

1      **The spinal cord facilitates cerebellar upper limb motor learning and**  
2      **control; inputs from neuromusculoskeletal simulation**

3      **The spinal cord facilitates cerebellar upper limb motor learning**

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12 **Abstract:** Complex interactions between brain regions and the spinal cord (SC) govern body motion,  
13 which is ultimately driven by muscle activation. Motor planning or learning are mainly conducted at  
14 higher brain regions, whilst the SC acts as a brain-muscle gateway and as a motor control centre pro-  
15 viding fast reflexes and muscle activity regulation. Thus, higher brain areas need to cope with the SC as  
16 an inherent and evolutionary older part of the body dynamics. Here, we address the question of how SC  
17 dynamics affects motor learning within the cerebellum; in particular, does the SC facilitate cerebellar  
18 motor learning or constitute a biological constraint? We provide an exploratory framework by inte-  
19 grating biologically plausible cerebellar and SC computational models in a musculoskeletal upper limb  
20 control loop. The cerebellar model, equipped with the main form of cerebellar plasticity, provides motor  
21 adaptation; whilst the SC model implements stretch reflex and reciprocal inhibition between antagonist  
22 muscles. The resulting spino-cerebellar model is tested performing a set of upper limb motor tasks,  
23 including external perturbation studies. A cerebellar model, lacking the implemented SC model and  
24 directly controlling the simulated muscles, was also tested in the same benchmark. The performances  
25 of the spino-cerebellar and cerebellar models were then compared, thus allowing directly addressing  
26 the SC influence on cerebellar motor adaptation and learning, and on handling external motor pertur-  
27 bations. Performance was assessed in both joint and muscle space, and compared with kinematic and  
28 EMG recordings from healthy participants. The differences in cerebellar synaptic adaptation between  
29 both models were also studied. We conclude that the SC facilitates cerebellar motor learning; when  
30 the SC circuits are in the loop, faster convergence in motor learning is achieved with simpler cerebellar  
31 synaptic weight distributions. The SC is also found to improve robustness against external perturbations,  
32 by better reproducing and modulating muscle cocontraction patterns.

33  
34 **Summary:** Accurate motor control emerges from complex interactions between different brain areas,  
35 the spinal cord (SC), and the musculoskeletal system. These different actors contribute with distributed,  
36 integrative and complementary roles yet to be fully elucidated. To further study and hypothesise about  
37 such interactions, neuromechanical modelling and computational simulation constitute powerful tools.  
38 Here, we focus on the SC influence on motor learning in the cerebellum, an issue that has drawn little  
39 attention so far; does the SC facilitate or hinder cerebellar motor learning? To address this question, we  
40 integrate biologically plausible computational models of the cerebellum and SC, equipped with motor  
41 learning capability and fast reflex responses respectively. The resulting spino-cerebellar model is used  
42 to control a simulated musculoskeletal upper limb performing a set of motor tasks involving two degrees  
43 of freedom. Moreover, we use kinematic and EMG recordings from healthy participants to validate the  
44 model performance. The SC fast control primitives operating in muscle space are shown to facilitate  
45 cerebellar motor learning, both in terms of kinematics and synaptic adaptation. This, to the best of our  
46 knowledge, is the first time to be shown. The SC also modulates muscle cocontraction, improving the  
47 robustness against external motor perturbations.

## 48 1 Introduction

49 Accurate motor control enables interactions with the environment and others, a process in which sen-  
50 sory information is integrated by the central nervous system (CNS) and translated into muscle activity,  
51 eventually driving body motion. Body motion results from the interaction between the musculoskeletal  
52 system and diverse neural regions with distributed, integrative and complementary roles [1]. In the  
53 brain, various neural regions project descending motor control signals to the spinal cord (SC); e.g., the  
54 motor cortex, involved in the volitional control of motion [2]; the basal ganglia, involved in selecting  
55 motor behaviour and balance control [3, 4]; the cerebellum, involved in motor coordination and learning  
56 [5]. The SC circuits integrate those motor descending signals to regulate motoneuron activity, ultimately  
57 driving muscle activation. Besides, the SC also implements its own motor control mechanisms; e.g., fast  
58 reflexes, control of rhythmic locomotion movements, or responses against perturbations [5].

59 Motor control within the CNS could be synthesised as a hierarchical process; higher brain areas  
60 govern motor functions such as planning or learning, and the SC then integrates their descending control  
61 signals, provides faster and lower-level control mechanisms, and ultimately drives muscle activity. To  
62 comprehend and hypothesise about this hierarchical interaction, neuromechanical modelling and com-  
63 putational simulation represent powerful tools, providing a holistic view conjugating from neuron to  
64 neural network to motor behaviour levels [6]. To that aim, we present a hierarchical structure comprising:  
65 a cerebellar model, a higher brain area equipped with motor learning and adaptation; an SC model,  
66 integrating the cerebellar descending control signals and implementing fast-reflexes and muscle activity  
67 regulation, and finally actuating a musculoskeletal upper limb model. This spino-cerebellar integration  
68 thus provides a computational exploratory framework, which was further complemented with kinematic  
69 and EMG data validation. Both the cerebellum and SC main physiological mechanisms have been pre-  
70 viously described, however, little attention has been put on the SC influence on cerebellar motor control.  
71 Spinal circuits are evolutionary old, they were present in the first vertebrates emerged about 500 million  
72 years ago [7] and fully allowed basic locomotion [8]. As new higher neural areas evolved to handle more  
73 complex motor control, they had to coexist and interact with the old lower spinal circuits. It is not clear  
74 whether that interaction facilitates motor control or implies a constraint with which higher neural regions  
75 have to live with. On the one hand, the SC benefits motor control providing fast feedback loops, lower  
76 dimensionality for planning and control, and motor primitives (i.e., low level motor building blocks).  
77 On the other hand, higher brain areas have to deal with the highly non-uniform control space and hidden  
78 states in the SC, and the need for inverse models that cover not only the body dynamics but also the  
79 SC dynamics. Here, we study whether the SC facilitates cerebellar motor learning, or it is simply an  
80 evolutionary constraint to be handled.

81 The cerebellum is key in motor control and coordination, and most importantly motor learning [9].  
82 The Marr-Albus-Ito theory on cerebellar function [10] established the computational principles for su-  
83 pervised cerebellar learning [11], by which the cerebellum enables the adaptation of our actions so their  
84 consequences match up to our expectations, i.e., minimising the difference between our intention and  
85 the actual movement [12]. This motor learning capability stands upon the plasticity exhibited at the  
86 synapses from parallel fibres (PF), i.e., axons of granule cells (GC), to Purkinje cells (PC); plasticity  
87 regulated by the action of climbing fibres (CF) reaching PCs [13]. The Marr-Albus-Ito theory assumes  
88 the GCs carry a recoding of the sensory inputs conveyed through mossy fibres (MF) [14], whereas CFs  
89 carry an instructive signal coding the disparity between our motor expectation and the actual motor state.  
90 Despite the well-accepted common ground on the cerebellum established by the Marr-Albus-Ito theory,  
91 new findings keep refining the understanding about cerebellar structure and operation, for which com-  
92 putational models are key contributors [15]. Computational models of the cerebellum have been used  
93 to study its inner dynamics [16, 17], as well as harnessing cerebellar motor adaptation capabilities to  
94 develop adaptive controllers based on internal model building [18, 19].

95 Lower down in the CNS hierarchy, the SC transmits control signals from brain motor areas to the  
96 muscles, and it also conveys sensory signals from muscle receptors back to the brain. But its role in  
97 motor control goes beyond a mere gateway between the brain and muscles [20, 21]. The SC contains  
98 neural pathways that regulate muscle activity, control reflex responses and produce rhythmic locomotion  
99 movements. These spinal pathways channel the sensory feedback mainly from stretch sensitive muscle  
100 spindles and tension sensitive Golgi tendon organs (GTO). This sensory feedback is then transmitted to  
101 motoneurons through afferent fibres and spinal interneurons, allowing reflex responses and muscle reg-  
102 ulation mechanisms: e.g., stretch velocity reflex, static stretch reflex, Golgi tendon reflex, or reciprocal  
103 inhibition between antagonist muscles [5]. Besides, these spinal pathways are modulated by higher brain  
104 areas during movement execution such as between the stance and swing phases during gait [22, 23], or  
105 during arm movements [24, 25, 26], thus highlighting the importance of the interaction between the SC  
106 and higher brain areas.

107 Computational models have been used to gain deeper insight on the SC role in motor control; e.g.,

108 control of centre-out reaching movements [27]; control of biceps stretch reflex [28]; reflex modulation  
109 via feedback gains [29]; rejection of dynamic perturbations, highlighting the latency hierarchy levels of  
110 feedback [30], or the contribution of GTO feedbacks [31]. However, these approaches lacked complex  
111 descending signals from higher brain areas, usually applying open-loop supraspinal modules, hence hin-  
112 dering their use to study the interaction between the SC and higher neural regions; larger scale models  
113 are required.

114 Little work has been done on large scale modelling to dig into the SC interaction with higher CNS  
115 regions. A recent example coupled spinal circuits with sensory and motor cortex models, forming a  
116 feedback control loop designed to reduce the difference between the desired and perceived state of a  
117 planar six-muscle arm [32]. The model showed motor control success and reproduced some previous  
118 experimental phenomena, whilst it was suggested that the ataxic nature of the produced movements  
119 could be due to the lack of a cerebellum model in the loop.

120 Regarding spino-cerebellar integration in particular, a few previous computational approaches ex-  
121 ist. Contreras-Vidal et al. modelled a cerebellum cooperating with an SC-based muscular force model,  
122 together with a central pattern generator representing the motor cortex and basal ganglia [33]. The  
123 cerebellar model, developed in analogue form and lacking the temporal correlation nature of cerebel-  
124 lar learning, succeeded in learning muscle synergies, including cocontraction of antagonist pairs, that  
125 improved upon the SC feedback control of tracking. Different cerebellar lesions were studied, but the  
126 influence of the SC in cerebellar motor adaptation was sidestepped. Subsequently, Spoelstra et al. inte-  
127 grated a cerebellar model with an SC model for postural control of a six-muscle two-dimensional arm  
128 model [34]. The study assessed the predictive role of the cerebellum in accurate motor control, but  
129 again, the effect of the SC in cerebellar learning was not addressed. More recently, Jo integrated a func-  
130 tional cerebellar model with spinal circuits equipped with plasticity but lacking reflex or other complex  
131 spinal dynamics [35]. Results showed the effectiveness of the model to learn movements, with synaptic  
132 plasticity at the SC helping to acquire muscle synergies. However, as stated by the author, that learning  
133 capacity provided to the SC could be located anywhere in the corticospinal pathway, hence loosening  
134 possible conclusions on the cerebellum-SC relation.

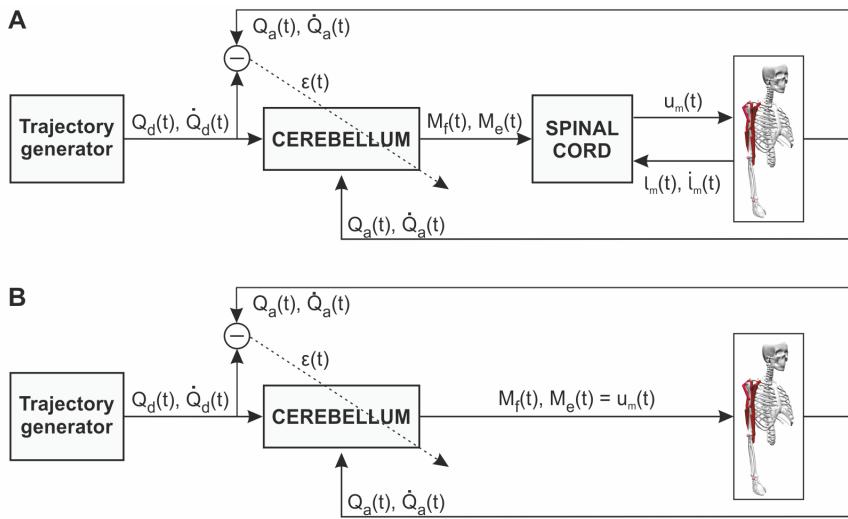
135 With the present work, we intend to extend the spino-cerebellar integration studies; we addressed the  
136 questions of whether the SC facilitates cerebellar learning or it is just as an evolutionary constraint, and  
137 how the SC contributes to handling motor perturbations. We modelled a biologically plausible cerebellar  
138 spiking neural network (SNN), equipped with synaptic plasticity at GC-PC connections guided by the  
139 instructive signal conveyed through CFs, thus, able to provide motor adaptation. We added an SC model  
140 equipped with stretch reflex and reciprocal inhibition, integrating the descending signals from the cere-  
141 bellum and sending muscle excitation commands to the musculoskeletal upper limb model, equipped  
142 with two degrees of freedom (DOF) actuated by eight Hill-based muscles. Both the cerebellar and SC  
143 model were integrated in a negative feedback control loop. The study, developed using computational  
144 tools and neuromechanical modelling, is also supported by lab recorded kinematics and EMG data from  
145 healthy participants.

146 In the presented framework, the cerebellar model provides the motor adaptation required for the  
147 musculoskeletal upper limb model to achieve a set of goal motor behaviours, i.e., different upper limb  
148 movements are defined in joint space (position and velocity), and the cerebellum acquires the inverse  
149 model allowing accurate position and velocity tracking. We suggest the SC fast control primitives and  
150 regulation of muscle activity to be key in facilitating the cerebellar learning of the muscle dynamics; the  
151 SC allowed faster motor learning with simpler cerebellar synaptic adaptation. We also hypothesise that  
152 the SC plays a major motor control role through cocontraction modulation; i.e., regulation of simultane-  
153 ous activation of antagonist muscles. Cocontraction has been shown to improve stability by increasing  
154 joint apparent stiffness [36], enhance upper limb movement accuracy [37], and it has also appeared use-  
155 ful in movements requiring robustness against perturbations [38]. We found that the stretch reflex and  
156 reciprocal inhibition mechanisms participate in modulating cocontraction, with a significant impact on

157 cerebellar motor adaptation and response against external perturbations.

## 158 2 Results

159 We integrated the spinal cord and cerebellum models in an upper limb musculoskeletal feedback control  
 160 loop (Fig. 1A). The spino-cerebellar model commanded the upper limb to perform a set of motor tasks,  
 161 a motor benchmark divided in two groups: i) lab recorded upper limb movements performed by two  
 162 healthy participants to study natural self-selected movements, ii) lab designed upper limb movements  
 163 with bell-shaped velocity profiles to study standard characteristic reaching movements. A cerebellar  
 164 model lacking the SC integration performed in the same motor benchmark (Fig. 1B) thus providing a  
 165 spino-cerebellar vs. cerebellar control framework that allowed contextualising the SC and cerebellum  
 166 integration (see Methods for a further description of the control loop and motor benchmark).



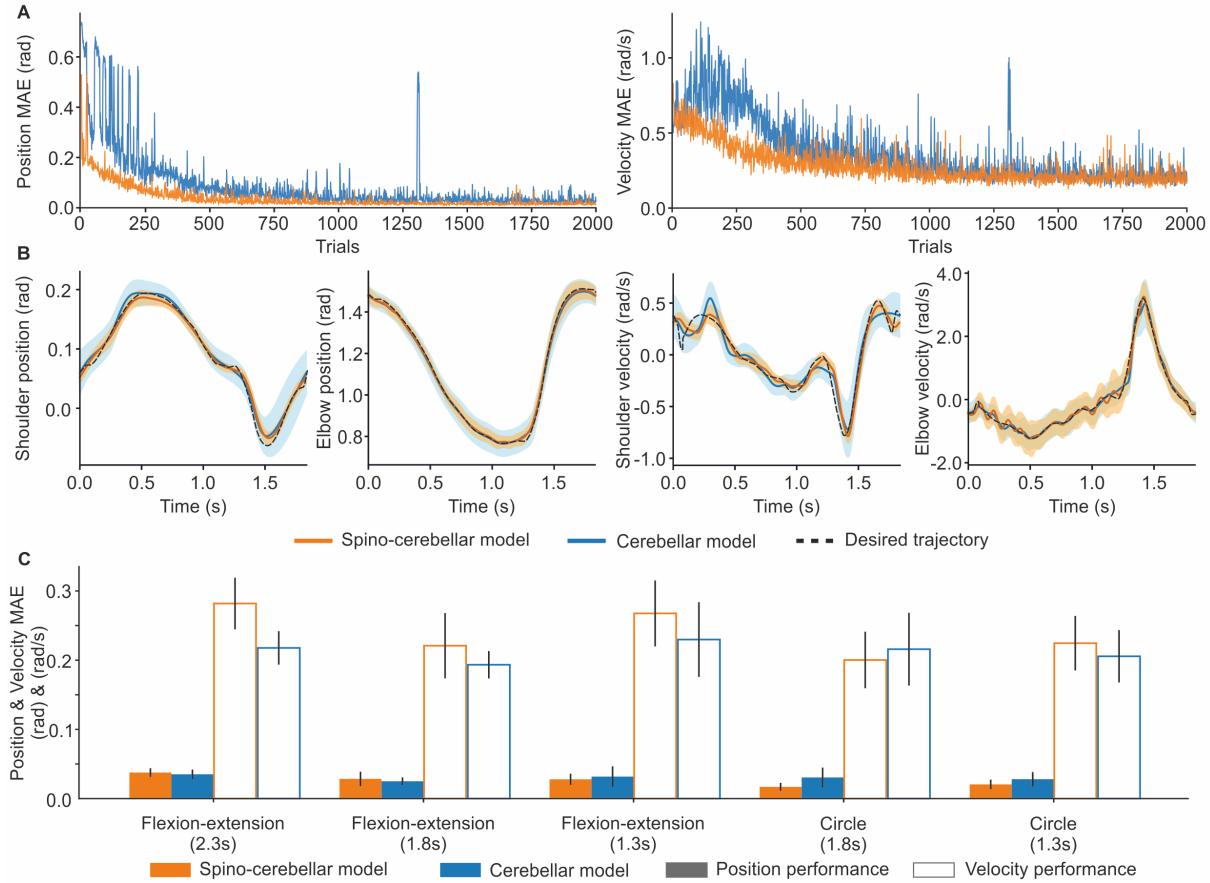
**Fig. 1. Spino-cerebellar and cerebellar control loops.** **A)** Spino-cerebellar model. The cerebellum received the following input sensory information: the desired trajectory (joint position,  $Q_d$ , and velocity,  $\dot{Q}_d$ ) coming from a trajectory generator, representing the motor cortex and other motor areas performing motor planning and inverse kinematics; the actual upper limb state (joint position,  $Q_a$ , and velocity,  $\dot{Q}_a$ ) received from the musculoskeletal model; the instructive signal ( $\epsilon$ ) obtained as the mismatch between the desired and actual joint state. The cerebellum then generated two output control signals per joint ( $M_f$  and  $M_e$ , for flexor and extensor muscles, respectively), which were processed at the spinal cord. The spinal cord also received the muscle state (length,  $l_m$ , and velocity,  $\dot{l}_m$ ) and generated the final muscle excitation signals ( $u_m$ ) which actuated the musculoskeletal model. The musculoskeletal model included two joints, shoulder and elbow, actuated by eight muscles: deltoid posterior and biceps long as shoulder flexors; deltoid anterior and triceps long as shoulder extensors; biceps long, short and brachialis as elbow flexors; triceps long, lateral and medial as elbow extensors. **B)** Cerebellar model.  $M_f$  and  $M_e$  were directly applied as muscle excitation signals commanded to the upper limb. For bi-articular muscles (biceps long and triceps long), the resulting  $u_m$  was the mean of the control signal ( $M_f$  or  $M_e$ ) from both joints.

167 The following sections present the validation of the spino-cerebellar model with the lab recorded  
 168 kinematics and EMG data; an evaluation of the SC effect in cerebellar motor adaptation in joint, synaptic  
 169 and muscle spaces; and testing the response against external motor perturbations.

## 170 2.1 Spino-cerebellar and cerebellar models perform the recorded kinematics

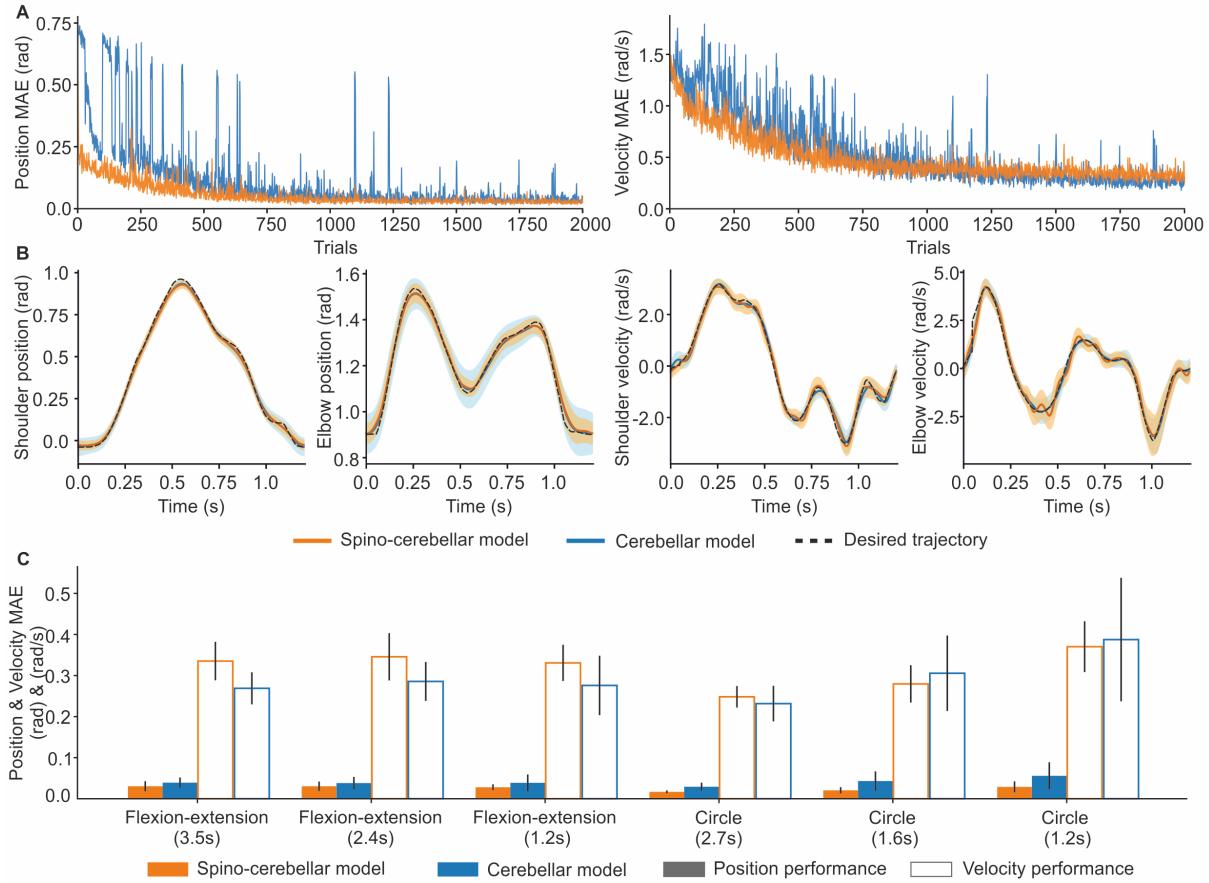
171 We extracted kinematics and EMG data from two healthy participants (P1 and P2) performing upper  
172 limb movements in the vertical plane involving the shoulder and elbow (see Methods). The motor tasks  
173 performed by P1 and P2 can be grouped in: i) flexion-extension movements, ii) hand-tracked circular  
174 trajectories. Both motor task groups were performed at different speeds, thus providing a set of natural  
175 upper limb trajectories which constituted our initial motor control benchmark. We used the joint kine-  
176 matics (i.e., shoulder and elbow position,  $Q_d$ , and velocity,  $\dot{Q}_d$ ) extracted from the recording sessions  
177 as the desired trajectory to be learnt by the spino-cerebellar (Fig. 1A) and cerebellar (Fig. 1B) models  
178 in the simulation framework. Both models performed 2000 consecutive trials of each desired trajectory,  
179 a trial-and-error process that allowed motor adaptation to fully deploy from scratch. The performance  
180 metric was given by the position and velocity mean absolute error (MAE), i.e., difference between the  
181 desired and actual trajectory in joint space, allowing to assess motor behaviour (see Methods).

182 We first calculated the position and velocity MAE evolution for both the spino-cerebellar and cere-  
183 bellar models performing the trajectories extracted from each participant (Fig. 2A, P1's 1.8s circle tra-  
184 jectory; Fig. 3A, P2's 1.2s flexion-extension; see Supporting Information for all P1 and P2 motor tasks  
185 MAE evolution (S1A to S9A Fig.)). As the trajectory was repeated over time, the cerebellar adaptation  
186 allowed position and velocity error reduction. At the end of the motor adaptation process, both the spino-  
187 cerebellar and cerebellar models followed the target kinematics (Fig. 2B and Fig. 3B; see Supporting  
188 Information for all P1 and P2 motor tasks kinematics performance (S1B,C to S9B,C Fig.)).



**Fig. 2. Spino-cerebellar and cerebellar models kinematics performance for the lab recorded scenario, participant 1 (P1).** **A)** Position and velocity mean absolute error (MAE) over the 2000-trial motor adaptation process for both the spino-cerebellar and cerebellar models performing P1's slow circle trajectory (1.8s). **B)** Joint kinematics of the last 200 trials (mean and *std*) for both models performing P1's slow circle trajectory (1.8s). **C)** Mean and *std* of the position and velocity MAE (last 200 trials) for all P1 recorded trajectories. All spino-cerebellar vs. cerebellar mean position and velocity MAE have a T-test p-value  $\leq 0.001$ .

189 We found that, attending to the MAE mean and standard deviation (std) of the last 200 trials of the  
 190 motor adaptation process (Fig. 2C and Fig. 3C), the spino-cerebellar model reached better performance  
 191 in terms of position tracking for all trajectories except for P1's slow (2.3s) and moderate (1.8s) flexion-  
 192 extension (all spino-cerebellar vs. cerebellar mean position MAE having a T-test p-value  $\leq 0.001$ ).  
 193 Conversely, the cerebellar model reached better performance in terms of velocity tracking except for  
 194 P1's slow (1.8s) circle and P2's moderate (1.6s) and fast (1.2s) circle (all spino-cerebellar vs. cerebellar  
 195 mean velocity MAE having a T-test p-value  $\leq 0.001$ , except for P2's fast circle (1.2s) with a p-value =  
 196 0.136).



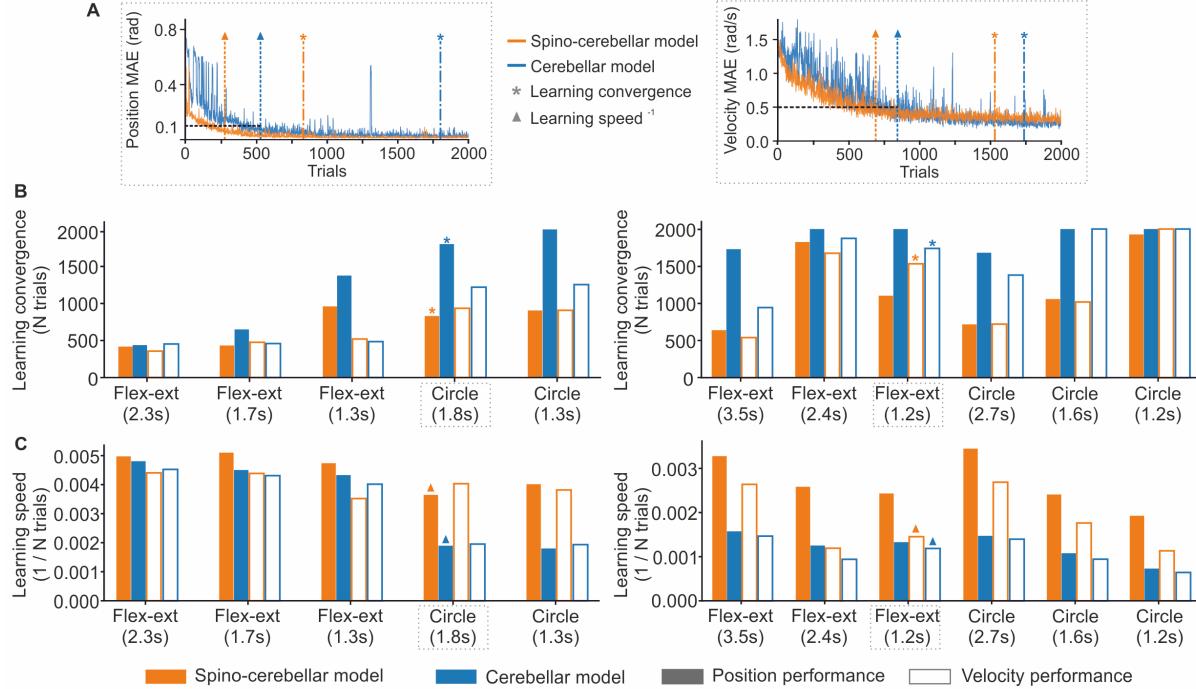
**Fig. 3. Spino-cerebellar and cerebellar models kinematics performance for the lab recorded scenario, participant 2 (P2). A)** Position and velocity mean absolute error (MAE) over the 2000-trial motor adaptation process for both the spino-cerebellar and cerebellar models performing P2's fast flexion-extension (1.2s). **B)** Joint kinematics of the last 200 trials (mean and *std*) for both models performing P2's fast flexion-extension (1.2s). **C)** Mean and *std* of the position and velocity MAE (last 200 trials) for all P2 recorded trajectories. All spino-cerebellar vs. cerebellar mean position and velocity MAE have a T-test p-value  $\leq 0.001$ , except for fast circle (1.3s) velocity with a p-value = 0.136.

## 197 2.2 The spinal cord improves cerebellar learning convergence and speed

198 Once we revealed the adaptation capability of both the spino-cerebellar and cerebellar models, we studied  
 199 the influence of the SC model on cerebellar learning over the adaptation process. Using the position  
 200 and velocity MAE evolution of each P1 and P2 trajectory, we compared the spino-cerebellar and cerebel-  
 201 lar models learning convergence and learning speed. To study learning convergence we applied control  
 202 charts on the MAE data to determine the number of trials required to achieve a stable performance [39].  
 203 To check learning speed we analysed the number of trials required for the mean MAE of 200 samples  
 204 to reach a given target (i.e., 0.1 rad for position MAE, and 0.5 rad/s for velocity MAE). Learning con-  
 205 vergence and speed were tested on both position and velocity tracking performance (see Fig. 4A for  
 206 an example of position and velocity MAE evolution and the metrics used, see Methods for a further  
 207 description).

208 The SC was proven to facilitate cerebellar learning as it reduced learning convergence time (Fig. 4B),  
 209 and increased learning speed (Fig. 4C) for both position and velocity for both P1 and P2 trajectories  
 210 (Fig. 4 left and right column, respectively). Thus, cerebellar motor adaptation was shown to be: i)

211 stabilised by the SC: average convergence time for  $MAE_{pos}$  was  $988 \pm 466$  trials for the spino-cerebellar  
 212 model, and  $1607 \pm 536$  trials for the cerebellar model; and for  $MAE_{vel}$   $978 \pm 512$  trials, and  $1255 \pm 581$   
 213 trials, respectively; ii) accelerated by the SC: average learning speed for position was  $3.5e-3 \pm 1.0e-3$   
 214 trials $^{-1}$  for the spino-cerebellar model, and  $2.3e-3 \pm 1.4e-3$  trials $^{-1}$  for the cerebellar model; and for  
 215 velocity  $2.8e-3 \pm 1.2e-3$  trials $^{-1}$ , and  $2.1e-3 \pm 1.4e-3$  trials $^{-1}$ , respectively.



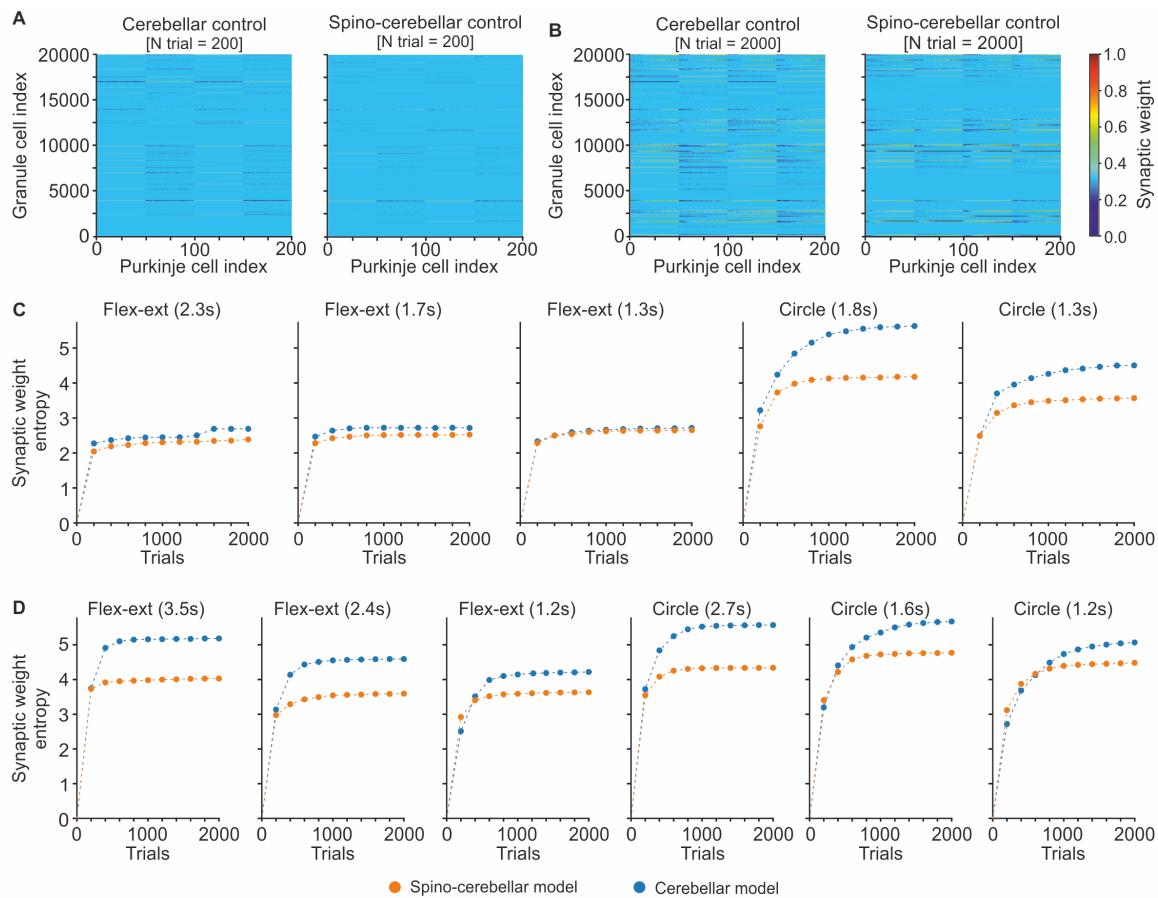
**Fig. 4. Spino-cerebellar and cerebellar models motor adaptation for all P1 and P2 recorded trajectories.** A) Position MAE for the spino-cerebellar and cerebellar models for P1 slow circle (left column), and velocity MAE for both models performing P2 fast flexion-extension (right column). Both MAE plots show the trials at which the learning convergence and learning speed metrics are fulfilled. B) Learning convergence for both models and all trajectories from P1 (left column) and P2 (right column). The bar plots display the number of trials required by each model to fulfill the learning convergence criteria (see Methods). C) Learning speed for both models and all trajectories from P1 (left column) and P2 (right column). The bar plots depict the inverse of the number of trials required to reach a position MAE of 0.1 rad and a velocity MAE of 0.5 rad/s.

## 216 2.3 The spinal cord simplifies cerebellar synaptic adaptation at GC-PC

217 Consistently with the Marr-Albus-Ito cerebellar theory, learning in the cerebellum was provided by  
 218 means of an STDP mechanism adjusting the synaptic weights at GC to PC synapses (a connection  
 219 established through PFs, i.e., GC axons). The effect of the SC on cerebellar learning, already checked  
 220 in terms of motor performance in the previous section, must leave its trace at the level of cerebellar  
 221 synaptic adaptation.

222 During the motor adaptation process of both the spino-cerebellar and cerebellar models, we recorded  
 223 the synaptic weight evolution at GC-PC connections every 200 trials for all P1 and P2 trajectories  
 224 (Fig. 5A and B). We then measured the entropy of the GC-PC synaptic weight distributions to quan-  
 225 tify the synaptic complexity for both models: the higher the entropy, the more complex the synaptic

226 weight distribution, i.e., higher heterogeneity of synaptic weights at the GC-PC population. Contrasting  
 227 the synaptic entropy of both models allowed evaluating the effect of the SC on cerebellar synaptic adap-  
 228 tation (Fig. 5C and D). Noteworthy, results showed that for all motor tasks the SC reduced the entropy  
 229 of the synaptic weight distribution: the mean entropy over all P1 and P2 trajectories was  $3.65 \pm 0.78$   
 230 for the spino-cerebellar model, and  $4.41 \pm 1.14$  for the cerebellar model. When the SC was lacking in  
 231 the control loop, more complex synaptic patterns (i.e., higher specialisation) were required at cerebellar  
 232 GC-PC connections. The spino-cerebellar model showed a simpler distribution of synaptic weights at  
 233 GC-PC connections; in other words, the spinal cord was therefore shown to simplify learning in the  
 234 cerebellum.



**Fig. 5. Spino-cerebellar and cerebellar synaptic entropy.** **A), B)** Synaptic weights at granule cell - Purkinje cell synapses, after 200 and 2000 trials respectively, for both models performing P1's 1.8s circle trajectory. The heat map represents the normalised GC-PC synaptic weights, which could range from 0.0 to 15.0 nS. **C), D)** Evolution of the synaptic entropy at the GC-PC synapses over the 2000-trial motor adaptation process, for all P1 and P2 trajectories, respectively. The higher the entropy, the more complex the GC-PC synaptic distribution (i.e., higher heterogeneity in the synaptic weights over the GC-PC synapses).

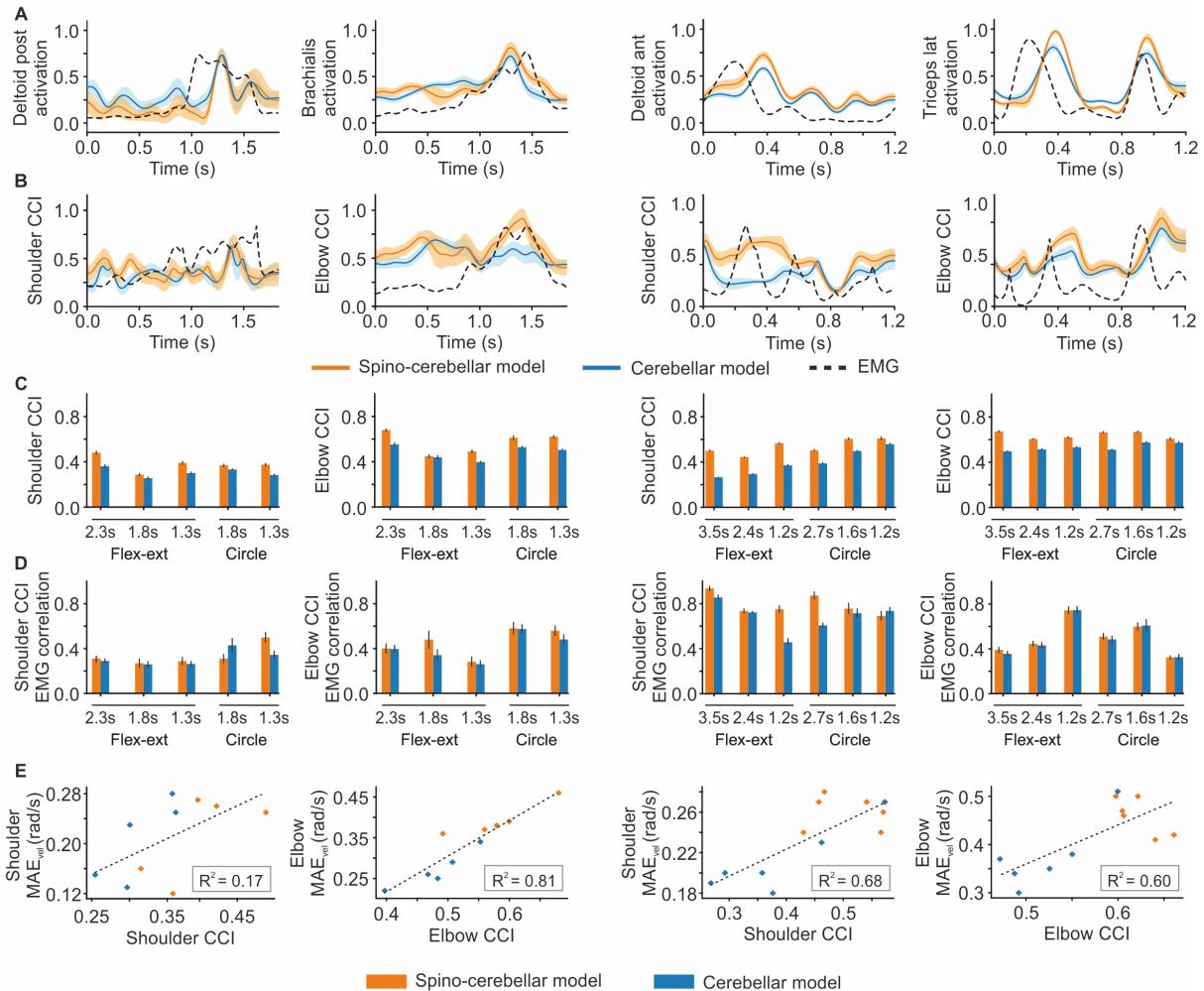
## 235 2.4 Spino-cerebellar and cerebellar outcome in muscle space

236 We then evaluated the outcome in muscle space of both the spino-cerebellar and cerebellar models.  
 237 We compared the recorded EMG envelopes to the main activated muscles during P1 and P2 trajec-  
 238 tories (Fig. 6A, deltoid posterior (DELTpost) and brachialis (BRA) for P1 slow circle, deltoid anterior

239 (DELTant) and triceps lateral (TRIlat) for P2 fast flexion-extension; please find a figure displaying all  
240 the recorded EMG in Supporting Information (S13 and S14 Fig.)). Both models reproduced the main ac-  
241 tivation patterns of each muscle with a small shift for P2 DELTant and TRIlat. The correlation between  
242 the spino-cerebellar or cerebellar activation and the EMG signals was generally larger than 0.5 (see Sup-  
243 porting Information (S15 and S16 Fig.)). The correlation was, however, larger for the spino-cerebellar  
244 model for most of the muscles and scenarios (all spino-cerebellar vs. cerebellar correlation having a  
245 T-test p-value  $\leq 0.001$ ). Nevertheless, the correlation averaged over muscles was similar between the  
246 two models for all the movements and we could not conclude on a better muscle pattern reproduction  
247 by one or the other model (all spino-cerebellar vs. cerebellar mean correlation having a T-test p-value  $\geq$   
248 0.05).

249 Results might not be conclusive when referred to a direct, muscle by muscle comparison between  
250 our models performance and the recorded EMG; note that our musculoskeletal upper limb model was  
251 actuated by 8 muscles, a mere simplification of the complex muscle dynamics of the human upper  
252 limb. To overcome this, we further studied performance in muscle space using the joint cocontraction  
253 index (CCI), thus unifying muscle activity per joint and providing a more comprehensive analysis (see  
254 Methods). We found that the spino-cerebellar model better reproduced the CCI patterns at the level of  
255 the elbow for P1 slow circle and at the level of the shoulder for P2 fast flexion-extension (Fig. 6B).  
256 Significantly, the spino-cerebellar model provided a higher CCI for all P1 and P2 trajectories, both for  
257 the shoulder and elbow (Fig. 6C, all spino-cerebellar vs. cerebellar CCI having a T-test p-value  $\leq 0.001$ ).  
258 We then compared the CCI provided by both models with the CCI from the recorded EMG (Fig. 6D).  
259 The correlation was mainly higher for the spino-cerebellar model for all the trajectories except P1's slow  
260 circle (1.8s) and P2's fast circle (1.2s) for the shoulder (all spino-cerebellar vs. cerebellar correlation  
261 with a T-test p-value  $\leq 0.001$ , except for the fast trajectories for the elbow). We observed a similar trend  
262 as that observed for  $MAE_{vel}$ , therefore, we performed a linear regression between the CCI and  $MAE_{vel}$   
263 for each joint. The results (Fig. 6E) highlighted a linear trend between these quantities for P1 elbow and  
264 P2 shoulder and elbow (with a coefficient of determination of 0.81, 0.68 and 0.60 respectively), whereas  
265 P1 shoulder presented a weaker relationship (with a coefficient of determination of 0.17).

266 Overall, we highlighted various findings that were consistent for various trajectories with various  
267 initial and final positions and speeds. The spino-cerebellar model provided more stable and faster learn-  
268 ing with simpler cerebellar synaptic adaptation, and an increase in CCI with better correlation to the  
269 recorded EMG.



**Fig. 6. Spino-cerebellar and cerebellar model performance in muscle space for all P1 and P2 recorded trajectories.** **A)** Comparison of muscle activation signals with recorded EMGs: the comparison only shows the main activated muscles during recordings of P1's slow circle (two left columns) and P2's fast flexion-extension (two right columns). The plots show the muscle activity of the 200 trials prior to reaching the learning convergence metric, as well as their mean and std, for the two models performance. EMG signals are scaled by the maximum of the activation signals for each muscle for the sake of representation. **B)** Joint cocontraction indexes (CCI) from EMG activity and both models performance, for the trajectories represented in A). EMG CCI are scaled by the maximum of the models CCI for the sake of representation. **C)** Joint CCI values for both models and all P1 (two left columns) and P2 (two right columns) trajectories. All spino-cerebellar vs. cerebellar CCI have a T-test p-value  $\leq 0.001$ . **D)** Joint CCI correlation between the models and EMG for all P1 (two left columns) and P2 (two right columns) trajectories. All spino-cerebellar vs. cerebellar CCI correlation have a T-test p-value  $\leq 0.001$ , except for the fast trajectories for the elbow. **E)** CCI- $MAE_{vel}$  relation: linear regression between joint CCI and joint  $MAE_{vel}$  over all the trajectories from P1 (two left columns) and P2 (two right columns).

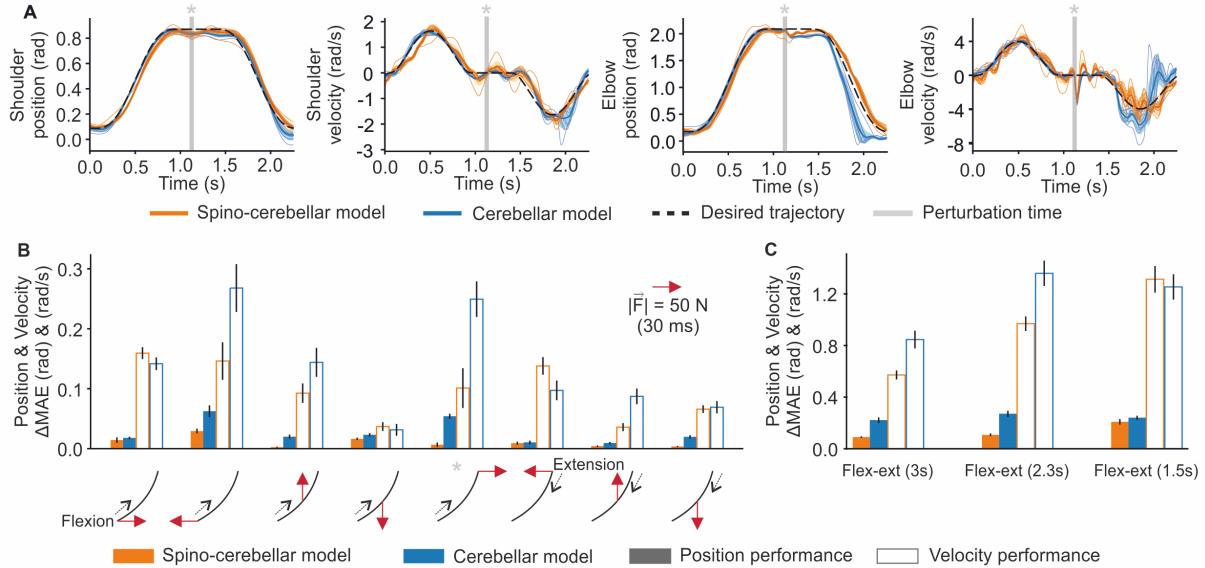
## 270 2.5 The spinal cord increases the robustness against motor perturbations

271 To study the response against external perturbations of both the spino-cerebellar and cerebellar models,  
 272 we used our lab designed benchmark: upper limb flexion-extension movements with bell-shaped ve-  
 273 locity profiles, characteristic of reaching movements [40]. This kind of movement is usually used for

274 addressing active-limb control malfunctioning, as cerebellar patients usually display upper limb oscillatory tremors that result in endpoint overshooting and undershooting when reaching a target [41].  
275

276 Both models faced 2000 consecutive trials of the flexion-extension movement performed at different speeds (3s, 2.3s, 1.5s); after motor adaptation, both models succeeded in performing the target 277 kinematics (see Supporting Information (S17 Fig.)). Once both models adapted to perform the desired 278 trajectories, we tested the contribution of the SC in handling motor perturbations. For that, we induced 279 a set of external forces: i.e., 50 N for 30 ms applied to the hand in different directions and at different 280 points along the flexion-extension movement, resulting in kinematics deviation (Fig. 7A). We then mea- 281 sured the MAE deviation from the ideal, no-perturbation scenario (Fig. 7B). Each perturbation type was 282 applied on 10 separate trajectory trials to get an average response (see Methods). The cerebellar learning 283 capability was disabled to avoid adaptation to the perturbations. Fig. 7A displays the kinematics perfor- 284 mance of both models under one perturbation type, whilst performing the moderate flexion-extension 285 movement (2.3s). Larger kinematic deviation can be observed for the cerebellar model compared to 286 the spino-cerebellar one, especially at the level of the elbow. Fig. 7B presents spino-cerebellar and 287 cerebellar model response against all the perturbations applied during the moderate flexion-extension 288 trajectory. The spino-cerebellar model shows smaller MAE deviation ( $\Delta\bar{MAE}$ ) in position performance 289 for all perturbation types, and smaller velocity  $\Delta\bar{MAE}$  for all perturbations except for the first, fourth 290 and sixth perturbation types. It can be noted that there were both inter and intra-variability in the effect 291 of the various perturbation types on the trajectory kinematics, resulting in T-test p-values  $\geq 0.05$  for 292 spino-cerebellar vs. cerebellar MAE deviation for some cases (see Fig. 7 caption). Similar results were 293 obtained for the slow and fast bell-shaped flexion-extension trajectories; please find the corresponding 294 figure in Supporting Information (S18 Fig.). The spino-cerebellar model was shown to be more robust 295 against perturbations than the cerebellar model.  
296

297 Fig. 7C finally presents the average MAE deviation over all the applied perturbations for the three 298 bell-shaped, flexion-extension trajectories. The spino-cerebellar model results in larger velocity MAE 299 deviation for the fast trajectory, but lower MAE deviation for all the other cases (all spino-cerebellar vs. 300 cerebellar mean MAE deviation having a T-test p-value  $\geq 0.05$  due to the variable effect of the various 301 perturbation types). The SC is thus shown to help handling motor perturbations in most cases.



**Fig. 7. Spino-cerebellar and cerebellar model response against external force perturbations during bell-shaped flexion-extension trajectories.** **A)** Kinematics performance for both the spino-cerebellar and cerebellar models under one forward perturbation at the flexed position whilst performing the 2.3s flexion-extension trajectory. 10 trials are displayed. **B)** Position and Velocity MAE deviation ( $\Delta\bar{MAE}$ ) due to all the perturbations applied during the 2.3s flexion-extension trajectory. Mean  $\Delta\bar{MAE}$  and  $se$  of 10 trials are displayed. Spino-cerebellar vs. cerebellar MAE deviation have a T-test  $p$ -value  $\leq 0.05$  for position for the 3rd, 5th, 6th, 7th and 8th perturbation type, and for velocity for the 1st, 2nd, 4th, 6th and 7th, whereas the other cases have a T-test  $p$ -value  $\geq 0.05$ . **C)** Mean  $\Delta\bar{MAE}$  and  $se$  for all the perturbations applied to the flexion-extension trajectories with different speeds (3s, 2.3s, 1.5s). 10 perturbed trials were used for each perturbation type. All spino-cerebellar vs. cerebellar mean MAE deviations have a T-test  $p$ -value  $\geq 0.05$ .

### 302 3 Discussion

303 The integration of biologically plausible computational models of neural regions allows studying their  
 304 interaction and complementarity. We presented a computational exploratory approach integrating a cere-  
 305 bellar and an SC model, performing motor control of an upper limb musculoskeletal model; a simulation  
 306 framework complemented with kinematic and EMG data validation. We contrasted the spino-cerebellar  
 307 integrated model with a cerebellar model, both performing in the same motor benchmark, which al-  
 308 lowed us to extract some key elements of the kinematic and muscle performance directly attributable to  
 309 the presence of the SC in the spino-cerebellar control loop. The SC was found to stabilise and accelerate  
 310 cerebellar motor adaptation and to improve the response against perturbations through stretch reflexes  
 311 and reciprocal inhibition. Rather than being an evolutionary constraint, the SC offers motor control ben-  
 312 efits.

313 Both the spino-cerebellar and cerebellar models succeeded in learning the musculoskeletal dynam-  
 314 ics to achieve the goal motor behaviour. Noteworthy, the presence of the SC provided faster motor  
 315 adaptation, thus assisting cerebellar learning. In this regard, a significant finding was the fact that the  
 316 spino-cerebellar model revealed less complexity at the GC-PC synaptic weight distribution; i.e., the SC  
 317 led to the formation of less specialised GC-PC synapses in the cerebellum. To the best of our knowledge,  
 318 it is the first time that a computational model highlights and weights the influence of the SC in facilitat-  
 319 ing cerebellar learning. Direct regulation of muscle activity by the SC has been here found to facilitate

320 the cerebellar acquisition of the upper limb inverse dynamics. Indeed, the body plant dynamics to be  
321 learnt by higher brain areas, might be simplified by the SC taking over lower level and faster control  
322 primitives, such as the SC potential role in gravity compensation [42, 43]. Thus, the SC performance in  
323 muscle space may lighten other operations of the sensorimotor process, occurring at a higher level such  
324 as the cerebellum's contribution in compensating interaction torques in joint space [44], or in shaping  
325 spatiotemporal muscle synergies rather than generating specific complex muscle patterns [45].

326 The SC stabilises the system at muscle level, increasing cocontraction through stretch reflexes and  
327 coordinating the antagonist activation patterns through reciprocal inhibition. Thus, the SC participates in  
328 modulating cocontraction, which plays an important role in motor control and stability [36, 38], providing  
329 better accuracy despite its energy cost [37]. In our framework, the spino-cerebellar model increased  
330 the joint CCI in all the studied motor tasks compared to the cerebellar model; i.e., cocontraction was  
331 indeed mostly determined by the SC motor action. Importantly, the CCI from the spino-cerebellar model  
332 also resulted in a better correlation with the CCI patterns from the recorded EMG signals, thus supporting  
333 closer biological plausibility than the cerebellar model. The CCI increment was also revealed when  
334 inducing perturbations in the control loop; the spino-cerebellar model provided a better response, reducing  
335 the kinematic deviation. Muscle elasticity has been previously pointed as a key passive contributor  
336 in handling perturbations [46]. Our framework, using the same muscle mechanical properties in both  
337 the spino-cerebellar and cerebellar control loops, allowed directly assigning to the SC a pivotal role in  
338 providing robustness against external perturbations, thus supporting previous findings [30, 31].

339 The cocontraction increase carried by the SC involved a poorer velocity tracking. Indeed, the spinal  
340 reflexes between antagonist muscles may induce oscillatory activation patterns and thus alter the velocity  
341 performance. We did not observe, however, any trend in CCI values related to movement speeds despite  
342 higher cocontraction values have been reported in slower movements [38]. Due to the SC and cerebellar  
343 models conception, our implementation lacks differentiation between the roles of the cerebellum and SC  
344 depending on movement speed. Note however that it is expected a major role of the cerebellum in fast  
345 ballistic movements which cannot rely on feedback availability [47, 34], and which do present lower  
346 cocontraction levels [38].

347 Our model could be further improved by adding other cocontraction mechanisms to the control loop.  
348 Clinical studies supported a potential role of the cerebellum and basal ganglia in cocontraction mechanisms.  
349 In particular, patients with cerebellar ataxia showed excessive agonist-antagonist coactivation [48] and cerebellar stimulation was shown to reduce coactivation in patients with spasticity [49]. Thus,  
350 future development of the cerebellar model shall include control of the cocontraction level. On the SC  
351 side other pathways could be included, in particular modulation mechanisms that are present during  
352 arm movements [24, 25, 26]. For instance, presynaptic inhibition of Ia terminals at both activated and  
353 antagonist pathways is slightly decreased at the onset of a voluntary contraction through descending signals.  
354 Thus, the increased gain of the stretch reflex pathway ensures that activated motoneurons receive  
355 Ia feedback support. The reciprocal Ia inhibition is also depressed during a voluntary contraction at  
356 the corresponding muscle to prevent its inhibition by the stretch-induced Ia discharge from its antagonist.  
357 During cocontraction, reciprocal Ia inhibition is also depressed by increased presynaptic inhibition  
358 on Ia terminals [5]. Also synaptic plasticity could be included in the SC model, as done in previous  
359 computational approaches [32]. Activity dependent plasticity mechanisms have been reported in the  
360 SC: e.g., the spinal stretch reflex can indeed be conditioned [50]; the feedforward circuits within the  
361 SC, in addition to somatosensory feedbacks, may contribute to SC learning by allowing motoneurons to  
362 contrast feedforward and feedback motor inputs [51]. Supporting the latter, [52] showed that signals in  
363 human muscle spindle afferents during unconstrained wrist and finger movements predict future kinematic  
364 states of their parent muscle. Muscle spindles would then have a forward-sensory-model role, as  
365 that attributed to the cerebellum [53], emphasising the complementarity and overlapping functionality  
366 between neural regions.

367 Integrated computational models represent a powerful tool to support and guide experimental studies

369 in the pursuit of a better understanding of the CNS. We believe our spino-cerebellar model to contribute  
370 in this direction, providing a picture of how the SC influences cerebellar motor adaptation and learn-  
371 ing. Further development of the model, together with addition of other neural regions, will help to keep  
372 elucidating CNS operation.

## 373 4 Methods

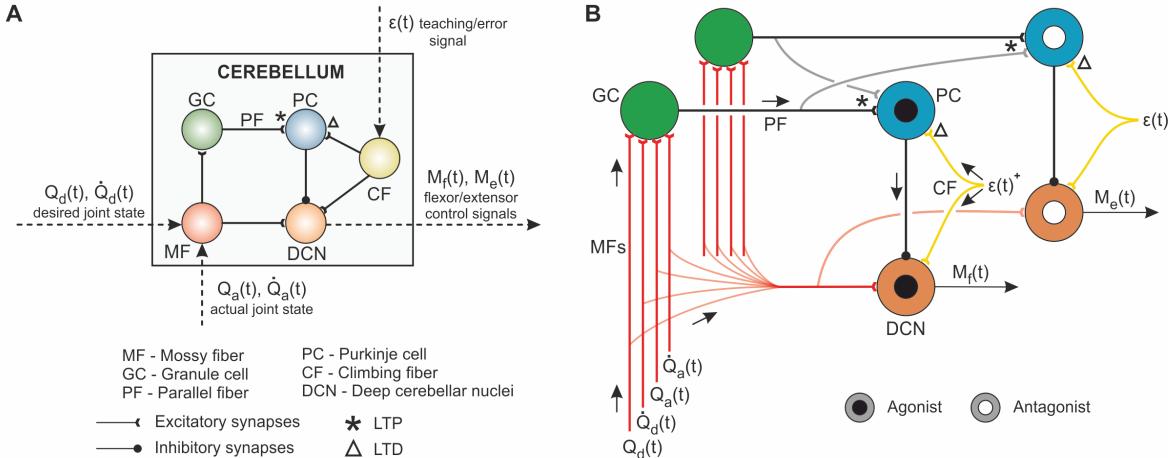
374 The cerebellar and SC models operated in a closed loop with joint and muscle feedback (Fig. 1A), in  
375 which cerebellar motor learning was assisted by fast reflex response and muscle activity regulation pro-  
376 vided by the SC. The cerebellar model received sensory input signals describing the desired motor state  
377 (desired position,  $Q_d$ , and velocity,  $\dot{Q}_d$ , per joint) and the actual motor state of the upper limb muscu-  
378 loskeletal model (actual position,  $Q_a$ , and velocity,  $\dot{Q}_a$ , per joint). The comparison of the desired and  
379 actual motor states provided the instructive signal ( $\epsilon$  per joint), also received by the cerebellum. The  
380 cerebellar output comprised a flexor-extensor (i.e., agonist-antagonist) pair of control signals ( $M_f$  and  
381  $M_e$  per joint) that were sent to the SC model, which also received direct muscle feedback (length,  $l_m$ ,  
382 and velocity,  $\dot{l}_m$ , per muscle). The SC generated the muscle excitation signals ( $u_m$  per muscle) resulting  
383 in muscle activation which finally actuated the upper limb musculoskeletal model, thus closing the loop.  
384 To contextualise the spino-cerebellar integration, we also implemented the control loop lacking the SC  
385 circuits (Fig. 1B). In this scenario, the cerebellar output signals were directly used as muscle excitation  
386 signals. The control loop included sensory and motor delays, mimicking the biological pathways. In  
387 the cerebellar sensorimotor pathway, there exists a delay ranging from about 100 to 150ms (with inter-  
388 and intraindividual variations), accounting for the time spent from the generation of a motor command  
389 until sensing back its effect [54]. Regarding the SC to muscles transmission, a delay of about 30ms  
390 has been reported for the upper limb [55, 56]. Our spino-cerebellar model included a 50ms sensorial  
391 delay affecting the reception of sensory inputs in the cerebellum; a transmission delay of 30ms from the  
392 cerebellum to the SC, and 30ms from the SC to the muscles, total motor delay of 60ms. The asymmetry  
393 between sensory and motor delay stands for the higher latency found in neuromuscular junction, elec-  
394 tromechanical and force generation delays (involved in the motor pathway), compared to the sensing,  
395 nerve conduction and synaptic delays (involved in the sensory pathway) [57].

396 The following subsections describe the different components of our spino-cerebellar control loop.  
397 The various building blocks were integrated using Robot Operating System (ROS), allowing a modular  
398 implementation.

### 399 4.1 Cerebellar model

400 We implemented a spiking neural network (SNN) replicating some cerebellar neural layers and equipped  
401 with spike-timing-dependent plasticity (STDP) to allow motor learning and adaptation. The cerebellar  
402 SNN model was adapted from previous models applied to robot control loops [18, 19]. The cerebellar  
403 SNN structure was divided in the following neural layers: i) mossy fibres (MFs), constituted the sensory  
404 input layer conveying the desired and actual motor state signals ( $Q_d$ ,  $\dot{Q}_d$ ,  $Q_a$ ,  $\dot{Q}_a$ ); ii) the spiking activity  
405 of MFs was transferred through excitatory afferents to the granule cell (GC) layer, where the sensory  
406 input information was univocally recoded; iii) the axons of the GCs, i.e., the parallel fibres (PFs), formed  
407 excitatory connections with the Purkinje cells (PCs); iv) PCs also received the excitatory action of the  
408 climbing fibres (CFs) conveying the instructive signal ( $\epsilon$ ); v) the deep cerebellar nuclei (DCN) layer  
409 received the inhibitory action from PCs and excitatory connections from both MFs and CFs. The DCN  
410 spiking activity was translated into output motor commands (flexor-extensor motor control signals,  $M_f$   
411 and  $M_e$ ) that constituted the cerebellar motor response to the sensory stimuli. Every neural layer was  
412 divided in two microcomplexes [58], being each microcomplex oriented to drive one of the two joints  
413 (shoulder or elbow). Each microcomplex at the PC-CF-DCN loop was partitioned into two regions: ag-

414 onist and antagonist. The agonist region operated the joint flexor muscles, whereas the antagonist region  
 415 operated the extensor muscles. This synergic agonist-antagonist (flexor-extensor) architecture allowed  
 416 the cerebellar model to regulate the spatiotemporal muscle activity patterns [45], key for successful mo-  
 417 tor control [59]. See Fig. 8 for a schematic representation of the cerebellar network, and Table 1 for  
 418 network topology.



**Fig. 8. Cerebellum model.** **A)** Neural layers, connections, input and output sensorimotor signals. The input signals are conveyed by the mossy fibres (MFs), which project excitatory synapses to the granule cells (GCs). These perform a recoding of the input signals, and project excitatory connections through the parallel fibres (PFs) reaching Purkinje cells (PCs). PF-PC connections are endowed with plasticity, balanced between the long-term potentiation (LTP) caused by the input PF spikes, and long-term depression derived from the climbing fibres (CFs) activity reaching PCs. CFs convey the instructive signal. Finally, PCs project inhibitory synapses towards the deep cerebellar nuclei (DCN), the output layer of the cerebellar model, which also receives a baseline excitatory action from MFs and CFs. **B)** Detailed schematic of the cerebellar connections. Each GC receives the input excitatory action from a unique combination of four MFs. Each input signal ( $Q_d$ ,  $\dot{Q}_d$ ,  $Q_a$ ,  $\dot{Q}_a$ ), is codified by ten MFs, being only one out of the ten MFs active at each time step. Hence, at each time step, four MFs will be active (one per input signal). That unique combination of four input MFs excites one single GC, allowing to perform a univocal representation of the sensory input at the granular layer. PCs then receive the excitatory action from all GCs in the cerebellar model and only one CF, allowing to relate the joint-specific instructive signal, to the global sensory state received from GCs. The PC-CF-DCN loop differentiates between agonist and antagonist regions, thus allowing simultaneous control of both flexor and extensor muscles.

**Table 1.** Cerebellar neural topology. Dashed entries stand for not applicable.

Neurons		Synapses			
Pre-synaptic	Post-synaptic	Number	Type	Initial Weight (nS)	Weight range (nS)
80 MFs	20x10 <sup>3</sup> GCs	80x10 <sup>3</sup>	AMPA	0.18	-
80 MFs	200 DCN	16x10 <sup>3</sup>	AMPA	0.3	-
20x10 <sup>3</sup> GCs	200 PCs	4000x10 <sup>3</sup>	AMPA	4.8	[0.0, 15.0]
200 PCs	200 DCN	200	GABA	1.0	-
200 CFs	200 PCs	200	AMPA	0.0	-
200 CFs	200 DCN	200	AMPA	0.5	-
200 CFs	200 DCN	200	NMDA	0.25	-

419 Consistently with the Marr-Albus-Ito theory on cerebellar motor adaptation [60, 61, 62], our cere-  
 420 bellar SNN model was equipped with synaptic plasticity at the GC-PC synapses. The synaptic weights  
 421 were adjusted by means of an STDP mechanism that correlated the sensory information (univocally  
 422 coded at GCs and transferred to PCs through PFs) and the instructive signal (conveyed to PCs by CFs).  
 423 This STDP mechanism was a balanced process of long-term potentiation (LTP) and long-term depre-  
 424 sition (LTD). Each time a PC neuron received a GC spike through a PF, that synapse was potentiated  
 425 (LTP) by a fixed amount as follows:

$$LTP\Delta W_{GC_i-PC_j}(t) = \alpha(\delta_{GCspike}(t) * dt) \quad (1)$$

426 where  $\Delta W_{GC_i-PC_j}(t)$  stands for the synaptic weight change between GC  $i$  and PC  $j$ ;  $\alpha = 0.006nS$  is the  
 427 synaptic weight increment; and  $\delta_{GCspike}(t)$  is the Dirac delta function of a GC spike, received at PCs  
 428 through PFs.

429 When the spiking activity of a CF conveyed an instructive signal to a PC neuron, the GC-PC con-  
 430 nection that was involved in that error generation was depressed (LTD) as described by:

$$LTD\Delta W_{GC_i-PC_j}(t) = \beta * \int_{-\infty}^{t_{CFspike}} k(t - t_{CFspike}) * \delta_{GCspike}(t) * dt \quad (2)$$

431 where  $\beta = -0.003nS$  stands for the synaptic weight decrement; and  $k(x)$  defines the integrative kernel  
 432 with eligibility trace correlating past sensory inputs with the present instructive signal, i.e., the amount of  
 433 LTD due to a CF spike depended on the previous GC activity received at PCs through PFs (see [18, 19]  
 434 for a further description). A well-balanced LTP-LTD process changed the PF-PC synaptic weights, thus  
 435 modifying the PCs output activity and the inhibitory action of PCs over DCN neurons, which ultimately  
 436 varied the DCN output activity. Modulating the DCN activity allowed adaptation of the output motor  
 437 response to the input stimuli. An iterative exposure to the sensory patterns defining the desired motor  
 438 task, allowed adapting the motor response for error reduction.

439 We used leaky integrate and fire (LIF) neurons (see Supporting Information (S1)) and EDLUT sim-  
 440 ulator [63] to build the cerebellar SNN model. Please see [18, 19] for a further review of the STDP  
 441 mechanism and cerebellar layers.

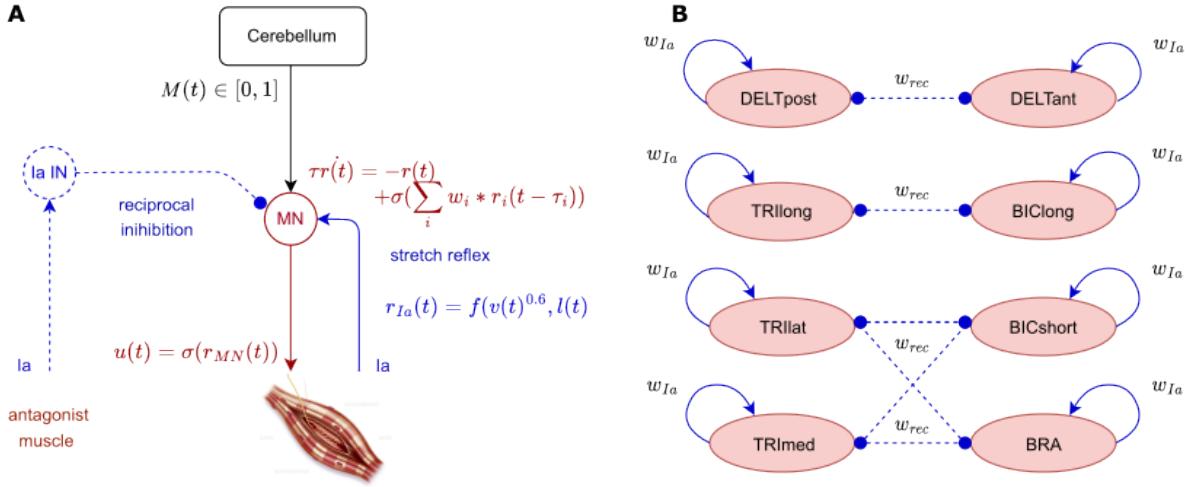
## 442 4.2 Spinal cord model

443 Our SC model integrated the descending control signals from the cerebellum and the direct muscle feed-  
 444 back (Fig. 9A). The SC model allowed fast reflex response and muscle activity regulation by means of  
 445 monosynaptic Ia stretch reflex and disynaptic reciprocal inhibition pathways between antagonist mus-  
 446 cles. The motoneuron (MN) of a given muscle received the following inputs: i) an excitatory connection  
 447 conveying the cerebellar output signal ( $M_f$  or  $M_e$ , for flexor or extensor muscle); ii) an excitatory con-  
 448 nection from the Ia afferent fibre of the muscle (i.e., stretch reflex); iii) an inhibitory connection from the  
 449 Ia interneuron (Ia IN) innervated by the Ia afferent of the antagonist muscle (i.e., reciprocal inhibition).  
 450 The antagonist relation between the muscles of the upper limb model is detailed below. The neuron  
 451 leaky integrate dynamics of the MN firing rate,  $r$ , were modelled as follows:

$$\tau\dot{r}(t) = -r(t) + \sigma(\sum_i w_i r_i(t - \tau_i)) \quad (3)$$

452 where  $\tau = 1\text{ms}$  stands for the spinal neuron activation time constant;  $\sigma(x) = \frac{1}{1+\exp(-D(x-0.5))}$  with  $D = 8$ ,  
 453 emulating the on-off behaviour of neurons;  $i$  describes the MN input signals;  $w_i$  is the synaptic weight of  
 454 the input connection, being 1 for excitatory synapses and 0.5 for the inhibitory;  $r_i$  is the input activity;  
 455 and  $\tau_i = 30\text{ms}$  stands for the stretch reflex response delay. Depending on neuron size,  $\tau$  can vary from  
 456 1 to 10ms [64], we only considered fast-response neurons as in [28]. For the upper limb,  $\tau_i$  is about

457 30ms [55, 56]. The output rates of the MNs are finally provided as muscle excitation signals to the  
 458 musculoskeletal model through a sigmoid ( $u(t) = \sigma(r(t))$ ), thus inducing movement. The dynamics of Ia  
 459 IN neurons followed the same description, with differing input activity including inhibitory connections  
 460 between antagonist Ia IN (Fig. 9B).



**Fig. 9. Spinal cord model.** **A)** The spinal cord circuits were modelled as one motoneuron per muscle, receiving an excitatory input control signal ( $M$ ) from the cerebellum, an excitatory connection from the Ia afferent fibre of the muscle (i.e., stretch reflex) and an inhibitory connection from the Ia interneuron (Ia IN) innervated by the Ia afferent of the antagonist muscle (i.e., reciprocal inhibition). We also included inhibitory connections between antagonist Ia interneurons. Each neuron is modelled with leaky integrate dynamics. **B)** Antagonist relation between the 8 upper limb muscles: all the muscles shared the same synaptic weight for the stretch reflex and reciprocal inhibition pathways, i.e., 1 for excitatory synapses and 0.5 for the inhibitory.

461 We used Prochazka's model for the Ia afferent feedback dynamics [65], with a mean firing rate of  
 462 10Hz [28, 66, 67]:

$$r_{Ia}(t) = \text{sgn}(\dot{l}_m(t)) * 4.3|\dot{l}_m(t)|_+^{0.6} + 2(l_m(t) - l_{0,m}) + 10 \quad (4)$$

463 where  $l_m$  and  $\dot{l}_m$  describes the muscle fibre length and velocity in mm and mm/s; and  $|x|_+ = \max(|x|, 0.01)$ .  
 464 The output rate,  $r_{Ia}$ , was scaled by its maximum  $r_{Ia,max}$  to get a normalised value, i.e.,  $r_{Ia} \in [0, 1]$ .  
 465

To model the SC we used FARMS Python library, developed at the BioRobotics laboratory.

### 466 4.3 Musculoskeletal upper limb model

467 We used a 2 DOF musculoskeletal upper limb model as the front-end body to be controlled. The model,  
 468 adapted from [68], included two flexion-extension joints: shoulder and elbow. The model was actuated  
 469 by 8 Hill-based muscles [69], with the following joint distribution: i) for the shoulder, flexion was  
 470 carried by the deltoid anterior and posterior (DELTant, DELTpost) and the biceps long (BIClong), and  
 471 extension was conducted by the triceps long (TRIlong); ii) for the elbow, flexion was provided by the  
 472 biceps long and short (BICshort) and the brachialis (BRA), whilst extension was allowed by the triceps  
 473 long, lateral and medial (TRIlat, TRImed). Note that BIClong and TRIlong were bi-articular muscles, as  
 474 they actuated both joints. The antagonist relation between muscles is depicted in Fig. 9B. The Hill-based  
 475 muscle dynamics were the following:

$$\begin{cases} f_m = (a * f_{lv}(l_m, \dot{l}_m) + f_p(l_m)) * \cos\theta \\ \frac{da}{dt} = \frac{u-a}{\tau(u, A)} \end{cases} \quad (5)$$

476 with  $f_m$  the muscle force,  $f_{lv}$  a combination of the force-length and force-velocity curves,  $f_p$  the passive  
477 force-length curve,  $\theta$  the pennation angle,  $a$  the muscle activation (i.e., the concentration of calcium ions  
478 within the muscle), and  $u$  the muscle excitation (i.e., the firing of the MN) [69]. We used OpenSim  
479 physics engine to simulate the muscle and skeleton dynamics [70]. To allow using kinematics and EMG  
480 from lab recordings, an OpenSim upper limb model was scaled to match the morphology of each lab  
481 participant. This scaling process was achieved using OpenPifPaf Human Pose Estimation algorithm [71]  
482 during the static period and OpenSim scaling tool.

#### 483 4.4 Benchmarking with various motor tasks

484 We used a set of different motor tasks to be performed by the spino-cerebellar and cerebellar models,  
485 differentiating between two scenarios: lab recorded and lab designed motor tasks.

486 For the lab recorded scenario, we used kinematics and EMG recordings from healthy participants  
487 performing different arm movements. Experiments were approved by the CER-VD under the license  
488 number 2017-02112 and performed in accordance with the Declaration of Helsinki in NeuroRestore  
489 laboratory at Lausanne CHUV. Two participants, P1 and P2, were asked to perform planar reaching  
490 movements (flexion-extension) and continuous circular movements, both movements performed in the  
491 vertical plane and at various speeds (self-selected speeds). For flexion-extension movements both shoul-  
492 der and elbow moved in the same direction, whilst during the continuous circular movements the joints  
493 moved in opposite directions. Thus, our benchmark includes interaction torques both assisting and re-  
494 sisting the movement. The recorded kinematics (i.e., joint position and velocity) constituted the desired  
495 motor state ( $Q_d, \dot{Q}_d$ ) used as the control loop sensory input, whilst the EMG recordings supported model  
496 validation in muscle space. For each recorded motor task we ran the experimental setup with both the  
497 spino-cerebellar and cerebellar models, using an OpenSim upper limb model scaled to match the partic-  
498 ipant's morphology. We then compared the models' experimental performance to the lab recordings in  
499 both joint and muscle spaces.

500 P1 and P2 movements were recorded using an RGB-D camera, and we used OpenPifPaf human pose  
501 estimation algorithm [71] to extract the 2D positions of the participant's anatomical joints at a frame rate  
502 of 25fps. Then 3D pose was deduced from the 2D pose, camera intrinsic, and depth information after  
503 accounting for distortion. The occlusions were removed using specially designed filters that ensure co-  
504 herence in joint anatomy and time. We scaled an OpenSim upper limb musculoskeletal model to match  
505 the participant's morphology, and ran inverse kinematics (IK) over the body segment kinematics, thus  
506 allowing the extraction of joint position and velocity from the participant's motion. P1 generally per-  
507 formed fast movements, and the kinematics recordings of his fast circular movements were too noisy to  
508 extract joint position, thus we excluded this scenario from our analysis. For muscle activity, we recorded  
509 EMG using Delsys system and Trigno Avanti and Trigno Quattro sensors with a acquisition frequency  
510 of 1259.3Hz. We aligned the EMG with the kinematics signals thanks to a trigger inducing a pulse in an  
511 additional EMG channel and lightning a led in the camera range. We then computed the EMG envelopes  
512 to compare with our models muscle activation signals. For each recorded signal, we removed the mean  
513 and rectified the signal, which was then filtered using a low pass Butterworth filter with a 5Hz cutoff  
514 frequency. We applied the same processing steps to the maximal voluntary contraction (MVC) signal  
515 of each muscle (recorded at the beginning of the session), and used the maximal value of the processed  
516 MVC to normalise the corresponding muscle processed EMG signal.

517 For the lab designed scenario, we implemented a set of flexion-extension movements with different  
518 bell-shaped joint velocity profiles, characteristic of multi-joint arm reaching movements [40]. We then  
519 used the joint kinematics ( $Q_d, \dot{Q}_d$ ) as the desired motor state to be performed by the spino-cerebellar  
520 and cerebellar models (please see Supporting Information for a depiction of the bell-shaped trajectories  
521 (S10 to S12 Fig.)). We broadened the benchmark by adding a perturbation study using these bell-shaped  
522 trajectories. After cerebellar learning consolidation, we applied a set of motor perturbations whilst the

523 trajectories were being performed: 50N for 30ms, applied to the hand in different directions and at different points along the flexion-extension movement. Each perturbation type was applied to 10 separate trials to get an average response, leaving 3 non-perturbed trials in between perturbed trials so that the model returned to its unperturbed state. Note that cerebellar learning was disabled during the perturbation study, to avoid cerebellar adaptation to the external forces and focus on SC response.

528 Using this motor benchmark, and comparing the performance of the spino-cerebellar and cerebellar models, we could evaluate the cerebellum and spinal cord integration in terms of: muscle activity, motor adaptation and joint space performance, synaptic adaptation, and response to motor perturbations, for various trajectories with different initial and final positions and speeds. Please see Supporting Information for a representation of the motor tasks joint kinematics (S1 to S12 Fig.).

## 533 4.5 Cerebellar instructive signal

534 The cerebellar instructive signal  $\epsilon(t)$  was obtained as the mismatch between the desired and actual joint state, combining in a single value per joint both position and velocity errors as follows:

$$\epsilon(t) = K_p[Q_d(t) - Q_a(t)] + K_v[\dot{Q}_d(t) - \dot{Q}_a(t)] \quad (6)$$

536 where  $K_p = 3$  and  $K_v = 1$  are the position and velocity error gain, respectively. The trajectory error signal in joint space can be derived from the proprioceptive and sensory information conveyed by the 537 spino-cerebellar tract from the muscle spindles (muscle length) and Golgi tendon organs (muscle force) 538 to the cerebellum [72].

## 540 4.6 Performance metrics

### 541 4.6.1 Measuring kinematics performance

542 To evaluate the kinematic performance of the spino-cerebellar and cerebellar models, we defined a set 543 of metrics based on the mean absolute error (MAE) between the desired ( $Q_d, \dot{Q}_d$ ) and actual ( $Q_a, \dot{Q}_a$ ) 544 motor state of the arm:

545

$$\begin{cases} MAE_{pos}(t) = \frac{1}{N} \sum_{j=1}^N |Q_{d,j}(t) - Q_{a,j}(t)| \\ MAE_{vel}(t) = \frac{1}{N} \sum_{j=1}^N |\dot{Q}_{d,j}(t) - \dot{Q}_{a,j}(t)| \end{cases} \quad (7)$$

546

547 where  $N$  stands for the number of joints (2), and  $j$  for the joint index. We considered the position and 548 velocity MAE of each motor task trial to assess the performance accuracy:

549

$$\begin{cases} MAE_{pos} = \frac{1}{T} \sum_{t=0}^T MAE_{pos}(t) \\ MAE_{vel} = \frac{1}{T} \sum_{t=0}^T MAE_{vel}(t) \end{cases} \quad (8)$$

550 where  $T$  stands for the motor task period. We finally averaged these values over 200 trials and compared 551 the final performance of the two models with the final mean  $MAE_{pos}$  and  $MAE_{vel}$  ( $\bar{MAE}_{pos,f}$ ,  $\bar{MAE}_{vel,f}$ ). 552 We also computed the standard deviation ( $std$ ) and the T-test p-value between the two models' results 553 with a T-test for the means of two independent samples of values.

### 554 4.6.2 Measuring learning performance

555 To measure the learning convergence (i.e., number of trials required to reach a stable trajectory tracking), we used control chart metrics [39]. Throughout the  $MAE_{pos}$  and  $MAE_{vel}$  curve of each motor task 556 (all performed for a total of 2000 learning trials) we computed the mean ( $\mu$ ) and standard deviation ( $\sigma$ )

558 using a sample size of 200 trials, which provided the following performance stability limits:

559

$$\begin{cases} L1 = \bar{MAE}_x \in [\mu - \sigma, \mu + \sigma] \\ L2 = \bar{MAE}_x \in [\mu - 3\sigma, \mu - 2\sigma] \cup [\mu + 2\sigma, \mu + 3\sigma] \\ L3 = \bar{MAE}_x \in ] -\infty, \mu - 3\sigma] \cup [\mu + 3\sigma, +\infty[ \end{cases} \quad (9)$$

560

561 We then checked the percentage of those 200 trials within each limit. As the limits were defined by  
 562 the *std*, we also checked that the *std* value was below 0.012rad for position and 0.055rad/s for velocity.  
 563 Thus, at trial  $x$ , the behaviour was stable if the percentage of the 200 previous trials within each limit  
 564 fulfilled the metrics defined in Table 2, and the *std* was equal or below the aforementioned values.  
 565 By comparing the learning convergence of the spino-cerebellar and cerebellar models (i.e., number of  
 566 trials required to reach a stable performance) we quantified the effect of the SC in the cerebellar motor  
 567 adaptation process.

568 Additionally, we assessed the learning speed of the two models by considering the number of trials  
 569 required to reach a target  $MAE_{pos}$  of 0.1rad and a target  $MAE_{vel}$  of 0.5rad/s. We defined the learning  
 570 speed metric as 1 over this number of trials ( $N_{trials}^{-1}$ ).

571 Thus, we evaluated how long it took for the performance to stabilise (learning convergence) and how  
 572 fast the performance approached accurate tracking (learning velocity).

**Table 2.**  $MAE$  convergence criteria from control chart

Stability limit	$MAE_{pos}$	$MAE_{vel}$
$L1 = MAE_x \in [\mu - \sigma, \mu + \sigma]$	$\geq 78\%$	$\geq 73\%$
$L2 = MAE_x \in [\mu - 3\sigma, \mu - 2\sigma] \cup [\mu + 2\sigma, \mu + 3\sigma]$	$\leq 3\%$	$\leq 3\%$
$L3 = MAE_x \in ] -\infty, \mu - 3\sigma] \cup [\mu + 3\sigma, +\infty[$	$\leq 2\%$	$\leq 2\%$
$\sigma$	$\leq 0.012$	$\leq 0.055$

#### 573 4.6.3 Measuring cerebellar synaptic adaptation

574 To study the effect of the SC in cerebellar synaptic adaptation we quantified the difference in the synaptic  
 575 weight distribution at GC-PC connections between the spino-cerebellar and cerebellar models. Each PC  
 576 was innervated by all GCs in the model; i.e., a GC formed an excitatory synapse with each PC (total  
 577 number of GCs in the model  $i = 20000$ ; total number of PCs in the model  $j = 200$ ). We stored the  
 578 synaptic weight of all GC-PC synapses in a matrix of size  $ixj$ :

579

$$W = \begin{bmatrix} w_{1,1} & w_{1,2} & \dots & w_{1,j} \\ w_{2,1} & w_{2,2} & \dots & w_{2,j} \\ \dots & & & \\ w_{i,1} & w_{i,2} & \dots & w_{i,j} \end{bmatrix} \quad (10)$$

580

581 where  $w_{x,y}$  is the synaptic weight of the synapse between GC  $x$  and PC  $y$ .

582 We then represented the normalised weights stored in  $W$ , using  $i$  as the y-axis and  $j$  as the x-axis,  
 583 providing a visual representation of the synaptic weight distribution (Fig. 5). To analyse the differences  
 584 between the synaptic patterns that were formed in each model, we applied to the images Shannon's  
 585 entropy from [73], thus providing a quantitative measure of the complexity of the synaptic distribution.  
 586 The higher the entropy, the more heterogeneous the synaptic weights; i.e., more specialised GC-PC  
 587 connections were formed.

588 **4.6.4 Measuring robustness against perturbations**

589 To assess the robustness against perturbations, for each applied perturbation type we computed the mean  
 590 MAE deviation from the no-perturbation scenario over the 10 perturbed trials as follow:

591

$$\begin{cases} \Delta \bar{MAE}_{pos} = \frac{1}{10} \sum_{i=1}^{10} |MAE_{pos,i} - \bar{MAE}_{pos,f}| \\ \Delta \bar{MAE}_{vel} = \frac{1}{10} \sum_{i=1}^{10} |MAE_{vel,i} - \bar{MAE}_{vel,f}| \end{cases} \quad (11)$$

592

593 where  $MAE_{x,i}$  is the MAE resulting from the  $i^{th}$  perturbed trial and  $\bar{MAE}_{x,f}$  the final MAE for the  
 594 corresponding no-perturbation scenario. We also computed the *std* and T-test p-value between the spinocerebellar and cerebellar model results as above.

596 **4.6.5 Measuring muscle space performance**

597 We also evaluated performance in the muscle space using the lab recorded benchmark. Activation signals  
 598 from models are commonly compared to EMG envelopes, but such comparisons are generally difficult  
 599 to achieve due to scaling issues that hinder a direct analogy between the model and the real muscle  
 600 dynamics. To overcome this issue, we followed a more comprehensive approach by computing the correlation  
 601 between activation signals and EMG envelopes. We computed the EMG envelopes by rectifying  
 602 and low pass filtering the signals using a 5th order Butterworth filter with a cut-off frequency of 5Hz.  
 603 We also recorded the maximal velocity contraction (MVC) signals for each participant, we processed  
 604 them the same way and finally normalised the EMG signals by the maximum of the muscle MVC signal.  
 605 Then, for each movement type, we considered only the main activated muscles with clear activation patterns  
 606 during the recordings, i.e., DELTant, BIClong, BICshort, TRIlat and BRA for P1 flexion-extension  
 607 movements; DELTant, DELTpost, BIClong, TRIlat and BRA for P1 circular movements; DELTant, BI-  
 608 Clong, TRIlong and TRIlat for P2 flexion-extension movements; and DELTant, DELTpost, and BRA  
 609 for P2 circular movements. Thus, there is inter-participant variability in muscle patterns. A figure per  
 610 participant displays all the recorded EMG and highlights these main patterns in Supporting Information  
 611 (S13 and S14 Fig.). It is worth noting that P1 performed smaller shoulder flexion with larger elbow  
 612 flexion during flexion-extension movements compared to P2, corresponding to additional BICshort and  
 613 BRA activation without TRIlong activation. In our experimental setup, we computed the maximal correlation  
 614 around lag 0 (on a window of one-fourth of the movement duration) for the 200 trials prior  
 615 to reaching the learning convergence metric and extracted the mean, *std* and T-test p-value between the  
 616 spino-cerebellar and cerebellar model results. Regarding the lab recorded data, we did not consider those  
 617 muscles that presented low and noisy EMG signals; however, those muscles were actually activated in  
 618 our experimental simulations. Our musculoskeletal model indeed contained only 8 muscles, so that such  
 619 overactivation may reproduce other non-modelled muscle recruitment.

620 To study our cocontraction hypothesis, we computed and compared the cocontraction index (CCI)  
 621 for each joint. From lab recordings or experimental simulations, we considered the average of EMG  
 622 envelop or muscle activation signals, respectively, within each agonist and antagonist muscle group  
 623 (i.e., DELTant and BIClong for shoulder flexor muscles; DELTpost and TRIlong for shoulder extensors;  
 624 BIClong, BICshort and BRA for elbow flexors; TRIlong and TRIlat for elbow extensors) and the CCI  
 625 defined by [74] and assessed by [75]:

$$CCI_j(t) = \frac{\bar{EMG}_{j,l}(t)}{\bar{EMG}_{j,h}(t)} (\bar{EMG}_{j,l}(t) + \bar{EMG}_{j,h}(t)) \quad (12)$$

626 where  $\bar{EMG}_{j,l}$  is the level of activity in the less active muscle group and  $\bar{EMG}_{j,h}$  the level of activity  
 627 in the most active muscle group for each joint. As this index is also sensitive to scaling, we computed  
 628 the maximal correlation around lag 0 (on a window of one-fourth of the movement duration) for the

629 first 200 trials reaching our learning convergence metric (see Methods) and extracted the mean, *std* and  
630 T-test p-value between the spino-cerebellar and cerebellar model results. We also computed the mean  
631 joint CCI over each trajectory. A similar trend as that seen for the *MAE<sub>vel</sub>* was observed. We studied  
632 this potential relationship through a linear regression over all P1 and P2 trajectories.

## 633 **Data availability**

634 For reproducibility and comparative purposes, the source code is available on Zenodo at <https://doi.org/10.5281/zenodo.7701436>

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## 666 Ethics

667 Experiments were approved by the CER-VD under the license number 2017-02112 and performed in  
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