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Complementary Cytoskeletal Feedback Loops Control Signal Transduction Excitability and Cell Polarity

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Abstract:

To move through complex environments, cells must constantly integrate chemical and mechanical cues. Signaling networks, such as those comprising Ras and PI3K, transmit chemical cues to the cytoskeleton, but the cytoskeleton must also relay mechanical information back to those signaling systems. Using novel synthetic tools to acutely control specific elements of the cytoskeleton in *Dictyostelium* and neutrophils, we delineate feedback mechanisms that alter the signaling network and promote front- or back-states of the cell membrane and cortex. First, increasing branched actin assembly increases Ras/PI3K activation while reducing polymeric actin levels overall decreases activation. Second, reducing myosin II assembly immediately increases Ras/PI3K activation and sensitivity to chemotactic stimuli. Third, inhibiting branched actin alone increases cortical actin assembly and strongly blocks Ras/PI3K activation. This effect is mitigated by reducing filamentous actin levels and in cells lacking myosin II. Finally, increasing actin crosslinking with a controllable activator of cytoskeletal regulator RacE leads to a large decrease in Ras activation both globally and locally. Curiously, RacE activation can trigger cell spreading and protrusion with no detectable activation of branched actin nucleators. Taken together with legacy data that Ras/PI3K promotes branched actin assembly and myosin II disassembly, our results define front- and back-promoting positive feedback loops. We propose that these loops play a crucial role in establishing cell polarity and mediating signal integration by controlling the excitable state of the signal transduction networks in respective regions of the membrane and cortex. This interplay enables cells to navigate intricate topologies like tissues containing other cells, the extracellular matrix, and fluids.

Introduction:

Cell migration is a fundamental process that plays critical roles in development, immune system function, and disease progression, including metastasis. While there is a broad diversity of cell migration strategies, efficient motion usually depends on the spontaneous formation of membrane protrusions and the establishment of front-back polarity. Both protrusion formation and polarity rely on coordination between actin cytoskeletal dynamics and signaling networks. The precise mechanisms by which signaling controls cytoskeletal activity are still being unraveled, and even less is known about the potential feedback from changes in cytoskeletal organization and mechanics on these same signaling networks[1,2].

Regulation of the actin cytoskeleton is intricately linked to signaling molecules, such as Ras GTPases and phosphoinositides. The activation of Ras GTPase, associated signaling molecules, and the lowering of anionic lipids correlates strongly with the formation of cell protrusions[3–8]. In amoeboid migrating cells, protrusion formation involves the activation of branched actin nucleator Arp2/3 and the local disassembly of myosin II (hereafter referred to as 'myosin') filaments and actin-actin crosslinkers[9–14]. Previous studies have suggested positive feedback exists between Arp2/3-mediated actin polymerization and PI3K activity at the front[8,11,15–18]. Synergistically, there is

72 evidence that negative feedback from actomyosin inhibits signaling. For example, cells
73 lacking myosin have elevated Ras activation, and retracting pseudopods are insensitive
74 to chemotactic stimulation[19–21]. Together these findings suggest that branched actin and
75 actomyosin networks may differentially feedback on signaling networks. However,
76 because the network governing cell migration is complex and adaptable, local and acute
77 perturbations are critical to dissect the cause and nature of cytoskeletal feedback.

78 Both signal transduction networks and actin cytoskeletal networks exhibit properties of
79 excitability, including an activation threshold and propagating waves[22–29]. Waves of Ras-
80 GTP, phosphatidylinositol 3,4,5-trisphosphate (PIP3), actin polymerization, and Arp 2/3
81 traverse the basal cell membrane and define the "front" state of the cortex.
82 Complementary zones ("shadow waves") of PI(4,5)P2, cortexillin, and myosin II
83 depletion define the "back" state of the cortex. While waves of signaling and
84 cytoskeletal activity are coupled, they are morphologically distinct and independent[24]. In
85 the absence of the cytoskeleton, signaling waves still propagate but cannot create
86 protrusions, and in the absence of signaling activity, cytoskeletal activity exhibits
87 excitable properties but does not propagate in broad waves that move cells[22,27]. These
88 networks have been referred to as the Signal Transduction Excitable Network (STEN)
89 and the Cytoskeletal Excitable Network (CEN), respectively. Previous studies suggest
90 that modifying the threshold of STEN tunes the size and speed of these waves and
91 ultimately the nature of actin-based protrusions[3,24]. Changes in wave behavior are
92 therefore a surrogate for alterations in the STEN and CEN and can predict effects on
93 cell behavior.

94 The properties of the signaling and cytoskeletal networks can be captured in
95 computational models [3,24,30–33]. Excitable systems require both fast positive and delayed
96 negative feedback[34]. In the models, we have previously reported mutual inhibition
97 between front and back activities, which leads to a positive feedback loop, and
98 molecules at the cell front produced their own inhibitor on longer timescales[3,22]. These
99 models predicted the behavior of coupled STEN-CEN waves and the response of cells
100 to chemotactic stimulus. However, these models oversimplified the behavior of the
101 cytoskeleton in this process. CEN activity represented the activation of Arp2/3 by Rac at
102 the cell front and did not consider regulation to and feedback from the morphologically
103 distinct actomyosin network at the cell back[24]. Furthermore, they have not been able to
104 easily explain experimental observations about front-back polarity, which was shown to
105 be dependent on cytoskeletal architecture[35].

106 We sought to understand the impact of modulating the F-actin or actomyosin
107 cytoskeletal structures on the STEN. First, we uncovered a positive feedback
108 mechanism that promotes the front state. By increasing the pool of available actin
109 monomers and promoting the formation of branched actin networks, STEN activation is
110 enhanced. Second, it was shown previously that increasing Ras activity can lower
111 myosin assembly[12,36]. Here, by designing precise chemically induced dimerization
112 system (CID) and optogenetic tools to control myosin assembly in real time, we found
113 that disassembly of the actomyosin cortex increases STEN activity. Together, these
114 mutually negative effects constitute a positive loop that augments the back state.

115 Consistently, increasing the abundance of linear actin and crosslinked actin inhibits
116 STEN activation. Moreover, inhibiting branched actin nucleation further enhances the
117 overall effect. Our study here delineates the reciprocal relationship between
118 cytoskeletal dynamics and signaling networks that takes place during cell migration.
119 The cross-interaction of these molecular mechanisms allow cells to integrate signal
120 transduction and mechanical cues and successfully navigate complex three-
121 dimensional environments.

Results:

Positive and negative feedback loops from the cytoskeleton control signaling networks

125 To investigate the effects of altering the cytoskeleton on signaling, we first examined the
126 impact of increasing free monomeric actin in *Dictyostelium*, a classic model of amoeboid
127 migration. Previously we found that mutating actobindins, which bind and sequester free
128 G-actin, increases actin polymerization at the cell front[37,38]. To determine the effects of
129 this on signaling, we measured Ras activation levels in *actobindin* triple knockout (*ABN*
130 *ABC-*) cells to examine the effect of increased "front" actin network formation on STEN
131 activity (**Fig. 1A-C, Movie S1**). Significantly, the *ABN ABC-* cells exhibited elevated
132 levels of Ras activation, suggesting a positive regulatory role for front actin networks in
133 STEN. To assess whether this increase is mediated by enhanced Arp2/3 activity, we
134 measured the localization of WAVE complex subunit HSPC300 to the cell front in *ABN*
135 *ABC-* and wild-type cells. As hypothesized, *ABN ABC-* cells showed greater recruitment
136 of HSPC300 to the cortex compared to controls (**Fig. S1**). This result indicates the
137 presence of a positive feedback loop from the front actin, which appears to form a
138 branched Arp2/3-assembled network, to STEN.

139 We next sought to determine whether cytoskeletal proteins at the cell back also regulate
140 signaling networks. To measure how changing contractility effects signaling, we utilized
141 myosin heavy chain kinase C (MHCKC) to control bipolar thick filament (BTF) assembly
142 of myosin. MHCKC is recruited to the cell cortex after chemoattractant stimulation,
143 leading to myosin phosphorylation and disassembly at specific locations[39,40]. However,
144 since chemoattractant addition triggers multiple events simultaneously, we aimed to
145 develop a method for specifically controlling myosin assembly. To achieve this, we
146 designed a chemically induced dimerization system (CID) utilizing a MHCKC-FRB
147 fusion protein, which is expected to dimerize with cAR1-2xFKBP, a uniformly distributed
148 membrane protein, upon addition of rapamycin (**Fig. 1D-F, Movie 2**).

149 To confirm BTF disassembly, we engineered the CID system into *myosin II*-null (*mhcA*
150 null) cells "rescued" with GFP-myosin and imaged with total internal reflection
151 fluorescence (TIRF) microscopy. Adding rapamycin led to uniform recruitment of
152 MHCKC to the membrane and an approximately 40% decrease in the intensity of GFP-
153 myosin on the bottom cortex (**Fig. S2A-B**). Imaging cell shape using confocal
154 microscopy revealed that MHCKC recruitment to the cell periphery induced cell

155 spreading, with an approximately 40% increase in cell area, and triggered dynamic
156 changes in cell shape that persisted for at least 20 minutes (**Fig. 1 D-F, Movie 2**).

157 Increased area and shape change suggested that MHCKC recruitment increased the
158 cells deformability, most likely by reducing its elastic modulus, which is a short time-
159 scale mechanical parameter[41]. This increased deformability then likely makes
160 protrusion formation more likely. To analyze the impact of MHCKC recruitment on STEN
161 activity specifically, we imaged RBD-GFP, an active Ras biosensor as one of the
162 indicators of STEN activation[42]. MHCKC recruitment resulted in a 50% increase in Ras
163 activity at the periphery where protrusions formed (**Fig. 1 G-I, Movie 3**).

164 Previously, we found that reducing PI(4,5)P2 levels lowers the STEN threshold,
165 increasing the size and number of Ras and PIP3 membrane patches[3]. We sought to
166 determine whether inhibiting myosin would similarly lower this threshold. To address
167 this, we prepared sets of cells having MHCKC recruited to the membrane by
168 pretreatment with rapamycin with untreated cells having no recruitment. We exposed
169 each set to two doses of cAMP (1 nM and 100 nM). At 1 nM cAMP, the pretreated set
170 exhibited a higher average peak response, as measured by depletion of RBD-GFP from
171 the cytoplasm, compared to the untreated set, while at 100 nM cAMP, the two sets
172 responded similarly (**Fig. S2C-D**). Altogether, these findings reveal a negative feedback
173 loop from myosin which increases the STEN activation threshold and inhibits front state
174 formation (**Fig. 1J**).

175 **Effects of removing branched actin networks on STEN activity**

176 To further investigate negative feedback from the actomyosin network and to probe
177 whether actin populations at the cell front can tune signaling, we inhibited branched
178 actin nucleation with the Arp2/3 inhibitor CK666[43] and examined changes in actin
179 network morphology and STEN activation. LimE$_{\Delta Coil}$, a biosensor for polymerizing actin,
180 localizes to growing pseudopods and macropinosomes in randomly migrating
181 *Dictyostelium* cells[44]. However, within 2 minutes of CK666 treatment, the formation of
182 new pseudopods was significantly inhibited. Interestingly, instead of leaving the cell
183 periphery, LimE redistributed from transient patches and ruffles into a more stable ring-
184 like structure, which began to form after 4 minutes and reached completion after 12
185 minutes (**Fig. 2A-B, Movie 4**). Because this ring-like actin organization resembled
186 proteins in the actomyosin cortex, we further investigated the effect of CK666 on the
187 localization of Cortexillin I. Cortexillin I is an actin-actin crosslinker, actin-membrane
188 crosslinker, and myosin-binding protein that, as noted earlier, enriches at the cell back,
189 "shadow" waves, and also the cleavage furrow of dividing cells[26,45–49]. Treatment with
190 CK666 led to a substantial increase of approximately 30% in the membrane to cytosol
191 ratio of Cortexillin I relative to DMSO controls (**Fig. S3A-B**). These results show that
192 CK666 treatment not only inhibits branched actin nucleation, but leads to increased
193 "rear cortex-type" assembly.

194 To assess the impact of CK666 treatment on signal transduction network (STEN)
195 activity, we employed the biosensor PH$_{CRAC}$, which detects PI(3,4,5)P3[50]. In single cells,

196 PH$_{CRAC}$ overlaps with RBD and LimE in growing pseudopods and macropinosomes.
197 Similar to actin, PIP3 disappeared from these patches following CK666 treatment.
198 Unlike actin, PIP3 did not relocalize elsewhere, suggesting inhibition of the STEN (**Fig.**
199 **2A-B**). To further examine how CK666 treatment affects STEN, we measured changes
200 in STEN waves on the bottom cell surface of electrofused giant cells[51]. Initially, these
201 cells displayed propagating waves of RBD along the bottom membrane; however, upon
202 addition of CK666, these waves disappeared within two minutes (**Fig. 2C-E, Movie 5**).
203 These experiments reveal that both PIP3 production, Ras activation, and likely many
204 other STEN activities, are reduced when branched actin is removed and cortical
205 assembly is increased.

206 To determine whether the decrease in STEN activation was due to the loss of branched
207 actin or the increase in cortical actin, we introduced the actin depolymerizing drug
208 latrunculin to CK666-treated cells to eliminate all remaining actin subpopulations.
209 Significantly, the reduction of F-actin levels in cells lacking branched actin led to the
210 recovery of RBD waves within two minutes (**Fig. 2C-E, Movie 5**). The inhibitory role of
211 cortical actin networks on STEN activity were not limited to *Dictyostelium*. We
212 conducted the same experiment using human neutrophil-like HL60 cells expressing the
213 PIP3 biosensor PH-AKT. Consistent with previous reports, PIP3 was observed in
214 patches at the front of migrating HL60 cells. Upon CK666 addition, these cells rounded
215 up and lost their pseudopods within 2 minutes. Similar to *Dictyostelium*, the elimination
216 of branched actin in neutrophils also resulted in a decrease in PIP3 levels on the
217 membrane. Subsequently, the addition of latrunculin, which removed the remaining
218 actin networks, partially restored PIP3 levels (**Fig. 2F-H, Movie 6**). These findings
219 suggest that the actomyosin cortex suppresses STEN activity and that this phenomenon
220 is evolutionarily conserved.

221 To test if the inhibition of STEN by the actomyosin cortex was due to an increase in the
222 STEN threshold, we examined the accumulation of PIP3 in response to low (1 nM) and
223 high (100 nM) cAMP stimuli in *Dictyostelium* cells treated with CK666 alone or CK666
224 and latrunculin in combination. The average peak PIP3 level in response to low cAMP
225 was significantly smaller in cells treated with only CK666 versus cells treated with both
226 latrunculin and CK666. However, there was no significant difference between the two
227 populations when stimulated with high cAMP (**Figs 2I-J, S3**). This relative inhibition
228 indicates that the threshold for STEN was raised, but the system is still functional.
229 Together, these findings suggest that the actomyosin cortex tunes response to receptor
230 inputs by lowering STEN excitability (**Fig. 2K**).

231 **Myosin II is a critical contributor to negative feedback from the cortex to signaling**
232 **networks**

233 Because myosin is a critical component of the cortex, we investigated whether removing
234 myosin ameliorates the effect of CK666 on the STEN. CK666 treatment in *myosin*-null
235 cells prevented protrusions and decreased PIP3 levels similar to its effects in wild-type
236 cells. However, unlike the near absence of PIP3 in wild-type cells, *myosin*-null cells
237 treated with CK666 periodically exhibited bright, transient PIP3 patches (**Fig. 3A, Movie**

238   **S7**). *Myosin*-null cells treated with CK666 had significantly more PIP3 patches than wild
239   type cells (**Fig. 3B**), indicating that myosin is required for the full effect of cortical
240   suppression of STEN. To further elucidate the role of the actomyosin cortex, we applied
241   our method to rapidly dissemble myosin in cells treated with CK666. First, cells were
242   inhibited with CK666, which reduced the number of Ras patches by 95% and
243   immobilized the cell. Then, MHCKC was recruited to the membrane using rapamycin.
244   While disassembling myosin filaments did not restore motility, it caused Ras activation
245   to recover to 40% of its wild type value (**Fig. 3C-E, Movie S8**). Taken together, these
246   results show that myosin is major contributor to cortical feedback on the STEN (**Fig.**
247   **3F**).

248   **Using RacE as a tool to probe the role of cortical actin in STEN regulation**

249   To further probe the role of the actomyosin cortex in signaling, we turned to RacE, a
250   member of the Rac/Rho subfamily which has been shown to regulate linear actin
251   nucleation, actin crosslinking, Myosin contraction, and cortical viscoelasticity and
252   tension[52–56]. To abruptly increase RacE activity in migrating cells and assess signaling
253   impacts, we designed a CID system to recruit the RacE GEF, GXCT[57], to the cell
254   membrane. Recruiting the GEF domain of GXCT to the cell membrane by adding
255   rapamycin led to a phenotype with cells dramatically flattening and undulating rapidly
256   around the perimeter, while losing well-defined protrusions and motility (**Fig. 4A-D,**
257   **Movie S9**). LimE localization shifted from a few broad patches to a uniform distribution
258   along the cell perimeter. Quantitative analysis showed a 40% increase in F-actin cortical
259   localization within 8 minutes after rapamycin addition (**Fig. 4E-G, Movie S10**). Similarly,
260   the amount of actin crosslinker dynacortin increased significantly upon GXCT
261   recruitment, consistent with the role of RacE in the recruitment this cytoskeletal protein
262   to the cortex[52](**Fig. S4A-C**). Furthermore, we confirmed that the changes in actin were
263   not due to an unknown role of RacE in activating Arp2/3 by repeating the experiment in
264   cells treated with CK666. When we recruited GXCT to the membrane, there was still a
265   significant increase in actin polymerization, indicating that RacE activates actin
266   polymerization independently of Arp2/3 (**Fig. S4D-E**).

267   To determine the effects of RacE activation on STEN, we observed changes in the
268   localization of the active Ras biosensor, RBD, after GXCT recruitment. Before
269   recruitment, cells displayed several large, intense, and long-lived RBD patches along
270   their periphery. However, upon activating RacE, the RBD patches became smaller,
271   weaker, and shorter-lived, with a potential increase in the total number of patches. The
272   amount of Ras activation on the cell periphery dropped by 30% within 8 minutes (**Fig.**
273   **4H-J, Movie S11**). Taken together, these results suggest that RacE activation is able to
274   increase actin polymerization in an Arp2/3-independent manner and thereby inhibit
275   STEN activation (**Fig. 4K**).

276   **RacE reversibly and locally inhibits STEN and triggers arp2/3-independent**
277   **protrusions**

278 To reversibly and locally control RacE activity, we designed an iLID-based optogenetic
279 system[58] to recruit GXCT to the membrane by applying blue light to cells. In this system,
280 the GEF domain of GXCT was fused to a SSPB domain which binds to a membrane-
281 localized iLid domain (see methods) when exposed to blue light. Similar to the CID
282 system, uniform light stimuli led to rapid cell flattening and cessation of movement,
283 which rapidly reversed upon removal of illumination (**Fig. 5A-C, Movie S12**). We then
284 examined how transiently increasing RacE activity affected propagating basal RBD
285 waves. Recruiting GXCT caused a sudden decrease in RBD wave activity, which was
286 quickly reversed upon removal of blue light and dissociation of GXCT (**Fig. 5D-F, Movie
287 S13**).

288 Next, we took advantage of our optogenetic system to assess the morphological and
289 signaling effects of local increases in RacE activity. Interestingly, despite the ability of
290 RacE to turn off Ras activity, the localized recruitment of GXCT induced the formation of
291 protrusions expanding from the recruitment site towards the source of the blue light.
292 These protrusions were observed to form even in the presence of CK666, suggesting
293 that RacE-triggered actin polymerization can occur independently of Arp 2/3 (**Fig. 5G-H,
294 Movie S14**). However, the lifetime and length of these protrusions is lower than typical
295 chemoattractant-induced pseudopods. Moreover, recruiting GXCT to specific regions on
296 the basal surface of the cell led to the local extinguishment or redirection of propagating
297 RBD waves (**Fig. 5I, Movie S15**)

Feedback loops from the cytoskeleton can generate cell polarity

299 Our results suggest the presence of two different cytoskeletal feedback loops. To
300 determine how these loops could affect excitability and cell polarity, we turned to a
301 computational model. The core of the model is an activator-inhibitor system (**Fig. 6A**) in
302 which the activator positive feedback is implemented as double negative feedback
303 between Ras and anionic lipids, including PIP2, and the slow inhibition is between Ras
304 and PKB[24]. Simulations of this core system show occasional firings randomly distributed
305 around a cell perimeter (**Fig. 6B**). These elevated regions of activity propagate for
306 several seconds before they extinguish. The complementary pattern between Ras and
307 PIP2 was used as a readout.

308 To the basic network, we add two complementary feedback loops (Black lines in **Fig.
309 6A**). The first loop implements the feedback between branched actin and Ras at the cell
310 front while the second implements feedback between actomyosin and Ras at the rear.
311 Details of the mathematical model are given in the Methods. Simulations of the system
312 with added cytoskeletal feedback have the same complementarity as before, but Ras
313 shows increased persistence, characterized by localized long-lived regions of elevated
314 Ras with minimal lateral propagation (**Fig. 6B**).

315 To illustrate the effect of these feedback loops on cell movement, we first plotted the
316 trajectories of simulated cells (see Methods) migrating randomly in the absence of
317 branched actin and actomyosin feedback (**Fig. 6C, top**) and compared it to those in the

318 presence of these loops (**Fig. 6C, bottom**). Cells without feedback remained near their
319 starting point, while the addition of feedback loops enabled cells to move farther away.
320
321 To characterize the effect of the two loops separately, we altered the strength of each
322 loop individually while holding the other constant and quantified the total Ras activity.
323 Increases in branched actin feedback led to elevated Ras-GTP levels, greater
324 persistence, and wider patches (**Fig. 6D, E**). Increases in actomyosin feedback had the
325 opposite effect (**Fig. 6F, G**).

326 Finally, we carried out simulations in a two-dimensional surface to recapitulate basal
327 waves and recreated the experiments of **Fig. 2C-D**. Initially, waves are seen, but after
328 simulating the effect of CK666 addition through the removal of the branched actin
329 feedback, they disappear. The subsequent removal of the actomyosin feedback loop,
330 mimicking Latrunculin addition, leads to a partial recovery of the Ras waves (**Fig. 6H;**
331 **Movie S16**). Quantitating the effect over multiple simulations shows that total Ras
332 activity decreases greatly when CK666 is added and partial recovery upon Latrunculin
333 treatment (**Fig. 6I**).

Discussion

335 Much previous work has focused on control of the cytoskeleton by Ras/PI3K signal
336 transduction networks, particularly in the context of chemotaxis, and many studies have
337 focused on the reaction of cytoskeletal elements to mechanical forces, but feedback
338 from the cytoskeleton to "upstream" signal transduction events has only occasionally
339 been considered. Using synthetic biological techniques, we have uncovered two crucial
340 feedback mechanisms from different actin networks that characterize the front and back
341 regions of the cell cortex. A front-promoting mechanism is supported by the observation
342 that increases in Arp2/3 actin strongly boost Ras/PI3K activation, while reduction of F-
343 actin decreases the activation. A back-promoting mechanism is indicated by multiple
344 observations. First, acute reduction of myosin assembly enhances Ras/PI3K activation
345 and heightens sensitivity to chemotactic stimuli, indicating that the actomyosin cortex
346 suppresses Ras activation. Second, selective inhibition of branched actin nucleation
347 nearly eliminates Ras activity; this inhibition is mitigated by depolymerizing the bulk of
348 actin and decreasing myosin assembly, as well as in cells lacking myosin. Collectively,
349 these observations indicate that the inhibition depends on the cortical actomyosin
350 network. Third, recruitment of RacE GEF, which promotes actin crosslinking and formin
351 nucleation, substantially reduces Ras/PI3K activation and yet can still induce
352 protrusions. This indicates that cells can suppress Ras/PI3K signaling locally or globally
353 by increasing the abundance of the actomyosin cortex.

354 When taken together with interactions discovered previously, the mechanisms we have
355 delineated create two positive feedback loops between signal transduction and
356 cytoskeletal networks. A front-promoting loop becomes clear by merging earlier
357 findings that Ras/PI3K activation promotes Arp2/3 nucleation with our observations here
358 that branched actin activates these signal transduction networks[59]. A back-promoting

359 loop emerges by bringing together our studies here that myosin assembly and
360 strengthening the actomyosin cortex inhibits Ras/PI3K activation with prior work that
361 Ras/PI3K activation leads to activation of myosin heavy chain kinase and consequent
362 disassembly of myosin[12,36]. In human neutrophil-like cells, Ras has recently been shown
363 to reverse back polarity through its downstream target AKT1, indicating a similar
364 relationship may exist[60]. The existence of these front- and back-promoting loops points
365 to reciprocal interactions between Ras/PI3K signal transduction and the branched actin
366 and actomyosin cytoskeletal networks. These interconnected networks provide a
367 molecular scheme for generating cell polarity and for integrating the chemical and
368 mechanical cues that a cell would encounter in navigating a complex environment

369 Previous investigators have speculated that polarity is established by dual front and
370 back positive feedback loops, but these findings differ from ours in several ways. First,
371 much of the work on these feedback loops focuses on direct feedback between different
372 cytoskeletal regulators such as Rac and Rho and do not consider a role for upstream
373 signaling events like Ras/PI3K activation. Second, while previous models have also
374 described positive feedback to PIP3 from Rac[8,11,15–18], we show here that the
375 actomyosin cortex is a direct negative regulator of Ras/PI3K signaling, even in cells
376 without Arp2/3 activity. These findings are not inconsistent, but our work reveals an
377 additional critical layer of regulation.

378 The mechanism of negative feedback from the actomyosin cortex to signaling is not yet
379 clear, but there are several attractive possibilities. One possibility is that integrity of the
380 underlying cortex influences the fluidity of membrane. Lower fluidity in regions with high
381 cortical density may slow the diffusion of signaling activators, locally lowering
382 excitability. Supporting this, multiple studies have reported lower membrane fluidity in
383 back regions where actomyosin density should be high[61–63]. Another possibility is
384 related to the finding that anionic lipids such as PI(4,5)P2 on the inner leaflet of the
385 membrane inhibits Ras/PI3K signaling[6]. Electrostatic interactions between molecules in
386 the actomyosin cortex and the lipids, such as through cortexillin and PI(4,5)P2[64], or the
387 enzymes that regulate them may contribute to the enrichment of these inhibitory lipids at
388 the cell back. Recent work has indicated that actin and the membrane are more tightly
389 associated at the cell back, indicating a stronger interaction between the membrane and
390 the actomyosin cortex than branched actin[63]. Finally, force generation by the
391 actomyosin cortex could alter membrane tension or curvature, leading to the recruitment
392 or activation of negative regulators specifically at the cell back[65–69].

393 A cell migrating though its natural environment towards a chemical cue encounters a
394 complex mix of other cells, the extracellular matrix, and shear forces. These physical
395 features are usually integrated with chemical cues to determine the optimal path
396 towards a destination. One might imagine that the cell is like a self-driving car, following
397 a GPS signal to a destination: if the car merely followed a pre-planned route, it would
398 soon collide with an unmarked obstacle. To safely reach its goal, the car must use
399 sensors to detect other cars or road work. While cells have well-characterized

400 biochemical sensors, their methods for detecting mechanical stimuli are less well-
401 understood, nor is it clear how cells integrate these two cues. Recent studies have
402 suggested various physical properties, like nuclear stiffness and membrane curvature,
403 may help steer cells in crowded environments[69–71]. Our findings, combined with long-
404 standing evidence that physical forces alter the properties of the cytoskeleton, suggest
405 an attractive hypothesis. These physical cues could locally alter the balance between
406 actomyosin and branched actin. As we have shown here, altering this balance has quite
407 significant effects on the same signaling nodes that are also controlled by chemical
408 stimuli. Therefore, the core excitable system we and others have described likely serves
409 as an integrator of diverse environmental signals to bring about successful navigation[72].

410 Our results also have important implications for current and future therapeutic
411 interventions. Currently, many cancer therapies target specific signaling molecules
412 involved in cell growth and migration. Layers of redundancy and feedback from the local
413 environment may compensate for inhibition at any single node. Targeting the
414 cytoskeleton in combination with molecules like Ras and PI3K may be critical for
415 preventing tumor growth and metastasis[73–75].

416 **Methods**

417 **Cells and plasmids:** *Dictyostelium discoideum* cells were cultured in HL5 media[76] for a
418 maximum of 2 months after thawing from frozen stock. AX3 cells were obtained from
419 the R. Kay laboratory (MRC Laboratory of Molecular Biology, UK), *abnABC*- cells were
420 generated with homologous recombination previously in the Devreotes Lab. *mhcA*- cells
421 were obtained from the D. Robinson Lab (JHU). Female human neutrophil-like HL-60
422 cells stably expressing RFP-PH$_{AKT}$ was previously created in the Devreotes lab[77]. Cells
423 were cultured in RPMI medium 1640 with L-glutamine and 25 mM HEPES (Gibco;
424 22400-089) supplemented with 15% heat-inactivated fetal bovine serum (FBS; Thermo
425 Fisher Scientific; 16140071) and 1% penicillin-streptomycin (Thermo Fisher Scientific;
426 15140122). Cells were split at a density of 0.15 million cells/ml and every 3 days. 1.3%
427 DMSO was added to cells at a density of 0.15 million cells/ml to trigger differentiation 5-
428 7 days before imaging.

429 Plasmids were introduced into *Dictyostelium* cells using electroporation[78]. To improve
430 efficiency, heat-killed *Klebsiella aerogenes* was added after transformation. In
431 chemically-induced dimerization (CID) experiments (**Fig. 1D-I, Fig. 3C-E, Fig. 4, Fig
432 S4**), all cells were transformed with an unlabeled cAR1-tandem FKBP (cAR1-FKBP-
433 FKBP) in a pCV5 vector as well as an FRB-tagged protein in a separate pCV5 vector.
434 cAR1 was selected because it is a uniform membrane protein[79] and will therefore recruit
435 FRB-tagged proteins to the membrane evenly upon rapamycin addition (**Fig. 1D**).
436 mCherry-FRB-MHCKC was created using standard restriction digest cloning starting
437 with a GFP-MHCKC construct (from the D. Robinson lab). mCherry-FRB-GXCT$_{\Delta NT}$ was
438 made by inserting the PH and RhoGEF (DH) domains of GXCT [80] from a GFP-GXCT
439 construct (gift from the M. Iijima lab, JHU) into a pCV5 plasmid containing mCherry and
440 FRB. While both cAR1-2xFKBP and FRB vectors contain G418-resistance markers, a

441 significant population of cells simultaneously transformed with both have significant FRB
442 protein expression and membrane recruitment.

443 For optogenetic experiments (**Fig. 5**), cells were transformed with hygromycin-resistant
444 vector pDM358[81], containing an iLID[58] domain linked to the myristoylation domain of
445 PKBR1 (n150-ILID), which was previously shown to localize to the membrane [3]. Cells
446 were subsequently transformed with SSPB(R73Q)-tagRFP-GXCT$_{\Delta NT}$ in a pCV5 vector
447 (**Fig. 5A-C, Fig. 5G-H**) created by In-Fusion cloning or a dual-expression G418
448 resistance vector (O1N), containing mCherry-SSPB(R73Q)-GXCT$_{\Delta NT}$ and RBD-
449 emiRFP670 (**Fig. 5D-F, Fig. 5I-K**) created by GoldenBraid cloning[82].

450 pDM358 RBD-EGFP (**Fig. 1A, Fig. 1G-I, Fig. 3C-E, Fig. 4H-J**), LimE$_{\Delta Coil}$-EGFP (**Fig.
451 4E-H, S1A-C**), pDM358 PH$_{CRAC}$-YFP/LimE$_{\Delta Coil}$-RFP (**Fig. 2A-B, Fig. 2 I-J**), and
452 pDM358 PH$_{CRAC}$-YFP (**Fig. 3A-B**) were previously created in the Devreotes lab[3].
453 Hygromycin resistant vector pDRH EGFP-MyosinII (**Fig. S2A-B**), pDRH-Cortexillin I
454 (**Fig. S3A-B**), and pDRH-Dynacortin (**Fig. S4D-E**) were created in the the D. Robinson
455 lab. pDM358 EGFP-HSPC300 (**Fig. S1**) was a gift from the C. Huang lab (JHU).

456 **Microscopy:** For *Dictyostelium* imaging experiments, cells were seeded in 8-well Lab-
457 Tek chambers (Thermo-Fisher, 155409) and left to settle for ten minutes before the
458 media was gently aspirated and replaced with Development Buffer (DB) (5 mM
459 NA$_2$HPO$_4$, 5 mM KH$_2$PO$_4$, 1mM CaCl$_2$, 2 mM MgCl$_2$). In experiments with non-
460 electrofused vegetative cells, cells were allowed to sit for an hour starving in DB prior to
461 imaging to decrease photosensitivity. For experiments requiring cAMP stimulation (**Fig.
462 S2C-D, Fig. 2I-J**), growth-phase cells were washed and suspended in DB at a density
463 of 2×10^7 cells/ml. Cells were then developed by being shaken for 1 hour and
464 subsequently pulsed with 50–100 nM cAMP every 6 minutes and shaken for 4 hours.

465 For dHL60 cells, cells were seeded in Lab-Tek 8-well chambers coated with fibronectin
466 at approximately 35 μg/cm and allowed to adhere for one hour prior to imaging. Directly
467 prior to imaging, cells were treated with 200 nM N-Formyl-Met-Leu-Phe (FMLP) to
468 encourage migration.

469 Laser scanning confocal imaging was carried out on two microscopes: a Zeiss
470 AxioObserver inverted microscope with an LSM800 confocal module and a Zeiss
471 AxioObserver with 880-Quasar confocal module & Airyscan FAST module. On the
472 LSM800 microscope, GFP and YFP proteins were excited with a solid-state 488 nm
473 laser and on the 880 with an argon laser. mCherry and other red fluorescent proteins
474 were excited with a solid-state 561 nm laser on both systems. Emission wavelengths
475 collected were chosen to avoid overlap between GFP and mCherry emission profiles.
476 All imaging was done with 63X/1.4 PlanApo oil DIC objectives and appropriate raster
477 zoom. Brightfield images acquired using a transmitted-photomultiplier tube (T-PMT)
478 detector.

479 For Total Internal Reflection Fluorescence (TIRF) imaging, experiments measuring the
480 response of RBD to CK666 and latrunculin (**Fig. 2C-E**) were performed on a Nikon TiE

481 microscope with a solid state 561 nM laser for mCherry excitation, a 100x/1.49 Apo
482 TIRF objective, an RFP emission filter set, and a Photometrics Evolve 512 EMCCD
483 camera. Experiments measuring the response of RBD to RacE GEF recruitment (**Fig.**
484 **5D-F, Fig. I-K**) were performed on a Nikon Ti2-E microscope with an iLas2 Ring-TIRF
485 and optogenetics module (GATACA Systems). Red fluorescent proteins were excited
486 with a 561 nM solid-state laser and far-red proteins were excited with a 647 nm solid-
487 state laser. Global and local recruitment were accomplished using a 488 nM solid-state
488 laser connected to the iLas2 system. Cells were imaged using a 60x/1.49 Apo TIRF
489 objective and a Hamamatsu FusionBT camera.

490 **Cell fusion:** Protocol adapted from (Miao et al., 2019).Growth-phase cells were washed
491 twice with and then resuspended in SB (17 mM Sorensen Buffer containing 15 mM
492 KH_2PO_4 and 2 mM Na_2HPO_4, pH 6.0) at a density of 1.5×10^7 cells/ml. 3 ml of cells
493 were put into a 15-ml conical tube and rolled gently for ~ 30 min, to promote cell
494 clustering. 800 µl of rolled cells were transferred to a 4-mm-gap electroporation cuvette
495 (Bio-Rad, 1652081), using pipette tips whose edges were cut off to avoid breaking
496 clusters. Cells were then electroporated using the following settings: 1,000 V, 1 µF three
497 times, with 1–2 s between pulses. Then, 30 µl of cells was transferred to the center of a
498 well in an 8-well chamber and was left still for 5 min. 370 (**Fig. 2C-E**) or 470 (**Fig. 5D-F,**
499 **Fig. 5I-J**) µl of SB containing 2 mM $CaCl_2$ and 2 mM $MgCl_2$ was added to the well and
500 was pipetted briefly to suspend the cells evenly. After allowing cells to settle for 10
501 minutes, all media together with excess floating cells were removed and 450 µl of new
502 SB plus 2 mM $CaCl_2$ and 2 mM $MgCl_2$ was gently added to the well against the wall.
503 Cells were then allowed to recover for 1 h before imaging. 50 µg/ml Biliverdin was
504 added to cells expressing RBD-emiRFP670 (**Fig. 5D-F, Fig. 5I-J**) during the rolling
505 stage to activate emiRFP970 fluorescence.

506 **Preparation of Reagents and inhibitors**: Rapamycin (Millipore Sigma, 553210) was
507 dissolved in DMSO to a concentration of 10 mM. Then, 1 µl aliquots were diluted 1:200
508 in the imaging buffer of the experiment (DB or SB plus 2 mM $CaCl_2$ and 2 mM $MgCl_2$) to
509 a 10x concentration (50 µM). CK666 (Millipore Sigma, 182515) was dissolved in DMSO
510 to concentration of 100 mM. Then, 0.5 µl aliquots were diluted 1:100 in warm imaging
511 buffer of the experiment (DB, SB plus 2 mM $CaCl_2$ and 2 mM $MgCl_2$, or RPMI) to a 10x
512 concentration (1 mM). 2.5 µl aliquots of 1 mM latrunculin in DMSO (Millipore Sigma,
513 428026) were diluted 1:20 in the imaging buffer of the experiment, creating the 50 µM
514 10x solution used for the experiments (DB, SB plus 2 mM $CaCl_2$ and 2 mM $MgCl_2$, or
515 RPMI). cAMP (Millipore-Sigma, A6885) was dissolved to 1 mM in water and then diluted
516 to a 10x working concentration (1 µM or 10 nM) in DB. Caffeine (Millipore-Sigma,
517 1085003) was dissolved to 1 M in water and then diluted to a 10x concentration (30 µM)
518 in SB plus 2 mM $CaCl_2$ and 2 mM $MgCl_2$. FMLP was dissolved in DMSO to a
519 concentration of 10 mM and then individual aliquots were diluted in RPMI to a 10X
520 concentration (2 µM).

Chemically induced dimerization and inhibitor experiments: When imaging FRB protein recruitment without any additional inhibitors (**Fig. 1D-I, Fig. 4, Fig. S4**), 50 µl of 50 µM rapamycin was added to a well containing 450 µl of buffer at the indicated time for a final concentration of 5 µM. Similarly, in experiments with CK666 alone (**Fig. 2A-B, Fig. S3, Fig. 3A-B**), 50 µl of 1 mM CK666 was added to a well containing 450 µl of buffer at the indicated time for a final concentration of 100 µM. For experiments with rapamycin and CK666 (**Fig. 3C-E, Fig. S4A-C**) or CK666 and latrunculin (**Fig. 2C-H**), 50 µl of each of the drugs was added to a well containing 400 µl of buffer at the indicated times for a final concentration of 5 µM Rapamycin, 100 µM CK666, and 5 µM latrunculin. In **Fig. 2C-E**, cells were pre-incubated with 3 mM caffeine, and all drugs were diluted in buffer containing 3 mM Caffeine.

For cAMP stimulation experiments, cells were pre-treated in 400 µl DB containing rapamycin (**Fig. S2C-D**), CK666, or CK666 and latrunculin at the concentrations indicated above for 30 minutes. Then, 50 µl of 10 nM cAMP was added to the well during imaging followed at least a minute later by 50 µl of 1 µM cAMP for final concentrations of 1 nM and 100 nM respectively.

In **Fig. S2A-B**, the + rap population was treated with 5 µM rapamycin at least 30 minutes prior to imaging. For cells pre-treated with CK666 in **Fig. 2F-G** and **Fig. 3C-E**, cells were treated with 100 µM CK666 at least 30 minutes prior to imaging.

Optogenetics: In **Fig. 5A-C** and **5G-H**, experiments were performed on the Zeiss 800 LSM. For global activation (**Fig. 5A-C**), the 488 laser was switched on and scanned across the entire field of imaging for the indicated time. For local activation (**Fig. 5G-H**), the microscope's bleaching tool was used to scan the 488 laser in an approximately 1 µm square 1 µm away from the cell edge.

In **Fig. 5D-F** and **5I-K**, experiments were performed on the iLas TIRF system. For global activation (**Fig. 5D-F**), the cells were exposed to 488 laser light at every timepoint for the indicated time. For local activation (**Fig. 5I-K**), the microscope's targeted illumination tool was used to scan the 488 laser in an approximately 300 µm square on the cell membrane at the indicated location.

Image analysis: To quantify biosensor intensity on the membrane in confocal images, single cells were selected for analysis using cell health, biosensor expression, and FRB/SSPB protein recruitment (if applicable). Cells were then tracked manually using the Manual Tracking plugin in FIJI[83]. After manual tracking, masks of individual cells were created in MATLAB (Mathworks). Background was subtracted from the image by applying a 2D gaussian blur filter with a high σ value (100) to the original image and then subtracting the resulting image from the original. Then, a threshold intensity value was calculated on the background-subtracted image using Otsu's method[84] and applied to a smoothed version of the background-subtracted image created using a 2D gaussian blur filter with a low σ value (2). Masks were then modified by performing a morphological closing operation followed by a hole-filling operation. The selected cell

561 was then identified by comparing the centroid of every object in the binary mask to the
562 manual tracking coordinates and removing every object but the object closest to the
563 tracking coordinate. Finally, a watershed filter was applied to remove cells which
564 transiently collided with the selected cell. If the selected cell could not be satisfactorily
565 separated from neighbors it was discarded in the dataset. All shape and motion
566 descriptors were created using the properties extract from this centroid using Matlab's
567 regionprops function.

568 These binary masks were then used to create kymographs of membrane intensity over
569 time. The boundary of the binary mask was identified and then smoothed using a
570 moving average filter. Then, the membrane intensity (I_M) at equally spaced points along
571 the membrane was determined by taking a 3 µm long, 1-pixel wide line scan
572 perpendicular to the boundary and finding the maximum intensity along that boundary.
573 I_M was equal to the sum of that brightest pixel along and any pixel 250 nm in either
574 direction of the pixel along the line scan. The number of pixels (n_{pix}) summed was
575 saved for later. Then, cytosolic intensity (I_C) was calculated by performing a binary
576 erosion to original image mask to remove the membrane and then taking the average
577 intensity inside that eroded mask. A background intensity (I_{bg}) was acquired by
578 manually selecting a 1 µm box outside of a cell and taking the average intensity in that
579 box. Finally, the background-corrected membrane-to-cytosol ratio (**M/C**) at each point
580 on the membrane was acquired using this formula: $\frac{I_M - I_{bg} \times n_{pix}}{I_C - I_{bg}}$. This value was then
581 used for kymograph display.

582 To calculate the average M/C ratio at each timepoint, each line in a kymograph,
583 excluding black space, was averaged. Alternatively, for dim biosensors with variable
584 expression levels, (**Fig. 1C, 1I**), the percentage of pixels in each line above an intensity
585 threshold was calculated. This threshold was determined by hand-identifying 3 separate
586 patches in the image and finding the value 10 percentile points lower than the average
587 of those three pixels in the distribution of all kymograph intensities. To average over an
588 entire movie (**Fig. 1C**), the intensity at each timepoint recorded was simply averaged.
589 To create a plot of average intensity or area over time, all traces were synchronized to
590 the specified perturbation and then all values were placed in time "bins" relative to 0
591 where 0 is the rightmost edge of a bin and then averaged. Bin width was determined by
592 the rate of acquisition but was generally 30 seconds. In all cases, intensities were then
593 normalized to the average intensity from -1 minute to 0.

594 The calculate the membrane intensity in TIRF images (**Fig. S1B, S2B, 2D-E, 5E-F**), a
595 mask of the entire cell was first created at every timepoint using Otsu's method on a
596 background-subtracted image similar to confocal images. For the average intensity (**Fig.
597 2D-E, S2B**), all pixels in the original image within this mask were averaged and then
598 background-corrected by subtracting the average intensity of a 1 µm box outside the
599 cell. For data with multiple timepoints (**Fig. 2D-E**), intensities were then normalized to
600 the average intensity from -1 minute to 0 prior to CK666 addition. To obtain the
601 percentage of area occupied by a wave (**Fig. S1B, 5E-F**), a wave mask was created

602 using a threshold calculated from only intensities inside the cell mask on a frame in the
603 movie where there is a clear active wave. The percentage was calculated by dividing
604 the area of the wave mask by the area of the cell mask and multiplying by 100. All cells
605 were selected based on criteria of cell health, biosensor expression, SSPB recruitment
606 (where applicable) and wave formation prior to perturbation.

607 To calculate the average biosensor patch number (**Fig. 3B, 3E**), the number of patches
608 was identified manually at every timepoint. The total number of patches over an interval
609 (for example, all timepoints prior to CK666 addition) was then divided by the total time of
610 that interval.

611 To calculate the angle of protrusion formation relative to SSPB recruitment (Fig. 5H), in
612 FIJI, a line was drawn from the center of the cell to the center of the stimulation region
613 and then another from the center of the cell to center of the first protrusion formed after
614 stimulation. The angle between these two lines was calculated using each of their
615 angles relative to the x axis of the image.

616 To calculate the RBD extinction from light (**Fig. 5K**), a linear kymograph was created by
617 drawing a line through the region of light stimulation and through the wave targeted by
618 the stimulation in FIJI and then using the reslice tool. The extinction rate is calculated by
619 drawing one line along the border of the RBD region 30 s (10 timepoints) before
620 stimulation and another along the border 30 s after. The height of this line (μm traveled)
621 divided by the width (time) indicates the rate the RBD patch is displacing from the
622 region of stimulation.

623 To calculate the cytoplasmic intensity of RBD in cAMP MHCKC expressing cells with or
624 without rapamycin (**Fig. S2D**), the cytoplasm of a cell was identified manually using the
625 freehand selection tool in FIJI. The intensity in this selection was averaged and then
626 background-corrected by subtracting the average intensity of a 1 μm box outside the
627 cell. Intensities were then normalized to the average intensity at 0.

628 **Simulations:** The simulations are based on a model, previously described, in which
629 three interacting species, RasGTP, PIP2, and PKB, form an excitable network [24]. The
630 concentrations of each of these molecules is described by stochastic, reaction-diffusion
631 partial differential equations:

632 $$\frac{\partial[\text{Ras}]}{\partial t} = -(a_1 + a_2[\text{PKB}])[\text{Ras}] + \frac{a_3}{1 + a_4^2[\text{PIP2}]^2} + a_5 + w_F + D_{\text{Ras}}\nabla^2[\text{Ras}]$$

633 $$\frac{\partial[\text{PIP2}]}{\partial t} = -(b_1 + b_2[\text{Ras}])[\text{PIP2}] + b_3 + w_B + D_{\text{PIP2}}\nabla^2[\text{PIP2}]$$

634 $$\frac{\partial[\text{PKB}]}{\partial t} = -c_1[\text{PKB}] + c_2[\text{Ras}] + w_F + D_{\text{PKB}}\nabla^2[\text{PKB}]$$

635 In each of these equations, the final term represents the diffusion of the species, where
636 D_* is the respective diffusion coefficient and ∇^2 is the spatial Laplacian (in one or two
637 dimensions). The second-to-last terms represent the molecular noise. Our model

638 assumes a Langevin approximation in which the size of the noise is based on the
639 reaction terms[85]. For example, in the case of PKB, the noise is given by

640
$$w_F(t) = \alpha \sqrt{c_1[\text{PKB}] + c_2[\text{Ras}]} \times w(t)$$

641 where $w(t)$ is a zero mean, unit variance Gaussian, white noise process. In the
642 simulations, the size of this noise was adjusted with the empirical parameter α.

643 In addition to the excitable dynamics described above, we incorporated two other terms.
644 The first represents feedback from branched actin onto Ras. Since the cytoskeleton is not
645 directly modeled, we model the origin of this feedback from PKB, which is upstream to
646 the cytoskeleton[24].

649
$$\frac{\partial [\text{P}_{\text{BrAc}}]}{\partial t} = -p_1[\text{P}_{\text{BrAc}}] + p_2[\text{PKB}] + w_{P_{\text{BrAc}}} + D_{P_{\text{BrAc}}} \nabla^2[\text{P}_{\text{BrAc}}]$$

647 The second feedback loop accounts for the inhibitory regulation by actomyosin on Ras
648 that originates from back molecules, such as PIP2.

651
$$\frac{\partial [\text{P}_{\text{AcMy}}]}{\partial t} = -p_3[\text{P}_{\text{AcMy}}] + p_4[\text{PIP2}] + w_{P_{\text{AcMy}}} + D_{P_{\text{AcMy}}} \nabla^2[\text{P}_{\text{AcMy}}]$$

650
652 Together, they modify the equation for Ras:

653
$$(a_1 + a_2[\text{PKB}])[\text{Ras}] \mapsto \frac{\left(a_1 + a_2[\text{PKB}] + a_{P_{\text{AcMy}}}[\text{P}_{\text{AcMy}}]\right)[\text{Ras}]}{1 + a_{P_{\text{BrAc}}}[\text{P}_{\text{BrAc}}]}$$

654 having the effect of increasing front and back contributions. In both equations, we
655 include noise and diffusion terms.

656 Simulations were run on MATLAB 2023a (Mathworks) on custom-code based on the Ito
657 solution in the Stochastic Differential Equation toolbox
658 (http://sdetoolbox.sourceforge.net). Two-dimensional simulations were used to recreate
659 the observed wave patterns of larger electrofused cells, and so assume a grid 40 μm
660 × 40 μm with a spacing of 0.4 μm × 0.4 μm per grid point (*i.e.*, 100 × 100 points) and
661 zero flux boundary conditions. The one-dimensional simulations aim to recreate the
662 membrane fluorescence observed in single-cell confocal images. The dimension is,
663 therefore, smaller, assuming a cell radius of 5 μm and a spacing of 0.25 μm, resulting in
664 $2\pi \times 5/0.25 \approx 126$ points along the perimeter, and periodic boundary conditions.

Table 1: Parameters used in simulation

Parameter	Value	Units	Parameter	Value	Units
a_1(1D)	1.5	s^{-1}	a_1(2D)	1.2	s^{-1}
a_2(1D)	55.5	µM^{-1} s^{-1}	a_2(2D)	44.4	µM^{-1} s^{-1}
a_3	12	s^{-1}	a_4	444	µM^{-1}
a_5	5.4×10^{-3}	s^{-1}	b_1	0.06	s^{-1}
b_2	8880	µM^{-1} s^{-1}	b_3	8.20	µM s^{-1}
c_1	0.15	µM^{-1} s^{-1}			
c_2 (1D)	1.50	µM^{-1} s^{-1}	c_2 (2D)	0.75	µM^{-1} s^{-1}
p_1	0.05	µM^{-1} s^{-1}	p_2	0.05	µM^{-1} s^{-1}
p_3	0.05	µM^{-1} s^{-1}	p_4	0.05	µM^{-1} s^{-1}
D_{Ras}	0.15	µm^2/s	D_{PIP2}	0.15	µm^2/s
D_{PKB} (1D)	1.50	µm^2/s	D_{PKB} (2D)	0.25	µm^2/s
D_{P_F}	0.0125	µm^2/s	D_{P_B}	0.025	µM^{-1}
a_{P_F}(1D)	3	µM^{-1}	a_{P_F}(2D)	6	µM^{-1} s^{-1}
a_{P_B} (1D)	6	µM^{-1} s^{-1}	a_{P_B} (2D)	0.8	µM^{-1} s^{-1}
α (1D)	0.0833		α (2D)	0.0417	

665

666   To determine the effect of these firings on cell movement, we follow an approach that
667   simulates the movement of cells using a center-of-mass approximation. Using the
668   spatially dependent level of activity, shown in the kymographs in **Fig. 6B**, we generated
669   a series of force vectors normal to the cell surface. The vector sum of all these vectors
670   was used to obtain a net protrusive force. After scaling this force so that it is in the
671   range of experimentally observed protrusive pressures (0.5–5 nN/m^2), we used it to
672   push a viscoelastic model of *Dictyostelium* mechanics[86]. In this model, the net stress in
673   the *x*-direction: σ (the direction of the gradient) alters the center-of-mass position (CM)
674   through the following dynamics:

675
$$\ddot{x} + (k_c/\gamma_c)\dot{x} = (1/\gamma_c + 1/\gamma_a)\dot{\sigma}_x + (k_c/\gamma_c)\sigma_x$$

676   with a similar equation for the displacement in the *y*-direction (CM). Parameter values
677   adopted from previous work[87] are provided in the following table:

678

Table 2: Parameters from Yang et al.		
Parameter	**Value**	**Units**
γ_a	6.09	s^{-1}
γ_c	0.064	$\mu M^{-1}\ s^{-1}$
k_c	0.098	$\mu M^{-1}\ s^{-1}$

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Contributions

JK, PND, and DNR conceived the experiments. JAK performed the experiments and most analysis of experimental data. AH and PAI assisted with image analysis. PB and PA. developed the computational model and performed simulations. The manuscript was primarily written by JK and PND. with some initial writing generated by ChatGPT3 (OpenAI). Text pertaining to computational modeling was written by PB and PAI. DNR assisted in editing the paper.

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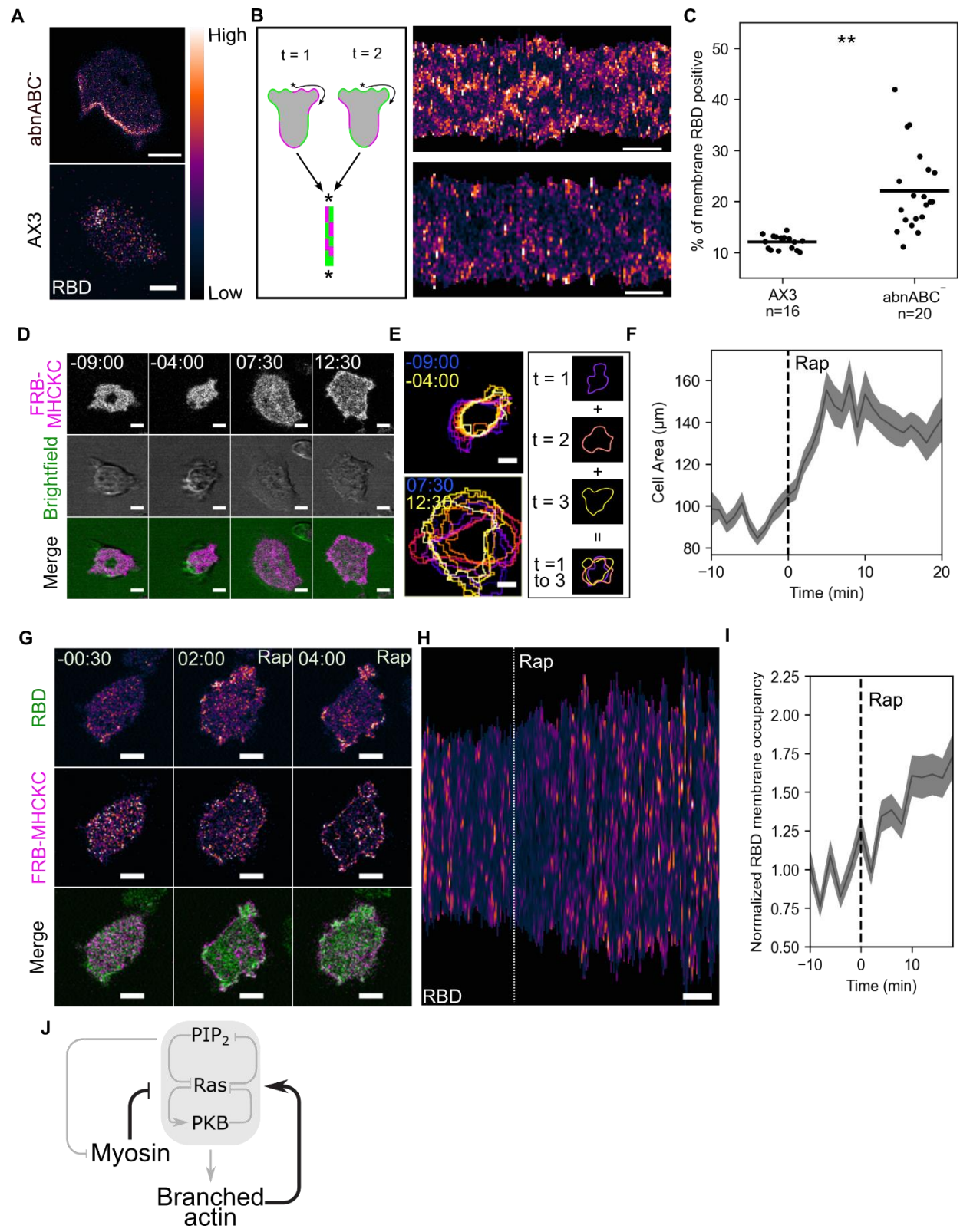
923 **Figure 1**

Figure 1: Cytoskeletal feedback loops at the cell front and back control Ras activity.

(A) Scanning confocal imaging of Ras activation (RBD-EGFP) in wild-type (AX3) or *actobindin ABC* triple knockout (*abnABC*-) *Dictyostelium* cells. **(B)** Diagram (left) and experimental data (right) of RBD membrane kymographs corresponding to the movies in (A) (right). *Scale bars = 2 minutes.* **(C)** Individual (dots) and average (lines) percentages of the membrane periphery with RBD localization significantly above background in AX3 and *abnABC*- cells. *n = cells, **= p< 0.005.* **(D)** Scanning confocal imaging of mCherry-FRB-MHCKC membrane recruitment and cell shape (brightfield) in AX3 cells. Cells are also expressing an unlabeled membrane-localized FKBP domain (cAR1-2xFKBP, see methods). *t = 00:00 indicates rapamycin addition.* **(E)** Examples (left) and diagram (right) of temporal color projections of cell outlines corresponding to the movie in (D). Blue and yellow times indicate the first and last images in the projection, respectively. **(F)** Average (line) and SEM (shaded area) of cell area before and after MHCKC recruitment by rapamycin addition (dashed line, t = 0). *n = 16 cells.* **(G)** Scanning confocal imaging of RBD and MHCKC membrane recruitment in AX3 cells. *t=00:00 indicates rapamycin addition.* **(H)** Membrane kymograph of Ras activation corresponding to the movie in (G). *Dashed line indicates rapamycin addition, scale bar = 6 minutes.* **(I)** Average (line) and SEM (shaded area) of normalized percentages of the membrane periphery with RBD localization significantly above background before and after MHCKC recruitment by rapamycin addition (dashed line, t = 0). *n = 20 cells.* **(J)** Schematic of the core signaling system controlling cell migration (shaded area) as well as cytoskeletal effectors. Gray arrows indicate previously known interactions while the black arrows indicate the positive feedback from branched actin (**Fig 1A-C, S1A-B**) and the negative feedback from myosin (**Fig 1D-I**) shown here. *Time is in min:sec; scale bars = 5 µm unless otherwise noted.*
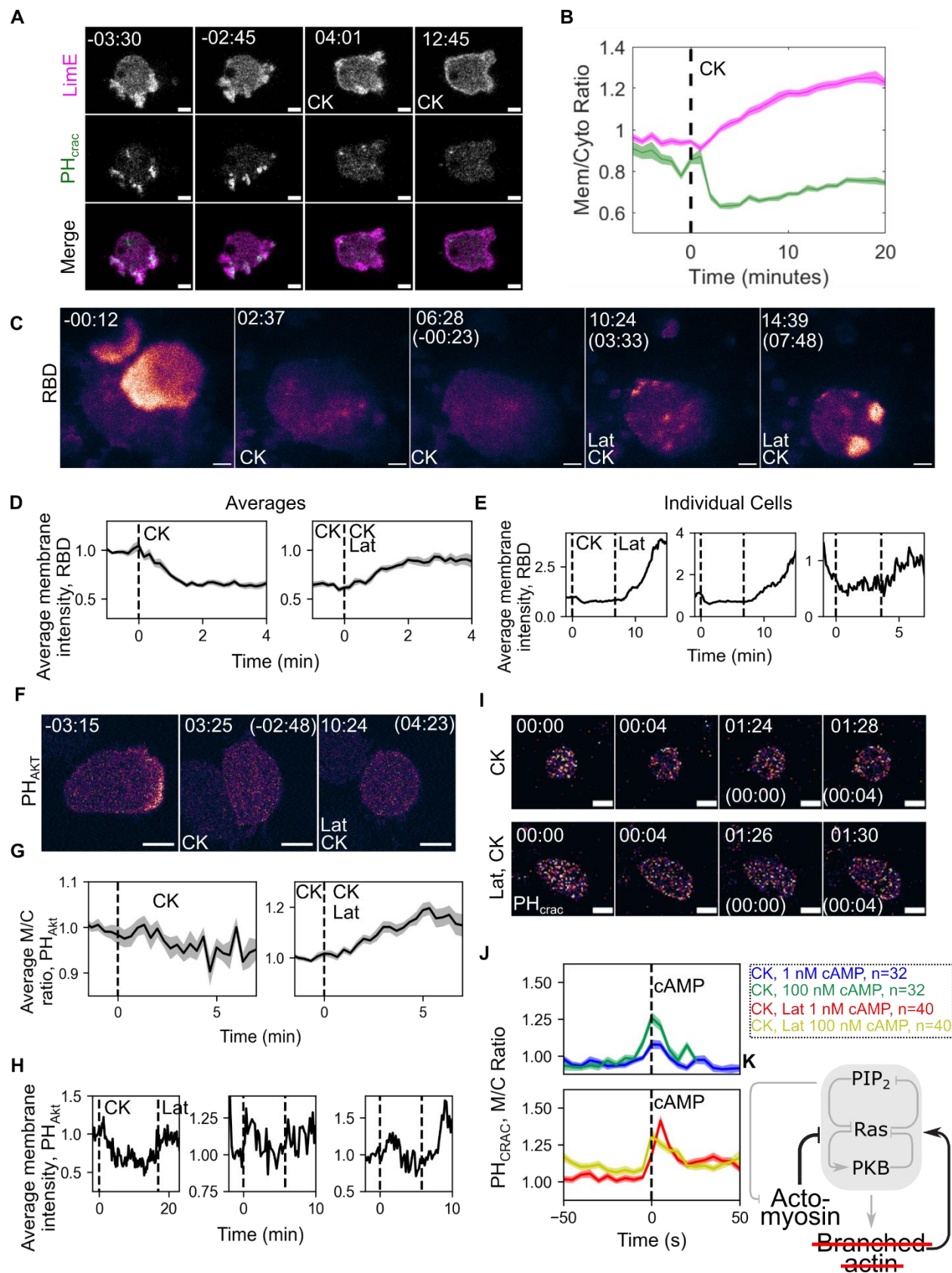
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Figure 2: Cortical actin suppresses signaling network activation.

(A) Scanning confocal imaging of polymerizing actin (LimE$_{\Delta Coil}$-RFP) and PIP$_3$ levels (PH$_{CRAC}$-YFP) in wild type (AX3) *Dictyostelium* cells before and after treatment with the Arp2/3 inhibitor CK666 (CK). *t = 00:00 indicates CK666 addition*. **(B)** Average (line) and SEM (shaded area) of the membrane-to-cytosol intensity ratio of LimE (magenta) and PH$_{CRAC}$ (green) before and after CK666 addition (dashed line, t = 0). *n = 27 cells*. **(C)** TIRF imaging activated Ras (RBD-mCherry) in electrofused ("giant") AX3 cells before and after CK666 addition and subsequently latrunculin addition. Cells are incubated in caffeine to raise basal activity levels. *t = 00:00 indicates the addition of CK666 or, in parentheses, latrunculin*. **(D)** Average (line) and SEM (shaded area) of average RBD intensity on the membrane of giant AX3 cells in buffer before and after CK666 addition (left, dashed line, t = 0) or in CK666 before and after latrunculin addition (right, dashed line, t = 0). The left plot excludes data after latrunculin addition while the right excludes data before CK666 addition. *n = 22 cells*. **(E)** Selected individual traces from the dataset in (D). The left plot corresponds to the movie in (C). t = 00:00 indicates CK666 addition; dashed lines correspond to indicated drug addition. **(F)** Scanning confocal imaging of PIP3 levels (RFP-PH$_{AKT}$) in human neutrophil-like (dHL60) cells before and after the addition of CK666 addition and subsequently latrunculin addition. *t = 00:00 indicates the addition of CK666 or, in parentheses, latrunculin*. **(G-H)** Average (G, line), SEM (G, shaded area), and individual traces (H) of the normalized PH$_{AKT}$ membrane-to-cytosol ratio before and after CK666 and subsequently latrunculin addition in dHL60 cells. The right plot in (G) contains both cells starting in buffer and cells pre-incubated in CK666 while the left only contains cells starting in buffer. The left plot in (H) corresponds to the movie in (F), all dashed lines indicate drug addition. *n = 27 cells prior to CK666 addition, 55 cells after CK666 addition and latrunculin addition.* **(I)** Scanning confocal imaging of PIP3 levels in developed AX3 *Dictyostelium* cells treated with CK666 (CK) or CK666 and latrunculin (CK, Lat) before and after the addition of 1 nM cAMP and subsequently 100 nM cAMP. *t = 00:00 indicates the addition of 1 nM cAMP or, in parentheses, 100 nM cAMP*. **(J)** Average (line) and SEM (shaded area) of the membrane-to-cytosol ratio of PH$_{CRAC}$ before and after the indicated dose of cAMP. *n=cells*. **(K)** Arp2/3 experiments reveal negative feedback to signaling from F-Actin left behind after CK666 treatment and positive feedback from branched actin networks. Red line striking out "Branched actin" reflects the CK666 treatment effect. *Time is in min:sec; scale bars = 5 µm*.
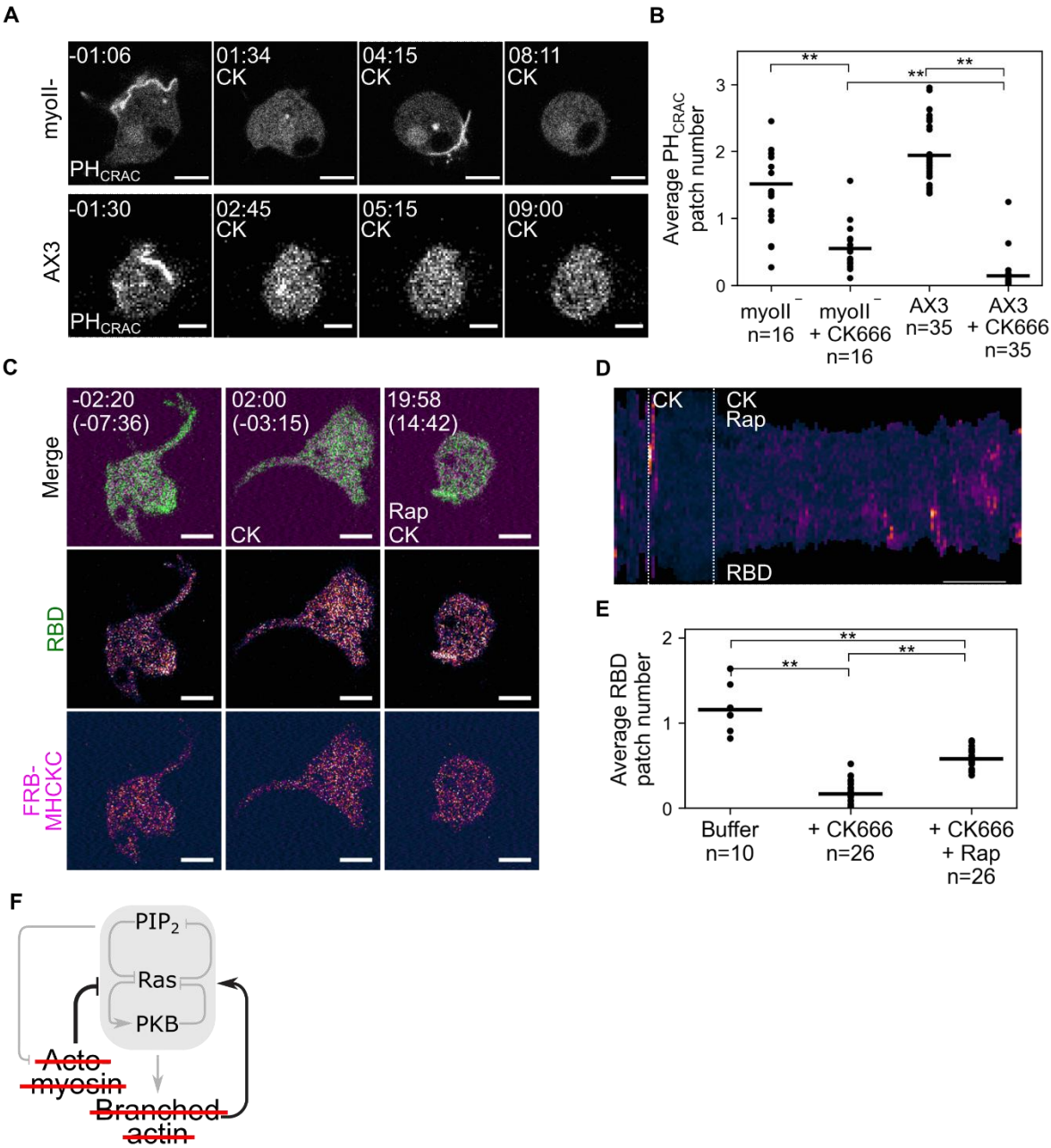
Figure 3: The actomyosin cortex exhibits negative feedback onto signaling networks.

(A) Scanning confocal images of PIP$_3$ levels (PH$_{CRAC}$-YFP) in wild type (AX3) and *myosin II*-null (*myoII-*) *Dictyostelium* cells before and after CK666 addition. *t = 00:00 indicates CK666 addition.* **(B)** Average (lines) and individual (dots) mean number of PIP$_3$ patches over time before and after CK666 addition in AX3 and *myoII-* cells. *n = cells, ** = p < 0.005.* **(C)** Scanning confocal images of Ras activation (RBD-EGFP) before and after CK666 addition and subsequently mCherry-FRB-MHCKC membrane recruitment in AX3 cells. Cells are also expressing an unlabeled membrane-localized FKBP domain (cAR1-2xFKBP). *t = 00:00 indicates the addition of CK666 or, in parentheses, rapamycin.* **(D)** Membrane kymograph of Ras activation corresponding to the movie in (C). *Dashed lines represent the addition of specified drug, scale bar = 5 minutes.* **(E)** Average (lines) and individual (dots) mean number of RBD patches over time before and after CK666 addition and subsequently MHCKC recruitment by rapamycin addition. *n = cells, ** = p < 0.005.* **(F)** The partial reversal of CK666's effect on signaling by ablating myosin (**Fig 3A-E**) indicates that the actomyosin cortex as an ensemble feeds back negatively on cell signaling. Red lines indicate that Arp 2/3 and Myosin have been eliminated or reduced. *Time is in min:sec; scale bars = 5 µm unless otherwise noted.*
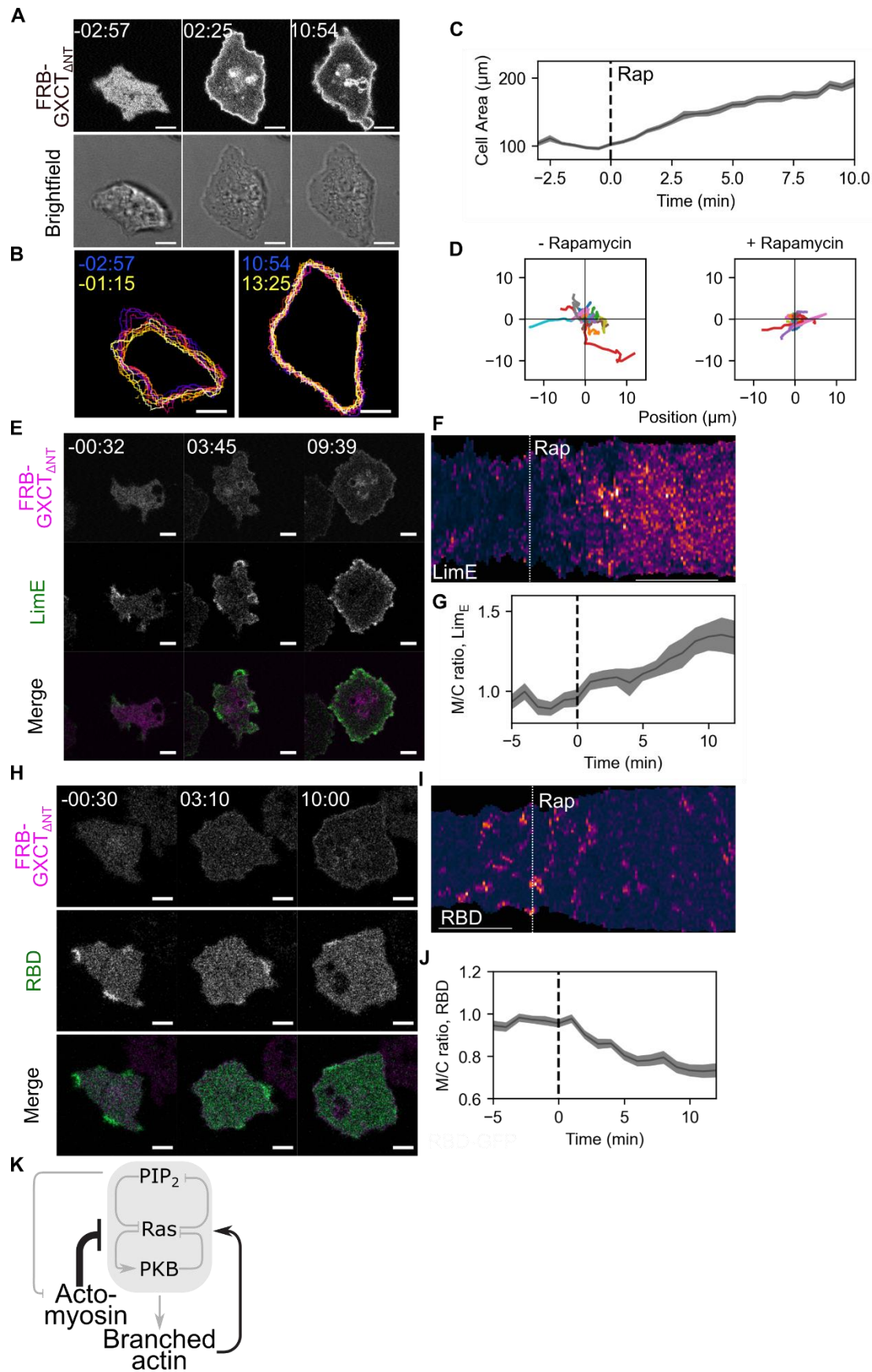
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Figure 4: Increasing the abundance of the actomyosin cortex using RacE leads to signaling inhibition.

(A) Scanning confocal imaging of RacE-GEF (mCherry-FRB-GXCT$_{\Delta NT}$) membrane recruitment and cell shape in wild type (AX3) *Dictyostelium* cells. Cells are also expressing an unlabeled membrane-localized FKBP domain (cAR1-2xFKBP). *t = 00:00 indicates rapamycin addition.* **(B)** Temporal color projections of cell outlines corresponding to the movie in (A). Blue and yellow times indicate the first and last images in the projection, respectively. **(C)** Average (line) and SEM (shaded area) of cell area in AX3 cells before and after GXCT recruitment (dashed line, t=0). *n = 35 cells.* **(D)** Traces of cell movement in AX3 cells 200 seconds before and after GXCT recruitment. *n = 35 cells.* **(E)** Scanning Confocal imaging of GXCT recruitment and polymerizing actin (LimE$_{\Delta Coil}$-EGFP) in AX3 cells. *t = 00:00 indicates rapamycin addition.* **(F)** Membrane kymograph of LimE from the movie in (E). *Dashed line indicates rapamycin addition, scale bar = 5 minutes.* **(G)** Average (line) and SEM (shaded area) membrane-to-cytosol ratio of LimE before and after GXCT recruitment by rapamycin addition (dashed line, t = 0). *n = 8 cells.* **(H)** Scanning Confocal imaging of GXCT recruitment and Ras activation (RBD-EGFP) in AX3 cells. *t = 00:00 indicates rapamycin addition.* **(I)** Membrane kymograph of RBD from the movie in (H). *Dashed line indicates rapamycin addition, scale bar = 5 minutes.* **(J)** Average (line) and SEM (shaded area) membrane-to-cytosol ratio of RBD before and after GXCT recruitment by rapamycin addition (dashed line, t = 0). *n = 9 cells. Time is in min:sec.* **(K)** Increasing the abundance of the actomyosin cortex (thick black arrow) inhibits the core signaling module. *Scale bars = 5 µm unless otherwise noted.*
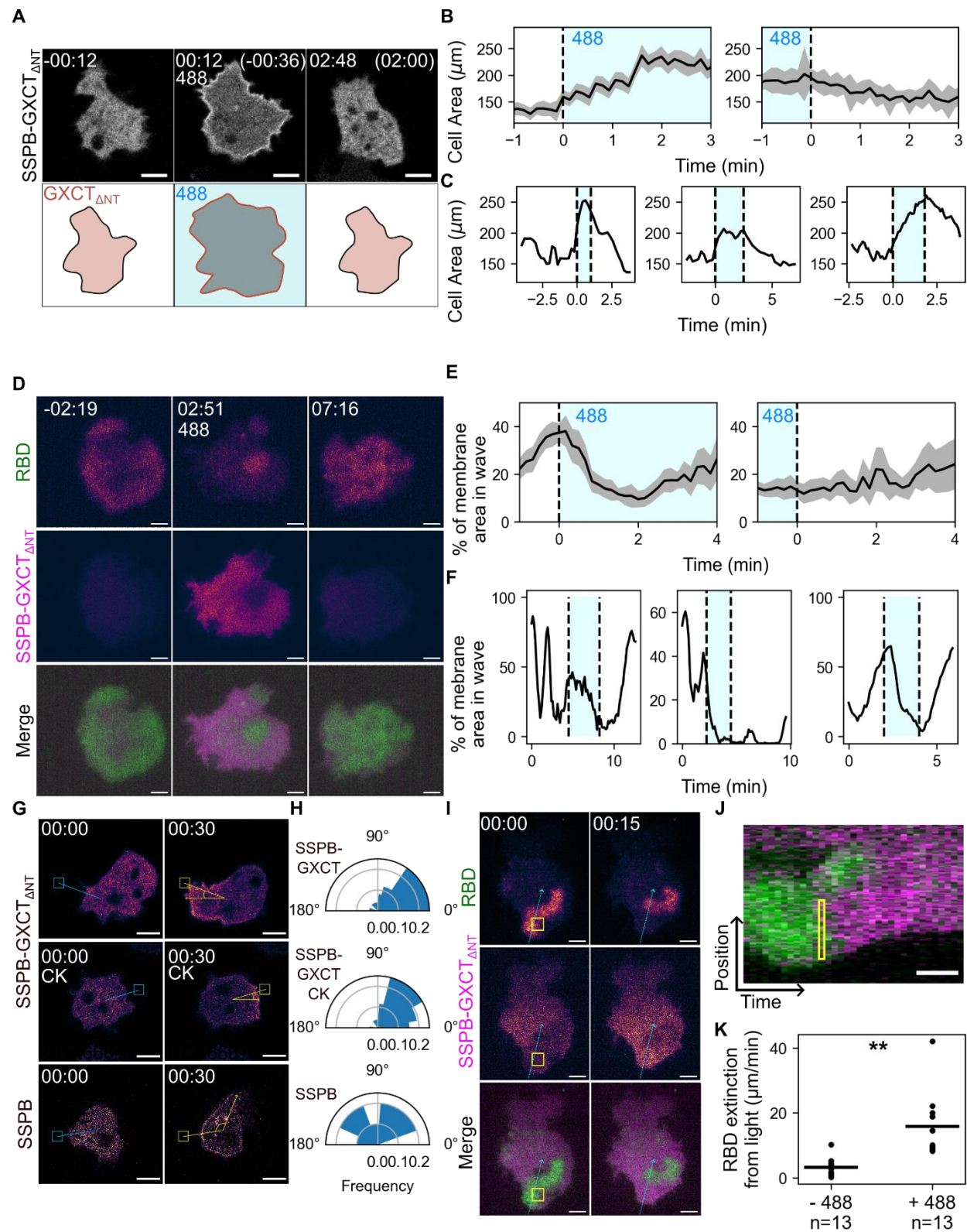
Figure 5: RacE reversibly and locally control cell signaling and actin polymerization.

1033   **(A**) Scanning confocal imaging of RacE-GEF (tagRFP-SSPB-GXCT$_{\Delta NT}$) optical

1034   membrane recruitment in wild type (AX3) *Dictyostelium cells*. Cells are also expressing

1035   an unlabeled membrane-localized iLID domain (N150-ILID, see methods). *t = 00:00*

1036   *indicates blue light exposure or blue light loss (parentheses).* **(B)** Average (lines) and

1037   SEM (shaded area) of cell area before and after GXCT membrane recruitment (left,

1038   dashed line) or GXCT membrane dissociation (right, dashed line). *n = 17 cells (left) and*

1039   *6 cells (right).* **(C)** Individual traces of cell area in cells before, during (shaded area), and

1040   after GXCT recruitment. The plot on the left corresponds to the movie in (A). **(D)** TIRF

1041   imaging of Ras activation (RBD-emiRFP670) before, during, and after GXCT

1042   recruitment in electrofused ("giant") AX3 cells. Cells are treated with 50 µg/ml Biliverdin

1043   to activate emiRFP670 fluorescence. *t = 00:00 indicates blue light exposure.* **(E)**

1044   Average (lines) and SEM (shaded area) of the percentage of the cell membrane with

1045   RBD localization significantly above background before and after GXCT membrane

1046   recruitment (left, dashed line) or GXCT membrane dissociation (right, dashed line). *n =*

1047   *7 cells.* **(F)** Individual traces of the percentage of the cell membrane with RBD

1048   localization significantly above background in giant cells before, during (shaded area),

1049   and after GXCT recruitment. The plot on the left corresponds to the movie in (D). **(G)**

1050   Scanning confocal imaging of cell protrusion formation after local recruitment of SSPB-

1051   GXCT or SSPB alone. +CK indicates cells were pre-treated with CK666. Boxes indicate

1052   the region of blue light exposure; arrows form a line between the center of the

1053   protrusion formed after stimulation and the center of the cell. *t = 00:00 indicates the last*

1054   *timepoint before blue light exposure.* **(H)** Angular histograms of the angle formed

1055   between the center of the protrusion and the location of GXCT recruitment relative to

1056   the cell center as demonstrated in (G). *n = 26 cells, SSPB-GXCT and SSPB-GXCT +*

1057   *CK666. n = 15 cells, SSPB.* **(I)** TIRF imaging of RBD membrane localization before and

1058   after local GXCT recruitment in giant AX3 cells. The yellow box indicates the region of

1059   blue light exposure and the blue arrow indicates the line and direction for linear

1060   kymograph creation. *t = 00:00 indicates the last timepoint before blue light exposure.* **(J)**

1061   Linear kymograph of GXCT recruitment and RBD intensity corresponding to the blue

1062   line in (I). Yellow box indicates the approximate region of blue light exposure. *Scale bar*

1063   *indicates 20 seconds.* **(K)** Quantification of the motion of RBD waves away from the

1064   region of GXCT recruitment (see methods). Because this measurement is a composite

1065   of RBD translocation and disappearance it is not a true velocity. *n = cells, ** = p <*

1066   *0.005. Time is in min:sec; scale bars = 5 µm unless otherwise noted.*
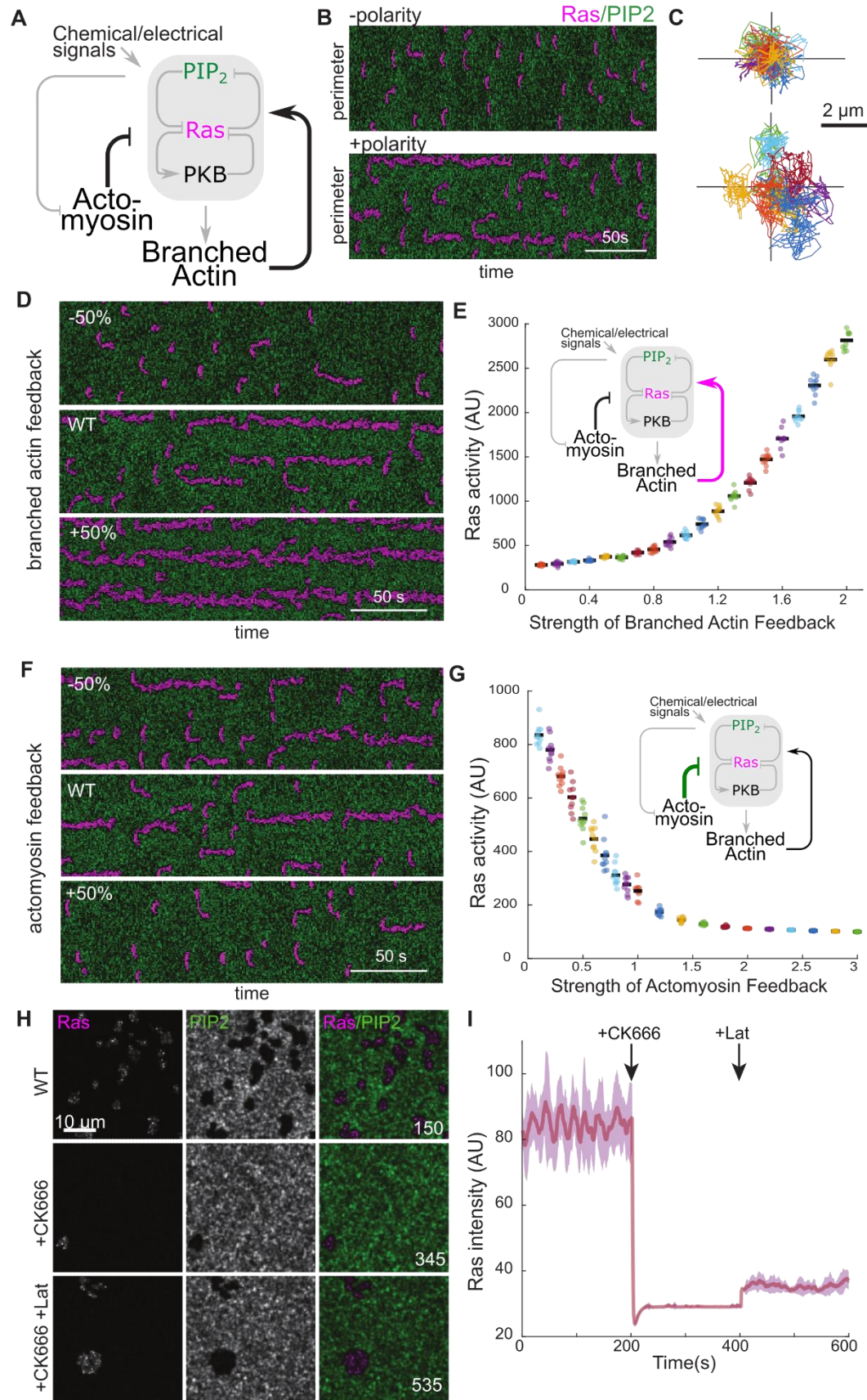
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Figure 6: Cytoskeletal networks can create polarity by feeding back onto a core signaling module.

(A) Schematic showing the signal transduction network involving Ras/ PIP2 and PKB and how they couple to the two types of actin feedback loops. **(B)** Kymographs showing activity around the cell perimeter as function of time. PIP2 and Ras are shown in green and magenta respectively. The top and bottom correspond to simulations without and with the feedback loops, respectively. **(C)** Simulated cell trajectories of 10 cells each with feedback loops turned off (top) and on (bottom). **(D)** Kymographs showing wave activity across cell perimeter for varying strengths of the branched actin feedback. **(E)** Total Ras activity around the cell perimeter with respect to the strength of the branched actin feedback. Wildtype corresponds to a strength of 1. Black bar denotes the mean of 10 simulations per strength. Simulations with total Ras activity less than 500 showed no firings. **(F)** Kymographs showing wave activity across cell perimeter for varying strengths of the actomyosin feedback. **(G)** Total Ras activity around the cell perimeter with respect to the strength of the actomyosin feedback. Wildtype corresponds to a strength of 0.4. Black bar denotes the mean of 10 simulations per strength. Simulations with total Ras activity less than 200 showed no firings. **(H)** Frames from a 2D simulation of effects of adding CK666 and then Latrunculin to wild type cells. The three rows represent waves in the wildtype cell, waves after CK666 addition, and subsequent Latrunculin treatment. **(I)** The total Ras activity for simulations as in panel H. The solid line and the shaded area represent the mean ± 1 standard deviation. In all the simulations the CK666 effect is incorporated at the 200 s and the additional Latrunculin effect is added at the 400 s. *Scale bars = 10 microns*