

¹ Neural geometrodynamics, complexity, and plasticity: a
² psychedelics perspective

³ G. Ruffini^{1*}, E. Lopez-Sola^{1,2}, J. Vohryzek^{2,3} and R. Sanchez-Todo^{1,2}

¹ Brain Modeling Department, Neuroelectrics, Barcelona

² Computational Neuroscience Group, UPF, Barcelona

³ Centre for Eudaimonia and Human Flourishing, Linacre College, University of Oxford

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⁵ **Abstract**

We explore the intersection of neural dynamics and the effects of psychedelics in light of distinct timescales in a framework integrating concepts from dynamics, complexity, and plasticity. We call this framework *neural geometrodynamics* for its parallels with general relativity's description of the interplay of spacetime and matter. The geometry of trajectories within the dynamical landscape of "fast time" dynamics are shaped by the structure of a differential equation and its connectivity parameters, which themselves evolve over "slow time" driven by state-dependent and state-independent plasticity mechanisms. Finally, the adjustment of plasticity processes (metaplasticity) takes place in an "ultraslow" time scale. Psychedelics flatten the neural landscape, leading to heightened entropy and complexity of neural dynamics, as observed in neuroimaging and modeling studies linking increases in complexity with a disruption of functional integration. We highlight the relationship between criticality, the complexity of fast neural dynamics, and synaptic plasticity. Pathological, rigid, or "canalized" neural dynamics result in an ultrastable confined repertoire, allowing slower plastic changes to consolidate them further. However, under the influence of psychedelics, the destabilizing emergence of complex dynamics leads to a more fluid and adaptable neural state in a process that is amplified by the plasticity-enhancing effects of psychedelics. This shift manifests as an acute systemic increase of disorder and a possibly longer-lasting increase in complexity affecting both short-term dynamics and long-term plastic processes. Our framework offers a holistic perspective of the acute effects of these substances and their potential long-term impacts on neural structure and function.

*Corresponding author: giulio.ruffini@neuroelectrics.com

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36 1 Introduction

Spacetime tells matter how to move;
matter tells spacetime how to curve.

*John Archibald Wheeler, in
Gravitation (1973)*

37 In this paper, we explore new perspectives to interpret changes in the brain's landscape
38 and connectivity, focusing on the subtle interplay between structural and dynamical
39 aspects across timescales (fast, slow, and ultraslow). Our primary goal is to present a
40 framework that enhances the understanding of the intricate relationships among brain
41 dynamics, complexity, structure, and plasticity. This framework, which we call "neural
42 geometrodynamics", draws on principles from non-linear dynamics and is further inspired
43 by conceptual links to general relativity in physics.

44 In describing neural dynamics, we will refer to the mathematical formalism of neural
45 mass models (NMMs), although other computational neuroscience formulations are
46 equally relevant [1, 2]. Neural mass models have been extensively utilized to model various
47 brain activities, from localized brain functions to the coordinated activity observed in
48 different brain regions. By employing mathematical formulations that include essential
49 features like synaptic connectivity and neuronal excitability, NMMs enable the simulation
50 and analysis of complex brain activities in various dynamic regimes [3]. NMMs
51 are particularly useful because they provide a link between the mesoscopic physiological
52 scale and macroscopic brain function, allowing for the connection of effects on neurons at
53 the molecular level, such as those of psychedelics, with those of whole-brain connectivity
54 [4, 5].

55 Analyzing the effects of psychoactive neuroplastogens (psychedelics such as psilocybin
56 or LSD) serves as an illustrative case of the framework, given the immediate and potentially
57 lasting plastic changes these substances can provoke in the brain [6]. By altering
58 neural dynamics and connectivity, psychedelics are thought to induce both transient
59 and sustained shifts in cognition and perception [7]. Several studies underscore the role
60 of psychedelics in inducing neuroplasticity with antidepressant effects, revealing mechanisms
61 at molecular, synaptic, and dendritic levels [8, 9], and with significant potential
62 for treating neuropsychiatric disorders [10, 11], although the duration and permanence
63 of these effects remain to be fully understood.

64 Recent conceptual perspectives have enhanced our understanding of the brain's response
65 to psychedelics, combining biological, dynamical systems, complexity science, and arti-

66 ficial intelligence viewpoints. The REBUS (RElaxed Beliefs Under pSychedelics) frame-
67 work [12], grounded in the Free Energy Principle (FEP) and the entropic and anarchic
68 brain models, offers a perspective on the effects of psychedelics on the brain whereby
69 psychedelic action results in the collapse of brain functional hierarchies or, in other words,
70 in the “flattening of the landscape” of brain’s dynamics to allow the brain state to es-
71 cape a deep local minimum. The term *annealing* is also used in this context in relation
72 to physical annealing in metallurgy and simulated annealing in numerical optimization
73 [13].

74 Consequently, it has been argued that the observed expansion of the repertoire of func-
75 tional patterns elicited by hallucinogenic substances can be associated with an increase in
76 entropy in brain dynamics [14, 15], with the brain moving to a more disordered state from
77 a relaxation of high-level cognitive priors [12, 16]. This may lead to a favorable context
78 for conducting psychotherapy [12, 17, 18]. Studies on functional neuroimaging regarding
79 psilocybin and LSD effects have shown initial evidence of the mechanistic alterations
80 on brain dynamics at the network level, with the majority of the findings suggesting a
81 relative weakening of usual functional configurations giving place to an increase of brain
82 entropy, global functional integration, and more flexible brain dynamics [14, 19–28]. As
83 mentioned above, these changes are traditionally reflected in the complexity of neural
84 dynamics, which can be evaluated using various techniques such as criticality measures
85 [29, 30], complexity measures [31], connectome harmonic decomposition [23–25], control
86 theory [26] and Ising (or spinglass) modeling [32, 33].

87 For example, Ising modeling of psychedelics has shown that the increased complexity of
88 brain dynamics under LSD (e.g., increased Ising temperature, Lempel-Ziv, and the Block
89 Decomposition Method complexity) is associated with a decrease of interhemispheric
90 connectivity — especially homotopic links [34], corroborating earlier modeling studies
91 suggesting the central role of long-range connections in controlling phase transitions
92 [35].

93 The observed push of brain dynamics towards disorder and away from criticality aligns
94 with the REBUS and FEP frameworks, which link the vividness of experience to the en-
95 tropy of brain activity. At the same time, the notion that a wakeful brain exhibits
96 dimensionality reduction and criticality features that are disrupted by the effect of
97 psychedelics is also predicted by an algorithmic perspective on consciousness [16, 36,
98 37], where the psychedelic shift towards disorder is associated with a disruption of the
99 world-modeling/world-tracking circuits in the brain.

100 Another feature of brain dynamics related to the collapse of higher-order cognitive
101 functions under psychedelics in the REBUS framework is the hierarchical organization
102 along the uni- to trans-modal functional gradient [38]. This asymmetry in neural ac-
103 tivity reflects the bottom-up and top-down information flows in cognitive processing
104 [39, 40]. This has been suggested to be intimately linked to non-equilibrium dynam-
105 ics in thermodynamic-inspired frameworks where the level of hierarchy is related to the
106 amount of brain signal irreversibility as well as entropy production [41–43]. Indeed it has
107 been demonstrated that the principal functional gradient collapses under the influence
108 of various psychedelics [44–46].

109 A related perspective for this paper is the CANAL framework [11] for describing the
110 pathological plasticity of “being stuck in a rut” in certain mood disorders and the po-
111 tential therapeutic role of psychedelics through the concept of metaplasticity. In contrast
112 to psychedelics, these changes are reflected in neural dynamics with brain signatures of
113 excessively rigid and highly ordered functional states [47]. The CANAL framework has
114 been further extended by establishing connections with deep artificial neural networks
115 (Deep CANAL [48]) to introduce a distinction between two distinct pathological phe-
116 nomena — one related to fast brain dynamics and their slow and ultraslow counterparts.
117 These distinctions will be naturally integrated into the presented framework (see the Ap-
118 pendix for a figure relating the concepts in the different frameworks).

119 While the discussion is centered on the effects of psychedelics, the framework proposed
120 here extends more generally to other phenomena related to plasticity, including neu-
121 rodevelopment, pathological plasticity in mood disorders [49], and interventions that
122 alter brain dynamics like transcranial brain stimulation (tES) [50], transcranial mag-
123 netic stimulation (TMS), or electroconvulsive therapy (ECT).

124 In what follows, we formalize the notions of brain dynamics, plasticity, and their asso-
125 ciated timescales and subsequently use them to study the impact of psychedelics on the
126 brain. In the last section, we draw connections between the framework and concepts
127 from general relativity in physics. We hope these parallels will illuminate the complex
128 relationship between the structure and function of brain dynamics. Figure 1 illustrates
129 the reciprocal dynamics between brain states and connectivity as conceptualized in the
130 neural geometrodynamics framework.

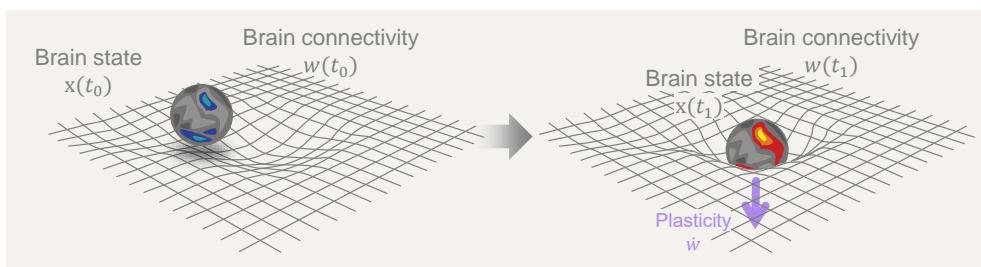


Figure 1: Neural Geometrodynamics: a dynamic interplay between brain states and connectivity. A central element in the discussion is the dynamic interplay between brain state (x) and connectivity (w), where the dynamics of brain states is driven by neural connectivity while, simultaneously, state dynamics influence and reshape connectivity through neural plasticity mechanisms. The central arrow represents the passage of time and the effects of external forcing (from, e.g., drugs, brain stimulation, or sensory inputs), with plastic effects that alter connectivity (\dot{w} , with the overdot standing for the time derivative).

131 2 Dynamics across timescales

132 The state of a system can be defined by a set of coordinates in phase space: a multidimensional manifold in which each dimension corresponds to one of the variables. For a 133 single particle moving in one dimension, the phase space is two-dimensional, with one 134 axis representing its position and the other representing its momentum. For example, 135 Figure 2 illustrates the phase space of a pendulum with friction. In phase space, and per- 136 haps after some transient period, the possible trajectories of the states of the system lie 137 in a reduced or invariant manifold (an attractor, see Box 1 for a glossary of terms), which 138 we may refer to as the “geometry” or latent “structure” of the phase space. Together, 139 the structure (geometry and topology) of the phase space with its invariant properties 140 can be referred to as the dynamical landscape, where the depth or shallowness of the 141 “valleys” can, in some cases, be interpreted as the stability of the state in that location 142 given some stochastic forcing. For example, in mechanics, the landscape can be labeled 143 by potential energy isolines, e.g., in a physical system such as in the pendulum example 144 in Figure 2 (bottom right), or their generalization, Lyapunov functions [55]. 145

146 Fast time: neural dynamics

147 Here, we discuss the first equation in neural geometrodynamics in the context of neural 148 mass models, but the ideas are applicable more extensively in computational neuro- 149 science. The standard equation we use in neural mass modeling is a multidimensional

Box 1 - GLOSSARY

State of the system: Depending on the context, the state of the system is defined by the coordinates x (Eq. 1, fast time view) or by the full set of dynamical variables (x, w, θ) — see Eqs. 1, 2 and 3.

Entropy: Statistical mechanics: the number of microscopic states corresponding to a given macroscopic state (after coarse-graining), i.e., the information required to specify a specific microstate in the macrostate. Information theory: a property of a probability distribution function quantifying the uncertainty or unpredictability of a system.

Complexity: A multifaceted term associated with systems that exhibit rich, varied behavior and entropy. In algorithmic complexity, this is defined as the length of the shortest program capable of generating a dataset (Kolmogorov complexity). Characteristics of complex systems include nonlinearity, emergence, self-organization, and adaptability.

Critical point: Dynamics: parameter space point where a qualitative change in behavior occurs (*bifurcation point*, e.g., stability of equilibria, emergence of oscillations, or shift from order to chaos). Statistical mechanics: phase transition where the system exhibits changes in macroscopic properties at certain critical parameters (e.g., temperature), exhibiting scale-invariant behavior and critical phenomena like diverging correlation lengths and susceptibilities. These notions may interconnect, with bifurcation points in large systems leading to phase transitions.

Temperature: In the context of Ising or spinglass models, it represents a parameter controlling the degree of randomness or disorder in the system. It is analogous to thermodynamic temperature and influences the probability of spin configurations. Higher temperatures typically correspond to increased disorder and higher entropy states, facilitating transitions between different spin states.

Effective connectivity (or connectivity for short): In our high-level formulation, this is symbolized by w . It represents the connectivity relevant to state dynamics. It is affected by multiple elements, including the structural connectome, the number of synapses per fiber in the connectome, and the synaptic state (which may be affected by neuromodulatory signals or drugs).

Plasticity: The ability of the system to change its effective connectivity (w), which may vary over time.

Metaplasticity: The ability of the system to change its plasticity over time (dynamics of plasticity).

State or Activity-dependent plasticity: Mechanism for changing the connectivity (w) as a function of the state (fast) dynamics and other parameters (α). See Eq. 2.

State or Activity-independent plasticity: Mechanism for changing the connectivity (w) independently of state dynamics, as a function of some parameters (γ). See Eq. 2.

Connectodynamics: Equations governing the dynamics of w in slow or ultraslow time.

Fast time: Timescale associated to state dynamics pertaining to x .

Slow time: Timescale associated to connectivity dynamics pertaining to w .

Ultraslow time: Timescale associated to plasticity dynamics pertaining to $\theta = (\alpha, \gamma)$ — v. Eq. 3.

Phase space: Mathematical space, also called **state space**, where each point represents a possible state of a system, characterized by its coordinates or variables.

Geometry and topology of reduced phase space: State trajectories lie in a submanifold of phase space (the reduced or invariant manifold). We call the geometry of this submanifold and its topology the “structure of phase space” or “geometry of dynamical landscape”.

Topology: The study of properties of spaces that remain unchanged under continuous deformation, like stretching or bending, without tearing or gluing. It’s about the ‘shape’ of space in a very broad sense. In contrast, geometry deals with the precise properties of shapes and spaces, like distances, angles, and sizes. While geometry measures and compares exact dimensions, topology is concerned with the fundamental aspects of connectivity and continuity.

Invariant manifold: A submanifold within (embedded into) the phase space that remains preserved or invariant under the dynamics of a system. That is, points within it can move but are constrained to the manifold. Includes stable, unstable, and other invariant manifolds.

Stable manifold or attractor: A type of invariant manifold defined as a subset of the phase space to which trajectories of a dynamical system converge or tend to approach over time.

Unstable Manifold or Repellor: A type of invariant manifold defined as a subset of the phase space from which trajectories diverge over time.

Latent space: A compressed, reduced-dimensional data representation (see Box 2).

Topological tipping point: A sharp transition in the topology of attractors due to changes in system inputs or parameters.

150 ODE of the form

$$\dot{x} = f(x; w, \eta(t)) \quad (1)$$

151 with $x \in \mathbb{R}^n$ and where w denotes connectivity parameters¹ and where, as usual, a
152 dot over a variable denotes its time derivative. This equation governs dynamics at

¹In the REBUS model [56], from the Free Energy perspective, w would correspond to the weights or precision assigned to priors/beliefs; from the Entropic Brain perspective, w would correspond to the weights of the effective connectivity between neuronal populations on the macroscopic scale.

Box 2 - The manifold hypothesis and latent spaces

The dimension of the phase (or state) space is determined by the number of independent variables required to specify the complete state of the system and the future evolution of the system. The **Manifold hypothesis** posits that high-dimensional data, such as neuroimaging data, can be compressed into a reduced number of parameters due to the presence of a low-dimensional invariant manifold within the high-dimensional phase space [51, 52]. **Invariant manifolds** can take various forms, such as **stable manifolds or attractors** and unstable manifolds. In attractors, small perturbations or deviations from the manifold are typically damped out, and trajectories converge towards it. They can be thought of as lower-dimensional submanifolds within the phase space that capture the system's long-term behavior or steady state. Such attractors are sometimes loosely referred to as the “**latent space**” of the dynamical system, although the term is also used in other related ways. In the related context of deep learning with variational autoencoders, latent space is the compressive projection or embedding of the original high-dimensional data or some data derivatives (e.g., functional connectivity [53, 54]) into a lower-dimensional space. This mapping, which exploits the underlying invariant manifold structure, can help reveal patterns, similarities, or relationships that may be obscured or difficult to discern in the original high-dimensional space. If the latent space is designed to capture the full dynamics of the data (i.e., is constructed directly from time series) across different states and topological tipping points, it can be interpreted as a representation of the invariant manifolds underlying system.

153 short time scales (seconds or less) when connectivity parameters w are assumed to be
154 constant.
155 The external input term $\eta(t)$ makes the equations non-autonomous (an autonomous
156 ODE does not explicitly depend on time). This term can refer to external forces pro-
157 viding random kicks to the trajectory or to a more steady and purposeful forcing from
158 unspecified internal systems, external inputs from sensory systems, or external electric
159 fields, for example.
160 We may think of this equation describing phenomena in **fast time** scales as providing
161 the “structure” for the dynamics of neuronal population state. The fast timescale is
162 set by synaptic transmission (milliseconds) and by ephaptic coupling (electromagnetic
163 waves) [57–60] in a nanosecond or subnanosecond scale [59].
164 Equation 1 characterizes the **dynamical landscape**, which is established through the
165 geometric structure of the phase space, where trajectories are shaped by the given set
166 of ordinary differential equations. The landscape is determined by the functional form
167 of $f(x; w, \eta(t))$ and by the parameters w , and is analogous to the Neural Activation
168 Landscape proposed in [48]. More specifically, we talk about the landscape as defined by
169 the manifold generated by the motion of trajectories with coordinates $x \in \mathbb{R}^n$. Typically,
170 trajectories lie in a reduced manifold of dimensionality lower than \mathbb{R}^n . The fact that
171 such a reduced space exists means that it can be generated by coordinates in a reduced
172 latent space. The geometry and topology of this reduced space in different states provide

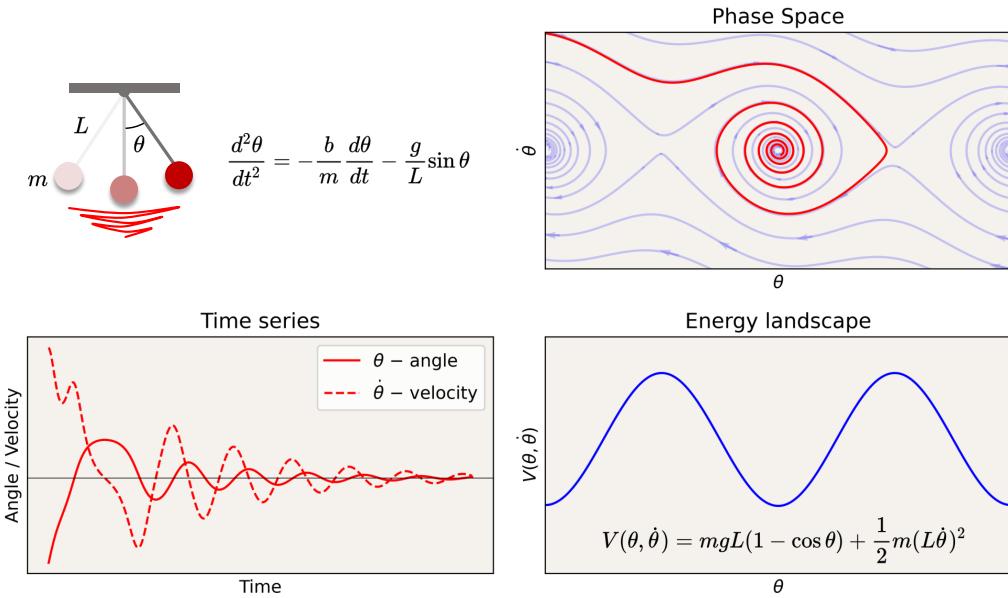


Figure 2: Dynamics of a pendulum with friction. Time series, phase space, and energy landscape. Attractors in phase space are sets to which the system evolves after a long enough time. In the case of the pendulum with friction, it is a point in the valley in the “energy” landscape (more generally, defined by the level sets of a Lyapunov function).

173 a synthetic description of the dynamics and are of special interest [37].

174 **Slow time: connectodynamics**

175 The landscape, like that on planet Earth, may appear to be static, but in reality, it is
 176 not fixed. It also flows in *slow time*. We thus consider changes in connectivity in the
 177 system, that is, now $w = w(t)$. We call the potential for such changes *plasticity of the*
 178 *system*. The general form of this equation is $\dot{w} = g(x, w; \theta)$, with θ standing for a set of
 179 parameters controlling plasticity.

180 To be more concrete, we can think of two types of process: one that modifies the
 181 connectivity parameters independently of the system’s state (ψ) and another that is a
 182 function of the state (e.g., Hebbian plasticity [61], h). We express this by writing

$$\dot{w} = \psi(w; \gamma) + h(x, w; \alpha) \quad (2)$$

183 (with the second term understood as not separable into parts where any part is a function
 184 of only w). This decomposition separates out *state-dependent* (via the term $h(x, w; \alpha)$)

185 and *state-independent plasticity* (with $\psi(w; \gamma)$) processes. The set of parameters θ is
186 similarly decomposed as $\theta = (\alpha, \gamma)$: we separate out the plasticity-controlling parameters
187 in order to differentiate the *state-dependent* (α) and *state-independent* (γ) plasticity
188 control parameters (e.g., Hebbian vs. drug-enhanced structural plasticity [11]). The
189 parameters (α, γ) may vary in time to reflect, for example, the effects of drugs. The
190 dynamics of these parameters are formalized in the next section.

191 Hebbian plasticity is the most prominent example of state-dependent plasticity [61].
192 State dependence implies that state-related concepts such as system temperature, phase
193 transitions, and critical phenomena are relevant for the study of the dynamics of plas-
194 ticity. In particular, within the scope of slower “slow time” (taking place over many
195 hours), we include *homeostatic plasticity* [62–65], which may itself target desired com-
196 plexity states as a homeostatic goal [66, 67]. In the case of state-independent plasticity,
197 there are numerous candidates for these plastic processes, such as heterosynaptic plas-
198 ticity [68] or critical-period plasticity [69].

199 In summary, the functions h and ψ with parameters α and γ regulate *connectodynamics*,
200 defining where and how fast the effective connectivity will change in a state-dependent
201 or state-independent way.

202 These connectodynamics differential equations define a new dynamical landscape, which
203 we can call the *plasticity landscape* (analogous to the Synaptic Weight Landscape in [48]).
204 The state w in this plasticity landscape will determine the shape of the neural dynamics
205 landscape.

206 **Ultraslow time: metaplasticity**

207 Plasticity is required to adapt to a changing environment [70], and the environment may
208 change at different rates at different times. Plasticity in the healthy brain should match
209 this variation in the character of dynamics accordingly. This is analogous to the situation
210 in biology, where optimal mutation rates ensure successful adaptation in a tradeoff with
211 genetic integrity [71]. More specifically, the plasticity-regulating parameters α and γ in
212 Equation 2 should adapt to changes in the environmental conditions.

213 In pathological cases, plasticity levels can either become overly exuberant, reflecting the
214 notion of catastrophic forgetting in artificial neural networks, or impoverished and rigid,
215 reflecting general plasticity loss [48]. These scenarios can be tentatively related to certain
216 neurological and psychiatric conditions. For example, reduced plasticity could underlie
217 conditions such as major depressive disorder, obsessive-compulsive disorder, anxiety, or

218 substance abuse [48, 72].

To account for the dynamics of plasticity, we allow the plasticity parameters to be dynamic, i.e.,

$$\dot{\theta} = \xi(x, w, \theta; \mu(t)) \quad (3)$$

219 This equation is again state-dependent, allowing the system to respond to changes in the
220 neural dynamics (with state dynamics as drivers of plasticity parameter regulation [73]),
221 including critical phenomena (changes in criticality regime [66]) and complexity. Plas-
222 ticity dynamics reflect changes in the parameters regulating state-dependent (Hebbian)
223 plasticity (changes in α) during neurodevelopment, and state-independent plasticity,
224 such as the ones induced by psychedelics in the acute or post-acute phases (changes in
225 γ). Finally, this equation is a function of other parameters and non-autonomous terms
226 ($\mu(t)$), reflecting external perturbations of the system, such as those from drugs. We
227 provide analogies in the context of sailing and electrodynamics in the appendix to further
228 clarify these concepts.

229 The dynamics of plasticity presented above reflect a physiological principle well described
230 by Abraham et al. in the definition of metaplasticity [74]:

231 **Metaplasticity** [...] is manifested as a change in the ability to induce
232 subsequent synaptic plasticity, such as long-term potentiation or depres-
233 sion. Thus, metaplasticity is a higher-order form of synaptic plasticity [74].

234 Thus, metaplasticity and its counterparts are terms used in neuroscience to refer to
235 the plasticity of synaptic plasticity. That is, the idea that the ability of synapses to
236 strengthen or weaken in response to increases or decreases in their activity (which is
237 called synaptic plasticity) can be modulated based on the history of the synaptic ac-
238 tivity or other factors (e.g., age, neuromodulatory systems, drugs, or lifestyle [75]).
239 Metaplasticity has important implications for the learning and memory of an organism,
240 as it can regulate the ability of synaptic plasticity to change and adapt over time as
241 required by its environmental context.

242 We call the set of equations 1,2 and 3 — somewhat whimsically — the equations for
243 *neural geometrodynamics* in reference to the equations of general relativity in physics.
244 We recall that general relativity provides equations defining the dynamics of spacetime
245 geometry (via the “metric”) coupled with matter [76]. Section 4 elaborates further on
246 this parallel.

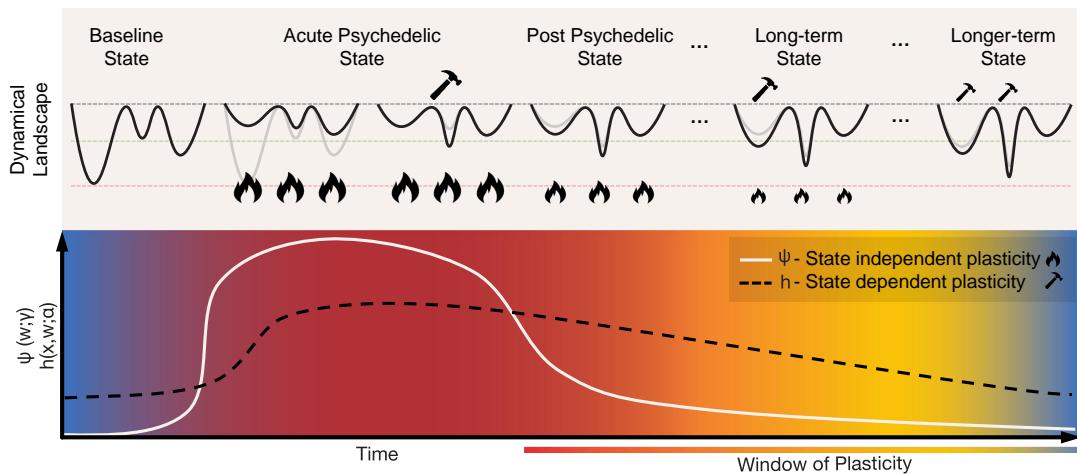


Figure 3: Geometrodynamics of the acute and post-acute plastic effects of psychedelics. The **acute** plastic effects can be represented by rapid state-independent changes in connectivity parameters, i.e., the term $\psi(w; \gamma)$ in Eq. 3. This will result in the flattening or de-weighting of the dynamical landscape. Such flattening allows for the exploration of a wider range of states, eventually creating new minima through state-dependent plasticity, represented by the term $h(x, w; \alpha)$ in Eq. 3. As the psychedelic action fades out, the landscape gradually transitions towards its initial state but with lasting changes due to the creation of new attractors during the acute state. The **post-acute** plastic effects can be described as a “window of enhanced plasticity”. These transitions are brought about by changes of the parameters γ and α , each controlling the behavior of state-independent and state-dependent plasticity, respectively. In this post-acute phase, the landscape is more malleable to internal and external influences.

247 3 Dynamics under psychedelics

248 Psychedelics like psilocybin and LSD act as agonists or partial agonists for serotonin 5-
 249 hydroxytryptamine 2A (5-HT_{2A}) receptors, specifically targeting Layer V cortical pyra-
 250 midal neurons [11, 14, 56, 77, 78], leading to increased neuronal excitability through an
 251 increase in excitatory postsynaptic currents and discharge rates in pyramidal neurons
 252 [12]. The highest expression of 5-HT_{2A}Rs is found on the apical dendrites of Layer
 253 5 pyramidal cells in both cortical and subcortical structures [12, 79]. In the cortex,
 254 5-HT_{2A} receptors are strongly expressed along a steep anteroposterior gradient [80].
 255 When psychedelics bind to these receptors, they can lead to a gradual increase of the
 256 excitability of these pyramidal neurons — depolarizing them and making them more
 257 susceptible to excitatory inputs such as those associated with glutamate receptors [80]
 258 — much as the gain knob in an amplifier. This increased excitability and susceptibility
 259 to inputs can lead to changes in the firing patterns of these neurons and alterations in

260 the overall neural circuit activity. Recognized for their potent and immediate impact on
261 the brain, these drugs cause a swift reconfiguration of neural dynamics. As we explain,
262 this immediate effect is represented in our model by state-independent alterations in the
263 connectivity parameters (w) (see Figure 3).

264 How are these effects represented in Equations 1 and 2? If we include the neuromodulatory
265 nodes in our model — the dorsal raphe and median raphe nuclei in the brainstem
266 are the source of most serotonergic neurons projecting throughout the brain [80] —, the
267 modulation of serotonin receptors could be represented by changes in neuromodulatory
268 connectivity (the subset of w parameters in the model connecting the raphe nuclei to
269 other nodes). Alternatively, if neuromodulatory nodes are not explicitly included in the
270 model, for the purposes at hand, we can think of the changes in the excitability of the
271 nodes affected by neuromodulatory inputs as leading to changes in their effective connec-
272 tivity (w) to other nodes (e.g., through an increase of the connectivity of glutamatergic
273 synapses into Layer 5 pyramidal cells).

274 The abrupt shift induced by psychedelics can be thought of as a transformation of the
275 phase space’s geometry, allowing the neural state to explore new trajectories. This
276 process manifests in an increase of complexity and disorder, which can be measured
277 using various tools in different modalities (e.g., EEG or fMRI BOLD with measures
278 such as entropy, fractal dimension, algorithmic complexity, etc. [29, 31, 34, 81]). The
279 decrease in effective connectivity under LSD (especially in interhemispheric homotopic
280 connections), as inferred using Ising modeling of BOLD signals measured using fMRI
281 imaging, is associated with a subsequent increase in algorithmic complexity [34].

282 Psychedelic-induced changes in connectivity correspond to a flattening of the dynamical
283 landscape [12] or a destabilization of it [48]. In our framework, the alteration of effective
284 connective results in an immediate and state-independent remodeling of the dynamical
285 landscape during the acute phase of psychedelics, which is represented by the term
286 $\psi(w; \gamma)$ in the connectodynamics equation (Eq. 2)².

287 The instantaneous modification of the landscape is, however, ephemeral, gradually fad-
288 ing as the acute effects of the psychedelics wear off. The system returns to near its
289 original geometrical configuration but with lasting influences brought about by the plas-
290 tic changes resulting from the exploration of new trajectories in the acute phase. These
291 residual changes are captured by the state-dependent plasticity term, $h(x, w; \alpha)$, which

²In the REBUS model and the Entropic Brain perspective [56], the weights of the effective connectivity during the psychedelic-induced state are “flattened” or “de-weighted”, representing a more symmetrical and non-hierarchical connectivity profile.

292 reflects changes in connectivity due to Hebbian plasticity that arise from the co-activation
293 of neurons during the psychedelic acute stage.

294 In the literature, there is an increasing body of evidence suggesting a post-acute phase
295 following psychedelic exposure characterized by a period of enhanced plasticity [11, 12,
296 82–84]. This phase can be interpreted as an extended window of malleability of the land-
297 scape, which could have profound implications for learning and therapy. Such window of
298 plasticity has been related to increased neurogenesis and upregulation of Brain-Derived
299 Neurotropic Factor (BDNF) in humans and mice [8]. The activity-dependent release of
300 BDNF plays a crucial role in selectively strengthening active synapses while weakening
301 inactive ones, a critical process for Hebbian-type plasticity. Intriguingly, recent studies
302 with mice have found psychedelic-induced changes in plasticity and antidepressant-like
303 behavior dependent on the increase of endogenous BDNF and TrkB binding (the receptor
304 of BDNF), but independent from the activation of 5-HT_{2A} [9, 10].

305 In terms of our model, these two pathways correspond to changes of connectivity through
306 Equation 2 due to a temporary modulation of the parameters γ and α (i.e., metaplastic-
307 ity, see Equation 3) upregulating state-independent and state-dependent plasticity pro-
308 cesses, respectively. The strong acute-phase increase of state-independent plasticity (ψ)
309 would be directly associated with the activation of serotonergic receptors, as discussed
310 above, with a possible gradual decrease during the post-acute phase (solid white line
311 in Figure 3). The sustained increase of state-dependent plasticity (h) in the post-acute
312 phase (dashed black line in Figure 3) would be linked to dendritic growth, neurogenesis,
313 upregulation of BDNF, and other related changes. This means that in the post-acute
314 period, the landscape would be more responsive to state changes (itself influenced by
315 external factors), offering a potential mechanism for the long-lasting changes reported
316 after psychedelic experiences. Such external influences are modeled by the external input
317 term $\eta(t)$ in the state equation (Eq. 1) and can represent environmental/sensory inputs,
318 psychotherapy, or neuromodulatory brain stimulation techniques such as transcranial
319 electrical current stimulation (tES).

320 Dynamics of psychedelics and psychopathology

321 Recently, psychedelic medicine has emerged as a promising direction for treating mental
322 disorders such as depression or addiction [85]. The nuanced interaction between the
323 brain's neurophysiology and the emergent brain activity underlies the pathophysiology
324 of mood disorders, often resulting in a persistent and maladaptive rigidity in cognitive
325 and emotional processes [86]. Such changes to the brain's neurophysiology can be ex-

326 plained through the CANAL framework whereby pathological plasticity, often caused
327 by a traumatic event, asserts itself and dominates brain activity, driving the brain state
328 to be “stuck in a rut” [11], i.e., a deepening minimum in the dynamical landscape (see
329 Figure 4).

330 The interplay between external inputs, neural (fast time), and connectivity (slow time)
331 dynamics can drive the system into a joint canalized, stable state of lower complexity.
332 Under the influence of psychedelics, more diverse and complex dynamics destabilize the
333 plasticity equilibrium point, leading to a more fluid and adaptable neural state in a
334 process that is amplified by the plasticity-enhancing effects of psychedelics. This shift
335 manifests as an acute systemic increase of disorder and possibly a longer-lasting increase
336 in complexity (Ising temperature, Lempel-Ziv complexity, etc.) that affects both short-
337 term dynamics and long-term plastic processes.

338 The CANAL framework offers insight into the neural mechanisms underlying the persis-
339 tence of various brain disorders. In particular, psychedelics may mediate their effects by
340 altering the balance between stability and plasticity in neural networks through meta-
341 plasticity and thus act as potential therapeutic treatments. By acting on the serotonergic
342 receptors, they trigger a cascade of neurochemical events, subsequently facilitating the
343 reorganization of entrenched neural patterns. As discussed above, this alteration of
344 the neural network during the acute phase (connectodynamics) can be interpreted as
345 a rapid deformation or flattening of the landscape that allows the trapped state to es-
346 cape and access more adaptive cognitive and emotional patterns. The rapid increase
347 in complexity (a change in the dynamics) is in itself a likely driver of metaplasticity.
348 The acute phase is believed to be followed by an extended window of malleability of
349 the landscape, otherwise known as a “window of plasticity”, where treatments such as
350 psychotherapy and transcranial electrical stimulation can further alter the pathological
351 rigidity characteristic of various brain disorders (see Figure 4).

352 4 Neural geometrodynamics and general relativity

353 A parallel can be drawn between neural geometrodynamics and Einstein’s equations
354 of general relativity — the original geometrodynamics. Both frameworks involve the
355 dynamical interaction between structure and resulting activity, each influencing and
356 being influenced by the other. The Einstein field equations, including the cosmological
357 constant Λ , are

$$R_{\mu\nu} - \frac{1}{2}g_{\mu\nu}R + \Lambda g_{\mu\nu} = \frac{8\pi G}{c^4}T_{\mu\nu}. \quad (4)$$

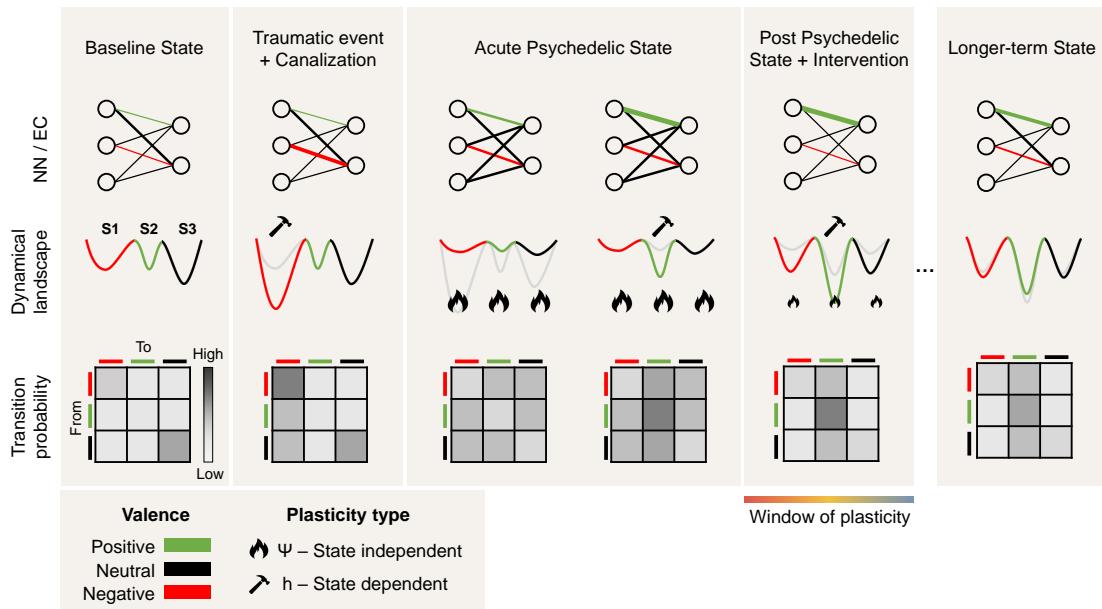


Figure 4: Psychedelics and psychopathology: a dynamical systems perspective. From left to right, we provide three views of the transition from health to canalization following a traumatic event and back to a healthy state following the acute effects and post-acute effects of psychedelics and psychotherapy. The top row provides the *neural network (NN) and effective connectivity (EC) view*. Circles represent nodes in the network and edge connectivity between them, with edge thickness representing the connectivity strength between nodes. The middle row provides the *landscape view*, with three schematic minima and colors depicting the valence of each corresponding state (positive, neutral, or negative). The bottom row represents the *transition probabilities across states* and how they change across the different phases. Due to traumatic events, excessive canalization may result in a pathological landscape reflected as a deepening of a negative valence minimum where the state may be trapped. During the acute psychedelic state, the landscape is deformed, enabling the state to escape. Moreover, plasticity is enhanced during the acute and post-acute phases, benefiting interventions such as psychotherapy or brain stimulation (i.e., changes in effective connectivity). Not shown is the possibility that a deeper transformation of the landscape may take place during the acute phase (see the discussion on the wormhole analogy in Section 4).

358 Here, $g_{\mu\nu}$ is the metric tensor, $R_{\mu\nu} = R_{\mu\nu}[g_{\mu\nu}]$ is the Ricci curvature tensor and a
 359 function of $g_{\mu\nu}$, $R[g_{\mu\nu}]$ is the Ricci scalar (or curvature scalar) and a function of $g_{\mu\nu}$,
 360 $T_{\mu\nu}$ is the stress-energy tensor³, a function of the mass and energy distribution (all the

³The stress-energy tensor (also called the energy-momentum tensor) is a central concept in general relativity. It encapsulates the distribution and flow of energy and momentum in spacetime, and its

361 indices refer to spacetime dimensions), G is the gravitational constant, c is the speed
362 of light, and Λ is the cosmological constant. These equations describe the fundamental
363 interaction of gravitation as a result of spacetime being curved by matter and energy.
364 Specifically, they equate local spacetime curvature (on the left-hand side) with the local
365 energy and momentum within that spacetime (on the right-hand side).

366 To complete these equations, the *geodesic equation* portrays how particles (matter) move
367 in this curved spacetime, encapsulated by the notion that particles follow the straightest
368 possible paths (geodesics) in curved spacetime,

$$\frac{d^2x^\mu}{d\tau^2} + \Gamma_{\rho\sigma}^\mu \frac{dx^\rho}{d\tau} \frac{dx^\sigma}{d\tau} = 0 \quad (5)$$

369 where x^μ are the coordinates of the particle, τ is the proper time along the particle's
370 path, and $\Gamma_{\rho\sigma}^\mu[g_{\mu\nu}]$ are the Christoffel symbols, which are a function of $g_{\mu\nu}$ and encode
371 the *connection* (a mathematical object that describes how vectors change as they are
372 parallel transported along curves in spacetime). The stress-energy tensor $T_{\mu\nu}$ can be
373 computed from the state of the particles, closing the system of equations. For example,
374 for N particles, it is given by $T^{\mu\nu} = \sum_i m_i u_i^\mu u_i^\nu \delta(\mathbf{x} - \mathbf{x}_i)$, where m_i and u_i are the mass
375 and velocity of the i th particle. More generally, the stress-energy tensor represents the
376 state of matter and energy, which corresponds to x in our neural model. The metric
377 $g_{\mu\nu}$, which specifies the geometry of spacetime, is akin to the connectivity w — which
378 shapes the structure of the space where fast dynamics occur.

379 In the context of neural mass models, the state equation, $\dot{x} = f(x; w)$, is analogous
380 to the geodesic equation — “the state of the system evolves according to the landscape
381 geometry specified by the parameters w ”. On the other hand, the connectodynamics
382 equation, $\dot{w} = h(x, w; \theta)$ (with θ standing for plasticity parameters), is analogous to
383 Einstein's field equations — the parameters w , which describe the “structure” of the
384 space where dynamics take place, evolve according to the current state of the system x
385 and its ‘readiness’ for plasticity (parametrized by θ).

386 The analogy to psychedelic effects in general relativity can be clarified further. The
387 neural effects of psychedelics, as we understand them, start with a disruption of con-
388 nectivity in a spatially dependent manner. Since the analog of w is g (the metric), in
389 cosmological terms, we would first see a dynamic deformation of spacetime independent
390 of the mass distribution (state-independent plasticity). Spacetime would “flatten”. This
391 would cause the mass in the universe to escape from gravitational wells following new

392 components include energy density, momentum density, and stress (pressure and shear stress) within a
393 given region.

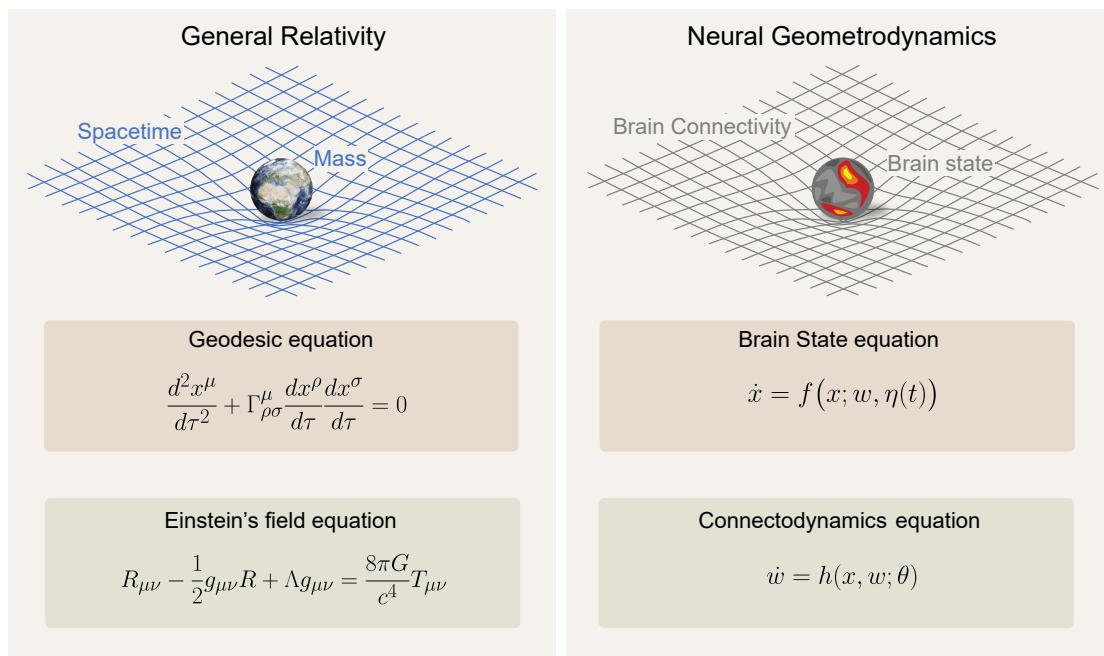


Figure 5: General Relativity and Neural Geometrodynamics. Left: Equations for general relativity (the original geometrodynamics), coupling dynamics of matter with the dynamics of spacetime. Right: Equations for neural geometrodynamics, coupling neural state, and connectivity. Only fast and slow time equations are shown (ultraslow time endows with dynamics the “constants” appearing in these equations).

392 geodesics (just as the state in the brain will explore new regions of phase space), in turn
 393 creating further deformations of spacetime (state-dependent plasticity).

394 We emphasize that this comparison is largely metaphorical and therefore limited: the
 395 mutual influence between particles and spacetime in general relativity is akin to the state
 396 of the neural system and its underlying connectivity parameters. In both cases, dynamics
 397 and structure are intertwined (see Figure 5). However, as an example of the limitations
 398 of the analogy, the slow and fast nature of the different variables is interchanged in the
 399 two formulations, with spacetime responding faster (at the speed of light) to changes in
 400 the distribution of energy than the stress-energy tensor itself.

401 Metaplasticity and variable constants in cosmology

In our neural mass model framework, the concept of metaplasticity is introduced as dynamic variations in the plasticity control constants, namely θ in the connectodynamics equation. This set of constants can be represented as evolving over time as a function

of the state of the system or other relevant variables,

$$\dot{\theta} = \xi(x, w, \theta; \lambda) \quad (6)$$

402 In this equation, ξ defines the evolution of the plasticity control constants with param-
403 eters λ .

404 Analogously, in the realm of general relativity and cosmology, it has been speculated
405 that the fundamental constants, such as the speed of light c , the gravitational constant
406 G , or the cosmological constant Λ , may, in fact, be dynamic. Although not part of the
407 mainstream cosmological model, theories proposing variable constants, such as “Variable
408 Speed of Light” (VSL) or “Variable Cosmological Constant” provide an intriguing par-
409 allel. For instance, within VSL theories, the speed of light c is postulated to vary over
410 cosmological time scales. Certain hypothetical dynamical equations could dictate the
411 dynamical evolution of these constants. Although these theories are quite speculative
412 and do not form a part of mainstream physics, they offer an interesting perspective on
413 the concept of metaplasticity and its potential implications for the dynamical evolution
414 of neural mass models and the structure of their landscapes.

415 **Psychedelics as wormholes in the neural landscape**

416 In the parallel of general relativity and neural geometrodynamics, we see the effects of
417 psychedelics as a deformation of the neural landscape (spacetime) that allows the brain
418 state (of a particle or set of particles) to escape from a local minimum and transition
419 to another location in the landscape (spacetime). Although transitions may be smooth
420 and respect the topology of the landscape (as described by topological quantities such
421 as the Euler characteristic of Betti numbers⁴ [87, 88]), deformations of the landscape
422 may also be more extreme — sharp transitions through a *topological tipping point* of
423 the dynamical landscape. This may be due to external inputs ($\eta(t)$), when our system
424 is non-autonomous [89], e.g., from sensory or brain stimulation effect. And as we have
425 discussed, it may be due to connectivity dynamics.

426 The creation of a wormhole in general relativity⁵ can be viewed as a profound deforma-

⁴In algebraic topology, Betti numbers provide a way to count the number of n -dimensional “holes” in a manifold. The creation of a wormhole (in 4D or higher dimensional spaces), being a topological feature that connects two otherwise distant regions of spacetime, would alter the topological structure of the manifold it inhabits and the associated Betti numbers.

⁵Wormholes, a term due to John A. Wheeler [90], also known as Einstein-Rosen bridges, are solutions to the Einstein field equations of general relativity which some models suggest could exist under certain conditions. However, creating or stabilizing a traversable wormhole would likely require forms of exotic

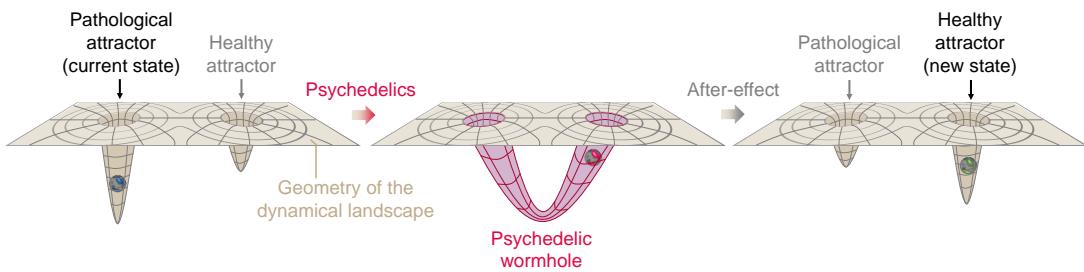


Figure 6: A hypothetical psychedelic wormhole. On the left, the landscape is characterized by a deep pathological attractor, where the neural state is trapped. After ingestion of psychedelics (middle), a radical transformation of the neural landscape takes place, with the formation of a wormhole connecting the pathological attractor to another, healthier attractor location and allowing the neural state to tunnel out. After the acute effects wear off (right panel), the landscape returns near its original topology and geometry, but activity-dependent plasticity reshapes it into a less pathological geometry.

427 tion of spacetime, bending and connecting distant parts of the universe in such a way
428 that matter/energy, like an astronaut, can travel through vast distances in an instant.
429 This change in the geometry and topology of spacetime can be likened to the effect of
430 psychedelics on the human mind. Just as the wormhole alters the structure of spacetime,
431 psychedelics may radically alter the dynamical landscape of neural dynamics, creating
432 connections across distant landscape locations. In the same way that the astronaut uses
433 the wormhole to bypass vast stretches of space, the deformation caused by psychedelics
434 may allow the state of the brain to tunnel out and escape from a local minimum or
435 stuck pattern of thought, providing access to new areas of the landscape — new per-
436 spectives and potentially unexplored territories of consciousness. This analogy, although
437 speculative, aims to highlight that both phenomena are characterized by a fundamen-
438 tal transformation that enables traversal into otherwise inaccessible regions — whether
439 in physical space or the brain's dynamical landscape (see Figure 6 for a sketch of this
440 concept).

matter with properties not yet observed in the known universe — there is no current consensus about this in classical general relativity, where some theorems suggest it may not be possible in some conditions because of the necessity of singularities, or in quantum gravity, where topology change is a natural concept [91].

441 **Characterizing the landscape**

442 An important challenge in the program of neural geometrodynamics is to explore practical
443 methods to characterize the landscape. Here again, we can draw inspiration from
444 physics and mathematics.

445 The roots of this approach can be traced back to the 19th century when Carl Friedrich
446 Gauss pioneered the field of differential geometry. Gauss's Theorema Egregium demon-
447 strated that the curvature of a surface could be determined entirely by measurements
448 within the surface, without any reference to the surrounding space [92]. This seminal in-
449 sight has laid the groundwork for understanding manifolds in various contexts, including
450 the theory of relativity. In the era of general relativity, the interplay between geometry
451 and physics was further enriched. Differential geometry and algebraic topology — which
452 comes into play when one is interested in the global properties of the manifold, such as its
453 shape, connectedness, and the presence of holes [93, 94] — became essential in describ-
454 ing the fabric of spacetime itself. It enabled physicists to conceptualize how mass and
455 energy warp the geometry of spacetime, thus influencing the motion of objects.

456 In our current endeavor, these ideas find application in characterizing the complex dy-
457 namical landscapes of neural data. Modern tools from deep learning, such as variational
458 autoencoders, can be used to unravel the reduced spaces underlying neuroimaging or
459 neurophysiological data [53, 54], while dynamical systems theory in concert with dif-
460 ferential geometry, group theory, and algebraic topology data analysis [95] offer robust
461 frameworks to understand and characterize them [89, 96–100]. Topological data anal-
462 ysis can also be used to explore the graphs associated with model space, for example,
463 the structural (connectome) or effective connectivity between regions in the brain (see
464 [101] for a recent review). Topological methods have already been successfully employed
465 to analyze detailed microscopic models [98], to study the relationship of criticality and
466 topology in models [102], and to characterize functional brain networks derived from
467 neuroimaging data [87, 88, 101].

468 World-tracking constraints force the brain as a dynamical system to mirror the symmetry
469 in the data [37], a requirement that translates into constraints on structural and dynam-
470 ical aspects of the system (and which can be analyzed using Lie group theory). This
471 suggests leveraging the known links between topology and Lie groups [103]. The con-
472 vergence of these mathematical techniques extends to neuroscience the fruitful exercise
473 in physics of linking geometry and topology.

474 Finally, it would be interesting to explore if hierarchical data processing systems such as

475 the brain display dynamical manifolds with hierarchical structure, including topology.
476 This possibility is intuitive given the connections between the notions of criticality, in-
477 formation processing, and hierarchical organization [34, 104]. In this sense, the effects
478 of psychedelics, which are seen to increase the temperature of the system [34] and the
479 complexity of dynamics, should be reflected as an increase in the topological complex-
480 ity of the associated dynamical attractors, as we discussed above with the analogy to
481 wormholes.
482 The relationship between hierarchy and topological complexity could be analyzed, for
483 example, by exploring artificial neural networks carrying out hierarchical processing
484 (any generative deep network trained on real-world data would do, in principle). Such
485 networks could then be used to generate neural activation data and analyze, for instance,
486 whether the depth of the network (the number of layers in its hierarchical architecture)
487 is reflected in the topology (e.g., in Betti numbers) associated with the data or its latent
488 space.

489 5 Conclusions

490 In this paper, we have defined the umbrella of neural geometrodynamics to study the
491 coupling of state dynamics and their complexity, geometry, and topology with plastic
492 phenomena. We have enriched the discussion by framing it in the context of the acute
493 and longer-lasting effects of psychedelics.
494 As a source of inspiration, we have established a parallel with other mathematical theo-
495 ries of nature, namely in general relativity, where dynamics and the “kinematic theatre”
496 are intertwined (see the Appendix for a similar parallel with electrodynamics).
497 Although we can think of “geometry” in neural geometrodynamics as referring to the
498 structure imposed by connectivity on state dynamics (paralleling the role of the met-
499 ric in general relativity), it is more appropriate to think of it as the geometry of the
500 reduced phase space (or invariant manifold) where state trajectories ultimately will lie:
501 this is where the term reaches its fuller meaning. Since the fluid geometry and topol-
502 ogy of the invariant manifolds underlying apparently complex neural dynamics may be
503 strongly related to brain function and first-person (structured) experience [16], further
504 research should focus on creating and characterizing these fascinating mathematical
505 structures.

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796 A Appendix

797 A.1 A nautical analogy

798 To illustrate the interconnected dynamics of neural states, connectodynamics, and meta-
799 plasticity, consider a toy sailing boat navigating a circular pond. The boat moves through
800 the pond, creating ripples that propagate across the water's surface, eventually reflecting
801 off the pond's boundaries. These reflected ripples, in turn, influence the boat's trajec-
802 tory. This mirrors the dynamics of brain states, analogous to neural dynamics expressed
803 by the equation $\dot{x} = f(x; w, \eta(t))$, where the boat's position represents the state x and
804 the water surface's geometry reflects the effective connectivity w . The term $\eta(t)$ may be
805 associated with an external force such as the wind.

806 The changes in the geometry of the water surface caused by the boat's movement symbol-
807 ize connectodynamics. This is captured by the plasticity equation $\dot{w} = g(x, w; \theta)$, where
808 the evolving connectivity parameters w depend on the boat's position x and other fac-
809 tors. The boat's position and the water's surface geometry are intrinsically linked, akin
810 to brain state and effective connectivity.

811 Further, imagine that other external factors, such as temperature fluctuations or changes
812 in water viscosity, modify the water's molecular structure over time. For example, a tem-
813 perature decrease nearing freezing could alter the water structure (density and viscosity
814 [105]) in the pond and how the boat's movement affects the water geometry. This
815 change in the water's properties symbolizes the dynamics of plasticity, or metaplasticity,
816 as described by $\dot{\theta} = \xi(x, w, \theta; \mu(t))$.

817 A.2 Classical dynamics of particles and fields

818 Here we provide the equations for other systems where one can think of part of the
819 equation describing the geometry of a space-providing subsystem ("kinematic theatre")
820 and another the subsystem moving in this space, influenced by the structure and affecting
821 its geometry in return. Several such examples can be found in physics.

822 Non-relativistic electrodynamics

823 The non-relativistic dynamics of N -charged particles and the associated electromag-
824 netic field are described by (coupled) Newton's second law and Maxwell's equations.
825 The charged particles are influenced by the electromagnetic field and at the same time,
826 generate it. This can lead to problematic scenarios, such as the self-interaction prob-

827 lem: charged particles generate an electromagnetic field, and if one considers a particle's
 828 interaction with its own field, paradoxical or unphysical results can arise. This self-
 829 interaction leads to divergences in calculations and has been a longstanding challenge in
 830 classical electrodynamics until recently [106].

831 The motion of the i th electron is given by $m_i \frac{d^2 \mathbf{r}_i}{dt^2} = \mathbf{F}_i$, where $\mathbf{F}_i = q_i(\mathbf{E} + \mathbf{v}_i \times \mathbf{B})$ is
 832 the Lorentz force. The electromagnetic field obeys Maxwell's equations:

$$\begin{aligned}\nabla \cdot \mathbf{E} &= \frac{\rho}{\varepsilon_0}, \\ \nabla \cdot \mathbf{B} &= 0, \\ \nabla \times \mathbf{E} &= -\frac{\partial \mathbf{B}}{\partial t}, \\ \nabla \times \mathbf{B} &= \mu_0 \mathbf{J} + \mu_0 \varepsilon_0 \frac{\partial \mathbf{E}}{\partial t},\end{aligned}$$

833 where $\rho(\mathbf{r}, t) = \sum_i q_i \delta(\mathbf{r} - \mathbf{r}_i(t))$ and $\mathbf{J}(\mathbf{r}, t) = \sum_i q_i \mathbf{v}_i(t) \delta(\mathbf{r} - \mathbf{r}_i(t))$ are the charge and
 834 current densities.

835 Relativistic equations

836 Maxwell's equations are relativistic (they transform properly under Lorentz transforma-
 837 tions), but Newton's is not. For the **relativistic version**, the field strength tensor $F^{\mu\nu}$
 838 is defined in terms of the four-potential A^μ [107],

$$F^{\mu\nu} = \partial^\mu A^\nu - \partial^\nu A^\mu$$

839 The dual tensor $\tilde{F}^{\mu\nu}$ is defined in terms of $F_{\alpha\beta}$ and the Levi-Civita symbol $\varepsilon^{\mu\nu\alpha\beta}$,

$$\tilde{F}^{\mu\nu} = \frac{1}{2} \varepsilon^{\mu\nu\alpha\beta} F_{\alpha\beta}$$

840 The homogeneous Maxwell's equations are given by:

$$\partial_\mu \tilde{F}^{\mu\nu} = 0$$

841 and the inhomogeneous Maxwell's equations are given by:

$$\partial_\mu F^{\mu\nu} = \mu_0 J^\nu$$

842 where J^ν is the four-current vector, which we now define for a particular case. Given a
 843 distribution of N particles each with charge q_i and four-velocity u_i^μ , the four-current J^μ

844 at position \mathbf{x} and time t is given by

$$J^\mu(\mathbf{x}, t) = \sum_{i=1}^N q_i u_i^\mu \delta^3(\mathbf{x} - \mathbf{x}_i(t))$$

845 Here, $\mathbf{x}_i(t)$ is the position of the i -th particle at time t , and δ^3 is the three-dimensional
846 Dirac delta function.

847 The equation of motion for a charged particle in an electromagnetic field, commonly
848 known as the Lorentz force equation, in its relativistic form is:

$$\frac{dp^\mu}{d\tau} = q F^{\mu\nu} u_\nu$$

849 Here, p^μ is the four-momentum of the particle, u^ν is the four-velocity of the particle,
850 $F^{\mu\nu}$ is the electromagnetic field tensor, and q is the charge of the particle. The equation
851 describes how the four-momentum of the particle changes with proper time τ under the
852 influence of the electromagnetic field.

853 A.3 Modeling plasticity in neural mass models

854 In this section, we provide a brief overview of plasticity mechanisms and how they
855 relate to the terms in the formalism, namely the functions h and ψ . See Table 1 for a
856 summary. Including plasticity in Neuronal Mass Models (NMMs) allows for the modeling
857 of time-varying connectivity strengths that reflect the learning and adaptation processes
858 observed in biological neuronal networks.

859 Functional Plasticity

860 The simplest and most common way to include synaptic plasticity is through Hebbian
861 learning rules. Hebbian plasticity, a type of functional plasticity, follows the principle
862 that “neurons that fire together wire together” [61]. It can be included in NMM using
863 the equation

$$864 \quad \dot{w}_{ij} = \eta x_i x_j - \delta w_{ij} \quad (7)$$

865 where w_{ij} is the synaptic strength from neuron j to neuron i , x_i and x_j are the neuronal
866 activities, and η and δ are parameters controlling the learning and decay rates.

866 Homeostatic Plasticity

867 Homeostatic plasticity, a form of plasticity that adjusts synaptic strengths to keep the
868 overall activity of a neuron or network within a certain range, can be included in an
869 NMM using the equation [62–66],

$$864 \quad \dot{w}_{ij} = \eta(x_i - x_{\text{target}})x_j - \delta w_{ij} \quad (8)$$

870 where x_{target} is the target activity level.

871 Structural Plasticity

872 Structural plasticity, where the actual number and dendrites and arrangement of synapses
873 change over time, can be represented in NMMs by modifying (or even adding) rows
874 and columns from the w adjacency matrix to represent the formation or elimination of
875 synapses or even fibers.

876 Empirically-derived Structural Plasticity

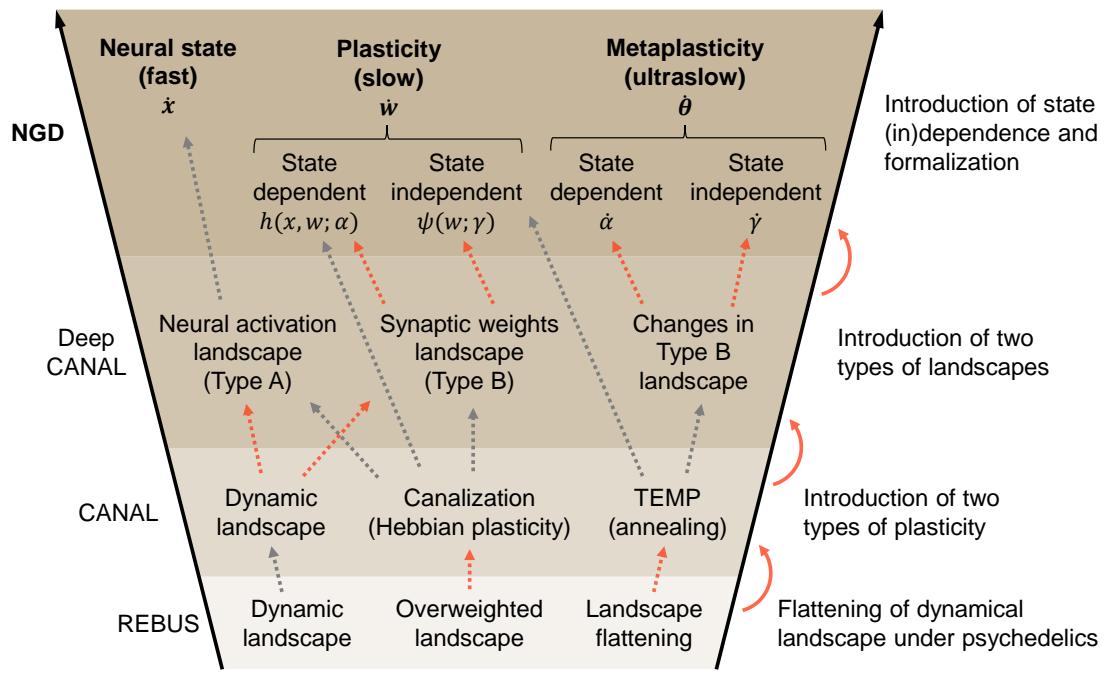
877 NMMs can be used to infer the structural changes to plasticity without explicitly de-
878 scribing the plastic mechanism per se. For example, in the post-acute psychedelic state,
879 NMMs can be used to infer the plastic changes to w_{ij} by optimizing the model functional

880 connectivity FS_{ij}^{model} to approximate the empirical functional connectivity FS_{ij}^{model} with
881 a certain learning rate ϵ as in the following equation.

$$w_{ij} = w_{ij} + \epsilon(FS_{ij}^{empirical} - FS_{ij}^{model}) \quad (9)$$

882 Such optimization is, for example, computed through gradient descent methods with
883 priors on the topology of structural connectivity between brain regions [108]. Recent
884 methods have further extended this framework by adding time-shifted correlation [42]
885 to the optimization as a better description of the overall brain state, as in this case, the
886 post-acute psychedelic state.

887 Including these forms of plasticity in NMMs allows for more realistic modeling of neural
888 systems in better capturing their adaptive nature and the impact of learning and
889 experience on synaptic connections.



NGD – Neural Geometrodynamics
 TEMP – Temperature of Entropy Mediated Plasticity
 REBUS – Relaxed Belief Under pSychedelics

Figure A.1: Conceptual funnel of terms between the NGD (neural geometrodynamics), Deep CANAL [48], CANAL [11], and REBUS [12] frameworks. The figure provides an overview of the different frameworks discussed in the paper and how the concepts in each relate to each other, including their chronological evolution. We wish to stress that there is no one-to-one mapping between the concepts as different frameworks build and expand on the previous work in a non-trivial way. In red, we highlight the main conceptual leaps between the frameworks. See the main text or the references for a definition of all the terms, variables, and acronyms used.

Type	Time Scale	Mechanism	Effects	State-dependence
Functional or dynamical Plasticity	Milliseconds to minutes	Changes in strength/efficiency of synapses (e.g., Hebbian plasticity, LTP, LTD)	Short and long-term memory, fine-tuning of connections	State-dependent (h)
Acute Psychedelic-induced Plasticity	Minutes to Hours	Targeting of serotonergic neuroreceptors especially the 5-HT _{2A} with a result in overall excitability [11, 12, 82, 83]	Flattens or de-weights the dynamical landscape	State-independent (ψ)
Homeostatic Plasticity	Hours to days	Regulation of overall excitability to maintain stability (e.g., adjusting synapse strength for E/I balance) [62–66]	Balances and stabilizes network	State-dependent (h)
Structural Plasticity (e.g., post-acute psychedelic-induced plasticity)	Hours to years	Larger physical changes in neurons (e.g., dendrite growth, synapse formation) through an increase of endogenous BDNF and via TrkB binding (the receptor of BDNF) [84]	Long-term memory, development	Depends on context
Metaplasticity	Various, often longer-term	Changes in mechanisms governing synaptic plasticity (e.g., modulation of thresholds/rules)	Regulates other forms of plasticity, “plasticity of plasticity” [74]	Depends on context

Table 1: Summary of Different Types of Neural Plasticity Phenomena. **State-dependent Plasticity** (h) refers to changes in neural connections that depend on the current state or activity of the neurons involved. For example, functional plasticity often relies on specific patterns of neural activity to induce changes in synaptic strength. **State-independent Plasticity** (ψ) refers to changes that are not directly dependent on the specific activity state of the neurons. For example, acute psychedelic-induced plasticity acts on the serotonergic neuroreceptors and thus acts on the brain networks regardless of specific activity patterns. Some forms of plasticity, like structural plasticity and metaplasticity, may exhibit characteristics of both state-dependent and state-independent plasticity, depending on the context and specific mechanisms involved. Finally, **metaplasticity** refers to the adaptability or dynamics of plasticity mechanisms.