

1 **Distinct computational mechanisms of uncertainty processing explain**  
2 **opposing exploratory behaviors in anxiety and apathy**

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24 Main Text

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27 **Abstract**

28 Decision-making in uncertain environments often leads to varied outcomes. Understanding how  
29 individuals interpret the causes of unexpected feedback is crucial for adaptive behavior and  
30 mental well-being. Uncertainty can be broadly categorized into two components: volatility and  
31 stochasticity. Volatility is about how quickly conditions change, impacting results. Stochasticity,  
32 on the other hand, refers to outcomes affected by random chance or “luck”. Understanding these  
33 factors enables individuals to have more effective environmental analysis and strategy  
34 implementation (explore or exploit) for future decisions. This study investigates how anxiety and  
35 apathy, two prevalent affective states, influence the perceptions of uncertainty and exploratory  
36 behavior. Participants (N = 1001) completed a restless three-armed bandit task that was analyzed  
37 using latent state models. Anxious individuals perceived uncertainty as more volatile, leading to  
38 *increased* exploration and learning rates, especially after reward omission. Conversely, apathetic  
39 individuals viewed uncertainty as more stochastic, resulting in *decreased* exploration and  
40 learning rates. The perceived volatility-to-stochasticity ratio mediated the anxiety-exploration  
41 relationship post-adverse outcomes. Dimensionality reduction showed exploration and  
42 uncertainty estimation to be distinct but related latent factors shaping a manifold of adaptive  
43 behavior that is modulated by anxiety and apathy. These findings reveal distinct computational  
44 mechanisms for how anxiety and apathy influence decision-making, providing a framework for  
45 understanding cognitive and affective processes in neuropsychiatric disorders.

46

47 **Introduction**

48

49 Life is filled with unexpected challenges. How individuals interpret the causes of undesirable  
50 outcomes, such as investment failures, career plateaus, or bad weather, in uncertain environments  
51 shapes their subsequent actions (1). When people attribute changes in outcomes to environmental  
52 volatility (the speed at which the environment is changing), they may be motivated to explore  
53 more, seeking additional information and altering their behavior. In contrast, attributing adverse  
54 outcomes to mere chance or “bad luck” (stochasticity) may decrease the motivation to explore,  
55 leading some individuals to persist with their existing strategies (2).

56

57 The response to environmental uncertainty likely interacts with individuals’ affective states in a  
58 bidirectional manner. Attributing adverse outcomes to stochasticity may lead individuals to stick  
59 to previous behaviors, potentially protecting them from hurtful feedback through additional  
60 interaction with the world. However, this approach may also dampen an individual’s ability to  
61 adapt to a changing environment, potentially reinforcing a negative cycle and leading to apathy  
62 and depression. Conversely, perceiving sources of negative outcome as volatile may motivate  
63 individuals to learn more about the world and reduce uncertainty, though this may also increase  
64 the chances of experiencing more adverse outcomes and potentially worsening negative feelings  
65 such as anxiety.

66

67 Reciprocally, how individuals perceive and respond to environmental uncertainty can be  
68 influenced by underlying affective states (3). Apathy, characterized by a lack of motivation and  
69 goal-directed behavior (4, 5), is an affective state associated with imprecise beliefs about action

70 outcomes (6) and a tendency to persist with previous choices rather than explore (7). This  
71 suggests that apathetic individuals may view outcomes as primarily stochastic, attributing events  
72 more to chance than controllable variables. This bias could discourage exploration and  
73 potentially reinforce a cycle of failure and helplessness (8).

74

75 In contrast, anxiety, marked by excessive worry and a heightened perception of potential threats  
76 (9, 10) and uncertainty (11), may lead individuals to overestimate environmental volatility.  
77 Consequently, anxious individuals could be driven to seek new information to update their  
78 beliefs and reduce uncertainty (12). However, research on the link between anxiety and  
79 exploration has yielded mixed findings, with some studies showing increased exploration to  
80 mitigate uncertainty (13, 14) and others showing reduced exploration to avoid unpredictable  
81 feedback under high anxiety (15, 16). Notably, apathy and anxiety often coexist in clinical  
82 populations, such as Alzheimer's (17), Parkinson's disease (18), and depression (19), despite  
83 having distinct neural representations (20, 21).

84

85 Building on these findings, we propose three fundamental questions to further elucidate the  
86 relationship between affective states and decision-making under uncertainty. First, we aim to  
87 investigate whether apathy and anxiety exhibit distinct behavioral patterns when individuals are  
88 faced with uncertain situations. Second, we seek to examine how individual differences in levels  
89 of apathy and anxiety are associated with perceptions of different types of uncertainty,  
90 specifically volatility and stochasticity. Finally, we intend to explore how perceived volatility  
91 influences exploratory behavior during decision-making processes.

92

93 We posit two competing hypotheses:

94 1. Apathetic individuals manifest less exploration, while anxious individuals engage in more  
95 exploration. Apathetic individuals weigh stochasticity over volatility and explore less, while  
96 anxious individuals overestimate volatility but explore more to reduce their uncertainty. This  
97 result would be consistent with previous findings suggesting that the two affective states have  
98 distinct neural substrates (20, 22).

99 2. Both apathetic and anxious individuals engage in less exploratory behavior but through  
100 different computational mechanisms. Apathetic individuals weigh stochasticity over volatility  
101 and explore less, while anxious individuals overestimate volatility, leading to a sense that their  
102 actions cannot track or learn from the environment, ultimately leading to exploitation. This may  
103 provide a computational account for learned helplessness (23) and the co-occurrence of apathy  
104 and anxiety in various clinical populations, such as Parkinson's and Alzheimer's diseases.

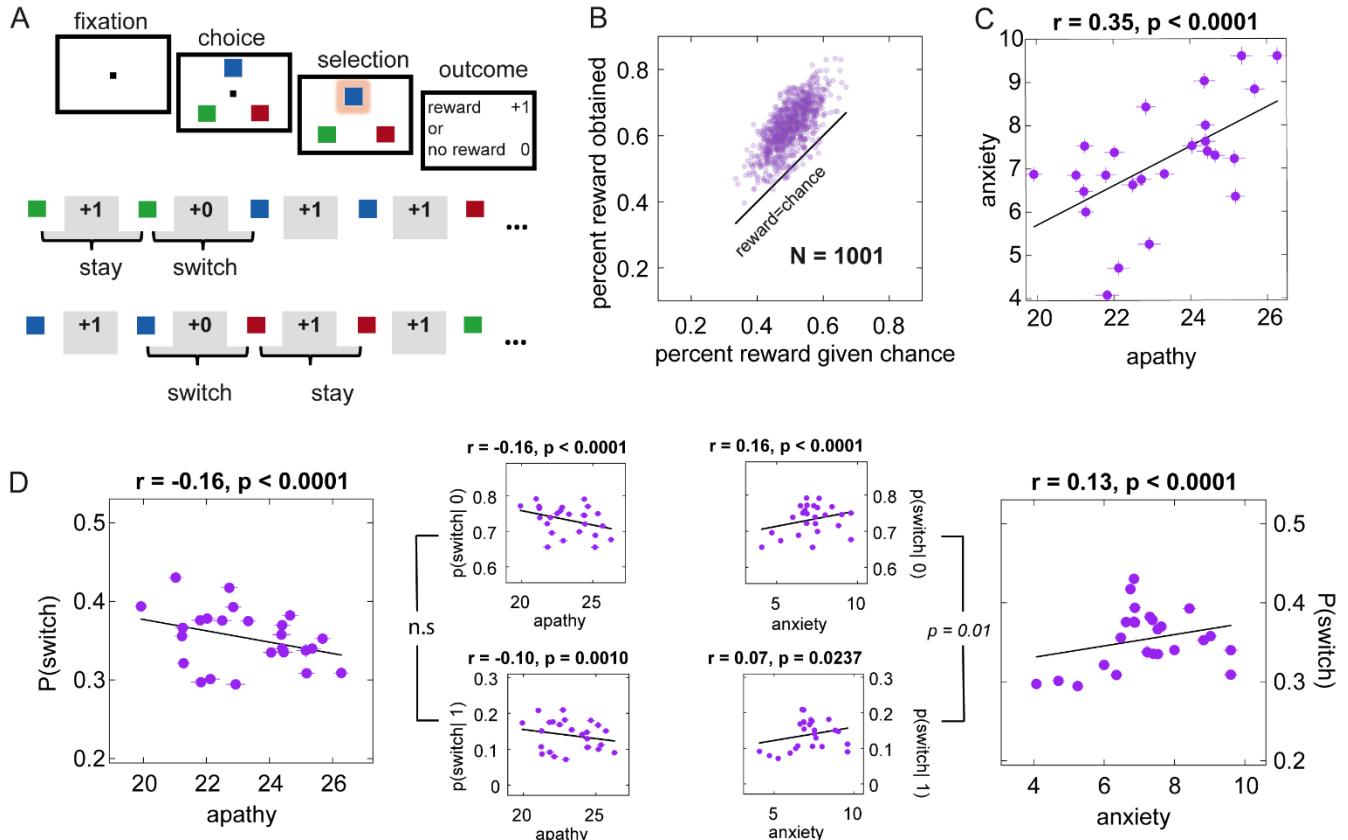
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106 To address these questions, we employed a restless three-armed bandit task ([Figure 1A](#)), a well-  
107 established paradigm for capturing adaptive learning in volatile environments(24). We adopted  
108 Hidden Markov Model (HMM) to obtain the likelihood of individuals switching between  
109 exploitation and exploration states (25, 26). To further investigate how volatility and  
110 stochasticity modulate exploration, we utilized a Kalman filter model, which can dissociate two  
111 distinct sources of noise, volatility (process noise variance) and stochasticity (observation noise  
112 variance), during inference (27). Together, these methods offer a comprehensive view of the  
113 cognitive mechanisms underlying exploratory behavior and the manifestation of anxiety and  
114 apathy.

115

116 **Results**

117 We recruited a large gender-balanced online sample consisting of 1,001 adults. The participants,  
118 ranging in age from 18 to 54 years (mean  $\pm$  SD =  $28.446 \pm 10.354$  years; gender: 493 female),  
119 performed a restless three-armed bandit task, as depicted in [Figure 1A](#). During this task,  
120 participants selected among three playing card images, with each card representing a different  
121 option. They made their selections by moving their cursor over their chosen card. The probability  
122 of receiving a reward from each card deck varied randomly over time. After each choice,  
123 feedback was displayed on the screen indicating whether a reward was received. Participants also  
124 completed symptom surveys assessing levels of anxiety and apathy (details in Methods and [SI](#)  
125 [Section 1, Table S1](#)). We defined the trial as a *switch* trial if the chosen option was different from  
126 the last trial, and a *stay* trial if the choice was the same as the last trial.



129 **Figure 1. Three-armed restless bandit task and distinct behavioral patterns associated with**  
130 **apathy and anxiety.**

131 (A) Three-armed restless bandit task. Participants chose one option from among the three targets  
132 to receive reward or non-reward feedback. Each target was associated with a hidden reward  
133 probability that randomly and independently changed throughout the task. The lower panel  
134 indicates the example choice and reward sequence and the definition of stay and switch.  
135 Specifically, stay was defined as choosing the same target as in the previous trial, while switch  
136 was defined as choosing a different target. “+1” denotes reward feedback, and “+0” denotes  
137 reward omission.

138 (B) Most participants earned more rewards than expected by chance

139 (C) Apathy and anxiety correlated positively.  
140 (D) Apathy correlated negatively with switch behaviors, while anxiety correlated positively with  
141 switch behaviors. Anxious individuals were more sensitive to undesired feedback (no reward)  
142 and exhibited more switch behaviors compared to reward feedback.  
143 (Panels in Figure 1C and 1D utilize binned correlation plots [25 quantile bins based on the x-  
144 axis], with lines representing the standard error (S.E.). N.B. that these may be smaller than the  
145 symbol. Statistical analyses were performed on raw data.)

146

147 ***Apathy and anxiety predicted distinct exploratory behaviors***

148 We first evaluated the performance by comparing the total number of rewarded trials each  
149 participant experienced against the number expected by chance. Out of the 1001 participants,  
150 985 accrued more rewarded trials than would be statistically expected by chance, suggesting  
151 significant effectiveness in their decision-making strategies (Figure 1B). As expected, anxiety  
152 and apathy showed a significant positive correlation ( $r = 0.35, p < 10^{-29}$ , Figure 1C), which is  
153 consistent with previous findings on their co-occurrence (17).

154 To investigate the relationship between apathy and the percentage of switch behaviors  
155 ( $P(\text{switch})$ ), as well as anxiety and  $P(\text{switch})$ , we conducted partial correlations between apathy  
156 and exploration while controlling for anxiety, and between anxiety and exploration while  
157 controlling for apathy. We found that apathy negatively predicted  $P(\text{switch})$  ( $r = -0.16, p < 0.001$ )  
158 regardless of feedback type (reward or no-reward), while anxiety positively correlated with  
159  $P(\text{switch})$  ( $r = 0.13, p < 0.001$ ). Intriguingly, the relationship between anxiety and switch  
160 behaviors was greater after non-reward feedback ( $r = 0.16, p < 0.001$ ) compared to reward  
161 feedback ( $r = 0.07, p = 0.024$ ) (their difference,  $z$ -score = 2.40,  $p = 0.01$ ). Though co-existing in

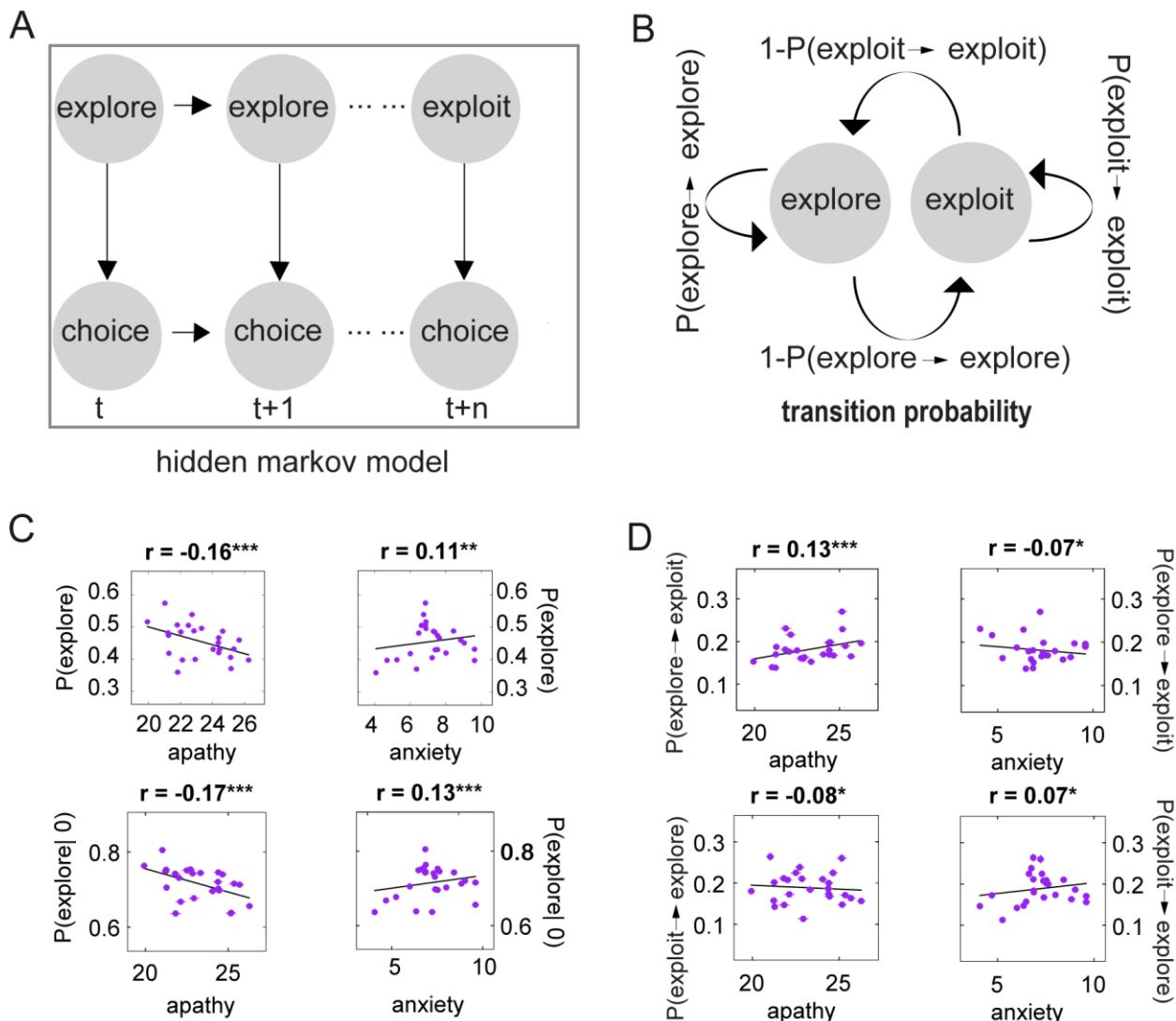
162 this population, these two affective states predicted distinct switch behaviors under uncertainty  
163 ([Figure 1D](#)). The stronger relationship between anxiety and  $P(\text{switch})$  after undesirable feedback  
164 indicates that highly anxious individuals are more sensitive to negative feedback, which may  
165 lead them to disengage.

166 Next, we fitted the behavior with a Hidden Markov Model (HMM) to decode the hidden states,  
167 “*explore*”, and “*exploit*” ([Figure 2A](#)) (24, 25, 28, 29). Each arm is associated with a hidden  
168 reward probability that randomly and independently changes throughout the task ([Figure 2A](#)). In  
169 our study, exploration and exploitation states are considered hidden states underlying the  
170 observed choices, such as switching between decks or repeatedly choosing from the same deck.  
171 We calculated the percentage of *explore* states, i.e.,  $P(\text{explore})$ . Consistently, apathy correlated  
172 negatively with  $P(\text{explore})$  ( $r = -0.17, p < 0.001$ ), while anxiety positively correlated with  
173 ( $P(\text{explore})$ ) ( $r = 0.11, p = 0.003$ ) as well as the percentage of exploration after reward  
174 omission( $P(\text{explore}|0)$ ) ( $r = 0.13, p < 0.001$ ) ([Figure 2C](#)).  
175 In addition to the overall frequency with which hidden states occur, examining the transitions  
176 between these states can further illuminate the dynamics of decision-making. Therefore, we  
177 investigated how apathy and anxiety manifest in the transition probability ([Figure 2B](#)) between  
178 *explore* and *exploit*. As predicted, apathy had a positive correlation with the transition  
179 probability from *explore* to *exploit* ( $r = 0.13, p < 0.001$ ) but a negative correlation with the  
180 transition probability from *exploit* to *explore* ( $r = -0.08, p = 0.011$ ). In contrast, anxiety had a  
181 negative correlation with the transition probability from *explore* to *exploit* ( $r = -0.07, p = 0.035$ )  
182 but a positive correlation with the transition probability from *exploit* to *explore* ( $r = 0.07,$   
183  $p < 0.022$ ) ([Figure 2D](#)). All significant results reported in the study survived False Discovery Rate

184 (FDR,  $p < 0.05$ ) correction.

185

186



187

188

189 **Figure 2. Apathy and anxiety have opposing relationships with exploration and explore and  
190 exploit state dynamics.**

191 (A) Unrolled structure of the hidden Markov model (HMM) used to infer the explore and  
192 exploit states' underlying behavior.

193 (B) The transition probabilities within and between states in the HMM.

194 (C) The probability of exploration, plotted as a function of apathy (top left) and anxiety (top

195 right). The probability of exploration following a reward omission is plotted as a function of

196 apathy (bottom left) and anxiety (bottom right).

197 (D) The transition probability from explore to exploit, plotted as a function of apathy (top

198 left) and anxiety (top right); the transition probability from exploit to explore plotted as a

199 function of apathy (bottom left) and anxiety (bottom right).

200 (Panels in Figure 2C and 2D utilize binned correlation plots [25 quantile bins based on the x-

201 axis], with lines representing the standard error (S.E.). N.B. that these may be smaller than

202 the symbol. Statistical analyses were performed on raw data). \*  $p < 0.05$ , \*\*  $p < 0.01$ , \*\*\*  $p$

203  $< 0.001$ . All p-values remained significant after FDR  $p < 0.05$  correction.

204

205 *Apathy and anxiety are associated with distinct computational processes underlying*  
206 *exploration.*

207 We then asked whether differing perceptions of the environment might explain the distinct  
208 patterns of exploration predicted by apathy and anxiety we observed.

209 To address this question, we utilized a Kalman filter model (Figure 3A), which can dissociate  
210 sources of uncertainty into perceived volatility and stochasticity (27). Kalman filter (KF) models  
211 have been widely applied in psychology and neuroscience to study various aspects of learning  
212 and decision-making (30, 31) (for more detailed information about the model, please refer to the  
213 Method section).

214 We also fitted the behavioral data to alternative models including volatile Kalman filter (VKF)  
215 (27), Rescorla-Wagner models single (RW1) (32) and dual learning rates (RW2) to weigh  
216 positive and negative learning rates (33). We employed Hierarchical Bayesian inference (HBI) to  
217 fit models to choice data (34). Further, we used Bayesian model selection (BMS) and protected  
218 exceedance probability (PXP) to select the winning model (Figure 3B). The Kalman filter served  
219 as the best model for our population, and we examined the resulting distribution of volatility and  
220 stochasticity (Figure 3B).

221 We first conducted correlation analyses using all data points. Specifically, we found that apathy  
222 was positively correlated with stochasticity ( $r = 0.08, p=0.013$ ) but negatively correlated with  
223 volatility ( $r = -0.08, p=0.008$ ). Conversely, anxiety showed a negative correlation with  
224 stochasticity ( $r = -0.12, p=0.001$ ) and a positive correlation with volatility ( $r = 0.12, p=0.002$ ).  
225 These correlations highlight the distinct cognitive biases associated with apathy and anxiety in  
226 processing environmental uncertainties.

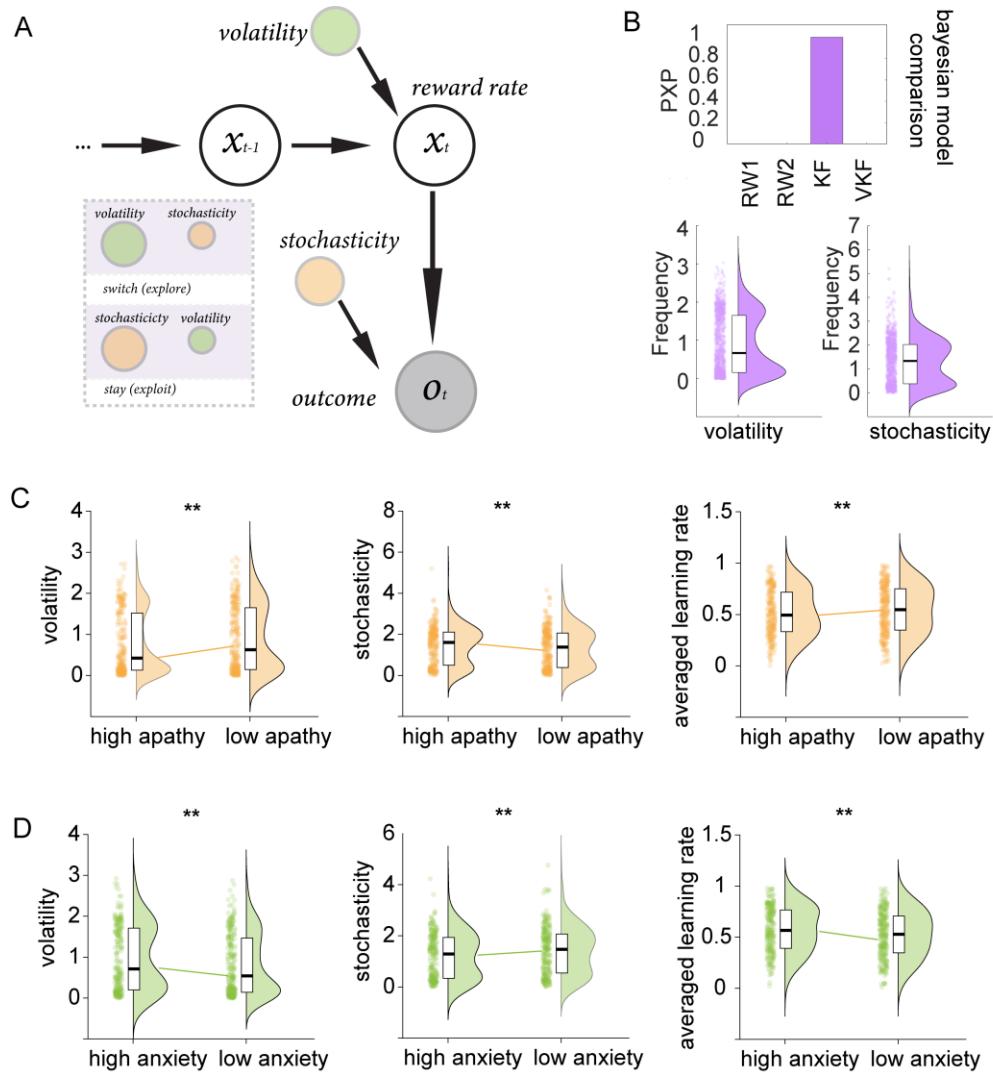
227 To clearly illustrate and confirm the findings, we categorized participants into distinct groups

228 based on their apathy and anxiety levels. For apathy, we identified the high apathy group (N =  
229 223) as those scoring in the top 25% on the Apathy Motivation Index (AMI), which assesses  
230 apathy in behavioral and social domains (35). Conversely, the low apathy group (N = 251)  
231 comprised individuals scoring in the bottom 25% of apathy scores. Similarly, for anxiety, the  
232 high anxiety group (N = 228) included participants within the top 25% of scores on the GAD-7  
233 scale (36), while the low anxiety group (N = 250) consisted of those in the bottom 25%. These  
234 classifications allowed for a direct comparison of behaviors and traits between individuals with  
235 varying degrees of apathy and anxiety.

236 We conducted linear regression analyses using volatility and stochasticity as the dependent  
237 variables with the high versus low anxiety and apathy groups as predictors. The Methods section  
238 provides details of the regression model specifications.

239 As hypothesized, apathetic individuals overestimated stochasticity ( $t(471) = 3.06, p=0.002$ ) and  
240 underestimated the volatility compared to those with low apathy ( $t(471) = -3.24, p=0.001$ ) (Figure  
241 3C). Consequently, apathetic individuals exhibited a lower learning rate than their low apathy  
242 counterparts ( $t(471) = -3.11, p=0.002$ ).

243 In contrast, individuals with high anxiety levels tended to overestimate volatility ( $t(475) = 2.84,$   
244  $p=0.004$ ) and underestimate stochasticity compared to those with low anxiety ( $t(475) = -3.04,$   
245  $p=0.002$ ), resulting in a higher learning rate among the high anxiety group ( $t(475) = 3.21,$   
246  $p=0.001$ ) (Figure 3D). Furthermore, comparisons showed that anxious individuals had higher  
247 volatility estimates than those with high apathy ( $t(449) = 2.75, p=0.006$ ), whereas apathetic  
248 individuals had higher stochasticity estimates than their anxiety counterparts ( $t(449) = -3.01,$   
249  $p=0.002$ ) (SI Section 2, Figure S1).



250

251 **Figure 3. Apathy and anxiety have opposing relationships with volatility and stochasticity.**

252 (A) The schematic of the Kalman filter model used in our analysis. The diagram illustrates how

253 this model can differentiate between volatility (process noise variance) and stochasticity

254 (observation noise variance), providing insights into the underlying decision-making processes.

255 (B) Bayesian model comparison and the distribution of volatility, stochasticity

256

257 (C) Highly apathetic individuals overestimated stochasticity but underestimated the volatility,

258 resulting in a lower learning rate.

259 (D) In contrast, highly anxious individuals overestimated volatility but underestimated  
260 stochasticity, resulting in a higher learning rate.

261  $*p < 0.05$ ,  $** p < 0.01$ ,  $*** p < 0.001$ . All p-values remained significant after FDR  $p < 0.05$   
262 correction.

263

264 ***The ratio of volatility to stochasticity distinguished apathy and anxiety***

265 To clarify the differential impacts of apathy and anxiety on decision-making under uncertainty,  
266 we computed the ratio of volatility to stochasticity,  $v/s$  to represent the balance between these  
267 two types of uncertainties. A higher  $v/s$  indicates a perception of greater volatility relative to  
268 stochasticity, while a lower ratio suggests a perception of more stochasticity relative to volatility.

269 We applied a logarithmic transformation to the ratio to manage extreme values (e.g. cases where  
270 individuals might perceive very high volatility but very low stochasticity).

271 Consistently, our findings reveal a clear distinction:  $v/s$  correlated negatively with apathy ( $r = -$   
272  $0.08, p=0.010$ ) but positively with anxiety ( $r = 0.13, p < 0.001$ ) (Figure 4A).

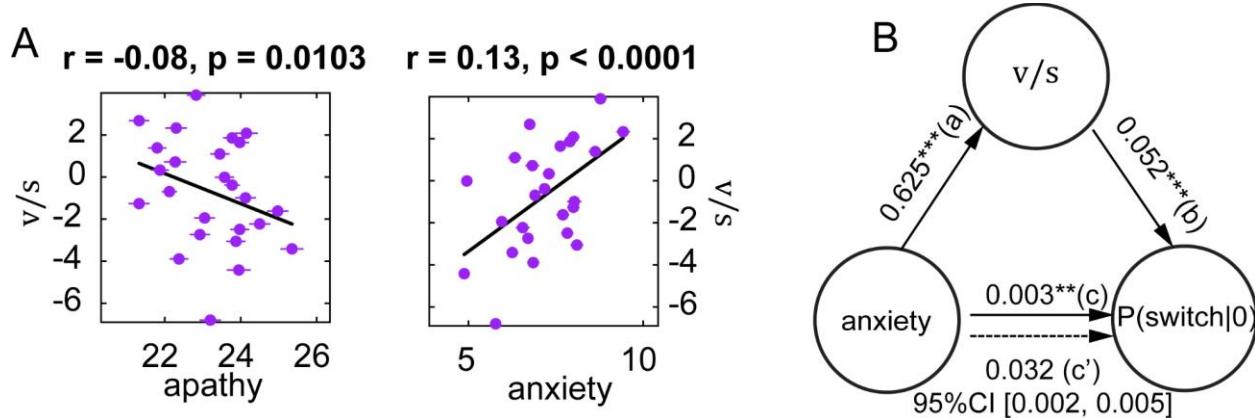
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274 ***The ratio of volatility and stochasticity mediated the relationship between anxiety and the***  
275 ***exploration after negative feedback***

276 To determine whether individual differences in the perception of uncertainty explain the  
277 relationship between exploratory behavior and affect, we conducted a mediation analysis with  
278 anxiety, switching after reward omission ( $P(\text{switch} | 0)$ ), and  $v/s$ . The results demonstrate that  
279 the relationship between anxiety and the tendency to switch after receiving no reward is  
280 significantly mediated by  $v/s$  (Figure 4B). This mediation was also significant for the analogous  
281 HMM model-based measures (see SI Section 3, Figure S2). No significant mediation effect was

282 found for apathy, however, reinforcing the unique pathways through which anxiety influences  
283 exploratory behavior. These results explain why individuals with higher anxiety might explore  
284 more after negative feedback, driven by an overweighting of perceived volatility relative to  
285 stochasticity as a strategy to reduce uncertainty and manage risks.

286



289 **Figure 4. Distinctions in apathy and anxiety on the ratio of volatility to stochasticity and its  
290 mediation effect.**

291 (A) The ratio of volatility to stochasticity, plotted as a function of apathy (left) and anxiety  
292 positively (right).

293 (B) Mediation analysis, showing the mediating effect of the ratio of volatility to stochasticity on  
294 the relationship between anxiety and switch behavior after reward omission.

295 (Panels in Figure 4A utilize binned correlation plots [25 quantile bins based on the x-axis], with  
296 lines representing the standard error (S.E.). N.B. that these may be smaller than the symbol.

297 Statistical analyses were performed on raw data). \*  $p < 0.05$ , \*\*  $p < 0.01$ , \*\*\*  $p < 0.001$ . All p-  
298 values remained significant after FDR  $p < 0.05$  correction).

299

300

301 **A low dimensional manifold unifies exploration, perceptions of uncertainty and affective**  
302 **state.**

303 The HMM state-model of exploration-exploitation and the Kalman filter process model of  
304 uncertainty estimation represent complementary ways of understanding adaptive behavior that  
305 our mediation results suggest are intrinsically related. We hypothesized that a latent structure  
306 underlying adaptive behavior on this task might unify these descriptions of behavior. We utilized  
307 advanced dimensionality reduction methods to uncover such a latent structure in the raw task  
308 behavior.

309 First, we formatted each participant's trial-by-trial task data into sequences of choices to stay  
310 (repeat the choice on the last trial) or switch (choose a different option) and reward outcome for  
311 two consecutive trials ( $\{\text{choice}_{t-1}, \text{outcome}_{t-1}, \text{choice}_t\}$ , [Figure 5A and 5B](#)). The behavioral data  
312 for each participant was then transformed into counts for each of these eight unique sequences.

313 Then we applied Uniform Manifold Approximation and Projection (UMAP) (37), a  
314 computationally efficient algorithm that can preserve both the local and global distances between  
315 data points in high-dimensional space, to learn the two-dimensional manifold underlying the  
316 eight-dimensional behavioral data ([Figure 5C](#), see Methods for more algorithm details).

317 Including additional reward history and applying other dimensionality reduction methods like  
318 principle component analysis (PCA), and t-distributed Stochastic Neighbor Embedding (t-SNE)  
319 did not change the results ([SI Section 4, Figure S3, Table S2](#)).

320 Our analysis using UMAP revealed distinct correlations within the derived dimensions.  
321 Specifically, the dimension 1 score (the horizontal axis) exhibited a very strong significant  
322 negative correlation with exploratory behavior ( $P(\text{explore})$ ) ( $r = -0.90, p < 10^{-200}$ ), but it showed no

323 significant relationship with the ratio of volatility to stochasticity ( $v/s$ )( $r = 0.01, p=0.74$ ) (Figure  
324 [5D](#), [5E](#)). In contrast, the dimension 2 score (the vertical axis) demonstrated a strong negative  
325 correlation with  $v/s$  ( $r = -0.76, p<10^{-185}$ ), which was significantly more pronounced than its  
326 correlation with P(explore) ( $r = -0.19, p<10^{-10}$ ) ([Figure 5F](#), [5G](#)). This suggests that dimension 1  
327 primarily represents exploratory behavior, while dimension 2 primarily reflects the  
328 computational factors: volatility and stochasticity (i.e., volatility and stochasticity).  
329 Further, both dimensions also showed correlations with affective states: the dimension 1 score  
330 was positively correlated with apathy ( $r= 0.14, p<0.001$ ), and negatively correlated with anxiety  
331 ( $r = - 0.11, p<0.001$ ). Similarly, the dimension 2 score had a positive correlation with apathy ( $r =$   
332  $0.097, p=0.002$ ) and a negative correlation with anxiety ( $r = -0.088, p=0.004$ ).  
333 It is worth noting that we only found linear relationships between apathy, anxiety, and  
334 exploration, as well as between these affective states and the ratio of volatility to stochasticity  
335 (our analysis using higher order effects among these variables did not yield significant results,  
336 more details can be found in [SI Section 5, Table S3](#)).  
337 To delve deeper into how these factors interact in the low-dimensional space defined by UMAP,  
338 we divided the data manifold into two groups based on the dimension1 score: a monotonically  
339 decreasing group (left part, dimension 1 score  $< -0.671, N=390$ ) and a monotonically increasing  
340 group (right part, dimension 1 score  $> -0.671, N=611$ ). The methodology used to identify the  
341 turning point (dimension 1 score =  $-0.671$ ) that differentiates the monotonically decreasing group  
342 from the monotonically increasing group is detailed in the Methods section. The analysis  
343 revealed that the monotonically decreasing group had relatively higher levels of anxiety  
344 compared to the monotonically increasing group ( $t(999)=2.08, p =0.037$ ), while their apathy  
345 levels were significantly lower ( $t(999)= -3.56, p=0.0003$ ). This segmentation allows us to further

346 explore and understand the complex interplay between affective states, computational  
347 parameters, and exploratory behaviors within a structured, low-dimensional framework.

348 Notably, individuals in the left monotonically decreasing group, characterized by high anxiety  
349 and low apathy, generally perceive higher volatility relative to stochasticity and demonstrate  
350 greater exploratory behavior compared to those in the right monotonically increasing group.

351 Within the decreasing group, higher perceived volatility correlates with reduced exploration.

352 Conversely, in the increasing group, an increased perception of volatility tends to stimulate more  
353 exploratory actions. These results suggest that while severe anxiety might suppress exploration  
354 due to overwhelming uncertainty, moderate anxiety in the general population can promote  
355 exploration as a coping mechanism to gather information and reduce anxiety symptoms.

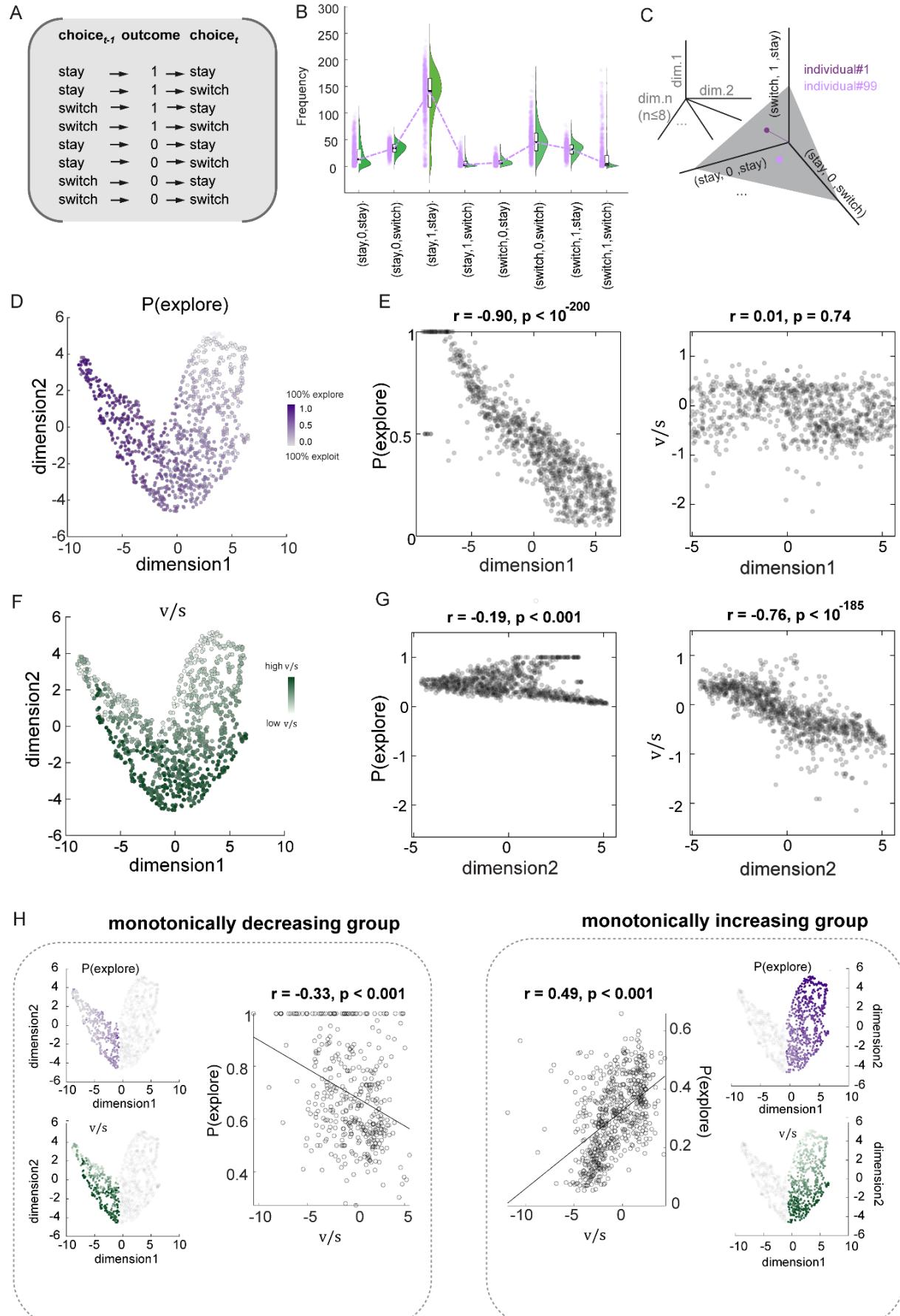
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357 We now address our final research question; what is the relationship between volatility and  
358 exploratory behavior? Considering the parabolic relationship between the manifold dimension  
359 reflecting exploration and the dimension representing  $\nu/s$ , we hypothesized that the relationship  
360 between exploration and  $\nu/s$  might be quadratic.

361 To test this hypothesis, we constructed a regression model as follows:

362  $P(explore) \sim \nu/s + \nu/s^2 + anxiety + apathy$

363 The results revealed that both the linear and quadratic terms are significant (linear term,  
364 coefficient = 0.02, SE = 0.003,  $t(996)=5.83, p<10^{-9}$ ; quadratic term, coefficient = 0.005, SE =  
365  $7.86 \times 10^{-4}$ ,  $t(996)=6.59, p<10^{-9}$ ), indicating a complex, non-linear relationship between the ratio  
366 of volatility to stochasticity and exploration (see [SI Section 6, Figure S4](#)), which was consistent  
367 with the manifold representation.



369 **Figure 5. Visualizing the complex relationships in decision-making through low-**  
370 **dimensional space.**

371 (A) All possible sequences of choices and rewards that participants could make during the  
372 experiment

373 (B) The frequency distribution of individual decision-making patterns. The black line in the box  
374 plot represents each pattern's mean value, highlighting participants' typical behaviors

375 (C) Schematic high-dimensional space of participants' decision-making pattern

376 (D) The two-dimensional space representation of exploration by using the Uniform Manifold  
377 Approximation and Projection (UMAP) (Different dimensionality reduction methods such as  
378 principal component analysis (PCA), and t-distributed Stochastic Neighbor Embedding (t-SNE)  
379 lead to a similar space)

380 (E) Dimension 1 exclusively represents P(explore) but does not represent the ratio of volatility to  
381 stochasticity

382 (F) The two-dimensional space representation of the ratio of volatility to stochasticity behavior  
383 by using UMAP (Different dimensionality reduction methods such as principal component  
384 analysis (PCA), and t-distributed Stochastic Neighbor Embedding (t-SNE) lead to a similar  
385 space)

386 (G) Dimension 2 mainly represents the ratio of volatility to stochasticity but not P(explore)

387 (H) The manifold has been separately dissociated into the monotonically decreasing group (the  
388 most left panel) and monotonically increasing group (the most right panel). The monotonically  
389 decreasing group was associated with a relatively higher anxiety level than the monotonically  
390 increasing group, while the apathy level was significantly lower than the monotonically  
391 increasing group. Within the monotonically decreasing group (left part), a higher volatility to

392 stochasticity ratio leads to decreased exploration. In contrast, within the monotonically  
393 increasing group (right part), a higher volatility to stochasticity ratio encouraged higher  
394 exploration. This exploration serves as a coping strategy to relieve anxious feelings in the  
395 environment.

396 All p-values remained significant after FDR  $p<0.05$  correction.

397

398

399

400 **Discussion**

401 We found that apathy and anxiety predicted opposing patterns of exploratory behavior, which  
402 were explained partly by differing perceptions of uncertainty. Anxiety was associated with  
403 increased exploration after reward omission and greater volatility estimation: the attribution of  
404 uncertainty to a rapidly changing (but still learnable) environment. Apathy, in contrast, predicted  
405 decreased exploration and higher stochasticity estimation: the perception of uncontrollable  
406 randomness. Following a dimensionality reduction of the raw behavioral data, exploration and  
407 perceptions of uncertainty emerged as the dimensions of an underlying latent structure that  
408 unified the different model approaches and the affective states. These findings elucidate the  
409 complex interplay between cognitive assessments of uncertainty, affective states, and decision-  
410 making processes, offering several key insights into adaptive and maladaptive behaviors under  
411 uncertainty.

412

413 The distinct patterns of exploratory behavior observed in anxious and apathetic individuals  
414 highlight the role of affective states in shaping responses to uncertainty. Anxious individuals,  
415 who generally display a heightened sensitivity to potential threats and environmental changes,  
416 exhibited a bias toward perceiving greater volatility and exploring more after negative outcomes.  
417 Our mediation analysis revealed that the perception of volatility relative to stochasticity partially  
418 mediates the relationship between anxiety and exploratory behavior after reward omission. This  
419 finding is consistent with previous results (38) and offers a mechanistic explanation for why  
420 anxious individuals in a healthy population might choose to explore more after receiving  
421 negative feedback. The perceived overweighting of volatility relative to stochasticity may drive

422 these individuals to seek more information, potentially as a strategy to reduce uncertainty and  
423 manage perceived risks more effectively (39). Although such a strategy may be beneficial for  
424 adaptation in genuinely volatile environments, it may also contribute to excessive worry and  
425 stress, especially if the perceived level of volatility exceeds actual environmental volatility (9,  
426 11). Consequently, anxious individuals may find themselves in a prolonged state of heightened  
427 arousal and uncertainty, leading to suboptimal decision-making and diminished well-being.

428

429 On the other hand, apathetic individuals, who generally exhibit diminished motivation and  
430 responsiveness (40), tended to attribute outcomes more to stochasticity in our study. This  
431 perception might underlie their reduced exploratory behavior, reflecting a disengagement from  
432 active learning and adaptation. If outcomes seem random and beyond our control, expending  
433 energy to explore may seem futile, and focusing on what we know seems rational. While this  
434 approach may conserve energy, the inflexibility can perpetuate a cycle of disengagement and  
435 maintain apathetic symptoms (41, 42). Apathetic individuals may fail to recognize the potential  
436 benefits of exploration and remain stuck in suboptimal decision-making patterns, further  
437 reinforcing their disengagement from the environment (4).

438

439 The dimensionality reduction of the behavioral sequence data using UMAP allowed us to  
440 examine the relationship between exploration and the estimation of volatility and stochasticity.  
441 Despite the intuitive connection between these two behavior models, their relationship has not  
442 been directly examined. Our results showed that exploration and uncertainty estimation related  
443 closely to the two axes of a parabolic latent structure of adaptive behavior. As a result, both  
444 model-based metrics were necessary to characterize the spectrum of individual differences fully.

445 Segmenting the data on the manifold further illuminated the fine-grained interplay between  
446 affective states and exploratory behavior. Individuals with relatively higher anxiety and lower  
447 apathy (the monotonically decreasing group) generally weighted volatility more and  
448 demonstrated greater exploratory behavior compared to those with lower anxiety and higher  
449 apathy (the monotonically increasing group). However, *within* these groups formed on the  
450 manifold, individuals exhibited opposing relationships between uncertainty and exploration. In  
451 the higher anxiety group, perceived volatility correlates inversely with exploration. However, in  
452 the lower anxiety group, increased volatility perception predicts greater exploration.

453

454 These results reconcile previously inconsistent findings regarding exploratory behavior in  
455 individuals with anxiety, with some studies showing more exploitative behavior (15, 16), and  
456 others finding that higher anxiety predicts more exploratory behaviors (13, 14). The relationship  
457 between perceived volatility and exploration is modulated by the degree of anxiety, with more  
458 severe anxiety potentially suppressing exploration as a form of avoidance. Conversely, moderate  
459 anxiety may drive exploration to gather information and reduce uncertainty, potentially easing  
460 discomfort. This dual response to perceived volatility underscores the complex interplay between  
461 anxiety levels, environmental perceptions, and behavioral strategies in managing emotional  
462 responses.

463

464 Our findings have implications for personalized behavioral interventions in mental health. For  
465 anxious individuals, therapies focusing on recalibrating volatility perceptions and improving  
466 uncertainty management may reduce worry and enhance decision-making (43, 44). Encouraging  
467 longer-term information integration could also benefit anxiety management (38). For apathetic

468 individuals, strengthening perceived control and action efficacy may counteract stochasticity  
469 attribution. Incorporating these strategies into existing therapies like Behavioral Activation and  
470 Motivational Interviewing (45) could promote balanced environmental perceptions and  
471 exploration.

472

473 Another important clinical implication involves using an individual's position on the behavioral  
474 manifold (Figure 5) to predict how their behavior might change in response to treatment based  
475 on their symptoms. For example, a patient positioned in the upper left quadrant before treatment  
476 may exhibit higher anxiety, lower apathy, and increased exploratory behavior. During and after  
477 treatment, monitoring these behavioral shifts may allow us to infer changes in their affective  
478 states or symptoms based on their new manifold position. To develop such a tool, several  
479 questions remain: Do changes within an individual follow a predictable trajectory on this  
480 manifold? Do clinical populations conform to the same manifold, or do they deviate, projecting  
481 into the larger, unoccupied areas of the manifold? The answers to these questions could enhance  
482 the implementation of dimensional approaches for individualized neuropsychiatric care (46).

483

484 Our results must be interpreted in light of notable limitations. First, the study primarily utilized  
485 an online sample, which may not accurately represent the demographic and clinical  
486 characteristics of populations with specific mental health diagnoses. The potential differences in  
487 internet access, motivation, and the self-report nature of online studies can introduce biases that  
488 may differ from clinical settings. Consequently, the generalizability of our findings to clinical  
489 populations remains to be determined. Second, while our results are statistically robust and  
490 significant, it is important to note that the observed effect sizes are relatively small. This is not

491   uncommon in studies of individual differences, where effect sizes often are modest due to the  
492   complex nature of human behavior and the multitude of factors influencing decision-making  
493   processes (47). Nonetheless, these small effects can still provide valuable insights into the  
494   relationships between affective states and decision-making under uncertainty. Third, our results  
495   are inherently correlational, limiting our ability to infer causal relationships between the affective  
496   states of apathy and anxiety and their impacts on decision-making processes. The observed  
497   associations provide a strong foundation for hypothesizing causal mechanisms but do not  
498   confirm them. Future studies may examine clinical samples of conditions known to affect  
499   adaptive decision-making under uncertainty, such as depression, anxiety disorders, and  
500   Parkinson's disease, as well as interventions targeting the physiology of adaptive behavior.

501

502

503 **Method**

504 ***Ethics approval***

505 The experimental procedures of all experiments were in line with the standards set by the  
506 Declaration of Helsinki and were approved by the local Research Ethics Committee of the  
507 University of Minnesota, Twin Cities. Participants provided written informed consent after the  
508 experimental procedure had been fully explained and were reminded of their right to withdraw at  
509 any time during the study.

510

511 ***Participants***

512 We recruited a sample of 1512 participants via Amazon Mechanical Turk (MTurk) and Prolific  
513 (Prolific. co); exclusion criteria included current or history of neurological and psychiatric  
514 disorders. 1001 participants completed all questionnaires and the bandit task (age range 18-54,  
515 mean  $\pm$  SD =  $28.446 \pm 10.354$  years; gender, 493 female). All participants were compensated for  
516 their time in accordance with minimum wage.

517

518 ***Questionnaire measurement***

519 Participants' anxiety and apathy states were measured by the General Anxiety Disorder Screener  
520 (GAD-7) (36), and the Apathy-Motivation Index (35), respectively. More specifically, GAD-7  
521 contains 7 items for assessing anxiety severity in the last two weeks. All items were rated on a 4-  
522 point scale, with higher scores indicating greater anxiety. Participants' apathy level was  
523 measured using the 18-item Apathy-Motivation Index (AMI), which was designed to identify  
524 and measure general apathy, as well as subtypes of apathy in behavioral, social, and emotional

525 domains. Higher scores on AMI represent greater apathy. We also measured depressive and  
526 anhedonia states by Patient Health Questionnaire (PHQ-9) (48) and Snaith-Hamilton Pleasure  
527 Scale (SHPS) (49). Our analysis did not reveal any significant results related to depressive states  
528 or anhedonia. For all questionnaire scores, see [SI, Section 1 & Table S1](#).

529

530 ***Three-armed restless bandit task***

531 We assessed exploration-exploitation behavioral dynamics using a 300-trial three-armed restless  
532 bandit task (25). Participants were free to choose between three targets for the potential to earn a  
533 reward of 1 point. Each target is associated with a hidden reward probability that randomly and  
534 independently changes throughout the task. We seeded each participant's reward probability  
535 walks randomly to prevent biases due to particular kinds of environments. We assessed  
536 performance by comparing the total number of rewarded trials to that expected by chance. Out of  
537 the 1001 participants, 985 accrued more rewarded trials than would be expected by chance.

538

539 ***Dimensionality reduction method***

540 Popular and valid dimensionality reduction techniques to reveal manifolds include t-distributed  
541 stochastic neighborhood embedding (t-SNE) (50), uniform manifold approximation and  
542 projection (UMAP) (37), and Principal component analysis (PCA) (51). However, t-SNE suffers  
543 from limitations, including slow computation time and loss of global data structure, and it is not  
544 a deterministic algorithm (52). The main drawback of PCA is that it is highly affected by outliers  
545 in the dataset (51). In contrast, UMAP is a deterministic and efficient algorithm, it also preserves  
546 both local and global structure of original high-dimensional data. Uniform Manifold  
547 Approximation and Projection (UMAP)

548 UMAP was implemented in the R language. The eight-dimensional datasets from all participants  
549 were passed into the R package *umap*, version 0.2.8.0, available at <https://cran.r-project.org/web/packages/umap/>) with default parameter setting as *n\_component* = 2,  
550 *n\_neighbors* = 15, *min\_dist* = 0.3, *metric* = ‘Euclidean’. For reproducibility reasons, we fixed the  
551 *random\_state* in this algorithm. The hyperparameter *n\_neighbors* decide the radius of the search  
552 region. Larger values will include more neighbors, thus forcing this algorithm to consider more  
553 global structure of original n-dimension data. Another important hyper-parameter, *min\_dist*  
554 determines the allowed minimum distance apart for cases in lower-dimensional space. *metric*  
555 defines the way that UMAP is used to measure distances along the manifold.

557

558 ***Model-free analyses***

559 We adopted some widely used model-free measures, including win-stay and lose-shift (33, 53) as  
560 the direct measurement for this learning task.

561 *Win-stay*. Win-stay is defined as the percentage of times that the choice in trial  $t-1$  was repeated  
562 on trial  $t$  following a reward.

563 *Lose-shift*. In contrast, lose-shift equals the percentage of trials that the choice was shifted or  
564 changed when the outcome of trial  $t-1$  was non-reward.

565 Model free results can be found at [SI Section 7, Table S4](#).

566

567 ***Mediation analyses***

568 Mediation analysis is a statistical method used to examine the underlying mechanisms by which  
569 an independent variable influences a dependent variable through one or more mediator variables  
570 (54). In our study, we employed the bootstrapping method to estimate the mediation effect of

571 volatility and stochasticity on the relationship between affective states (apathy and anxiety) and  
572 exploration. Bootstrapping is a nonparametric approach to effect-size estimation and hypothesis  
573 testing that is increasingly recommended for many types of analyses, including mediation (55).  
574 This method involves repeatedly resampling from the available data to generate an empirical  
575 approximation of the sampling distribution of the indirect effect (i.e., the effect of the  
576 independent variable on the dependent variable through the mediator). We used this distribution  
577 to calculate p-values and construct confidence intervals based on 5,000 resamples. Bootstrapping  
578 is preferred over other methods, such as the Sobel test because it does not assume the normality  
579 of the sampling distribution and provides more accurate confidence intervals that are bias-  
580 corrected and accelerated (54, 55). This approach offers a robust and powerful way to test  
581 mediation hypotheses, particularly in cases where the sample size is relatively small or the data  
582 violate assumptions of normality (56).

583

584 ***Hidden Markov Model***

585 We fit a Hidden Markov Model (HMM) to the behavior, to decode the hidden state of each trial  
586 for each participant. Fundamentally, the HMM has two layers, the hidden layer (i.e., state) and  
587 the observable layer. The hidden dimension should satisfy the Markov property. That is, the  
588 current hidden state only depends on the previous state but not any past model history. The  
589 observable dimension entirely depends on the current hidden states and is independent of other  
590 observations. Parameters of the hidden Markov model can be represented as  $\Omega \rightarrow (T, O, c)$ .  
591 Specifically,  $T$  is the transition probabilities matrix,  $O$  is the observation probabilities matrix, or  
592 emissions matrix, and  $c$  refers to a vector with initial probabilities for each hidden state. Here,  
593 we have two hidden states, an “exploration” state and an “exploitation” state.

594 The transition probability between exploration and exploitation states can be represented by:

595

596 
$$T = \begin{pmatrix} t_{11} & \cdots & t_{1m} \\ \vdots & \ddots & \vdots \\ t_{m1} & \cdots & t_{mm} \end{pmatrix}$$

597

598 
$$t_{explore,exploit} = P(q_k = s_{exploit} | q_{k-1} = s_{explore})$$

599

600 Where  $t_{explore,exploit}$  refers to the transition probability from hidden state  $s_{exploit}$  to another  
601 hidden state  $s_{explore}$

602  $k$  = time instant,  $m$  = state sequence length

603

604 Then matrix  $O$  represents the transition probabilities between hidden and observable states.

605

606 
$$O = \begin{pmatrix} o_{11} & \cdots & o_{1n} \\ \vdots & \ddots & \vdots \\ o_{m1} & \cdots & o_{mn} \end{pmatrix}$$

607

608 
$$o_{explore,exploit} = P(\lambda_k = r_{exploit} | q_{k-1} = s_{explore})$$

609

610  $k$  = time instant,  $n$  = observation sequence length

611 Both matrix  $O$  and  $T$  satisfy the principle that the sum along the rows must be equal to 1.

612  $c$  is an  $m$ -dimensional row vector that refers to the initial probability distribution. In our current  
613 study, the initial probability was fixed and equal to the available choices.

614 We fit HMM via expectation-maximization using the Baum-Welch algorithm and decode hidden  
615 states from observed choice sequences by the Viterbi algorithm (57). Model results of HMM can  
616 be found at [SI Section 7, Table S5](#).

617

618 ***Kalman filter***

619 The Kalman filter (KF) model has been widely applied in psychology and neuroscience to study  
620 various aspects of learning and decision-making (30, 31).

621 In the Kalman filter model for a multi-armed bandit task, *process noise* and *observation noise*  
622 refer to two distinct sources of uncertainty that affect the learning and decision-making process.  
623 Process noise represents the uncertainty in the evolution of the hidden state (reward mean) over  
624 time. It accounts for how the true state evolves from one point in time to the next. In  
625 mathematical terms, process noise is part of the state transition equation in the Kalman Filter:

$$x_t = x_{t-1} + e_t$$

626  $x_t$  is the state at time  $t$

627  $e_t$  is the process noise  $t$ , which is assumed to be drawn from a normal distribution with zeros  
628 mean and **process noise variance**  $\nu$ . Where the  $e_t \sim N(0, \nu)$ .

629 The process noise captures the idea that the reward-means for each arm can change from one  
630 trial to the next, even in the absence of any observations. A higher process noise variance  $\nu$   
631 indicates a more volatile environment, where the reward means are expected to change more  
632 rapidly.

633 In contrast, **observation noise** represents the uncertainty in the observed rewards, given the  
634 current hidden state (reward mean). Which is assumed to be Gaussian with zero mean and a  
635 fixed variance  $\sigma^2$ .

637 The observation noise captures the idea that the observed rewards are noisy and can deviate from  
638 the true reward mean due to random fluctuations or measurement errors.  
639 A higher measurement noise variance indicates a more stochastic environment, where the  
640 observed rewards are less reliable and informative about the underlying reward means.  
641 The Kalman Filter operates optimally when the statistical properties of the process noise and the  
642 measurement noise are accurately known.  
643 When observation noise variance ( $\sigma^2$ ) is high relative to the process noise variance ( $\nu$ ), the  
644 Kalman gain will be small, and the model will rely more on its prior beliefs and less on noisy  
645 observations. Conversely, when the observation noise variance ( $\nu$ ), is high relative to the process  
646 noise variance ( $\sigma^2$ ), the Kalman gain will be large, and the model will update its beliefs more  
647 strongly based on the observed rewards.

648

649 ***Extended Kalman filter for three-armed bandit task***

650 The Kalman filter model can be extended to capture the effects of both volatility and  
651 stochasticity in a multi-armed bandit task (27, 58).  
652 In the current study, process noise variance ( $\nu$ ) and observation noise variance ( $\sigma^2$ ) represent  
653 volatility and stochasticity, respectively.  
654 A traditional assumption of the Kalman filter is that the process noise variance,  $\nu$ , as well as the  
655 observation noise variance,  $\sigma^2$  are constant.

656 Reward means update:

657

658 
$$m_t = m_{t-1} + k_t(O_t - m_{t-1})$$

659

660 Where  $m_t$  is the estimated mean or value of the chosen arm at time  $t$   
661 and  $O_t$  is the observed reward at time  $t$ .  
662 The mean update is driven by the prediction error, which is the difference between the observed  
663 reward and the previous estimate.

664

665 Kalman gain is defined as:

666

667 
$$k_t = (w_{t-1} + v) / (w_{t-1} + v + \sigma^2)$$

668

669 Here,  $k_t$  represents the Kalman gain or learning rate, which adjusts the weight given to new  
670 information based on the relative uncertainty of the prior estimate ( $w_{t-1}$ ) and the total noise ( $v +$   
671  $\sigma^2$ ). When the stochasticity ( $\sigma^2$ ) is high relative to the volatility ( $v$ ), the Kalman gain (learning  
672 rate) will be small, and the model will rely more on its prior beliefs and less on the observations.  
673 Conversely, when the volatility ( $v$ ), is high relative to the stochasticity ( $\sigma^2$ ), the Kalman gain  
674 (learning rate) will be large, and the model will update its beliefs more strongly based on the  
675 observed rewards.

676

677 Variance update equation:

678

679 
$$w_t = (1 - k_t)(w_{t-1} + v)$$

680

681 This equation updates the posterior variance ( $w_t$ ), which represents the estimate's uncertainty  
682 after observing  $O_t$ .

683

684 ***Volatile Kalman filter for three-armed bandit task***

685 The key difference between a standard Kalman filter and a volatile Kalman filter (VKF) is the  
686 variance of the process noise, a stochastic variable that changes with time. In other words, the  
687 VKF introduces parameters to handle the volatility in the process noise. Specifically, it allows  
688 the process noise variance  $\nu$  to vary with the observed prediction errors, reflecting changes in  
689 environmental volatility.

690 Our approach here is essentially the same as that taken by Piray and Daw (27). Here, we briefly  
691 described the model details as follows.

692

693 Kalman gain:

694 
$$k_t = (w_t + \nu_{t-1}) / (w_{t-1} + \nu_{t-1} + \sigma^2)$$

695 Update for the reward means:

696

697 
$$m_t = m_{t-1} + k_t (O_t - m_{t-1})$$

698

699 Update for posterior variance  $w_t$ :

700

701 
$$w_t = (1 - k_t)(w_{t-1} + \nu_{t-1})w_{t-1,t} = (1 - k_t)w_{t-1}$$

702

703 Update for volatility:

704 
$$\nu_t = \nu_{t-1} + \lambda((m_t - m_{t-1})^2 + w_{t-1} + w_t - 2w_{t-1,t} - \nu_{t-1})$$

705

706 **Rescorla-Wagner models**

707 We also fitted the data to the classical Rescorla-Wagner model. Successful adaptation in a dynamic  
708 situation requires the appropriate feedback-based learning process where individuals integrate the  
709 feedback (reward or non-reward) into the stimulus-outcome association (59). The basic  
710 reinforcement learning model, the Rescorla-Wagner model can address this process well. So the  
711 first model (RW1) was defined as:

712

713 
$$v_t = v_{t-1} + a \times (R_{t-1} - v_{t-1})$$

714

715 where  $v_t$  is the value of the option on trial  $t$ .

716  $a$  represents the general learning rate from feedback.

717

718 To verify whether participants employed distinct or shared computational responses to positive  
719 and negative feedback, we built another model with two learning rates, one for positive feedback  
720 and the other for negative feedback (33). This model (RW2) can be defined as:

721

722

723 
$$v_t = v_{t-1} + \alpha^{pos} \times (R_{t-1} - v_{t-1}), \text{positive feedback}$$

724 
$$v_t = v_{t-1} + \alpha^{neg} \times (R_{t-1} - v_{t-1}), \text{negative feedback}$$

725

726 Where  $v_t$  is the value of the option on trial  $t$ .  $\alpha^{pos}$  and  $\alpha^{neg}$  represent the learning rates from  
727 positive and negative feedback, respectively.

728 For these two models,  $R_{t-1} \in \{0,1\}$  represents the feedback received in response to participants'  
729 choice on trial  $t-1$ . And  $R_{t-1} - v_{t-1}$  represents prediction error in trial  $t-1$ .

730

731

732 We used a softmax choice function to map the value into choice. The softmax function for these  
733 four models can be defined as:

734

735

$$P^t = \frac{\exp(\beta V_{t,t})}{\exp(\beta V_{t,1} + \beta V_{t,2} + \beta V_{t,3})}$$

736

737 Where the  $\beta$  represents the inverse temperature with choice value.

738

739 ***Model fitting and comparison***

740 Hierarchical Bayesian inference (HBI) is a powerful method for model fitting and comparison in  
741 group studies (34). Unlike traditional approaches such as maximum likelihood estimation (MLE)  
742 or maximum a posteriori (MAP) estimation, which fit models to each subject independently, HBI  
743 simultaneously fits models to all subjects while constraining individual fits based on group-level  
744 statistics (i.e., empirical priors). This approach yields more robust and reliable parameter  
745 estimates, particularly when individual subject data is noisy or limited.

746 In our study, we employed HBI to fit models to choice data. The method quantifies group-level  
747 mean parameters and their corresponding hierarchical errors. To ensure that parameter estimates  
748 remain within appropriate bounds during the fitting process, we used the sigmoid function to  
749 transform parameters bounded in the unit range or with an upper bound and the exponential  
750 function to transform parameters bounded to positive values. The initial parameters of all models

751 were obtained using a MAP procedure, with the initial prior mean and variance for all parameters  
752 set to 0 and 6.25, respectively, based on previous research (27). This initial variance allows  
753 parameters to vary widely without substantial influence from the prior.

754 For model comparison, we used Bayesian model selection, specifically employing the protected  
755 exceedance probability (PXP) to select the winning model. The PXP quantifies the probability  
756 that a given model is more frequent in the population than all other models under consideration  
757 while accounting for the possibility that the observed differences in model evidence may be due  
758 to chance (60). The model with the highest PXP is selected as the winning model. This approach  
759 inherently penalizes model complexity, favoring models that balance goodness-of-fit and  
760 parsimony. Model performance (log-likelihood) can be found in [SI Section 8, Table 6](#).

761

762 ***Turning point to divide the manifold into monotonically increasing and decreasing group***

763 To divide the manifold into monotonically increasing and decreasing groups, we sorted the  
764 scores for dimension 1 in ascending order. Initially, we fitted a linear model using the first three  
765 data points located on the upper left of the manifold. We then expanded this model by  
766 sequentially including one additional data point from dimension 1, continuing this process until  
767 we incorporated the last score (i.e., the maximum dimension 1 score, situated on the upper right  
768 of the manifold). Throughout this procedure, we monitored the t-statistic of the dimension1  
769 coefficient to assess the statistical significance of dimension1 as a predictor. Notably, a  
770 dimension 1 score of -0.671 marked the most significant negative coefficient, after which the  
771 relationship between dimension 1 and dimension2 gradually shifted to become positive (see [SI](#)  
772 [Section 9, Figure S5](#))

773

774 ***False discovery rate correction***

775 We adopted FDR (False Discovery Rate) correction, which was introduced by Benjamini and

776 Hochberg (61) to control the expected proportion of false positives (Type I errors).

777

778

779

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789

790

791 **Code and data availability.**

792 The source scripts used to do data analysis are published at  
793 [https://github.com/hermandarrowlab/uncertainty\\_apathy\\_anxiety](https://github.com/hermandarrowlab/uncertainty_apathy_anxiety)  
794 Data is available upon request.

795

796 **Reference**

- 797 1. A. Soltani, A. Izquierdo, Adaptive learning under expected and unexpected uncertainty. *Nat. Rev. Neurosci.* **20**, 635–644 (2019).
- 799 2. P. Piray, N. D. Daw, A model for learning based on the joint estimation of stochasticity and 800 volatility. *Nat. Commun.* **12**, 6587 (2021).
- 801 3. E. Pulcu, M. Browning, The Misestimation of Uncertainty in Affective Disorders. *Trends 802 Cogn. Sci.* **23**, 865–875 (2019).
- 803 4. M. Husain, J. P. Roiser, Neuroscience of apathy and anhedonia: a transdiagnostic approach. 804 *Nat. Rev. Neurosci.* **19**, 470–484 (2018).
- 805 5. R. S. Marin, Apathy: Concept, Syndrome, Neural Mechanisms, and Treatment. *Semin. Clin. 806 Neuropsychiatry* **1**, 304–314 (1996).
- 807 6. F. H. Hezemans, N. Wolpe, J. B. Rowe, Apathy is associated with reduced precision of prior 808 beliefs about action outcomes. *J. Exp. Psychol. Gen.* **149**, 1767–1777 (2020).
- 809 7. J. Scholl, H. A. Trier, M. F. S. Rushworth, N. Kolling, The effect of apathy and 810 compulsion on planning and stopping in sequential decision-making. *PLoS Biol.* **20**, 811 e3001566 (2022).
- 812 8. Q. J. M. Huys, P. Dayan, A Bayesian formulation of behavioral control. *Cognition* **113**, 813 314–328 (2009).
- 814 9. M. Browning, T. E. Behrens, G. Jocham, J. X. O'Reilly, S. J. Bishop, Anxious individuals 815 have difficulty learning the causal statistics of aversive environments. *Nat. Neurosci.* **18**, 816 590–596 (2015).
- 817 10. K. Uhr, M. J. Dugas, The role of fear of anxiety and intolerance of uncertainty in worry: an 818 experimental manipulation. *Behav Res Ther* **47**, 215–223 (2009).
- 819 11. C. Gagne, O. Zika, P. Dayan, S. J. Bishop, Impaired adaptation of learning to contingency 820 volatility in internalizing psychopathology. *Elife* **9**, e61387 (2020).
- 821 12. J. B. Hirsh, R. A. Mar, J. B. Peterson, Psychological entropy: a framework for 822 understanding uncertainty-related anxiety. *Psychol. Rev.* **119**, 304–320 (2012).
- 823 13. K. C. Aberg, I. Toren, R. Paz, A neural and behavioral trade-off between value and 824 uncertainty underlies exploratory decisions in normative anxiety. *Mol. Psychiatry* **27**, 1573– 825 1587 (03/2022).
- 826 14. K. Witte, T. Wise, Q. J. Huys, E. Schulz, Exploring the Unexplored: Worry as a Catalyst for 827 Exploratory Behavior in Anxiety and Depression. (2024).
- 828 15. H. Fan, S. J. Gershman, E. A. Phelps, Trait somatic anxiety is associated with reduced 829 directed exploration and underestimation of uncertainty. *Nat Hum Behav* 1–12 (2022).

830 16. R. Smith, *et al.*, Lower Levels of Directed Exploration and Reflective Thinking Are  
831 Associated With Greater Anxiety and Depression. *Front. Psychiatry* **12** (2022).

832 17. V. A. Holthoff, *et al.*, Regional cerebral metabolism in early Alzheimer's disease with  
833 clinically significant apathy or depression. *Biol. Psychiatry* **57**, 412–421 (2005).

834 18. M.-C. Wen, L. L. Chan, L. C. S. Tan, E. K. Tan, Depression, anxiety, and apathy in  
835 Parkinson's disease: insights from neuroimaging studies. *Eur. J. Neurol.* **23**, 1001–1019  
836 (2016).

837 19. D. C. Steffens, M. Fahed, K. J. Manning, L. Wang, The neurobiology of apathy in  
838 depression and neurocognitive impairment in older adults: a review of epidemiological,  
839 clinical, neuropsychological and biological research. *Transl. Psychiatry* **12**, 1–16 (2022).

840 20. R. Dan, *et al.*, Separate neural representations of depression, anxiety and apathy in  
841 Parkinson's disease. *Sci. Rep.* **7**, 12164 (2017).

842 21. S. Tinaz, *et al.*, Distinct neural circuits are associated with subclinical neuropsychiatric  
843 symptoms in Parkinson's disease. *J. Neurol. Sci.* **423**, 117365 (2021).

844 22. C. S. Oosterwijk, C. Vriend, H. W. Berendse, Y. D. van der Werf, O. A. van den Heuvel,  
845 Anxiety in Parkinson's disease is associated with reduced structural covariance of the  
846 striatum. *J. Affect. Disord.* **240**, 113–120 (2018).

847 23. M. E. P. Seligman, Helplessness: On depression, development, and death. *A series of books  
848 in psychology*. **250** (1975).

849 24. C. S. Chen, E. Knep, A. Han, R. B. Ebitz, N. M. Grissom, Sex differences in learning from  
850 exploration. *Elife* **10**, e69748 (2021).

851 25. R. B. Ebitz, E. Albaran, T. Moore, Exploration Disrupts Choice-Predictive Signals and  
852 Alters Dynamics in Prefrontal Cortex. *Neuron* **97**, 450–461.e9 (01/2018).

853 26. E. A. Kaske, *et al.*, Prolonged Physiological Stress Is Associated With a Lower Rate of  
854 Exploratory Learning That Is Compounded by Depression. *Biol Psychiatry Cogn Neurosci  
855 Neuroimaging* (2022). <https://doi.org/10.1016/j.bpsc.2022.12.004>.

856 27. P. Piray, N. D. Daw, A simple model for learning in volatile environments. *PLoS Comput.  
857 Biol.* **16**, e1007963 (2020).

858 28. A. N. Hampton, P. Bossaerts, J. P. O'Doherty, The role of the ventromedial prefrontal  
859 cortex in abstract state-based inference during decision making in humans. *J. Neurosci.* **26**,  
860 8360–8367 (2006).

861 29. F. Schlagenhauf, *et al.*, Striatal dysfunction during reversal learning in unmedicated  
862 schizophrenia patients. *Neuroimage* **89**, 171–180 (2014).

863 30. S. Cheng, *et al.*, Uncertainty-aware and multigranularity consistent constrained model for  
864 semi-supervised hashing. *IEEE Trans. Circuits Syst. Video Technol.* **32**, 6914–6926 (2022).

865 31. P. Dayan, S. Kakade, P. R. Montague, Learning and selective attention. *Nat. Neurosci.* **3**  
866 *Suppl*, 1218–1223 (2000).

867 32. D. Saffron, *The Rescorla - Wagner Interpretation of Blocking and Overshadowing in*  
868 *Pavlovian Conditioning* (University of Sydney, 1979).

869 33. H. E. M. den Ouden, *et al.*, Dissociable effects of dopamine and serotonin on reversal  
870 learning. *Neuron* **80**, 1572 (2013).

871 34. P. Piray, A. Dezfouli, T. Heskes, M. J. Frank, N. D. Daw, Hierarchical Bayesian inference  
872 for concurrent model fitting and comparison for group studies. *PLoS Comput. Biol.* **15**,  
873 e1007043 (2019).

874 35. Y.-S. Ang, P. Lockwood, M. A. J. Apps, K. Muhammed, M. Husain, Distinct Subtypes of  
875 Apathy Revealed by the Apathy Motivation Index. *PLoS One* **12**, e0169938 (2017).

876 36. B. Löwe, *et al.*, Validation and standardization of the Generalized Anxiety Disorder  
877 Screener (GAD-7) in the general population. *Med. Care* **46**, 266–274 (2008).

878 37. L. McInnes, J. Healy, N. Saul, L. Großberger, UMAP: Uniform Manifold Approximation  
879 and Projection. *Journal of Open Source Software* **3**, 861 (2018).

880 38. J. Aylward, *et al.*, Altered learning under uncertainty in unmedicated mood and anxiety  
881 disorders. *Nat Hum Behav* **3**, 1116–1123 (2019).

882 39. D. W. Grupe, J. B. Nitschke, Uncertainty and anticipation in anxiety: an integrated  
883 neurobiological and psychological perspective. *Nat. Rev. Neurosci.* **14**, 488–501 (2013).

884 40. M. Fahed, D. C. Steffens, Apathy: Neurobiology, assessment and treatment. *Clin.  
885 Psychopharmacol. Neurosci.* **19**, 181–189 (2021).

886 41. J. Pagonabarraga, J. Kulisevsky, A. P. Strafella, P. Krack, Apathy in Parkinson’s disease:  
887 clinical features, neural substrates, diagnosis, and treatment. *Lancet Neurol.* **14**, 518–531  
888 (2015).

889 42. M. Pessiglione, F. Vinckier, S. Bouret, J. Daunizeau, R. Le Bouc, Why not try harder?  
890 Computational approach to motivation deficits in neuro-psychiatric diseases. *Brain* **141**,  
891 629–650 (2018).

892 43. J. S. Beck, *Cognitive behavior therapy: Basics and beyond* (Guilford Press, 2011).

893 44. M. G. Craske, J. L. Mystkowski, “Exposure therapy and extinction: Clinical studies” in *Fear  
894 and Learning: From Basic Processes to Clinical Implications*, (American Psychological  
895 Association, 2007), pp. 217–233.

896 45. G. S. Alexopoulos, P. Arean, A model for streamlining psychotherapy in the RDoC era: the  
897 example of “Engage.” *Mol. Psychiatry* **19**, 14–19 (2014).

898 46. B. N. Cuthbert, T. R. Insel, Toward the future of psychiatric diagnosis: the seven pillars of  
899 RDoC. *BMC Med.* **11**, 126 (2013).

900 47. D. C. Funder, D. J. Ozer, Evaluating effect size in psychological research: Sense and  
901 nonsense. *Adv. Methods Pract. Psychol. Sci.* **2**, 156–168 (2019).

902 48. K. Kroenke, R. L. Spitzer, J. B. W. Williams, The PHQ-9. *J. Gen. Intern. Med.* **16**, 606–613  
903 (2001).

904 49. R. P. Snaith, *et al.*, A scale for the assessment of hedonic tone the Snaith-Hamilton Pleasure  
905 Scale. *Br. J. Psychiatry* **167**, 99–103 (1995).

906 50. G. E. Hinton, S. Roweis, Stochastic neighbor embedding. *Adv. Neural Inf. Process. Syst.* **15**  
907 (2002).

908 51. I. T. Jolliffe, J. Cadima, Principal component analysis: a review and recent developments.  
909 *Philos. Trans. A Math. Phys. Eng. Sci.* **374**, 20150202 (2016).

910 52. H. I. Rhys, *Machine Learning with R, the tidyverse, and mlr* (Simon and Schuster, 2020).

911 53. A. Bari, *et al.*, Serotonin modulates sensitivity to reward and negative feedback in a  
912 probabilistic reversal learning task in rats. *Neuropsychopharmacology* **35**, 1290–1301  
913 (2010).

914 54. A. F. Hayes, *Introduction to mediation, moderation, and conditional process analysis: a  
915 regression-based approach.* xvii (Guilford Press, 2017).

916 55. D. P. MacKinnon, C. M. Lockwood, J. Williams, Confidence Limits for the Indirect Effect:  
917 Distribution of the Product and Resampling Methods. *Multivariate Behav. Res.* **39**, 99  
918 (2004).

919 56. K. J. Preacher, A. F. Hayes, Asymptotic and resampling strategies for assessing and  
920 comparing indirect effects in multiple mediator models. *Behav. Res. Methods* **40**, 879–891  
921 (2008).

922 57. J. P. Coelho, T. M. Pinho, J. Boaventura-Cunha, *Hidden Markov Models: Theory and  
923 Implementation using Matlab®* (CRC Press, 2019).

924 58. K. Chakroun, D. Mathar, A. Wiehler, F. Ganzer, J. Peters, Dopaminergic modulation of the  
925 exploration/exploitation trade-off in human decision-making. *Elife* **9** (2020).

926 59. B. U. Forstmann, R. Ratcliff, E.-J. Wagenmakers, Sequential sampling models in cognitive  
927 neuroscience: Advantages, applications, and extensions. *Annu. Rev. Psychol.* **67**, 641–666  
928 (2016).

929 60. L. Rigoux, K. E. Stephan, K. J. Friston, J. Daunizeau, Bayesian model selection for group  
930 studies — Revisited. *Neuroimage* **84**, 971–985 (2014).

931 61. Y. Benjamini, Y. Hochberg, Controlling the false discovery rate: A practical and powerful  
932 approach to multiple testing. *J. R. Stat. Soc.* **57**, 289–300 (1995).