

1 A knockoff calibration method to avoid over-clustering in 2 single-cell RNA-sequencing

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16 **Abstract**

17 Standard single-cell RNA-sequencing (scRNA-seq) pipelines nearly always include unsupervised
18 clustering as a key step in identifying biologically distinct cell types. A follow-up step in these
19 pipelines is to test for differential expression between the identified clusters. When algorithms over-
20 cluster, downstream analyses will produce inflated P -values resulting in increased false discoveries. In
21 this work, we present **callback** (**C**alibrated **C**lustering via **K**nockoffs): a new method for protecting
22 against over-clustering by controlling for the impact of reusing the same data twice when performing
23 differential expression analysis, commonly known as “double-dipping”. Importantly, our approach
24 can be applied to a wide range of clustering algorithms. Using real and simulated data, we show
25 that **callback** provides state-of-the-art clustering performance and can rapidly analyze large-scale
26 scRNA-seq studies, even on a personal laptop.

27 **Main**

28 Recent advances in single-cell RNA sequencing (scRNA-seq) technologies have enabled the generation of
29 datasets that contain the transcriptomic profiles of thousands to millions of individual cells [1, 2]. Unless
30 an additional assay is paired with sequencing (e.g., CITE-seq [3]), cell type labels are not provided with
31 the corresponding genomic profiles. This has led to many scRNA-seq bioinformatic pipelines requiring
32 both (i) clustering to identify putative cell types based on shared gene expression covariation and (ii)
33 differential gene expression analysis between cells in each cluster to identify “marker genes” uniquely
34 expressed by each putative cell type. The most commonly used software packages, such as **Seurat** [4]
35 and **Scanpy** [5], perform these two steps on the same dataset. This double use of data is often referred
36 to as “circular analysis” or “double-dipping,” and is known to result in highly inflated P -values, even

37 in the null case when gene expression is identically distributed and there are no true groupings that
38 distinguish cell populations [6, 7]. Due to the miscalibrated test statistics produced by circular analyses,
39 it is challenging to assess whether the genes found to be differentially expressed between two putative cell
40 groups are “real” or solely identified due to chance based on the way that the cells are being partitioned
41 by the clustering algorithm that is being used. Importantly, simple solutions such as sample splitting
42 between cells do not appropriately correct for this type of post-selective inference [7].

43 Several methods have been recently developed to correct for post-selective inference after clustering.
44 These methods include: (i) an approximate test based on the truncated normal distribution [8], (ii) a data
45 splitting strategy that splits data at the level of individual gene counts [7], and (iii) using synthetic null
46 variables called knockoffs for calibrating hypothesis testing [6]. The point of each of these methods is to
47 identify an appropriate hypothesis testing significance threshold to account for the statistical inflation that
48 occurs due to the double use of data. However, none of these tests inform if (or how) the re-clustering
49 of cells should be done. They simply return a list of calibrated P -values. As a result, approaches
50 for protecting against over-clustering have recently been proposed including “single cell significance of
51 hierarchical clustering” (**sc-SHC**) and “clustering hierarchy optimization by iterative random forests”
52 (**CHOIR**) [9, 10]. Here, we introduce **callback** (**C**alibrated **C**lustering via **K**nockoffs): a method that
53 integrates the negative control variable framework of knockoffs [11, 12] to the problem of identifying the
54 number of clusters that have statistical support in a single-cell dataset. Our approach can be paired with
55 any existing clustering algorithm that has a hyperparameter for tuning the number of clusters and it
56 makes no strong assumptions about the input data. We statistically motivate the need for an algorithm
57 like **callback**, evaluate its utility against other recently proposed clustering correction methods, and
58 demonstrate its ability to efficiently scale to large-scale scRNA-seq studies.

59 The **callback** algorithm consists of three simple steps (Methods). First, we generate synthetic null
60 variables, formally called knockoff features [11], where we augment the single-cell data being analyzed
61 with “fake” genes that are known not to contribute to any unique cell type but that match the real data
62 in distribution. Second, we perform both preprocessing and clustering on this augmented dataset. Third,
63 we calibrate the number of inferred clusters by using a hypothesis testing strategy with a data-dependent
64 threshold to determine if there is a statistically significant difference between groups and if re-clustering
65 should occur (Fig. 1a). The synthetic knockoff genes act as negative control variables; they go through
66 the same analytic steps as the real data and are presented with the same opportunity to be identified
67 as marker genes. The **callback** algorithm uses the guiding principle that well-calibrated clusters (i.e.,
68 those representing real groups) should have statistically significant differentially expressed genes after
69 correcting for post-selective testing, while over-clustered groups will have greatly fewer. We use this rule
70 to iteratively re-cluster cells until the inferred clusters are well-calibrated and the observed differences in
71 expression between groups are not due to the effects of double-dipping.

72 As a simple proof-of-concept, we simulated single-cell gene expression data to compare the clusters
73 found by the widely used Louvain algorithm with default parameter settings in **Seurat** (with the
74 **FindClusters** function where the resolution parameter is set to 0.8) versus using the same Louvain al-
75 gorithm paired with **callback**. We generated data under two scenarios. In the first scenario, there was
76 only one true “cell type”. Here, the default approach with **Seurat** incorrectly identified four clusters
77 while **callback** correctly identified only a single cluster (Fig. 1b). In the second scenario, we simulated
78 the data such that there were three true cell types. In this case, the **Seurat** default incorrectly identified
79 four clusters by splitting the larger group into two clusters whereas **callback** correctly identified three
80 clusters (Fig. 1c).

81 To evaluate the performance of **callback** on real single-cell RNA sequencing studies, we analyzed 20
82 different tissues from the Tabula Muris dataset [13]. We compared **callback** with two recently proposed
83 methods for preventing over-clustering: (i) single-cell significance of hierarchical clustering (**sc-SHC**) [9]
84 and (ii) clustering hierarchy optimization by iterative random forests (**CHOIR**) [10]. Both of these methods
85 utilize hierarchical clustering paired with permutation tests to decide whether or not to merge clusters.

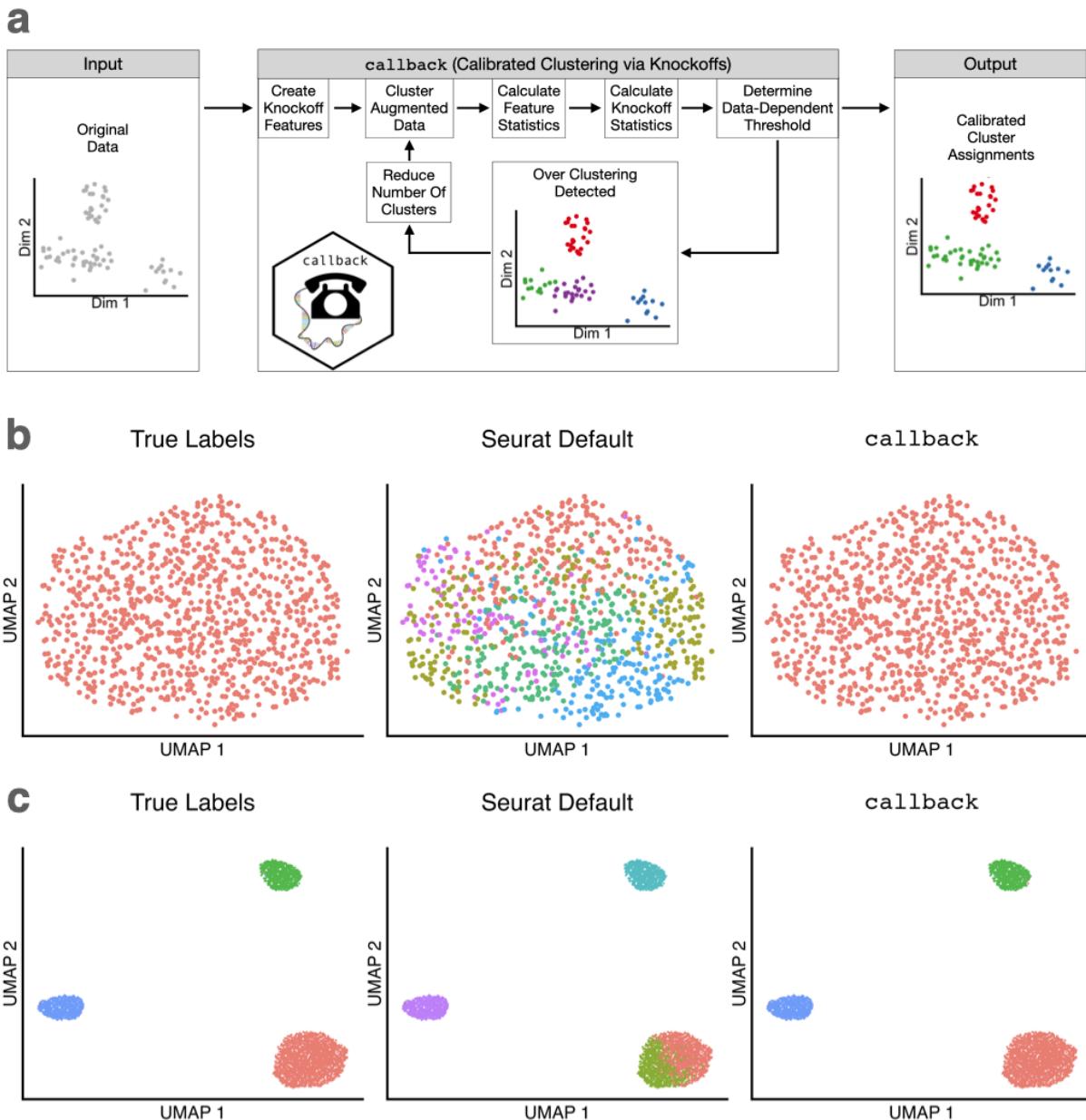


Figure 1. Overview of the callback algorithm and examples of results from different clustering approaches on simple simulated datasets. (a) Schematic of the clustering workflow with the `callback` approach. (b) Demonstration of the traditional clustering framework versus the alternative using `callback` for simulated data with one known group. Panels left to right show the true labels, clusters found using the Louvain algorithm with default parameter settings in `Seurat`, and the clusters found using the same Louvain algorithm paired with `callback`. (c) Demonstration of the traditional clustering framework versus the alternative using `callback` for simulated data with three known groups. Panels left to right show the true labels, clusters found using the Louvain algorithm with default parameter settings in `Seurat`, and the clusters found using the same Louvain algorithm paired with `callback`.

86 All **callback** results are determined using the Louvain algorithm. We analyzed the 20 different tissues
87 separately and evaluated the performance of each method by comparing their inferred cluster assignments
88 to the manually curated cell type annotations from the original Tabula Muris study. To empirically
89 assess the relative quality of clustering assignments, we utilized common metrics including the adjusted
90 Rand index (ARI), the Jaccard index, the Fowlkes-Mallows index (FMI), *V*-measure, completeness, and
91 homogeneity [14]. We include a vignette on these cluster evaluation metrics showing their behavior in a
92 simple case study of over-clustering and under-clustering (Supplementary Note and Fig. S1). In the main
93 text, we focus on ARI due to its popularity in the literature [14] and *V*-measure because it is the harmonic
94 mean of completeness and homogeneity and balances the impact of over-clustering and under-clustering
95 (Supplementary Note).

96 When evaluated by ARI (Fig. 2a), *V*-measure (Fig. 2b), completeness (Fig. S2), homogeneity (Fig. S3),
97 Jaccard index (Fig. S4), and FMI (Fig. S5), **callback** shows state-of-the-art performance. In particular,
98 when evaluated by ARI, **callback** performs best in 17 out of the 20 tissues, **sc-SHC** performs best in 2
99 tissues, and **CHOIR** performs best in 1 tissue. Similarly, when evaluated by *V*-measure, **callback** performs
100 best in 18 tissues, while **sc-SHC** and **CHOIR** perform best in 1 tissue each. The clustering results for all
101 algorithms across all 20 tissues are displayed via uniform manifold approximation and projection (UMAP)
102 plots in Figs. S6-S25 (for visualization purposes only). For many tissues, **CHOIR** tended to group cells
103 into many small sub-populations; while, for other tissues, **sc-SHC** severely under-clustered and failed to
104 find any distinct cell types at all, returning only a single group (e.g., aorta, brain myeloid, and pancreas).
105 In the diaphragm tissue, which contains five manually curated cell types, **callback** and **sc-SHC** matched
106 the five manually curated cell type labels almost exactly, while **CHOIR** seemingly over-clustered the data
107 (Fig. 2c). On the other hand, in the limb muscle dataset, which contains six manually curated cell types,
108 **callback** finds six clusters that closely match the manually curated labels (ARI = 0.97 and *V*-measure
109 = 0.95), while **sc-SHC** finds 8 clusters (ARI = 0.74 and *V*-measure = 0.79), and **CHOIR** finds 16 clusters
110 (ARI = 0.40 and *V*-measure = 0.69) (Fig. 2d). Importantly, **callback** exhibited better computational
111 efficiency (i.e., shorter runtime) than the other methods. While implementing each method on a personal
112 laptop with 6 cores, **callback** was overall the fastest, **sc-SHC** exhibited a similarly short runtime, and
113 **CHOIR** was the slowest (Fig. 2e). For example, in the fat tissue, **callback** finished 1 minute faster than
114 **sc-SHC** and 15.6 minutes faster than **CHOIR**.

115 In order to show that **callback** generates useful hypotheses for downstream analyses, we further
116 compared the clusters determined by the default **Seurat** implementation of the Louvain algorithm to
117 the clusters determined by using the Louvain algorithm with **callback** for the limb muscle tissue in the
118 Tabula Muris study (Fig. 3a-c). Using the **FindMarkers** function in **Seurat**, we identified the top 10 marker
119 genes for each inferred cluster from both approaches. Qualitatively, the default Louvain implementation
120 appears over-clustered, where inferred clusters 1, 2, 6, and 7 show similar marker gene expression to
121 one another, as do inferred clusters 3 and 5 (Fig. 3d). In contrast, the groups found by **callback** show
122 much less shared expression between clusters (Fig. 3e). To further investigate whether cells had been
123 over-clustered by the default Louvain algorithm, we performed differential expression analysis between its
124 inferred clusters and observed a high correlation in *P*-values when comparing (i) inferred clusters 1 and
125 2 versus 3 (Pearson correlation $r = 0.923$) and (ii) inferred clusters 1 and 2 versus 5 ($r = 0.925$) (Fig. 3f).
126 For the default Louvain algorithm, the inferred clusters 1 and 2 both correspond to skeletal muscle
127 satellite cells as annotated by the Tabula Muris Consortium, and inferred clusters 3 and 5 correspond to
128 mesenchymal stem cells. As a comparison, only the inferred clusters 1 and 2 from **callback** correspond
129 to skeletal muscle satellite and mesenchymal stem cells, respectively. Differential expression analysis for
130 the **callback** clusters (Fig. 3g) results in 506 differentially expressed genes (adjusted *P*-value < 0.05
131 and an absolute log-fold change greater than one) which include many known skeletal muscle satellite
132 cell markers up-regulated in the inferred cluster 1 relative to the inferred cluster 2 (e.g., *Des*, *Chodl*,
133 *Myl12a*, *Asb5*, *Sdc4*, *Apoe*, *Musk*, *Myf5*, *Chrdl2*, *Notch3*) [15] and mesenchymal stem cell type markers
134 up-regulated in the inferred cluster 2 relative to the inferred cluster 1 (e.g., *Col6a3*, *Col1a1*, *Igfbp6*,

135 *Pdgfra, C1s, Mfap5, Ecm1, Dcn, Dpep1*) [16].

136 As a final analysis of computational scalability, we benchmarked the runtime and peak memory use
137 of **callback**, **sc-SHC**, and **CHOIR** on several other publicly available datasets containing 2700, 8444, 30K,
138 and 40K cells (Figs. S26-S27) [17–20]. Each method was run on a machine with 16 cores (Methods).
139 On these datasets, **sc-SHC** was the fastest, closely followed by **callback**, and **CHOIR** was an order of
140 magnitude slower. Additionally, we applied each method using their default settings on subsets of the
141 68,579 total peripheral blood mononuclear cells (PBMCs) provided by Zheng et al. [1]. These subsets
142 were of sizes 1K, 2K, 5K, 10K, 20K, 30K, 40K, 50K, and 60K cells as well as the full dataset. On these
143 subsets, both **callback** and **sc-SHC** were very similar in speed, while **CHOIR** was an order of magnitude
144 slower (Fig. S28). In terms of peak memory consumption, **callback** used the least memory while **sc-SHC**
145 showed quadratic memory growth as a function of the number of cells (Fig. S29). In summary, **callback**
146 is as fast (or faster) than alternatives and uses less memory. Notably, **callback** required less than 10
147 gigabytes (GB) of memory on datasets with nearly 70K cells and was able to cluster those cells in less
148 than 15 minutes (with 16 cores). This demonstrates the ability to analyze large datasets with **callback**
149 on a personal laptop.

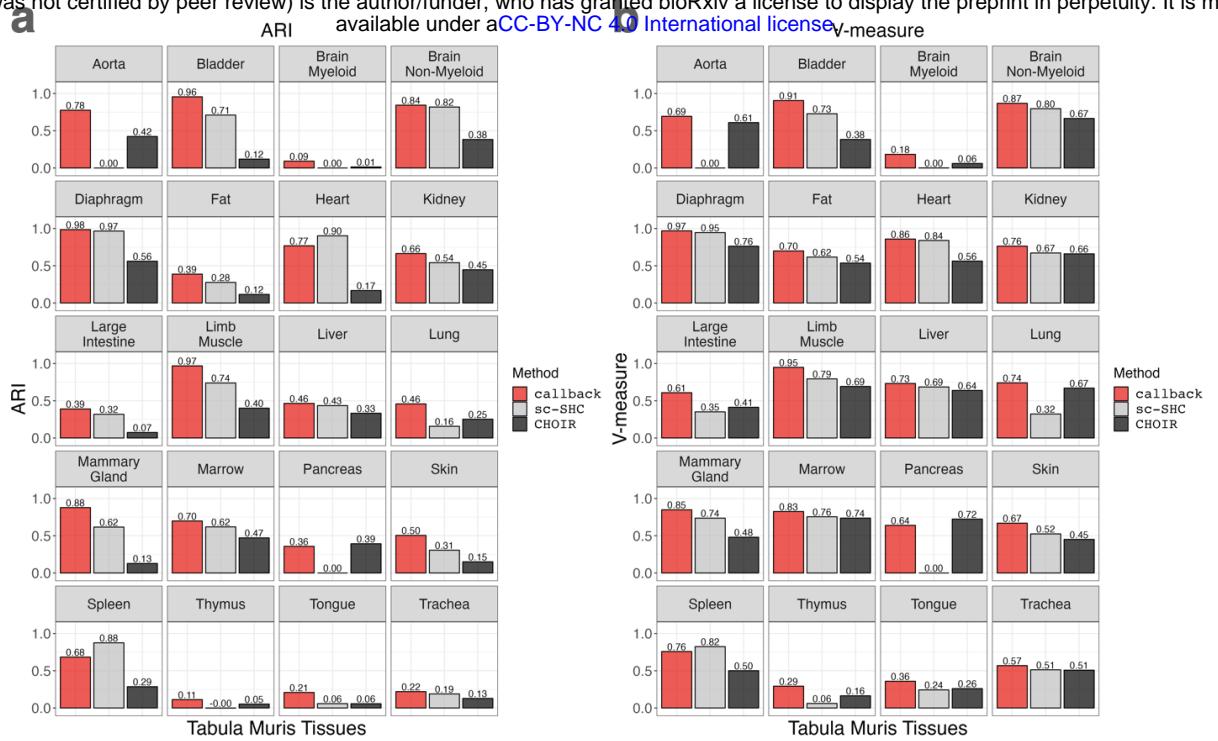
150 The **callback** approach is not without its limitations. First, the algorithm works downward from an
151 upper bound on the number of clusters (often parameterized by K in the literature). This strategy could
152 potentially lead to under-clustered results if the starting upper bound is too conservative (i.e., if K is too
153 small). To circumvent this limitation, **callback** can be initialized with a large set of clusters; however,
154 this will come with an additional computational cost because more iterations will likely need to be
155 performed until the algorithm converges onto a statistically appropriate number of clusters. Second, the
156 current implementation of **callback** does not account for additional metadata or confounding that might
157 be present in a scRNA-seq dataset. For example, in the presence of batch effects, spurious relationships
158 between cells can be created and **callback** might determine that cells of the same type need to be
159 partitioned into different groups (or vice versa). To that end, incorporating data integration steps, like
160 batch effect correction, into the **callback** software is a relevant direction for future work. One possible
161 extension of the **callback** algorithm would be to run an integration approach (e.g., **Harmony** [21]) on
162 the principal component embeddings of the augmented count matrix to correct for possible confounding
163 before building a KNN graph and performing calibrated clustering.

164 In conclusion, we have presented **callback**, a novel approach aimed to protect against over-clustering
165 when analyzing single-cell transcriptomic data. Through the analysis of several large-scale datasets,
166 we have shown that **callback** provides state-of-the-art clustering results at a fraction of the runtime
167 and computer memory when compared to other competing algorithms. Importantly, **callback** can be
168 efficiently run on a personal laptop when analyzing tens of thousands of cells. As a disclaimer, cells may
169 exhibit a variety of heterogeneous cell states, continuous axes of variation rather than discrete groups,
170 or other complexities for which **callback**, or any clustering algorithm, is not completely well-suited.
171 Overall, we envision that **callback** will be a useful aid when needing to assign labels to unknown cell
172 types. With both its speed and flexibility, **callback** will save practitioners the hours often spent manually
173 investigating and re-clustering single-cell RNA sequencing datasets.

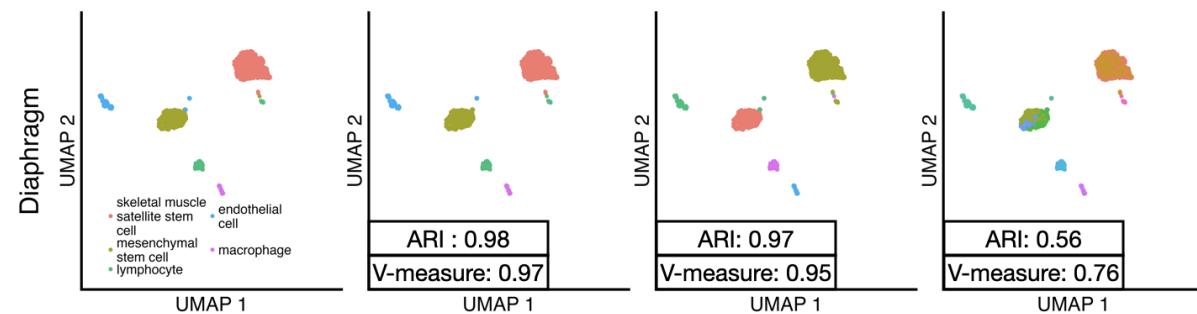
174 Methods

175 Overview of the **callback** algorithm

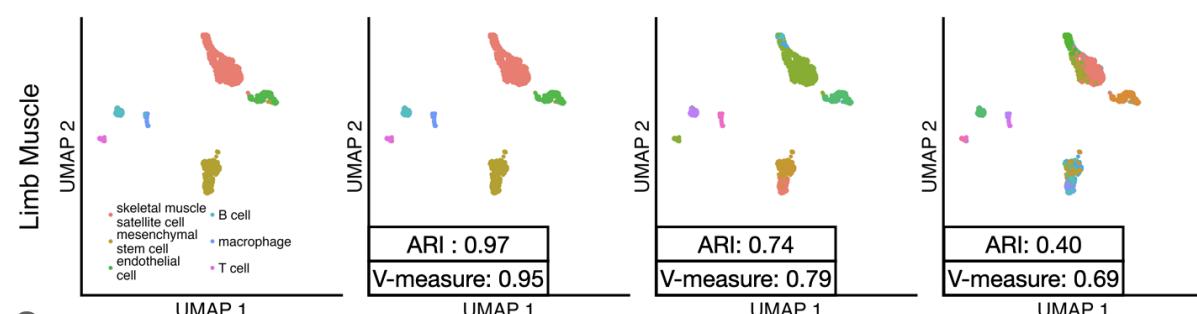
176 Consider a study with single-cell RNA sequencing (scRNA-seq) expression data for $i = 1, \dots, N$ cells
177 that each have measurements for $j = 1, \dots, G$ genes. Let this dataset be represented by an $N \times G$ matrix
178 \mathbf{X} where the column-vector \mathbf{x}_j denotes the expression profile for the j -th gene. The **callback** method
179 augments the real expression matrix with knockoff genes which are generated to have no association with
180 any particular cell type [11, 12]. These negative control variables go through the same preprocessing,



C Curated Labels callback sc-SHC CHOIR



d Curated Labels callback sc-SHC CHOIR



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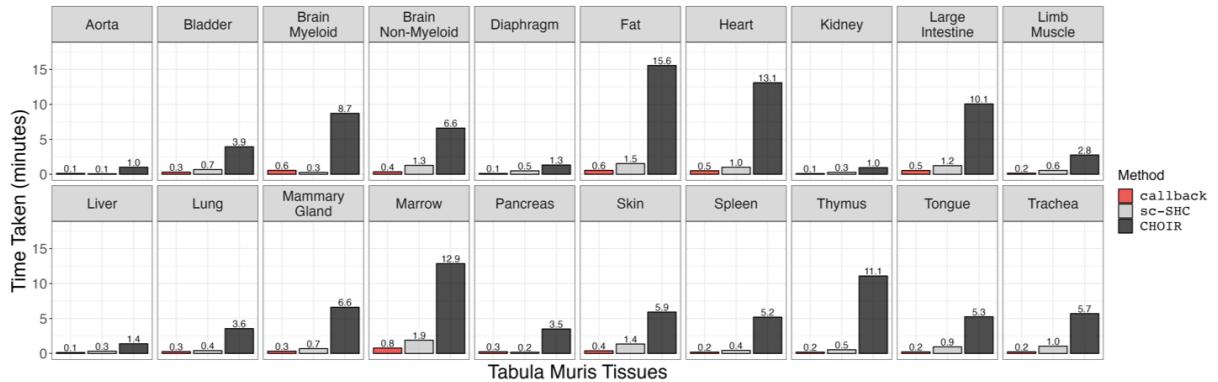


Figure 2. (Continued on the following page).

Figure 2. The callback algorithm shows state-of-the-art performance according to commonly used cluster quality metrics when compared to competing methods in the Tabula Muris dataset. (a-b) Comparison of `callback`, `sc-SHC`, and `CHOIR` using (a) ARI and (b) V -measure for each tissue. **(c-d)** Uniform manifold approximation and projection (UMAP) plots displaying the cell type annotations for (c) the diaphragm tissue and (d) the limb muscle tissue datasets, respectively. From left to right, we show the manually curated labels from the original study and clusters inferred by `callback`, `sc-SHC`, and `CHOIR`, respectively. **(e)** Runtime comparison of `callback`, `sc-SHC`, and `CHOIR` for each tissue in the Tabula Muris dataset. Each method was run using 6 cores on a personal laptop.

clustering, and differential expression analyses as the real observed genes in the study; therefore, they are presented with the same opportunity to be identified as marker genes. Since the knockoff genes are essentially noise variables, the distribution of their test statistics represent the impact of post-selective inference (i.e., deviations from the null). As a result, we can correct for these same deviations from the null in the observed test statistics for the real genes which allows us to also calibrate our cluster assignments. This process is also known as implementing a “knockoff filter” (which controls the false discovery rate) when testing for differentially expressed genes between clusters [11, 12]. If there are no detectable differences between the inferred clusters, we assume that over-clustering has occurred and re-cluster with a smaller number of groups.

More specifically, `callback` works by implementing the following steps:

1. For each gene in the study \mathbf{x}_j , generate a knockoff expression vector $\tilde{\mathbf{x}}_j$. Next, concatenate all of the knockoff genes together and construct a matrix of knockoff variables $\tilde{\mathbf{X}} = [\tilde{\mathbf{x}}_1, \dots, \tilde{\mathbf{x}}_G]$.
2. Combine the real gene expression matrix with the knockoff features into a single object $\mathbf{X}^* = [\mathbf{X}; \tilde{\mathbf{X}}]$. Then perform the usual preprocessing on the augmented data matrix \mathbf{X}^* . In this paper, preprocessing consists of normalizing the expression counts followed by principal component analysis (PCA).
3. Apply a given clustering algorithm (e.g., the Louvain algorithm) to the PCA embeddings of the augmented matrix \mathbf{X}^* (or, alternatively, apply the clustering algorithm to the augmented matrix directly).
4. Conduct differential expression analysis between each k -th and l -th cluster pair, denoted by \mathcal{C}_k and \mathcal{C}_l , respectively. Obtain P -values for all genes (real and knockoff) across each comparison.
5. Let $p_j(k; l)$ represent the P -value for the j -th real gene when comparing differential expression between clusters \mathcal{C}_k and \mathcal{C}_l . Similarly, let $\tilde{p}_j(k; l)$ represent the P -value for the same comparison but for the corresponding j -th knockoff gene. We use these two P -values to compute the following knockoff test statistic

$$W_j(k; l) = -\log p_j(k; l) - [-\log \tilde{p}_j(k; l)]. \quad (1)$$

Intuitively, a large, positive value of $W_j(k; l)$ represents evidence that the j -th gene is truly different between clusters $\mathcal{C}_k, \mathcal{C}_l$, while a value less than or equal to zero represents strong evidence that there is no difference in the expression of the j -th gene between the groups.

6. Next, compute the data-dependent threshold via the following formulation

$$\tau(k, l) = \min \left\{ t > 0 : \frac{\#\{j : W_j(k; l) \leq -t\}}{\max\{\#\{j : W_j(k; l) \geq t\}\}} \leq q \right\} \quad (2)$$

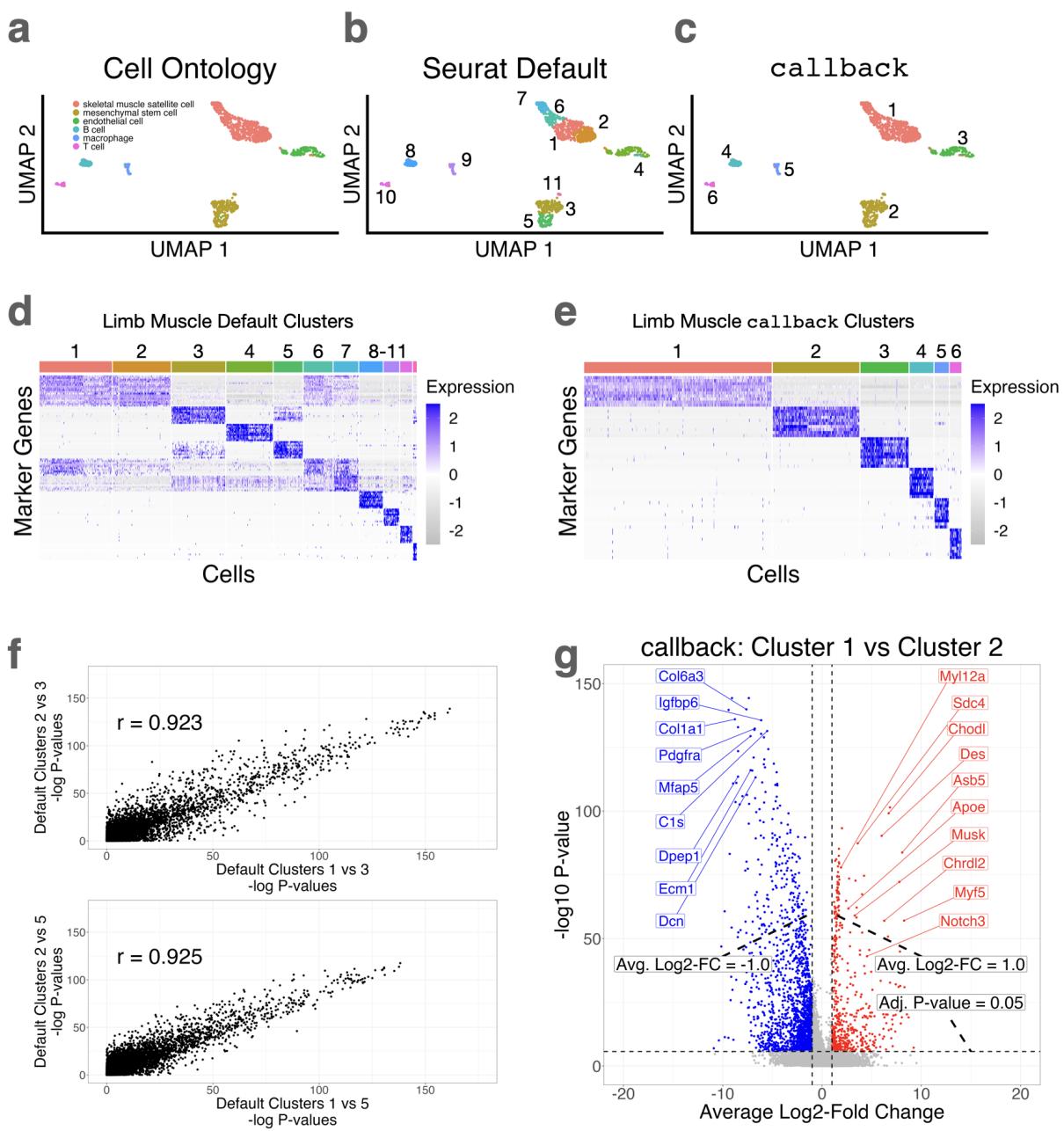


Figure 3. Using callback to avoid over-clustering leads to improved hypothesis generation for downstream analyses. (a-c) Uniform manifold approximation and projection (UMAP) plots of (a) the manually curated cell ontology class labels, (b) inferred clusters using the Louvain algorithm with default parameter settings in Seurat, and (c) inferred clusters using the Louvain algorithm paired with callback for the limb muscle tissue from the Tabula Muris study. (d) Heatmap of the top 10 marker genes for each inferred cluster shown in panel b with the default Louvain implementation. (e) Heatmap of the top 10 marker genes for each inferred cluster shown in panel c with the Louvain algorithm paired with callback. (f) Scatter plots and corresponding Pearson correlation coefficient (r) of the $\log_{10} P$ -values for all genes being tested for differential expression between (i) inferred clusters 1 and 2 versus 3 ($r = 0.923$) and (ii) inferred clusters 1 and 2 versus 5 ($r = 0.925$) from panel (d) using the default Louvain algorithm in Seurat. (g) Volcano plot of all genes being tested for differential expression between inferred clusters 1 and 2 from panel (e) using the callback version of the Louvain algorithm. The genes colored in red and blue are those with a significant P -value after Bonferroni correction and with a \log_2 -fold change greater than 1 (i.e., up-regulated in cluster 1) or less than -1 (i.e., up-regulated in cluster 2), respectively. The inferred cluster 1 from callback corresponds to skeletal muscle satellite cells and cluster 2 corresponds to mesenchymal stem cells. The genes that are labeled are well-known markers of both skeletal muscles (red, up-regulated in cluster 1 relative to cluster 2) and cardiac mesenchymal stem cells (blue, up-regulated in cluster 2 relative to cluster 1).

212 where $\#\{\bullet\}$ denotes the cardinality of a set and q is a hyperparameter representing the desired
 213 false discovery rate (FDR) when testing for differential expression. By default, and for all results
 214 presented in this paper, `callback` sets $q = 0.05$. If no such $t > 0$ exists, we set $\tau(k, l) = \infty$.

215 If, for any pair of clusters, $\tau(k, l) = \infty$, we return to step #3 and rerun the clustering algorithm with a
 216 smaller number of clusters. However, if $\tau(k, l) < \infty$ for all pairs of clusters, then we see no evidence of
 217 over-clustering and return the inferred cluster assignments to the user.

218 **Knockoff test statistics.** To compute the knockoff test statistics for each cluster $W_j(k; l)$ in Eq. (1),
 219 `callback` uses P -values $p_j(k; l)$ and $\tilde{p}_j(k; l)$ from the Wilcoxon rank sum test as implemented by the
 220 `FindMarkers` function in the `Seurat` software package [4] and accelerated by `Presto` [22].

221 **Differences between `callback` and `ClusterDE`.** Both `callback` and `ClusterDE` [6] use synthetic null
 222 variables and the knockoff filter. The key distinction between these methods is that `ClusterDE` takes
 223 given cell clusters and computes knockoff data to calibrate statistical null hypothesis tests between those
 224 clusters, while `callback` computes knockoff data on the full dataset first and uses the augmented data
 225 matrix as input to the clustering algorithm in order to calibrate the choice of clusters.

226 Construction of knockoff genes

227 To construct knockoff genes that “match” the distribution of expression for the original real genes (but
 228 without being associated with any particular cell types), we use a univariate parametric modeling approach
 229 which we apply to each individual gene separately. There has been a large body of work focused
 230 on choosing the correct distributions for modeling scRNA-seq count data [23–26]. Here, we utilize the
 231 zero-inflated Poisson (ZIP) model. Importantly, this parametric generative method creates knockoff gene
 232 variables that (i) do not have any association with any particular cell group and (ii) do not retain any
 233 covariance structure with the original real genes. The ZIP model mixes two generative processes—the
 234 first generates zeros and the second is governed by a Poisson distribution that generates counts (some of
 235 which may also be zero) [27]. For a random variable $X \sim \text{ZIP}(\pi_0, \lambda)$, we have the following mixture

$$236 \quad \Pr[X = 0] = \pi_0 + (1 - \pi_0) \exp\{-\lambda\}, \quad \Pr[X = x] = (1 - \pi_0) \frac{\lambda^x \exp\{-\lambda\}}{x!} \quad (3)$$

237 where $x \in \mathbb{N}^+$ is any non-negative integer value, λ is the expected count from the Poisson distribution
 238 (i.e., the rate parameter), and π_0 is the proportion of extra zeroes arising in addition to those from
 239 the underlying Poisson distribution. The maximum likelihood estimators for the ZIP model, given the
 240 expression of the j -th gene, take the following form

$$241 \quad \hat{\lambda}_j = W_0(-\theta_j \exp\{-\theta_j\}) + \theta_j, \quad \hat{\pi}_{0j} = 1 - \frac{\bar{x}_j}{\hat{\lambda}_j} \quad (4)$$

242 where $r_{0j} = \sum_i \mathbb{I}(x_{ij} = 0)/N$ denotes the proportion of observed zeroes for the j -th gene across all cells
 243 (with $\mathbb{I}(\bullet)$ being an indicator function), $\theta_j = \bar{x}_j/(1 - r_{0j})$, \bar{x}_j is the sample average expression for the
 244 j -th gene of interest, and W_0 is the principal branch of the Lambert W function (i.e., $W_0(a) = b$ implies
 245 $b \exp\{b\} = a$). For each j -th real gene \mathbf{x}_j , we fit the maximum likelihood estimators $\hat{\pi}_{0j}$ and $\hat{\lambda}_j$ and then
 246 sample the synthetic expression for the corresponding knockoff gene as $\tilde{\mathbf{x}}_j \sim \text{ZIP}(\hat{\pi}_{0j}, \hat{\lambda}_j)$.

247 Parameters for the `callback` algorithm

248 The default starting resolution parameter for the Louvain and Leiden algorithms within `callback` is
 249 $\gamma = 0.8$, the same as the default in the `FindClusters` function in `Seurat`. Since `callback` works by

250 iteratively reducing the starting number of clusters, if the starting parameter is too low (i.e., if you start
251 with correctly calibrated clusters or under-cluster) there is no opportunity for `callback` to iteratively
252 reduce the number of clusters. There is a warning produced by `callback` software when this occurs and
253 users can re-run `callback` with a new parameter to begin with a larger number of clusters.

254 Simulation study

255 We simulated scRNA-seq data using the `splatter` R package [28] which implements a gamma-Poisson
256 model to create a count matrix for cells. In Fig. 1, the one-group dataset was simulated with 1000 genes
257 and 1000 cells; while the three-group dataset was simulated to have 1000 genes and 4000 cells with the
258 three groups being separated in proportions of 0.6, 0.2, and 0.2, respectively. Differential gene expression
259 between the groups was controlled using the `de.prob` parameter with a value of 0.05.

260 Preprocessing and data availability

261 Below we briefly describe all of the datasets used in this work. All datasets outside of the Tabula Muris
262 were used exclusively to test the scalability of `callback` and competing methods; therefore, clustering
263 performance was not recorded. All preprocessing steps were done using the `Seurat` software package. For
264 each of these datasets, the count matrices were log-normalized using the `NormalizeData` function with
265 the default parameters. Here, we set the `scale.factor` = 10000. The number of variable genes was set
266 to 1000 for all analyses. These were determined by using the `vst` selection method implemented by the
267 `FindVariableFeatures` function. All data were centered and scaled using the `ScaleData` function with
268 default parameters, principle components were computed with the `RunPCA` using the variable genes as
269 input, and the nearest neighbor graphs were computed using the first 10 principal components within the
270 `FindNeighbors` function. Each evaluated method (`callback`, `sc-SHC`, and `CHOIR`) was provided with the
271 top 1000 highly variable genes and the first 10 principal component embeddings. The implementations
272 of the Louvain clustering algorithms analyzed the nearest neighbor graphs with resolution values set to
273 $\gamma = 0.8$.

274 **Tabula Muris.** To compare the clustering performance of `callback` against competing methods, we
275 utilized the 20 organs from the Tabula Muris dataset [13]. This dataset contains 53,760 total cells with
276 human-curated cell type labels for each organ. After following the quality control steps outlined in the
277 original study (i.e., filtering to exclude cells with less than 500 total genes detected and to exclude cells
278 with less than 50,000 total reads) and additionally removing cells without a manually curated cell type
279 label, we were left with a total of 45,423 cells for the analysis. The individual scRNA-seq expression
280 datasets for each tissue can be found on figshare: https://figshare.com/articles/dataset/Single-cell_RNA-seq_data_from_Smart-seq2_sequencing_of_FACS_sorted_cells/5715040.

282 **PBMC 3K, Bone Marrow 30K, and Bone Marrow 40K.** To assess the runtime and peak memory
283 usage of `callback` and other competing approaches, we utilized multiple datasets available through the
284 `SeuratData` R package found here: <https://github.com/satijalab/seurat-data>. In particular, we
285 downloaded data under the `pbmc3k`, `bmcite`, and `hcabm40k` variable names. For each of these datasets,
286 `callback` was run with a larger starting resolution parameter of $\gamma = 1.5$ to ensure that more than one
287 iteration took place.

288 **PBMC 68K.** We took scRNA-seq data from fluorescence-activated cell sorted (FACS) populations
289 of peripheral blood mononuclear cells (PBMCs) provided by Zheng et al. [1] and concatenated each
290 population into one dataset. This dataset contains 68,579 cells with ten different labels corresponding
291 to each purified population that was sorted. The dataset can be found on the 10X Genomics website

292 and the URL can be found on this GitHub page: https://github.com/10XGenomics/single-cell-3-prime-paper/blob/master/pbmc68k_analysis/README.md. It can also be directly downloaded here: 293 https://cf.10xgenomics.com/samples/cell/pbmc68k_rds/pbmc68k_data.rds. 294

295 **Liver 8K.** This dataset contains 8,444 cells provided by MacParland et al. [18]. It can be loaded using 296 the `HumanLiver` R package available here: <https://github.com/BaderLab/HumanLiver>. For this 297 dataset, `callback` was run with a larger starting resolution parameter of $\gamma = 1.5$ to ensure that more 298 than one iteration took place.

299 **Code availability**

300 All code is available under the open-source MIT license at <https://github.com/lcrawlab/callback> 301 with documentation at <https://lcrawlab.github.io/callback>. The scripts used to analyze the data 302 and to reproduce the figures from this paper are available at <https://github.com/lcrawlab/callback-reproducibility>. The fully rendered results can also be viewed at <https://lcrawlab.github.io/callback-reproducibility>. 303 304

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312 **Author contributions**

313 AD and LC conceived the study and developed the methods. AD developed the algorithm, software, 314 and led the analyses. AD, MLR, and AWN conducted secondary analyses. SR, PSW, APA, and LC 315 co-supervised the project. AKS and LC provided resources. AD and LC wrote the initial draft. All 316 authors interpreted the results, and revised the manuscript.

317 **Competing interests**

318 SR holds equity in Amgen. SR and PSW receive research funding from Microsoft. AKS reports com- 319 pensation for consulting and/or scientific advisory board membership from Honeycomb Biotechnologies, 320 Cellarity, Ochre Bio, Relation Therapeutics, Fog Pharma, Bio-Rad Laboratories, IntrECate Biothera- 321 peutics, Passkey Therapeutics and Dahlia Biosciences unrelated to this work. All other authors have 322 declared that no competing interests exist.

323 **References**

- 324 1. Grace X. Y. Zheng, Jessica M. Terry, Phillip Belgrader, Paul Ryvkin, Zachary W. Bent, Ryan
325 Wilson, Solongo B. Ziraldo, Tobias D. Wheeler, Geoff P. McDermott, Junjie Zhu, Mark T. Gregory,
326 Joe Shuga, Luz Montesclaros, Jason G. Underwood, Donald A. Masquelier, Stefanie Y. Nishimura,
327 Michael Schnall-Levin, Paul W. Wyatt, Christopher M. Hindson, Rajiv Bharadwaj, Alexander
328 Wong, Kevin D. Ness, Lan W. Beppu, H. Joachim Deeg, Christopher McFarland, Keith R. Loeb,
329 William J. Valente, Nolan G. Ericson, Emily A. Stevens, Jerald P. Radich, Tarjei S. Mikkelsen,
330 Benjamin J. Hindson, and Jason H. Bielas. Massively parallel digital transcriptional profiling of
331 single cells. *Nature Communications*, 8(1):14049, Jan 2017. ISSN 2041-1723. doi: 10.1038/ncom
332 ms14049. URL <https://doi.org/10.1038/ncomms14049>.
- 333 2. Evan Z. Macosko, Anindita Basu, Rahul Satija, James Nemesh, Karthik Shekhar, Melissa Goldman,
334 Itay Tirosh, Allison R. Bialas, Nolan Kamitaki, Emily M. Martersteck, John J. Trombettu,
335 David A. Weitz, Joshua R. Sanes, Alex K. Shalek, Aviv Regev, and Steven A. McCarroll.
336 Highly parallel genome-wide expression profiling of individual cells using nanoliter droplets.
337 *Cell*, 161(5):1202–1214, May 2015. ISSN 0092-8674. doi: 10.1016/j.cell.2015.05.002. URL
338 <https://doi.org/10.1016/j.cell.2015.05.002>.
- 339 3. Marlon Stoeckius, Christoph Hafemeister, William Stephenson, Brian Houck-Loomis, Pratip K.
340 Chattopadhyay, Harold Swerdlow, Rahul Satija, and Peter Smibert. Simultaneous epitope and
341 transcriptome measurement in single cells. *Nature Methods*, 14(9):865–868, Sep 2017. ISSN 1548-
342 7105. doi: 10.1038/nmeth.4380. URL <https://doi.org/10.1038/nmeth.4380>.
- 343 4. Yuhan Hao, Stephanie Hao, Erica Andersen-Nissen, William M. Mauck III, Shiwei Zheng, Andrew
344 Butler, Maddie J. Lee, Aaron J. Wilk, Charlotte Darby, Michael Zagar, Paul Hoffman, Marlon
345 Stoeckius, Efthymia Papalex, Eleni P. Mimitou, Jaison Jain, Avi Srivastava, Tim Stuart, Lamar B.
346 Fleming, Bertrand Yeung, Angela J. Rogers, Juliana M. McElrath, Catherine A. Blish, Raphael
347 Gottardo, Peter Smibert, and Rahul Satija. Integrated analysis of multimodal single-cell data.
348 *Cell*, 2021. doi: 10.1016/j.cell.2021.04.048. URL <https://doi.org/10.1016/j.cell.2021.04.048>.
- 349 5. F. Alexander Wolf, Philipp Angerer, and Fabian J. Theis. Scanpy: large-scale single-cell gene
350 expression data analysis. *Genome Biology*, 19(1):15, Feb 2018. ISSN 1474-760X. doi: 10.1186/s1
351 3059-017-1382-0. URL <https://doi.org/10.1186/s13059-017-1382-0>.
- 352 6. Dongyuan Song, Kexin Li, Xinzhou Ge, and Jingyi Jessica Li. Clusterde: a post-clustering differ-
353 ential expression (de) method robust to false-positive inflation caused by double dipping. *bioRxiv*,
354 2023. doi: 10.1101/2023.07.21.550107. URL <https://www.biorxiv.org/content/early/2023/07/25/2023.07.21.550107>.
- 356 7. Anna Neufeld, Lucy L Gao, Joshua Popp, Alexis Battle, and Daniela Witten. Inference after latent
357 variable estimation for single-cell RNA sequencing data. *Biostatistics*, 12 2022. ISSN 1465-4644.
358 doi: 10.1093/biostatistics/kxac047. URL <https://doi.org/10.1093/biostatistics/kxac047>.
359 kxac047.
- 360 8. Jesse M. Zhang, Govinda M. Kamath, and David N. Tse. Valid post-clustering differential analysis
361 for single-cell rna-seq. *Cell Systems*, 9(4):383–392.e6, 2019. ISSN 2405-4712. doi: <https://doi.org/10.1016/j.cels.2019.07.012>. URL <https://www.sciencedirect.com/science/article/pii/S2405471219302698>.
- 364 9. Isabella N. Grabski, Kelly Street, and Rafael A. Irizarry. Significance analysis for clustering with
365 single-cell rna-sequencing data. *Nature Methods*, Jul 2023. ISSN 1548-7105. doi: 10.1038/s41592-
366 023-01933-9. URL <https://doi.org/10.1038/s41592-023-01933-9>.

- 367 10. Cathrine Petersen, Lennart Mucke, and M. Ryan Corces. Choir improves significance-based detection of cell types and states from single-cell data. *bioRxiv*, 2024. doi: 10.1101/2024.01.18.576317.
368 URL <https://www.biorxiv.org/content/early/2024/01/23/2024.01.18.576317>.
- 370 11. Rina Foygel Barber and Emmanuel J. Candès. Controlling the false discovery rate via knockoffs. *The Annals of Statistics*, 43(5), October 2015. doi: 10.1214/15-aos1337. URL <https://doi.org/10.1214/15-aos1337>.
- 373 12. Emmanuel Candès, Yingying Fan, Lucas Janson, and Jinchi Lv. Panning for gold: ‘model-x’
374 knockoffs for high dimensional controlled variable selection. *Journal of the Royal Statistical Society: Series B (Statistical Methodology)*, 80(3):551–577, January 2018. doi: 10.1111/rssb.12265. URL
375 <https://doi.org/10.1111/rssb.12265>.
- 377 13. TM Consortium, Nicholas Schaum, Jim Karkanas, Norma F. Neff, Andrew P. May, Stephen R. Quake, Tony Wyss-Coray, Spyros Darmanis, Joshua Batson, Olga Botvinnik, Michelle B. Chen, Steven Chen, Foad Green, Robert C. Jones, Ashley Maynard, Lolita Penland, Angela Oliveira Pisco, Rene V. Sit, Geoffrey M. Stanley, James T. Webber, Fabio Zanini, Ankit S. Baghel, Isaac Bakerman, Ishita Bansal, Daniela Berdnik, Biter Bilen, Douglas Brownfield, Corey Cain, Min Cho, Giana Cirolia, Stephanie D. Conley, Aaron Demers, Kubilay Demir, Antoine de Morree, Tessa Divate, Haley du Bois, Laughing Bear Torrez Dulgeroff, Hamid Ebadi, F. Hernán Espinoza, Matt Fish, Qiang Gan, Benson M. George, Astrid Gillich, Geraldine Genetiano, Xueying Gu, Gungsagar S. Gulati, Yan Hang, Shayan Hosseinzadeh, Albin Huang, Tal Iram, Taichi Isobe, Feather Ives, Kevin S. Kao, Guruswamy Karnam, Aaron M. Kershner, Bernhard M. Kiss, William Kong, Maya E. Kumar, Jonathan Y. Lam, Davis P. Lee, Song E. Lee, Guang Li, Qingyun Li, Ling Liu, Annie Lo, Wan-Jin Lu, Anoop Manjunath, Kaia L. May, Oliver L. May, Marina McKay, Ross J. Metzger, Marco Mignardi, Dullei Min, Ahmad N. Nabhan, Katharine M. Ng, Joseph Noh, Rasika Patkar, Weng Chuan Peng, Robert Puccinelli, Eric J. Rulifson, Shaheen S. Sikandar, Rahul Sinha, Krzysztof Szade, Weilun Tan, Cristina Tato, Krissie Tellez, Kyle J. Travaglini, Carolina Tropini, Lucas Waldburger, Linda J. van Weele, Michael N. Wosczyna, Jinyi Xiang, Soso Xue, Justin Youngyumpipatkul, Macy E. Zardeneta, Fan Zhang, Lu Zhou, Paola Castro, Derek Croote, Joseph L. DeRisi, Christin S. Kuo, Benoit Lehallier, Patricia K. Nguyen, Serena Y. Tan, Bruce M. Wang, Hanadie Yousef, Philip A. Beachy, Charles K. F. Chan, Kerwyn Casey Huang, Kenneth Weinberg, Sean M. Wu, Ben A. Barres, Michael F. Clarke, Seung K. Kim, Mark A. Krasnow, Roel Nusse, Thomas A. Rando, Justin Sonnenburg, Irving L. Weissman, The Tabula Muris Consortium, Overall coordination, Logistical coordination, Organ collection, processing, Library preparation, sequencing, Computational data analysis, Cell type annotation, Writing group, Supplemental text writing group, and Principal investigators. Single-cell transcriptomics of 20 mouse organs creates a tabula muris. *Nature*, 562(7727):367–372, Oct 2018. ISSN 1476-4687. doi: 10.1038/s41586-018-0590-4. URL <https://doi.org/10.1038/s41586-018-0590-4>.
- 403 14. Lijia Yu, Yue Cao, Jean Y. H. Yang, and Pengyi Yang. Benchmarking clustering algorithms on estimating the number of cell types from single-cell rna-sequencing data. *Genome Biology*, 23(1):49, Feb 2022. ISSN 1474-760X. doi: 10.1186/s13059-022-02622-0. URL <https://doi.org/10.1186/s13059-022-02622-0>.
- 407 15. Andrea J De Micheli, Emily J Laurilliard, Charles L Heinke, Hiranmayi Ravichandran, Paula Fraczek, Sharon Soueid-Baumgarten, Iwijn De Vlaminck, Olivier Elemento, and Benjamin D Cosgrove. Single-Cell analysis of the muscle stem cell hierarchy identifies heterotypic communication signals involved in skeletal muscle regeneration. *Cell Rep*, 30(10):3583–3595.e5, March 2020.
- 411 16. Paola Pisterzi, Lanpeng Chen, Claire van Dijk, Michiel J W Wevers, Eric J M Bindels, and Marc H

412 G P Raaijmakers. Resource: A cellular developmental taxonomy of the bone marrow mesenchymal
413 stem cell population in mice. *Hemasphere*, 7(2):e823, January 2023.

414 17. URL https://cf.10xgenomics.com/samples/cell/pbmc3k/pbmc3k_filtered_gene_bc_matrices.tar.gz.

415

416 18. Sonya A. MacParland, Jeff C. Liu, Xue-Zhong Ma, Brendan T. Innes, Agata M. Bartczak, Blair K.
417 Gage, Justin Manuel, Nicholas Khuu, Juan Echeverri, Ivan Linares, Rahul Gupta, Michael L.
418 Cheng, Lewis Y. Liu, Damra Camat, Sai W. Chung, Rebecca K. Seliga, Zigong Shao, Elizabeth
419 Lee, Shinichiro Ogawa, Mina Ogawa, Michael D. Wilson, Jason E. Fish, Markus Selzner, Anand
420 Ghanekar, David Grant, Paul Greig, Gonzalo Sapisochin, Nazia Selzner, Neil Winegarden, Oyedele
421 Adeyi, Gordon Keller, Gary D. Bader, and Ian D. McGilvray. Single cell rna sequencing of human
422 liver reveals distinct intrahepatic macrophage populations. *Nature Communications*, 9(1):4383,
423 Oct 2018. ISSN 2041-1723. doi: 10.1038/s41467-018-06318-7. URL <https://doi.org/10.1038/s41467-018-06318-7>.

424

425 19. Tim Stuart, Andrew Butler, Paul Hoffman, Christoph Hafemeister, Efthymia Papalexis, William M.
426 Mauck, Yuhan Hao, Marlon Stoeckius, Peter Smibert, and Rahul Satija. Comprehensive integration
427 of single-cell data. *Cell*, 177(7):1888–1902.e21, 2019. ISSN 0092-8674. doi: <https://doi.org/10.1016/j.cell.2019.05.031>. URL <https://www.sciencedirect.com/science/article/pii/S0092867419305598>.

428

429 20. Aviv Regev, Sarah A Teichmann, Eric S Lander, Ido Amit, Christophe Benoist, Ewan Birney,
430 Bernd Bodenmiller, Peter Campbell, Piero Carninci, Menna Clatworthy, Hans Clevers, Bart De-
431 plancke, Ian Dunham, James Eberwine, Roland Eils, Wolfgang Enard, Andrew Farmer, Lars
432 Fugger, Berthold Göttgens, Nir Hacohen, Muzlifah Haniffa, Martin Hemberg, Seung Kim, Paul
433 Klenerman, Arnold Kriegstein, Ed Lein, Sten Linnarsson, Emma Lundberg, Joakim Lundeberg,
434 Partha Majumder, John C Marioni, Miriam Merad, Musa Mhlanga, Martijn Nawijn, Mihai
435 Netea, Garry Nolan, Dana Pe'er, Anthony Phillipakis, Chris P Ponting, Stephen Quake, Wolf
436 Reik, Orit Rozenblatt-Rosen, Joshua Sanes, Rahul Satija, Ton N Schumacher, Alex Shalek, Ehud
437 Shapiro, Padmanee Sharma, Jay W Shin, Oliver Stegle, Michael Stratton, Michael J T Stubbing-
438 ton, Fabian J Theis, Matthias Uhlen, Alexander van Oudenaarden, Allon Wagner, Fiona Watt,
439 Jonathan Weissman, Barbara Wold, Rammik Xavier, Nir Yosef, and Human Cell Atlas Meeting
440 Participants. Science forum: The human cell atlas. *eLife*, 6:e27041, dec 2017. ISSN 2050-084X.
441 doi: 10.7554/eLife.27041. URL <https://doi.org/10.7554/eLife.27041>.

442

443 21. Ilya Korsunsky, Nghia Millard, Jean Fan, Kamil Slowikowski, Fan Zhang, Kevin Wei, Yuriy
444 Baglaenko, Michael Brenner, Po-ru Loh, and Soumya Raychaudhuri. Fast, sensitive and accu-
445 rate integration of single-cell data with harmony. *Nature Methods*, 16(12):1289–1296, Dec 2019.
446 ISSN 1548-7105. doi: 10.1038/s41592-019-0619-0. URL <https://doi.org/10.1038/s41592-019-0619-0>.

447

448 22. Ilya Korsunsky, Aparna Nathan, Nghia Millard, and Soumya Raychaudhuri. Presto scales wilcoxon
449 and auroc analyses to millions of observations. *bioRxiv*, 2019. doi: 10.1101/653253. URL
450 <https://www.biorxiv.org/content/early/2019/05/29/653253>.

451

452 23. Abhishek Sarkar and Matthew Stephens. Separating measurement and expression models clarifies
453 confusion in single-cell rna sequencing analysis. *Nature Genetics*, 53(6):770–777, Jun 2021. ISSN
454 1546-1718. doi: 10.1038/s41588-021-00873-4. URL <https://doi.org/10.1038/s41588-021-00873-4>.

455

455 24. Valentine Svensson. Droplet scRNA-seq is not zero-inflated. *Nature Biotechnology*, 38(2):147–150,
456 Feb 2020. ISSN 1546-1696. doi: 10.1038/s41587-019-0379-5. URL <https://doi.org/10.1038/s41587-019-0379-5>.

458 25. Peter V. Kharchenko, Lev Silberstein, and David T. Scadden. Bayesian approach to single-cell
459 differential expression analysis. *Nature Methods*, 11(7):740–742, Jul 2014. ISSN 1548-7105. doi:
460 10.1038/nmeth.2967. URL <https://doi.org/10.1038/nmeth.2967>.

461 26. Constantin Ahlmann-Eltze and Wolfgang Huber. glmGamPoi: fitting Gamma-Poisson generalized
462 linear models on single cell count data. *Bioinformatics*, 36(24):5701–5702, 12 2020. ISSN 1367-
463 4803. doi: 10.1093/bioinformatics/btaa1009. URL <https://doi.org/10.1093/bioinformatics/btaa1009>.

464 27. Stefanie Dencks, Marion Piepenbrock, and Georg Schmitz. Assessing vessel reconstruction in
465 ultrasound localization microscopy by maximum likelihood estimation of a zero-inflated poisson
466 model. *IEEE Transactions on Ultrasonics, Ferroelectrics, and Frequency Control*, 67(8):1603–1612,
467 2020. doi: 10.1109/TUFFC.2020.2980063.

468 28. Luke Zappia, Belinda Phipson, and Alicia Oshlack. Splatter: simulation of single-cell rna sequencing
469 data. *Genome Biology*, 18(1):174, Sep 2017. ISSN 1474-760X. doi: 10.1186/s13059-017-1305-0.
470 URL <https://doi.org/10.1186/s13059-017-1305-0>.

471