

1 **Formation of brain-wide neural geometry during visual item
2 recognition in monkeys**

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48 designed the experiments. H.Y., H.C., J.K., Y.I., and T.M. performed the experiments. H.Y.

49 and Y.T. developed the analytical tools. H.Y., H.C., J.K., and Y.H. analyzed the data. H.Y.,
50 H.C., and J.K. wrote the manuscript. All authors edited and approved the final version of
51 the manuscript.

52 **Data availability:** All data and analysis codes used in this study are available in the
53 supporting files.

54 Exp.1: Analysis code: Analy_mainchen.r and AnalyCue_PCAChen.r

55 Data: ChenMatData_All1506_inter_ranked.csv for 50 ms time bin

56 Chen_CellListAll1506.csv for cell type list

57 Exp. 2: Analysis code, Analy_mainkuni.r and AnalyCue_PCAKuni.r

58 Data: KuniMatData_All116_nointer_ranked.csv for 50 ms time bin

59 Exp. 3: Analysis code, Analy_mainhori.r and AnalyCue_PCAhori.r

60 Data: HoriMatData_All150.csv for 50ms time bin

61 Exp. 4: Analysis code, Analy_mainyamadai.r and AnalyCue_PCAyamada.r

62 Data: MatDataPCAProMag_50ms2021Sep09.txt for 50 ms data

63 CellList_DSVSOFcMofC2019_0116.csv for cell type list

64 Common code for all experiments (1 to 4):

65 ParaData_BS1k50ms3ave.csv: Bootstrap replicate Data for the selected
66 geometric features.

67 ParaData_BS1k50ms3aveLissague3final.csv: bootstrap replicate Data for
68 Lissajous curve.

69 Analysis code for PCA: Analy_pca1.0final.r.

70

71 **Abstract (150/150)**

72 Neural dynamics assumes to reflect computations that relay and transform information in
73 the brain. Previous studies have identified the neural population dynamics in many
74 individual brain regions as a trajectory geometry, preserving a manifest of computational
75 motifs. However, whether these populations share particular geometric patterns across
76 brain-wide neural populations remains unclear. Here, by mapping neural dynamics widely
77 across temporal/frontal/limbic regions in the cortical and subcortical structures of monkeys,
78 we show that 10 neural populations, including 2,500 neurons, propagate visual item
79 information in a stochastic manner. We found that visual inputs predominantly evoked
80 rotational dynamics in the higher-order visual area, TE and its downstream striatum tail,
81 while curvy/straight dynamics appeared frequently downstream in the
82 orbitofrontal/hippocampal network. These geometric changes were not deterministic but
83 rather stochastic according to their respective emergence rates. Our meta-analysis results
84 indicated that visual information propagates as a heterogeneous mixture of stochastic
85 neural population signals in the brain.

86

87 **Introduction**

88 Visual inputs activate a large number of neurons in the brain that construct numerous
89 neural networks to process information in an environment (1-3). This brain-wide activity
90 change reflects the information processing embedded in each individual neural circuit;
91 however, limitations of spatial and temporal resolution in the measurements of circuitry
92 activity disrupt our understanding of brain-wide visual information processing (4-9). Under
93 this limitation, considerable attempts have been made toward understanding how the brain
94 processes information using a variety of developing theoretical frameworks (10-15).

95 One of the analytic frameworks developed within the last decade is state-space
96 analysis (16) that provides a mechanistic structure of information processed in the lower-
97 dimensional space of a neural population (17-19). This analytical tool identified dynamic
98 neural population structures that reflect information processing for general biological
99 features (20, 21) and allowed us to describe those features as a neural geometry in a fine
100 time resolution (13-15) in the sub-second order. A large number of unidentifiable neural
101 circuits may process information moment-by-moment (6), and they may form a population
102 geometry, such as rotational (18), curvy (19, 22), or straight geometries (23), as the typical
103 and basic features of dynamics. A recent finding suggests that the combination of neural
104 population geometries may be the key to processing information to transform sensory
105 inputs into memory (24). Recent studies have extended these analytical frameworks (25-
106 29); however, because of poor comparisons among brain-wide neural populations, how
107 the brain processes information in the form of geometry remains elusive.

108 To examine how brain-wide neural dynamics are formed to process visual information,
109 we accumulated the neural population data of monkeys from four laboratories that
110 contained 10 neural populations, including 2,500 neurons across temporal/frontal/limbic
111 networks (i.e., meta-analysis). We applied targeted dimensional reduction, with a

112 bootstrap resampling technique that detects and replicates neural modulation dynamics
113 in a low-dimensional neural space. Following a parametric bootstrap analysis using the
114 Lissajous curve function, our cross-study comparison revealed that a gradual shift in
115 stochastic neural population signals occurred throughout the temporal-to-frontal brain
116 regions.

117

118 **Results**

119 We compared the trajectory geometries across many neural populations widely distributed
120 in the brain from the output brain regions in the ventral visual pathway (30-33) and its
121 downstream brain regions that may access memories associated with a visual stimulus.
122 These included ten brain regions that were accumulated from nine monkeys examined in
123 the four laboratories (Table. S1), from the higher-order visual area TE and their
124 downstream brain regions in cortical, subcortical, and limbic structures, such as the
125 temporal/orbitofrontal cortices, striatum, and hippocampus (HPC) (Fig. 1A, No. 1 to 10). A
126 total of 2,500 neurons were accumulated across the four behavioral tasks (Fig. S1), in
127 which visual items provided monkeys with position and/or reward information during the
128 active (Exps. 1 and 3), and passive (Exps. 2 and 4) behavioral responses. Using state-
129 space analysis, we characterized structures of neural population geometry that appeared
130 in the lower dimensional neural space, which describes how neural modulation by the task
131 parameters of interest processes information at the population level (23, 29).

132 We found all three types of geometric patterns, rotational, curvy, and straight
133 geometries, in the top two dimensions (Fig. 1B-D, see Fig. S2 for performance as the
134 percentage of variance explained), including unclear structures based on visual inspection
135 (Fig. 1E). All the 10 neural populations showed a significant structure at the principal
136 component (PC)1-2 plane based on shuffle controls (Fig. S3, $P < 0.05$ for all PC1 and

137 PC2). PC3 did not show statistical significance in some neuronal populations (Fig. S3, Exps.
138 2 and 4; compare the black and gray dots for each PC). These identified geometric
139 structures appeared to be distributed from complex to simple, reflecting the circuit distance
140 to the visual input (Fig. 1). For example, TE (Fig. 1B, No. 1, A11 plane in A) and its
141 downstream region striatum tail (STRt) (Fig. 1B, No. 2, A11 plane in A), showed rotational
142 geometries during visual item recognition. In more detail, at the beginning of information
143 processing after the visual item presentation (Fig. 1B left, see green **s** at time = 0), the
144 neural state was positioned at around the center of the PC1-2 plane, and then rotated at
145 approximately 0.2 s and started to move the second quadrant with the counterclockwise
146 rotation going back close to the initial point (see green **e** 0.6 s after visual item onset). An
147 opposite rotation was observed for the worst visual item, with a smaller change (orange).
148 These rotational structures were also observed at the STRt on a similar timescale (Fig.
149 1B, right).

150 In the downstream brain regions, such as the perirhinal cortex (PRC) and caudate
151 body (CDb), rotational or curvy dynamics were observed (Fig. 1C, No. 3, PRC, A11 plane
152 in A and No. 4, CDb, A23 plane in A), which were characterized by a half rotation ending
153 at the opposite neural space and end points deviating from the initial point, although it was
154 unclear whether they showed rotational or curvy dynamics. In contrast, straight dynamics
155 were observed in brain regions far away from the visual inputs in the HPC (Fig. 1A, No. 5
156 in the A11 plane, Fig. 1D) and central part of the orbitofrontal cortex (cOFC) (Fig. 1A, No.
157 7 in the A32 plane, Fig. 1D). In addition, the ventral striatum (VS) showed straight
158 dynamics (Fig. 1A, No. 6 in the A23 plane, Fig. 1D), although some structures could not
159 be clearly determined (Fig. 1E, parahippocampal cortex, PHC, medial orbitofrontal cortex,
160 mOFC). The straight dynamics also showed a geometric change back and forth along the
161 straight trajectory (Fig. 1D). These qualitative observations based on visual inspection

162 suggest that neural population structures may change dynamically through visual
163 recognition process, and the shift of neural population geometries might occur throughout
164 the cortical and sub-cortical structures across the temporal/frontal/limbic network.

165

166 **Evaluation of geometric patterns based on their selected features**

167 To quantify these geometric patterns occurring at approximately half a second, we
168 estimated indices for the characteristics of dynamic neural changes in the low-dimensional
169 neural state (Fig. 2A). They were as follows: accumulated angle difference weighted by
170 deviance, $\Sigma d \theta$, which reflects a measure similar to the centrifugal force (see Materials
171 and Methods for details, Fig. 2A, top); mean distance of vectors (d , Fig. 2A, top); rotational
172 speed ($\Theta/0.1$ s, Fig. 2A, bottom); and distance between start and end of trajectory (d_{S-E} ,
173 Fig. 2A, bottom). Following the replication of the neural population geometries based on
174 the bootstrap resampling technique (see Materials and Methods), we calculated these
175 parameter values for each replicated neural population.

176 We found that across the 10 neural populations, these indices captured geometric
177 features to some extent, similar to the rotational geometries observed in the TE and STRt
178 (Fig. 2B-E). For instance, identified clusters based on the dendrogram and principal
179 component analysis (PCA) (Fig. 2B-C) showed that they possess a rotational
180 characteristic with high rotational speed (Fig. 2D, right, red), large $\Sigma d \theta$ (Fig. 2D, middle,
181 red), large d (Fig. 2D, middle, red), and small d_{S-E} (Fig. 2D, left, red), which occupy more
182 than 90% of the STRt population in the best item condition (Fig. 2E, see also Fig. 1B, right
183 green trajectory). A smaller rotational structure characterized by smaller values of $\Sigma d \theta$
184 was also captured by another cluster (Fig. 2D and E, shallow red), which occupied
185 approximately 90% of the STRt population in the worst item condition (Fig. 2E, see also
186 Fig. 1B right, orange trajectory). These rotational features were observed in other temporal

187 brain regions (Fig. 2E, see reddish, more than 50% in TE, 20-40% in PRC and PHC), but
188 merely observed at the frontal/limbic brain regions, such as HPC (less than 10% in all
189 remaining brain regions). In contrast, curvy/straight dynamics were observed in other
190 clusters in the downstream brain regions (Fig. 2E, green and blue).

191 Collectively, in each of the 10 brain regions, a cluster with high rotational speed
192 occupied the STRt and half of the TE populations (Fig. 2D, reddish), while the
193 curvy/straight dynamics occupied most of the replicates in the remaining cortical and
194 subcortical regions (Fig. 2D and E, blue and green).

195

196 **Parameterization of geometric patterns using Lissajous curve function**

197 To parameterize these geometric features in more detail, we fitted the Lissajous curve
198 function (34) to the replicated data, which can mathematically capture all rotational, curvy,
199 and straight dynamics by this single function. In the Lissajous function, any two-
200 dimensional geometric features represented by $F(x, y)$ are captured using the following
201 equations:

202
$$x = Ax \cos (\omega x t(i) + \Phi x) + bx \quad (1)$$

203
$$y = Ay \cos (\omega y t(i) + \Phi y) + by \quad (2)$$

204 where ω and Φ represent cycle of the rotation and their deviance as a function of time, $t(i)$.
205 $t(i)$ takes the values from 0 to 0.6 s in all the four experiments, and thus, one cycle of the
206 trajectory is represented as 0 to 3.33π for ω . For the horizontal and vertical axes, Ax and
207 Ay define the amplitude of the trajectory, respectively, whereas bx and by determine its
208 location. In this function, rotational dynamics is represented by the same ω among x and
209 y formulas, and 0.5π cycle differences in Φ values between x and y formulas (Fig. 3A,
210 left, see also Fig. S4A for more details). We note that this rotational example represents
211 less than one cycle due to $\omega x = 3.0 \pi$. In contrast, straight dynamics are represented with

212 the same ω and also same ϕ values between the two formulas (Fig. 3A, right, see also
213 Fig. S4C). Curvy dynamics are represented with some difference of ω and same ϕ values
214 (Fig. 3A, middle, see also Fig. S4B). We fitted this Lissajous curve function to each of the
215 20,000 bootstrap replicates derived from the 10 neural populations (see Materials and
216 Methods, 1000 replicates times 10 populations times two conditions). For instance, three
217 replicated examples obtained from the HPC population were well captured by the
218 Lissagous curve function, as rotational-to-straight trajectories (Fig. 3B). We obtained all
219 the estimates for these parameters (Fig. 3C), and thereafter, applied clustering to these
220 data (Fig. 3D-F) to identify geometry types as a function of the Lissajous curve parameters.

221 We found that the rotational dynamics (Fig. 3G-H, clusters C1-C5, reddish) appeared
222 at the TE and STRt, which occupied high percentages of these neural populations (Fig.
223 3H, approximately 70%), and they were also observed in more than 50% of temporal brain
224 regions. Cluster 5 seemed to have the intermediate characteristics between rotational and
225 curvy structures; if we define this cluster 5 as the curvy one, the rotational percentage
226 becomes low in the PRC, PHC, and HPC (30-40%), but not in the STRt (50-70%). Curvy
227 structures were predominantly observed in the CDb population in more than 40% (Fig. 3G
228 and H, Clusters 6 and 7, greenish). These clusters were note observed deterministically
229 but rather stochastically, as also seen in the predominant percentages of intermediate
230 features between curvy and straight dynamics (Fig. 3G and H, Cluster 8). Straight
231 dynamics were predominant at the frontal brain regions, while they were also observed at
232 the temporal cortices (Fig. 3G and H, Clusters 8-10, bluish). Even with the STRt, the neural
233 population contained curvy or straight dynamics in more than 20%. These heterogeneous
234 mixtures of replicated signals in each population suggested that neural dynamics emerged
235 in a stochastic manner with a functional gradient in the temporal/frontal/limbic networks of
236 cortical and subcortical structures. The brain-wide neural population may propagate item

237 information as a heterogeneous mixture at approximately half a second.

238

239 **Discussion**

240 Collectively, our results revealed that parts of the orbitofrontal cortex (cOFC and mOFC)
241 and their target subcortical brain region VS predominantly showed curvy, straight, and
242 intermediate dynamics (Fig. 3G-H). These dynamics exhibited maximum modulation at
243 approximately 0.3 sec after visual onset, except in the slowest VS dynamics (Fig. 1D).
244 Rotational dynamics were observed at the temporal cortices and their connected striatal
245 regions, at the relatively shorter latency around 0.2 s when rotation started (Fig. 1B).
246 Remarkably, the rotational dynamics were observed at different neural proportions of
247 replicated population in a stochastic manner (Fig. 3H), whereas different monkeys
248 performed active (Exps. 1 and 3), and passive (Exps. 2 and 4) behavioral tasks. In contrast,
249 straight dynamics started its geometric change approximately after 0.2 s of the visual onset
250 (Fig. 1D, see the distance between initial point S and 0.2 s location), indicating that they
251 follow the rotational dynamics. Taken together, these three dynamics were distinctive in
252 terms of geometric patterns and their dynamic changes over time (Fig. 4B for summary),
253 in which a rotational/curvy change was followed by a change in straight dynamics.

254 A previous study showed that rotational dynamics have been uncovered broadly in
255 the primary sensory (24, 35) and motor (36) cortices, which are closer to the inputs and
256 outputs of the brain, such as motor unit activity (37). Other studies have shown that the
257 prefrontal cortex (38, 39) and parietal cortex (22, 35) exhibit curvy dynamics. We found
258 curvy dynamics in the CDb, where action information was transferred from the cortices
259 (40). These characteristic differences in the individual previous studies were not
260 deterministic, similar to the stochastic differences among the populations observed in the
261 present study, which may reflect the neural computations processed in the brain.

262 In the present study, we specifically focused on neural dynamics in two core areas: i)
263 low-dimensional geometries and ii) neural modulation dynamics. First, although these data
264 were obtained from four different laboratories using distinctive behavioral tasks during the
265 passive and active responses of monkeys, the low-dimensional features of neural
266 dynamics are thought to be preserved across mammals in the brain-wide network (41, 42).
267 A recent study provides clear evidence that different animal species share and preserve
268 their neural geometries during behavioral tasks (41). It is suggested that a low-dimensional
269 manifold in the neural state space might be one of the representational states of
270 biologically relevant information, similar to many combinations of physical properties in the
271 world (43). Second, the dynamics in neural modulations examined here are comparable
272 with those using the standard analytic frameworks in the rate coding model, which has
273 provided a huge amount of knowledge corresponding to low-dimensional neural activity
274 modulation in the literature, such as the Gabor function in the visual cortices (44, 45),
275 movement direction and muscle force in the motor cortex (46, 47), reward value in the
276 parietal cortex (48), and comprehension of the location of animals during navigation in the
277 HPC (49). Thus, in our analysis, the dynamics of these well-known brain region features
278 were compared as the geometric patterns across neural populations during visual
279 recognition (29).

280 One concern with our approach is that there may be limitations in data interpretation
281 in terms of data sharing and comparisons across different behavioral tasks and different
282 individual animals. Is it possible to compare the neural population trajectory using
283 accumulated data across animals and tasks with a certain analytical tool? In previous
284 literature, when we analyzed neural modulation using a linear regression model,
285 comparisons of firing rate modulations were accepted by most neurophysiologists for
286 different animals as well as different behavioral tasks. In one study, a challenge was made

287 to compare the neural modulation dynamics as the trajectory geometry between different
288 laboratories' data (50). Thus, the neural trajectory would be comparable among our shared
289 data with greater deliberation.

290 Our findings would add to the emerging literature describing how visual inputs alter
291 the brain-wide neural dynamics associated with visual memories by connecting neural
292 geometry types and their alignments across many brain regions. Previous studies have
293 shown the existence of different types of neural population dynamics in each individual
294 study (22, 24, 35, 36, 38, 39). Although some of these dynamics may reflect task demand,
295 as observed in the dorsolateral prefrontal cortex (38, 51), they are difficult to disentangle
296 from changes in behavior and neural activity levels and may involve some transformation
297 of information for behavioral responses (52). It is possible that the dorsal and motor-related
298 brain regions have this type of flexibility in their dynamics, as partly observed in this study
299 in the CDb, where curvy dynamics were predominantly observed (Fig. 4B).

300 Our results raise the possibility that geometric features determine the important neural
301 mechanisms widely observed in the brain. For instance, the stochastic gradient relative
302 distance to the visual input may reflect the dynamics of the neural circuitry in half a second
303 (Fig. 4B). The unidimensional straight dynamics in the hippocampal-frontal circuitry may
304 reflect memory access during visual recognition, such as location and reward. The
305 rotational dynamics might reflect the visual recognition process, during which recurrent
306 feedback signals change the circuit dynamics. Future studies should test the underlying
307 mechanisms and define whether engagement is best considered a change in behavior
308 and/or task context for whole-brain neural population activity. Regardless of the
309 mechanism, the shift of modulation structures in the lower-dimensional neural space could
310 play a fundamental role in brain-wide information processing, such as transforming visual
311 feature recognition to memory access.

312

313 **Materials and Methods**

314 **Subjects and experimental procedures**

315 Nine rhesus monkeys were used in the present study (Exp. 1: *Macaca mulatta*, A, 9.3 kg,
316 male; *Macaca mulatta*, D, 9.5 kg, male; Exp 2: *Macaca mulatta*, WK, 12.0 kg, male;
317 *Macaca mulatta*, SP, 7.0 kg, male; Exp 3: *Macaca mulatta*, BI, 8.2 kg, male; *Macaca*
318 *mulatta*, FG, 11.0 kg, male; *Macaca mulatta*, ST, 5.2 kg, male; Exp 4: *Macaca mulatta*,
319 SUN, 7.1 kg, male; *Macaca fuscata*, FU, 6.7 kg, female). All experimental procedures were
320 approved by the Institutional Animal Care and Use Committee of Laboratory Animals
321 approved by Peking University (Exp. 1, project number Psych-YujiNaya-1), and Animal
322 Care and Use Committee of the National Eye Institute, and complied with the Public Health
323 Service Policy on the Humane Care and Use of Laboratory Animals (Exp. 2, protocol
324 number NEI-622), the Animal Ethics Committee of the National Institutes for Quantum
325 Science and Technology (Exp. 3, protocol no. 11-1038-11), and the Animal Care and Use
326 Committee of the University of Tsukuba (Exp. 4, protocol no H30.336). All procedures
327 were performed in compliance with the US Public Health Service Guide for the Care and
328 Use of Laboratory Animals.

329

330 **Behavioral task**

331 *Exp. 1. Item-location-retention (ILR) task.* The animals performed the task under dim light
332 conditions in an electromagnetically shielded room. The task started with an encoding
333 phase, which was initiated by the animal pulling a lever and fixating on a white square
334 (0.6°) presented within one of four quadrants at 12.5° (monkey A) or 10° (monkey D) from
335 the center of the touchscreen (3M™ MicroTouch™ Display M1700SS, 17 in), situated
336 approximately 28 cm from the subjects. The eye position was monitored using an infrared

337 digital camera with a sampling frequency of 120 Hz (ETL-200, ISCAN). After fixation for
338 0.6 s, one of six items (3.0° for monkey A and 2.5° for monkey D, radius) was presented
339 in the same quadrant as a sample stimulus for 0.3 s, followed by another 0.7 s fixation on
340 the white square. If the fixation was successfully maintained (typically < 2.5°), the encoding
341 phase ended with the presentation of a single drop of water.

342 The encoding phase was followed by a blank interphase delay interval of 0.7–1.4 s
343 during which no fixation was required. The response phase was initiated using a fixation
344 dot presented at the center of the screen. One of the six items was then presented at the
345 center for 0.3 s, as a cue stimulus. After another 0.5 s delay period, five disks were
346 presented as choices, including a blue disk in each quadrant and a green disk in the center.
347 When the cue stimulus was the same as the sample stimulus, the animal was required to
348 make a choice by touching the blue disk in the same quadrant as the sample (i.e., the
349 match condition). Otherwise, the subject was required to choose the green disk (i.e., non-
350 match condition). If the animal made the correct choice, four–eight drops of water were
351 provided as a reward; otherwise, an additional 4 s was added to the standard inter-trial
352 interval (1.5–3 s). The number of reward drops was increased to encourage the animal to
353 maintain good performance in the latter phase of a daily recording session, which was
354 typically conducted in blocks (e.g., a minimal set of 60 trials with equal numbers of visual
355 items presented in a match/nonmatch condition). During the trial, a large gray square (48°
356 on each side) was presented at the center of the display as a background. At the end of
357 the trial, all stimuli disappeared, and the entire screen displayed a light red color during
358 the inter-trial interval. The start of a new trial was indicated by the reappearance of a large
359 gray square on the display, at which point the monkey could pull the lever, triggering the
360 appearance of a white fixation dot.

361 In the match condition, sample stimuli were chosen pseudo-randomly from six well-
362 learned visual items, and each item was presented pseudo-randomly within four quadrants,
363 resulting in 24 (6 × 4) configuration patterns. In the non-match condition, the location of
364 the sample stimulus was randomly chosen from the four quadrants, and the cue stimulus
365 was randomly chosen from the remaining five items that differed from the sample. The
366 match and non-match conditions were randomly presented in a ratio of 4:1, resulting in 30
367 (24 + 6) configuration patterns. The same six stimuli were used during all the recording
368 sessions.

369 *Exp. 2. Scene-based object-value task.* Animals learned the scene-object associations.
370 After the monkeys fixated on the red-square fixation point on the scene image for 0.6–1 s,
371 the fixation cue disappeared, and two visual items (objects of different values) appeared
372 simultaneously in a different hemifield (for training and neuronal testing) or the same
373 hemifield (for pharmacological experiments). A reward was given after the monkeys made
374 a saccade to the stimulus and maintained fixation for 0.2 s. Half of the fractal visual items
375 were associated with a large reward (0.3 mL), and the other half were associated with a
376 small reward (0.1 mL). This reward association changed depending on the scene (Fig. S1
377 D). *Passive Viewing Task.* One of the two scene images was presented for 0.8 s randomly.
378 If the monkey fixated on a central red square, two to four fractals were presented
379 sequentially on the scene image within the neuron's receptive field (presentation time, 0.4
380 s; interstimulus interval, 0.4 s; Fig. S1C). A liquid reward (0.2 mL) was delivered 0.3 s after
381 the last object was presented. Thus, reward occurrence was not associated with any of
382 the visual items. Each item was presented at least seven times per session.

383 *Exp. 3. Delayed reward tasks.* The monkeys were seated on a primate chair inside a dark,
384 sound-attenuated, electrically shielded room. A touch-sensitive bar was mounted on the
385 chair. The visual stimuli were displayed on a computer video monitor placed in front of the

386 animals. Each of the six cues was associated with a combination of reward size (1 drop;
387 3 or 4 drops) and reward delay (0, 3.3, and 6.9 s). The trials began when the monkey
388 touched the bar. A visual cue appeared, and the monkey released a bar when a red spot
389 (waiting signal) turned green (go signal) after a variable interval. If the monkey released
390 the bar 0.2–1 s after this go signal, the trial was considered correct and the spot turned
391 blue (correct signal). A liquid reward of a small (1 drop, approximately 0.1 mL) or large
392 amount (3 drops, except for monkey BI, 4 drops) was delivered immediately (0.3 ± 0.1 s)
393 or with an additional delay of either 3.3 ± 0.6 s or 6.9 ± 1.2 s after correct release of the
394 bar. The cues were chosen with equal probability and were independent of the preceding
395 reward condition. Anticipatory bar releases (before or no later than 0.2 s after the
396 appearance of the go signal) and failure to release the bar within 1 s of the appearance of
397 the go signal were counted as errors. In the error trials, the trial was terminated
398 immediately, all visual stimuli disappeared, and following inter trial interval (1 s), the trial
399 was repeated; that is, the reward size/delay combination remained the same as that in the
400 error trial. Behavioral control and data acquisition were performed using a real-time
401 experimentation system (REX) (53). The Neurobehavioral Systems Presentation software
402 was used to display the visual stimuli (Neurobehavioral Systems).

403 *Exp. 4. Cued lottery tasks.* The animals performed one of two visually cued lottery tasks:
404 a single-cue or a choice task. Neuronal activity was only recorded during the single-cue
405 task.

406 Animals performed the task under dim lighting conditions in an electromagnetically
407 shielded room. Eye movements were measured using a video camera system at 120 Hz
408 (EyeLink, SR Research). Visual stimuli were generated using a liquid-crystal display at 60
409 Hz, placed 38 cm from the monkey's face when seated. At the beginning of the single-cue
410 task trials, the monkeys had 2 s to align their gaze within 3° of a 1° -diameter gray central

411 fixation target. After a fixation for 1 s, a pie chart was presented for 2.5 s, to provide
412 information regarding the probability and magnitude of rewards in the same location as
413 the central fixation target. The probability and magnitude of the rewards were associated
414 with the number of blue and green 8° pie chart segments, ranging from 0.1 to 1.0 mL in
415 0.1 mL increments for magnitude, and 0.1 to 1.0 in 0.1 increments for probability. Following
416 a 0.2 s interval from the removal of the pie chart, a 1 kHz or 0.1 kHz tone of 0.15 s duration
417 was provided to indicate reward or no-reward outcomes, respectively. After a 0.2 s interval
418 following the high tone, a fluid reward was delivered, whereas no rewards were delivered
419 following the low tone. An inter-trial interval of 4–6 s was used. During the choice task,
420 animals were instructed to choose one of two peripheral pie charts, each of which
421 indicated either the probability or magnitude of an upcoming reward. The two target
422 options were presented for 2.5 s at 8° to the left or right of the central fixation location. The
423 animals received a fluid reward as indicated by the green pie chart of the chosen target,
424 with the probability indicated by the blue pie chart. Otherwise, no reward was delivered.

425 A total of 100 pie charts composed of 10 levels of probability and magnitude of
426 rewards were used in the experiments. In the single-cue task, 100 pie charts were
427 presented once in random order. In the choice task, two pie charts were randomly
428 assigned to the two options. During one electrophysiological recording session,
429 approximately 30–60 trial blocks of the choice task were interleaved with 100–120 trial
430 blocks of the single-cue task.

431

432 ***Electrophysiological recordings and data preprocessing***

433 *Exp. 1.* To record the single-unit activity, we used a 16-channel vector array microprobe
434 (V1 X 16-Edge, NeuroNexus), 16-channel U-Probe (Plexon), tungsten tetrode probe
435 (Thomas RECORDING), or single-wire tungsten microelectrode (Alpha Omega).

436 Electrophysiological signals were amplified, bandpass-filtered (200–6000 Hz), and
437 monitored. Single-neuron activity was isolated based on spike waveforms, either online or
438 offline. For both clustering and offline sorting, the activities of all single neurons were
439 sampled when the activity of an isolated neuron demonstrated a good signal-to-noise ratio
440 (>2.5). The signal-to-noise ratio was visually checked by calculating the range of
441 background noise against the spike amplitude, which was monitored online using the
442 OmniPlex Neural Data Acquisition System, or offline using the sorter software Plexon. The
443 recorded neurons were not blinded. The sample sizes required to detect the effect sizes
444 (numbers of recorded neurons, recorded trials in a single neuron, and monkeys) were
445 estimated based on previous studies (31, 54). Neural activity was recorded during 60–240
446 trials of the ILR task. We recorded 590 hippocampal neurons, among which the recording
447 sites appeared to cover all subdivisions (i.e., the dentate gyrus, CA3, CA1, and subiculum
448 complex).

449 *Exp. 2.* We used conventional techniques to record the single-neuron activity in the STRt,
450 including the caudate and putamen tails. A tungsten microelectrode (1–3 MΩ Frederic
451 hair; 0.5–1.5 MΩ Alpha Omega Engineering) was used to record single-neuron activity.
452 The recording site was determined using a grid system that allowed electrode penetration
453 at 1 mm intervals. We amplified and filtered (0.3 to 10 kHz; Model 1800, A-M Systems;
454 Model MDA-4I, BAK) signals obtained from the electrodes and collected at 1 kHz. Single
455 neurons were isolated online using custom voltage–time window discriminator software
456 (Blip; available at <http://www.robilis.com/blip/>). The presumed medium spiny neurons were
457 identified based on their low baseline activity (<3 spikes/s) and broad action potentials
458 (55). The recorded neurons were not blinded. The sample sizes required to detect the
459 effect sizes (numbers of recorded neurons, recorded trials in a single neuron, and
460 monkeys) were estimated based on previous studies (56, 57). Neural activity was recorded

461 during 10–30 trials of the *passive viewing task*. We recorded 115 medium spiny neurons
462 in the STRt. In Exp. 2, only a single-neuron recording was performed online. We note that
463 we termed the scene and object for two visual stimuli in our previous study (58), but here
464 we termed them scene and item.

465 *Exp. 3.* Conventional techniques were used to record single-neuron activity in the dorsal
466 part of the head of the caudate nucleus (CD). A tungsten microelectrode (1.1–1.5 MΩ,
467 Microprobes for Life Science; 1.0 MΩ, Alpha Omega Engineering Ltd.) was used to record
468 single-neuron activity. The electrophysiological signals were amplified and monitored
469 using a TDT recording system (RZ2, Tucker-Davis Technologies, TDT). Single-neuron
470 activity was manually isolated based on the online spike waveforms. The activity of all
471 single neurons was sampled from the activity of presumed projection neurons, which are
472 characterized as having a low spontaneous discharge rate (<2 spikes/s) outside the task
473 context and exhibiting phasic discharges in relation to one or more behavioral task events
474 (Yamada et al, 2016). Neural activity was recorded during 100–120 trials per block in the
475 delayed-reward task. We recorded the CD of the left or right hemisphere in each of the
476 three monkeys in the experiment, with 150 CD neurons (51, 31, and 68 from the BI, FG,
477 and ST, respectively).

478 *Exp. 4.* Conventional techniques were used to record single-neuron activity in the DS, VS,
479 cOFC (area 13M), and mOFC (area 14o). A tungsten microelectrode (1–3 MΩ, FHC) was
480 used to record single-neuron activity. Electrophysiological signals were amplified, band-
481 pass filtered (50–3,000 Hz), and monitored using a TDT recording system (RZ5D, Tucker-
482 Davis Technologies, TDT). Single-neuron activity was manually isolated based on the
483 online spike waveforms. The activity of all single neurons was sampled when the activity
484 of an isolated neuron demonstrated a good signal-to-noise ratio (>2.5). The signal-to-noise
485 ratio was calculated online as the ratio of the spike amplitude to the baseline voltage range

486 on the oscilloscope. The recorded neurons were not blinded. The sample sizes required
487 to detect the effect sizes (numbers of recorded neurons, recorded trials in a single neuron,
488 and monkeys) were estimated based on previous studies (59-61). Neural activity was
489 recorded during 100–120 trials of the single-cue task. Neural activity was not recorded
490 during selection trials. We recorded the neurons of a single right hemisphere in each of
491 the two monkeys: 194 DS neurons (98 and 96 from monkeys SUN and FU, respectively),
492 144 VS neurons (89 SUN and 55 FU), 190 cOFC neurons (98 SUN and 92 FU), and 158
493 mOFC neurons (64 SUN and 94 FU). In Exp. 1, only a single-neuron recording was
494 performed online.

495

496 ***Statistical analysis***

497 For statistical analysis, we used the statistical software package MATLAB (MathWorks,
498 Exps. 1 and 2), and R (Exps. 3 and 4) for conventional analyses such as linear regression
499 and ANOVA. To analyze the regression matrix using PCA, we used R software. All
500 statistical tests for the neural analyses were two-tailed.

501

502 ***Behavioral analysis***

503 No new behavioral results were included; however, the procedure for the behavioral
504 analysis was as follows:

505 *Exp. 1.* We previously reported that two monkeys learned to retain the item and location
506 information of a sample stimulus (62). Here, we describe the analysis steps used to check
507 whether the monkey used both item and location information to perform the task.

508 To examine this, we compared the animals' actual correct rates during the recording
509 to random correct rates (chi-square test). The ILR response phase had five options,
510 resulting in a 20% random correct rate. If the animal used an incorrect strategy, such as

511 only retaining the location information of the sample stimulus and ignoring the item
512 information, the correct rate for the match condition would be 100% and that for the
513 nonmatch condition would be 0. Based on the above considerations, we examined the
514 correct rates of the two animals in the match and nonmatch conditions, respectively. In
515 general, the average correct rates for both animals in the match and nonmatch conditions
516 were well above chance levels after training.

517 *Exp. 2.* We previously reported that two monkeys switched their behavior depending on
518 the value of the item based on the scene (58). Here, we describe how to check whether
519 the monkey learned both the scene and item information. We calculated the correct rate
520 for the scene-based object-value task. Because the two scenes appear in random
521 sequences, the monkey must switch object choice if the scene has changed. After
522 performing more than 160 trials, the correct rate reached a plateau above chance. The
523 monkey was able to switch object choices immediately after the scene changed. Once the
524 monkeys learned this extensively, their choice behavior became automatic, as the choice
525 tended to occur even when the reward was not delivered after saccades to high-valued
526 items according to the scene.

527 *Exp. 3.* We previously reported that the three monkeys behaved based on temporally
528 discounted values that integrated both delay and reward size information provided by
529 visual stimuli (63). Here, we describe an analysis to check how monkeys discount reward
530 values for delay and reward information. Error rates in task performance were calculated
531 by dividing the total number of errors by the total number of trials for each reward condition
532 and then averaged across all sessions. The average error rates were fitted to the inverse
533 function of reward size with hyperbolic temporal discounting: $E = 1+kD/ aR$ (E : average
534 error rates, D : delay, R : reward size, k : discounting factor, a : incentive impact), and
535 exponential temporal discounting: $E = e^{-kd}/aR$. We used the 'optim' function in R, evaluated

536 the goodness of fit of the two models by least-squares minimization, and compared the
537 models by leave-one-out cross-validation as described previously (Minamimoto et al.,
538 2009).

539 *Exp. 4.* We previously reported that monkey behavior depends on expected values,
540 defined as the probability time magnitude (23). We described the analysis steps to check
541 whether the monkey's behavior reflected task parameters, such as reward probability and
542 magnitude. Importantly, we showed that the monkey's choice behavior reflected the
543 expected values of the rewards, that is, the probability multiplied by the magnitude. For
544 this purpose, the percentage choosing the right-side option was analyzed in the pooled
545 data using a general linear model with a binomial distribution:

546 $P_{\text{chooses}_R} = 1/(1 + e^{-z})$ (3)

547 where the relationship between P_{chooses_R} and Z is given by the logistic function in each
548 of the following three models: number of pie segments (M1), probability and magnitude
549 (M2), and expected values (M3).

550 $M1: Z = b_0 + b_1 N_{\text{pie}_L} + b_2 N_{\text{pie}_R}$ (4)

551 where b_0 is the intercept, and N_{pie_L} and N_{pie_R} are the number of pie segments contained
552 in the left and right pie chart stimuli, respectively. The values of b_0 to b_2 are free parameters
553 and estimated by maximizing the log likelihood.

554 $M2: Z = b_0 + b_1 P_L + b_2 P_R + b_3 M_L + b_4 M_R$ (5)

555 where b_0 is the intercept; P_L and P_R are the probabilities of rewards for the left and right
556 pie chart stimuli, respectively; and M_L and M_R are the magnitudes of rewards for the left
557 and right pie chart stimuli, respectively. The values of b_0 to b_4 are free parameters and
558 estimated by maximizing the log likelihood.

559 $M3: Z = b_0 + b_1 EV_L + b_2 EV_R$ (6)

560 where b_0 is the intercept and EV_L and EV_R are the expected values of rewards as
561 probability multiplied by magnitude for the left and right pie chart stimuli, respectively. The
562 values of b_0 to b_2 are free parameters and estimated by maximizing the log likelihood. We
563 identified the best model to describe monkey behavior by comparing goodness-of-fit
564 based on Akaike's information criterion and Bayesian information criterion (64).

565

566 ***Neural analysis***

567 Peri-stimulus time histograms were constructed for each single-neuron activity aligned at
568 the onset of the visual stimulus. Average activity curves were smoothed for visual
569 inspection using a Gaussian kernel ($\sigma = 20, 15, 10$, and 50 ms in Exps. 1–4, respectively),
570 whereas the Gaussian kernel was not used for statistical tests.

571 To ensure that the four different datasets were as fair as possible, we used the same
572 criteria to analyze the neural activity. For the neural analyses, we used the following four
573 criteria: 1) the same analysis window size, 2) visual response within a short time (0.6 s),
574 3) neural modulations detected at the same significance level ($P < 0.05$), and 4) a general
575 linear model (ANOVA in Exps. 1 and 2 and the linear regression in Exp. 3 and 4). The
576 details of these analytical procedures for the rate coding and dynamic models are shown
577 below.

578

579 ***Rate-coding model: Conventional analyses to detect neural modulations in each***
580 ***neuron***

581 *Exp. 1.* For neural responses during the encoding phase after the sample presentation,
582 we evaluated the effects of “item” and “location” for each neuron using two-way ANOVA
583 ($P < 0.05$ for each). We analyzed neurons that were tested in at least 60 trials (10 trials

584 for each stimulus and 15 trials for each location). On average, we tested 100 trials for each
585 neuron. These results have been previously reported (62).

586 *Exp. 2.* For neural responses during the appearance of the visual item, we evaluated the
587 effects of “item” and “scene” for each neuron using paired t-test ($P < 0.05$ with Bonferroni
588 correction). These results have been previously reported (58).

589 *Exp. 3.* The neural discharge rates (F) were fitted using a linear combination of the
590 following variables:

591
$$F = b_0 + b_d \text{Delay} + b_m \text{Magnitude} \quad (7)$$

592 where Delay and Magnitude are the delay and magnitude of the reward, respectively, as
593 indicated by the visual stimulus. b_0 is the intercept. If b_d and b_m were not zero at $P < 0.05$,
594 the discharge rates were regarded as being significantly modulated by that variable. These
595 results have been previously reported (63).

596 *Exp. 4.* The neural discharge rates (F) were fitted using a linear combination of the
597 following variables:

598
$$F = b_0 + b_p \text{Probability} + b_m \text{Magnitude} \quad (8)$$

599 where Probability and Magnitude are the probability and magnitude of the rewards,
600 respectively, as indicated by the pie chart. b_0 is the intercept. If b_p and b_m were not zero at
601 $P < 0.05$, the discharge rates were regarded as being significantly modulated by that
602 variable. These results have been previously reported (23).

603

604 ***Population dynamics using principal component analysis***

605 We analyzed neural activity during an identical 0.6 s duration from the sample onset (Exp.
606 1), item onset (Exp. 2), CUE onset (Exp. 3), and cue onset (Exp. 4). To obtain a time series
607 of neural firing rates within this time period, we estimated the firing rates of each neuron

608 for every 0.05 s time bin (without overlap) during the analysis periods. A Gaussian kernel
609 was not used.

610

611 *Regression subspace.* We used a general linear model to determine how items and
612 locations (Exp. 1), items and scenes (Exp. 2), delay and magnitude of rewards (Exp. 3),
613 and the probability and magnitude of the rewards (Exp. 4) affect the activity of each neuron
614 in the neural populations. Each neural population was composed of all the recorded
615 neurons in each brain region.

616 *Exp. 1.* First, we set six visual items and four locations as categorical variables. We then
617 described the average firing rate of neuron i at time t as a linear combination of the item
618 and the location in each neural population:

619
$$F_{(i,t,k)} = b_{0(i,t)} + b_{1(i,t)}\text{Item}_{(k)} + b_{2(i,t)}\text{Location}_{(k)} \quad (9)$$

620 where $F_{(i,t,k)}$ is the average firing rate of neuron i at time t in trial k , $\text{Item}_{(k)}$ is the types of
621 items cued to the monkey in trial k , and $\text{Location}_{(k)}$ is the types of locations cued to the
622 monkey in trial k . The regression coefficients $b_{0(i,t)}$, $b_{1(i,t)}$, and $b_{2(i,t)}$ describe the degree to
623 which the firing rates of neuron i depend on the mean firing rates (hence, firing rates
624 independent of task variables, item, and location), the degree of firing rate in each item
625 relative to the mean firing rates, and the degree of firing in each location relative to the
626 mean firing rates, respectively, at a given time t during the trials. The interaction term is
627 not included in the model.

628 In the analysis, we performed preference ordering for item and location in each neuron.
629 $\text{Item}_{(k)}$ and $\text{Location}_{(k)}$ were rank-ordered items and locations, respectively, cued to the
630 monkey in trial k . Items 1–6 and locations 1–4 were rank-ordered from the most preferred
631 to least preferred, respectively, defined as the mean firing rate during the entire analysis

632 time window from 0.08 to 0.6 s. This preference ordering did not change over time t for
633 each neuron n .

634 *Exp. 2.* We first set eight items and two scenes as the categorical variables. We then
635 described the average firing rate of neuron i at time t as a linear combination of the item
636 and scene in each neural population:

637
$$F_{(i,t,k)} = b_{0(i,t)} + b_{1(i,t)}\text{Item}_{(k)} + b_{2(i,t)}\text{Scene}_{(k)} \quad (10)$$

638 where $F_{(i,t,k)}$ is the average firing rate of neuron i at time t in trial k , $\text{Item}_{(k)}$ is the types of
639 items cued to the monkey in trial k , and $\text{Scene}_{(k)}$ is the types of scene stimuli cued to the
640 monkey in trial k . The regression coefficients $b_{0(i,t)}$, $b_{1(i,t)}$ and $b_{2(i,t)}$ describe the degree to
641 which the firing rates of neuron i depend on the mean firing rates (hence, firing rates
642 independent of task variables, item and scene), the degree of firing rate in each item
643 relative to the mean firing rates, and the degree of firing in each scene relative to the mean
644 firing rates, respectively, at a given time t during the trials. The interaction term was not
645 included in the model.

646 In the analysis, $\text{Item}_{(k)}$ and $\text{Scene}_{(k)}$ were the rank-ordered item and scene,
647 respectively, cued to the monkey in trial k . Items 1 to 8 and Scenes 1 and 2 were rank-
648 ordered from the most preferred to least preferred, respectively, defined as the mean firing
649 rate during the whole analysis 0.6 s window after the item onset. This preference ordering
650 did not change over time t for each neuron n .

651 *Exp. 3.* We first set the delay and magnitude as 0, 3.3, and 6.9 s and one and three drops
652 of rewards, respectively, during the behavioral task. In the analysis, we normalized these
653 values from 0 to 1 divided by the maximum values in each: 0, 0.48, and 1 for delay, and
654 0.33, 0.66, and 1 for magnitude. This is because these values affect the extent of the
655 regression subspace between two continuous variables. We then described the average

656 firing rate of neuron i at time t as a linear combination of the delay and magnitude in each
657 neural population:

$$658 F_{(i,t,k)} = b_{0(i,t)} + b_{1(i,t)}\text{Delay}_{(k)} + b_{2(i,t)}\text{Magnitude}_{(k)} \quad (11)$$

659 where $F_{(i,t,k)}$ is the average firing rate of neuron i at time t in trial k , $\text{Delay}_{(k)}$ is the normalized
660 delay to obtain a reward cued to the monkey in trial k , and $\text{Magnitude}_{(k)}$ is the normalized
661 number of reward drops cued to the monkey in trial k . The regression coefficients $b_{0(i,t)}$ to
662 $b_{2(i,t)}$ describe the degree to which the firing rates of neuron i depend on the mean firing
663 rates (hence, firing rates independent of task variables), delay in rewards, and magnitude
664 of rewards, respectively, at a given time t during the trials.

665 *Exp. 4.* We first set the probability and magnitude as 0.1 to 1.0 and 0.1 to 1.0 mL,
666 respectively. We did not normalize these values because they were originally prepared
667 from 0 to 1 originally. We then describe the average firing rate of neuron i at time t as a
668 linear combination of probability and magnitude in each neural population:

$$669 F_{(i,t,k)} = b_{0(i,t)} + b_{1(i,t)}\text{Probability}_{(k)} + b_{2(i,t)}\text{Magnitude}_{(k)} \quad (12)$$

670 where $F_{(i,t,k)}$ is the average firing rate of neuron i at time t in trial k , $\text{Probability}_{(k)}$ is the
671 probability of the reward cued to the monkey in trial k , and $\text{Magnitude}_{(k)}$ is the magnitude
672 of the reward cued to the monkey in trial k . The regression coefficients $b_{0(i,t)}$ to $b_{2(i,t)}$ describe
673 the degree to which the firing rates of neuron i depend on the mean firing rates (i.e., firing
674 rates independent of task variables), probability of rewards, and magnitude of rewards,
675 respectively, at a given time t during the trials.

676 We used the regression coefficients (i.e., the regression table in the case of ANOVA)
677 described in Eq. 9–12 to identify how the dimensions of the neural population signals were
678 composed of information related to the item and location (Exp. 1), item and scene (Exp.
679 2), delay and magnitude (Exp. 3), and probability and magnitude (Exp. 4) as aggregated
680 properties of individual neural activity. In this step, an encoding model is constructed in

681 which the regression coefficients are explained by a temporal structure in the neural
682 modulation of two categorical variables (Exps. 1 and 2), or two continuous variables (Exps.
683 3 and 4) at the population level. Our procedures involve targeted dimensionality reduction
684 using the regression subspace and are aimed at describing neural modulation dynamics
685 (29).

686

687 *Principal component analysis.* We used PCA to identify the dimensions of the neural
688 population signal in orthogonal spaces composed of two variables in each neural
689 population of the four experiments. For each neural population, we first prepared a two-
690 dimensional data matrix X of size $N_{(n)} \times M_{(C \times T)}$. The regression coefficient vectors $b_{1(i,t)}$ and
691 $b_{2(i,t)}$ in Eq. 9–12, whose rows correspond to the total number of neurons (n) in each neural
692 population and columns correspond to C , the total number of conditions (that is, 10: six
693 items and four locations in Exp. 1, 10: eight items and two scenes in Exp. 2, 2: delay and
694 magnitude in Exp. 3, and 2: probability and magnitude in Exp. 4), and T is the total number
695 of analysis windows (i.e., 0.6 s divided by the window size bin, 0.05 s, 12 bin). A series of
696 eigenvectors was obtained by applying PCA once to the data matrix X in each neural
697 population. The PCs of this data matrix are vectors $v_{(a)}$ of length $N_{(n)}$ and the total number
698 of recorded neurons if $M_{(C \times T)} > N_{(n)}$; otherwise, the length is $M_{(C \times T)}$. PCs were indexed from
699 the principal components and explained the most to least variance. The eigenvectors were
700 obtained using the `prcomp()` function in R software. We did not include the intercept term
701 $b_{0(i,t)}$ to focus on the neural modulation by the variables of interest.

702

703 *Eigenvectors.* When we applied PCA to data matrix X , we decomposed the matrix into
704 eigenvectors and eigenvalues. Each eigenvector had a corresponding eigenvalue. In our
705 analysis, the eigenvectors at time t represented a vector, for example, in the space of

706 delay and magnitude in Exp. 3. The eigenvalues at time t for the delay and magnitude
707 were scalars, indicating the extent of variance in the data in that vector. Thus, the first PC
708 was the eigenvector with the highest eigenvalue. We analyzed the eigenvectors for the
709 top two PCs (PC1 and PC2) in the following analyses to describe the geometry in the most
710 predominant dimension. PCA was applied once to each neural population; thus, the total
711 variance contained in the data differed among the neural populations.

712

713 *Shuffle control for PCA.* To examine the significance of the population structures described
714 by PCA, we performed three shuffle controls. The two-dimensional data matrix X was
715 randomized by shuffling in three ways. In shuffled control 1, matrix X was shuffled by
716 permutating the allocation of neuron n at time i . This shuffle provided a data matrix X of
717 size $N_{(n)} \times M_{(C \times T)}$, eliminating the temporal structure of neural modulation by condition C in
718 each neuron but retaining the neural modulations at time t at the population level. In
719 shuffled control 2, matrix X was shuffled by permutating the allocation of time i in each
720 neuron n . This shuffle provided a data matrix X of size $N_{(neuron)} \times M_{(C \times T)}$, eliminating the
721 neural modulation structure under condition C maintained in each neuron but retaining the
722 neural modulation in each neuron at the population level. In shuffled control 3, matrix X
723 was shuffled by permutating the allocation of both time i and neuron n . In these three
724 shuffle controls, matrix X was estimated to be 1,000 times. PCA performance was
725 evaluated by constructing the distributions of the explained variances for PC1 to PC12.
726 The statistical significance of the variances explained by PC1 and PC2 was estimated
727 based on the 95th percentile of the reconstructed distributions of the explained variance
728 or bootstrap standard errors (i.e., standard deviation of the reconstructed distribution). We
729 note that because the significant dimensions of neural populations dynamics differed the

730 10 neural populations, we analyzed the neural dynamics at the top two dimension, PC1
731 and 2.

732

733 *Analysis of eigenvectors.* We evaluated the characteristics of the eigenvectors for PC1
734 and PC2 in each neural population in terms of vector angle, size, and deviation. The
735 eigenvectors were evaluated for each of the task parameters described above: item and
736 location in Exp. 1, item and scene in Exp. 2, delay and magnitude in Exp. 3, and probability
737 and magnitude in Exp. 4. The angle is the vector angle from the horizontal axis from 0° to
738 360° against the main PCs. The size is the length of the eigenvector. The deviation is the
739 difference between the vectors. The deviation from the mean vector for each neural
740 population was estimated. These three eigenvector characteristics were compared among
741 the populations at $P < 0.05$, using the Kruskal–Wallis test and Wilcoxon rank-sum test with
742 Bonferroni correction for multiple comparisons. The vector during the first 0.1 s was
743 extracted from these basic analyses.

744 To evaluate the neural population geometry using their selected feature, we estimated
745 the accumulated angle difference weighted by the deviance:

746
$$\sum_{t=S}^{t=E} d \theta \quad (13)$$

747 where the d is deviation between the vectors at times t and $t+1$, θ is the angle difference
748 between vectors at times t and $t+1$, S is zero, and E is the time period to stop the estimation,
749 i.e., 0.6 s. This index is analogous to the rotational force accumulated over time. If the
750 value of the accumulated angle difference was close to zero, the population geometry was
751 stable, such as a straight or non-dynamic structure, that is, it remained at some point in
752 the PC1-2 plane.

753 To quantitatively evaluate the trajectory geometry, we used the Lissajous curve
754 function, which describes any geometric pattern in a plane using $F(x,y)$:

755
$$x = Ax \cos (\omega x t(i) + \Phi x) + bx \quad (14)$$

756
$$y = Ay \cos (\omega y t(i) + \Phi y) + by \quad (15)$$

757 where ω and Φ represent cycle of the rotation and their deviance as a function of time, $t(i)$.
758 Ax and Ay represent the amplitudes of the trajectory, whereas bx and by represent the
759 location of the trajectory. For ω , 3.33π indicates that one cycle since the analysis window
760 is 0.6 s. Φ is 0 to 2π for one cycle. We estimated ωx , Φx , bx , ωy , and Φy , by parameters
761 by estimating maximum loglikelihood of the model. Nonlinear least squares in the `nls()`
762 function in the R program was used. A time series of eigenvectors for PC1 and PC2 in a
763 0.05 s analysis windows (12 data points) were used with a sliding average between three
764 time points (hence, 0.15 s time resolution).

765

766 *Bootstrap resampling and clustering using feature-based parameters.* We estimated $\Sigma d \theta$,
767 mean d , rotational speed $\Sigma \theta/0.1s$, and d_{s-e} , such as start to end distance using a
768 parametric bootstrap resampling method (65). In each neural population, the neurons
769 were randomly resampled in duplicate, and a data matrix X of size $N_{(neuron)} \times M_{(C \times T)}$ was
770 obtained. PCA was applied to the data matrix X . The time series of eigenvectors was
771 obtained, and these four features were estimated from the neural trajectory. This
772 resampling was conducted 1,000 times in each neural population, and the distributions of
773 these four parameters were obtained.

774 Following bootstrap resampling, we applied clustering of these parameters based on
775 PCA and a dendrogram across the replicates in the 10 brain regions, such as 20,000
776 replicates (10 brain regions times two conditions times 1,000 replicates). Based on this
777 clustering, proportion of the identified clusters in each brain region was estimated.

778

779 *Bootstrap resampling and clustering based on Lissajous curve parameters.* The Lissajous
780 curve parameters for the replicated trajectory were estimated using a bootstrap
781 resampling method (65). In each neural population, the neurons were randomly resampled
782 in duplicate, and a data matrix X of size $N_{(neuron)} \times M_{(C \times T)}$ was obtained. PCA was applied to
783 the data matrix X . The time series of eigenvectors was obtained for PC1 and PC2, which
784 describe the trajectory, and the fitted parameters using the Lissajous curve function were
785 estimated using the `nls()` function in R program. This resampling was conducted 1,000
786 times in each neural population, and the distributions of the Lissajous parameters were
787 obtained.

788 Following bootstrap resampling, we applied clustering of these parameters based on
789 PCA and a dendrogram across the replicates in the 10 brain regions, such as 20,000
790 replicates (10 brain regions times two conditions times 1,000 replicates). In this process,
791 the omega ratio (ω_x/ω_y) and phi difference ($\Phi_x - \Phi_y$) were also used, in addition to the ω_x ,
792 ω_y , Φ_x , and Φ_y . Based on this clustering, proportion of the identified clusters in each brain
793 region was estimated. We used the median of the estimated parameter in a cluster to
794 describe the trajectory geometries.

795

796

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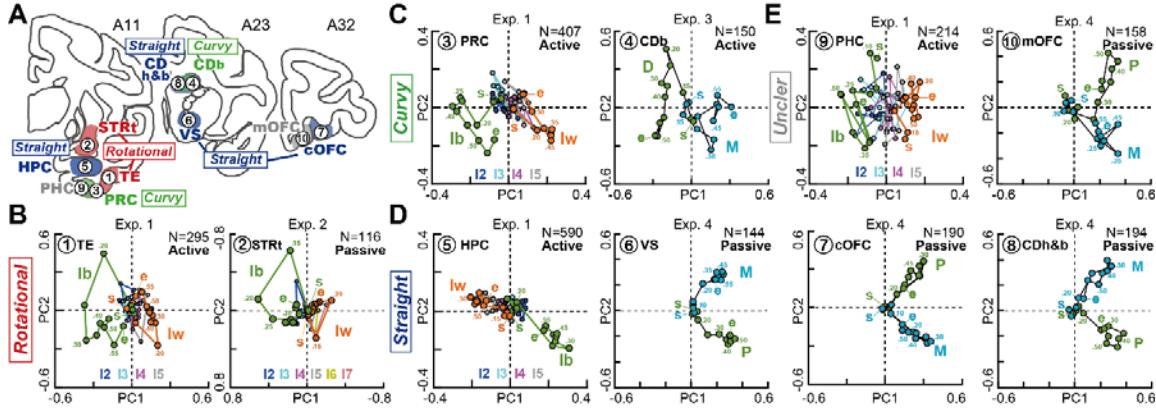
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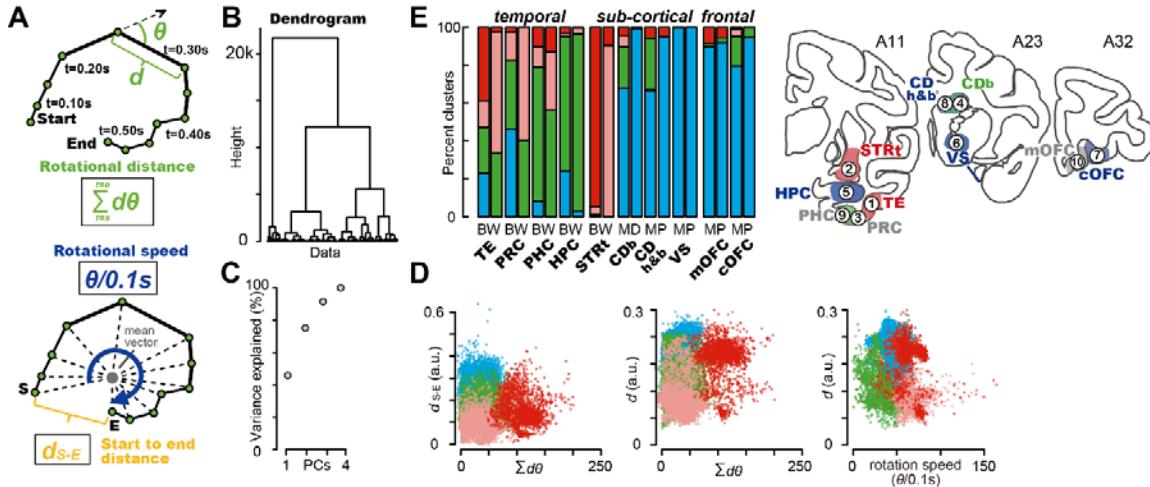


967

968 **Fig. 1.** Neural population geometries in the visual memory pathway

969 **A**, Anatomical depiction of neural populations obtained from the 10 brain regions in eight
970 macaques during the four different behavioral tasks in Exps. 1 to 4. **B-E**, Rotational (**B**),
971 curvy (**C**), straight (**D**), and unclear dynamics (**E**) detected by visual inspection. In **A-E**, the
972 10 brain regions are numbered as follows: 1. TE, 2. STRt, 3. PRC, 4. CDb, 5. HPC, 6. VS,
973 7. cOFC, 8. CDh&b, 9. PHC, and 10. mOFC. The 0.05 s time bin was used for the
974 dynamics analysis.

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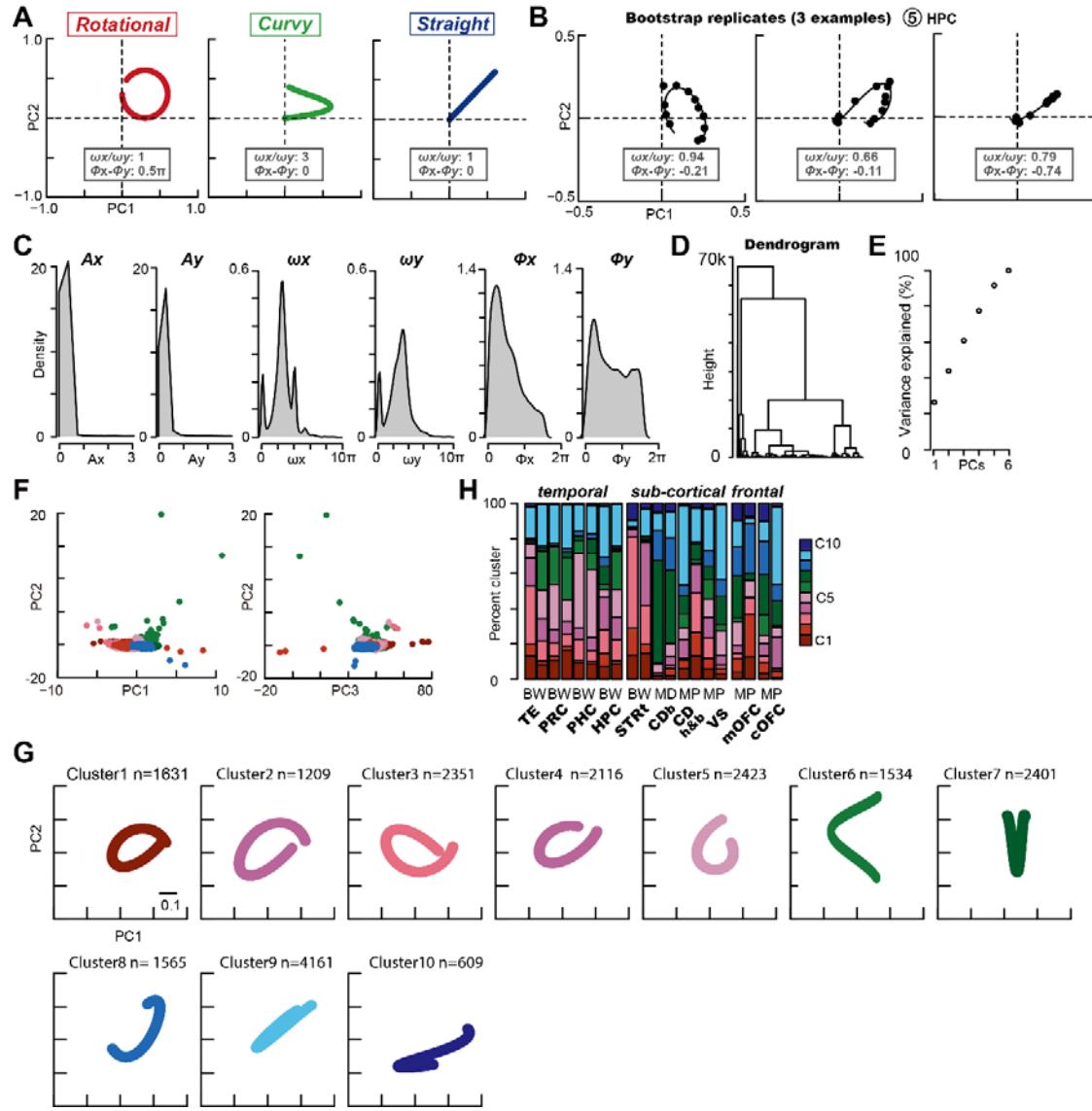


976

977 **Fig. 2.** Quantitative evaluation of geometric structures according to the rotational features.

978 **A**, Schematic depictions of the estimation of accumulated angle difference weighted by
979 the deviance, $\Sigma d\theta$. The accumulated angle difference indicates the degree of geometric
980 change in terms of the rotational force across time. Vector distance (d), rotational speed
981 ($\theta/0.1s$), and start to endpoint distance (d_{S-E}) were also estimated. **B**, Dendrogram
982 estimated from these four parameter values based on bootstrap resampling across 10
983 neural populations. **C**, Percentage of variance explained by PCA of bootstrap resampling
984 data across 10 neural populations. **D**, Clusters detected among the four parameters based
985 on the PCA. **E**, Percentage of the identified clusters in each of the 10 brain regions. Each
986 neural population contained two components of neural information: the best and worst
987 conditions (BW) in Exps. 1 and 3, magnitude and delay of the rewards (MD) in Exp. 2, and
988 magnitude and probability of rewards (MP) in Exp. 4.

989



990

991 **Fig. 3.** Quantitative evaluation of geometric structures using the Lissajous curve function.

992 **A**, Schematic depictions of trajectory geometries using Lissajous function parameters. For

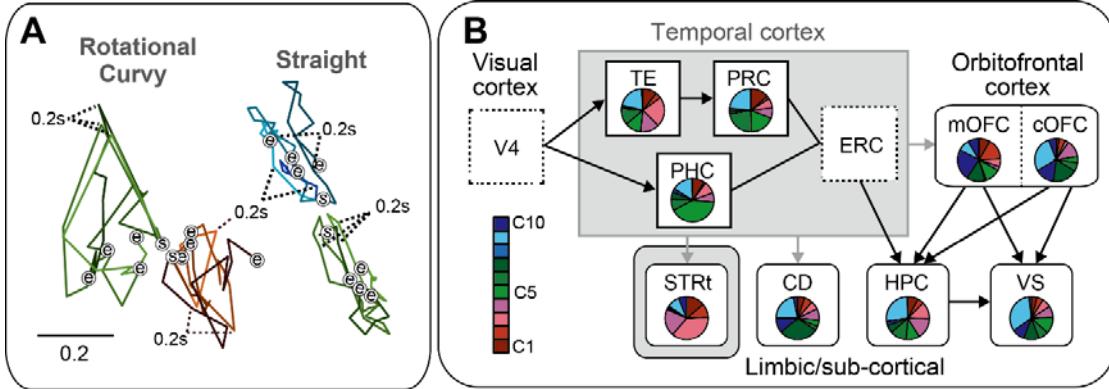
993 all figures, ω_x and ω_y are 3π . **B**, Three examples of bootstrap replicates for the HPC

994 population fitted by the Lissajous function. L indicates the maximum loglikelihood.

995 Estimated parameters were as follows: left, ω_x , 2.78π , Φ_x , -0.11 , L , 34.6 , ω_y , 2.96π , Φ_y ,

996 0.10 , L , 31.6 ; middle, ω_x , 2.51π , Φ_x , -0.03 , L , 24.2 , ω_y , 3.82π , Φ_y , -0.08 , L , 32.7 ; right,

997 ω_x , 2.21 π , ϕ_x , -0.16, L , 26.9, ω_y , 2.78 π , ϕ_y , 0.58, L , 29.1. **C**, Probability density
998 estimated for Lissajous parameters obtained from bootstrap replicates across 10 neural
999 populations times two conditions. **D**, Dendrogram estimated from Lissajous parameter
1000 values based on bootstrap resampling across 10 neural populations times two conditions.
1001 **E**, Percentage of variance explained by PCA of bootstrap resampling data across 10
1002 neural populations times two conditions. **F**, Clusters determined using PCA. Data are
1003 shown for PC1 to 3. **G**, Reconstructed trajectory in each cluster based on bootstrap
1004 resampling. The trajectories in clusters 1–10 were drawn using the median values of the
1005 Lissajous parameters in each cluster. **H**, Percentage of clusters in each of the 10 brain
1006 regions times two conditions. BW: best and worst conditions. MD: magnitude and delay
1007 conditions. MP: magnitude and probability conditions.

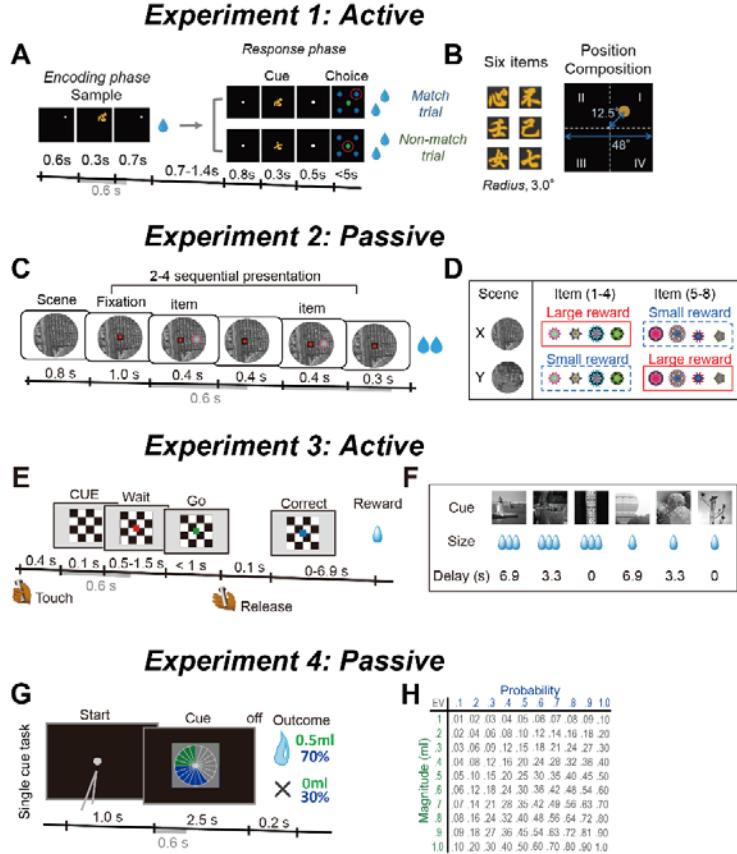


1008

1009 **Fig. 4.** Summary of the observed dynamics and anatomical connections in the visual
1010 memory pathway.

1011 **A**, Geometries depicted in the same arbitrary scales on the PC1-2 plane for the eight
1012 neural populations shown in Fig. 1B-D. The start of the trajectory (S) is aligned to describe
1013 each trajectory. e indicates the end of the trajectory at 0.6 s. **B**, Proportion of the clusters
1014 defined in each of the 10 brain regions are described with the anatomical connection.
1015 Reddish: rotational, greenish: curvy, bluish: straight dynamics. Data from CDh&b and CD_b
1016 are merged (CD).

1017

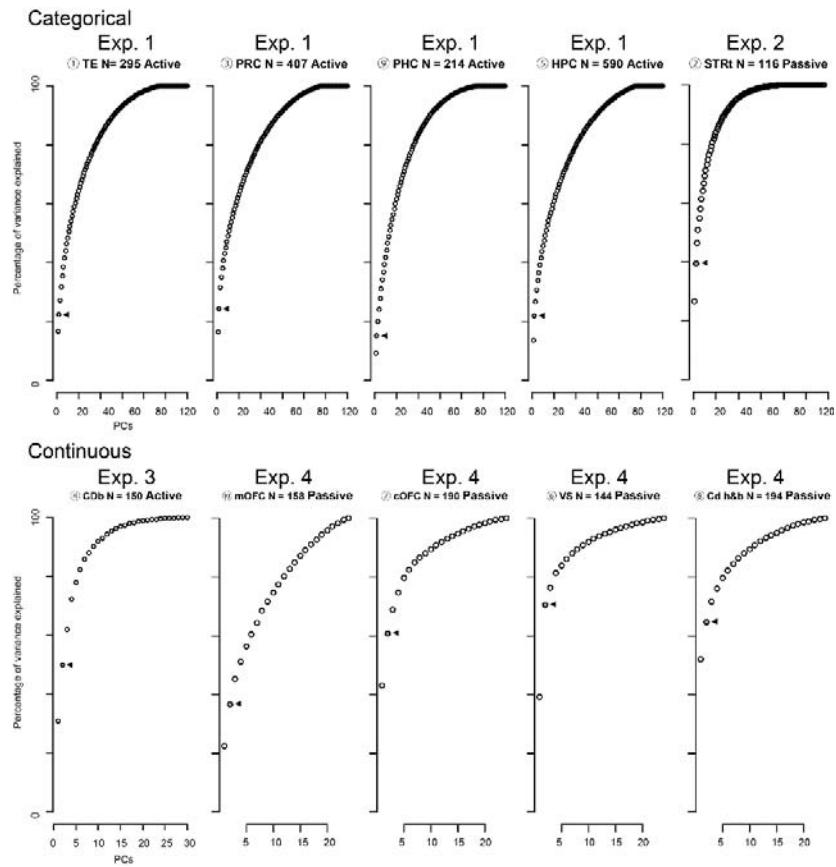


1018

1019 **Fig. S1. Behavioral tasks**

1020 **A**, Sequence of events during the ILR task in Exp. 1. The cue stimulus during the response
 1021 phase was the same as the sample stimulus during the encoding phase of the match trial,
 1022 whereas the two stimuli differed in the nonmatch trial. Neural activity was analyzed during
 1023 0.6 s after sample onset (gray bar). During the task, the monkeys actively responded or
 1024 did not respond by making a choice and performing the following action. **B**, Six visual
 1025 stimuli and spatial composition of the sample stimulus. **C**, Sequence of events during the
 1026 passive viewing task in Exp. 2. During fixation, the visual items were presented
 1027 sequentially within two to four times. These visual items were associated with reward or
 1028 no-reward outcomes in other behavioral contexts during the learning trials. During the task,
 1029 the monkeys were not required to respond, except for fixation to the center (passive).

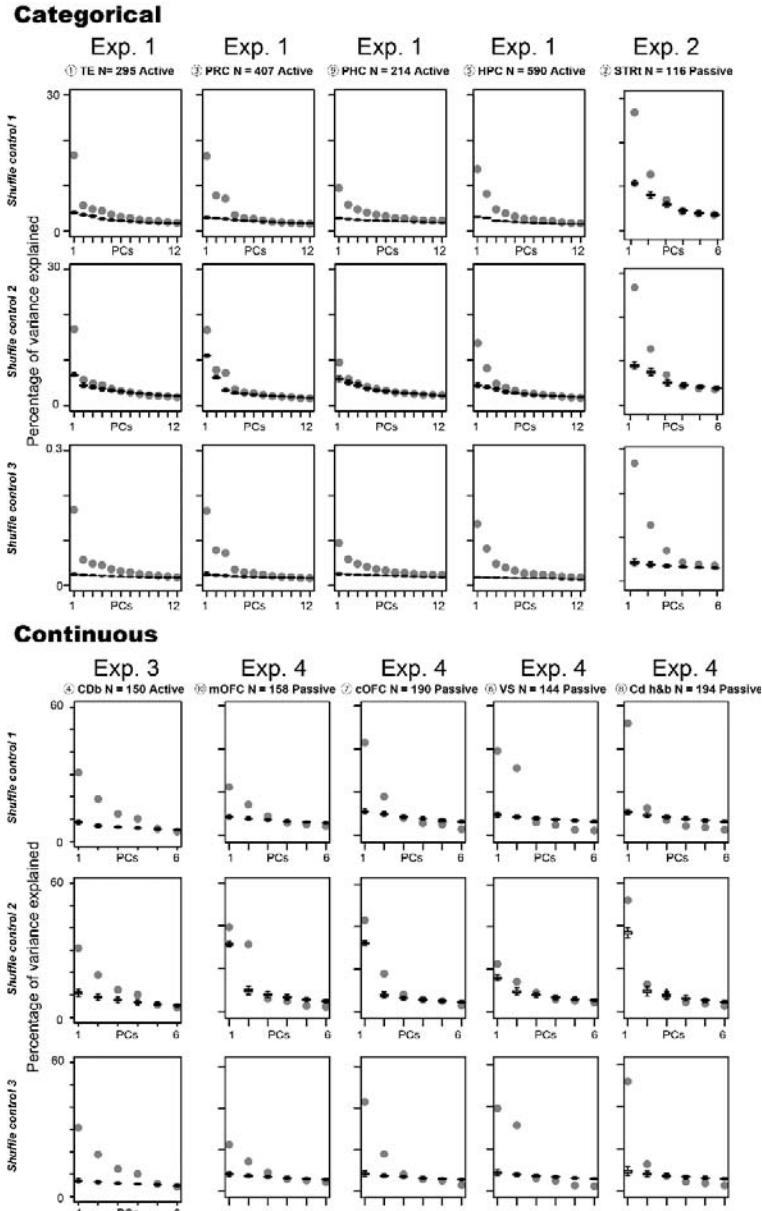
1030 Neural activity was analyzed during 0.6 s after object onset (gray bars). **D**, Eight visual
1031 items were divided into two groups (items 1–4 and 5–8). In each scene (e.g., scene X),
1032 one group was associated with a large reward and the other with a small reward. This
1033 reward association was reversed in the other scene (e.g., scene Y). In each trial, two items
1034 appeared as shown in **C**, one in items 1–4 and the other in items 5–8 as a random
1035 combination. **E**, Sequence of events during the delayed reward task in Exp. 3. During the
1036 task, the monkeys actively responded to the GO signal by releasing the lever (active).
1037 Neural activity was analyzed during 0.6 s after cue onset (gray bar). **F**, During the task,
1038 six visual items indicated the forthcoming reward size and delay duration to the reward
1039 after the bar release. **G**, Sequence of events during the single-cue task in Exp. 4. A single
1040 visual pie chart with green and blue segments was presented to the monkeys. During the
1041 task, the monkeys were not required to respond, except for fixation to the center during
1042 the start (passive). Neural activity was analyzed during 0.6 s after cue onset. **H**, Payoff
1043 matrix: Each of the magnitudes was fully crossed with each of the probabilities, resulting
1044 in a pool of 100 lotteries.



1045

1046 **Fig. S2. Variances explained by PCA in each neural population.**

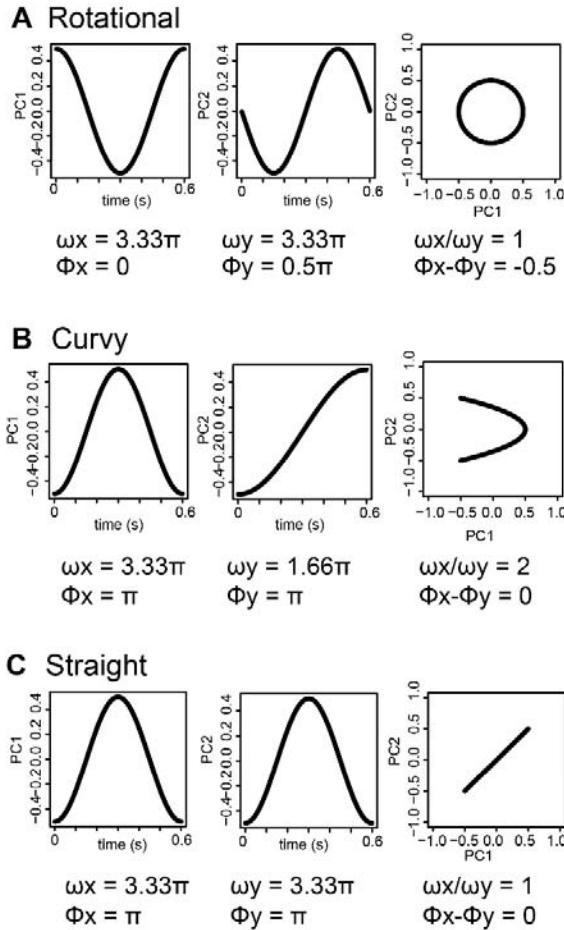
1047 Cumulative variance explained by PCA in each neural population in Exp. 1 to 4. The 0.05
1048 s time bin was used for the analysis. In Exp. 1 and Exp. 2, categorical task parameters
1049 were used. In Exp. 3 and Exp. 4, continuous task parameters were used. Triangle
1050 indicates the variance explained by the first two PCs.



1051

1052 **Fig. S3. Variances explained by PCA under shuffle control.**

1053 Boxplot of variances explained by PCA under the three shuffled conditions (see Methods
1054 section for details). The plot was not cumulative. A boxplot was made with 1,000 repeats
1055 of the shuffle for each condition. Gray plots indicate the percentage of variance explained
1056 by PCA. Results using 0.05 s bin data are shown.



1057

1058 **Fig. S4. Examples of Lissajous curve represented with the parameter combination.**

1059 Rotational, curvy, and straight dynamics are shown against ω ratio and Φ difference. In
1060 this study one cycle is defined with 3.33π for ω during 0.6 s analysis period ($3.33\pi \times 0.6$
1061 = 2π in the Lissajous function, $A \cos(\omega t(i) + \Phi) + b$). Φ from 0 to 2π defines the phase.
1062 A and b denote the size and location of the curve, respectively. Combination of ω ratio and
1063 Φ difference between x and y determines the shape of trajectory. For example, straight
1064 geometry is defined as the same ω and the same Φ . Rotational dynamics is defined as
1065 the same ω and not identical Φ . Curvy dynamics is defined as the different ω and the
1066 same Φ .

1067

1068 **Supplementary Table S1. Summary of the data set and standard analysis methods.**

NO	Brain region	Number of recorded neurons	Experimental number	Original report	Recording methods	Number of monkeys used	Behavioral task and standard analysis
1	TE	295	Exp. 1.	Chen and Naya, 2020	Single neuron recording /Multi neuron recording	2	<ul style="list-style-type: none">• Item-location-retention task• Active behavior: match-nonmatch choice• ANOVA (6 visual stimuli, 4 locations)
2	Perirhinal cortex (PRC)	407					
3	Parahippocampal cortex (PHC)	214					
4	Hippocampus (HPC)	590					
5	Striatum tail STRt	116	Exp. 2.	Kunimatsu et al., 2021	Single neuron recording	2	<ul style="list-style-type: none">• Scene-based object-value task• Passive behavior: no required response• ANOVA (8 visual stimuli, 2 rewards)
6	Caudate body (CDb)	150	Exp. 3.	Hori et al., 2021	Single neuron recording	3	<ul style="list-style-type: none">• Delayed reward tasks• Active behavior: lever release response• Linear regression (delay, magnitude)
7	Medial orbitofrontal cortex (mOFC)	158	Exp. 4.	Yamada et al., 2021	Single neuron recording	2	<ul style="list-style-type: none">• Cued lottery tasks• Passive behavior: no required response• Linear regression (probability, magnitude)
8	Central orbitofrontal cortex (cOFC)	190					
9	Ventral striatum (VS)	144					
10	Caudate head and body (CDh&b)	194					

1069

1070 For the standard analysis, we analyzed visual response within a short time (0.6 s). Neural
1071 modulations were detected at the same significance level ($P < 0.05$) using a general linear
1072 model (ANOVA in Exps. 1 and 2 and the linear regression in Exp. 3 and 4). See each
1073 reference for the results based on the standard analysis using general linear model.