-forward fully-connected

625   layer (128 dimensions). The LASE embedding model was trained with a masking percent of

626   15%, over 100 epochs with a batch size of 32 using the Adam optimizer. Loss was determined

627   as the categorical cross entropy loss. Performance over training was assessed with perplexity

628   and categorical accuracy (**Supplementary Figure 8**).

629

630   **Local Dirichlet energy calculations.**

631   To estimate the local ruggedness of each PETase variant, the k-nearest neighbors of each

632   node were used to produce a KNN sub-graph for each variant with scikit-learn 1.2.1. The kNN

633   sub-graphs were made symmetric by defining an edge in either direction to be a single edge.

634   The dirichlet energy was calculated as previously described[52,66]:

635

636 $$\lambda_m = 1/N \, y^T L y$$

637

638   Where, λ_m is normalized dirichlet energy, N, the number of variants in the sub-graph, y, the

639   activity (absorbance) of each variant and L the graph Laplacian operator of the adjacency

640   matrix of each kNN sub-graph.

641

642   **Acknowledgements**

643   This research was undertaken in part using the MX2 beamline at the Australian Synchrotron,

644   part of ANSTO, and made use of the Australian Cancer Research Foundation (ACRF)

645   detector.

646

647   **Availability**

648   The code for model training and analysis is available on GitHub:

649   https://github.com/RSCJacksonLab/cutinase_lase

650   Deposited crystal structures are available on the Protein Data Bank under accession IDs

651   8ETY and 8ETX.

652

653   **Note**

654

655   The authors declare the following competing financial interest(s): C.J.J., V.V., M.A.S., R.G.,

656   D.M., J.S., A.M.D., and J.T. hold equity in the plastic recycling company, Samsara Eco.

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