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2     High-resolution genomic ancestry reveals mobility in early medieval Europe  
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15  
16     Abstract

17     Ancient DNA has unlocked new genetic histories and shed light on archaeological and historical  
18     questions, but many known and unknown historical events have remained below detection thresholds  
19     because subtle ancestry changes are challenging to reconstruct. Methods based on sharing of  
20     haplotypes<sup>1,2</sup> and rare variants<sup>3,4</sup> can improve power, but are not explicitly temporal and have not  
21     been adopted in unbiased ancestry models. Here, we develop *Twigstats*, a new approach of time-  
22     stratified ancestry analysis that can improve statistical power by an order of magnitude by focusing on  
23     coalescences in recent times, while remaining unbiased by population-specific drift. We apply this  
24     framework to 1,151 available ancient genomes, focussing on northern and central Europe in the  
25     historical period, and show that it allows modelling of individual-level ancestry using preceding  
26     genomes and provides previously unavailable resolution to detect broader ancestry transformations.  
27     In the first half of the first millennium ~1-500 CE (Common Era), we observe an expansion of  
28     Scandinavian-related ancestry across western, central, and southern Europe. However, in the second  
29     half of the millennium ~500-1000 CE, ancestry patterns suggest the regional disappearance or  
30     substantial admixture of these ancestries in multiple regions. Within Scandinavia itself, we document  
31     a major ancestry influx by ~800 CE, when a large proportion of Viking Age individuals carried ancestry  
32     from groups related to continental Europe. This primarily affected southern Scandinavia, and was  
33     differentially represented in the western and eastern directions of the wider Viking world. We infer  
34     detailed ancestry portraits integrated with historical, archaeological, and stable isotope evidence,  
35     documenting mobility at an individual level. Overall, our results are consistent with substantial mobility  
36     in Europe in the early historical period, and suggest that time-stratified ancestry analysis can provide  
37     a new lens for genetic history.  
38

## 39 Introduction

40 Ancient genome sequencing has revolutionised our ability to reconstruct expansions, migrations and  
41 admixture events in the ancient past and understand their impact on human genetic variation today.  
42 However, tracing history using ancestry has remained challenging, particularly in (proto-)historical  
43 periods where the richest comparative information from history and archaeology often exists. This is  
44 because ancestries in many geographic regions are often so similar as to be statistically  
45 indistinguishable. One example is northern and central Europe since the start of the Iron Age c.500  
46 BCE, where many longstanding questions remain, such as the nature of large-scale patterns of  
47 human migration during the 4th-6th centuries CE, their impact on the Mediterranean world, and later  
48 patterns of human mobility during the Viking Age (c. 750-1050 CE).

49

50 Reconstructing genetic histories from ancient DNA (aDNA) data commonly utilises so-called *f*-  
51 statistics<sup>5-9</sup>. Their popularity is rooted in a number of favourable properties, such as allowing analyses  
52 of lower-quality aDNA data, relative robustness to ascertainment, and theoretical guarantees of  
53 unbiasedness including in the presence of population bottlenecks<sup>7,10</sup>. *F*-statistics-derived approaches,  
54 such as *qpAdm*<sup>8</sup>, are close to unique in enabling the unbiased fitting of admixture events involving  
55 multiple source groups, including identifying the number of such events and choosing the best fitting  
56 sources<sup>8,10,11</sup>. However, *f*-statistics have not always had sufficient power to reconstruct events  
57 involving closely related ancestries, despite increasing sample sizes<sup>12,13</sup>. While the pairwise genetic  
58 differentiation ( $F_{ST}$ ) between the commonly studied hunter-gatherer, early farmer, and steppe-  
59 pastoralist groups that shaped the ancestry of Stone- and Bronze Age Europe<sup>8,11,14,15</sup> is between 5%  
60 and 9%<sup>8,16</sup>, the differentiation between Iron Age groups in central and northern Europe is an order of  
61 magnitude lower at  $F_{ST}=0.1$ -0.7% (Supplementary Figure 1). Methods that identify haplotypes, or  
62 shared segments of DNA that are not broken down by recombination, have previously been shown to  
63 have more power than single-SNP markers, but this information has not been accessible in  
64 combination with the advantages of *f*-statistics<sup>2,13,17,18</sup>. Furthermore, the overwhelming majority of  
65 available ancient DNA is from capture of 1.2 million SNPs<sup>19</sup> and no clear advantages have been  
66 demonstrated for analysis of the >50 million SNPs available with whole-genome shotgun data as of  
67 yet.

68

69 One class of methods that use haplotype information is full genealogical tree inference, which can  
70 now readily be applied to many thousands of modern and ancient whole genomes<sup>20-25</sup>. These have  
71 been successfully applied to boost the detection of positive selection<sup>22,26-28</sup>, population  
72 structure<sup>21,23,25,29</sup>, infer geographic locations of ancestors<sup>24,30</sup>, demography<sup>21,22</sup>, and mutation rate  
73 changes<sup>21</sup>, among others. Genealogical trees can be thought of as containing essentially full, time-  
74 resolved information about ancestry, including information typically captured by recent haplotype  
75 sharing or identity-by-descent. In contrast, rare variant ascertainment, haplotypes, or chromosome  
76 blocks can be thought of as subsets or summaries of the information available in genealogies.

77

78 Here, we propose a new approach which we refer to as 'time-stratified ancestry analysis' to boost the  
79 statistical power of *f*-statistics several-fold by utilising inferred genome-wide genealogies (Figure 1a).  
80 We apply our method to the genetic history of northern and central Europe from c.500 BCE-1000 CE,  
81 from the start of the Iron Age to the Viking Age, using 1151 previously published whole-genome  
82 shotgun sequences (Supplementary Figure 1). We construct a fine-scale map of relationships  
83 between individuals and groups to understand ancestry shifts and expansions, for example of  
84 Germanic- and Slavic- speakers, and mobility in the Viking world.

## 85 Results

### 86 Genealogy-informed ancestry modelling improves power in simulations

87 *F*-statistics, by definition, count the occurrence of local genealogical relationships that are implied by  
88 how mutations are shared across individuals<sup>31</sup>. New genealogy inference methods trace common  
89 ancestors back in time beyond what is implied by individual mutations by utilising linkage information  
90 across genomic loci. By dating inferred coalescence events, genealogies add a time dimension onto  
91 genetic variation data; in particular, they enable, in principle, the best attainable age estimate of  
92 mutations from genetic variation<sup>22,32</sup>. This inherent relationship between *f*-statistics and local  
93 genealogies makes it straightforward to compute *f*-statistics directly on inferred genealogies<sup>33</sup>. Instead  
94 of computing *f*-statistics on observed mutations, they are now calculated on the inferred branches of  
95 genealogies, some of which may not be directly tagged by mutations but are inferred through  
96 resolving the local haplotype structure (**Methods**).

97

98 We develop mathematical theory and simulate a simple admixture model, in which the ancestry  
99 proportion is constrained in a single ratio of two *f*<sub>4</sub>-statistics<sup>5</sup>, to test this approach (Figure 1b,  
100 Supplementary Information). While unbiased, we find that using *f*-statistics computed on genealogies  
101 by itself does not yet yield a large improvement in statistical power for quantifying admixture events.  
102 However, we show, through theoretical prediction and simulation, that large improvements in power  
103 can be gained without bias by focusing on recent coalescences, which are most informative on recent  
104 admixture events (Supplementary Figure 3). Coalescences older than the time of divergence of the  
105 sources carry no information with respect to the admixture event and only add noise to the *f*-statistics.  
106 Excluding these therefore increases statistical power, while introducing no bias, in principle.

107

108 We implement this idea of studying the 'twigs' of gene trees in a new tool, *Twigstats* (Figure 1a,  
109 **Methods**), which we demonstrate in simulations reduces standard errors by up to 10-fold and  
110 potentially more, depending on sample sizes and details of the genetic history model. The approach  
111 does not produce detectable bias in estimates of admixture proportions (Figure 1b,c,d,  
112 Supplementary Figure 3). Additionally, we demonstrate that computing *f*-statistics on mutation age  
113 ascertained genotypes produces a close to equal power gain to the use of full genealogies in many  
114 examples, while adding flexibility by allowing lower-quality genomes to be grafted onto a genealogy  
115 reconstructed with higher-quality genomes<sup>21</sup>.

116

117 Previous studies have suggested ascertaining rare mutations as a proxy for recent history<sup>3,4</sup>, but we  
118 show that this approach is prone to bias when effective population sizes vary, and that using full time-  
119 restricted genealogies is both unbiased and more powerful (Figure 1b, Supplementary Figure 3). We  
120 attribute this to the observation that mutation age is not always highly predictive of allele frequency  
121 (Supplementary Figure 2) and the genealogy-based approach gains power from the inclusion also of  
122 higher frequency young mutations that tag recent coalescences. We also demonstrate that a widely-  
123 used chromosome painting approach, where groups are modelled using a non-negative least squares  
124 of genome-wide painting profiles<sup>2</sup>, is also prone to bias, when source groups have undergone strong  
125 drift since the admixture event (Figure 1b, Supplementary Figure 3).

### 126 Three empirical examples of applying *Twigstats* to study fine-scale ancestry

127 We next tested the *Twigstats* approach on a range of empirical examples. First, we used our time-  
128 restricted genealogy approach to boost pairwise outgroup *f*<sub>3</sub>-statistics<sup>34</sup> to quantify fine-scale

129 population structure, which we demonstrated using a previously proposed simulation<sup>29</sup>  
130 (Supplementary Figure 4a). When applied to published genomes from Neolithic Europe, more than  
131 4,500 years old, we were able to replicate previously suggested fine-scale structure between  
132 individuals buried in megalithic structures in Ireland compared to others<sup>35</sup>, which was apparent with  
133 time-restricted genealogies, but not with SNP data alone (Figure 2a).

134

135 Next, we applied the *Twigstats* approach to the well-studied example of three major ancestries  
136 contributing to prehistoric Europe: Mesolithic hunter-gatherers, early farmers, and steppe  
137 populations<sup>8,11,14,15</sup>. We obtain unbiased estimates and a ~20% improvement in standard errors in an  
138 already well-powered *qpAdm* model for estimating these ancestries<sup>36</sup> (Supplementary Figure 4c) and  
139 a remarkable power gain in distinguishing ancestries in Iron Age Northern Europe (Figure 3), mirroring  
140 our observation in simulations and theoretical prediction that the boost is most effective if differences  
141 between source groups are subtle (Supplementary Figure 3). For example, in models of admixture of  
142 British Iron Age and continental northern European ancestries in early medieval England<sup>37</sup> (see  
143 below; Figure 3), *Twigstats* time-stratification halves standard errors from 8.0% with SNPs to 3.7%  
144 when using time-stratification (point estimates 65% and 73% Iron Age Britain-related ancestry,  
145 respectively)

146

147 Finally, we demonstrate that *Twigstats* can be used to resolve competing models of punctual  
148 admixture and long-standing gene flow, or constrain the time of admixture. For instance, it has  
149 previously been suggested that long-standing deep structure and gene flow between Neanderthals  
150 and early modern humans may produce patterns resembling a punctual admixture event some 60  
151 thousand years ago<sup>38–40</sup>, and that some commonly used population genetic methods cannot  
152 distinguish between them, casting doubt on the model of Neanderthal admixture. However, while  
153 long-standing deep substructure in Africa does confound SNP-based *f*-statistics to produce patterns  
154 similar to Neanderthal admixture, we demonstrate, in simulations, that *Twigstats* can clearly  
155 distinguish this history from recent admixture (Figure 2b, Supplementary Figure 4b). Application of  
156 *Twigstats* on empirical whole genomes produces results inconsistent with deep substructure alone,  
157 but consistent with Neanderthal admixture into ancestors of Eurasians<sup>40–42</sup>.

## 158 **A framework for high resolution ancestry modelling in Metal Age and Medieval** 159 **Northern Europe**

160 Roman historians write extensively about the geographic distribution and extensive movements of  
161 groups and tribes immediately beyond the imperial frontier. The fall of the western Roman Empire has  
162 long been argued to have been both facilitated and in part caused by such population movements  
163 during the ‘Migration Period’. However, the exact nature and scale of these historically attested  
164 demographic phenomena—and their genetic impact—have been questioned due to uncertain  
165 historical sources and have been difficult to test with genetic approaches due to the close relations  
166 shared between many groups that were ostensibly involved. Less is understood at further distances  
167 from the Roman frontier due to lack of historical accounts.

168

169 Several recent studies have documented substantial mobility and genetic diversity in these time  
170 periods, suggesting stable population structure despite high mobility<sup>43</sup>, and documenting genetic  
171 variation in Viking Age Scandinavia<sup>13,44,45</sup>, early medieval England<sup>3,37</sup>, early medieval Hungary<sup>46,47</sup>,  
172 and Iron Age and medieval Poland<sup>48</sup>, but largely had to resort to using high-sample size modern  
173 cohorts to build models of ancestry change through time and space. Modern populations provide  
174 ample power to detect differences, but their genetic affinity to ancient individuals may be confounded

175 by later gene flow, *i.e.* after the time of the ancient individual(s)<sup>49</sup>. The most principled approach is  
176 thus to build ancestry models where source and 'outgroup/reference' populations are older than, or at  
177 least contemporary with, the target genome or group which we are trying to model<sup>49</sup>. The improved  
178 statistical power of time-restricted ancestry in *Twigstats* thus offers an opportunity to develop  
179 principled ancestry models based solely on temporally appropriate source proxy groups.  
180

181 To develop an ancestry model with sources from the Early Iron Age, we used hierarchical UPGMA  
182 clustering based on pairwise clade testing between all individuals, and formally tested the cladality of  
183 proposed ancestry groups with *qpWave* tests<sup>43</sup> (**Methods**). This resulted in a set of model ancestry  
184 sources that included Iron Age and Roman Britain, the Iron Age of central European regions of  
185 Germany, Austria, and France, Roman Portugal, Roman Italy, Iron Age Lithuania, the Early Iron Age  
186 Scandinavian Peninsula (Sweden and Norway), as well as Bronze- and Iron Age Eastern and  
187 Southern Europe (Figure 3a,b, Supplementary Figure 1). Our source groups capture regional fine-  
188 scale genetic structure, such as separation of predominantly Norwegian and northern Swedish Early  
189 Iron Age individuals from southern Peninsular Scandinavia (Figure 3a), that is not detected without  
190 *Twigstats*. We employ a rotational *qpAdm* approach to narrow down the set of contributing sources  
191 from a larger pool of putative sources<sup>50</sup>. In addition, we made qualitative observations on results from  
192 non-parametric multi-dimensional scaling (MDS) on 'outgroup- $f_3$ ' statistics<sup>34</sup> (Supplementary Table 2).

### 193 **Expansion of ancestry related to Early Iron Age Scandinavia before and during the 194 Migration Period**

195 We assembled time transects using available ancient DNA data across several geographic regions in  
196 Europe, and inferred their ancestry using a model with Early Iron or Roman Age sources. Our  
197 modelling provides direct evidence of individuals with ancestry originating in northern Germany or  
198 Scandinavia appearing in these regions as early as the first century CE (Figure 3b, Supplementary  
199 Table 3).  
200

201 In the region of present-day Poland, our analysis suggests several clear shifts in ancestry. First, in the  
202 Middle to Late Bronze Age (1500 BC - 1000 BC), we observe a clear shift away from preceding  
203 ancestry related to Corded Ware cultures<sup>51</sup> ~500CE. Second, in the 1st to 5th century CE, individuals  
204 associated with Wielbark culture<sup>43,48</sup> represent an additional drastic qualitative shift away from the  
205 preceding Bronze Age groups, and can only be modelled with a >75% component attributed to the  
206 Early Iron Age (EIA) Scandinavian Peninsula, with multiple individuals at ~100% and a stronger  
207 affinity in earlier Wielbark individuals. The Wielbark archaeological complex has been associated with  
208 the Goths, a Germanic-speaking group, but this attribution has remained unclear. Our modelling  
209 supports the idea that some early Germanic-speaking groups expanded into the area between the  
210 Oder and Vistula rivers, but since a considerable proportion of burials during this period were  
211 cremations, the possible presence of individuals with other ancestries can not be strictly rejected if  
212 they were exclusively cremated (and therefore invisible in the aDNA record).  
213

214 A previous study could not reject continuity in ancestry from the Wielbark-associated individuals to  
215 later medieval individuals<sup>48</sup>. With *Twigstats*' improved power, models of continuity are strongly  
216 rejected, with no 1-source model of any preceding Iron Age or Bronze Age group providing a  
217 reasonable fit ( $p << 1e-33$ ). Instead, individuals from medieval Poland can only be modelled as a  
218 mixture of majority Lithuanian Roman Iron Age ancestry, which is similar to ancestries of individuals  
219 from middle to late Bronze Age Poland, and a minority (95% CI: 18.9%-26.0%) ancestry component  
220 related to individuals from Roman Italy ( $p = 0.015$ ) (Figure 3b). These medieval individuals from

221 Poland thus carry no detectable Scandinavian-related ancestry, unlike the earlier Wielbark-associated  
222 individuals. Instead, present-day people from Poland are similar in ancestry to these medieval  
223 individuals (Figure 3c). The presence of a southern European-like ancestry component (represented  
224 by Roman Italy), which is not present in the Lithuanian Roman Iron Age, could be consistent with  
225 models of admixture taken place further south and arriving in Poland through north-westerly Slavic  
226 expansions.

227

228 In present-day Slovakia, individuals associated with the Iron Age La Tène period appear close to  
229 Hungarian Scythians in the two dimensions of our MDS analysis and are modelled as a mixture of  
230 central and eastern European ancestry. However, a 1<sup>st</sup> century burial of a female aged 50-60 years  
231 from Zohor is modelled only with Scandinavian-related ancestry, corroborating the idea that this  
232 individual was associated with a nearby settlement that has been attributed culturally with Germanic-  
233 speakers<sup>43,52</sup>. Later Migration period individuals only have partial Scandinavian-related ancestry,  
234 suggesting later broader ancestry shifts in the region.

235

236 Nearby, in present-day Hungary, we observe Scandinavian-related ancestry components in several  
237 Longobard burials (Longobard\_EMED(I)) dating to the middle of the 5th century CE<sup>46</sup> (Figure 3b). This  
238 is consistent with the original study, which reported affinity to present-day groups from northwestern  
239 Europe (GBR, CEU, and FIN in the 1000 Genomes Project)<sup>46</sup>, but which we can extend with higher-  
240 resolution using earlier genomes. The Longobards were dominated by Germanic-speakers, and our  
241 result is consistent with attestations that they originated in the area of present-day Northern Germany  
242 or Denmark. In contrast, several other Longobard-associated individuals from the region  
243 (Longobard\_EMED(II)) show ancestry more closely related to continental Europe, putatively  
244 representing local ancestry prior to Langobardic influence. This is consistent with the notion that the  
245 Longobards of the fifth and sixth centuries headed a confederation of several different groups.  
246 Present-day populations of Hungary do not appear to derive their ancestry from early medieval  
247 Longobards, and are instead more similar to Scythian ancestry sources (Supplementary Figure 5),  
248 consistent with the impact of later arrivals of Avars, Magyars and other eastern groups<sup>53</sup>.

249

250 In southern Germany, the genetic ancestry of individuals from early medieval Bavaria likely  
251 associated with the Germanic-speaking *Baiuvari*<sup>54</sup> cannot be modelled as deriving ancestry solely  
252 from earlier groups in Iron Age Germany. Our current best model indicates a mixture with ancestry  
253 derived from EIA Peninsular Scandinavia, suggesting a regional ancestry shift and expansion of  
254 Scandinavian-related ancestry (Figure 3b). A subset of individuals from Iron Age and Roman Austria,  
255 France, and Germany are also best modelled with a minority Scandinavian-derived ancestry  
256 component. This may reflect expansions southwards—towards the Roman frontier—of other  
257 Germanic-speaking populations originating in Northern Europe.

258

259 In southern Britain, the ancestries of Iron Age and Roman individuals form a tight cluster in our MDS  
260 analysis (Figure 3a), shifted relative to available preceding Bronze Age individuals from Ireland and  
261 Orkney, and adjacent to, but distinct from, available individuals in Iron Age and Roman central Europe  
262 (Austria, France and Germany). However, two burials from a Roman military fortress site in Austria  
263 (Klosterneuburg)<sup>43</sup> carry ancestry which is currently indistinguishable from Iron Age/Roman  
264 populations of Britain, to the exclusion of other groups (qpWave cladal p-value = 0.6). At least one  
265 of these skeletons (R10657 - Verf. Fn. 806/10), a 25-35-year old male buried beneath a horse<sup>13</sup>,  
266 shows osteological traits possibly linked to intense equestrianism, hinting that these may be non-local  
267 Roman soldiers. While one option is that they had ancestry from Britain, an alternative is that currently

268 unsampled populations from large areas of western continental Europe carried ancestries similar to  
269 what we see in Iron Age southern Britain.

270  
271 We further identify that an earlier Roman individual (6DT3) dating to ~2nd century CE from the  
272 purported gladiator or military cemetery at Driffield Terrace in York (Roman *Eboracum*), England<sup>55</sup>,  
273 who was previously identified broadly as an ancestry outlier<sup>56</sup>, specifically carried EIA Scandinavian  
274 Peninsula-related ancestry. This documents an earlier presence of Scandinavian-related ancestry in  
275 Britain than in previous studies that suggested substantial influx of individuals carrying 'continental  
276 northern European' (CNE) ancestry associated with 'Anglo-Saxon migrations' from the 5th century  
277 onwards<sup>37</sup>. Roman-period individuals and groups from Northern Europe are indeed recorded in  
278 Roman sources both as soldiers and as slave gladiators condemned to die in Roman arenas<sup>57,58</sup>.

## 279 **Ancestry change in Late Iron Age southern Scandinavia**

280 In Scandinavia, we found evidence for broad homogeneity in the Early Iron Age (<500CE).  
281 Specifically, individuals from Denmark 100CE - 300CE were indistinguishable from contemporary  
282 people in the Scandinavian Peninsula. However, we observe a clear shift in genetic ancestry already  
283 in the 8th century (Late Iron Age/early Viking Age) in Zealand island (present-day Denmark) for which  
284 a 100% Early Iron Age ancestry model is rejected ( $p = 1.2e-11$  using *Twigstats*;  $p = 5e-3$  without).  
285 This shift in ancestry persists among later Viking Age groups in Denmark, where all groups are  
286 modelled with varying proportions of ancestry related to 'continental' Iron Age groups from present-  
287 day Austria, France, or Germany (Figure 4a,b). A non-parametric MDS of Viking Age individuals  
288 suggests that variation between individuals forms a cline spanning from the EIA Scandinavian  
289 Peninsula into continental Europe (Figure 4c). The observation of a shift in ancestry in Denmark could  
290 not be confounded by potentially unknown gene flow into the Iron Age groups in Austria, France, and  
291 Germany used in the model, but such gene flow could affect the exact ancestry proportions (Figure  
292 3b).

293  
294 These patterns are consistent with northwards gene flow into the Jutland peninsula and Zealand  
295 island in present-day Denmark, and expanding towards southern Sweden, potentially starting before  
296 the Viking Age. The timing is only constrained by the samples available, where the ancestry is not yet  
297 observed in the following latest individuals from south to north: individuals from Brøndsager and  
298 Århushave Ødetofter in the Copenhagen area of Denmark dated to ~100-300CE<sup>13</sup>, an individual from  
299 the southern tip of Sweden ~500CE<sup>15</sup>, individuals from the Sandby Borg massacre site on Öland  
300 ~500CE<sup>44</sup>, and a larger number of early Viking Age 8th century individuals from the Salme ship burial  
301 in present-day Estonia who likely originated in central Sweden<sup>13</sup> (Supplementary Figure 8). Most likely  
302 the ancestry transformation thus occurred after those dates in each particular region, and mostly in  
303 the second half of the first millennium CE.

304  
305 Interestingly, in southern Scandinavia, the archaeological record has yielded considerable evidence  
306 for periodic conflict and socio-political stress during the Iron Age, seen most explicitly in the many pre-  
307 Roman and Roman deposits of weapons and human remains in bogs<sup>59</sup>. While the context of these  
308 depositions remains debated and may have been variable, they could potentially relate to conflict  
309 associated with patterns of migration related to these ancestry shifts: a spread of other Germanic-  
310 speakers into the region from the south.

311  
312 To assess the full extent of the impact of this ancestry influx into Scandinavia, we next turned to  
313 understanding the ancestry of individuals in Scandinavia during the Viking Age. Previous studies have

314 suggested diversity of ancestries in Scandinavia in this period<sup>13,44,60</sup>, due to increased maritime  
315 mobility, but have not reported per-individual ancestry estimates based on preceding ancestry. We  
316 analysed each individual's ancestry using a rotational *qpAdm* scheme (Figure 4d, Supplementary  
317 Table 4, Supplementary Figure 8), which showed increased power in distinguishing models when  
318 restricting to recent coalescences with *Twigstats* (>70% of accepted 1 source models in *Twigstats*  
319 were also accepted 1 source models using all SNPs, compared to <25% for the inverse). We were  
320 able to find a uniquely accepted model ( $p > 0.01$ ) for 98 out of 165 individuals from Viking Age  
321 Scandinavia, compared to 70 using all SNPs, despite the fact that more *Twigstats* models had  
322 multiple ancestries (only 64 individuals with a 1 source model compared to 141 when using all SNPs)  
323 and were thus more complex.

324

325 We investigated regional differences in non-local ancestry across Scandinavia. In Denmark, 28 of 54  
326 Viking Age individuals had detectable ( $z > 1$ ) continental-related ancestry (Iron Age Germany, France  
327 or Austria) in their best accepted *qpAdm* models. In Sweden 28 of 74 individuals,, had detectable  
328 continental-related ancestry, concentrated almost entirely in southern regions (Figure 4d). By contrast,  
329 in Norway this ancestry was observed in only two individuals, indicating a wide-ranging impact of  
330 incoming ancestry in southern Scandinavia, and suggesting more continuity from the Early Iron Age in  
331 Norway and northern Sweden (Figure 4d). In more central parts of Scandinavia, the few individuals  
332 that show evidence of 'continental'-related ancestry are observed in regions historically within the  
333 Danish sphere of influence and rule, such as the Oslo fjord. Relatively few such individuals are noted  
334 in eastern Central Sweden, which was a focus of regional power of the Svear (Figure 4d). The  
335 difference in distribution could suggest that the continental ancestry was more common in regions  
336 dominated by the historical Götar and those that lay on the borders of the Danish kingdom.

337

338 To test the extent to which the variation in ancestry was consistent with mobility during the lifetime of  
339 the individuals, or alternatively that of established groups, we focused on the island of Öland in  
340 southeast Sweden, where 23 individuals for which we could reconstruct ancestry portraits also have  
341 extensive associated strontium stable isotope data<sup>61</sup>. Strontium isotope data from dental enamel  
342 reflects the geology of the region where an individual grew to maturity, and there are considerable  
343 differences in expectations between Öland and many other regions in northern Europe. The full range  
344 of strontium isotope ratios in 109 individuals show two modes, a majority group with low ratios and a  
345 second minority group with high ratios falling outside the expected range of local fauna (Figure 4e).  
346 Among 23 individuals with genomes in our data, all 5 individuals with clearly ~100% continental  
347 ancestry (including one with ancestry related to Britain) are part of the majority strontium values,  
348 consistent with them having grown up locally. In contrast, the six most clearly non-local individuals  
349 based on the stable isotopes all have ~50% or more EIA Scandinavian Peninsula-related ancestry,  
350 although five individuals with wholly EIA Scandinavian Peninsula-related ancestry also had local  
351 values. This suggests that the presence of continental ancestry was not a transient phenomenon, but  
352 an ancestry shift occurring at some point after the ~500CE individuals from a massacre site at Sandby  
353 Borg ringfort on Öland, who all have strictly EIA Scandinavian-related ancestry.

### 354 **Origins of Viking Age mobility into Scandinavia**

355 Previous studies had suggested a major influx of ancestry related to Britain into Viking Age  
356 Scandinavia<sup>13,44</sup>. While we detect this ancestry in some individuals (8 individuals in Norway, 12 in  
357 Denmark, 8 in Sweden), including some individuals whose ancestry appears to be entirely derived  
358 from Iron Age Britain, its overall impact appears reduced compared to previous reports. Our analysis  
359 indicates a proportionally larger impact of ancestry from Iron Age Britain in northern Norway, with

360 southern Scandinavia predominantly influenced by continental ancestries (Figure 4f). While the  
361 sample sizes are limited, we observe nominal significance for an overrepresentation of females with  
362 British-related ancestry (Supplementary Figure 6c,d). We hypothesise that our estimates of ancestry  
363 from Britain are reduced relative to previous studies because the phenomenon of continental ancestry  
364 related to Iron Age France, Austria, and Germany may have been indistinguishable from ancestry  
365 from Britain. This could be due to a lack of statistical power to distinguish these closely related  
366 sources with standard methods, as well as through potential biases introduced by using modern  
367 surrogate populations that have since been influenced by later gene flow (such as gene flow into  
368 Britain). We illustrate this by replicating analyses of Refs <sup>13,44</sup> (Supplementary Figure 7).  
369

370 Similarly, a previous study has suggested the presence of southern European ancestry at sites such  
371 as Kärda in southern Sweden<sup>13</sup>. In our models, two Kärda individuals are fit with continental ancestry,  
372 but none of the individuals have a substantial proportion of ancestry related to southern European  
373 sources (represented by Imperial Rome and Portugal in our analysis) (Supplementary Figure 7).  
374 Instead, southern European ancestry is only found in relatively small proportions in any individual in  
375 our models (Figure 4d).  
376

377 Interestingly, we detect ancestry from Bronze and Iron Age sources from Eastern Europe (present-  
378 day Lithuania and Poland), concentrated in south-eastern parts of Sweden, particularly the island of  
379 Gotland (21 individuals, Figure 4d). This is consistent with previous genetic studies<sup>13,44</sup>. We find that  
380 this ancestry is enriched in males (Supplementary Figure 6d), suggesting male-biased mobility and/or  
381 burial. The closest match tends to be Roman Iron Age Lithuanian genomes associated with Balts,  
382 which would be consistent with mobility across the Baltic Sea, but we caution that the geographic  
383 representation of available genomes is still limited.  
384

#### **Viking Age expansion from Scandinavia**

385 Traditionally, historical perspectives on what is now often referred to as the 'Viking diaspora' placed  
386 an emphasis on the movements and settlements of population groups from various parts of  
387 Scandinavia<sup>62</sup>. Here, we use individual-level ancestry resolution to delve into the dynamics of Viking  
388 Age mobility, settlements, and interactions with local populations. When examining individuals in  
389 Viking-related contexts outside of Scandinavia, our explorative MDS analysis again indicates mixed  
390 ancestries related to the Scandinavian EIA, with regional differences that point to varied local  
391 admixture (Figure 4c, Supplementary Figure 9).  
392

393 In Britain, most individuals recovered from the late Viking Age sites of Ridgway Hill, Dorset, and St.  
394 John's College, Oxford<sup>13</sup> show ancestries typical of those seen in Viking Age southern Scandinavia,  
395 suggesting that those executed could have been predominantly migrants or members of Viking raiding  
396 parties from Scandinavia (Figure 4g). In agreement with these genetic ancestry profiles, strontium and  
397 oxygen analyses of the individuals from Ridgway Hill and St. John's College have suggested  
398 childhood origins outside of Britain, and potentially in peninsular Scandinavia, particularly the island of  
399 Öland<sup>63,64</sup>, or parts of northern continental Europe<sup>65</sup>. Notably, VK166 (SK 1891) from St. John's  
400 College is a slight outlier in terms of both genetic ancestry, which is best explained by groups from  
401 Iron Age Austria, France, and Germany and Sarmatian-related populations from Russia, and the  
402 stable isotope analysis, where the oxygen results suggest a more continental origin and the  
403 strontium suggests he spent his childhood on more radiogenic geology.  
404

405 Further west, North Atlantic Viking Age individuals in the Faroe Islands, Iceland and Greenland show  
406 Scandinavian origins with several individuals showing the continental ancestry signal (Figure 4g). We  
407 observe that some individuals interred within pre-Christian burials in Viking Age Iceland share  
408 substantial ancestry with Iron Age Britain, which is consistent with previous studies<sup>45</sup> and historical  
409 records. Previous hypotheses have included female-biased arrival of ancestry related to Britain and  
410 Ireland on Iceland<sup>66</sup>. We tested this but, contrary to this prior hypothesis, we found a marginal  
411 enrichment of ancestry related to Britain/Ireland/continental Europe in males (12 of 17 males and 2 of  
412 7 females with at least one accepted model involving Iron/Roman Age Britain as source; Fisher's  
413 exact test p = 0.085) (Supplementary Figure 6c). However, sampling of additional individuals that will  
414 improve distinction of Anglo-Saxon-related and Norse related-ancestries would be required to fully  
415 test this hypothesis.

416

417 In eastern Europe, we observe similar EIA Scandinavian ancestries in a Viking Age burial from  
418 Ukraine, and these ancestries are overrepresented in Viking Age burials from present-day Russia. At  
419 Staraya Ladoga in western Russia, we observe several individuals with EIA Scandinavian Peninsula-  
420 related ancestry and at least one individual dated to the 11th century with apparent ancestry related to  
421 Iron Age Britain. The relative absence of continental ancestry, which was largely restricted to southern  
422 Scandinavia during the Viking Age, is thus inconclusive but indicative that these individuals originated  
423 in the central/northern parts of Sweden or Norway.

## 424 Conclusions

425 Our new approach, *Twigstats*, transfers the power advantage of haplotype-based approaches to a  
426 fully temporal framework, which is applicable to f-statistics and enables previously unavailable  
427 unbiased and time-stratified analyses of admixture. We demonstrated that *Twigstats* enables fine-  
428 scale quantitative modelling of ancestry proportions, revealing wide-ranging ancestry changes  
429 impacting Northern and Central Europe in the Iron, Roman, and Viking ages. We reveal evidence of  
430 expansion southwards and/or eastwards of likely Germanic speakers carrying Scandinavian-related  
431 ancestry in the first half of the first millennium CE. We note that 'Scandinavian-related' in this context  
432 relates to the ancient genomes available, and so it is entirely possible that these processes were  
433 driven e.g. from regions in northern-central Europe. This could be consistent with the attraction of the  
434 greater wealth, which tended to build up among Rome's immediate neighbours and may have played  
435 a major role in vectors of migration internal to communities in Europe who lived beyond the Roman  
436 frontier<sup>67</sup>. Later, patterns of gene flow seems to have turned northwards, with the spread of  
437 continental-related ancestry in Scandinavia, which is later reflected in differential ancestries in the  
438 western and eastern directions of the Viking diaspora. Overall, our results suggest that whole-genome  
439 sequencing offers additional power over SNP capture through the use of time-restricted ancestry  
440 analysis, and opens up the possibility of the reconstruction of new high-resolution genetic histories  
441 around the world.

## 442 Acknowledgements

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446 (FC001595) from Cancer Research UK, the UK Medical Research Council, and the Wellcome Trust.  
447 B.R. was supported by the Swedish Research Council (grant no. 2021-03333).

448 **Code availability**

449 *Twigstats* is freely available under an MIT licence through github  
450 <https://github.com/leospeidel/twigstats> and detailed documentation, as well as example data, is  
451 available under <https://leospeidel.com/twigstats/>.

452 **Data availability**

453 All ancient DNA data used in this study was publically available and is listed in Supplementary Table  
454 1.

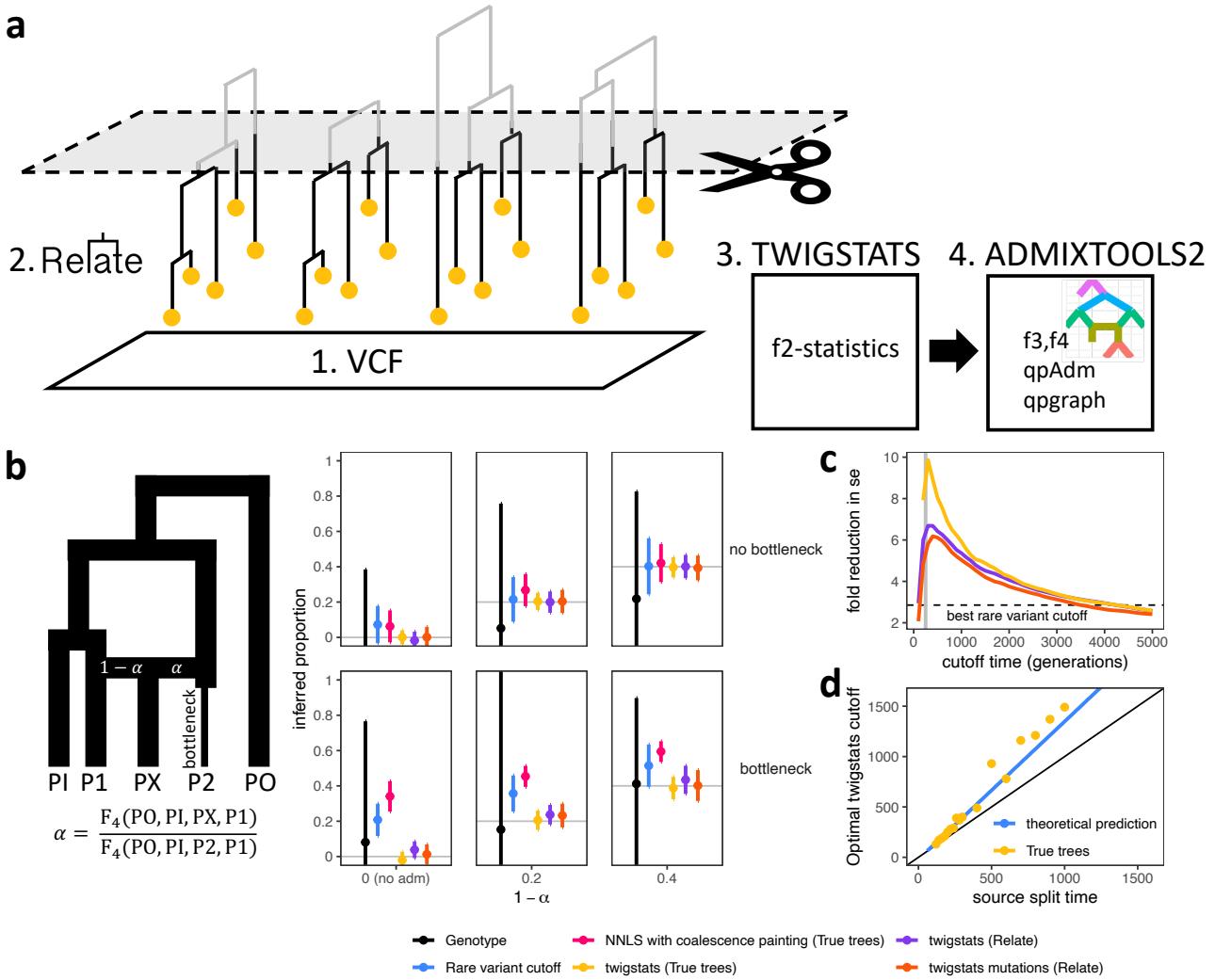
455 **Author contributions**

456 P.S. supervised the study. L.S. and P.S. developed the method, L.S, M.S., and P.S. curated the  
457 dataset, L.S. and P.S. analysed the data, all authors interpreted results and wrote the manuscript.

458 **Competing Interests**

459 The authors declare no competing interests.

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### Figure 1 *Twigstats* performance on simulated data

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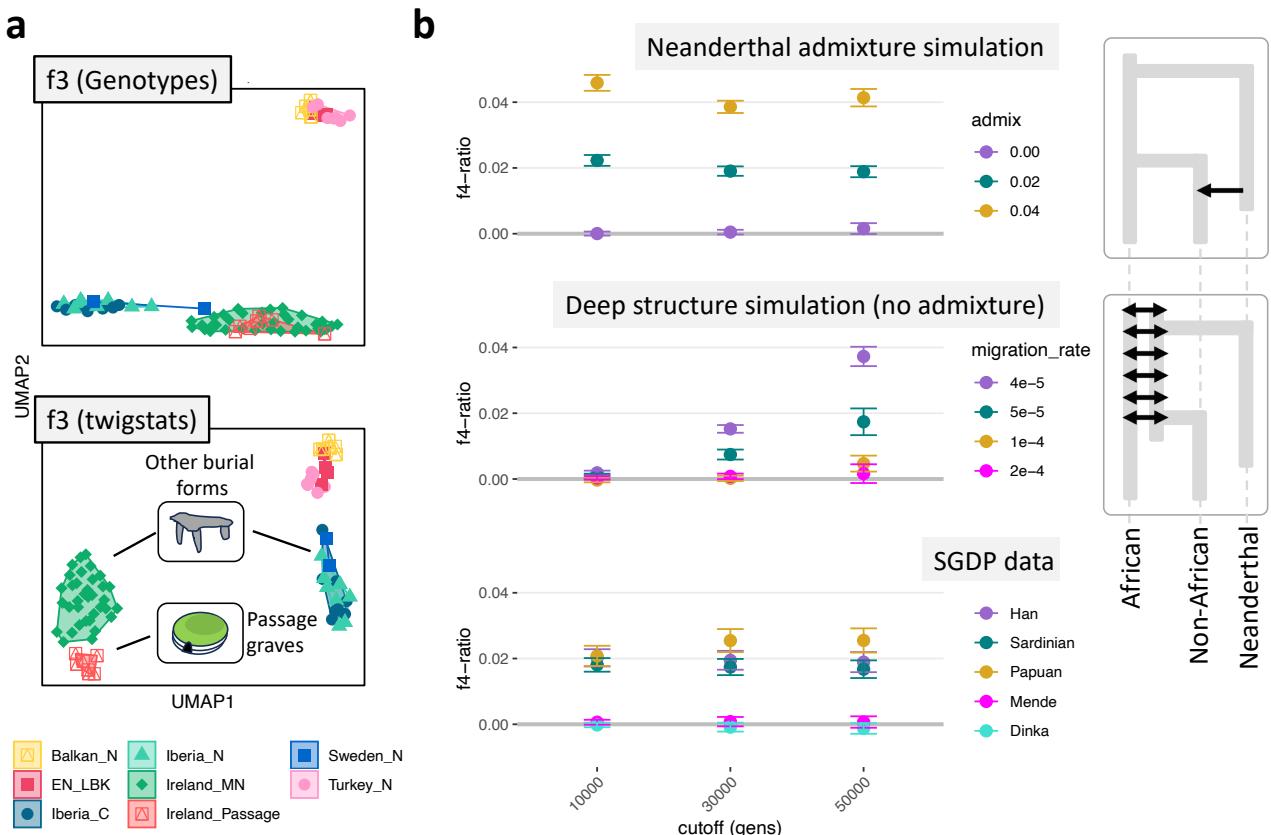
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**a**, Diagram of the *Twigstats* approach. We first construct genealogies from genetic variation data, and then use *Twigstats* to compute  $f_2$ -statistics between pairs of groups to be used by ADMIXTOOLS2. **b**, Admixture proportions inferred from an  $f_4$ -ratio statistic or non-negative least squares. Source groups P1 and P2 split 250 generations ago. Effective population sizes are equal and constant except for a recent bottleneck in P2 (see **Methods** for simulation details). The *Twigstats* cutoff is set to 500 generations, the rare variant cutoff is set to 5%, and we additionally infer admixture proportions by generating ‘first coalescence profiles’ for each population and modelling PX as a mixture of sources P1 and P2 using non-negative least squares (**Methods**). Two standard errors are shown. **c**, Fold improvement of standard errors relative to the genotype case as a function of the *Twigstats* cutoff time, for the same simulation as in b and averaged across different true admixture proportions. Dashed line shows the best standard error when ascertaining genotypes by frequency, when evaluated at different frequency cutoffs. **d**, Optimal *Twigstats* cutoff, defined as the largest reduction in standard errors relative to the genotype case, as a function of source split time in simulations using true trees. Blue line indicates our theoretical prediction (Supplementary Information).



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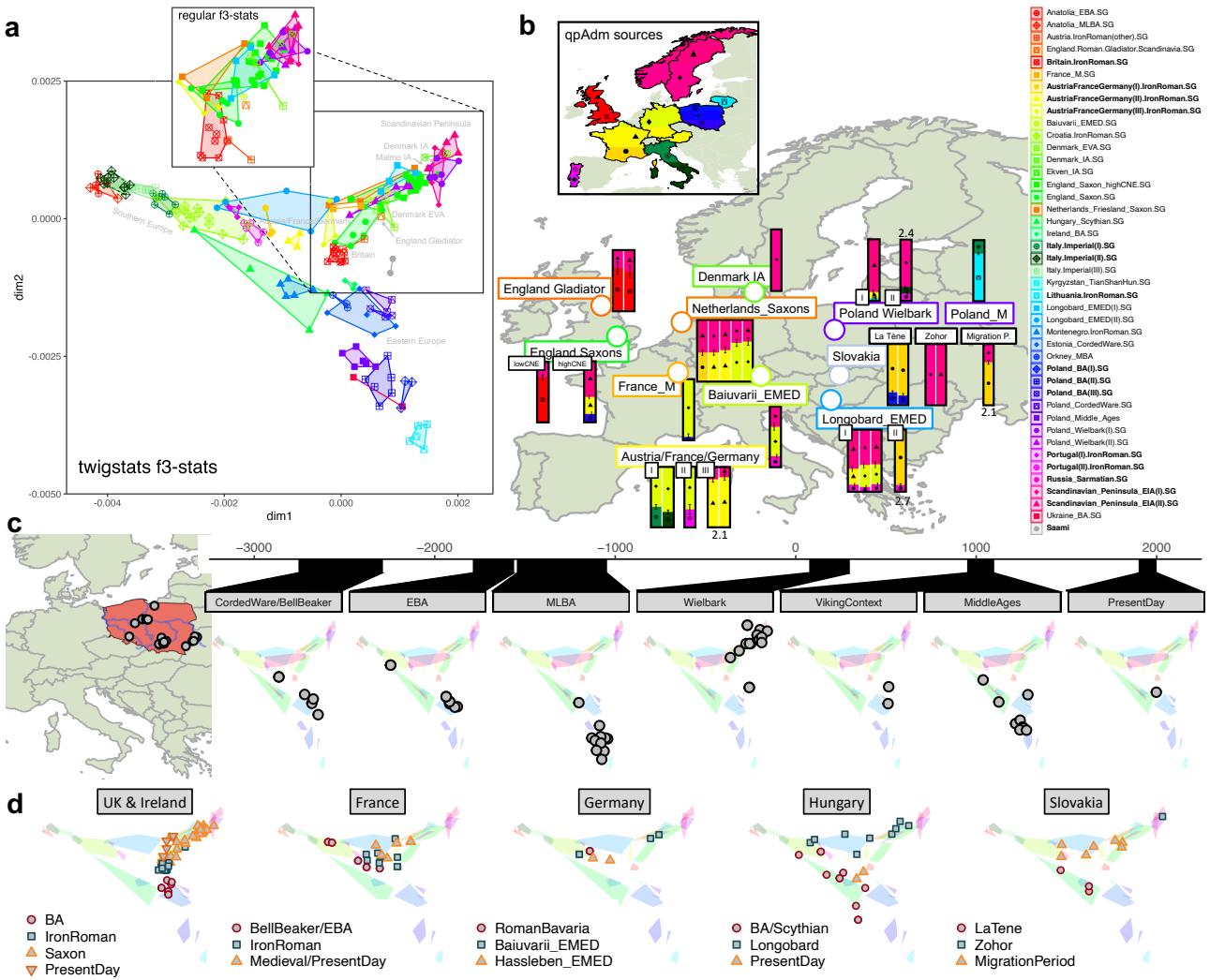
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**Figure 2. Two empirical applications where *Twigstats* time stratification reveals fine-scale structure and resolves timing of gene flow**

**a**, Fine-scale genetic structure quantified using a UMAP calculated on a symmetric matrix containing pairwise outgroup  $f_3$  statistics (outgroup: YRI) between individuals calculated as conventional directly on genotype calls or calculated from *Relate* genealogies with a cutoff of 1000 generations. **b**, Neanderthal admixture proportion inferred using an  $f_4$ -ratio of the form  $f_4(\text{outgroup}, \text{Altai}, \text{target}, \text{Mbuti})/f_4(\text{outgroup}, \text{Altai}, \text{Vindija}, \text{Mbuti})$ . We compute equivalent  $f_4$ -ratio statistics in a simulation emulating Neanderthal admixture 50,000 years ago and a second simulation involving no Neanderthal admixture but deep structure that leads to a similar inference unless deep coalescences are ignored by *Twigstats*.



**Figure 3. Ancestry in Iron Age and early medieval periods.**

**a**, Genetic structure of ancient groups from the Bronze Age to the medieval period quantified using a MDS of pairwise outgroup  $f_3$  statistics (outgroup: Han Chinese). These are calculated using *Twigstats* on Relate genealogies with a cutoff of 1000 generations. The magnified inset shows the MDS computed directly on genotypes. **b**, Ancestry models of Early Medieval groups across Europe computed using *qpAdm*. Sources are chosen from groups highlighted in the map and marked as bold in the legend, and were used in a rotational *qpAdm* scheme. For each target group, we remove models with infeasible admixture proportions and use a *Twigstats* cutoff of 1000 generations. All models satisfy  $p > 0.01$ , unless a  $-\log_{10}$  p-value is shown next to the model. **c**, Ancestry change visualised over a time transect spanning 5000 years in present-day Poland (grey circles) plotted on the same MDS as in **a**. **d**, Ancestry change around the Iron Age and early medieval periods in the UK and Ireland, France, Germany, Hungary, and Slovakia plotted on the same MDS as in **a**.



525 

## Methods

526 

### ***Twigstats***

527 *Twigstats* takes the *Relate* output format as input and allows computation of  $f$ -statistics directly on  
528 genealogies, by using the inferred expected number of mutations on each branch as input, which is  
529 computed as the product of a prespecified average mutation rate per base per generation, the  
530 branch length, and the number of bases each tree persists<sup>33</sup>. Importantly, *Twigstats* computes  $f_2$ -  
531 statistics ascertained by an upper date threshold, such that only branches younger than this  
532 threshold are used. If a branch crosses the threshold, we only use the proportion of the branch  
533 underneath the threshold. *Twigstats* additionally allows specifying a minimum derived allele  
534 frequency and lower date-threshold. *Twigstats* can also compute  $f_2$  statistics on age-ascertained  
535 mutations, which is particularly convenient for individuals not built into the genealogies.  
536

537 The computed  $f_2$ -statistics are fed into *admixtools2*<sup>69</sup> for computing derived statistics, which  
538 implements computation of genome-wide  $f_2$ ,  $f_3$ , and  $f_4$  statistics, as well as *qpgraph* and *qpAdm*  
539 models. We implement the sample size correction as detailed in Ref<sup>7</sup>. The  $f_2$  statistics are  
540 computed in blocks, typically of prespecified centi-Morgan size, or of prespecified physical distance.  
541 These blocks are used downstream within *admixtools2* to compute standard errors using a block-  
542 jackknife approach. By default, we compute  $f$ -statistics only on internal branches and exclude  
543 singleton tip branches to increase robustness against sample age.

544 The optimal *Twigstats* time cutoff is *a priori* unknown, however we develop theory that predicts the  
545 optimal choice in a simple 2-way admixture as a function of the admixture date, source split time,  
546 and admixture proportion (Supplementary Information). In this case, the optimal cutoff equals  
547 approximately 1.4 times the split time between admixing source groups, depending on exact  
548 parameters in the model (Figure 1b,c, Supplementary Figure 3).

549 

### **Non-negative least squares ancestry modelling**

550 We implement an approach that uses genealogies to emulate the chromosome painting technique  
551 of identifying closest genetic relatives along the genome<sup>1,2</sup> to fit admixture weights. When applied to  
552 true genealogies in simulations, this approach represents an idealised version of this idea.  
553

554 Given known assignment of each sample to a population, we implement a function in the *Twigstats*  
555 R package that identifies, at each position in the genome, the population with which a sample  
556 coalescences first. Our implementation takes a list of reference populations as input, such that any  
557 coalescences not involving these reference populations are ignored when traversing back in time  
558 through genealogical trees. If the first coalescence involves multiple different reference populations,  
559 this coalescence event will be assigned to each population with weight proportional to the number of  
560 samples in each population involved in that event.  
561

562 We then compute, for each target population and putative source populations, the proportion of the  
563 genome where the first coalescence involves each of the reference populations. Given  $k$  reference  
564 populations, we denote by  $a_t$  the vector of length  $k$  storing these proportions for population  $t$ . We fit  
565 our target population as a mixture of putative source populations using a non-negative least squares  
566 approach that finds a solution to the following optimisation problem  $\min_{0 \leq \beta_i \leq 1} \| a_t - A\beta \|_2$ , where

567  $t$  indexes the target population,  $A$  is a matrix storing  $a_i$  for putative source populations as its column  
568 vectors and  $\beta$  are non-negative mixture weights.

## 569 **Admixture simulations**

570 We use msprime<sup>70</sup> to simulate genetic variation data to test our approach.

571

### 572 **$F_4$ -ratio admixture simulation**

573 Our simulation in Figure 1b and Supplementary Figure 3b,c simulates five populations named PI,  
574 PO, P1, P2, and PX, where PO splits from all other populations 10,000 generations ago, P1 and P2  
575 represent two proxy source groups that split from each other at 250 generations or 500 generations  
576 ago, PI splits from P1 100 generations ago and PX emerges from a pulse admixture between P1  
577 and P2 50 generations ago. All populations have a constant diploid population size of 5000 and a  
578 variable human-like recombination map, where our simulation only covers chromosome 1, and a  
579 human-like mutation rate of 1.25e-8 mutations per base per generation. We additionally have a  
580 modified simulation with a lower mutation rate of 4e-9 mutation per base per generation emulating a  
581 transversions-only data set and a simulation where P2 has a diploid population size of 1000 in the  
582 last 50 generations, emulating a recent bottleneck in this population. We sample 20 haploid  
583 sequences from all populations. The “large sample size” simulation samples 100 haploid sequences  
584 from all populations.

585

### 586 ***qpAdm* simulation**

587 Our simulation in Supplementary Figure 3d uses the simulation model and script provided with ref.  
588<sup>10</sup>, where we changed this script to use the human hotspot recombination map. We simulated only  
589 chromosome 1. In the original simulation model, admixing sources split 1200 generations ago, with  
590 admixture occurring 40 generations ago. We additionally simulate a version where all population  
591 split times and admixture times are reduced by a factor of 5.

592

### 593 **Neanderthal admixture and deep structure simulation**

594 Our simulation in Figure 2b and Supplementary Figure 4c emulates Neanderthal admixture, where  
595 Neanderthals and ancestors of modern humans split 25,000 generations ago and admixture occurs  
596 2,000 generations ago. The resulting admixed ‘non-African’-like population coexists with the non-  
597 admixed ‘African’-like population until the present-day. Additionally, two Neanderthal populations  
598 split from each other 7,000 generations ago, which can be interpreted as emulating the Altai and  
599 Vindija Neanderthal populations, with Vindija being closer to the admixing source.

600

601 Alternatively, we simulate a model with two subgroups emulating ancestral modern humans in Africa  
602 that have a non-zero symmetric migration rate, ranging from 4e-5 to 2e-4 per generation, up until  
603 3,000 generations before present. One of these subgroups gives rise to a present-day ‘African’-like  
604 population, while the other gives rise to a present-day ‘non-African’-like population. We further  
605 sample two Neanderthal populations that split 7,000 generations ago and merge 25,000 generations  
606 ago with the same ancestral modern human subgroup that will eventually give rise to non-Africans.

607

608 We simulate whole genomes with human-like recombination rates and a mutation rate of 1.25e-8  
609 mutations per base per generation. Diploid effective population sizes are set to 10,000 except on  
610 the Neanderthal lineage where it is set to 3,000. We sample 2 haploid sequences for each  
611 Neanderthal population and 20 haploid sequences for the target admixed population and African  
612 non-admixed population.

613

614 **Fine-scale structure simulation**

615 Our simulation in Supplementary Figure 4a emulates the emergence of fine-scale population  
 616 structure and is adapted from ref. <sup>29</sup>. In this simulation, populations split 100 generations ago into 25  
 617 sub-populations followed by a period in which individuals are allowed to migrate at a rate of 0.01  
 618 between adjacent populations in a 5x5 grid. The diploid effective population size is 500 in each of  
 619 the 25 populations, and 10,000 in the ancestral population. We simulate 10 replicates of  
 620 chromosome 10, with a human-like mutation rate of 1.25e-8 and hotspot recombination map. We  
 621 sample 2 diploid individuals from each population. In addition, we sample 100 individuals from an  
 622 ancestral population that splits from the 25 target populations 100 generations ago, prior to the  
 623 emergence of structure in these 25 populations. *Relate* trees are inferred assuming true mutation  
 624 rates, recombination rates, and average coalescence rates across all samples.

625 **Ancient sample selection**

626 A full list of ancient genomes can be found in Supplementary Table 1. Published ancient shotgun  
 627 genomes provided by Refs. <sup>44,45</sup> were only available aligned against GRCh38. These data were  
 628 realigned to GRCh37d5 reference using *bwa aln* (version 0.7.17-r1188).  
 629 We select genomes with average autosomal coverage exceeding 0.5x with exception of VK518 of  
 630 previously suggested to be of Saami ancestry who has coverage of 0.438 and was included to  
 631 capture this ancestry in our panel. Genomes above a coverage cutoff of 0.5x have previously been  
 632 shown to result in reliable imputation results<sup>71</sup>. We exclude samples with evidence of contamination.  
 633 We remove any duplicate individuals, such as individuals that were resequenced, choosing the file  
 634 with higher coverage. We then filter out any relatives annotated in the Allen Ancient DNA Resource  
 635 v54.1<sup>19</sup>, retaining the individual with highest coverage in each family clade.  
 636

637 Our final dataset includes 1151 ancient genomes.

638 **Imputation of ancient genomes**

639 We follow the recommended pipeline of *GLIMPSE*<sup>72</sup>, and first call genotype likelihoods for each  
 640 genome at 1000 Genomes Project segregating sites using *bcftools mpileup* with filter -q 20, -Q 20,  
 641 and -C 50. We subsequently impute each genome separately using *GLIMPSE* v1.1.1 using the  
 642 1000 Genomes Project Phase 3 reference panel<sup>73</sup>. These imputed genomes are merged into a  
 643 single VCF for further downstream processing.

644

645 We filter any site where more than 2% of sites have an imputation posterior of less than 0.8 and  
 646 retain all remaining sites so as to not have any missing genotypes at individual SNPs. We merge  
 647 these ancient genomes with a subset of the 1000 Genomes Project data (Supplementary Table 1)  
 648 to obtain a data set of a total of 1842 genomes.

649 ***Relate*-inferred genealogies**

650 We merge imputed ancient genomes with a subset of the 1000 Genomes Project dataset, including  
 651 all European populations, CHB (Chinese Han from Beijing), and YRI (Yoruba). We create a second  
 652 dataset where we merge imputed genomes with the Simon Genome Diversity Panel. We then infer  
 653 genealogies for the joint data set of ancient and modern genomes using *Relate* v1.2.1. We  
 654 restricted our analysis to transversions only and assume a mutation rate of 4e-9 mutations per base

655 per generation and input sample dates as shown in Supplementary Table 1. We use coalescences  
656 rates pre-inferred for the 1000 Genomes project.

657 ***QpAdm* modelling**

658  
659 Briefly, *qpAdm* models are a generalisation of  $f_4$ -ratios, where 1-, 2-, and 3-source models can be  
660 tested as hypotheses, and admixture components and their standard errors obtained with a block  
661 jackknife<sup>8</sup>. A *qpAadm* model is fully specified by a set of putative source groups and additional  
662 'outgroups' that are used to distinguish source ancestries. We employed a rotating approach where  
663 we iteratively selected a subset of source groups, and used all remaining putative sources as  
664 outgroups. This approach penalises models where true contributing sources are used as outgroups.  
665 With sufficient statistical power, *qpAdm* models will be statistically rejected if true contributing sources  
666 are used as outgroups. If statistical power is more limited, several models will fit the data, but the  
667 correct model is expected to be preferred over wrong models.

668 **Clustering using *qpwave***

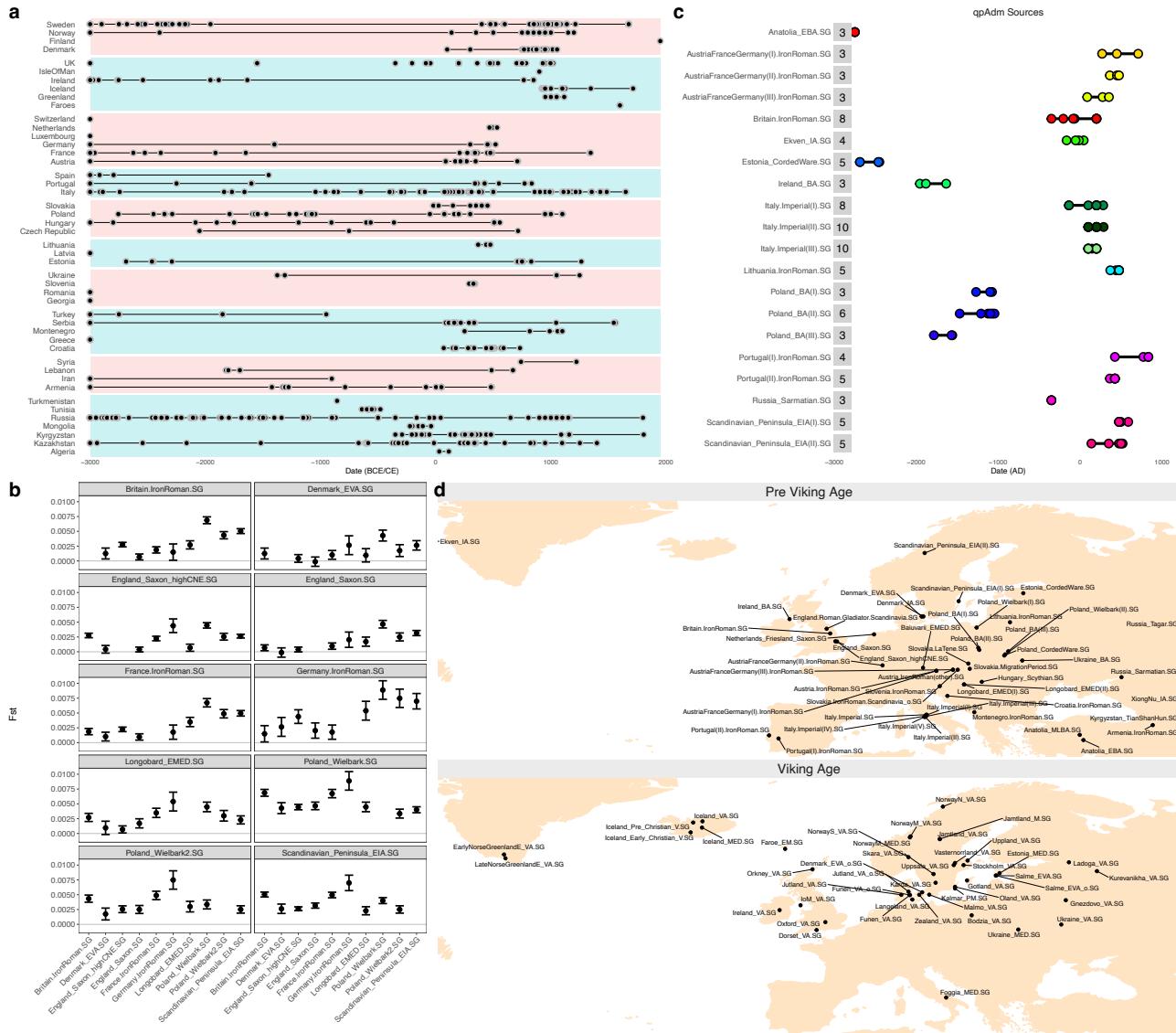
669 To identify homogeneous groups that we use as source groups in *qpAdm* modelling in Figures 3  
670 and 4, we follow ref. <sup>43</sup> and run *qpwave* using *Twigstats* between pairs of ancient individuals. We  
671 use CHB and five European population from the 1000 Genomes Project as reference groups. This  
672 approach tests if two individuals form a clade with respect to reference groups. The reason why this  
673 is a principled approach despite the 1000 genomes groups postdating the ancient individuals is that  
674 if a group of ancient individuals are truly homogeneous, they will be so with respect also to  
675 postdating individuals.

676  
677 We then define clusters by running UPGMA on -log10 p-values obtained from *qpwave* between all  
678 pairs of individuals and cut the resulting dendrogram at a height corresponding to a p-value of 0.01.  
679 We subsequently intersect cluster labels with pre-defined population labels.

680  
681 To choose source groups for Figure 3, we run this algorithm on samples from Britain.IronRoman,  
682 AustriaFranceGermany.IronRoman, Scandinavian\_Peninsula\_EIA, Poland\_BA,  
683 Lithuania.IronRoman, Portugal.IronRoman, and Italy.Imperial (Supplementary Table 1). We require  
684 a source group to have at least three individuals and therefore exclude clusters of size one or two.

685  
686 This approach results in two clusters in the Scandinavian Peninsula, approximately separating  
687 northern from southern Scandinavia, three clusters in Poland that separate samples temporally  
688 between the early and later Bronze Age and two clusters for Iron and Roman Age Portugal. In  
689 present-day Austria, Germany, and France this approach identifies three clusters, with each cluster  
690 spanning multiple archaeological sites in different countries, indicating genetic diversity in this region  
691 in the first millennium CE. In Figure 4b, we run this algorithm on Viking Age samples from Norway,  
692 Sweden, and Denmark dating to <1000CE. To restrict to the main genetic clusters, we select all  
693 groups with at least five individuals. This results in three clusters of samples in Sweden and  
694 Denmark and a single cluster in Norway.

# 695 Supplementary Figures



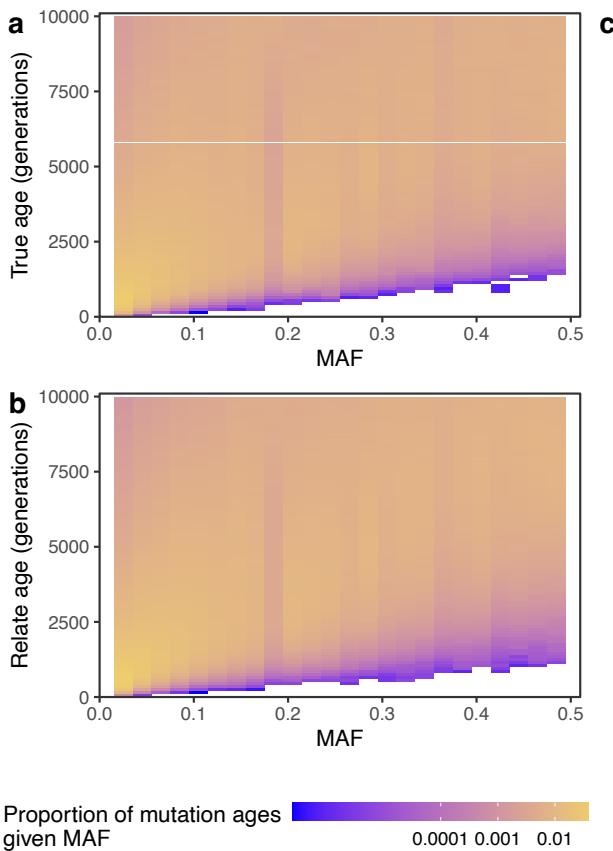
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# 697 Supplementary Figure 1

698

## 699 Collection of ancient genomes used in this study

700 **a**, Ancient DNA samples included in this study (Supplementary Table 1). Samples older than 3000  
 701 BCE are shown at 3000 BCE. **b**, Fst between Pre Viking Age groups computed using popstats<sup>74</sup>  
 702 using options --FST --informative. We show 1 standard error. **c**, Source groups used in qpAdm  
 703 modelling of Metal Age and Medieval Northern Europe (Figures 3 and 4), showing sample sizes and  
 704 sample ages. **d**, Map showing mean coordinates of sampled individuals in pre Viking Age and  
 705 Viking Age groups.



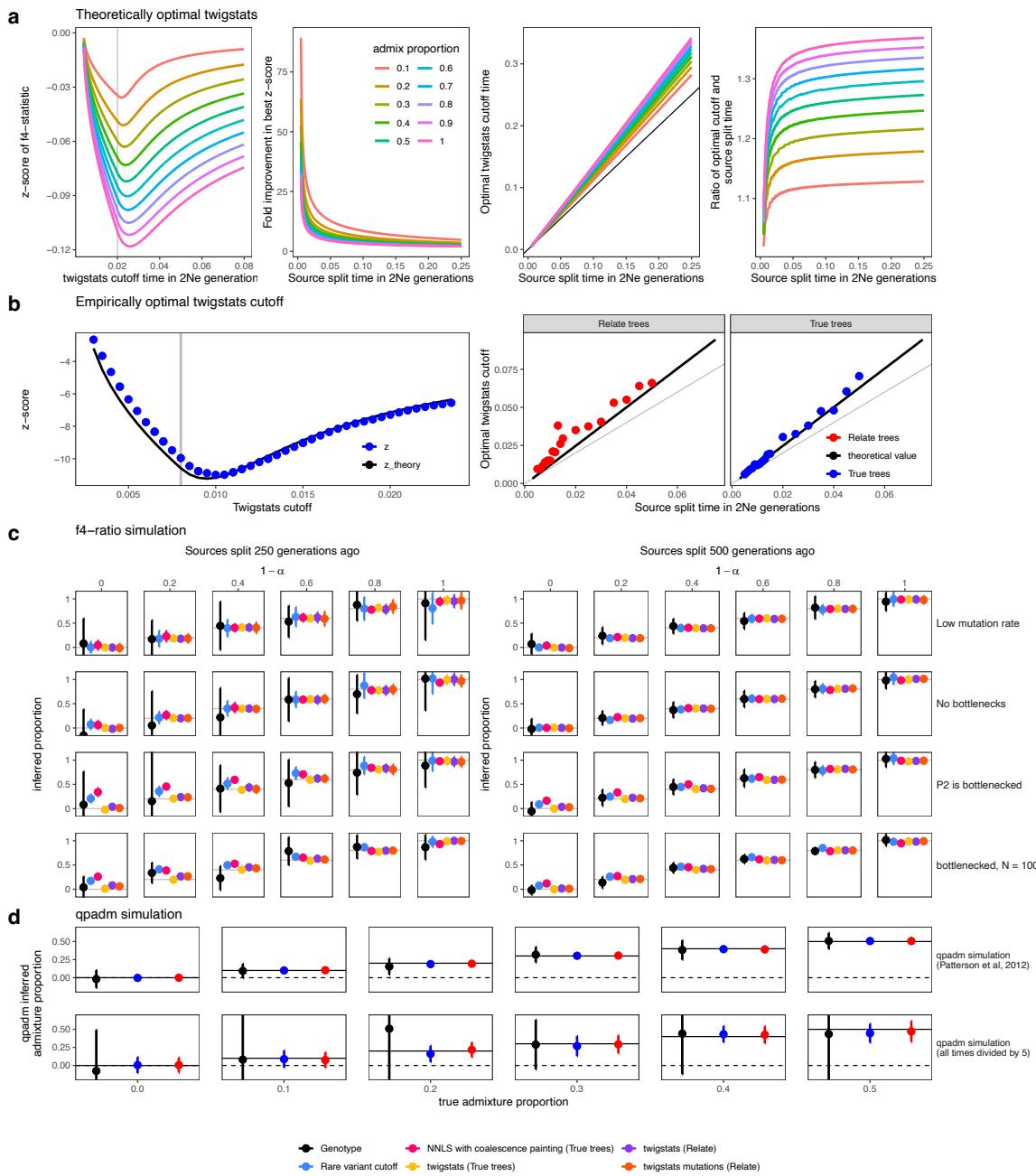
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707 **Supplementary Figure 2**

708

709 **Relationship of mutation age and MAF**

710 a, Heatmap showing the distribution of mutation ages for each minor allele frequency (MAF) bin. To  
 711 account for the uncertainty in when the mutation arose on a branch, we sample a random date  
 712 between the lower and upper ends of the branch onto which it maps. We use 20 replicates of the  
 713 simulation of Fig 1b, where sources split 500 generations ago and the admixture proportion is 0%.  
 714 b, Same as a but using mutation ages determined by *Relate*-inferred genealogies. We place  
 715 mutations at the same relative height between the lower and upper ends of a branch as in the true  
 716 trees to remove the uncertainty in when on the branch the mutation occurred, so that we would  
 717 recover the true allele age from a correctly inferred genealogy. c, Pearson correlation between  
 718 MAF, true mutation age, and Relate mutation ages, as well as the same comparisons when  
 719 restricting to mutations of MAF less than 0.1.



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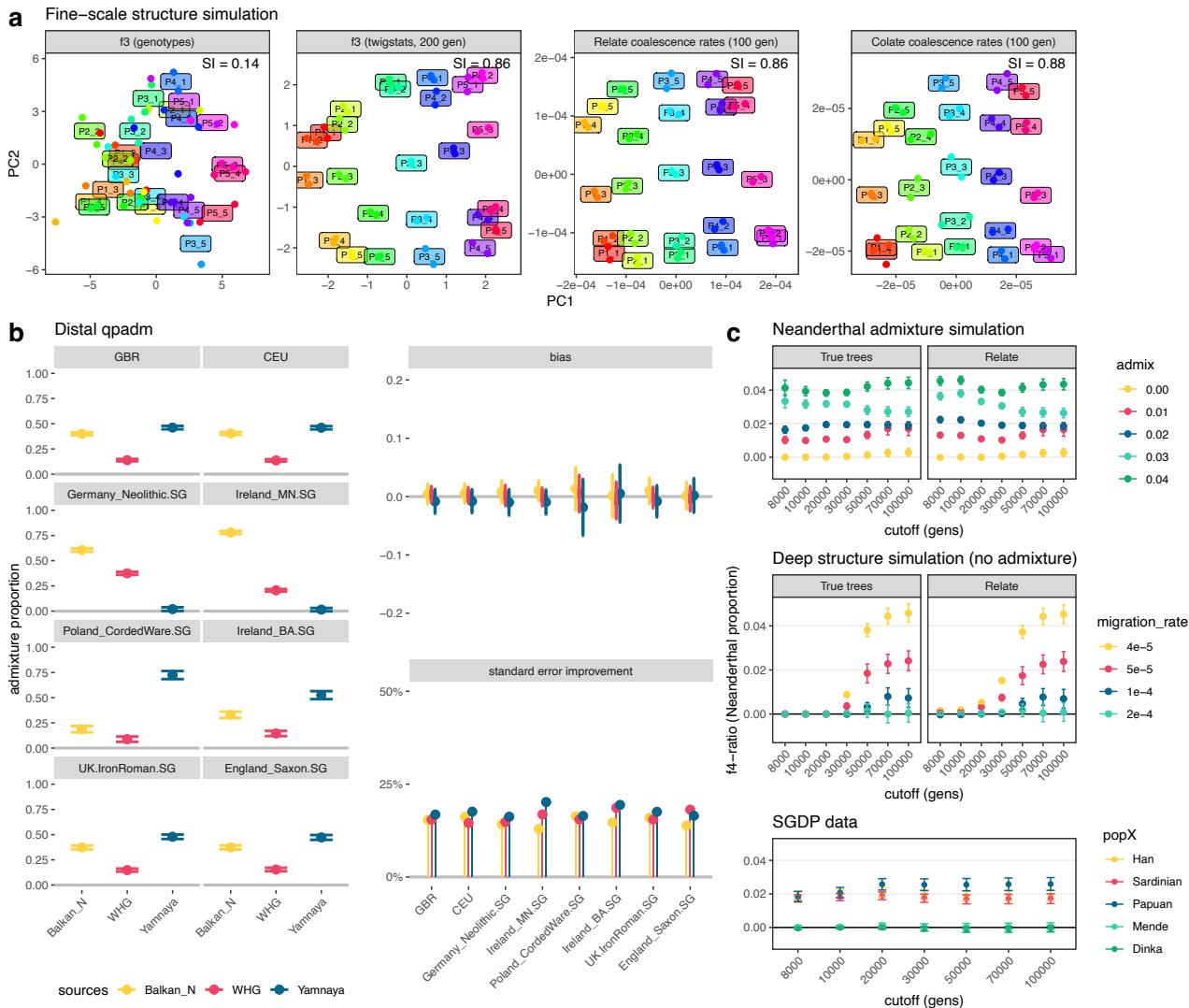
### Supplementary Figure 3

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#### Twigstats optimal cutoff and simulation performance

724 **a**, Theoretically computed z-score of  $f_4(\text{PO}, \text{P1}, \text{PX}, \text{P2})$  at a single genomic locus (Supplementary Information), assuming PX is admixed between P1 and P2 at time 0.004 (in units of 2Ne generations), e.g. corresponding to 100 generations with 2Ne of 25,000. Sources split at time 0.02 in the first panel. We show how the optimal z-score and *Twigstats* cutoff behaves as a function of the source split time and admixture proportions in subsequent panels. **b**, Comparison of z-scores computed using *Twigstats* to the corresponding theoretical values shown in **a**. **c**, Admixture simulation where sources P1 and P2 split 250 or 500 generations ago and a pulse admixture event gives rise to a target population PX 50 generations ago (see **Methods** for simulation details). Admixture proportions are computed using an  $f_4$ -ratio statistic and the *Twigstats* cutoff is set to twice the source split time and the rare variant cutoff is 5%. **d**, *QpAdm* simulation taken from<sup>7,10</sup>, as well as an adapted version where all population split times and the admixture date are divided by 5. The *Twigstats* cutoff time is chosen to be 1200 generations (top) and 600 generations (bottom).



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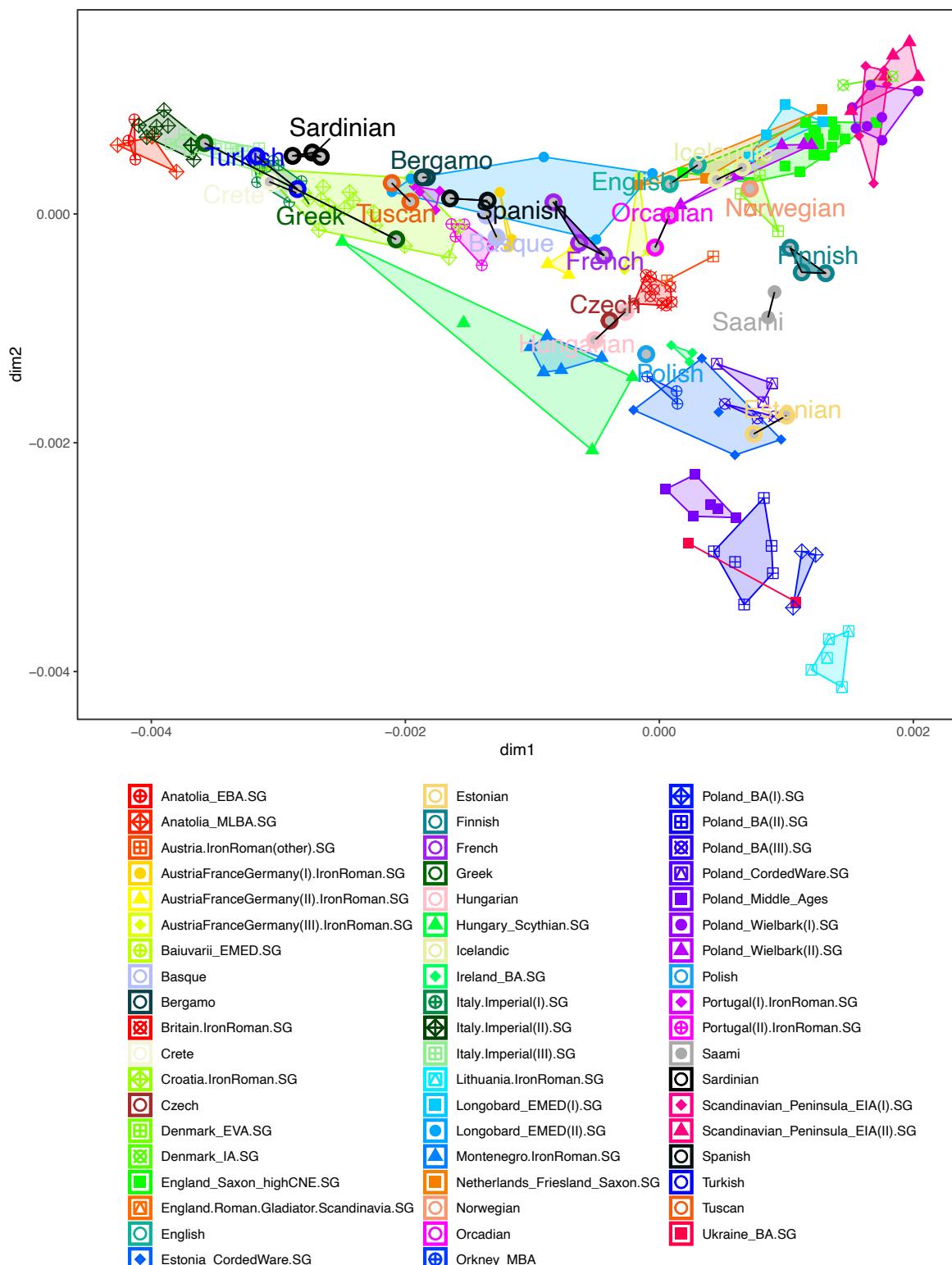
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## Supplementary Figure 4

### Three examples of applying *Twigstats*

**a** Fine-scale population structure simulation emulating Ref<sup>29</sup> (see Methods for simulation details). First two principal components are computed from pairwise outgroup f3 statistics on the genotypes directly and on *Relate* trees inferred from the 50 target individuals. In addition, we compute PCs on coalescence rates inferred from *Relate* trees or using *Colate*<sup>21</sup>. For *Colate*, we use a genealogy inferred only with 100 outgroup individuals, which are uncorrelated to the structure observed in the target populations and therefore emulates a situation where the genealogy is inferred on genomes that are closely related to, but separate, from the target populations of interest. Labels in plots show the average coordinates of members of that population. For each panel, we calculate a separation index as in<sup>29</sup>, which we define as the proportion of individuals for which the closest individual (by the Euclidean distance in PC space) is in the same population. **b**, Admixture proportions inferred using *qpAdm* with three distal sources of Western hunter-gatherers, early European farmers, and Yamnaya Steppe people<sup>36</sup>. We show results for *Twigstats*-5000. Bias is measured as the difference in admixture proportions obtained from *Twigstats*-5000 and all SNPs, and we show standard errors of the latter. The standard error improvement shown is one minus the ratio of standard errors obtained from *Twigstats*-5000 and using all SNPs. **c**, Admixture proportions as a function of the *Twigstats* cutoff time computed on true or *Relate* trees for simulations emulating Neanderthal admixture or deep structure, not involving admixture, as well as for real samples in the SGDP data set<sup>75</sup>.

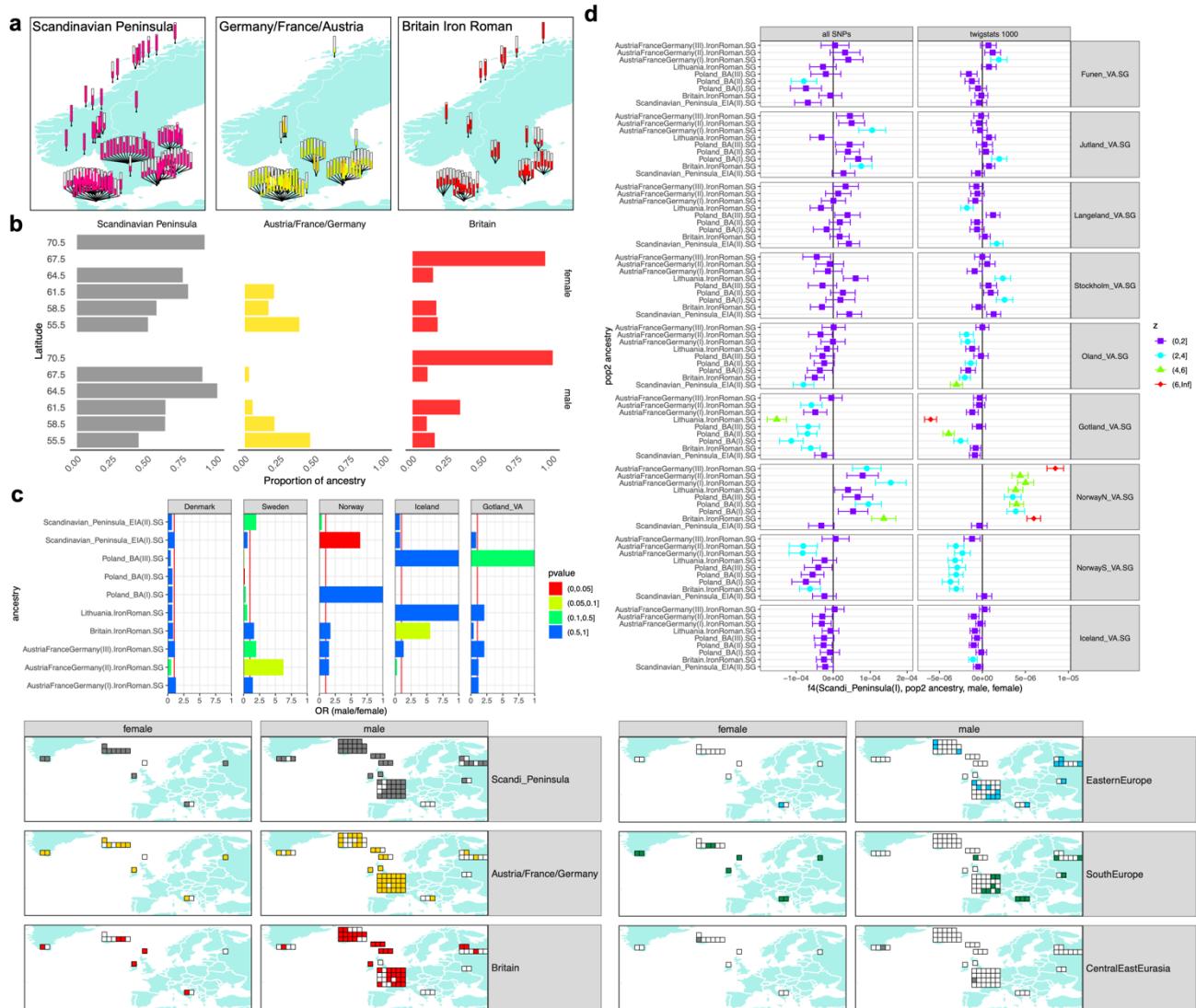


758  
759

## 760 **Supplementary Figure 5**

## 762 MDS of ancient and modern genomes

763 MDS of Iron and Roman Age groups, and modern groups in the Simons Genome Diversity Project  
764 (labelled).



765

766

## Supplementary Figure 6

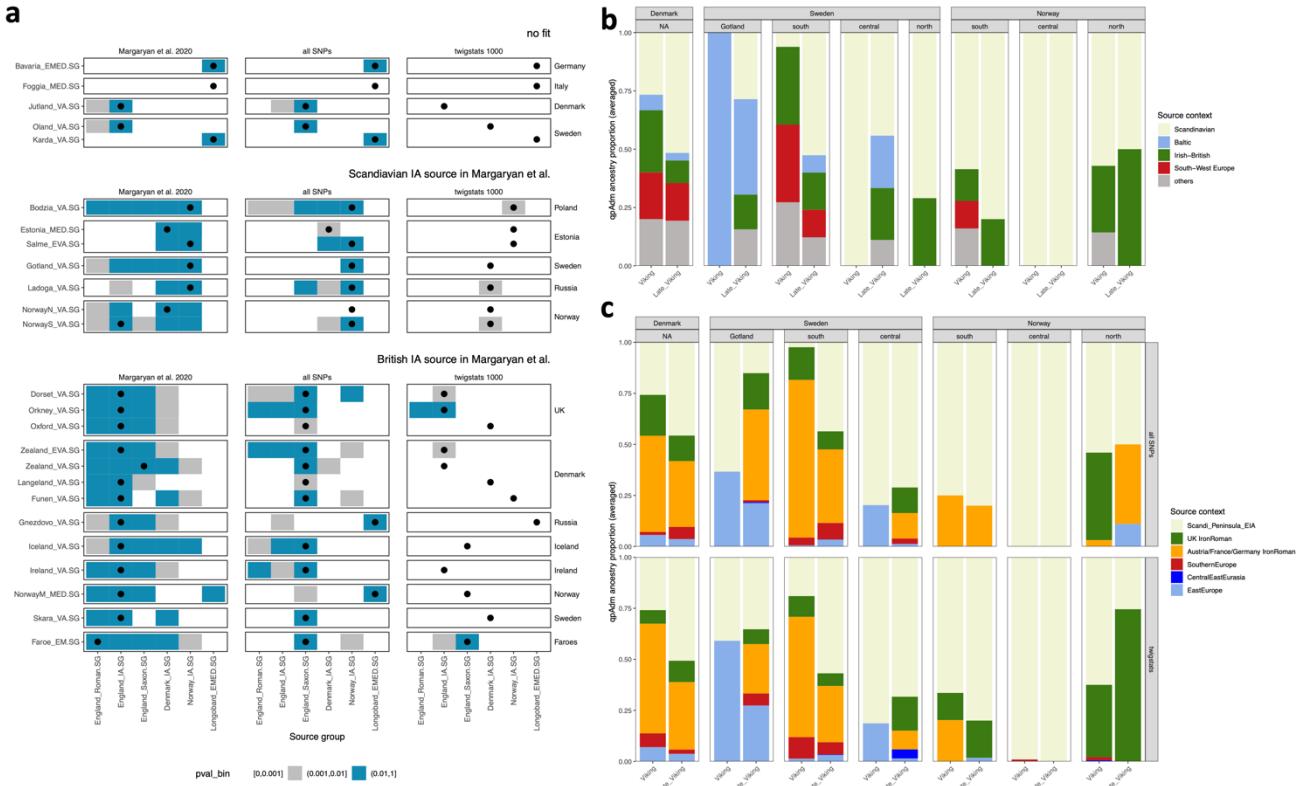
767

768

### Ancestry estimates stratified by genetic sex

769

770 **a**, Map showing ancestry carried by each Scandinavian Viking age individual. **b**, Ancestry  
 771 proportions across individuals grouped by Latitude and genetic sex. **c**, Odds ratio and p-values  
 772 calculated using a two-sided Fisher's exact test on the number of males and females carrying each  
 773 ancestry in Viking Age Denmark, Sweden, Norway, Iceland, and Gotland. **d**,  $F_4$  values of the form  
 774  $f_4(\text{Scandinavian\_Peninsula\_EIA(I)}, \text{alternative source group}, \text{males in Viking group}, \text{females in}$   
 775  $\text{Viking group})$  computed using all SNPs and *Twigstats*. A significantly positive value is evidence of  
 776 attraction of females with pop2 or males with Scandinavian\_Peninsula\_EIA(I). We only show groups  
 777 with at least four males and females. **e**, Map showing Farflung Viking individuals grouped by  
 778 ancestry and genetic sex. In contrast to Figure 4b, for **a**, **b**, **c**, and **e**, an individual is assigned an  
 ancestry group, if it has any accepted model ( $p > 0.01$ ) where that ancestry features.



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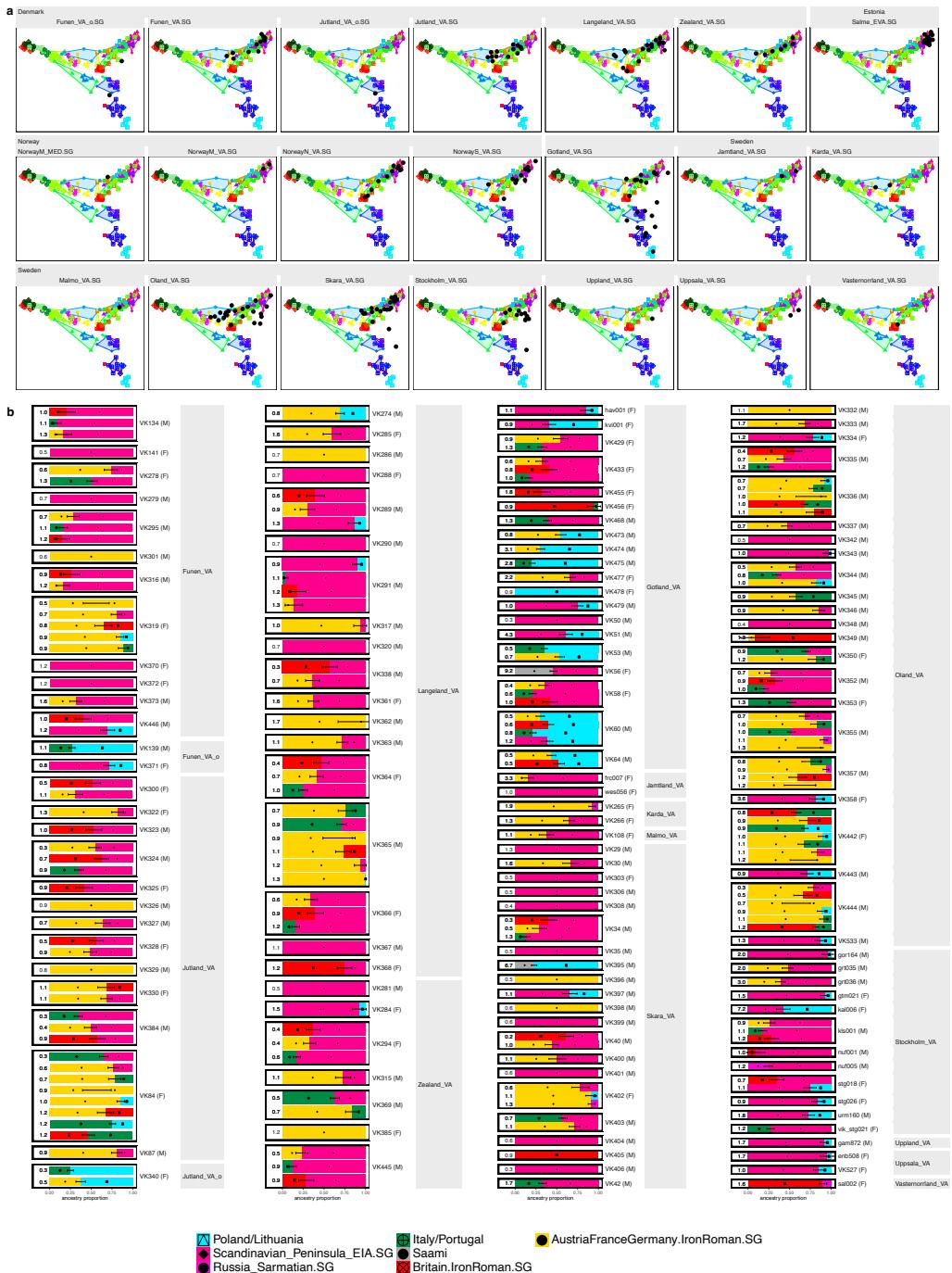
## Supplementary Figure 7

781

### Replication previous Viking Age ancestry modelling

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a, P-values of 1-source *qpAdm* models with target groups shown as rows and source groups shown as columns, replicating Supplementary Figure 5a of Ref<sup>13</sup>. Left column uses p-values obtained from Ref<sup>13</sup>. Middle and right column correspond to newly computed p-values in a *qpAdm* using, respectively, all SNPs and *Twigstats*-2000. Outgroups are YRI, CHB, DevilsCave\_N.SG, WHG, EHG, Anatolia\_N, Yamnaya, Estonia\_CordedWare.SG (Supplementary Table 1). We excluded Denmark\_IA.SG and England\_Roman.SG from the rotational scheme as these groups overlap in ancestry with England\_IA.SG and Norway\_IA, respectively. Only samples with coverage exceeding 0.5 are used. For each target group, the source group with the largest p-value is shown with a black circle. b, *QpAdm* models of Ref<sup>44</sup> where modern populations are used as sources. As in Ref<sup>44</sup>, we show ancestry proportions averaged over individuals in each group, where for each individual the model with the smallest number of sources and largest p-value is chosen. c, Replication using the same target samples as in b. We fit a maximum of two sources and choose the model with the smallest number of sources and largest p-value, requiring  $p > 0.05$  for 1 source and  $p > 0.001$  for 2 source models. The set of individuals used in b and c are identical and are comprised of targets with an accepted model in all SNPs and *Twigstats*-1000, removing 15 of 167 individuals. We additionally remove 17 individuals that did not have a feasible model in Ref.<sup>44</sup>.



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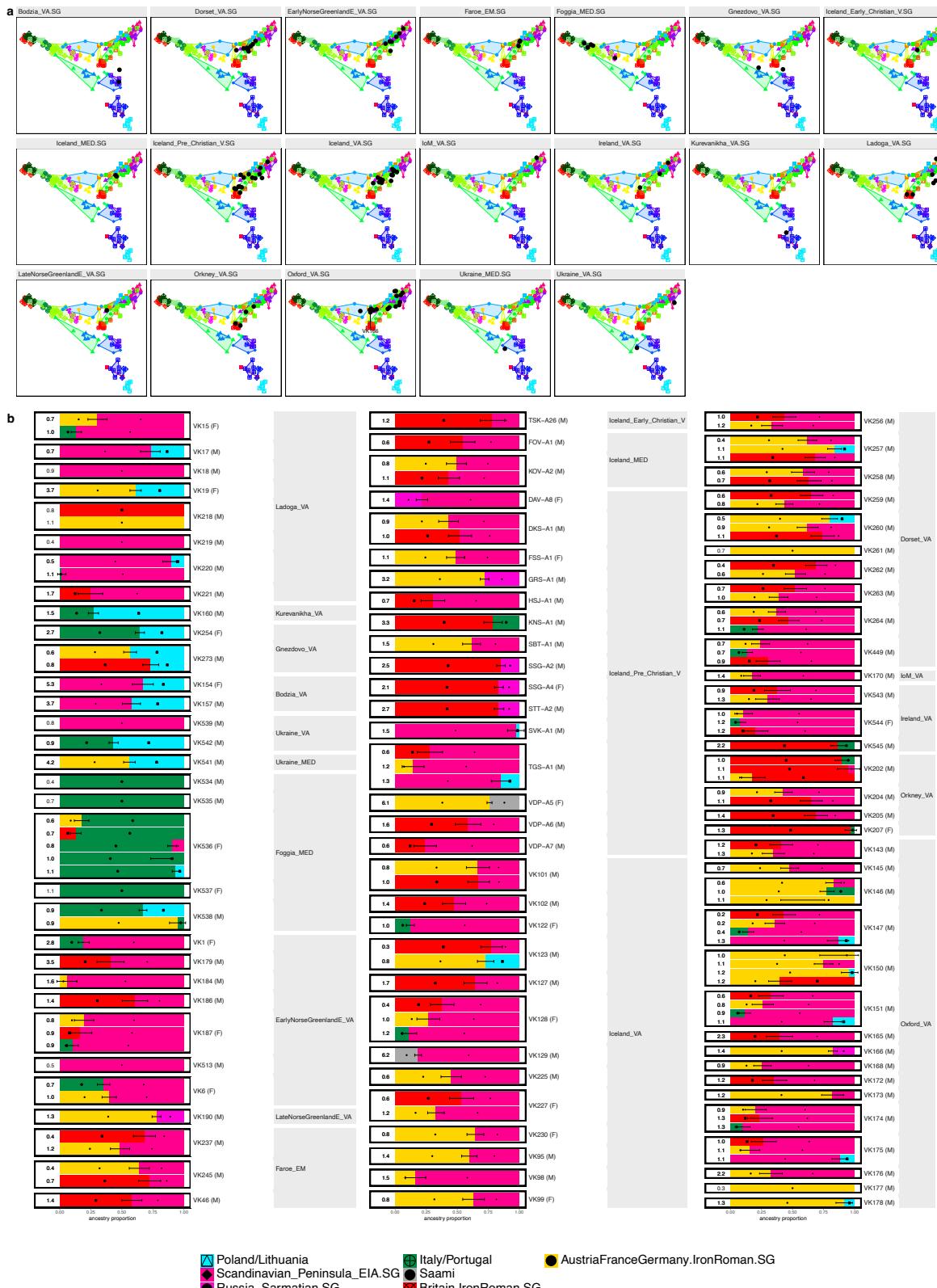
## Supplementary Figure 8

801

### Ancestry models of Viking Age individuals in Scandinavia

802

**a**, MDS of each Scandinavian Viking group plotted on top of preceding Iron age and Roman individuals. **b**, All accepted qpAdm models using twigstats-1000 for every Scandinavian Viking individual in Denmark, Sweden, and Norway, computed in a rotational qpAdm with source groups identical to Figure 4. We only retain models with feasible admixture proportions, standard errors of < 0.25, and show models with 1 source and a p-value greater than 0.05 or otherwise with 2 sources and a p-value greater than 0.05. If no such models exist, we select the model with the largest p-value. The -log10 p-values are shown to the left of each model. We combine models involving related sources, if they exist, by averaging their respective admixture proportions, standard errors, and p-values.



812

813 **Supplementary Figure 9**

814

815 **Ancestry models of farflung Viking individuals**

816 **a**, MDS of each farflung Viking group plotted on top of preceding Iron age and Roman individuals. **b**,  
 817 All accepted qpAdm models using twigstats-1000 for every non-Scandinavian Viking individual  
 818 computed in a rotational qpAdm with source groups identical to Figure 4.

819 

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