

1 **Higher-order interactions shape microbial interactions as microbial
2 community complexity increases**

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10 **ABSTRACT**

11 Non-pairwise interactions, or higher-order interactions (HOIs), in microbial communities have
12 been claimed to explain the emergent features in microbiomes. Yet, the re-organization of
13 microbial interactions between pairwise cultures and larger communities remains largely
14 unexplored from a molecular perspective but is central to our understanding and further
15 manipulation of microbial communities. Here, we used a bottom-up approach to investigate
16 microbial interaction mechanisms from pairwise cultures up to 4-species communities from a
17 simple microbiome (*Hafnia alvei*, *Geotrichum candidum*, *Pencillium camemberti* and *Escherichia*
18 *coli*). Specifically, we characterized the interaction landscape for each species combination
19 involving *E. coli* by identifying *E. coli*'s interaction-associated genes using an RB-TnSeq-based
20 interaction assay. We observed a deep reorganization of the interaction-associated genes, with
21 very few 2-species interactions conserved all the way up to a 4-species community and the
22 emergence of multiple HOIs. We further used a quantitative genetics strategy to decipher how 2-
23 species interactions were quantitatively conserved in higher community compositions. Epistasis-
24 based analysis revealed that, of the interactions that are conserved at all levels of complexity,
25 82% follow an additive pattern. Altogether, we demonstrate the complex architecture of microbial

26 interactions even within a simple microbiome, and provide a mechanistic and molecular
27 explanation of HOIs.

28 **Introduction**

29 Microbiomes are multidimensional systems containing up to thousands of interacting species. In
30 part due to this complexity, a common strategy to investigate their biology has been to use bottom-
31 up or reductionist approaches. Using *in vitro* microbial communities or monocultures, the features
32 of microbial communities are measured in low-dimensional settings, with the underlying objective
33 to understand whether high-dimension phenotypes can be predicted from lower-level
34 observations. The lack of predictability of microbial community features from monoculture
35 observations has demonstrated the critical importance of microbial interactions in shaping
36 microbial communities. For instance, community assembly^{1,2}, community function³, community
37 resistance to invasion⁴ or its effects on its host⁵ are highly different from the simple combination
38 of individual species effects. Some of these studies have also shown that, while 2-species, or
39 pairwise culture, observations could partially predict what happens in higher communities^{1,2,6},
40 context-specific phenotypes emerge as the microbial community becomes more complex, limiting
41 the use of pairwise information to obtain a descriptive picture of larger communities. For instance,
42 the function (amylolytic activity) of a soil-associated microbial community of 6 species has been
43 shown to differ from the simple linear combination (*i.e.* the addition) of the observed function of
44 pairwise cultures³. Similarly, 13 to 43% of measured *Drosophila melanogaster* traits (lifespan,
45 reproduction and development) in flies carrying a microbiome of 5 species were not predictable
46 from the associated traits from flies inoculated with pairwise combinations of the same 5 species⁵.
47 In the zebrafish gut microbiome, while strong negative pairwise interactions were measured, the
48 assembly of a more complex microbiome of 5 species strikingly diverged from any assembly
49 prediction based on pairwise interactions, and all 5 species actually co-occur in the final
50 microbiome⁷.

51 Reorganization of the interaction profile with varying community complexity and the presence of
52 higher-order interactions (HOIs) are the most likely explanation for the lack of predictability of
53 complex community phenotypes from pairwise observations. In ecology, HOIs are described as
54 key to stabilizing communities and promoting biodiversity in biological ecosystems^{8–10}. They are
55 commonly described as the modification of pairwise interactions when another species is
56 introduced, or any interaction that cannot be described by a pairwise model^{11,12}. For instance,
57 while the bacterium *Escherichia coli* can successfully invade cultures of *Chlamydomonas*
58 *reinhardtii* as well as cultures of *Tetrahymena thermophila*, it is unable to invade a coculture of
59 the alga and the ciliate. This is due to *C. reinhardtii* inhibition of *E. coli* aggregation specifically in
60 the presence of *T. thermophila*, which renders the bacterium vulnerable to predation¹³. Changes
61 in microbial interactions and HOIs are undoubtedly a significant feature of microbiome ecology
62 and functioning. Thus, investigating HOIs and deciphering how microbial interactions are
63 rearranged when microbial systems increase in complexity are essential to our understanding of
64 microbiomes and our ability to manipulate them.

65 In this work, we investigate how interactions are reorganized when the complexity of a microbial
66 community increases from two to four species. We use a simplified cheese rind microbiome
67 composed of the two gamma-proteobacteria *E. coli* and *Hafnia alvei*, the yeast *Geotrichum*
68 *candidum* and the filamentous fungus *Penicillium camemberti*. Our previous work comparing the
69 pairwise interaction patterns of this model microbiome to the interaction pattern in the full
70 community highlighted the prevalence of HOIs and the lack of conservation of pairwise
71 interactions¹⁴. However, we couldn't precisely resolve the origin of these HOIs or specific rules
72 underlying the emergence of these HOIs. For instance, we couldn't determine whether 2-species
73 interactions are alleviated by the introduction of a specific species or by the introduction of all the
74 other species. Similarly, we couldn't conclude whether community-specific interactions are
75 actually specific to the community or whether they arise at an intermediate level and
76 are maintained in the whole community. Relying on the ability to deconstruct and reconstruct this

77 model system and on the RBTnSeq-based interaction assay we have previously optimized to
78 compare gene fitness values across multiple conditions¹⁵, we aim to identify quantitative changes
79 in gene fitness values for *E. coli* in different interactive conditions to identify the genetic basis of
80 interactions at every level of community complexity.

81 Comparing interaction-associated genes across conditions, we can identify pairwise interaction-
82 associated genes that are also observed at higher levels of complexity as well as genes
83 associated with HOIs. Here, HOIs are defined as interaction-associated genes that emerge in the
84 3 or 4 species cultures and 2-species interaction-associated genes that are no longer observed
85 in the 3 or 4 species cultures. Analysis of the genes associated with HOIs and their functions
86 allowed us to further characterize the deep reorganization of the interaction landscape and
87 highlights that it is mostly associated with the reprogramming of metabolic interactions and the
88 introduction of a fungal partner. We further focus on the genetic basis of 2-species interactions
89 that are conserved in higher levels of complexity to elucidate principles behind interaction
90 conservation. We use an epistasis and quantitative genomics approach^{16,17} to understand
91 whether interactions that are conserved follow a linear, or additive, pattern. The evaluation of
92 interaction effects as quantitative traits allows us to define another form of HOIs as cases in which
93 there is a lack of additivity in interactions that are conserved from simpler to more complex
94 community composition. This form of HOIs is consistent with a more quantitative definition of
95 HOIs, highly similar to the definition of epistasis in population genetics¹⁸, that identify HOIs (or
96 epistasis) as any deviation, for a given quantitative trait, from the prediction of a linear model
97 where only pairwise interactions are included. Carrying out this analysis, we observe that 82% of
98 the conserved interactions follow an additive pattern of conservation from 2-species to 4-species,
99 and that 18% of the conserved 2-species interaction is associated with non-linear models of
100 conservation.

101 Overall, our work provides a unique illustration of the highly complex reorganization of interaction
102 mechanisms when microbial community complexity changes. This provides a mechanistic

103 explanation of HOIs in microbial communities that is essential for the further global understanding
104 of microbial communities.

105

106 **Results**

107

108 **Sets of interaction-associated genes change across interactive conditions**

109 To investigate how microbial interactions are reorganized in a microbial community with
110 increasing complexity, we reconstructed *in vitro* a modified bloomy rind cheese-associated
111 microbiome on Cheese Curd Agar plates (CCA plates) as described in our previous work¹⁴. The
112 original community is composed of the gamma-proteobacterium *H. alvei*, the yeast *G. candidum*
113 and the mold *P. camemberti*. Using a barcoded transposon library of the model bacterium *E. coli*
114 as a probe to identify interactions, we investigated microbial interactions in 2-species cultures (*E.*
115 *coli* + 1 community member), in 3-species cultures (*E. coli* + 2 community members) and in 4-
116 species cultures (or whole community: *E. coli* + 3 community members) (Figure 1A).
117 Quantification of species' final CFUs after 3 days of growth highlighted consistent growth for *H.*
118 *alvei* and *G. candidum* independent of the culture condition and slightly reduced growth for *E. coli*
119 in interactive conditions compared to growth alone except for following growth with *P. camemberti*
120 (Supplementary Figure 1). Although we were unable to quantify spores of *P. camemberti* after
121 three days, growth of *P. camemberti* was visually evident in all of the expected samples.

122 Previously, we developed an assay and a pipeline to identify microbial genes associated with
123 interactions by adapting the original RB-TnSeq approach¹⁹ to allow for consistent implementation
124 of biological replicates as well as for direct quantitative comparison of fitness values between
125 different culture conditions¹⁵. More specifically, the original RB-TnSeq assay relies on the use of
126 a pooled library of randomly barcoded transposon mutants of a given microorganism (RB-TnSeq
127 library)¹⁹. Measuring the variation of the abundance of each transposon mutant before and after
128 growth, the pipeline allows the calculation of a fitness value for each mutant. A negative fitness

129 indicates decreased growth of the mutant relative to a wild type strain, whereas a positive fitness
130 value indicates increased growth in the studied condition. Then, to identify genes associated with
131 interactions, we measure and compare gene fitness across the different studied conditions, for
132 example, comparing growth alone to growth in the presence of another species. Then, any gene
133 whose fitness values significantly change between such conditions is identified as an interaction-
134 associated gene.

135 In this work, we used the *E. coli* RBTnSeq Keio_ML9 library¹⁹ and grew it for 3 days alone or in
136 the seven different interactive conditions studied here (Figure 1A). For each interactive condition,
137 we calculated the Interaction Fitness Effect (IFE) for 3699 *E. coli* genes as the difference between
138 the gene fitness in the studied interactive condition and the gene fitness in growth alone
139 (Supplementary Data 1). To identify genes associated with interactions, we then tested for all the
140 IFEs that are significantly different from 0 (adjusted p-value ≤ 0.1 ; two-sided t-test and Benjamini-
141 Hochberg correction for multiple comparison²⁰). Negative IFE occurs when gene fitness
142 decreases in the interactive condition, and positive IFE occurs when gene fitness improves in the
143 interactive condition. Here, we identified between 6 (with *P. camemberti*) and 71 (with *H. alvei* +
144 *P. camemberti*) significant IFEs per condition (Figure 1B). Both negative IFEs and positive IFEs
145 were found in each interactive condition except for the 2-species culture with *P. camemberti*,
146 where only negative interactions were identified. A total of 330 significant IFEs associated with
147 218 unique genes were identified (as the same gene can have a significant IFE in multiple
148 conditions) including 125 genes associated with negative IFE and 120 genes associated with
149 positive IFE (Supplementary Figures 2 and 3).

150
151 To gain insight into the interaction mechanisms among microbes, we next analyzed the functions
152 associated with IFEs. Here, the vast majority of genes associated with significant IFEs are part of
153 an interaction network, highlighting the presence of genes with connected functions and from
154 similar pathways (Figure 1C). A significant fraction of the genes associated with a negative IFE

155 are part of amino acid biosynthesis and transport (17% - Figure 1C and Supplementary Figures
156 2 and 4), and more specifically with histidine, tryptophan and arginine biosynthesis. This points to
157 competition for these nutrients between *E. coli* and the other species. Another large set of genes
158 is related to nucleotide metabolism and transport (14% - Figure 1C and Supplementary Figures
159 2 and 5), highlighting competitive interactions for nucleotides and/or their precursors. The majority
160 of these genes relate to purine nucleotides and more specifically to the initial steps of their *de*
161 *novo* biosynthesis associated with the biosynthesis of 5-aminoimidazole monophosphate (IMP)
162 ribonucleotide. Of the genes with a positive IFE, 15% are related to amino acid biosynthesis and
163 transport (Figure 1C and Supplementary Figures 3 and 4), suggesting cross feeding of amino
164 acids between *E. coli* and the other species. More specifically, this includes phosphoserine,
165 serine, homoserine, threonine, proline and arginine. The presence of amino acid biosynthetic
166 genes among both negative and positive IFEs indicate that trophic interactions (competition
167 versus cross-feeding) depend on the type of amino-acid and/or the species interacting with *E.*
168 *coli*. For both negative and positive IFEs, numerous genes were annotated as transcriptional
169 regulators (Figure 1C and Supplementary Figures 2 and 3) emphasizing the importance of
170 transcriptional reprogramming in response to interactions. These transcriptional regulators
171 include metabolism regulators as well as regulators of growth, cell cycle and response to stress.
172 Finally, these interaction-associated genes and these interaction mechanisms are consistent with
173 previous findings in this microbiome¹⁴ as well as in a study of bacterial-fungal interactions
174 involving *E. coli* and cheese rind isolated fungal species¹⁵.

175

176 **Introduction of a third-interacting species deeply reshapes microbial interactions**

177 The differences in the number and sign of significant IFEs observed among the different
178 interactive conditions, with different numbers of interaction species, suggest that the number and
179 type of interacting partners influence interaction mechanisms. To characterize how the
180 interactions are reorganized with community complexity, we then investigated if and how the

181 genetic basis of interactions changes when the number of interacting partners increases by
182 comparing the genes associated with significant IFE in 2-species cultures, in 3-species cultures
183 and then in 4-species cultures.

184 First, we have identified 104 IFEs associated with 98 genes in 2-species cultures as well as 168
185 IFEs associated with 136 unique genes in 3-species conditions (Supplementary Figure 6 and
186 Supplementary Data 2). Comparing these gene sets, we can identify how the interaction-
187 associated genes change when a third-species is added to a 2-species culture. We identified 45
188 2-species interaction-associated genes maintained in at least one 3-species condition
189 (maintained interaction-genes), 55 2-species interaction-associated genes no longer associated
190 with interaction in any 3-species condition (dropped interaction-genes) and 100 3-species
191 interaction-associated that aren't associated with any 2-species interaction-associated genes
192 (emergent interaction-genes) (Figure 2A, Supplementary Figure 6 and Supplementary Data 3).
193 Both dropped and emerging interaction-associated genes represent 3-species HOIs; the third
194 species either removes an existing interaction or brings about a new one.

195 We further carried out functional analysis of maintained, dropped and emerging interaction-genes
196 to elucidate whether maintained and HOIs interaction-genes would be associated with specific
197 functions and thus interaction mechanisms (Figure 2B). For each set of genes, we calculated the
198 fraction of genes of that set associated with a given COG ontology category. Metabolism and
199 transport is the most observed COG group (Figure 2B - teal dots). For maintained interaction-
200 genes, this indicates that some trophic interactions can be maintained from 2-species to 3-species
201 conditions. For instance, serine biosynthetic genes *serA*, *serB* and *serC* as well as threonine
202 biosynthetic genes *thrA*, *thrB* and *thrC* are associated with positive IFEs in the 2-species condition
203 with *G. candidum* as well as in the 3-species conditions involving *G. candidum* (Supplementary
204 Figure 4). This suggests that, (i) *G. candidum* facilitates serine and threonine cross feeding and
205 (ii) this cross-feeding is still observed when another species is introduced. However, metabolism-
206 related genes identified among the dropped and emerging interaction-agenes indicate that many

207 trophic interactions are also rearranged through HOIs. Genes associated with lactate catabolism
208 (*lldP* and *lldD*) and lactate metabolism regulation (*lldR*) have a negative IFE in the 2-species
209 culture with *H. alvei*, suggesting competition for lactate between *E. coli* and *H. alvei*. Yet, these
210 genes are no longer associated with a significant IFE when at least another partner is introduced
211 (Supplementary Figure 7). Histidine biosynthesis genes *hisA*, *hisB*, *hisD*, *hisH* and *hisI* have a
212 negative IFE in the 2-species culture with *H. alvei* and sometimes in the 3 species culture with *H.*
213 *alvei* + *P. camemberti*. However, the negative IFE is alleviated whenever *G. candidum* is present,
214 suggesting that potential competition for histidine between *E. coli* and *H. alvei* is alleviated by this
215 fungal species (Supplementary Figure 4). Also, genes related to the COG section “Information
216 storage and processing” are mostly found among HOIs genes, suggesting a fine-tuning of specific
217 cellular activity depending on the interacting condition. For instance, we identified many
218 transcriptional regulators of central metabolism among the dropped genes (*rbsR* and *lldR*) and
219 the emerging genes (*purR*, *puuR*, *gcvR* and *mngR*), highlighting again the reorganization of
220 trophic interactions associated with HOIs. Also, many transcriptional regulators broadly
221 associated with growth control, cell cycle and response to stress were found among the emerging
222 interaction-genes with 3-species (*hyfR*, *chpS*, *sdiA*, *slyA* and *rssB*), underlining a noticeable
223 modification of *E. coli*’s growth environment with 3-species compare to with 2-species.
224 Finally, we further aimed to understand whether HOIs are associated with the introduction of any
225 specific species (Figure 2C and Supplementary Figure 8). We observe that interaction-associated
226 genes with *H. alvei* are more likely to be dropped, as 65% of them are alleviated by the
227 introduction of a fungal species (Figure 2C). This can be seen, for instance, with the
228 reorganization of *E. coli* and *H. alvei* trophic interactions following the introduction of *G. candidum*
229 (alleviation of lactate and histine competition for instance). Also, we observe that 76% of the
230 interactions in the 3-species cultures with *H. alvei* + *P. camemberti* and 65% in the 3-species
231 culture with *H. alvei* + *G. candidum* are emerging genes (compared to 38% of emerging
232 interaction-associated genes in the 3-species condition with *G. candidum* + *P. camemberti*)

233 (Figure 2C). For the 3-species with *H. alvei* + *P. camemberti*, they include for instance the genes
234 associated with purine *de novo* biosynthesis (*purR*, *purF*, *purN*, *purE*, *purC*) and the genes
235 associated with pyrimidine *de novo* biosynthesis (*pyrD*, *pyrF*, *pyrC*, *carA* and *ulaD*), suggesting
236 important trophic HOIs. For the 3-species with *H. alvei* + *G. candidum*, emerging interaction genes
237 include for example the transcriptional regulators *chpS*, *sdiA* and *slyA*, indicating the presence of
238 a stress inducing environment. Together, these observations suggest that the introduction of a
239 fungal partner may introduce multiple 3-species HOIs by both canceling existing interactions and
240 introducing new ones.

241
242 **HOIs are prevalent in a 4-species community**

243 To further decipher whether microbial interactions continue to change with increasing community
244 complexity, we investigated the changes in the genetic basis of interactions going from 3-species
245 to 4-species experiments. We identified 58 interaction-genes in the 4-species condition (*E. coli*
246 with *H. alvei* + *G. candidum* + *P. camemberti*), compared with 145 genes associated with
247 interactions in any 3-species conditions. Comparing these two sets of genes we identify: 26 3-
248 species interaction-genes that are maintained in the 4-species condition (including 16 directly
249 from 2-species interactions), 115 3-species interaction-genes that are no longer associated with
250 interactions in the 4-species condition (dropped interaction-genes) and 32 interaction-genes that
251 are observed solely in the 4-species condition (emerging interaction-genes) (Figure 3A,
252 Supplementary Figure 6 and Supplementary Data 3). Both dropped and emerging interaction-
253 genes represent 4-species HOIs. Here, HOIs are remarkably abundant when introducing a single
254 new species and moving up from 3-species interactions to 4-species interactions. Functional
255 analysis of maintained and HOI genes reveals the presence of many metabolism related genes
256 in every gene set (Figure 3), suggesting that some trophic interactions can be maintained from 3-
257 species to 4-species interactions while some other trophic interactions are rearranged with HOIs.
258 For instance, most of the genes of the initial steps of *de novo* purine biosynthesis have been

259 found to have a negative IFE in the 3 species condition with *H. alvei* + *P. camemberti* (*purC*, *purE*,
260 *purF*, *purL* and *purN*) as well as in the pairwise condition with *H. alvei* for *purH* and *purK*
261 (Supplementary Figure 5), suggesting competition for purine initial precursor IMP in these
262 conditions. Yet, the introduction of the yeast *G. candidum* as a fourth species cancels the negative
263 IFE value, suggesting that the competition is no longer happening in its presence. Altogether, the
264 observation of noticeable trophic HOIs moving up from 2 to 3 species and then from 3 to 4-species
265 interaction highlights a consistent reorganization of trophic interactions along with community
266 complexity. Also, genes related to Cell wall/membrane/envelope biogenesis are found abundantly
267 among the 4-species emerging genes (Figure 3B) and they represent the largest functional
268 fraction of this gene set. These genes have a negative IFE and are related to Enterobacterial
269 Common Antigen (ECA) biosynthetic processes (*wecG*, *wecB* and *wecA*) (Supplementary Figure
270 9). While the roles of ECA can be multiple but are not well defined²¹, they have been shown to be
271 important for response to different toxic stress, suggesting the development of a specific stress in
272 the presence of the four species.

273 As for the 2 to 3 species comparison, we investigated whether the introduction of a specific fourth
274 species would be most likely associated with HOIs. The 3-species culture that appears to be the
275 least affected by the introduction of a fourth member is with *G. candidum* + *P. camemberti* where
276 34% of the observed interactions are still conserved in the 4-species condition after the
277 introduction of *H. alvei* (versus 22% for with *H. alvei* + *G. candidum* when *P. camemberti* is added
278 and 21% for with *H. alvei* + *P. camemberti* when *G. candidum* is added) (Figure 3C and
279 Supplementary Figure 10). Together, these observations suggest that, again, the introduction of
280 a fungal partner may introduce multiple 4-species HOIs.

281 Finally, by increasing the number of interacting species in our system and investigating interaction
282 gene maintenance and modification with every increment of community complexity, we are able
283 to build our understanding of the architecture of interactions in a microbial community. Altogether,
284 we have observed a total of 218 individual genes associated with interactions in any experiment.

285 Only 16 of them (7%) were conserved across all levels of community complexity (Figure 3D).
286 Starting from 2-species interaction genes, 48% of them were maintained with 3-species and only
287 15% (16 out of 104) were still maintained with 4-species. Thus, we demonstrate here a
288 progressive loss and replacement of 2-species interactions as community complexity increases
289 and the prevalent apparition of HOIs. Tracking back the origins of the genetic basis of interactions
290 in the 4-species experiment that represents the full community of our model, we identify that 28%
291 of the full community interactions can be traced back to 2-species interactions, 18% are from 3-
292 species interaction and 54% are specific to the 4-species interaction (Figure 3D and 3E). Most of
293 the maintained interaction-genes from 2-species as well as from 3-species are associated with
294 metabolism (Figure 3D and Supplementary Figure 11) while Signal transduction and cell
295 membrane biosynthesis genes are most abundant among the 4-species interaction-genes as
296 previously mentioned. To conclude, this shows that the genetic basis of interactions and thus the
297 sets of microbial interaction are deeply reprogrammed at every level of community complexity
298 and illustrates the prevalence of higher order interactions (HOIs) even in simple communities.

299
300 **The majority of maintained 2-species interaction-genes in the 4-species culture follows an**
301 **additive conservation behavior**

302 While HOIs are abundant in the 4-species condition, our data yet suggest that up to 28% of the
303 interactions are maintained from 2-species interactions. However, we don't know whether and
304 how 2-species interactions are quantitatively affected by the introduction of other species and
305 whether they would follow specific quantitative models of conservation. For instance, we can
306 wonder how the strength of a given 2-species interaction is modified by the introduction of one or
307 two other species, or how two 2-species interactions associated with the same gene will combine
308 when all the species are present. In other words, can we treat species interactions as additive
309 when we add multiple species? Such information would generate a deeper mechanistic
310 understanding of the architecture of microbial interactions while allowing us to potentially predict

311 some whole community interactions from 2-species interactions. Here, two main hypothetical
312 scenarios can be anticipated. First, the conservation of 2-species interactions follows a linear or
313 additive behavior, where the introduction of other species either doesn't affect the strength of the
314 conserved 2-species interaction or two similar 2-species interactions combine additively. The
315 second scenario identifies non-linear or non-additive conservation of 2-species interactions,
316 where the strength of the conserved 2-species interaction is modified by the introduction of other
317 species or two similar 2-species interactions are not additive. The second scenario would
318 encompass for instance synergistic effects or inhibitory effects following the introduction of more
319 species. We next use an epistasis and quantitative genomics approach to understand whether
320 interactions that are conserved follow a linear, or additive, pattern. For the 16 genes that are
321 associated with interaction in 2-species cultures, in associated 3-species cultures and in the 4-
322 species condition, we use epistasis analysis to test the linear behavior of IFE when the number
323 of interacting species increases, as IFEs are quantitative traits related to the interaction strength.
324 In multi-dimensional systems, an epistasis analysis quantifies the additive (or linear) behavior of
325 conserved quantitative traits. In quantitative genetics, for instance, epistasis measures the
326 quantitative difference in the effects of mutations introduced individually versus together^{18,22,23}.
327 Using a similar rationale, we can use IFEs as a quantitative proxy for interaction strength and test
328 whether the IFEs of the maintained interaction genes in 3-species and in 4-species conditions
329 result from the linear combination of associated 2-species IFEs (Figure 4A). Nonlinear
330 combination, or non-additivity of 2-species IFEs in higher community level also highlights higher-
331 order interactions.
332 We adapted the pipeline Epistasis¹⁷, originally designed for quantitative genetics investigation.
333 We implemented the linear model with the gene fitness values for growth alone, for each of the
334 2-species conditions, for each of the 3-species cultures and for the 4-species condition. For each
335 gene, the software finds the simplest mathematical model that reproduces the observed IFEs
336 across all levels of community complexity. In the simplest case, the model will have a term

337 describing the effects for adding each species individually to the *E. coli* alone culture; that term
338 corresponds to the 2-species IFE. Then, if the IFE for two *E. coli*'s partners combined (3-species
339 IFE) differs from the sum of their individual effects (corresponding 2-species IFE), the software
340 adds a term capturing this epistasis (Figure 4A). Here, we call that term 3-species epistatic
341 coefficient or ϵ_{ij} . Finally, if the IFE for the combined community (*E. coli* plus all three species; 4-
342 species condition) differs from the prediction based on the 2-species and 3-species terms, the
343 software will add a high-order interaction term to the model (Figure 4B). Here, we name that term
344 4-species epistatic coefficient or ϵ_{ijk} .

345
346
347 We performed this analysis on the 16 genes that are associated with interactions at every level
348 of community complexity. To identify real additive behavior of IFE from non-additivity, we screen
349 for 3-species epistatic coefficients and 4-species epistatic coefficients that are significantly
350 different from 0 (adjusted p-value ≤ 0.01 , correction for multiple testing Benjamin-Hochberg). We
351 found that 13 genes behaved additively from 2-species to 4-species culture, with no epistatic
352 contributions in the 3-species conditions nor in the 4-species condition (Figure 4C, (i)). One gene
353 (*gadW*) exhibited nonlinear conservation of IFE only in the 4-species condition, but additive IFE
354 conservation from 2-species to 3-species (Figure 4C, (ii)). Another gene (*lsrG*) showed epistasis
355 in one 3-species condition but no epistasis in the 4-species condition (Figure 4C, (iii)) Finally, one
356 gene (*gltB*) displayed both non-additivity in 3-species and 4-species conditions (Figure 4C, (iv)).
357 If we look more closely at the additive genes, we find genes (*betA*, *betT*, *purD* and *purH*) are
358 associated with the conservation of negative IFEs (Supplementary Figure 12). While *betA* and
359 *betT* are associated with choline transport (*betT*) and glycine betaine biosynthesis from choline
360 (*betA*)²⁴, *purD* and *purH* are associated with *de novo* purine biosynthesis²⁵. This suggests that
361 requirements for glycine betaine biosynthesis from choline and for purine biosynthesis caused by
362 microbial interactions, possibly due to competition for the nutrients used as precursors, are

363 additively conserved from individual 2-species interactions requirements. Also, 5 genes
364 associated with amino acid biosynthesis (*serA*, *thrC*, *cysG*, *argG* and *proA*) are associated with
365 the additive conservation of positive IFE (Supplementary Figure 12), suggesting that cross
366 feeding can be additive when the community complexity increases. Altogether, this highlights the
367 existence of 2-species interactions, including trophic ones, conserved in an additive fashion in the
368 highest-level of complexity.

369 This leaves 3 genes (18%) of the maintained 2-species interaction-associated genes that are
370 associated with non-additive behavior, and thus HOIs, at at least one higher level of community
371 complexity (Figure 4C - (ii), (iii) and (iv)). The gene *gadW* is associated with non-additivity at the
372 4-species level, suggesting that while IFEs are additive in 3-species cultures, the introduction of
373 a fourth species introduces HOI. Moreover, the observed 4-species IFE is greater than the IFE
374 predicted by a linear model (Figure 4D), highlighting a potential synergistic effect when the 4
375 species are together. The gene *lsrg* is associated with non-additivity only at the 3-species culture
376 w *G.c* + *P.c*. More specifically, this indicates that HOI arise when these 2 fungal species are
377 interacting together with *E. coli*, but that no more HOI emerge when *H. alvei* is introduced (ie, the
378 4-species IFE can be predicted by the linear combination of the lower levels IFEs). As the
379 observed IFE for the 3-species condition w *G.c* + *P.c* is greater than the predicted IFE (Figure
380 4C), this suggests a synergistic effect between the 2 fungal species. Finally, the gene *gltB* is
381 associated with non-additivity at both the 3-species and 4-species levels. For this gene, the
382 conservation of IFE is never associated with an additive model. Here, the observed 4-species IFE
383 is not as negative as it would be as the result of the linear combination of the associated lower
384 IFE (Figure 4D), suggesting the existence of a possible IFE threshold, or plateau effect.
385 Altogether, this indicates that maintained 2-species-interactions can follow nonlinear behaviors
386 that could involve synergistic effects, inhibitory effects or constraints.

387

388 **Discussion**

389 Interactions between microbes are responsible for the specific and multiple phenotypes observed
390 in microbial communities compared to monocultures. Knowledge of microbial interactions could
391 be the key to controlling microbial communities, but deciphering these interactions is challenging
392 in complex microbiomes. Moreover, pairwise culture interactions are often insufficient to predict
393 what happens in more complex microbiomes, suggesting an important reprogramming of
394 interactions as community complexity increases in terms of the number of species present^{3,5,7,13,14}.
395 Understanding the restructuring of these interactions in complex communities is thus essential to
396 comprehending the biology of microbial communities. Using an *in vitro* multi-kingdom community,
397 we performed a molecular investigation of the reorganization of interaction profiles as community
398 complexity changed. Relying on the tractability of our model system and an RBTnSeq-based
399 interaction assay, we tracked interactions in 2-species, 3-species and 4-species cultures. In this
400 work, the combination of a qualitative and quantitative comparison of interaction profiles at the
401 molecular level underlines the complex dynamics of interaction reorganization with community
402 complexity and the existence of multiple forms of higher-order interactions.
403 This work offers an example of the different forms that HOIs can take in biological systems. We
404 report multiple mechanistic HOIs as defined in ecological studies and represented here by any
405 pairwise interaction-associated genes that are not observed in 3 and more species conditions as
406 well as any interaction-associated genes observed in higher-levels than pairwise cultures¹². We
407 also report another form of HOIs, as defined in quantitative genetics, which are associated with
408 the non-additive behavior of conserved 2-species interactions in 3 or 4 species communities²².
409 Here, each HOI level refers to different biological phenomena occurring in the same biological
410 system. Yet, they are essential and complementary to decipher the extremely convoluted
411 architecture and dynamics of microbial interactions and microbiome biology.
412 As the number of interaction-associated genes strongly decreased in the 4-species culture
413 compared to 2 or 3 species setups, our work points out a strong reduction of the interaction
414 landscape with 4 species that is associated with the loss of many lower-level interactions and the

415 emergence of context-specific interactions. While 43% of the 2-species interaction-associated
416 genes are still found with 3 species, only 15% are still found with 4 species, representing less
417 than a third (28%) of the total of 4-species interactions. This highlights the increasing dilution and
418 replacement of original 2-species interactions. To summarize, the more complex a community
419 gets, the more mechanistic HOIs emerge. While our work was limited to 4 species, it remains
420 necessary to verify whether this statement will be true for more complex communities: whether
421 more 2-species interactions will be lost and more HOIs will keep emerging at each level or whether
422 the interaction landscape will stabilize. Indeed, Friedman *et al.*, have highlighted that growth
423 observation for 2- and 3-species combination could predict the assembly of 7- to 8-species²; this
424 would suggest that interactions, or at least key interactions driving community assembly, could
425 change less dramatically in higher complexity microbiomes.

426 Our molecular approach enabled us to identify that most of the reorganization of the
427 interaction profile is associated with the reprogramming of metabolic or trophic interactions
428 including both competition for nutrients and cross-feeding. As more species are introduced it
429 appears that the dynamics of nutrient consumption is rearranged. For instance, we observed that
430 some 2-species competition for amino acids and for lactate between *E. coli* and *H. alvei* can be
431 alleviated by the introduction of *G. candidum*. While the competition for amino acids is likely
432 alleviated by amino acid cross-feeding from *G. candidum*, as this species is known to release
433 amino acids into the environment through digestion of proteins and peptides^{26–28}, the mechanism
434 relieving competition for lactate is unclear. Possibly, *G. candidum* provides other nutrients sources
435 like amino acids that alleviate the need for *E. coli* to rely on lactate. Trophic interactions are
436 described as core determinants in community assembly^{29,30} and simple rules of metabolic
437 interdependencies and metabolic specialization can be sufficient to predict the assembly of rather
438 complex communities^{31–33}. Yet in complex systems, such as the gut, with complex nutrient
439 composition, the important reorganization of metabolic interactions as community complexity

440 changes could likely explain the difficulty in predicting community assembly and composition in
441 some studies⁷. As previously suggested³⁴, ecological and metabolic factors associated with the
442 present species such as niche overlap, degree of metabolic specialization and species similarities
443 are likely to be drivers of these metabolic HOIs. Indeed, microorganisms display incredible
444 metabolic abilities, from nutrient usage to rapid metabolic switching, and in the presence of
445 multiple nutrient sources and/or other microorganisms they are likely to readjust the sequence of
446 nutrient uptake. Niche occupation and nutrient access are also two crucial aspects in the success
447 or failure of microbial invasion^{4,35}. The reorganization of metabolic interactions in different
448 community composition could likely explain the poor predictability of invasion resistance from
449 simple species-combinations and the emergence resistance-specific phenotype.

450 To some extent, our work also highlights the importance of fungal species as major actors in
451 reshaping interaction networks. Here, more 3-species HOIs and 4-species HOIs were observed
452 when one fungal species was added either as a third species with two bacteria or as a fourth
453 species with another fungus and two bacteria. In microbial communities, fungi are known to
454 impact community structure and access to nutrients through the formation of hyphal highways^{36,37},
455 to impact community assembly through environmental modification³⁸⁻⁴⁰ as well as to impact
456 community protection through the production of multiple secondary metabolites with antibiotic or
457 antimicrobial properties^{15,39,41}. In this specific context, fungi-associated HOIs seem to be related
458 to their metabolic characteristics, whether through cross-feeding or competition for nutrients. Yet,
459 the emergence of specific requirements for ECA biosynthetic genes in *E. coli* when all species
460 are present, suggesting a potential toxic stress, may reveal other fungal context-specific
461 properties, while it could also inform about a more precise role of the ECA in *E. coli*. We believe
462 this work contributes, along with other recent studies, to advocate for the need to include fungal
463 species more frequently into microbiome work studies.

464

465 Finally, to understand principles behind the conservation of pairwise interactions, we used
466 epistasis analysis to quantify the additive or non-additive behavior of conserved 2-species
467 interactions in 3 and 4 species conditions. Epistasis analysis offers an adaptable approach to test
468 the linear behavior of quantitative traits in systems with increasing complexity, whether it is the
469 effects of accumulation of mutations in a genome^{18,42}, the effect of drug combinations⁴³ or the
470 dynamics of predators-prey ecosystems⁴⁴. Recent studies in the field of microbiome research
471 have also relied on epistasis analysis to elucidate fundamentals of microbial communities such
472 as how the nutrient composition of the environment determines the assembly and the diversity of
473 a microbial community^{34,45}, how the functional landscape of microbial community is built³ or how
474 the commensal microbiome determines the development, lifespan and reproduction of its host⁵.
475 In this work, using the quantitative metric IFE for the strength of interactions, we used an epistatic
476 model to characterize the additivity or non-linearity of IFE of conserved 2-species interactions
477 when *E. coli* is growing with 2 and 3 other species (3-species and 4-species conditions
478 respectively). We observed that most of the conserved 2-species interaction genes followed an
479 additive model of conservation, including trophic-interaction related genes. While our study was
480 limited to a small number of interacting species, it remains to be investigated if this linear behavior
481 is propagated if the community complexity increases again. While we have observed both
482 synergistic effects and limitations effects for nonlinear conservation of interaction strength, we
483 believe that such behavior are likely to arise in more complex contexts and that additivity will
484 eventually stop. For instance, additivity of pairwise interactions is likely to saturate and to stop at
485 higher-levels of complexity due to environmental constraints (nutrient supply for instance) and/or
486 the metabolic capacities of the different species as highlighted in ³⁴. While this theory can apply
487 to conserved trophic interactions, like the ones highlighted in our work, other scenarios could
488 include molecule-driven or environment-mediated interactions such as exchange of metabolites,
489 quorum sensing, antibiosis and modification of the physiochemical properties of the environment.

490 While trait additivity is fairly easy to quantify in high-dimensional systems, our study, along with
491 other work using epistasis to study microbial communities^{3,5,34,45} suggest that additivity of
492 quantitative microbial features is not the only scenario in nature, and strongly emphasizes the
493 need to develop mathematical approaches to accurately understand the dynamics and
494 functionalities of microbiomes.

495

496 Overall, our work identifies the reorganization of microbial interactions along with community
497 complexity at the molecular level. While more advanced modeling is still required, this knowledge
498 of the mechanistic reorganization of interactions and patterns of HOIs is essential for bottom-up
499 approaches to be able predict, from minimal information, the biology of complex microbiomes and
500 will offer novel opportunities to design synthetic microbial communities or control natural ones.

501

502 **Methods**

503 Strains and media

504 *Strains*

505 The bloomy rind cheese community was reconstructed with the same strains from ¹⁴: *H. alvei*
506 JB232 isolated from cheese⁴⁶ and two industrial cheese strains: *G. candidum* (Geotrichum
507 candidum GEO13 LYO 2D, Danisco – CHOOZITTM, Copenhagen, Denmark) and *P. camemberti*
508 (PC SAM 3 LYO 10D, Danisco - CHOOZITTM).

509

510 *Medium*

511 All assays have been carried out on 10% cheese curd agar, pH7 (CCA) (10% freeze-dried Bayley
512 Hazen Blue cheese curd (Jasper Hill Farm, VT), 3% NaCl, 0.5% xanthan gum and 1.7% agar).
513 The pH of the CCA was buffered from 5.5 to 7 using 10M NaOH.

514

515 **Competition assay – RBTnSeq Assays**

516 The *E. coli* barcoded transposon library Keio_ML9¹⁹ was used for all RBTnSeq assays on CCA
517 during a 3-day growth in eight different culture conditions: alone, 2-species conditions (with *H.*
518 *alvei*; with *G. candidum*; and with *P. camemberti*), 3-species conditions (with *H. alvei* + *G.*
519 *candidum*; with *H. alvei* + *P. camemberti*; and with *G. candidum* + *P. camemberti*), and in the
520 single 4-species condition (with *H. alvei* + *G. candidum* + *P. camemberti*) (Figure 1).

521 From the species and library inoculation to cell harvest after 3 days of growth, we followed the
522 same procedure as described in¹⁴. We amplified the *E. coli* barcoded transposon library Keio_ML9
523 into 25 mL of liquid LB-kanamycin (50 mg/mL) up to an OD of 0.6-0.8. A 5mL sample of this
524 preculture was spun down and kept at -80C as the T0 sample required for fitness calculation. The
525 remaining cells were then washed in PBS1x-Tween0.05% and used to inoculate the competition
526 assays with 7*10⁶ cells of the library on each 100 mm petri dish plate. When necessary, the other
527 community members were then inoculated at the following densities: for *H. alvei*: 7*10⁶ cells; for
528 *G. candidum*: 7*10⁶ cells; for *P. camemberti*: 7*10⁵ cells.

529 After 3 days, cells were harvested by flooding the plates with 1.5mL of PBS1X-Tween0.05%,
530 gentle scraping and then transferring the resuspended cells into 1.5mL tubes. Cells were
531 centrifuged for 3 min at RT at 10 KRPM and stored at -80C until gDNA extraction.

532 All assays have been performed in triplicate.

533

534 **gDNA extraction, library preparation and sequencing**

535 gDNA from the samples of the competition assays was extracted by phenol-chloroform extraction
536 (pH 8) as described in¹⁴. For each sample, we resuspended the cells into 500 mL of buffer B (200
537 mM NaCl, 20 mM EDTA) and then transferred them into a 2mL screw-capped tube previously
538 filled with 125 mL of 425-600 mm acid-washed beads and 125 mL of 150-212 mm acid-washed
539 beads. Then, 210mL of SDS 20% and 500mL of Phenol:Chloroform (pH 8) were added to each
540 sample before mechanical lysis by vortexing the tubes for 2 minutes at maximum speed. Tubes
541 were then centrifuged for 3 min at 8 KRPM at 4C and 450mL of aqueous phase were recovered

542 for each sample. 45 mL of sodium acetate 3M and 450 mL of ice-cold isopropanol were added
543 and tubes were incubated for 10 min at -80C. Tubes were then centrifuged for 5 min at 4C at 13
544 KRPM, supernatant was removed and the pellet was washed in 750 mL of 70% ice-cold ethanol
545 before being resuspended in 50mL of DNase/RNase free water.

546 For library preparation, the 98C BarSeq PCR described in ¹⁹ was used to amplify the barcoded
547 region of the transposons and PCR was performed in a final volume of 50 mL: 25 mL of Q5
548 polymerase master mix (New England Biolab), 10 mL of GC enhancer buffer (New England
549 Biolab), 2.5 mL of the common reverse primer (BarSeq_P1¹⁹) at 10 mM, 2.5 mL of a forward
550 primer from the 96 forward primers (BarSeq_P2_ITXXX¹⁹) at 10 mM and 50 ng to 2 mg of gDNA.
551 The following PCR program was used: (i) 98 °C - 4 min, (ii) 30 cycles of: 98 °C – 30 s; 55 °C – 30 s;
552 72 °C – 30 s, (iii) 72 °C – 5 min. After the PCR, 10 mL of each of the PCR products were pooled
553 together to create the BarSeq library. 200 mL of the pooled library were purified using the MinElute
554 purification kit (Qiagen) and final elution of the BarSeq library was performed in 30 mL in DNase
555 and RNase free water.

556 The BarSeq library was quantified using Qubit dsDNA HS assay kit (Invitrogen) and then
557 sequenced on HiSeq4000 (50 bp, single-end reads), by the IGM Genomics Center at the
558 University of California San Diego.

559

560 **Data processing and interaction fitness effects (IFE) analysis**

561 For each library, BarSeq reads were first processed using the Perl script BarSeqTest.pl from ¹⁹ to
562 obtain the count file (all.poolcount) containing the number of reads per barcode for each
563 sample. This pipeline requires a table where each barcode is mapped to a location in the genome.
564 The Arkin lab (Physical Biosciences Division, Lawrence Berkeley National Laboratory, Berkeley,
565 California, USA) kindly provided the TnSeq table for the *E. coli* library. The original script used for
566 this analysis originates from ¹⁹ is publicly available on <https://bitbucket.org/berkeleylab/feba>.

567 The generated all.poolcount information was then implemented into custom R scripts from¹⁵ to
568 determine the average fitness scores for each gene across three RBTnSeq assay replicates for
569 each of the eight cultures (<https://github.com/DuttonLab/RB-TnSeq-Microbial-interactions>).
570 Insertion mutants that did not have a sufficient T0 count in each condition or that were not centrally
571 inserted (10–90% of gene) were removed from the analysis and counts were then normalized
572 using a set of five reference genes (*glgP*, *acnA*, *modE*, *leuA* - average of 52 strains
573 each). Detailed explanation of the fitness calculation strategy can be found in the Readme
574 document as well as in¹⁵. In each condition, to assess the possible variability between replicates,
575 we measured the correlation between the three replicates (Supplementary Figure 13). In this set
576 of experiments, Pearson coefficient between replicates varied from 0.79 to 0.86 suggesting low
577 technical noise.

578 Gene fitness values were then compared between interactive conditions and *E. coli* growth alone
579 conditions using two-sided *t*-tests (when the equality of variance was verified by Fisher test) and
580 correction for multiple comparison (Benjamini–Hochberg method²⁰). Comparisons associated
581 with an adjusted *P* value lower than 10% were considered a significant interaction fitness effect.
582

583 **Epistasis model analysis**

584 We used the Python package Epistasis¹⁷ to run the epistasis analysis on *E. coli*'s genes. We
585 implemented the model with the average fitness values across the three biological replicates
586 along with the corresponding variance, for each gene and for each of the culture conditions
587 (Alone, w *H.a*, w. *G.c* , w *P.c*, w *H.a* + *G.c*, w *H.a* + *P.c*, w *G.c* + *P.c*, w *H.a* + *G.c* + *P.c*). The
588 model is run for each gene individually. The 'genotypes' expected in the model correspond to the
589 culture conditions and are binary coded based on the presence or not of *E. coli*'s partners *G.*
590 *candidum*, *H. alvei* and *P. camemberti*. For instance, the Alone condition corresponds to
591 phenotype 000, the w *G.c* condition is coded 100, the w *H.a* + *P.c* condition is coded 011, the w
592 *H.a* + *G.c* + *P.c* is coded 111 and so on. The 'phenotype' implemented in the model corresponds

593 to the average fitness value across three biological replicates. After generating the genotype-
594 phenotype map for each gene, the model was run a first time using the 'local' parameter to set-
595 up the center of the map, and returns the set of epistatic coefficients for each gene calculated as
596 follows:

597

$$598 \text{IFE}_{\text{obs},\text{Ha},\text{Gc}} = \text{IFE}_{\text{Ha}} + \text{IFE}_{\text{Gc}} + \varepsilon_{\text{Ha},\text{Gc}}$$

$$599 \text{IFE}_{\text{obs},\text{Ha},\text{Pc}} = \text{IFE}_{\text{Ha}} + \text{IFE}_{\text{Pc}} + \varepsilon_{\text{Ha},\text{Pc}}$$

$$600 \text{IFE}_{\text{obs},\text{Gc},\text{Pc}} = \text{IFE}_{\text{Gc}} + \text{IFE}_{\text{Pc}} + \varepsilon_{\text{Gc},\text{Pc}}$$

$$601 \text{IFE}_{\text{obs},\text{Ha},\text{Gc},\text{Pc}} = \text{IFE}_{\text{Ha}} + \text{IFE}_{\text{Gc}} + \text{IFE}_{\text{Pc}} + \varepsilon_{\text{Ha},\text{Gc}} + \varepsilon_{\text{Ha},\text{Pc}} + \varepsilon_{\text{Gc},\text{Pc}} + \varepsilon_{\text{Ha},\text{Pc},\text{Gc}}$$

602
603 To determine whether each coefficient was different from zero, we generated 7,000
604 pseudoreplicates from our experimental variance from each gene and then calculated the
605 probability each coefficient was above or below zero from this distribution. P-values were then
606 adjusted for multiple comparison testing using Benjamini Hochberg Correction²⁰. As it has been
607 shown previously that epistatic analyses can fail if the effects of mutations combine non-linearly
608 instead of linearly (e.g. mutational effects multiply rather than add), we used the epistasis package
609 to look for such nonlinearity. However, no nonlinearity was observed (Supplementary Figure 14).

610

611
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613

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714

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722

723 **Author Contributions**

724 R.J.D., M.J.H. and M.A.M. conceptualized the study. M.A.M. performed the experiments. The Epistasis
725 pipeline was written and adapted by M.J.H. and A.J.M. Data analyses were performed by M.A.M. and A.J.M.
726 The article was written by M.A.M. and revised with input from all authors. The figures were made by M.A.M
727 with input from all authors. The study was supervised by R.J.D. and M.J.H.

728

729 **Additional information / Competing Interest Statement**

730 The authors declare that no financial and non-financial competing interests exist in relation to the work
731 described.

732

733 **Figure legends**

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735 species cultures.** **A.** Experimental design for the identification of interaction-associated genes in 7
736 interactive conditions from the Brie community. The *E. coli* RBTnSeq Keio_ML9 (Wetmore *et al.*, 2015) is
737 either grown alone or in 2, 3 or 4 species cultures to calculate *E. coli* gene fitness in each condition (in
738 triplicate). Interaction fitness effect (IFE) is calculated for each gene in each interactive culture as the
739 difference of the gene fitness in the interactive condition and in growth alone. IFE that are significantly
740 different from 0 (two-sided t-test, Benjamini-Hochberg correction for multiple comparisons) highlight the
741 genes associated with interaction in an interactive condition. **B.** Volcanoplot of IFEs calculated for each
742 interactive condition. Adjusted p-values lower than 0.1 highlight significant IFEs. Negative IFEs (blue)
743 identify negative interactions and positive IFE (red) identify positive interactions. Numbers on each plot
744 indicate the number of negative (blue) or positive (red) IFEs. **C.** Functional analysis of the interaction-
745 associated genes (significant IFEs). Interaction-associated genes have been separated into two groups:
746 negative IFE and positive IFE. For each group, we represent the STRING network of the genes (Nodes).
747 Edges connecting the genes represent both functional and physical protein association and the thickness
748 of the edges indicates the strength of data support (minimum required interaction score: 0.4 – medium
749 confidence). Nodes are colored based on their COG annotation and the size of each node is proportional
750 to the number of interactive conditions in which that given gene has been found associated with a significant
751 IFE. Higher resolution of the networks with apparent gene names are found in Supplementary Figures 2
752 and 3.

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754 **Figure 2: Comparison of the genetic basis of interaction for 2-species and 3-species
755 conditions.** **A.** Venn Diagram of 2-species and 3-species interaction-gene sets. This Venn Diagram
756 identifies 2-species interaction-genes that are dropped when a third species is introduced (Left side;
757 Dropped interaction-genes = any 2-species gene that are not found in any 3-species condition), 2-species
758 interaction-genes that are maintained in at least one associated 3-species condition (Intersection;
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760 Emerging interaction-genes). **B.** Functional analysis of the dropped, maintained and emerging interaction-
761 genes from 2-species to 3-species. Each dot represents the fraction of genes of the studied gene set
762 associated with a given COG category (Number of genes found in the category / Total number of genes in
763 the gene set). The color of the dots indicates the general COG group of the COG category: Teal:
764 Metabolism; Blue: Information storage and processing; Orange: Cellular Processes and Signaling ; Grey:
765 Unknown or no COG category. **C.** Species-level analysis of 3-species HOIs: for each 2-species condition,
766 we measure the fraction of interaction-genes that are dropped in associated 3-species cultures (Dropped
767 in 3-species) or maintained in at least one of the 3-species cultures (Maintained in 3-species); for each 3-
768 species condition, we measure the fraction of interaction-genes that have been conserved from at least one
769 associated 2-species condition (Maintained from 2-species) or that are emerging with 3-species (Emerging
770 in 3-species).

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773 species and 4-species interaction-gene sets. This Venn Diagram identifies 3-species interaction-genes that
774 are dropped when a fourth species is introduced (Left side; Dropped interaction-genes = any 3-species
775 gene that are not found in the 4-species condition), 3-species interaction-genes that are maintained in the
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780 category / Total number of genes in the gene set). The color of the dots indicates the general COG group
781 of the COG category: Teal: Metabolism; Blue: Information storage and processing; Orange: Cellular
782 Processes and Signaling; Grey: Unknown or no COG category. **C.** Species-level analysis of 4-species
783 HOIs: for each 3-species cultures we measure the fraction of interaction-genes that is conserved in the 4-
784 species culture (Maintained in 4-species) and the fraction of interaction-genes that has been dropped
785 (Dropped in 4-species). **D.** Alluvial plots of the interaction genes across community complexity levels. **E.**
786 STRING network of the 4-species interaction genes (Nodes). Edges connecting the genes represent both
787 functional and physical protein association and the thickness of the edges indicates the strength of data
788 support (minimum required interaction score: 0.4 – medium confidence). Nodes are colored based on the
789 level of community complexity the genes are conserved from.
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791 **Figure 4: Quantitative analysis of IFE conservation for the interaction associated genes**
792 **conserved from 2-species to 4-species conditions.** **A.** Schematized quantitative epistasis/non-
793 linearity measured in 3-species conditions (with partner i and j). Epistasis (ϵ_{ij}) is the difference between the
794 individual IFE of partner i and partner j (red and orange bars) versus placing them together (green).
795 Mathematically, we need three terms (IFE_i, IFE_j, and ϵ_{ij}) to reproduce the observed IFE for the 3-species
796 condition. **B.** This analysis can be extended to higher levels of community complexity: 4-species (*E. coli*
797 with 3-partners i, j, and k). The model first accounts for epistasis between i/j, i/k, and j/k. In this example, i
798 and j exhibit epistasis; i/k and j/k are additive (dark blue and purple). The predicted IFE for the 4-species
799 community is the sum of the individual 2-species effects (red, orange, light blue) and the 3-species epistatic
800 terms (green). The 4-species epistatic coefficient is the difference between this low-order prediction and
801 the observed IFE for the i,j,k community (pink). **C.** Conservation profiles of the 16 2-species interaction-
802 associated genes conserved up to 4-species. 2-species conditions: a colored square indicatea the 2-
803 species condition(s) in which the interaction-associated gene was identified; a grey square indicates non-
804 significant 2-species IFEs. 3-species conditions: a teal square indicates that the associated IFE is
805 associated with additive behavior from associated 2-species IFE (no ϵ_{ij} epistatic coefficient), a red square
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807 corresponds to a 3-species condition that is not associated with significant 2-species IFE (no epistasis
808 analysis performed); 4-species condition: a teal square indicates that the associated IFE is associated
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812

813 **Supplementary material list**

814 *Supplementary Figures:*

815 Supplementary Figure 1: Growth of the community species in the studied conditions

816 Supplementary figure 2: Functional analysis of interaction-associated genes with negative IFEs

817 Supplementary figure 3: Functional analysis of interaction-associated genes with positive IFEs

818 Supplementary figure 4: IFE profiles of Amino acid biosynthesis genes identified in this study

819 Supplementary figure 5: IFE profiles of Purine biosynthesis associated genes identified in this
820 study

821 Supplementary Figure 6: Comparison of interaction-associated genes across the different levels
822 of community complexity

823 Supplementary figure 7: IFE profiles of lactate metabolism genes

824 Supplementary figure 8: Condition specific comparison of interaction-associated genes for 2 and

825 3-species conditions

826 Supplementary figure 9: IFE profiles of Enterobacterial Common Antigen (EAC) genes

827 Supplementary figure 10: Condition specific comparison of interaction-associated genes for 3 and

828 4-species condition

829 Supplementary figure 11: Functional network of the 4-species interaction-genes and their origin

830 Supplementary figure 12: IFE profiles of the 16 2-species interaction genes maintained up to 4-

831 species

832 Supplementary figure 13: Pearson correlation of gene fitness across replicates

833 Supplementary figure 14: Non-linearity analysis of IFE in the Epistasis model

834

835 *Supplementary Datasets:*

836 Supplementary Data 1: RB-TnSeq based interaction analysis (Fitness values, Interaction Fitness

837 Effects and associated statistics)

838 Supplementary Data 2: Interaction-associated genes at each level of community complexity

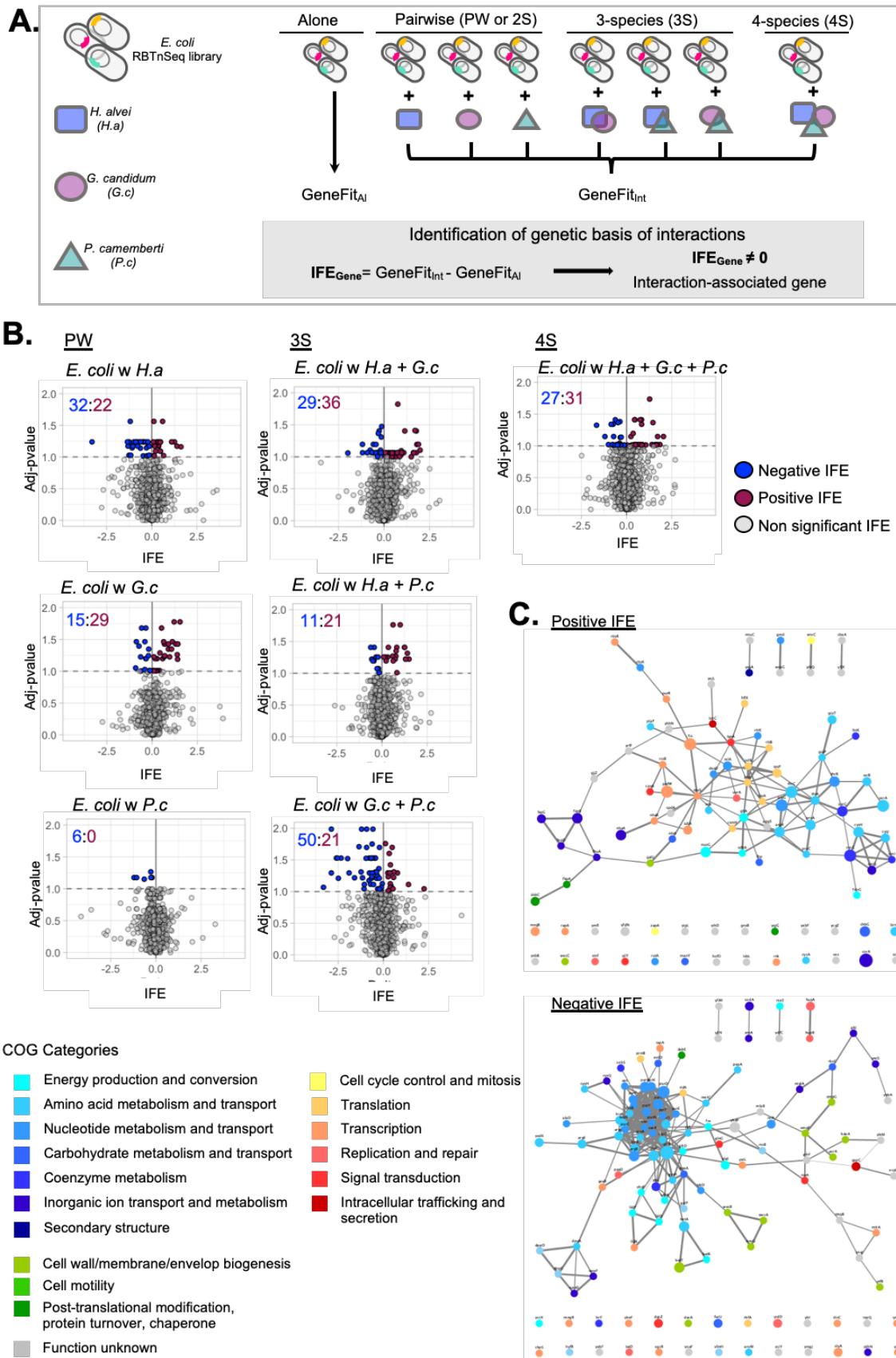
839 Supplementary Data 3: Comparison of interaction-associated genes across the different levels of

840 community complexity

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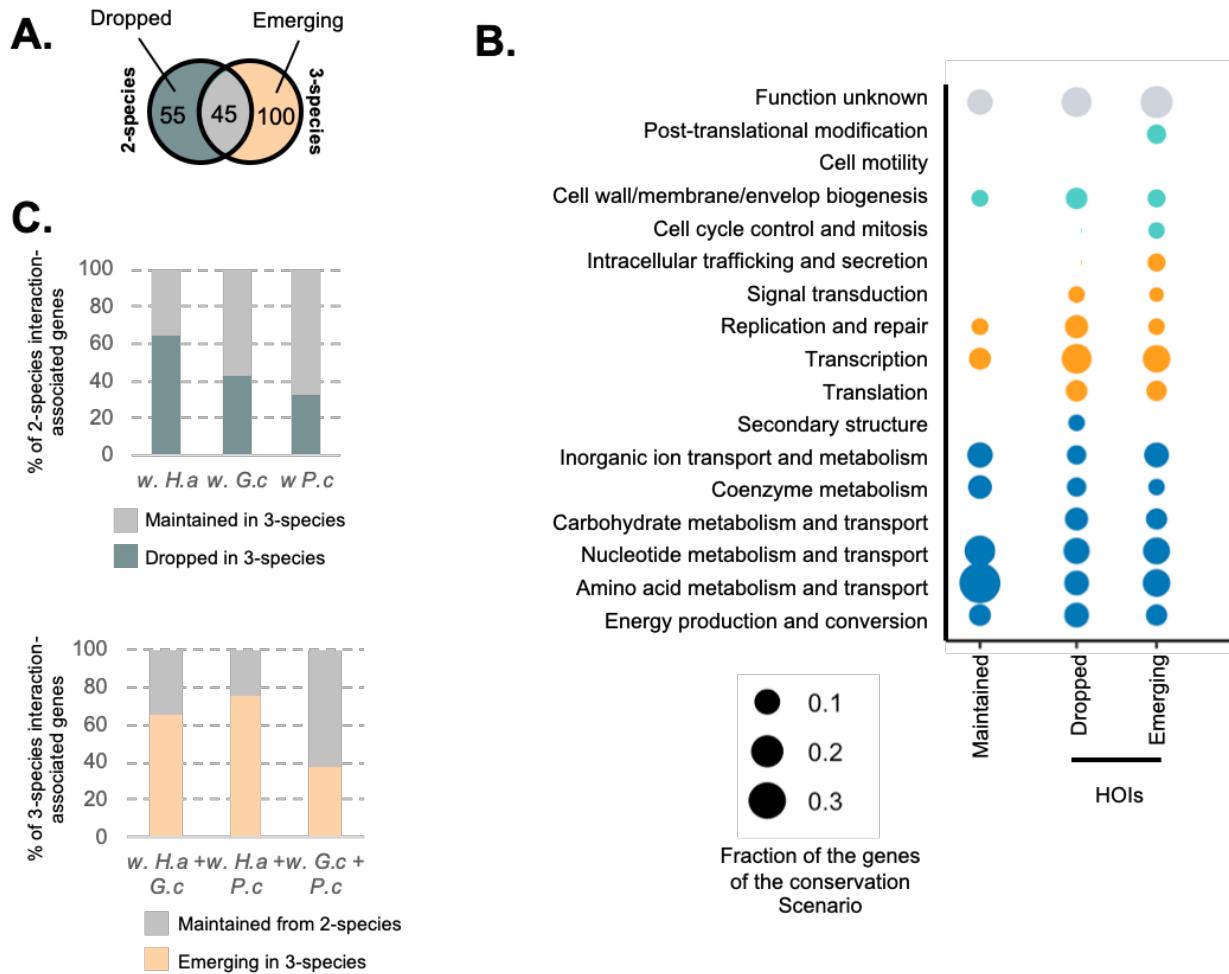
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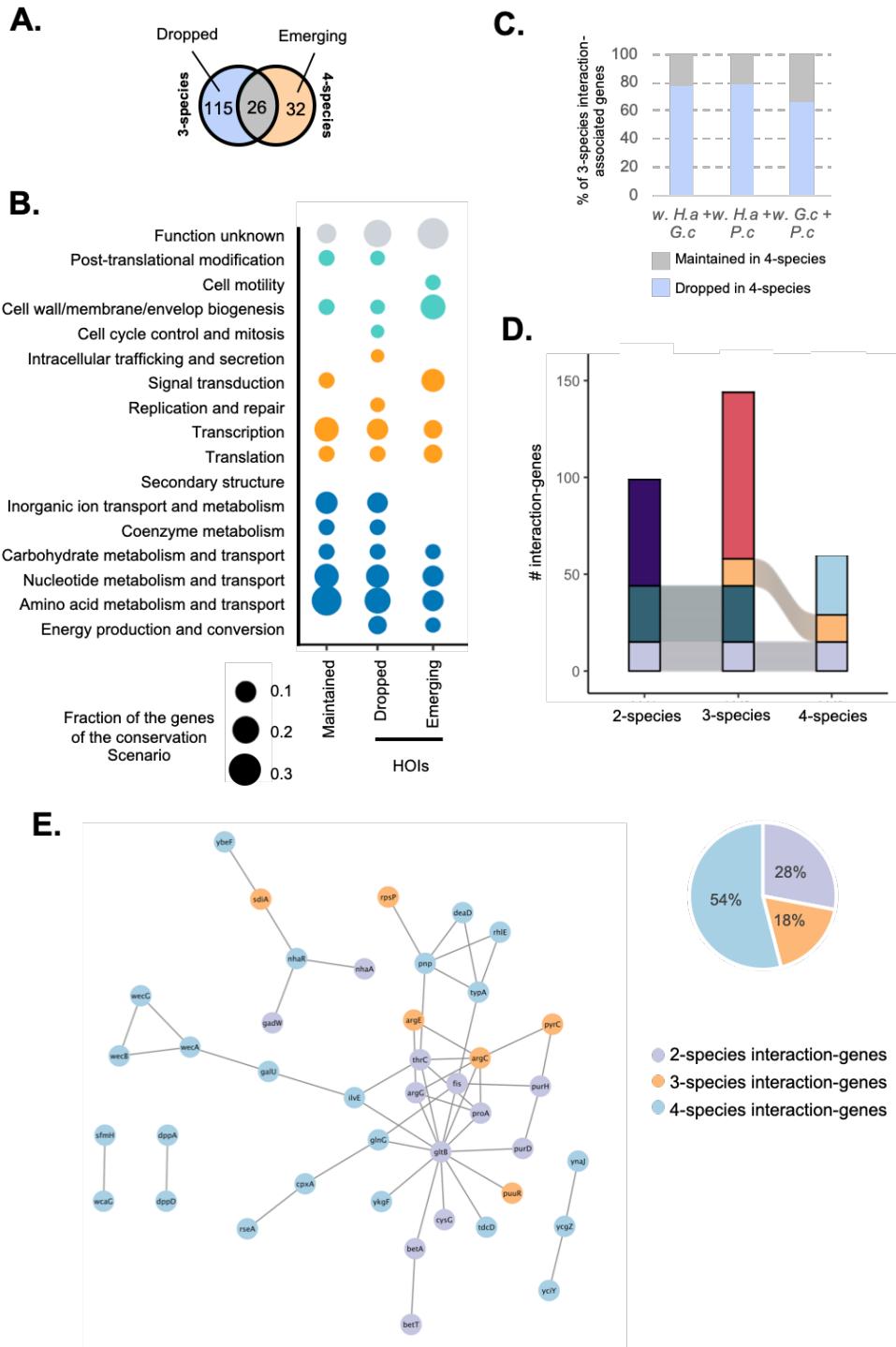


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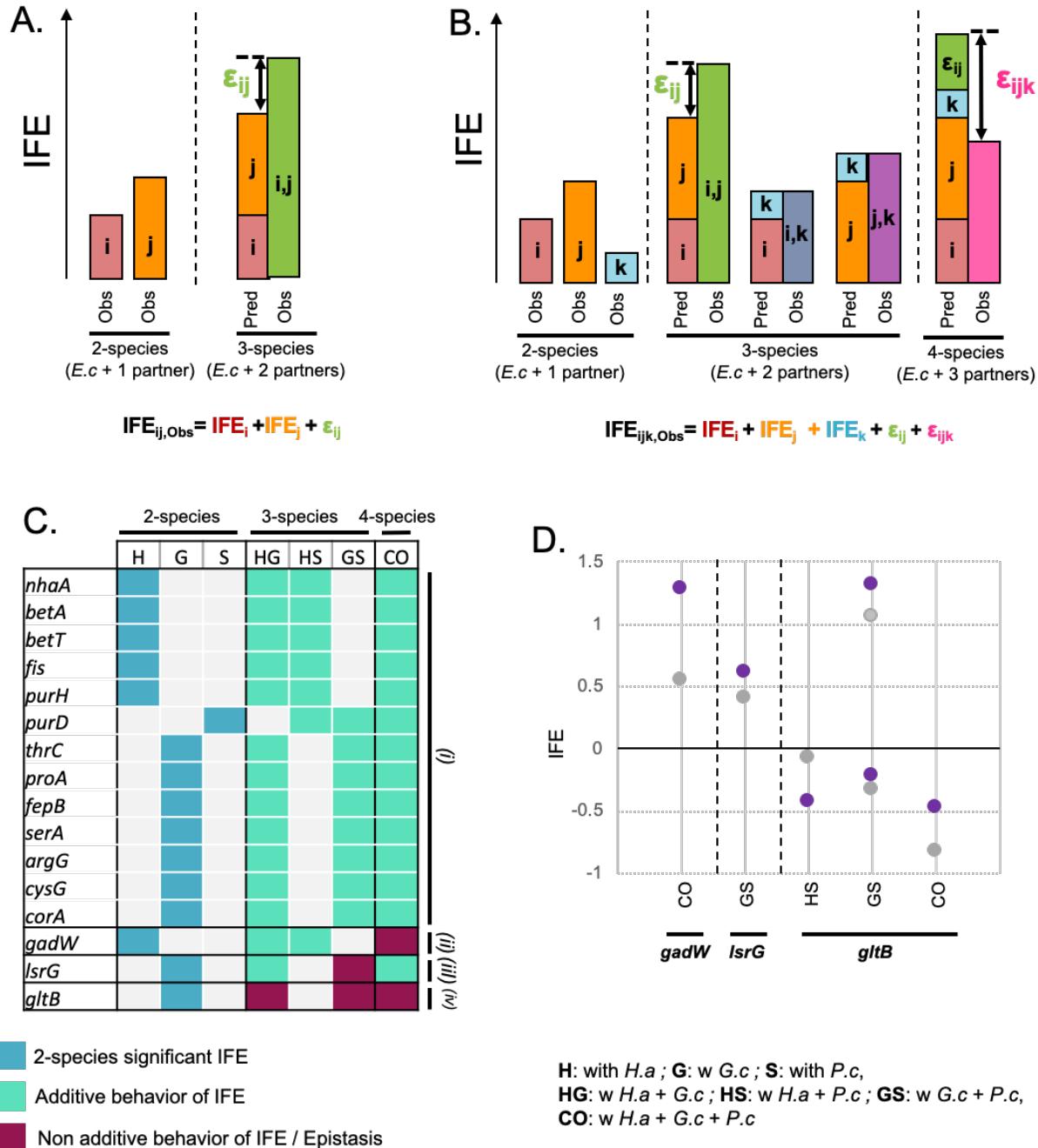
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