

1 Modeling interpretable correspondence between cell state and 2 perturbation response with CellCap

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12 Abstract

13 Single-cell transcriptomics, in conjunction with genetic and compound perturbations, offers a
14 robust approach for exploring cellular behaviors in diverse contexts. Such experiments allow un-
15 covering cell-state-specific responses to perturbations, a crucial aspect in unraveling the intricate
16 molecular mechanisms governing cellular behavior and potentially discovering novel regulatory
17 pathways and therapeutic targets. However, prevailing computational methods predominantly
18 focus on predicting average cellular responses, disregarding the inherent response heterogeneity
19 associated with cell state diversity. In this study, we present CellCap, a deep generative model de-
20 signed for the end-to-end analysis of single-cell perturbation experiments. CellCap employs sparse
21 dictionary learning in a latent space to deconstruct cell-state-specific perturbation responses into
22 a set of transcriptional response programs. These programs are then utilized by each pertur-
23 bation condition and each cell at varying degrees. The incorporation of specific model design
24 choices, such as dot-product cross-attention between cell states and response programs, along
25 with a linearly-decoded latent space, underlay the interpretation power of CellCap. We evaluate
26 CellCap’s model interpretability through multiple simulated scenarios and apply it to two real
27 single-cell perturbation datasets. These datasets feature either heterogeneous cellular populations
28 or a complex experimental setup. Our results demonstrate that CellCap successfully uncovers the
29 relationship between cell state and perturbation response, unveiling novel insights overlooked in
30 previous analyses. The model’s interpretability, coupled with its effectiveness in capturing hetero-
31 geneous responses, positions CellCap as a valuable tool for advancing our understanding of cellular
32 behaviors in the context of perturbation experiments.

33 1 Main

34 High-throughput single-cell RNA sequencing (scRNA-seq) has greatly advanced our understanding
35 of cellular and molecular biology [1–3]. Combining scRNA-seq with perturbation experiments has
36 further expanded our ability to explore the way cells behave in different conditions. Technologi-
37 cal innovations like Perturb-seq [4] and CROP-seq [5] use CRISPR to introduce genetic changes
38 or perturb gene expression levels in cells, and they enable systematic screening at large scale.
39 Single-cell perturbation datasets generated using these technologies are promising approaches for
40 discovering comprehensive maps of gene regulatory networks in complex cellular systems [6]. Such

41 an understanding of gene networks could substantially boost drug discovery efforts [7]. As the
42 number of large-scale single-cell perturbation datasets grows, so does the challenge of modeling
43 and interpreting perturbation responses at the single-cell level.

44 The most straightforward approach to single-cell perturbation data analysis is one aimed at un-
45 covering bulk effects, where expression data from perturbed cells are aggregated and compared to
46 the aggregate of untreated control cells. In practice, addressing cellular heterogeneity (both at the
47 level of cell types and cell states) and batch effects requires complicated data preprocessing steps,
48 including batch effect correction and cell type identification [8]. This rudimentary approach suffers
49 from a number of fundamental shortcomings: (1) The choice on the data preprocessing procedure
50 often lead to changes in biological conclusions; (2) Cell type identification and data stratification
51 often requires imposing arbitrary thresholds (in particular, in experiments dealing with cells on a
52 differentiation trajectory); (3) Bulk analysis testing overlooks potentially valuable information en-
53 coded in cell-state heterogeneity, such as cell-state-specific responses; (4) The standard differential
54 expression analysis does not immediately reveal commonalities and contrasts between the mecha-
55 nism of action of different perturbations, which requires further statistical modeling. It is therefore
56 desirable to address these shortcomings within a robust end-to-end computational framework.

57 In recent years, several machine learning approaches have made progress toward improving
58 upon simple differential expression testing. The computational framework MIMOSCA assumes
59 an additive model of perturbational responses and analyzes perturbation experiments within a
60 regularized linear regression framework [4]. The computational framework Augur adapts a random
61 forest classifier to prioritize the cell type on which a certain perturbation has primary impact. Once
62 this cell type is identified, a differential expression test can be performed in this cell type context to
63 reveal the perturbation effects [9]. While these approaches recover certain aspects of the underlying
64 biology, it is likely that more complex cellular behaviors are not captured by simple linear models.

65 Deep learning models have also been explored as a means to uncover the nonlinear complexity
66 in single-cell perturbation data. For example, scGen uses a deep generative model to predict
67 the impact of one perturbation on a new cell population [10], and GEARS takes advantage of
68 prior biological knowledge to model nonlinear gene interactions and nonlinearities in response
69 to multiple perturbations [11]. Though both scGen and GEARS show promise in predicting
70 nonlinear synergistic effects between multiple perturbations, they do not explicitly model the ways
71 in which cell type or cell state generate the nonlinear perturbation response. The Compositional
72 Perturbation Autoencoder (CPA) model, a follow-up to scGen, decomposes the perturbed gene
73 expression profiles into a cell state latent representation in which perturbation, batch, and other
74 effects are all modeled as vector translations [12]. This enables CPA to predict cell-state-specific
75 perturbation responses. Alternatively, PerturbNet encodes perturbation and cell state into two
76 separate latent representations via two different encoding neural networks, and it connects the
77 perturbation representation and cell state representation through a third neural network [13].
78 These designs allow CPA and PerturbNet to uncover the correspondence between cell state and
79 perturbation response. However, the nonlinear deep neural network decoders involved in the
80 models above do not readily lend themselves to succinct interpretation. Thus, these methods
81 primarily focus on the task of predicting unseen perturbation responses rather than understanding
82 and interpreting the perturbation responses measured by the dataset at hand.

83 Here we propose CellCap, a linearly-decoded variational autoencoder for modeling single-cell
84 perturbation data. CellCap builds upon the foundation laid by the CPA model but differs in
85 several key ways including its primary objective: while CPA aims to predict the responses of
86 unseen perturbations and in combinations, CellCap instead focuses on dissecting and interpreting
87 cellular responses in terms of a learned sparse dictionary of transcriptional response programs.
88 CellCap combines a nonlinear encoder with a linear decoder. The linear decoder lends the model
89 interpretability by allowing translating all latent space quantities to the gene expression space,
90 while the nonlinear encoder aims to uncover the basal (pre-perturbation) cell state from perturbed
91 cell states. In order to capture the complexity of cell-state-specific responses, CellCap moves the
92 nonlinear computations into the latent space algebra, using multi-head dot-product attention to
93 capture the correspondence between the state of individual cells and their perturbation response.
94 These response amplitudes then act on a sparse dictionary of transcriptional response programs to

95 generate the data. We demonstrate the interpretability and model identifiability of CellCap with
96 both simulated and real single-cell perturbation data.

97 2 Results

98 2.1 CellCap’s key concepts

99 CellCap is fundamentally a variational autoencoder (VAE) that encodes the observed gene count
100 matrix x_{ng} into and out of a K -dimensional latent space. What distinguishes CellCap from a stan-
101 dard VAE, however, is the additional structure imposed on the making of latent representations.
102 As a first step, the CellCap encoder projects the observed gene count matrix x_{ng} into a “basal
103 state” $z_{nk}^{(\text{basal})} \in \mathbb{R}^K$ using a multi-layer neural network (Fig. 1a). Here n and g are cell and gene
104 indices respectively, and k is the dimension of the latent space. The latent space modifications
105 arising from fixed effect covariates $\Delta z_{nk}^{(\text{cov})}$ and perturbations $\Delta z_{nk}^{(\text{pert})}$ are then added to $z_{nk}^{(\text{basal})}$
106 to produce the complete and “recomposed” cell latent representation z_{nk} . The linear fixed effects
107 modeled by $\Delta z_{nk}^{(\text{cov})}$ serve to regress out sources of variability that are not the object of study, for
108 example batch or donor identity. The complete latent representation z_{nk} is then transformed back
109 into gene expression space via a linear decoder and is matched with the observed gene expres-
110 sion matrix x_{ng} (loss $\mathcal{L}_{\text{reconstruction}}$) [14, 15]. Since the relationship between observed data and
111 the basal state can be highly complex and nonlinear (e.g. the observed data could correspond to
112 treated cells whereas the basal state would correspond to the inferred state of the same cells prior
113 to treatment), we use an expressive deep neural network to amortize the inference of the basal
114 state $z_{nk}^{(\text{basal})}$ from x_{ng} . At the same time, we use a linear decoder to maintain interpretability of
115 the latent space [16].

116 The “basal state” is a concept proposed in the CPA model by Lotfollahi *et al.* [12] and is
117 understood as an intermediate latent space vector that captures only the intrinsic and unmodeled
118 cell state variation. Throughout this manuscript, the terms “cell state” and “basal state” are
119 used interchangeably. Importantly, $z_{nk}^{(\text{basal})}$ ought not to contain information related to perturba-
120 tion and other known covariates such as batch or donor identity. To obtain such a basal state
121 representation, we simultaneously train the encoder network and adversarial classifier networks to
122 strip perturbation and known covariate information out of the basal latent space, similar to the
123 approach taken by the CPA model (loss $\mathcal{L}_{\text{adversarial}}$).

124 We formulate modeling the effect of perturbations as a “dictionary learning” problem. We
125 assume that the applied perturbations can induce up to Q transcriptional “response programs”.
126 The response programs can be collected as a matrix $w_{qk} \in (-1, 1)$ interval, with Q rows, with
127 each row representing a distinct response program. All cells share statistical power to estimate
128 w_{qk} , though individual programs can be used by different cells and perturbations with different
129 amplitudes (Fig. 1a). Explicitly, we assume $\Delta z_{nk}^{(\text{pert})} = \sum_{q=1}^Q h_{nq} w_{qk}$, where the h_{nq} represents
130 the to-be-inferred usage amplitude of response program q by cell n .

131 Our use of low-complexity building blocks for the sake of interpretability, namely a linearly-
132 decoded latent space and dictionary learning, necessitates invoking an element of nonlinearity to
133 allow modeling complex data distributions beyond the reach of linear models. In our formulation,
134 we introduce this nonlinearity in the computation of the variational posterior distribution of h_{nq} ,
135 which is one of the key methodological contributions of our work. We construct h_{nq} in the form
136 of “scaled dot-product attention” [17] between the basal cell state $z_{nk}^{(\text{basal})}$ and perturbation design
137 matrix $P_{np} \in \{0, 1\}$. The perturbations are associated with a set of learned “perturbation key”
138 vectors κ_{pq} (or equivalently, a 3-dimensional tensor κ_{pqk}). The key vectors, which live in the same
139 K -dimensional space as the basal states (see Eqn. 3), determine the amplitude of cell-state-specific
140 response program q in cell n as $\beta_{nq} = \text{softmax}_q(\kappa_{pq} \cdot z_{nk}^{(\text{basal})})$. Illustrated in Fig. 1a, the entries of β_{nq}
141 denote the normalized attention weights between cells and response programs. In the terminology
142 of scaled dot-product attention, the the basal state serves as “query”, the perturbation keys serve
143 as “key”, and finally the “value” is $v_{nq} = \sum_p H_{pq} P_{np}$, which is intuitively the linear action of H_{pq}

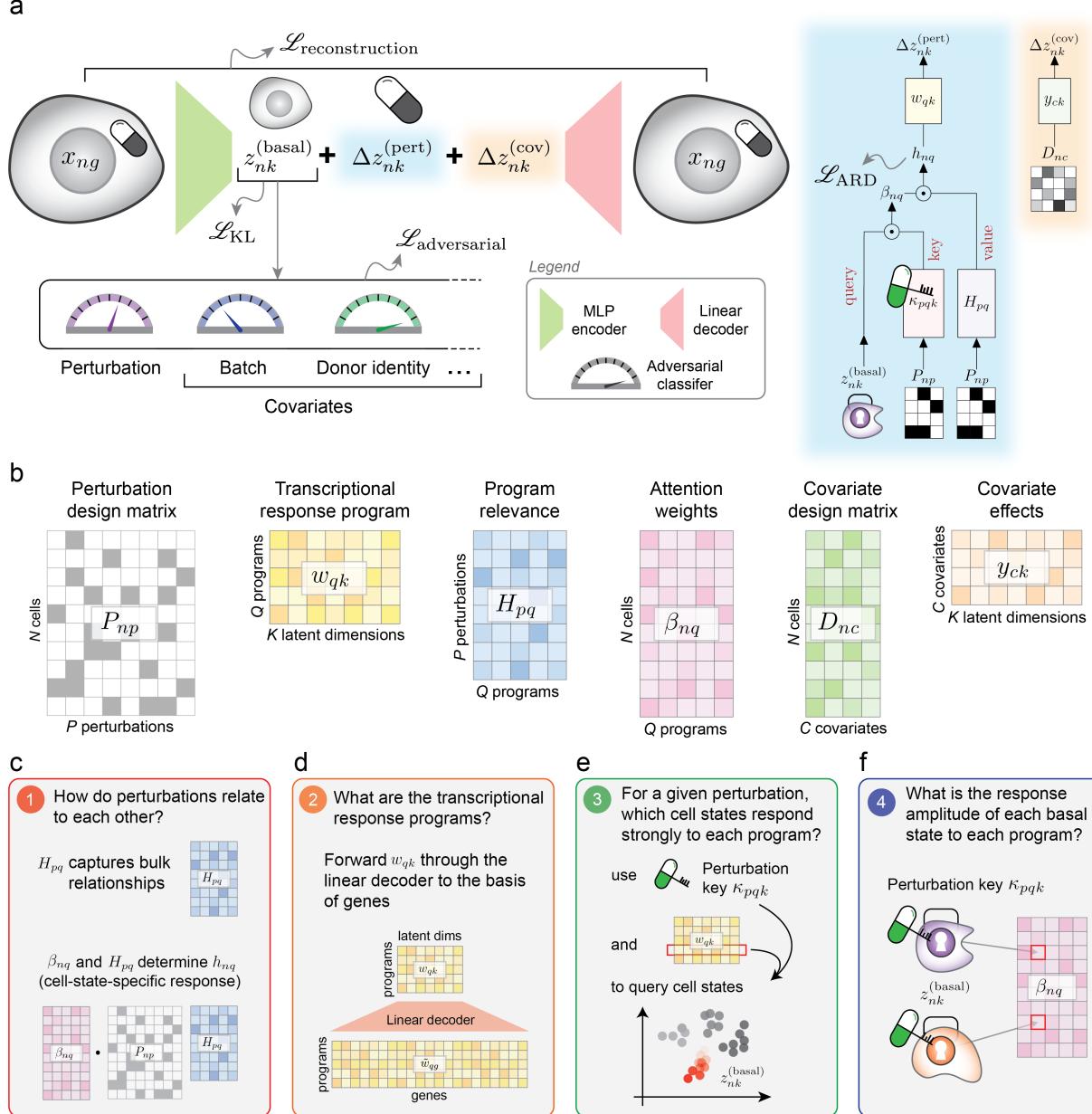


Figure 1: Key concepts underlying the CellCap model and its interpretable workflow. (a) A linearly decoded VAE is the backbone of CellCap, which encodes the perturbed single-cell data into basal state $z^{(\text{basal})}$ and reconstructs $z^{(\text{basal})} + \Delta z^{(\text{pert})} + \Delta z^{(\text{cov})}$ back to the observed gene expression count matrix x_{ng} via a linear decoder. (b) Graphical presentations of individual components of CellCap. (c-f) Various downstream applications of CellCap. (c) Understanding the relationship between bulk and cell-state-specific perturbation effects; (d) Interpretability of the transcriptional response programs with a linear decoder; (e) Uncovering characteristics of cell states that respond to each transcriptional program; (f) Uncovering cell-state-dependent response amplitude to each response program.

on the P_{np} . Here, H_{pq} is another learnable weight matrix, with the interpretation of the usage of response program q by perturbation p at an aggregate level. Ultimately, the program usage is given as $h_{nq} = \beta_{nq} v_{nq}$ and can be interpreted as the cell-state-specific amplitude of response program q in cell n after being treated with perturbation p . In practice, as in Ref. [17], we also found it beneficial to leverage multiple attention heads to distribute the inference of response program usages to specialized attention heads (see Methods).

We remark that the learned dictionary of response programs w_{qk} are reused across perturbations, leading to improved interpretability of the output and an understanding of the relatedness between perturbations. CellCap uses sparse Bayesian learning (SBL), in the form of “automatic relevance determination” [18], as a mechanism to learn as few response programs ($\leq Q$) as are necessary to explain the data (loss \mathcal{L}_{ARD}). The total loss function of CellCap balances this learning objective with the reconstruction loss and the adversarial loss (Fig. 1a). A formal definition of the generative and inference process is provided in the Methods section, as well as hyperparameter setup for balancing these learning objectives.

The CellCap model lends itself to interpretability by design (Fig. 1b). Here, we outline a few biological questions that can be answered using CellCap. First, CellCap reveals whether different perturbations elicit similar cellular responses (Fig. 1c). General relationships between perturbations are captured by H_{pq} , the usage of each learned response program by each perturbation. CellCap enables researchers to ask the same question under a specific cell-state context by examining h_{nq} , which is a combination of H_{pq} and β_{nq} , the cell-state-dependent attention outputs that describe the response amplitude of each response program in each perturbed cell. This enables a finer-grained understanding of relationships among perturbations while going beyond bulk effects and leveraging the single-cell resolution of the data. Next, CellCap defines the transcriptional response programs activated in a single-cell perturbation experiment (Fig. 1d). Instead of an overall effect for each perturbation, CellCap discovers individual transcriptional response programs in the form of w_{qk} . Since these programs live in the same latent space as cell states, we can use the linear decoder to translate these latent-space response programs to gene expression space, where each program can be understood in terms of gene expression patterns.

The key advantage of CellCap is its ability to model the correspondence between basal cell states and perturbation responses (Fig. 1e). This correspondence is critical for understanding why cells may respond to a perturbation in a particular way. For example, the activation of cell-state-specific gene expression programs, which could include cell maturity or cell cycle phase among others, may make a specific cell population uniquely vulnerable to a perturbation and lead them to respond with a specific transcriptional activation. This correspondence can be uncovered by using the perturbation key κ_{pqk} of perturbation p in the context of response program q , to query which basal state $z_{nk}^{(basal)}$ is relevant (see Methods). Finally, the attention weights β_{nq} indicate how the amplitude of response program q varies across different basal cell states (Fig. 1f).

2.2 CellCap captures cell-state dependent responses in simulated data

To explore different aspects of the behavior of CellCap in a controlled fashion, we generate and study three simulated scenarios that contain two perturbations in each (Fig. 2a). We assume that the basal cell states co-vary with a hypothetical “pseudotime” to serve as a simplified model of cell state trajectories. We used PROSSTT [19] to generate such continuous cell states, and each cell was assigned a pseudotime value (see Supplementary Section S.1). In simulated scenario (1), each perturbation induces a single unique transcriptional response program, with the amplitude of the response being proportional to the cell state “pseudotime”. In simulated scenario (2), the two perturbations induce a single shared response program, though the cells have a stronger response to one perturbation than the other. Again, the cell state pseudotime modulates the amplitude of the responses similarly for both perturbations. In simulated scenario (3), each perturbation induces one shared response and one unique response. In this case, the shared response amplitude is correlated with the cell state pseudotime, and the unique responses are anti-correlated with the

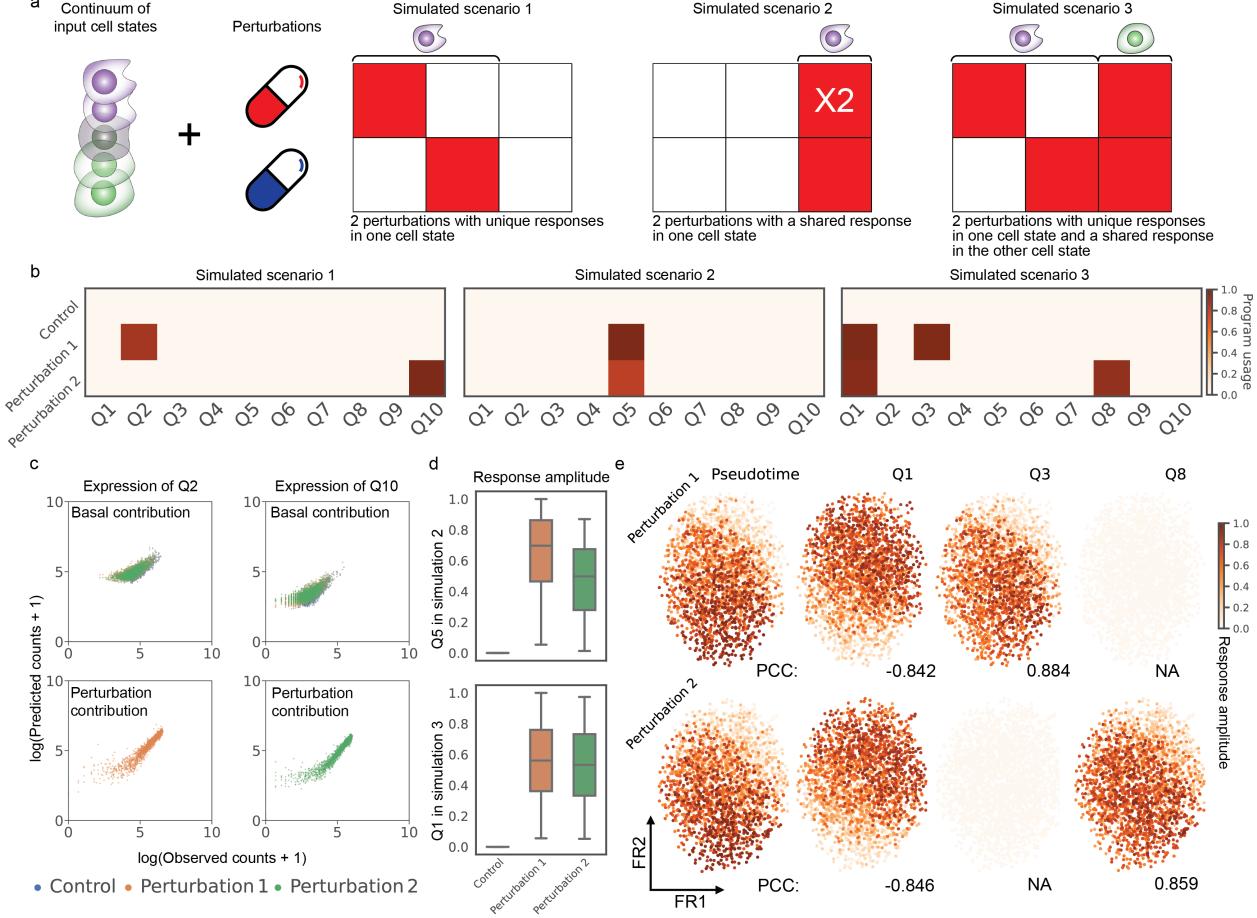


Figure 2: Exploring CellCap's model identifiability using simulated data. (a) Graphical setup of 3 simulated scenarios. (b) Usage of each transcriptional response program discovered by CellCap (h_{nq} averaged over cells). Automatic relevance determination effectively turns off response programs that are not necessary to explain the data, in agreement with the ground truth. (c) The linear decoder is used to directly interpret the learned basal state $z_{nk}^{(\text{basal})}$ and the learned perturbation $\Delta z_{nk}^{(\text{pert})}$. Each dot represents the sum of all relevant genes in one cell for the indicated response program, and cells are colored by perturbation condition. CellCap learns a basal state where perturbations are indistinguishable (top panels), while learning response programs whose expression correlates with ground truth (bottom panels). (d) Amplitudes h_{nq} of the shared response programs (Q5 in scenario (2) and Q1 in scenario (3)) in each perturbation condition are presented with boxplots. (e) Visualization of per-cell response amplitudes h_{nq} for the 3 learned response programs in scenario (3). The leftmost Fruchterman-Reingold (FR) plots are colored by the ground truth cell state pseudotime, whereas h_{nq} is used to color the FR plots shown in rightmost three columns. The pseudotime hidden variable is the ground truth covariate of the cell state response amplitude (see Supplementary Sec. S.1 for details). Unique (shared) response programs are expected to be correlated (anti-correlated) with the pseudotime.

195 pseudotime.

196 In scenario (1), we expect that CellCap should identify two response programs and that each
197 response should be specific to one perturbation. Indeed, only two programs stand out after model
198 training (Fig. 2b). CellCap also ascertains that there is only one relevant response program in
199 scenario (2) and three in scenario (3). In scenario (2), CellCap identifies response program Q_5
200 as a shared program induced by both perturbations (Fig. 2b). In scenario (3), CellCap identifies
201 response program Q_1 as the shared program, and response programs Q_3 and Q_8 as the programs
202 specific to perturbation 1 and perturbation 2, respectively (Fig. 2b). We also note that in all cases,
203 we have allowed CellCap to learn and use up to 10 response programs. However, the ARD sparsity-
204 inducing mechanism in CellCap correctly “turns off” the unnecessary transcriptional programs.

205 Next, we examined whether CellCap accurately decomposed the observed gene expression into
206 basal state (cell state) and response program in the latent space. To this end, we decoded the
207 learned $\mathbf{z}^{(\text{basal})}$ to obtain the predicted basal gene expression matrix. Our expectation is that
208 the results would be the same across all three conditions, and only exhibit the variation related to
209 pseudotime and not the specific perturbations. We further decoded the complete latent state vector
210 $\mathbf{z} = \mathbf{z}^{(\text{basal})} + \Delta\mathbf{z}^{(\text{pert})}$ to predict a full gene expression matrix. We subtracted the predicted basal
211 gene expression matrix from the full gene expression matrix to obtain the predicted perturbation-
212 induced gene expression. As expected, we found the basal state expression to be indistinguishable
213 among control and perturbed cells, and the expression of response programs to be perturbation-
214 specific (Fig. 2c). Additionally, CellCap successfully decomposed the observed gene expression into
215 basal state and response programs in scenarios (2) and (3) (Supplementary Fig. S1). Meanwhile,
216 we found that CellCap accurately learns response programs that match the simulated ground truth
217 (Supplementary Fig. S2).

218 As mentioned earlier, the two perturbations induce a shared response program in both scenarios
219 (2) and (3), with an unequal response amplitude in scenario (2) and an equal response amplitude in
220 scenario (3). We found that CellCap correctly identified this difference in scenario (2) and reported
221 similar response amplitudes in scenario (3) (Fig. 2d). In scenario (3), we have set up a situation in
222 which the shared response program’s amplitude should be negatively correlated with the basal state
223 “pseudotime”, in contrast to the unique response programs which are positively correlated with
224 basal state pseudotime. The response amplitude h_{nq} reported by CellCap in scenario (3) was highly
225 correlated with ground truth (Pearson correlation coefficient 0.884 for Q_3 in perturbation 1 and
226 0.859 for Q_8 in perturbation 2). As for the shared program, CellCap recovered a shared response
227 program Q_1 that captures the negative correlation with ground truth basal state, with Pearson
228 correlation coefficient -0.842 in perturbation 1 and -0.846 in perturbation 2 respectively (Fig. 2e).
229 In summary: (1) CellCap was able to identify shared and unique programs for two perturbations;
230 (2) CellCap could distinguish different response amplitudes; and (3) CellCap learned the correct
231 correspondence between basal cell state and perturbation response.

232 2.3 CellCap reveals heterogeneous responses in pathogen-exposed 233 human monocytes

234 We next sought to demonstrate the utility and interpretability of CellCap in real single-cell pertur-
235 bation data. To this end, we used CellCap to reanalyze a previously published pathogen-exposed
236 human peripheral blood mononuclear cell scRNA-seq dataset. In the original report, Oelen *et*
237 *al.* identified differentially expressed (DE) genes by comparing each treatment condition against
238 untreated control for every major cell type [20]. They observed the largest number of DE genes
239 in monocytes across different pathogen exposure conditions, and they concluded that monocytes
240 are the cell type with the strongest response to pathogens. Another highlight of their analysis is
241 that the interferon signaling pathway is specifically enriched at 3 hours post-exposure in mono-
242 cytes and that this response pathway is common to all three pathogens. The original analysis did
243 not leverage the single-cell resolution of the dataset for studying the complex and heterogeneous
244 cell-state-dependent responses to pathogen exposure. Here, we show that CellCap can be utilized
245 to uncover such novel insights about cellular responses at an increased granularity. The steps
246 outlined below demonstrate the overall workflow other practitioners could use to leverage CellCap

247 in studying their single-cell perturbation experiments.

248 First, we limited the scope of our analysis to the monocytes in the dataset, since this was
249 the cell type observed to exhibit the strongest responses in the original study. We noticed that
250 CellCap's encoding of cell states from different conditions into the shared basal state $z_{nk}^{(\text{basal})}$ results
251 in excellent mixing between the pathogen-exposed group and the untreated (UT) group (Fig. 3a).
252 We recall that the basal state representation should preserve only intrinsic cell state variations and
253 not the perturbations themselves. Examining the learned usage of each response program by each
254 perturbation condition, we were able to paint an overall picture of the relationship between the
255 6 treatment conditions by performing principal component analysis (PCA) on the perturbation
256 signatures, i.e. the rows of H_{pq} . In particular, PC1 separated the conditions by time post exposure:
257 all treatments 3 hours (3h) post pathogen exposure – *C. albicans* (CA), *M. tuberculosis* (MTB),
258 and *P. aeruginosa* (PA) – were closely grouped in the PC space, while all 3 treatments 24 hours
259 (24h) post pathogen exposure were located on the right side of the plot (Fig. 3b). Importantly,
260 this indicates that the top PC of response program usage by perturbation is the time post exposure
261 rather than the pathogen itself. Of note, pathogen exposure with PA was distinct from the other
262 two pathogens at the 24h timepoint. We further examined h_{nq} , the usage of each response program
263 by individual cells, and averaged over the top 90 percent of cells with the highest responses to the
264 treatment conditions (Fig. 3c). We observed that all 3 treatments 3h post pathogen exposure
265 primarily induce two programs (Q6 and Q9) but that all treatments 24h post pathogen exposure
266 induce more diverse response programs, including Q3, Q4, Q7, Q8, and Q10 (Fig. 3c). We also
267 note that Q2 and Q5 were not used, i.e. they were turned off during the course of model training,
268 suggesting that the experiment can be succinctly interpreted using 8 response programs.

269 Having obtained a global understanding of both the heterogeneity of basal cell states within the
270 monocyte population (Fig. 3a) and the relationships between different treatment conditions (Fig.
271 3b and c), we next examined the way in which transcriptional response programs are activated
272 in different basal states of monocytes. We started with program Q3, which is common to all 3
273 treatments 24h post pathogen exposure. Response amplitudes h_{nq} of individual cells 24 hours
274 after CA exposure show that the response program Q3 is enriched in a certain sub-population
275 of monocytes (Fig. 3d). We then examined the characteristics of cell states within this sub-
276 population of monocytes. To this end, we used the perturbation key κ_{pqk} for response program
277 Q3 at 24h post CA exposure to query the basal state $z_{nk}^{(\text{basal})}$ of the UT group. We assigned to
278 each untreated cell a relevance score (computed using cosine similarity) to represent the likelihood
279 of this cell to respond with program Q3 in the 24h post CA exposure condition given its basal
280 state (Supplementary Fig. 3a). We used this relevance score to identify the corresponding basal
281 expression program enriched in cells with a high relevance score (see Methods).

282 The basal expression program included top upregulated genes *ISG15*, *CCL2*, *ISG20*, and *IL7R*
283 (Fig. 3e left panel). We then identified the most highly responding genes in response program
284 Q3 (Fig. 3e right panel). We noted a striking correspondence between basal expression of specific
285 genes (Fig. 3e left) and the activation of Q3 (Fig. 3e right) in response to CA exposure at the
286 24h timepoint. Gene set enrichment analysis (GSEA) indicates that the response program Q3 is
287 enriched for pathways involved in Rho GTPase activation and DNA replication with $\text{FDR} \leq 0.1$
(Fig. 3f).

288 Using the same approach, we identified the basal expression program which results in a high
289 response of program Q6 in the 3h post CA exposure condition (Fig. 3g-i and Supplementary Fig.
290 S3b). We also examined the averaged and individual expression patterns of responding genes in Q3
291 and Q6 to confirm substantial perturbation changes from the untreated group (Supplementary Figs.
292 S4 and S5). The primary observation is that treatments 3h post exposure induce a higher response
293 of the interferon signaling pathway, and this response is enriched in non-classical monocytes with
294 marker genes *FCGR3A* and *HES4* identified in basal cell state expression. This result is consistent
295 with the finding in the original report, which used a multi-step analysis (clustering, cell state
296 annotation, and case-control comparison) [20]. CellCap not only automates this discovery workflow
297 within a unified end-to-end model, it also uncovers novel response patterns which we briefly outline
298 below.

299 Additional response patterns identified by CellCap are shown in Fig. 3j and Supplementary Fig.

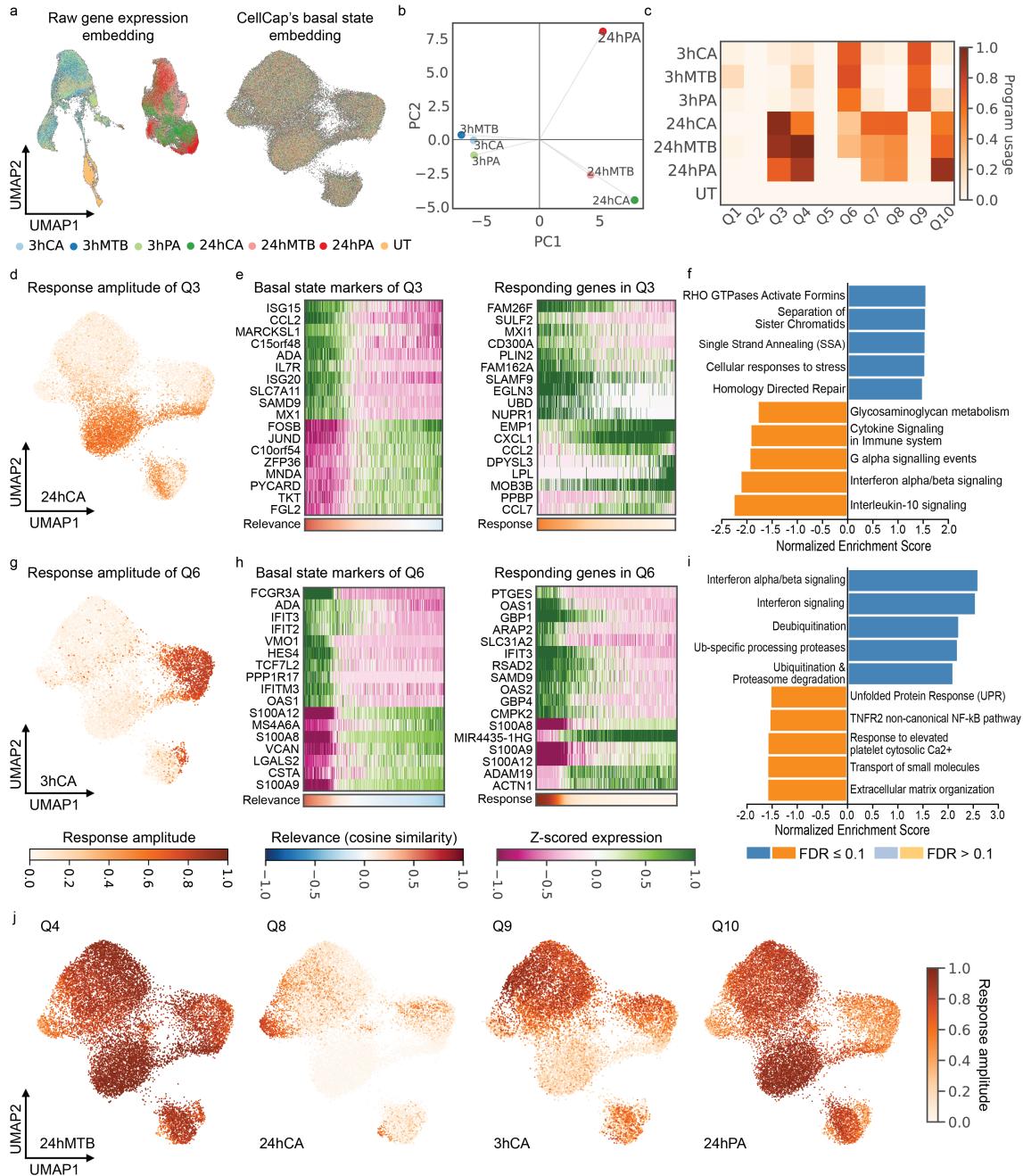


Figure 3: CellCap reveals heterogeneous responses in pathogen-exposed human monocytes. (a) The left and right UMAPs show the embedding of the raw gene expression and CellCap-inferred corresponding basal states, respectively. CellCap learns a basal latent space in which cells from all perturbation conditions are well-mixed. (b) General relationship between 6 pathogen-exposure conditions, visualizing H_{pq} using principal component analysis. (c) Program usages in each condition, h_{nq} , summed over responding cells in each perturbation group (see Supplementary Section S.2). (d) Per-cell response amplitudes h_{nq} of program Q3 in the 24hCA perturbation condition. (e) Top basal marker genes and responding genes in Q3. Top up- and down-regulated genes are shown to highlight expression patterns on both extremes. (f) GSEA for response program Q3. Top 5 positive and top 5 negative pathways are shown. (g) Per-cell response amplitudes of program Q6 in the 3hCA perturbation condition. (h) Top basal marker genes and responding genes in Q6. Top up- and down-regulated genes are shown to highlight expression patterns on both extremes. (i) GSEA for response program Q6. (j) Other major cell-state-specific response patterns identified by CellCap. Further investigation of these patterns is shown in Supplementary Figs. S6-S10. Abbreviations: [3hCA = 3 hours post *C. albicans* exposure, 24hCA = 24 hours post *C. albicans* exposure, GSEA = gene set enrichment analysis]

301 S6. With these patterns in hand, we identified all major basal expression programs and performed
302 soft annotation to assign cellular identities to different sub-populations of monocytes in the basal
303 state without clustering (Supplementary Fig. S7). One salient example is the enrichment of Q8 in
304 a small population of monocytes at 24h post CA exposure. We identified its corresponding basal
305 expression program using the same approach as above (Supplementary Fig. S8). As mentioned
306 earlier, PA pathogen exposure is distinct from the other two pathogens at the 24h timepoint. A
307 possible explanation for this difference could be the enrichment of response program Q10 in one
308 particular sub-population. Q3 is enriched in the same sub-population of monocytes in the all 24h
309 post exposure conditions. However, cells in this sub-population show a higher response of Q10 to
310 24h PA than to the other two pathogens at 24h. Averaged expression patterns of perturbed genes
311 in Q3 and Q10 indicate that Q3 is a shared program across the 3 pathogens but Q10 is specific
312 to PA exposure (Supplementary Fig. S9). In Q10, we identified macrophage markers like *APOE*,
313 *APOC1*, and *RNASE1* (Supplementary Fig. S10). This result suggests a possibility that cells in
314 this sub-population of monocytes (with basal marker genes *ISG15*, *CCL2*, *ISG20*, and *IL7R*) would
315 gain the potential to differentiate into macrophages after 24 hour exposure to PA. We remark that
316 this nuanced finding enabled by CellCap was not part of the original report by Oelen *et al.* [20].

317 2.4 CellCap captures complex patterns in large-scale genetic per- 318 turbation data

319 We next used CellCap to analyze a single-cell Perturb-seq dataset by Norman *et al.* [21]. The
320 study used CRISPR activation to over-express transcription factors in the K562 cell line at large
321 scale, including 105 single-target perturbations and 131 pairwise combinatorial perturbations. In
322 CellCap, this experimental design can be readily encoded as a design matrix $P_{np} \in \{0, 1\}$ (with
323 the p dimension of size 105), where $\sum_p P_{np} = 1$ for the cells receiving single-target perturbations,
324 and $\sum_p P_{np} = 2$ for the cells receiving double-target perturbations. We initially set up a maximum
325 of $Q = 50$ response programs for CellCap to learn. Following model training, we observed that a
326 majority of programs were turned off, leaving only 10 programs shared by the 236 perturbations
327 (Supplementary Fig. S11).

328 We obtained averaged perturbation response signatures, defined as the learned usage of each
329 response program averaged over responding cells (see Supplementary Section S.2) stratified by
330 each of the 236 perturbation conditions. We performed UMAP dimensionality reduction on the
331 obtained average perturbation signatures for visualization, and we clustered the signatures (Fig.
332 4a). This clustering largely agrees with the findings in the original study by Norman *et al.* [21]
333 and a reanalysis done by Roohani *et al.* [11]. Norman *et al.* clustered the perturbations using a
334 pseudo-bulk approach, while Roohani *et al.* used their proposed deep learning method GEARS.

335 We focused on 4 of these perturbation clusters for downstream investigation. Ranking the
336 perturbations by their usage of response program Q29, we found that the top ranked perturbations
337 primarily involve the activation of *KLF1* as well as *KLF1*-included combinatorial perturbations
338 (Fig. 4b). We noticed that perturbations like *AHR*, *BAK1*, *DUSP9*, *SET* are ranked lower than
339 their combinational perturbations with *KLF1* in response program Q29 (Fig. 4b). We wondered
340 whether response program Q29 is primarily driven by activation of *KLF1*. We examined the
341 expression of top responding genes in Q29 in perturbation conditions involving the activation of
342 *KLF1*, *AHR*, *BAK1*, *DUSP9*, *SET*, and their pairwise combinations *KLF1/AHR*, *KLF1/BAK1*,
343 *KLF1/DUSP9* and *KLF1/SET*. We found that the top responding genes in response program
344 Q29 are primarily expressed in *KLF1*-activated perturbations but not in *AHR*, *BAK1*, *DUSP9*-
345 or *SET*-activated perturbations (Supplementary Fig. S12). This indicates that response program
346 Q29 is mainly caused by activation of *KLF1*, with no or little dependence on the presence of *AHR*,
347 *BAK1*, *DUSP9* or *SET* activation.

348 Activation of *KLF1* has been shown to promote erythropoiesis [22, 23]. However, the analyses
349 in both Norman *et al.* [21] and Roohani *et al.* [11] categorized perturbations with activation
350 of *KLF1* as “pro-growth”. We performed GSEA and found that response program Q29 might
351 be related to metabolic processes or proteasome activation (Fig. 4c). Meanwhile, CellCap iden-
352 tified lymphocytes marker genes in response program Q29. These lymphocytes markers include

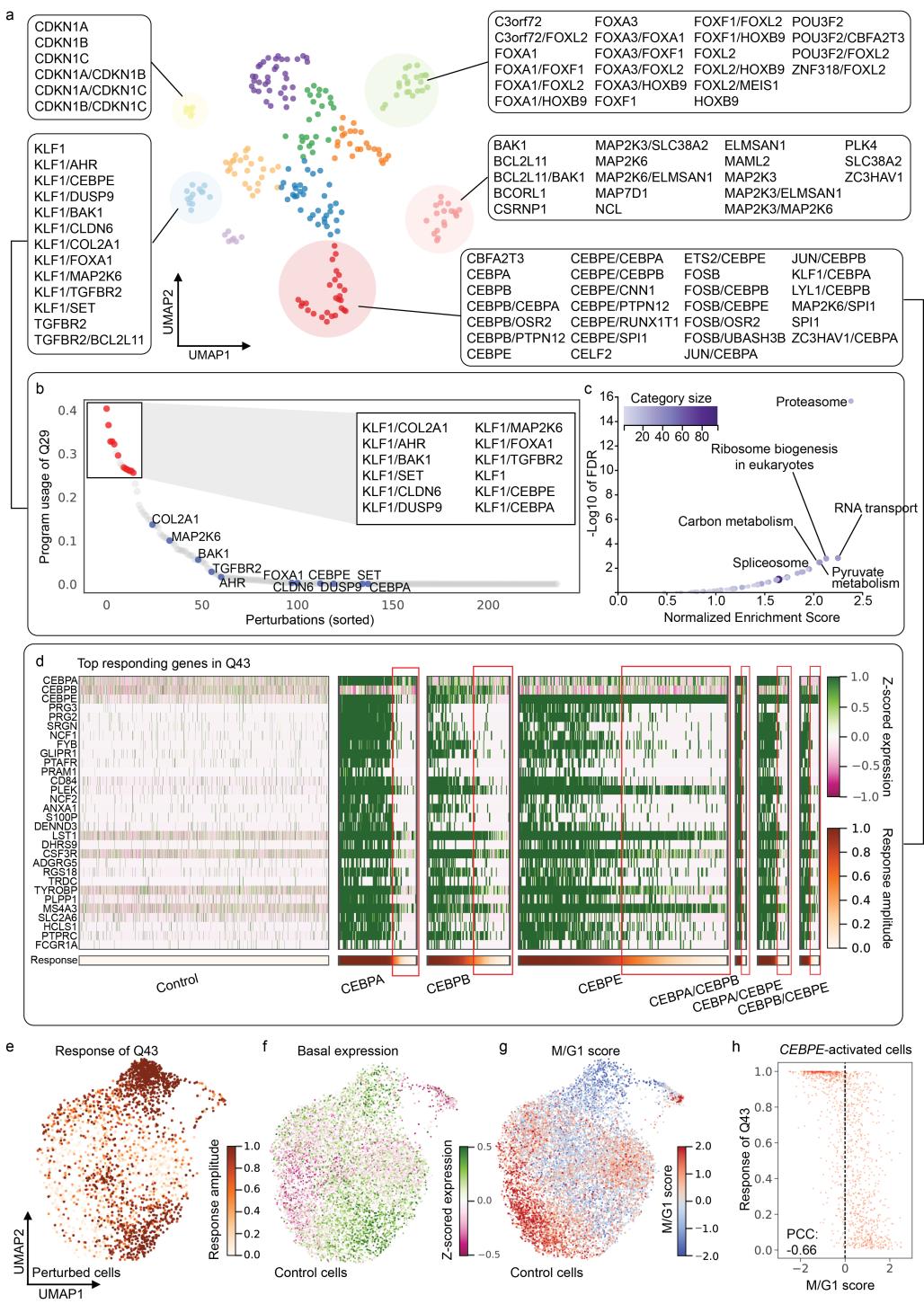


Figure 4: CellCap captures complex relations between genetic perturbations in large screens (data from Norman et al. [21]). (a) UMAP visualization of the relatedness of 236 perturbations obtained from the program usages inferred by CellCap (Supplementary Section S.2). Perturbations are colored by K-means clustering, highlighting 5 perturbation clusters. (b) Perturbations ranked by usage of the response program Q29. Perturbations involving *KLF1* activation are colored in red while others are colored in grey. Blue dots highlight the single-target perturbations (that lack *KLF1* activation) corresponding to those red perturbations. (c) GSEA results showing significant KEGG pathways related to response program Q29. KEGG pathways with $FDR \leq 0.1$ are highlighted. Dot size and color are proportional to the size of the gene set. (d) Expression of top responding genes in program Q43. For each perturbation, cells are ordered from the highest Q43 response amplitude to the lowest. (e) Per-cell usage h_{nq} of the Q43 response program are shown on the basal state UMAP for all the perturbed cells from panel (d). (f) The basal state UMAP of control cells showing the average z-scored expression of the top basal state marker genes that correspond to program Q43. (g) Same basal state UMAP showing M/G1 score for control cells. (h) Quantitative comparison of M/G1 score and Q43 response amplitude in *CEBPE*-activated cells reveals a strong correlation.

353 *CD3G*, *CD80*, and *IL2RG* (Supplementary Fig. S12). Response program Q29 also includes other
354 non-specific markers. For example, *TRABD2A* and *NMU* also have high expression in lympho-
355 cytess. Based on this, we hypothesize that *KLF1* activation in K562 cells could serve to enhance
356 lymphocytes identity.

357 Both Norman *et al.* and Roohani *et al.* identified the group of perturbations that includes
358 *CNN1*, *CBL*, and *UBASH3B* as “erythroid”. Consistent with their analyses, CellCap also identified
359 that erythroid markers like *HBE1*, *HBC1*, and *HBC2* are highly ranked in the response program
360 Q7 shared by these perturbations (Supplementary Fig. S13). Interestingly, CellCap also revealed
361 *KLF1* as one of top responding genes in response program Q7, suggesting *KLF1* may promote
362 erythropoiesis indeed [22, 23]. Although both Norman *et al.* and Roohani *et al.* labeled the group
363 of perturbations that includes *FOXA1*, *FOXA3*, and *FOXL2* as “pioneer factors”, a detailed
364 description of shared perturbation responses in this group is missing. Here, CellCap identified
365 that this group of perturbations shares response program Q22, which includes top responding
366 genes like *LYZ* and *ID3* (Supplementary Fig. S14).

367 We next focused on response program Q43, which is most strongly induced by activation
368 of *CEBPA*, *CEBPB*, *CEBPE*, and their combinatorial perturbations. Both Norman *et al.* and
369 Roohani *et al.* classified this group as granulocytes [11, 21]. CellCap identified neutrophil markers
370 in Q43, including *LST1* and *CSF3R* (Fig. 4d), showing great agreement with previous analyses.
371 Weinberger *et al.* also reanalyzed this Perturb-seq dataset with a primary focus on this group
372 of perturbations [24]. By visualizing a few neutrophil marker genes, they confirmed that only a
373 certain population of cells in which *CEBEB* and/or *SPI* are activated would differentiate towards
374 neutrophils. However, Weinberger *et al.* did not highlight the heterogeneity in response amplitudes
375 at the single-cell level in the *CEBPB* and *SPI*-activated perturbations. CellCap reveals that
376 this heterogeneity in per-cell response magnitude occurs in all perturbations involving *CEBPA*,
377 *CEBPB*, *CEBPE*, and their combinations (Fig. 4d: highlighted with red boxes). Expression levels
378 of genes *CEBPA*, *CEBPB*, and *CEBPE* (the target genes) suggest that this heterogeneity is not
379 likely due to a failure to activate the target gene in these cells (Fig. 4d: top 3 rows). For example,
380 the gene *CEBPE* is robustly activated in all perturbed cells in the *CEBPE* perturbation group,
381 even though the cells highlighted by the red box show a much lower level of the Q43 response
382 program.

383 This motivated us to examine the basal cell state to understand if some intrinsic, pre-existing
384 cellular variation would explain this phenomenon. We computed a cosine similarity between the
385 perturbation key κ_{pqk} of *CEBPA*, *CEBPB*, *CEBPE* or *SPI1* and the basal state z_{nk}^{basal} of control
386 cells, and we identified a basal program related to response program Q43. We compared the pattern
387 of response amplitudes of program Q43 in perturbed cells (Fig. 4e) with the average expression
388 of the related basal program in control cells (Fig. 4f), and we confirm that the patterns match.
389 Regarding this related basal program, the unperturbed K562 cells with high cosine similarity
390 to all 4 perturbations already present low expression of the granulocytes marker genes *CSF3R*,
391 *LST1*, *LGALS1*, and *APOC1* (Supplementary Fig. S15). This indicates the existence of or
392 ongoing differentiation towards granulocyte lineage in unperturbed K562 cells. CellCap finds that
393 cells which display some granulocyte markers in the basal state will continue on a path toward
394 granulocyte differentiation as a response to *CEBP** activation.

395 CellCap also indicates that cell cycle stage is anti-correlated with Q43 response. We visualized
396 cell cycle patterns in control cells (Fig. 4g and Supplementary Fig. S16) and confirmed that
397 a per-cell M/G1 score shows strong anti-correlation with the magnitude of Q43 response (Fig.
398 4h; with additional perturbations shown in Supplementary Fig. S17). CellCap pinpoints the cell
399 cycle genes that are anti-correlated with program Q43. This anti-correlation is especially strong
400 for *CENPA*, *CENPE* and *CENPF*, which are known marker genes for the M stage. Cells with
401 lower Q43 response amplitudes tend to have higher expressions of *CENPA*, *CENPE* and *CENPF*
402 (Supplementary Fig. S18). Weinberger *et al.* also found that cell cycle is a shared variation across
403 conditions [24]; however, their analysis did not uncover the anti-correlation between M/G1 score
404 and the transcriptional response to activation of *CEBPA*, *CEBPB*, and/or *CEBPE*. CellCap’s
405 nuanced findings suggest a possibility that cells that already show signs of differentiation towards
406 granulocytes and are not in G1/M phase would have higher response to activation of *CEBPA*,

407

CEBPB, and *CEBPE*.

408

3 Discussion

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In this study, we developed the computational method CellCap for end-to-end analysis of single-cell perturbation experiments. CellCap models an interpretable correspondence between cell states and perturbation responses and enables multiple downstream applications. We demonstrated the utility of CellCap and the consistency of its findings using both simulated and real single-cell perturbation datasets. Our reanalysis of pathogen-exposed human monocytes data from Oelen *et al.* [20] uncovered novel cell-state-dependent responses following pathogen exposure. In particular, we found a sub-population of monocytes that exhibit macrophage differentiation potential 24 hours after *P. aeruginosa* exposure, a finding that was overlooked in the original study. Our reanalysis of genetic perturbation data collected by Norman *et al.* [21] demonstrated agreement with previous analyses while also providing further insights into the ways in which the effects of genetic perturbations can be nuanced in relation to cell states.

420

The methodological innovations of CellCap are to be understood in relation to the existing methods developed in this domain which put different degrees of emphasis on interpretability and prediction accuracy. One of the key concepts underlying CellCap is that each cell is endowed with “basal state”, an inferred pre-perturbation transcriptional state that encodes intrinsic cell state variation. While we have borrowed this idea from the CPA model [12], we emphasize that the end goal of CellCap is interpreting and decomposing single-cell perturbation responses into a dictionary of response programs, in contrast to predicting unseen perturbation effects accurately. Even though both CPA and CellCap aim to model the correspondence between basal cell state and perturbation response, the interpretive advantage of the CellCap model lies in the additional structure imposed on the latent space operations. CellCap learns this correspondence explicitly in the form of attention weights that signify the coupling between basal state sub-populations, learned response programs, and the usages of these response programs within each perturbation condition. While CPA has the potential to exhibit greater accuracy at predicting perturbation effects in unseen conditions (using high-dimensional latent spaces and nonlinear decoders), CellCap’s utility lies in the complementary role it plays in dissecting perturbation experiments and transforming observed cellular responses into biological insights.

436

The computational tool contrastiveVI [24] encodes single-cell perturbation data into independent “shared” and “salient” latent spaces, and is another valuable method for dissecting single-cell perturbation data. The concepts of “shared” and “salient” representations in contrastiveVI have semblance to the separable basal state and perturbation representations in CellCap and CPA. One key difference is that contrastiveVI does not model the correspondence between the “shared” and “salient” components (i.e. the equivalent of CellCap’s attention structure), and as such, the model does not explicitly uncover the relationship between perturbation response and cell states. This difference was demonstrated by the results highlighted in Section 2.4 in which we reanalyzed the Perturb-seq data from Norman *et al.* [21]. CellCap was able to uncover previously unnoticed patterns in heterogeneous perturbation responses caused by interpretable differences in cellular basal state – in this case, pre-existence of granulocytes lineage and cell cycle phase. Learning the correspondence between basal cell state and perturbation response not only enhances interpretability, but also gives CellCap greater statistical power for response program discovery as opposed to more direct differential expression testing methods, which find transcriptional responses that are averaged over responding and non-responding cells.

451

Unsupervised Bayesian models such as CellCap, though highly effective in extracting insights from new datasets, come with certain trade-offs and practical considerations. One of these challenges involves determining appropriate hyperparameter values. For instance, the line between a “shared” and “unique” response program can be hard to draw in certain cases. There is a necessary trade-off between the model’s ability to explain the data *accurately* and its ability to explain the data *concisely*. Shared response programs lend interpretability to the output, but a model that finds additional unique responses for each perturbation can provide a better fit to the data. We

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458 make this trade-off transparent and explicit in CellCap by means of a hyperparameter that controls
459 the weight given to automatic relevance determination in the optimization objective function. A
460 larger value will encourage CellCap to explain the data using fewer response programs, whereas
461 a smaller value will encourage the model to reconstruct the data more accurately at the expense
462 of learning more response programs. This trade-off is discussed in more detail in Methods 4.1.6.
463 Researchers are encouraged to carefully scrutinize the hyperparameters for each dataset, making
464 thoughtful choices to align with other relevant factors and the overarching objectives of the study.

465 It is essential to learn a biologically meaningful basal state in both CellCap and CPA, akin to
466 the “shared” representation in contrastiveVI. However, there are scenarios where inferring the basal
467 state could prove challenging without gathering time courses of higher resolution. For instance, in
468 a diving cell culture, perturbations could lead to the emergence of a new cell state, coupled with the
469 elimination of specific cell sub-populations and/or a near-total loss of the original cell state post-
470 perturbation. Along these lines, Weinberger *et al.* have commented that the results produced by
471 contrastiveVI can be misleading if the “shared” background variations are not present in perturbed
472 cells [24]. Likewise, CellCap is likely to fail to correctly project perturbed cells back to the pre-
473 perturbation basal state, one that matches the distribution of control cells, if the perturbed cells
474 have undergone significant reprogramming or passages. The evidence for such a failure mode would
475 be (1) obtaining basal state distributions that do not match the state of unperturbed control cells,
476 combined with (2) the use of excessively large values for the hyperparameter γ that controls the
477 alignment between basal state distributions across different conditions (see 4.1.6 in Methods). In
478 such a case, downstream analyses and other CellCap inferences are questionable, and obtaining a
479 finer time course could provide the most robust remedy.

480 Careful consideration is essential when examining perturbation responses in diverse cell pop-
481 ulations. It is generally expected that the greater the heterogeneity within the cell population,
482 the more varied the perturbation responses will be. However, when conducting experiments with
483 multiple cell types and seeking to understand and analyze the impact of perturbations on each cell
484 type with the same level of detail, challenges may arise in choosing a single set of hyperparameter
485 values. For instance, cell types that exhibit strong responses may benefit from stronger ARD reg-
486 ularization to reduce the number of learned programs, but this decision may sacrifice granularity
487 in modeling the effects of perturbations in less responsive cell types. In our study, we specifically
488 trained CellCap on datasets featuring a single cell type, with a focus on addressing variations at
489 the fine-grained resolution of cell state. It is important to note that this limitation is not unique to
490 our methodology. For instance, GEARS must also be trained on a single cell type due to potential
491 variations in interactions between two perturbations in different cell type contexts [11]. Including
492 multiple cell types in the training of GEARS could result in compromised predictions.

493 In conclusion, we offer several recommendations for the practical application of CellCap. Firstly,
494 it is advisable to determine the desired resolution of variations. If the focus is on exploring hetero-
495 geneous responses at the nuanced level of cell state, it is recommended to narrow down to a single
496 cell type during the training of CellCap. Conversely, if the objective is to investigate more coarse-
497 grained response heterogeneity at the cell type level, all cell types can be included. Secondly, it is
498 crucial to ensure that the control group of cells encompasses all potential variations in the input
499 cell state. This necessitates a well-designed experiment where control cells and perturbed cells
500 originate from the same population, ensuring that the distribution of control cell states aligns with
501 the distribution of pre-perturbation cell states for the perturbed cells. Lastly, it is important to
502 acknowledge that certain hyperparameter choices, particularly the weight assigned to automatic
503 relevance determination, can impact the interpretation of results. While variations in hyperpa-
504 rameter values may yield slightly different outputs, they also present an opportunity for gaining
505 fresh perspectives on understanding the landscape of perturbation responses. We encourage users
506 to train CellCap with diverse setups and assess the model outputs using domain knowledge and
507 expertise.

508

4 Methods

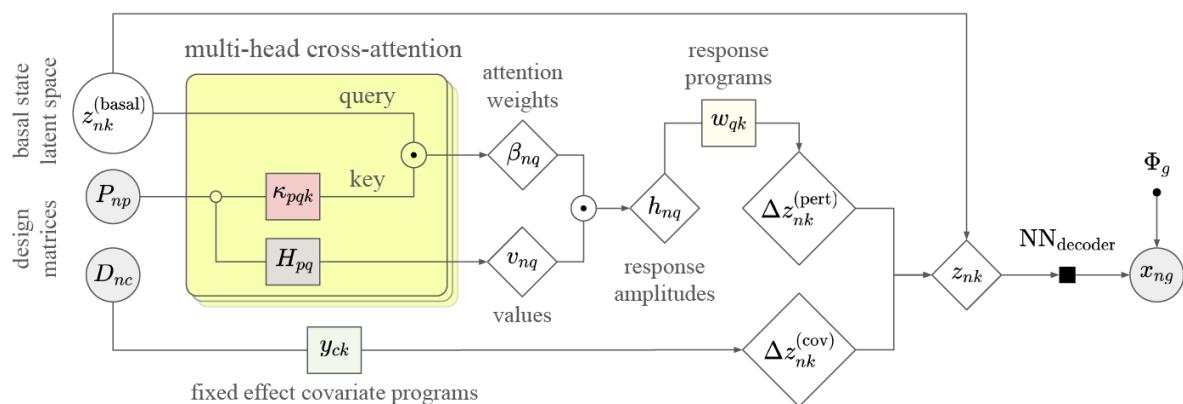
509 4.1 The CellCap model

510 CellCap is a probabilistic generative model for single-cell transcriptomics count data resulting from
 511 perturbation experiments, where groups of cells are subjected to different perturbation conditions.
 512 Perturbation responses are parameterized by linear combinations of learned “response programs”,
 513 which can be activated by one or more perturbations. An attention mechanism [17] is used to
 514 parameterize a correspondence between the “basal state” of a cell and the perturbation response
 515 amplitude, allowing the response to be heterogeneous at the single-cell level.

516 In designing CellCap, we draw inspiration from existing approaches that model single-cell
 517 perturbation data by leveraging latent space arithmetics, in particular the CPA model [12], and
 518 reconsider some of their design choices under the lens of model identifiability and interpretability.
 519 We pay much attention to where the nonlinearities appear in the model. In the CPA model, a
 520 linear latent space algebra gives rise to a latent representation of a cell which is put through a
 521 nonlinear decoder. In CellCap, we instead move the nonlinearity from the decoder to the latent
 522 space algebra, where an interpretable attention mechanism models the correspondence between cell
 523 state and perturbation response. The linear decoder allows us to interpret perturbation responses
 524 as the sum of linear “gene expression response programs” – programs which can be unique to
 525 one perturbation or shared across several perturbations – and which contribute to the measured
 526 response in a cell-state-dependent manner.

527 4.1.1 The CellCap generative process

528 A formal definition of the CellCap data generative process is given below, along with a glossary of
 529 random variables, intermediate quantities, and the implied meaning of subscript indices of various
 530 tensor quantities:



527 Figure 5: Probabilistic graphical model for the data generative process in CellCap. Observed data
 528 are depicted by shaded gray circles (P_{np} , D_{nc} , x_{ng}). Latent variables are in open circles ($z_{nk}^{(\text{basal})}$).
 529 Diamonds are deterministic computations (β_{nq} , v_{nq} , h_{nq} , $\Delta z_{nk}^{(\text{pert})}$, $\Delta z_{nk}^{(\text{cov})}$, z_{nk}). Rectangles of
 530 different shadings represent learnable parameters, as do nodes with dots (κ_{pqk} , H_{pq} , y_{ck} , w_{qk} ,
 Φ_g). $\text{NN}_{\text{decoder}}$ is a single-layer decoder neural network.

n	cell $\in 1 \dots N$
g	gene $\in 1 \dots G$
p	perturbation $\in 1 \dots N^{(\text{pert})}$
q	response program $\in 1 \dots Q$
c	fixed effect covariates $\in 1 \dots N^{(\text{cov})}$
k	latent space dimension $\in 1 \dots K$
$\kappa_{pqk}^{(i)}$	$P \times Q$ learnable K -dimensional vectors for each attention head i
P_{np}	perturbation “design matrix” indicating perturbation for each cell, values $\in \{0, 1\}$
H_{pq}	learnable non-negative matrix signifying the usage of response programs per perturbation
v_{nq}	value vectors which sum the relevant response programs for each cell
D_{nc}	$N \times N^{(\text{cov})}$ fixed effect “design matrix” indicating fixed effects for each cell
y_{ck}	$N^{(\text{cov})} \times K$ learnable matrix (fixed effect covariates)
h_{nq}	$N \times Q$ usage matrix of response programs
w_{qk}	$Q \times K$ learnable matrix of response programs in the latent space $\in (-1, 1)$ interval
x_{ng}	$N \times G$ observed count data $\in \{0, 1, 2, \dots\}$
ℓ_n	library size of cell n
α_q	the Laplace ARD prior scale factors $\in (0, 1)$ interval
Φ_g	negative binomial overdispersion of gene g

$$z_{nk}^{(\text{basal})} \sim \mathcal{N}(0, 1) \quad (1)$$

$$\kappa_{nqk}^{(i)} = \sum_p \kappa_{pqk}^{(i)} P_{np} \quad (2)$$

$$\beta_{nq} = \max_i \left[\text{softmax} \left(\frac{\tau}{\sqrt{K}} \sum_k \kappa_{nqk}^{(i)} z_{nk}^{(\text{basal})} \right) \right] \quad (3)$$

$$v_{nq} = \sum_p H_{pq} P_{np} \quad (4)$$

$$h_{nq} = \beta_{nq} v_{nq} \quad (5)$$

$$\Delta z_{nk}^{(\text{pert})} = \sum_q h_{nq} w_{qk} \quad (6)$$

$$\Delta z_{nk}^{(\text{cov})} = \sum_c D_{nc} y_{ck} \quad (7)$$

$$z_{nk} = z_{nk}^{(\text{basal})} + \Delta z_{nk}^{(\text{cov})} + \Delta z_{nk}^{(\text{pert})} \quad (8)$$

$$\chi_{ng} = \text{NN}_{\text{decoder}}(z_{nk}) \quad (9)$$

$$\ell_n = \sum_g x_{ng} \quad (10)$$

$$x_{ng} \sim \text{NegBinom}(\ell_n \chi_{ng}, \Phi_g) \quad (11)$$

531 $z_{nk}^{(\text{basal})}$ is a K -dimensional latent variable representing the “basal” (i.e. unperturbed) state of
 532 each cell, with a standard normal prior (Eqn. 1). The final latent representation of a cell, z_{nk} , is
 533 recomposed as the sum of $z_{nk}^{(\text{basal})}$ together with two “correction” terms: one for the perturbation
 534 itself, $\Delta z_{nk}^{(\text{pert})}$, and another for fixed linear covariates, $\Delta z_{nk}^{(\text{cov})}$. The simpler of these two terms,
 535 $\Delta z_{nk}^{(\text{cov})}$, is the matrix product of the covariate design matrix D_{nc} and the learnable linear fixed
 536 effects matrix y_{ck} . Linear fixed effects denoted in the design matrix D_{nc} can be used to effectively

537 “regress out” technical variation or other variation that is not the subject of the study, such as
 538 batch or donor (Eqn. 7).

539 The perturbation effect, $\Delta z_{nk}^{(\text{pert})}$, is modeled as a sum over independent response programs w_{qk}
 540 according to their usage by each cell, h_{nq} (Eqn. 6). h_{nq} is obtained as the product of a multi-head,
 541 scaled dot-product attention mechanism [17], whereby the effects of a given perturbation are made
 542 to depend upon the basal state of the cell. This is depicted graphically in Fig. 5. In the language
 543 of dot-product attention, the “keys” are κ_{nqk} , the “queries” are $z_{nk}^{(\text{basal})}$, and the “values” are v_{nq} .
 544 The keys are derived from the action of a learnable tensor κ_{pqn} on the perturbation design matrix
 545 P_{np} . Here, κ_{pqn} can be thought of as a dictionary containing $p \times q$ vectors in the K -dimensional
 546 latent space for each attention head i . β_{nq} represents the attention weights that quantify how much
 547 cell n attends to response program q (Eqn. 3). τ is a temperature hyperparameter which controls
 548 the sharpness of the distribution of attention weight over programs, and by default its value is 4
 549 so that the factor $\frac{\tau}{\sqrt{K}} = 1$ when $K = 16$, the default size of the latent space. The “value” vectors
 550 v_{nq} amount to picking out the response programs for the given cell’s perturbation(s) and summing
 551 them (Eqn. 4).

552 Much like the motivation for using multi-head attention (MHA) in natural language processing
 553 to capture different semantic views of the words in a given context, we interpret MHA here as
 554 a mechanism to capture the one-to-many correspondences between one basal state and different
 555 transcriptional response programs. The dot-product attention is computed separately for each
 556 head, and for each n and q , the highest attention score is taken across all heads (Eqn. 3). We
 557 deviate from the standard MHA implementation in using the max pooling operation to reduce the
 558 effect of multiple heads whereas the original implementation uses a linear combination.

559 The learned matrix w_{qk} can then be directly interpreted as latent-space response programs,
 560 which can be decoded to gene response programs via the linear decoder, i.e. $\text{NN}_{\text{decoder}}(w_{qk})$. As
 561 discussed by Svensson *et al.*, the single-layer decoder lends itself to model interpretation at the
 562 expense of a small increase in the reconstruction error [16].

563 Finally, the complete-information latent space vector z_{nk} , the sum of basal state and pertur-
 564 bation response, is put through the linear decoder $\text{NN}_{\text{decoder}}$ to obtain χ_{ng} , the normalized gene
 565 expression per cell (Eqn. 9). The count data itself, x_{ng} , is sampled from a negative binomial dis-
 566 tribution with mean χ_{ng} times the library size ℓ_n and with a learnable gene-specific overdispersion
 567 Φ_g (Eqn. 11) [14, 15]. As shown in Ref. [25], the zero observations in scRNA-seq data can be
 568 effectively accounted for by a negative binomial with appropriately tuned overdispersion without
 569 needing to resort to zero inflation to add artificial dropout.

570 4.1.2 The CellCap variational posterior

571 We fit CellCap using variational inference [26]. The posterior of CellCap’s only latent variable,
 572 $z_{nl}^{(\text{basal})}$, is approximated as:

$$z_{nk; \mu}^{(\text{basal})}[x_{ng}], z_{nk; \sigma}^{(\text{basal})}[x_{ng}] = \text{NN}_{\text{encoder}}(x_{ng}) \quad (12)$$

$$z_{nk}^{(\text{basal})} | x_{ng} \sim \mathcal{N}\left(z_{nk; \mu}^{(\text{basal})}[x_{ng}], z_{nk; \sigma}^{(\text{basal})}[x_{ng}]\right) \quad (13)$$

573 Here, we use a neural network to propose to parameterize the posterior distribution $p(z_{nk}^{(\text{basal})} | x_{ng})$,
 574 as in Kingma and Welling [26]. Surmising the complexity of the task of inferring the basal state
 575 from expression data, we use a deep neural network to this end. We note that this particular
 576 inference task is not constrained to be interpretable, justifying our use of a deep neural network.

577 4.1.3 Posterior regularization via adversarial classification

578 As at stands, the current model does not include a mechanism to ensure that the learned posterior
 579 distribution $z_{nk}^{(\text{basal})} | x_{ng}$ is indeed devoid of perturbation effects. Satisfying this condition, either
 580 rigorously or in approximation, is crucial for the correct behavior of CellCap and the interpretation

579 of its results: if perturbation effects, either entirely or in part, are subsumed by $z_{nk}^{(\text{basal})}$, the residual
 580 variation that is subject to explicit modeling via $\Delta z_{nk}^{(\text{pert})}$, would become non-existent or diminished.

581 As in the CPA model [12], we use an adversarial classification task to strip perturbation
 582 information out of the $z_{nk}^{(\text{basal})}$ latent space. We use a neural network, $\text{NN}_{\text{classifier}}$, to try to predict
 583 whether a given perturbation p was applied in cell n , $P_{np} \in \{0, 1\}$. This matrix P_{np} is the known
 584 design matrix given to CellCap as an input. We do the same for each of the covariates supplied in
 585 the covariate design matrix D_{nc} . We note that the inclusion of an adversarial loss can be formally
 586 related to the theory of posterior regularization by interpreting the adversarial loss term as a KL
 587 divergence, see Ref. [27, 28].

588 Unlike the CPA approach which uses a two-step minimax adversarial gradient update procedure,
 589 we apply a gradient reversal layer [29] as the first layer of our adversarial classifier, and we
 590 train the whole model with a single gradient update step. Due to the gradient reversal layer, the
 591 gradient updates that get applied to the adversarial classifier $\text{NN}_{\text{classifier}}$ encourage the classifier to
 592 perform better classification, while at the same time, the gradients that get applied to $\text{NN}_{\text{encoder}}$
 593 work against the classifier. This process effectively strips perturbation condition information out
 594 of the basal latent space.

595 4.1.4 Posterior regularization via automatic relevance determination

We additionally include a sparsity-inducing loss term as a form of automatic relevance determination (ARD) [18], inspired by the sparse Bayesian learning literature:

$$\mathcal{L}_{\text{ARD}} = \sum_{n,q} \left(\frac{|h_{nq}|}{\alpha_q} + \log 2\alpha_q \right). \quad (14)$$

596 This loss can be construed as the negative log likelihood of h_{nq} under a Laplace prior with zero
 597 mean and scale α_q . Intuitively, α_q determines the magnitude of response to program q . Performing
 598 maximum likelihood estimation over α_q induces sparsity in a data-driven fashion: all things being
 599 equal, the data likelihood under the model would be higher if it were to consolidate responses into
 600 a few programs q with nonzero h_{nq} by sending certain entries of $\alpha_q \rightarrow 0$.

601 We note that sparsity in the usage of response programs can be induced by placing an ARD
 602 prior on either h_{nq} or w_{qk} , and that to some extent this choice is arbitrary. So long as one of these
 603 variables is bounded, a shrinkage prior on the other performs model selection. In our case, we put
 604 the shrinkage prior on h_{nq} and bound $w_{qk} \in (-1, 1)$ interval. This way $\mathcal{L}_{\text{ARD}} \propto \mathcal{O}(N)$ so that
 605 the hyperparameter γ (below) is independent of the size of the dataset, since all pieces of the loss
 606 function scale as $\mathcal{O}(N)$.

607 4.1.5 The full loss function

In CellCap, the loss function is a sum of the variational evidence lower bound (ELBO) and the
 608 aforementioned adversarial loss, which acts as a posterior regularization to strip perturbation
 609 information out of the basal latent space. We include tunable hyperparameters α , β , and γ on
 various terms in the loss function (see below):

$$\mathcal{L}_{\text{reconstruction}} = -\log p_{\text{NegBinom}}(x_{ng} | \ell_n, \chi_{ng}, \Phi_g) \quad (15)$$

$$\mathcal{L}_{\text{ARD}} = -\log p_{\text{Laplace}}(h_{nq} | 0, \alpha_q) \quad (16)$$

$$\mathcal{L}_{\text{KL}} = \mathbb{D}_{\text{KL}} \left[q_{\phi} \left(z_{nk}^{(\text{basal})} | x_{ng} \right) \middle\| p \left(z_{nk}^{(\text{basal})} \right) \right] \quad (17)$$

$$\mathcal{L}_{\text{adversarial}} = - \sum_p \left[P_{np} \log \overleftarrow{q}_{\phi}(P_{np} | z_{nk}^{(\text{basal})}) + (1 - P_{np}) \log (1 - \overleftarrow{q}_{\phi}(P_{np} | z_{nk}^{(\text{basal})})) \right] \quad (18)$$

$$\mathcal{L} = \mathcal{L}_{\text{KL}} + \alpha \mathcal{L}_{\text{reconstruction}} + \beta \mathcal{L}_{\text{ARD}} + \gamma \mathcal{L}_{\text{adversarial}} \quad (19)$$

608 Here, $\mathbb{D}_{\text{KL}}[\cdot | \cdot]$ is the Kullback-Leibler divergence, and $\mathcal{L}_{\text{adversarial}}$ is a binary cross entropy loss
 609 summed over all perturbations. $\overleftarrow{q}_{\phi}(P_{np} | z_{nk}^{(\text{basal})})$ is the posterior binary probability distribution for

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 $P_{np} \in \{0, 1\}$ (i.e. whether or not perturbation p was applied to cell n), conditioned on the learned
basal cell state $z_{nk}^{(\text{basal})}$. Note that the left arrow indicates the application of a gradient reversal
layer as the first layer of the classifier network. The ϕ in $q_\phi(\cdot)$ denotes the bundle of learnable
parameters $\{\text{NN}_{\text{encoder}}, \text{NN}_{\text{classifier}}\}$.

614 4.1.6 Key model hyperparameters

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Each of the four main terms in the full loss function promotes a distinct learning objective. In order
to provide users with the flexibility to prioritize different learning objectives as needed, we equip
each term with a tunable coefficient as model hyperparameters. These include $\alpha \geq 0$ coefficient
to control $\mathcal{L}_{\text{reconstruction}}$, $\beta \geq 0$ coefficient to control \mathcal{L}_{ARD} , and $\gamma \geq 0$ coefficient to control
 $\mathcal{L}_{\text{adversarial}}$. (We note that one of the four loss terms can have its coefficient set to one without loss
of generality, so here we have arbitrarily fixed the coefficient of \mathcal{L}_{KL} to one.) While the choice of
proper hyperparameters can vary depending on the dataset, we provide rough guidelines for their
tuning based on our interpretation of the role of different terms in the total loss function. The
default values for these hyperparameters in CellCap are $\alpha = 2.0$, $\beta = 0.2$, and $\gamma = 1.0$. However,
we strongly advise users to explore the effects of varying these choices on their results.

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Promoting $\mathcal{L}_{\text{adversarial}}$ by increasing γ will encourage learning a well-mixed basal state represen-
tation. Supplementary Fig. S19 shows an example illustrating how small choices of γ can impair
the model’s ability to reach a decent fit, as illustrated by the lack of mixing in the left ($\gamma = 0$) and
middle ($\gamma = 0.1$) columns. Insufficient mixing in the basal state implies disrupting the required
compartmentalization of information needed for explicit modeling of $\Delta\mathbf{z}^{(\text{pert})}$. As expected, we
notice that the sought after response programs and their correct usage patterns only emerge for
 $\gamma = 1$ (right panel). We recommend users evaluate the receiver operating characteristic (ROC)
curve of the adversarial classifier to confirm if the model has reached a well-mixed solution for the
basal state. An acceptable fit of the basal state encoder should return adversarial classifier ROC
curves close to the diagonal line, such that cells from different perturbations are indistinguishable.

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Promoting $\mathcal{L}_{\text{reconstruction}}$ decreases the reconstruction error in decoding the recomposed latent
representation $z_{nk} = z_{nk}^{(\text{basal})} + \Delta z_{nk}^{(\text{pert})} + \Delta z_{nk}^{(\text{cov})}$ back to the original gene expression profile x_{ng} .
Given the influence of $\Delta z_{nk}^{(\text{pert})}$ in shaping the recomposed latent representation z_{nk} , promoting
the reconstruction loss term additionally drives learning a better and more nuanced description
of perturbations, often by learning additional response programs. We control the sparsity of the
response programs via the \mathcal{L}_{ARD} term with strength controlled by the β coefficient. Therefore, α
and β play conflicting roles. In practice, we have noticed that choosing the appropriate α and β
varies significantly from one dataset to another. For improved perturbation prediction, users can
increase α while decreasing β . However, doing so may render w_{qk} unnecessarily complicated and
difficult to interpret. Alternatively, increasing β will result in sparser transcriptional programs, as
demonstrated in Supplementary Fig. S20. Naturally, choosing very large values of β poses the risk
of attaining an over-simplified fit.

647 4.1.7 Key implementation details

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The CellCap model is implemented in Python on top of the `scvi-tools` framework for probabilistic
modeling of single-cell data [30]. The `scvi-tools` framework streamlines the implementation of
models following the setup of Kingma and Welling’s variational autoencoders for Bayesian inference
[26] and provides much of required logic for single-cell data loading and model training, leveraging
the PyTorch Lightning library. The reconstruction loss is evaluated by using single Monte Carlo
posterior samples of h_{nq} and $z_{nk}^{(\text{basal})}$ to compute χ_{ng} in the generative model. The adversarial
classifier is implemented as a dense neural network with 2 hidden layers and 1 output layer. Both
hidden layers have 128 neurons, and the last layer predicts a probabilistic perturbation assignment
matrix $P_{np}^{\text{pred}} \in (0, 1)$. A gradient reversal layer is inserted before the first hidden layer, for the
purpose of adversarial training.

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In practice, we found it quite beneficial for rapid model convergence to carefully initialize the
tensor $\kappa_{pqk}^{(i)}$ to a set of representative points from $z_{nk}^{(\text{basal})}$. We choose these representative points

660 using Louvain community detection to identify Q random “key” cells from the control group,
661 using their initial basal states as $\kappa_{pqk}^{(i)}$ for each perturbation and attention head. This ensures that
662 the key vectors start out in a configuration inside the distributional support of the basal state.
663 Poor initialization of $\kappa_{pqk}^{(i)}$ results in vanishing gradients due to the softmax operation and slow
664 convergence.

665 For datasets that have extreme class imbalance, we implemented a weighted random sampler to
666 balance the ratio of control and perturbed cells in each mini-batch during training. The sampling
667 weight for each condition was calculated as $N/(N_{\text{classes}} \times N_c)$, where N is the total number of
668 samples, N_{classes} is the number of classes, and N_c is the number of samples in class c . This
669 calculation is implemented in `sklearn.utils.class_weight.compute_sample_weight`. Training
670 of CellCap is equipped with NVIDIA Tesla T4 GPU. We use the AdamW optimizer to update
671 all trainable weights in the CellCap model. The initial learning rate is set to 10^{-3} followed by
672 reductions by a factor of 0.6 after each plateau, as implemented in PyTorch’s `ReduceLROnPlateau`
673 learning rate scheduler. We implemented early stopping, which is triggered if the loss does not
674 reduce for more than 50 epochs. Otherwise, training stops after reaching the maximum number
675 of epochs, which is 1000 in all cases in this study.

676 The number of cells and the number of perturbations vary across single-cell perturbation
677 datasets, which can influence the the total runtime of CellCap. For the real perturbation datasets
678 used in this study, the total runtime ranges from 1 - 2 hours on a single Nvidia Tesla T4 GPU.

679 Data Availability

680 Code to simulate all three scenarios and their ready-to-use data can be found at <https://github.com/broadinstitute/CellCap>. Raw data for pathogen-exposure human monocytes is
681 deposited at the European Genome-Phenome Archive (EGAS00001005376). A processed version
682 is hosted at <https://eqtlgen.org/sc/datasets/1m-scbloodnl.html>. Raw data from Norman *et*
683 *al.* is deposited at Gene Expression Omnibus (GEO), under accession number GSE133344. A pro-
684 cessed version of the Norman *et al.* data can also be found at <http://projects.sanderlab.org/scperturb>[31].

687 Code Availability

688 CellCap code and quick-start tutorials are available at <https://github.com/broadinstitute/CellCap>. To reproduce major results in this study, please follow the notebooks provided in the
689 CellCap GitHub repository.

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696 Disclosures

697 The authors declare no competing interests.

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