

1 Heritability enrichment in context-specific regulatory networks improves  
2 phenotype-relevant tissue identification

3 Zhanying Feng<sup>1,2</sup>, Zhana Duren<sup>3</sup>, Jingxue Xin<sup>4</sup>, Qiuyue Yuan<sup>3</sup>, Yaoxi He<sup>5</sup>, Bing Su<sup>5,6</sup>, Wing Hung  
4 Wong<sup>4\*</sup>, Yong Wang<sup>1,2,6,7\*</sup>

5

6 <sup>1</sup>CEMS, NCMIS, HCMS, MDIS, Academy of Mathematics and Systems Science, Chinese Academy of Sciences,  
7 Beijing 100190, China

8 <sup>2</sup>School of Mathematics, University of Chinese Academy of Sciences, Chinese Academy of Sciences, Beijing,  
9 100049, China

10 <sup>3</sup>Center for Human Genetics and Department of Genetics and Biochemistry, Clemson University, Greenwood, SC,  
11 29646, USA

12 <sup>4</sup>Department of Statistics, Department of Biomedical Data Science, Bio-X Program, Stanford University, Stanford,  
13 CA 94305, USA

14 <sup>5</sup>State Key Laboratory of Genetic Resources and Evolution, Kunming Institute of Zoology, Chinese Academy of  
15 Sciences, 650223, Kunming, China

16 <sup>6</sup>Center for Excellence in Animal Evolution and Genetics, Chinese Academy of Sciences, Kunming 650223, China

17 <sup>7</sup>Key Laboratory of Systems Biology, Hangzhou Institute for Advanced Study, University of Chinese Academy of  
18 Sciences, Chinese Academy of Sciences, Hangzhou, 330106, China

19

20 \*Corresponding authors: [ywang@amss.ac.cn](mailto:ywang@amss.ac.cn), [whwong@stanford.edu](mailto:whwong@stanford.edu)

21 **Abstract**

22 Systems genetics holds the promise to decipher complex traits by interpreting their associated SNPs  
23 through gene regulatory networks derived from comprehensive multi-omics data of cell types,  
24 tissues, and organs. Here, we propose SpecVar to integrate paired chromatin accessibility and gene  
25 expression data into context-specific regulatory network atlas and regulatory categories, conduct  
26 heritability enrichment analysis with GWAS summary statistics, identify relevant tissues, and depict  
27 shared heritability and regulations by relevance correlation. Our method improves power upon  
28 existing approaches by associating SNPs with context-specific regulatory elements to assess  
29 heritability enrichments and by explicitly prioritizing gene regulations underlying relevant tissues.  
30 Experiments on GWAS of six phenotypes show that SpecVar can improve heritability enrichment,  
31 accurately detect relevant tissues, and reveal causal regulations. Furthermore, SpecVar correlates  
32 the relevance patterns for pairs of phenotypes and better reveals shared heritability and regulations  
33 of phenotypes than existing methods. Studying GWAS of 206 phenotypes in UK-Biobank  
34 demonstrates that SpecVar leverages the context-specific regulatory network atlas to prioritize  
35 phenotypes' relevant tissues and shared heritability for biological and therapeutic insights. SpecVar  
36 provides a powerful way to interpret SNPs via context-specific regulatory networks and is available  
37 at <https://github.com/AMSSwanglab/SpecVar>.

38

39

## 40 Introduction

41 Genome-Wide Association Studies (GWAS) have gained a great success to identify thousands of  
42 genetic variants significantly associated with a variety of human complex phenotypes. Interpretation  
43 of those genetic variants holds the key to biological mechanism discovery and personalized  
44 medicine practice. However, this task is hindered by the genetic architecture that the heritability is  
45 distributed across SNPs of the whole genome with linkage disequilibrium (LD), cumulatively  
46 affecting complex traits. By quantifying the contribution of true polygenic signal considering  
47 linkage disequilibrium, LD Score regression (LDSC) provides a widely appreciated method to  
48 estimate heritability (B. K. Bulik-Sullivan et al., 2015) and genetic correlation (B. Bulik-Sullivan  
49 et al., 2015) from GWAS summary statistics.

50  
51 Another obstacle to genetic variant interpretation is that SNPs contribute to phenotype through gene  
52 regulatory networks in certain cellular contexts, i.e., causal tissues or cell types. Those tissues are  
53 characterized by different types of epigenetic data, which give the active regions of the genome that  
54 interact with transcription factors (TF) to regulate gene expression. Stratified LDSC (S-LDSC)  
55 extends LDSC and can estimate the partitioned heritability enrichment in the functional categories  
56 (Finucane et al., 2015). The categories can be non-specific genome annotations (such as coding,  
57 UTR, promoter, and intronic regions) and context-specific regulatory regions called from chromatin  
58 data of different cell types, such as DNase-I hypersensitive sites from DNase-seq data, accessible  
59 peaks from ATAC-seq data, histone marker or TF binding sites from ChIP-seq data (LDSC-AAP  
60 and LDSC-SAP). Using expression data, the functional categories can be alternatively constructed  
61 by the 100-kb windows around the transcribed regions of specifically expressed genes (LDSC-SEG)  
62 (Hilary K. Finucane et al., 2018). Essentially, these strategies summarize the high dimensional SNP  
63 signals from the whole genome into partitioned heritability enrichments and successfully identify  
64 relevant cellular tissues for many phenotypes (Finucane et al., 2015).

65  
66 The rapid increase of multi-modal data resources, especially matched gene expression, chromatin  
67 states, and TF binding sites (i.e., measured on the same sample), offers an exciting opportunity to  
68 construct better functional categories for estimating heritability enrichment. One efficient way is to  
69 integrate large-scale epigenomic and transcriptomic data spanning diverse human contexts to infer  
70 regulatory networks (Duren et al., 2017). Those regulatory networks provide rich context-specific  
71 information and usually comprise TFs, regulatory elements (REs), and target genes (TGs). Recently,  
72 we developed the PECA2 model to infer regulatory network from paired expression and chromatin  
73 accessibility data (Duren et al., 2017; Duren et al., 2020). The inferred regulatory networks have  
74 been used to identify the master regulators in stem cell differentiation (Li et al., 2019) and to  
75 interpret conserved regions for the non-model organisms (Xin et al., 2020). Non-coding genetic  
76 variants can be interpreted in the regulatory networks on how they cooperatively affect complex  
77 traits through gene regulation in certain tissues or cell types. For example, genetic variants in the  
78 regulatory network of cranial neural crest cells are elucidated on how they affect human facial  
79 morphology (Feng et al., 2021). RSS-NET utilizes gene regulatory networks of multiple contexts  
80 and shows better tissue enrichment estimation by decomposing the total effect of a SNP through  
81 TF-TG regulations (Zhu et al., 2021) and HiChIP RE-TG regulations (Ma et al., 2022). And the  
82 phenotype-associated SNPs often function in a tissue- or cell-type-specific manner (Westra &

83 Franke, 2014). The advances in constructing regulatory networks and interpreting genetic variants  
84 with regulatory networks enlighten us to 1) assemble a more comprehensive context-specific  
85 regulatory network atlas by using paired expression and accessibility data across diverse cellular  
86 contexts; 2) build context-specific regulatory categories by focusing on RE's specificity of  
87 regulatory networks; 3) systematically identify enriched tissues or cell types, shared heritability (van  
88 Rheenen et al., 2019), and the underlying gene regulations of phenotypes.

89

90 Specifically, we proposed SpecVar to first leverage the publicly available paired expression and  
91 chromatin accessibility data in ENCODE and ROADMAP to systematically construct context-  
92 specific regulatory networks of 77 human contexts, covering major cell types and germ layer  
93 lineages. This atlas served as a valuable resource for genetic variants interpretation in multi-cellular  
94 contexts. SpecVar then used this atlas to construct regulatory categories in the genome. The  
95 heritability enrichment of GWAS was shown to be significantly improved by our context-specific  
96 regulatory categories. Based on the heritability enrichment and P-value in our regulatory categories,  
97 SpecVar defined the relevance score to give the context-specific representation of the GWAS. We  
98 showed that, for a single phenotype, the relevance score of SpecVar could identify relevant tissues  
99 more efficiently; and for multiple phenotypes, SpecVar could use relevance correlation to reveal  
100 shared heritability, common relevant tissues, and underlying gene regulations. These results showed  
101 that SpecVar is promising to serve as a tool for post-GWAS analysis.

102

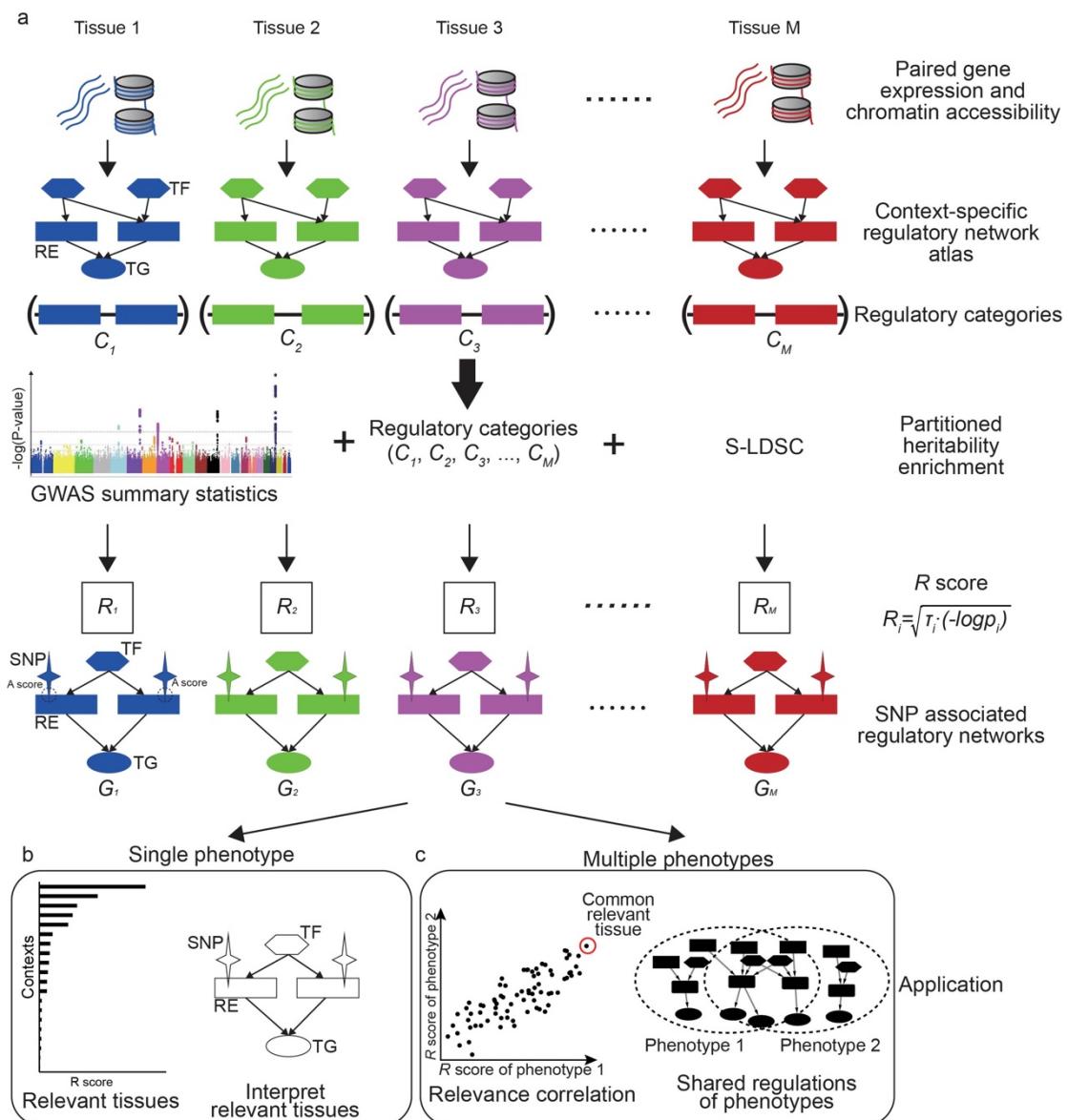
## 103 Results

### 104 Overview of SpecVar method

105 SpecVar assembled a context-specific regulatory network atlas and built the context-specific  
106 representation (relevance score and SNP-associated regulatory network) of GWAS summary  
107 statistics based on heritability enrichment. **Fig. 1** summarized the major steps of SpecVar to  
108 construct context-specific regulatory network atlas and regulatory categories, calculate heritability  
109 enrichment and SNP-associated regulatory network, and investigate interpretable relevant tissues  
110 and relevance correlation.

111

112 We first reconstructed regulatory networks of  $M$  ( $M=77$  in this paper) contexts. Each network is  
113 represented by a set of relations between TF and RE and between RE and TG. The  $M$  contexts  
114 included samples from all three germ layers, such as “frontal cortex” (ectoderm), “fetal thymus”  
115 (mesoderm), and “body of pancreas” (endoderm), which ensured the wide coverage and system-  
116 level enrichment (**Fig. S1**). The context-specific regulatory networks were extracted based on the  
117 specificity of REs in each context's regulatory network compared to other contexts, considering the  
118 hierarchical relationship of  $M$  contexts (**Methods, Table S1**). The REs in the  $i$ -th context-specific  
119 regulatory network were pooled to form a regulatory category  $C_i$  in the genome, which restricted  
120 the annotation to context-specific REs associated with active binding TFs and nearby regulated TGs  
121 (**Fig. 1a**). Our atlas leads to  $M$  regulatory categories,  $C_1, C_2, \dots, C_M$  of SpecVar. Given GWAS  
122 summary statistics, the  $M$  regulatory categories allowed partitioned heritability enrichment analysis  
123 by S-LDSC. For a phenotype, S-LDSC modeled genome-wide polygenic signal, partitioned SNPs  
124 into categories with different contributions for heritability, and considered SNP's linkage  
125 disequilibrium with the following polygenic model:



126

127 Fig. 1. Overview of SpecVar. (a) SpecVar constructs an atlas of context-specific regulatory networks and regulatory  
 128 networks. Then SpecVar represents GWAS summary statistics into relevance score and SNP-associated regulatory  
 129 subnetworks. (b) For a single phenotype, SpecVar can use relevance score and SNP-associated regulatory  
 130 subnetworks to identify and interpret relevant tissues. (c) For multiple phenotypes, based on relevance score,  
 131 SpecVar can reveal relevance correlation, common relevant tissues, and shared regulations.

132

133

$$E(\chi_j^2) = N \sum_i \tau_i l(j, i) + Na + 1 \quad (1)$$

134 Here  $\chi_j^2$  was the marginal association of SNP  $j$  from GWAS summary statistics;  $N$  was the  
 135 sample size;  $l(j, i) = \sum_{k \in C_i} r_{jk}^2$  was the LD score of SNP  $j$  in the  $i$ -th regulatory category  $C_i$ ,  
 136 where  $r_{jk}$  was the correlation between SNP  $j$  and SNP  $k$  in population;  $a$  measured the  
 137 contribution of confounding biases; and  $\tau_i$  represented the heritability enrichment of SNPs in  $C_i$ .  
 138 S-LDSC estimated the P-value  $p_i$  for the heritability enrichment (Finucane et al., 2015).

139

140 We defined the relevance score ( $R_i$ ) of this phenotype to  $i$ -th context (Fig. 1a) as follows by  
 141 combining the enrichment score and statistical significance (P-value):

142 
$$R_i = \sqrt{\tau_i \cdot (-\log p_i)} \quad (2)$$

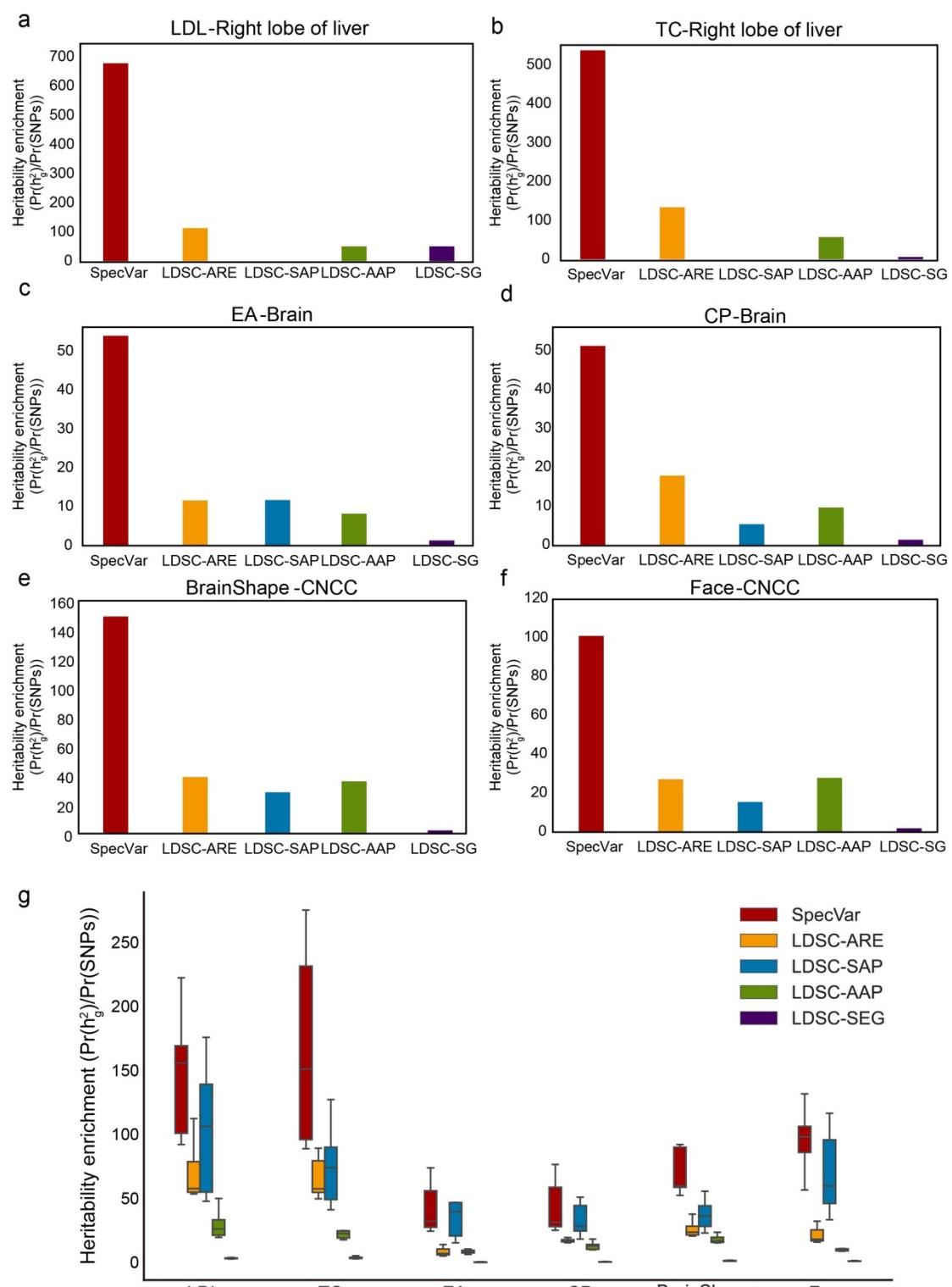
143 The relevance score ( $R$  score) provided a decision trade-off between the heritability enrichment  
144 and P-value resulting from a hypothesis test. It offered a new robust means to rank and select  
145 relevant tissues for a given phenotype (Xiao et al., 2014).

146  
147 Meanwhile, SpecVar associated SNPs with context-specific regulatory networks for biological  
148 interpretation. We defined an association score ( $A$  score) to prioritize the REs by combining its  
149 regulatory strength and association significance with the phenotype (averaged  $-\log P$  of SNPs  
150 located near the RE and down-weighted by their LD scores and distance to this RE). We extracted  
151 the REs with significant  $A$  scores ( $P \leq 0.05$ ), as well as their directly linked upstream TFs,  
152 downstream TGs, and associated SNPs, to form the SNP-associated regulatory subnetwork (**Fig. 1a, Methods**).  
153 Given GWAS summary statistics of a phenotype, SpecVar obtained  $M$  SNP-associated  
154 regulatory subnetworks,  $G_1, G_2, \dots, G_M$ , allowing to interpret relevant tissues by SNP's regulation  
155 mechanism.

156  
157 The relevance score to diverse human contexts and SNP-associated regulatory networks allowed  
158 SpecVar to perform post-GWAS analysis. For a single phenotype, the  $R$  scores indicated the  
159 relevance of this phenotype to  $M$  contexts, which could be used to identify relevant tissues. Then in  
160 the relevant tissues, we could investigate the SNP-associated regulatory subnetwork to interpret the  
161 relevance (**Fig. 1b, Methods**). For multiple phenotypes, we could correlate the  $R$  score vectors in  
162 multiple contexts to define relevance correlation (Hilary K. Finucane et al., 2018). The relevance  
163 correlation might give insights into the association of phenotypes since SpecVar could further  
164 interpret the relevance correlation between two phenotypes by common relevant tissues and the  
165 overlapped SNP-associated regulatory subnetwork in common relevant tissues (**Fig. 1c, Methods**).  
166

### 167 **Context-specific regulatory networks improve heritability enrichment**

168 We first designed experiments to show that the context-specific regulatory networks could improve  
169 heritability enrichment. We collected GWAS summary statistics of six phenotypes, including two  
170 lipid phenotypes (Willer et al., 2013): low-density lipoprotein (LDL) and total cholesterol (TC); two  
171 human intelligent phenotypes (Lee et al., 2018): educational attainment (EA) and cognitive  
172 performance (CP); and two craniofacial bone phenotypes: brain shape (Naqvi et al., 2021)  
173 (BrainShape) and facial landmark point distances (Xiong et al., 2019) (Face). We used these six  
174 phenotypes as a benchmark since their relevant tissues have been studied and partially known: lipid  
175 phenotypes are associated with the liver for its key role in lipid metabolism (Nguyen et al., 2008);  
176 human intelligent phenotypes are associated with brain tissues (Goriounova & Mansvelder, 2019);  
177 Face and BrainShape had shared heritability in cranial neural crest cells (CNCC) (Naqvi et al., 2021).  
178 We compared our context-specific regulatory networks with four alternative methods of functional  
179 categories: all regulatory elements (ARE), all accessible peaks (AAP), specifically accessible peaks  
180 (SAP) (Finucane et al., 2015), and specifically expressed genes (Hilary K. Finucane et al., 2018)  
181 (SEG) (**Methods**).  
182  
183



184

185 Fig. 2. (a) The heritability enrichment of LDL in the “right lobe of liver” by five regulatory categories methods. (b)  
 186 The heritability enrichment of TC in the “right lobe of liver” by five regulatory categories methods. (c) The  
 187 five brain tissues’ averaged heritability enrichment of EA by five regulatory categories methods. (d) The five brain tissues’  
 188 averaged heritability enrichment of CP by five regulatory categories methods. (e) The heritability enrichment of  
 189 BrainShape in “CNCC” by five regulatory categories methods. (f) The heritability enrichment of Face in “CNCC”  
 190 by five regulatory categories methods. (g) The heritability enrichment of top 10 tissues for each of the five  
 191 regulatory categories.

192

193 First, we showed that SpecVar could achieve higher heritability enrichment in the relevant tissues

194 than other methods. For LDL and TC, SpecVar obtained the highest heritability in their relevant  
195 tissue “right lobe of liver” than the other four methods (**Fig. 2a, b**). For EA and CP, they were  
196 relevant to brain tissues: “frontal cortex”, “cerebellum”, “caudate nucleus”, “Ammon’s horn” and  
197 “putamen”. SpecVar obtained the highest averaged heritability enrichment in these five brain tissues  
198 than the other four methods (**Fig. 2c, d**). For BrainShape and Face, SpecVar obtained a higher  
199 heritability enrichment in their relevant context “CNCC” than the other four methods (**Fig. 2e, f**).  
200 Second, except for the known relevant tissues, these complex traits may be relevant to other contexts.  
201 So, for every method, we ranked the heritability enrichment to get the top 10 contexts and used the  
202 top contexts’ heritability enrichment to compare the ability of these five methods to explain  
203 heritability in certain tissues or cell types. SpecVar also showed the best performance of heritability  
204 enrichment among the five methods (**Fig. 2g**). Taking BrainShape for example, SpecVar achieved  
205 significantly higher heritability enrichment (averaged heritability enrichment 96.13) than LDSC-  
206 ARE (26.77,  $P = 3.42 \times 10^{-3}$ ), LDSC-SAP (42.92,  $P = 1.85 \times 10^{-2}$ ), LDSC-SAP (20.34,  $P =$   
207  $1.84 \times 10^{-3}$ ), and LDSC-SEG (2.25,  $P = 3.05 \times 10^{-4}$ ). We found specificity could significantly  
208 improve the heritability enrichment. Among the five methods in our comparison, SpecVar and  
209 LDSC-SAP are categories based on the specificity of LDSC-ARE and LDSC-AAP, respectively.  
210 SpecVar showed significantly higher heritability enrichment than LDSC-ARE and LDSC-SAP  
211 showed significantly higher heritability enrichment than LDSC-AAP (**Fig. 2g**). For BrainShape,  
212 SpecVar obtained averaged heritability enrichment of 96.31 of the top 10 contexts, which was  
213 significantly higher than LDSC-ARE (averaged heritability enrichment 26.77,  $P = 3.42 \times 10^{-3}$ );  
214 LDSC-SAP obtained average heritability enrichment of 42.92, and LDSC-AAP’s averaged  
215 heritability enrichment was 20.34 ( $P = 2.68 \times 10^{-3}$ ). The other five phenotypes showed a similar  
216 improvement (**Fig. 2g**).  
217

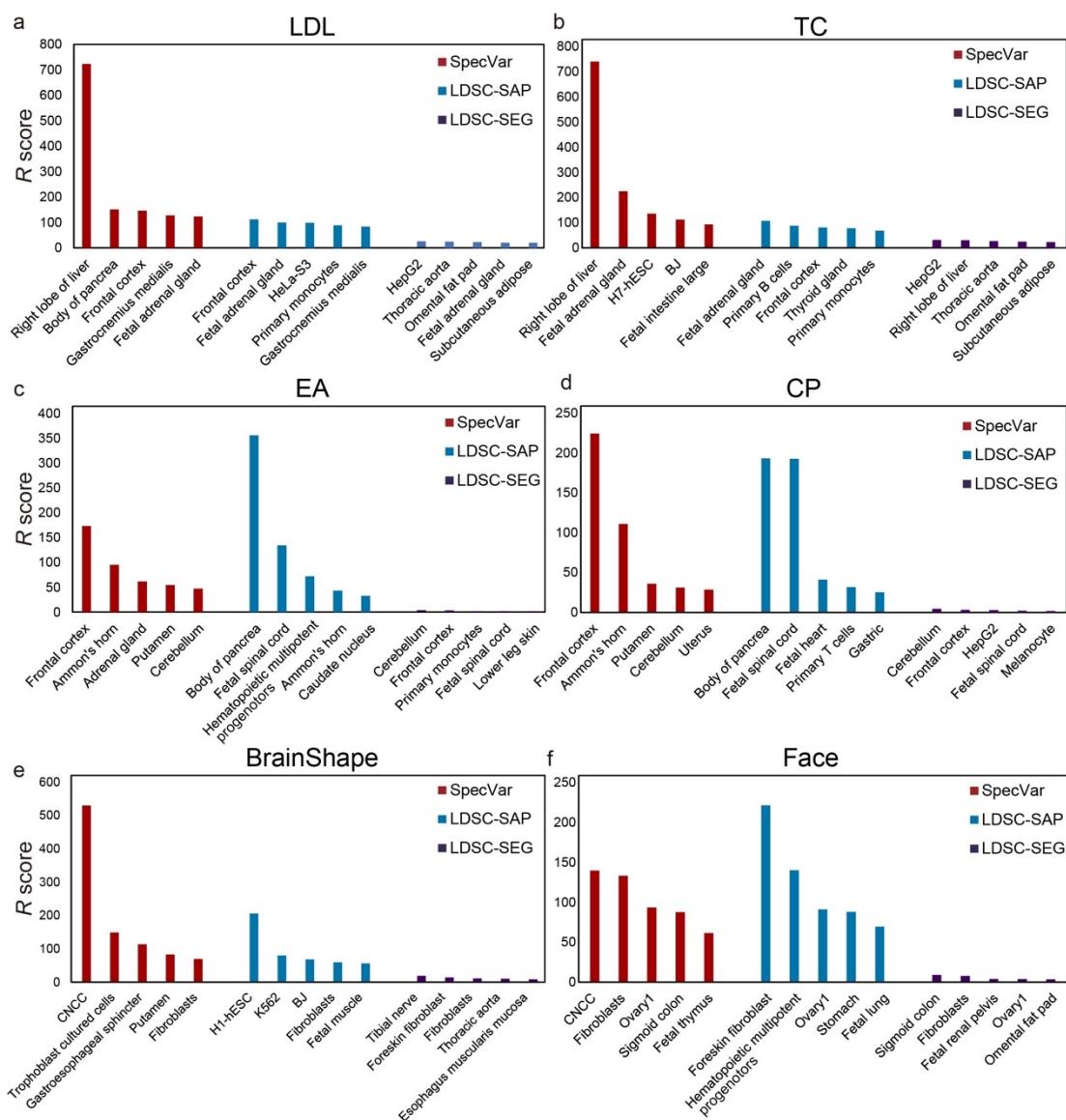
218 In summary, the experiment on six phenotypes’ GWAS summary statistics proved that SpecVar  
219 achieved the best performance in explaining the heritability of phenotypes. This demonstrated the  
220 power of integrating expression and chromatin accessibility data and considering contexts’  
221 specificity.  
222

### 223 **SpecVar can accurately reveal relevant tissues for phenotypes**

224 After establishing that SpecVar could use the context-specific regulatory networks to improve  
225 heritability enrichment, we next showed that for given phenotype, SpecVar could use *R* scores  
226 identify relevant tissues more accurately than other methods of functional categories. In this  
227 experiment, we also used the above six phenotypes with their known relevant tissues as a benchmark  
228 and compared SpecVar to the other two specificity-based methods: LDSC-SAP and LDSC-SEG  
229 (**Methods**).  
230

Trait	Sample size	Significant SNP number	SpecVar identified relevant tissues
LDL	173,082	3,077	Right lobe of liver
TC	187,365	4,169	Right lobe of liver, Fetal adrenal gland
EA	1070,751	30,519	Frontal cortex, Ammon’s horn, Adrenal gland
CP	257,841	13,732	Frontal cortex, Ammon’s horn
BrainShape	19,644	38,630	CNCC, Trophoblast cultured cells
Face	10,115	495	CNCC, Fibroblast

230 Table 1. The total sample size, number of significant SNPs, and SpecVar identified relevant tissues of six phenotypes.



231  
232 Fig. 3. The top 5 relevant tissues ranked by the relevant score of SpecVar, LDSC-SAP, and LDSC-SEG for (a) LDL,  
233 (b) TC, (c) EA, (d) CP, (e) BrainShape, and (f) Face. Compared to LDSC-SAP and LDSC-SEG, SpecVar identified  
234 relevant tissue more accurately and stably.

235  
236 For two lipid phenotypes, SpecVar revealed that both LDL and TC were most significantly relevant  
237 to the “right lobe of liver” (Fig. 3a, b, Table 1), which was consistent with the existing reports that  
238 the liver plays a central role in lipid metabolism, serving as the center for lipoprotein uptake,  
239 formation, and export to the circulation (Jha et al., 2018; Nguyen et al., 2008). SpecVar found TC  
240 was significantly relevant to the “fetal adrenal gland” and the adrenal cortex has been revealed to  
241 play an important role in lipid metabolism (Boyd et al., 1983). However, LDSC-SAP and LDSC-  
242 SEG failed to prioritize liver tissue as the significant relevant tissue. For LDL, LDSC-SAP identified  
243 the “frontal cortex” to be the most relevant tissue. LDSC-SEG identified the most relevant tissue to  
244 be “HepG2”, which was human hepatoma cell lines, but the relevance score was not significant (Fig.  
245 3a, Table S2). For TC, LDSC-SAP identified the “fetal adrenal gland” and LDSC-SEG obtained  
246 “HepG2” with an insignificant relevance score (Figure 3b, Table S2).

247

248 For two human intelligent phenotypes, SpecVar prioritized the “frontal cortex” to be the most  
249 relevant tissue for both EA and CP (**Fig. 3c, d, Table 1**). “Frontal cortex” is the cerebral cortex  
250 covering the front part of the frontal lobe and is implicated in planning complex cognitive behavior,  
251 personality expression, decision making, and moderating social behavior (Gabrieli et al., 1998;  
252 Yang & Raine, 2009). There were five tissues (“frontal cortex”, “Ammon’s horn”, “cerebellum”,  
253 “putamen”, “caudate nucleus”) from the brain in our atlas and they were significantly higher ranked  
254 by SpecVar’s relevance score than non-brain tissues for EA (Wilcoxon Rank-Sum test,  $P =$   
255  $6.07 \times 10^{-7}$ , **Fig. 3c**) and CP ( $P = 8.00 \times 10^{-6}$ , **Fig. 3d**). In comparison, for EA, LDSC-SAP  
256 prioritized brain tissues to be higher ranked than non-brain tissues, but with a less significant P-  
257 value ( $P = 2.28 \times 10^{-3}$ , **Fig. 3c, Table S2**). LDSC-SEG could not rank brain tissues to be higher  
258 than non-brain tissues ( $P = 0.64$ , **Fig. 3c, Table S2**). For CP, LDSC-SAP failed to rank brain tissues  
259 as the most relevant tissues ( $P = 0.06$ , **Fig. 3d, Table S2**), and LDSC-SEG identified brain tissues  
260 to be more relevant than non-brain tissues but with a less significant P-value ( $P = 3.18 \times 10^{-3}$ ,  
261 **Fig. 3d, Table S2**).

262

263 For both Face and BrainShape, SpecVar identified cranial neural crest cell (CNCC) as the most  
264 relevant context (**Fig. 3e, f, Table 1**). CNCC is a migratory cell population in early human  
265 craniofacial development that gives rise to the peripheral nervous system and many non-neural  
266 tissues such as smooth muscle cells, pigment cells of the skin, and craniofacial bones, which make  
267 it much more related to facial morphology and brain shape than the other 76 contexts (Cordero et  
268 al., 2011; “Neural crest makes a face,” 2008). Face morphology and brain shape were also revealed  
269 to share heritability in CNCC (Naqvi et al., 2021). But the other two methods failed to identify  
270 CNCC as the most relevant context. For BrainShape, LDSC-SAP identified “H1-hESC” and LDSC-  
271 SEG identified “tibial nerve” to be the most relevant tissue (**Fig. 3e, Table S2**). For Face, LDSC-  
272 SAP and LDSC-SEG identified “foreskin” and “sigmoid colon” to be the most relevant tissues,  
273 respectively (**Fig. 3f, Table S2**).

274

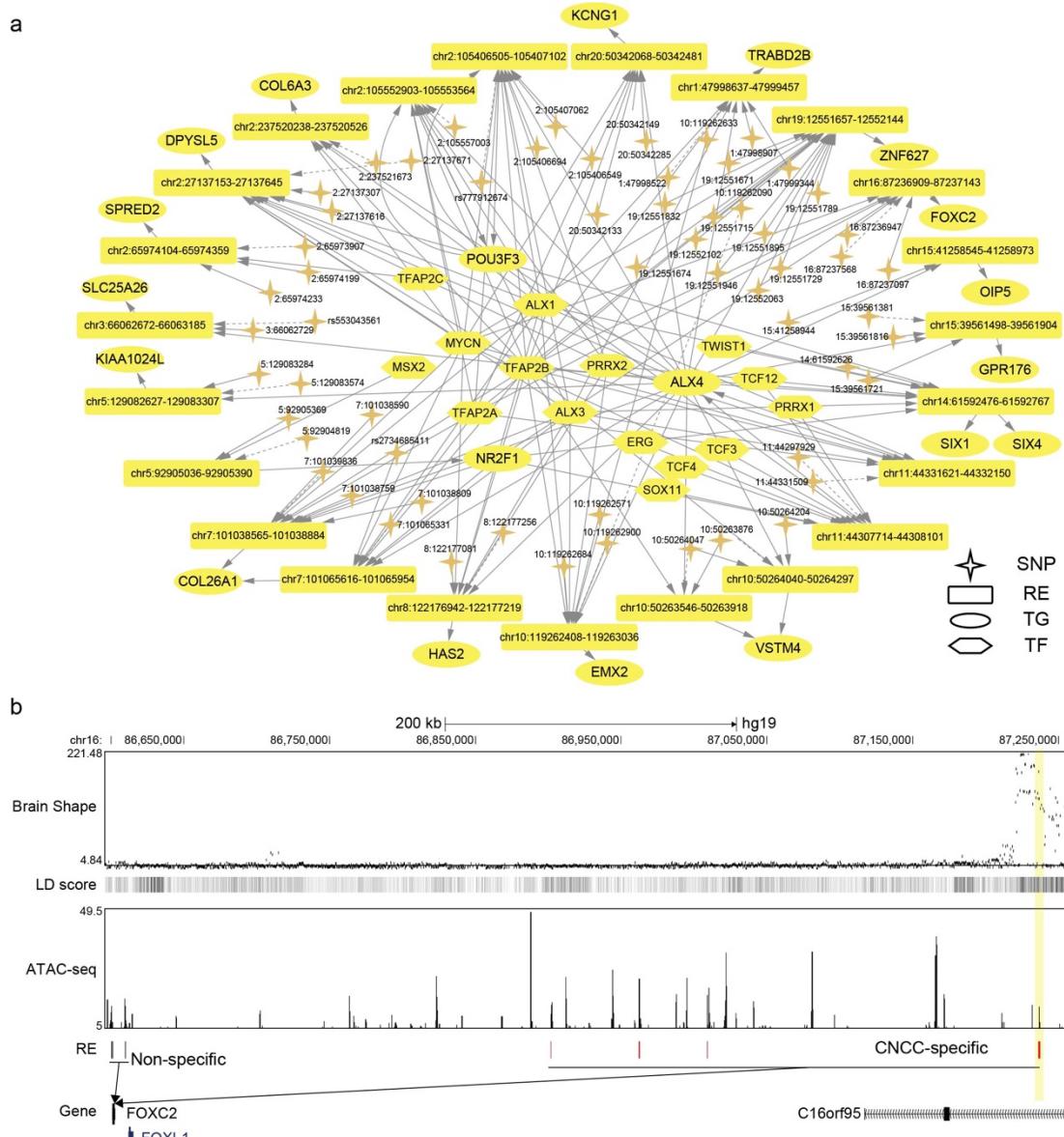
275 After identifying the relevant tissues, SpecVar could further interpret the relevance by extracting  
276 SNP-associated regulatory subnetwork (**Methods**). For example, we obtained BrainShape’s SNP-  
277 associated regulatory subnetwork in CNCC (**Fig. 4a**). There were 62 SNPs associated with 24 REs,  
278 73 TFs, and 52 TGs. The TGs were tightly involved with brain development. For example, *POU3F3*  
279 is a well-known transcription factor involved in the development of the central nervous system and  
280 is related to many neurodevelopmental disorders (Blok et al., 2019). *EMX2* is expressed in the  
281 developing cerebral cortex and involved in the patterning of the rostral brain (Cecchi & Boncinelli,  
282 2000). *FOXC2* is a member of the FOX family, which were modular competency factors for facial  
283 cartilage (Xu et al., 2018), and its mutation is linked to the cleft palate (Bahuau et al., 2002). By  
284 GWAS study, *FOXC2* was previously found to be associated with brain shape by its nearest  
285 significant SNP “16:86714715” (Naqvi et al., 2021). However, in CNCC, we did not find any  
286 accessible peaks that overlapped with this SNP. Instead, we found a CNCC-specific RE that  
287 regulated *FOXC2* in a locus of the 650k downstream. GWAS revealed the SNPs in this region had  
288 a strong association with brain shape and had high LD with each other (**Fig. 4b**). Our CNCC-specific  
289 regulations further prioritized only two SNPs (“16:87237097”, “16:87236947”) located in this  
290 CNCC-specific RE, which may influence the expression of *FOXC2* and the brain shape phenotypes.  
291 This example showed the power of SpecVar to interpret the genetic variants’ association to

292 phenotypes with detailed regulatory networks in relevant tissues.

293

294 In summary, we evaluated SpecVar's ability to identify relevant tissues using six well-studied  
295 phenotypes as the gold standard by comparison with the functional categories of LDSC-SAP and  
296 LDSC-SEG. The results showed that SpecVar could identify relevant tissues more accurately and  
297 stably and meanwhile provide detailed regulations to interpret the relevance to tissues.

298



299

300 Fig 4. (a) The BrainShape's SNP-associated regulatory subnetwork in CNCC. The dash arrows indicate significant  
301 SNPs that are not located in RE but near this RE. (b) SNP associated regulation of *FOXC2*. There is a group of  
302 significant SNPs of BrainShape that is located in the 650k downstream of *FOXC2* and they are with high linkage  
303 disequilibrium. SpecVar prioritizes SNPs located in a CNCC-specific RE as causal genetic variants affecting brain  
304 shape through regulation of *FOXC2*.

305

### 306 SpecVar reveals the association of multiple phenotypes by relevance correlation

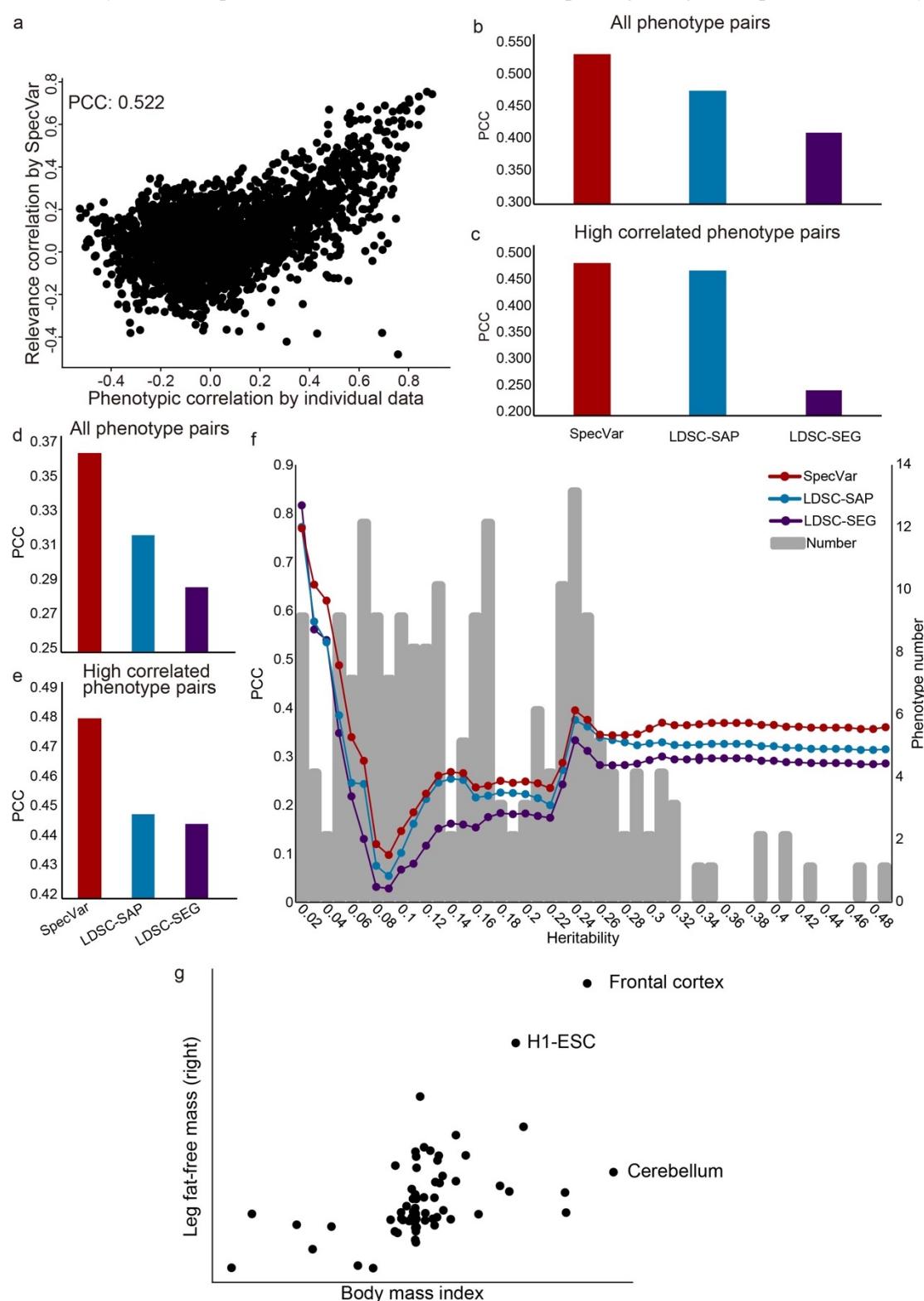
307 SpecVar's accurate and robust relevance to tissues enlightens us to define the relevance correlation  
308 of two phenotypes by Spearman correlation of their *R* scores (**Methods**). The relevance correlation  
309 might approximate phenotypic correlation since if two phenotypes are correlated, their relevance to

310 human contexts will also be correlated. We used two GWAS datasets with phenotypic correlation  
311 computed from individual phenotypic data as the gold standard and compared SpecVar to two other  
312 methods LDSC-SAP and LDSC-SEG.

313  
314 The first dataset was GWAS of 78 distances on the human face (Xiong et al., 2019). Based on  
315 summary statistics, we computed the relevance correlation of 3,003 pairs of distances with SpecVar,  
316 LDSC-SAP, and LDSC-SEG. We compared the relevance correlation with phenotypic correlation  
317 from individual phenotypic data and computed the Pearson coefficient correlation (PCC, **Methods**)  
318 to evaluate the performance of these three methods. SpecVar's relevance correlation showed the  
319 best performance in approximating phenotypic correlation (**Fig. 5a, b**, PCC=0.522), which  
320 outperformed the other three methods: LDSC-SAP PCC=0.467 (**Fig. 5b**), LDSC-SEG PCC=0.405  
321 (**Fig. 5b**). We also evaluated the ability to approximate the phenotypic correlation of highly  
322 correlated phenotypes. By setting the threshold of phenotypic correlation to be 0.4, we obtained the  
323 363 highly correlated phenotype pairs of facial landmark distances and compared the three methods  
324 based on their performance on these pairs of phenotypes. We found SpecVar also performed best  
325 with PCC 0.467, which was the largest among the three methods: LDSC-SAP PCC=0.454, LDSC-  
326 SEG PCC=0.245 (**Fig. 5c**). We used the mean square error as a metric to evaluate the performance  
327 (**Methods**) and SpecVar was also the best among the three methods (**Fig. S2**).  
328

329 The second GWAS dataset was from UK-Biobank. There were 4,313 GWAS in UK-Biobank, from  
330 which we selected 206 high-quality GWAS summary statistics of 12 classes (**Table S3, Methods**).  
331 We applied SpecVar and the other two methods to obtain the relevance correlations among these  
332 206 phenotypes and used the phenotypic correlation computed from individual data as validation.  
333 First, SpecVar performed best in the approximation of phenotypic correlation (PCC=0.360),  
334 followed by LDSC-SAP (PCC=0.315) and LDSC-SEG (PCC=0.285) (**Fig. 5d, Fig. S3a**). For highly  
335 correlated phenotypes, SpecVar's relevance correlation was also closest to phenotypic correlation  
336 (**Fig. 5e, Fig. S3b**). We found that the heritability of these 206 phenotypes was quite variable. For  
337 example, “100630” (Rose wine intake) had a heritability of  $6.52 \times 10^{-3}$ , and “5257\_irnt” (Corneal  
338 resistance factor right) had a heritability of 0.336. So, we checked if the heritability would influence  
339 the quality of relevance correlation. To do this, we set different thresholds of heritability and  
340 obtained a subset of phenotypes for each threshold. Then for the phenotype subset of each  
341 heritability threshold, we computed the PCC between relevance correlation and phenotypic  
342 correlation. For almost all the thresholds of heritability, SpecVar showed the best performance of  
343 PCC (**Fig. 5f, Fig. S3c**), and the smallest variance regarded heritability among these three methods  
344 (**Fig. S3d, e**). This means that the relevance correlation of SpecVar could estimate phenotypic  
345 correlation more accurately and robustly. SpecVar can interpret the relevance correlation by the  
346 common relevant tissues and shared regulations of two phenotypes. For example, body mass index  
347 and leg fat-free mass (right) were correlated with a phenotypic correlation of 0.697. SpecVar  
348 obtained a relevance correlation of 0.602, while LDSC-SAP obtained a relevance correlation of  
349 0.342 and LDSC-SEG obtained a relevance correlation of 0.437. SpecVar further revealed that these  
350 two phenotypes were correlated because they were both relevant to the “frontal cortex” (**Fig. 5g**).  
351 Body mass index has been reported to be related to frontal cortex development (Laurent et al., 2020)  
352 and relevant to the reduced and thin frontal cortex (Islam et al., 2018; Shaw et al., 2018). Obesity  
353 and fat accumulation are also revealed to be associated with the frontal cortex (Gluck et al., 2017;

354 Kakoschke et al., 2019). SpecVar further extracted these two phenotypes' SNP-associated regulatory  
 355 networks in the "frontal cortex" and found their SNP-associated networks were significantly  
 356 overlapped. The significant overlap was observed at SNP, RE, TG, and TF levels:  $P = 8.17 \times 10^{-63}$  for SNPs,  $P = 1.38 \times 10^{-47}$  for REs,  $P = 5.96 \times 10^{-25}$  for TGs, and  $P = 8.23 \times 10^{-25}$  for TFs (Fig. S4). The shared regulatory network was involved with body weight  
 357 and obesity. For example, in the brain, *SH2B1* enhances leptin signaling and leptin's anti-obesity  
 358 and obesity. For example, in the brain, *SH2B1* enhances leptin signaling and leptin's anti-obesity  
 359



360

361 Fig. 5. The scatter plot of true phenotypic correlation and relevance correlation by SpecVar. Each point means a pair  
362 of facial distances. (b) For all phenotype pairs of facial distances, the PCC between phenotypic correlation and  
363 relevance correlation of three methods. (c) For highly correlated phenotype pairs of facial distances, the PCC  
364 between phenotypic correlation and relevance correlation of three methods. (d) For all pairs of UKBB phenotypes,  
365 the PCC between phenotypic correlation and relevance correlation of three methods. (e) For highly correlated pairs  
366 of UKBB phenotypes, the PCC between phenotypic correlation and relevance correlation of three methods. (f) For  
367 UKBB phenotype pairs with different heritability thresholds, the PCC between phenotypic correlation and relevance  
368 correlation of four methods. (g) Scatter plot of  $R$  scores across 77 human contexts of body mass index and leg fat-  
369 free mass (right).

370

371 action, which is associated with the regulation of energy balance, body weight, and glucose  
372 metabolism (Rui, 2014).

373

374 Through the application of relevance correlation to two datasets with the gold standard of  
375 phenotypic correlation, we concluded that SpecVar can use the accurate relevance score to define  
376 relevance correlation, which could better estimate phenotypic correlation and could reveal shared  
377 heritability with common relevant tissues and overlapped context-specific regulatory networks.

378

379

## 380 Discussion

381 In this paper, we introduced the context-specific regulatory network, which integrated paired gene  
382 expression and chromatin accessibility data, to construct context-specific regulatory categories for  
383 better interpretation of GWAS data. SpecVar was developed as a tool to interpret genetic variants of  
384 GWAS summary statistics. The key message is that integrating chromatin accessibility and gene  
385 expression data into context-specific regulatory networks can provide better regulatory categories  
386 for heritability enrichment (Gazal et al., 2019). SpecVar is based on the popular model S-LDSC  
387 (Finucane et al., 2015), which includes 52 function categories as the baseline model. In addition,  
388 we showed extending the functional categories from non-context-specific regions to context-  
389 specific regions could improve the heritability enrichment, which is consistent with other studies  
390 based on gene expression (Hilary K. Finucane et al., 2018) and ChIP-seq (van de Geijn et al., 2020)  
391 data.

392

393 SpecVar outperformed the existing methods in three points. First, SpecVar defined relevance score  
394 based on both heritability enrichment and P-value. Because of the variability in the number of REs  
395 in the context-specific regulatory networks (Table S4), using only heritability enrichment or P-value  
396 will not give a stable estimation of the relevance of phenotype to tissues. For example, in the  
397 experiment of identifying six phenotypes' relevant tissues, heritability could select most relevant  
398 tissues for LDL and TC to be the "right lobe of liver" but failed to get correct tissues for other  
399 phenotypes (Fig. S5). P-value could obtain correct tissues for CP ("frontal cortex") and BrainShape  
400 (CNCC) but failed to get correct tissues for LDL, TC, EA, and Face (Fig. S6). By combining  
401 heritability enrichment and P-value into  $R$  score, SpecVar could prioritize correct relevant tissues  
402 for all the six phenotypes (Fig. 3). Like the  $R$  score-based relevance correlation, we could use the  
403 heritability enrichment and P-value to compute relevance correlation (Fig. S7a, b). We found  
404 heritability enrichment and P-value would give larger MSE (Fig. S7c, e) and lower PCC (Fig. S7d,  
405 f) than the  $R$  score, which showed that SpecVar's  $R$  score can achieve a better approximation of

406 phenotypic correlation. Those comparisons showed that the  $R$  score was a good metric to evaluate  
407 tissue's relevance to the phenotype. Second, SpecVar's regulatory categories had advantages over  
408 the existing functional categories to explain heritability. The context-specific regulatory networks  
409 formed regulatory categories enable better heritability enrichment than other methods (**Fig. 2**). The  
410 regulatory categories of SpecVar can be used to calculate  $R$  scores to identify relevant tissues more  
411 accurately than other methods (**Fig. 3**). And the  $R$  score of SpecVar can also be used to compute  
412 relevance correlation to better approximate phenotypic correlation than other methods when we do  
413 not have comprehensive phenotype measurement in each individual (**Fig. 5**). Third, with the  
414 constructed context-specific regulatory network atlas, SpecVar could further interpret the relevant  
415 tissue by SNP-associated regulatory networks (**Fig. 4**) and interpret relevance correlation by  
416 common relevant tissues and shared SNP-associated regulations in relevant tissues (**Fig. 5g, Fig.**  
417 **S4**). These three aspects made SpecVar an interpretable tool for heritability enrichment, identifying  
418 relevant tissues, and accessing associations of phenotypes.

419  
420 Based on the accurate and highly interpretable relevant tissue identification, the relevance  
421 correlation of SpecVar provides us with another perspective of associations between two phenotypes:  
422 if two phenotypes are correlated, their relevance to human contexts will also be correlated. This  
423 rationale is independent of genetic correlation, which is the proportion of variance that two  
424 phenotypes share due to genetic causes and can be estimated with GWAS summary statistics by  
425 LDSC-GC (B. Bulik-Sullivan et al., 2015). When using measured phenotype value correlation as  
426 the gold standard of phenotype correlation, we found that SpecVar performed better when the  
427 heritability of phenotype was low while LDSC-GC performed better when the heritability was high  
428 (**Fig. S8a, b**). This indicated that the integration of relevance correlation and genetic correlation  
429 might give a better estimation of phenotypic correlation. We validated this idea by regressing  
430 phenotypic correlation on relevance correlation and genetic correlation in two GWAS datasets. For  
431 the phenotypes of facial distances, if we only use relevance correlation to regress phenotypic  
432 correlation, the coefficient of determination ( $R$  square) was 0.2720; if we only used genetic  
433 correlation, the  $R$  square was 0.0002; if we used the linear combination of relevance correlation and  
434 genetic correlation to regress phenotypic correlation, the  $R$  square was 0.2765, which was  
435 significantly higher than that only with SpecVar ( $F$  test of  $R$  square increase,  $P \leq 1.77 \times 10^{-5}$ ) or  
436 only with LDSC-GC ( $P \leq 5.27 \times 10^{-213}$ ); and if we used a product (non-linear combination) of  
437 relevance correlation and genetic correlation, the  $R$  square was much higher: 0.2911 (**Fig. S8c, d**).  
438 And for 206 phenotypes of UK-BioBank, if we only used relevance correlation, the  $R$  square was  
439 0.1289; if we only used genetic correlation, the  $R$  square was 0.5614; if we used the linear  
440 combination of relevance correlation and genetic correlation to regress phenotypic correlation, the  
441  $R$  square was 0.5927, which was significantly higher than that only with SpecVar ( $P \leq$   
442  $2.20 \times 10^{-16}$ ) or only with LDSC-GC ( $P \leq 2.20 \times 10^{-16}$ ); and if we used a product of relevance  
443 correlation and genetic correlation, the  $R$  square was 0.7375, which was much improved (**Fig. S8e,**  
444 **f**). These results showed that relevance correlation and genetic correlation revealed the association  
445 of phenotypes in a complementary way.

446  
447 Our work can be improved in several aspects. The usage of context-specific regulatory networks  
448 contributed most to the improvement of SpecVar. But the context-specific regulatory networks can  
449 only cover part of the regulatory elements and genetic variants, which are highly essential and

450 representative. Higher-quality and more comprehensive regulatory networks will help obtain better  
451 representation. Currently, we built the atlas of regulatory networks of 77 human contexts and only  
452 included CNCC in the early developmental stage, which was far from complete. We expect more  
453 developmental stages will be included with multi-omics data from ENCODE (Consortium et al.,  
454 2020) and GTEx (Consortium, 2020). On the other hand, the 77 human contexts were tissues and  
455 cell lines. Single-cell-omics data (Han et al., 2020) will provide cell type level resolution and allows  
456 the extension of SpecVar to include broader cell types. The higher-quality and more comprehensive  
457 data will help SpecVar to construct better regulatory categories and improve interpretation. Lastly,  
458 it will be useful to extend the current approach using a model based on individual Whole Genome  
459 Sequencing data (Li et al., 2020).  
460

## 461 Methods

### 462 **Regulatory network inference with paired expression and chromatin accessibility data by 463 PECA2**

464 The regulatory networks were inferred by the PECA2 (Duren et al., 2020) model with paired  
465 expression and chromatin accessibility data. First, we collected paired expression and chromatin  
466 accessibility data of 76 human tissue or cell lines from ENCODE and ROADMAP (**Table S1**). Then  
467 with paired expression and accessibility data of each context, PECA2 calculated two scores. One  
468 was the trans-regulatory score. Specifically, PECA2 hypothesized that TF regulated the downstream  
469 TG by binding at REs. The trans-regulatory score was calculated by integrating multiple REs bound  
470 by a TF to regulate TG to quantify the regulatory strength of this TF on the TG. And PECA2 also  
471 considered a prior TF-TG correlation across external public data from ENCODE database. In detail,  
472 the TRS score  $TRS_{ij}$  of  $i$ -th TF and  $j$ -th TG was quantified as

$$473 \quad TRS_{ij} = \left( \sum_k B_{ik} O_k I_{kj} \right) \times 2^{|R_{ij}|} \times \sqrt{TF_i TG_j} \quad (3)$$

474 Here  $TF_i$  and  $TG_j$  were the expressions of the  $i$ -th TF and  $j$ -th TG.  $B_{ik}$  was the motif binding  
475 strength of  $i$ -th TF on  $k$ -th RE, which was defined as the sum of the binding strength of all the  
476 binding sites of  $i$ -th TF on  $k$ -th RE.  $O_k$  was the measure of accessibility for  $k$ -th RE.  $I_{kj}$   
477 represented the interaction strength between  $k$ -th RE and  $j$ -th TG, which was learned from the  
478 PECA model on diverse ENCODE cellular contexts (Duren et al., 2017; Duren et al., 2018).  $R_{ij}$   
479 was the expression correlation of  $i$ -th TF and  $j$ -th TG across diverse ENCODE samples. The  
480 significance of the TRS score was obtained by a background of randomly selected TF-TG pairs and  
481 the threshold of the TRS score was decided by controlling the false discovery rate (FDR) at 0.001.  
482

483 The other one was the cis-regulatory score to measure the regulatory strength of RE on a TG. The  
484 cis-regulatory score  $CRS_{kj}$  of  $k$ -th RE on  $j$ -th TG was quantified as

$$485 \quad CRS_{kj} = \left( \sum_i B_{ik} TRS_{ij} \right) \times I_{kj} \times O_k \quad (4)$$

486 We approximated the distribution of  $\log_2(1 + CRS_{kj})$  by a normal distribution and predicted RE-  
487 TG associations by selecting the RE-TG pairs that have P-value  $\leq 0.05$ .  
488

489 The output of PECA2 was a regulatory network with TFs, REs, and TGs as nodes and the regulations  
490 among them as edges. This procedure was applied to 76 human contexts with paired expression and  
491 chromatin accessibility data and obtained 76 regulatory networks. We noted that the regulatory  
492 network of early development stage CNCC was reconstructed recently (Feng et al., 2021) and we  
493 included the regulatory network of CNCC to form our regulatory network atlas of 77 human  
494 contexts.

495

#### 496 **Construction of context-specific regulatory network atlas**

497 The context-specific regulatory network was obtained based on the specificity of REs. In detail, we  
498 had 77 regulatory networks, and each regulatory network had a set of REs  $RE_i, 1 \leq i \leq 77$ . Firstly,  
499 we hierarchically clustered 77 contexts' the regulatory networks into 36 groups by trans-regulatory  
500 score (**Table S1**). Then for a given context, a RE was defined as a context-specific RE if it was not  
501 overlapped with REs of other contexts. Formally, the context-specific RE set of  $i$ -th context  $C_i$   
502 was defined as

$$503 C_i = \{RE_{ik} \in RE_i | RE_{ik} \notin RE_j, j \neq i\} \quad (5)$$

504 Here  $RE_{ik} \notin RE_j$  means  $RE_{ik}$  was not overlapped with any REs in  $RE_j$ :

$$505 RE_{ik} \notin RE_j \Leftrightarrow RE_{ik} \text{ is not overlapped with any } RE_{jl} \text{ in } RE_j \quad (6)$$

506 And we defined “overlapped” 1) for REs from contexts of the different groups, two REs were  
507 overlapped if their overlapping base ratio were over 50%; 2) for REs from contexts of the same  
508 group, two REs were overlapped if their overlapping base ratio were over 60%. The reason we used  
509 different “overlapped” criteria for REs from the same group and different groups was to retain  
510 group-specific REs. For example, for the brain tissues, we had five cell types: “Ammon’s horn”,  
511 “caudate nucleus”, “cerebellum”, “frontal cortex”, and “putamen”. If we defined RE’s specificity  
512 with stringent condition among these five brain cell types, many common brain REs would be lost.

513

514 Finally, the context-specific regulatory network was formed by specific REs and their directly linked  
515 upstream TFs and downstream TGs. And the context-specific RE sets  $C_i, 1 \leq i \leq 77$  gave the  
516 regulatory categories of SpecVar.

517

#### 518 **Heritability enrichment and $R$ score of GWAS summary statistics by SpecVar**

519 SpecVar used stratified LDSC (Finucane et al., 2015) to compute partitioning heritability  
520 enrichment. Under the linear additive model, S-LDSC models the causal SNP effect on phenotype  
521 as drawn from a distribution with mean zero and variance

$$522 \text{Var}(\beta_j) = \sum_i \tau_i 1_{\{j \in C_i\}} \quad (7)$$

523 And with the assumption that the LD of a category that is enriched for heritability will increase the  
524  $\chi^2$  statistic of a SNP more than the LD of a category that does not contribute to heritability, the  
525 expected  $\chi^2$  statistic is modeled as follows:

$$526 E(\chi_j^2) = N \sum_{C_i} \tau_i l(j, i) + Na + 1 \quad (8)$$

527 where  $N$  is the sample size,  $C_i$  denotes the regulatory category formed by the  $i$ -th context-  
528 specific regulatory network,  $\chi_j^2$  is the marginal association of SNP  $j$  from GWAS summary  
529 statistics,  $l(j, i) = \sum_{k \in C_i} r_{jk}^2$  is the LD score of SNP  $j$  in the  $i$ -th category,  $a$  measures the  
530 contribution of confounding biases and  $\tau_i$  represents heritability enrichment of SNPs in  $C_i$ . S-

531 LDSC estimates standard errors with a block jackknife and uses these standard errors to calculate  
532 the P-value  $p_i$  for the heritability enrichment (Finucane et al., 2015).

533  
534 To make a trade-off between heritability enrichment score and P-value resulting from a hypothesis  
535 test, we combined heritability enrichment and statistical significance (P-value) to define the  
536 relevance score ( $R_i$ ) of this phenotype to  $i$ -th context as follows:

537 
$$R_i = \sqrt{\tau_i \cdot (-\log p_i)} \quad (9)$$

538 The relevance score ( $R$  score) offered a new robust means to rank and select relevant tissue for a  
539 given phenotype (Xiao et al., 2014) (Fig. S5-7).

540  
541 **Four alternative methods to construct representations of GWAS summary statistics**  
542 Based on expression and chromatin accessibility data, there were four alternative methods for  
543 constructing regulatory categories: All Accessible Peaks (AAP), Specifically Accessible Peaks  
544 (SAP), Specifically Expressed Genes (SEG), and All Regulatory Elements (ARE).

545  
546 The AAP method used all the chromatin accessible peaks of each context to form a genome  
547 functional category, which was used for partitioned heritability enrichment analysis. The SAP  
548 method used the same rules of SpecVar above to obtain context-specifically accessible peaks of  
549 each context, and the context-specific peaks sets of  $M$  contexts formed functional categories of SAP.  
550 The SEG method was constructed by following the procedure in (H. K. Finucane et al., 2018). First,  
551 the t-statistics for differential expression of each gene in each of the  $M$  contexts were calculated.  
552 Then for each context, the top 10% genes ranked by t-statistic were selected, and the 100Kb  
553 windows around those top 10% genes were used to form a functional category. For the ARE method,  
554 we obtained all REs in the regulatory network of a context to be a functional category, and the RE  
555 sets of  $M$  contexts formed regulatory categories of ARE.

556  
557 We could conclude the relationship between the five methods: SpecVar, SAP, and SEG were  
558 methods based on specificity; SpecVar and SAP were based on the specificity of ARE and AAP,  
559 respectively. SpecVar and ARE used the expression and chromatin accessibility simultaneously;  
560 SAP and AAP only used the chromatin accessibility data; and SEG only used the gene expression  
561 data.

562  
563 After obtaining functional categories with these four alternate methods, we could also use S-LDSC  
564 to obtain heritability enrichment and define the  $R$  score representation of GWAS summary  
565 statistics with equations (8) and (9). We called them LDSC-AAP, LDSC-SAP, LDSC-SEG, and  
566 LDSC-ARE, respectively. We compared these four alternate methods with SpecVar.

567  
568 **Relevant tissue identification and relevance correlation analysis by SpecVar**  
569 SpecVar identified relevant tissues and defined relevance correlation based on  $R$  scores. The  $R$   
570 scores to  $M$  contexts could be aggregated into a context-specific vector representation of GWAS  
571 summary statistics:

572 
$$R = (R_1, R_2, \dots, R_M) \quad (10)$$

573 For a single phenotype, the  $R$  scores to  $M$  contexts could be used to get the relevant tissues. We

574 used six phenotypes to analyze the distribution of  $R$  scores and found that the  $R$  scores followed  
575 a Gaussian distribution (**Fig. S9**). We approximated the distribution of  $R$  to be Gaussian distribution  
576 and used the threshold P-value  $\leq 0.05$  to get the relevant tissues. This gave the relevant tissues of the  
577 six phenotypes (**Table 1**), which was consistent with prior knowledge.

578

579 For two phenotypes, such as phenotype  $p$  and phenotype  $q$ , we obtained their  $R$  score  
580 representations:

$$\begin{aligned} 581 \quad R^p &= (R_1^p, R_2^p, \dots, R_M^p) \\ 582 \quad R^q &= (R_1^q, R_2^q, \dots, R_M^q) \end{aligned} \quad (11)$$

583 Then the Spearman correlation of their  $R$  score representation was used to define the relevance  
584 correlation:

$$585 \quad \rho_g = \rho(R^p, R^q) = 1 - \frac{6 \sum_i [r(R_i^p) - r(R_i^q)]^2}{M * (M^2 - 1)} \quad (12)$$

586 Here  $r(R_i^p)$  and  $r(R_i^q)$  were the ranks of  $i$ -th context by the relevance score for the two  
587 phenotypes.

588

589 For two other specificity-based regulatory categories LDSC-SAP and LDSC-SEG, we also used  
590 their functional categories to compute heritability enrichment and P-value and defined the  $R$  score  
591 with equation (7-9). The  $R$  scores of LDSC-SAP and LDSC-SEG were used to obtain relevant  
592 tissues and relevance correlation.

593

#### 594 **Evaluation of relevant tissue identification and relevance correlation**

595 To evaluate the performance of the SpecVar and other methods, we used different datasets as the  
596 gold standard.

597

598 For the application to identify relevant tissues, we used six well-studied phenotypes that we had  
599 knowledge of the relevant tissues: two lipid phenotypes (LDL and TC) were relevant to the liver;  
600 two human intelligent phenotypes (EA and CP) were relevant to the brain; two craniofacial bone  
601 phenotypes (Face and BrainShape) were relevant to CNCC. We used different methods to identify  
602 relevant tissues of these six phenotypes and checked if they obtained the correct tissues.

603

604 For relevance correlation, we used the phenotypic correlation computed with individual phenotypic  
605 data as the gold standard. First, we computed the Pearson correlation coefficient (PCC) between  
606 relevance correlation and phenotypic correlation:

$$607 \quad PCC = \frac{\sum_{i,j \in P} (p_{ij} - \bar{p}_{ij})(p'_{ij} - \bar{p}'_{ij})}{\sqrt{\sum_{i,j \in P} (p_{ij} - \bar{p}_{ij})^2 \sum_{i,j \in P} (p'_{ij} - \bar{p}'_{ij})^2}} \quad (13)$$

608 Here  $P$  was the set of phenotypes, and  $N$  was the number of phenotype pairs;  $p_{ij}$  was the  
609 phenotypic correlation computed with individual phenotypic data, and  $p'_{ij}$  was the relevance  
610 correlation;  $\bar{p}_{ij}$  was the average of  $p_{ij}$ , and  $\bar{p}'_{ij}$  was the average of  $p'_{ij}$ . A larger PCC indicated  
611 better performance in approximating phenotypic correlation.

612

613 Another metric we used was the mean square error (MSE) between relevance correlation and  
614 phenotypic correlation:

615 
$$\text{MSE} = \frac{\sum_{i,j \in P} (p_{ij} - p'_{ij})^2}{N} \quad (14)$$

616 A smaller MSE indicated better performance in approximating phenotypic correlation.

617

## 618 **Extracting SNP-associated regulatory subnetworks in relevant tissues**

619 Given a phenotype's GWAS summary statistics and a context, SpecVar identified SNPs associated  
620 regulatory subnetwork by considering the following two factors: 1) the cis-regulatory score of SNP-  
621 associated RE should be large enough to indicate its importance in the regulatory network; 2) the  
622 risk signal of SNPs (i.e., P-value) on or near this RE should be large to indicate its association with  
623 phenotype. We combined these two factors to define the association score ( $A$  score) of SNP-  
624 associated REs.

625

626 First, the regulatory strength of  $k$ -th RE was measured by the maximum cis-regulatory score of this  
627 RE. Formally,

628 
$$C_k = \max_j CRS_{kj} \quad (15)$$

629 Here  $CRS_{kj}$  was the cis-regulatory score of  $k$ -th RE on  $j$ -th TG. For the  $k$ -th RE, the larger  $C_k$   
630 was, the more important this RE was in the regulatory network. Second, the risk score of GWAS  
631  $S_k$  for  $k$ -th RE was defined as the average of the -log(P-value) of SNPs located on or near this RE,  
632 which were down-weighted by their LD scores and distances to RE:

633 
$$S_k = \frac{1}{|P_k|} \sum_{l \in P_k} -\omega_l \cdot \log(p_l) \cdot e^{-\frac{d_{lk}}{d_0}} \quad (16)$$

634 Here  $P_k$  was the set of SNPs whose distances were less than 50Kb to the  $k$ -th RE and  $|P_k|$  was  
635 the total number of this SNP set;  $\omega_l$  (the reciprocal of LD score, downloaded at  
636 <https://data.broadinstitute.org/alkesgroup/LDSCORE/>) was the weight of the  $l$ -th SNP;  $p_l$  was p-  
637 value of the  $l$ -th SNP in summary statistics;  $d_{lk}$  was the base pair distance of the  $l$ -th SNP to  $k$ -th  
638 RE and  $d_0$  was a constant, which was set to be 5,000 as default. For the  $k$ -th RE, a larger value of  
639  $S_k$  indicated a stronger association with the given phenotype.

640

641 Finally, we obtained the association score ( $A$  score) of  $k$ -th RE by combining these two factors:

642 
$$A_k = \sqrt{C_k * S_k} \quad (17)$$

643 Every RE in the context-specific regulatory network was qualified by the  $A$  score. We used the  
644 GWAS of six phenotypes to analyze the distribution of  $A$  scores and found that the  $A$  scores  
645 followed a Gaussian distribution (Fig. S10). So, we hypothesized the distribution of  $A$  scores was  
646 Gaussian distribution and we selected the REs associated with the given phenotype by  $A$  scores'  
647 FDR threshold of 0.05. The prioritized REs, as well as their directly linked upstream TFs,  
648 downstream TGs, and the associated SNPs, formed the SNP-associated regulatory subnetwork.

649

650

## 651 **GWAS summary statistics of UK-Biobank**

652 The GWAS summary statistics of UK-Biobank were downloaded at <http://www.nealelab.is/uk->  
653 [biobank](http://www.nealelab.is/uk-biobank). There were 4,176 phenotypes and 11,372 GWAS summary statistics. We selected 206  
654 GWAS summary statistics (Table S3) based on the following conditions.

655 1. Excluding sex-specific and “raw” type GWAS.  
656 2. Sample size condition:  $N \geq 50,000$  and  $N_{control}, N_{case} \geq 10,000$  for binary and  
657 categorical phenotypes.  
658 3. Significant SNP number condition: the number of SNPs that pass the threshold of  $5 \times 10^{-8}$   
659 was not less than 500.  
660 4. Manually curation: removing duplicated phenotypes, “job”, “parent” and “sibling” associated  
661 phenotypes.

662

### 663 **Data and code available**

664 Codes and regulatory network resources are available at  
665 <https://github.com/AMSSwanglab/SpecVar>. Expression and chromatin accessibility data were  
666 summarized in Table S1. GWAS data used: GWAS summary statistics of LDL and TC were  
667 downloaded at <http://csg.sph.umich.edu/willer/public/lipids2013/>; GWAS summary statistics of EA  
668 (GCST006442), CP (GCST006572), BrainShape (GCST90012880-GCST90013164), and Face  
669 (GCST009464) were downloaded at GWAS catalog <https://www.ebi.ac.uk/gwas/summary-statistics>;  
670 GWAS summary statistics of UK-Biobank were downloaded at <http://www.nealelab.is/uk-biobank>.  
671 The LDSC genetic correlation and phenotypic correlation computed from individual phenotypic  
672 data were downloaded at <https://ukbb-rg.hail.is/>.

673

### 674 **Acknowledgments**

675 We acknowledge funding from the National Key Research and Development Program of China  
676 (2020YFA0712402), Strategic Priority Research Program of the Chinese Academy of Sciences  
677 [XDPB17], and the National Natural Science Foundation of China (grants 12025107, 11871463,  
678 and 11688101).

679

### 680 **Author contributions**

681 Y.W., and W.H.W. conceived and supervised the project. Z.F. designed the analytical approach and  
682 performed numerical experiments and data analysis. Z.D. contributed to the construction of  
683 regulatory networks. J.X., Q. Y., Y.H., B.S. contributed to interpreting biological insights. All  
684 authors wrote, revised, and contributed to the final manuscript.

685

### 686 **Declaration of interests**

687 The authors declare no competing interests.

688

### 689 **Reference**

690 Bahauau, M., Houdayer, C., Tredano, M., Soupre, V., Couderc, R., & Vazquez, M. P. (2002). FOXC2  
691 truncating mutation in distichiasis, lymphedema, and cleft palate. *Clinical Genetics*, 62(6),  
692 470-473. <https://doi.org/DOI 10.1034/j.1399-0004.2002.620608.x>  
693 Blok, L. S., Kleefstra, T., Venselaar, H., Maas, S., Kroes, H. Y., Lachmeijer, A. M. A., van Gassen, K. L.  
694 I., Firth, H. V., Tomkins, S., Bodek, S., Study, T. D. D. D., Ounap, K., Wojcik, M. H., Cunniff,  
695 C., Bergstrom, K., Powis, Z., Tang, S., Shinde, D. N., Au, C., . . . Fisher, S. E. (2019). De Novo  
696 Variants Disturbing the Transactivation Capacity of POU3F3 Cause a Characteristic  
697 Neurodevelopmental Disorder. *American Journal of Human Genetics*, 105(2), 403-412.

698 <https://doi.org/10.1016/j.ajhg.2019.06.007>

699 Boyd, G. S., McNamara, B., Suckling, K. E., & Tocher, D. R. (1983). Cholesterol metabolism in the  
700 adrenal cortex. *J Steroid Biochem*, 19(1C), 1017-1027. [https://doi.org/10.1016/0022-4731\(83\)90048-1](https://doi.org/10.1016/0022-4731(83)90048-1)

701 Bulik-Sullivan, B., Finucane, H. K., Anttila, V., Gusev, A., Day, F. R., Loh, P. R., Duncan, L., Perry, J. R.  
702 B., Patterson, N., Robinson, E. B., Daly, M. J., Price, A. L., Neale, B. M., Consortium, R.,  
703 Consortium, P. G., & Nervos, G. C. A. (2015). An atlas of genetic correlations across human  
704 diseases and traits. *Nature Genetics*, 47(11), 1236-+. <https://doi.org/10.1038/ng.3406>

705 Bulik-Sullivan, B. K., Loh, P. R., Finucane, H. K., Ripke, S., Yang, J., Schizophrenia Working Group of  
706 the Psychiatric Genomics, C., Patterson, N., Daly, M. J., Price, A. L., & Neale, B. M. (2015).  
707 LD Score regression distinguishes confounding from polygenicity in genome-wide  
708 association studies. *Nature Genetics*, 47(3), 291-295. <https://doi.org/10.1038/ng.3211>

709 Cecchi, C., & Boncinelli, E. (2000). Emx homeogenes and mouse brain development. *Trends  
710 Neurosci*, 23(8), 347-352. [https://doi.org/10.1016/s0166-2236\(00\)01608-8](https://doi.org/10.1016/s0166-2236(00)01608-8)

711 Consortium, E. P., Snyder, M. P., Gingeras, T. R., Moore, J. E., Weng, Z., Gerstein, M. B., Ren, B.,  
712 Hardison, R. C., Stamatoyannopoulos, J. A., Graveley, B. R., Feingold, E. A., Pazin, M. J.,  
713 Pagan, M., Gilchrist, D. A., Hitz, B. C., Cherry, J. M., Bernstein, B. E., Mendenhall, E. M.,  
714 Zerbino, D. R., . . . Myers, R. M. (2020). Perspectives on ENCODE. *Nature*, 583(7818), 693-  
715 698. <https://doi.org/10.1038/s41586-020-2449-8>

716 Consortium, G. T. (2020). The GTEx Consortium atlas of genetic regulatory effects across human  
717 tissues. *Science*, 369(6509), 1318-1330. <https://doi.org/10.1126/science.aaz1776>

718 Cordero, D. R., Brugmann, S., Chu, Y. N., Bajpai, R., Jame, M., & Helms, J. A. (2011). Cranial Neural  
719 Crest Cells on the Move: Their Roles in Craniofacial Development. *American Journal of  
720 Medical Genetics Part A*, 155a(2), 270-279. <https://doi.org/10.1002/ajmg.a.33702>

721 Duren, Z. N., Chen, X., Jiang, R., Wang, Y., & Wong, W. H. (2017). Modeling gene regulation from  
722 paired expression and chromatin accessibility data. *Proceedings of the National Academy of  
723 Sciences of the United States of America*, 114(25), E4914-E4923.  
724 <https://doi.org/10.1073/pnas.1704553114>

725 Duren, Z. N., Chen, X., Xin, J. X., Wang, Y., & Wong, W. H. (2020). Time course regulatory analysis  
726 based on paired expression and chromatin accessibility data. *Genome Research*, 30(4),  
727 622-634. <https://doi.org/10.1101/gr.257063.119>

728 Duren, Z. N., Chen, X., Zamanighomi, M., Zeng, W. W., Satpathy, A. T., Chang, H. Y., Wang, Y., &  
729 Wong, W. H. (2018). Integrative analysis of single-cell genomics data by coupled  
730 nonnegative matrix factorizations. *Proceedings of the National Academy of Sciences of  
731 the United States of America*, 115(30), 7723-7728.  
732 <https://doi.org/10.1073/pnas.1805681115>

733 Feng, Z. Y., Duren, Z. N., Xiong, Z. Y., Wang, S. J., Liu, F., Wong, W. H., & Wang, Y. (2021). hReg-  
734 CNCC reconstructs a regulatory network in human cranial neural crest cells and annotates  
735 variants in a developmental context. *Communications Biology*, 4(1). <https://doi.org/ARTN 442>

736 10.1038/s42003-021-01970-0

737 Finucane, H. K., Bulik-Sullivan, B., Gusev, A., Trynka, G., Reshef, Y., Loh, P. R., Anttila, V., Xu, H.,  
738 Zang, C. Z., Farh, K., Ripke, S., Day, F. R., Purcell, S., Stahl, E., Lindstrom, S., Perry, J. R. B.,  
739 Okada, Y., Raychaudhuri, S., Daly, M. J., . . . Consortium, R. (2015). Partitioning heritability  
740 741

742 by functional annotation using genome-wide association summary statistics. *Nature*  
743 *Genetics*, 47(11), 1228-+. <https://doi.org/10.1038/ng.3404>

744 Finucane, H. K., Reshef, Y. A., Anttila, V., Slowikowski, K., Gusev, A., Byrnes, A., Gazal, S., Loh, P.-R.,  
745 Lareau, C., Shores, N., Genovese, G., Saunders, A., Macosko, E., Pollack, S., Perry, J. R. B.,  
746 Buenrostro, J. D., Bernstein, B. E., Raychaudhuri, S., McCarroll, S., . . . The Brainstorm, C.  
747 (2018). Heritability enrichment of specifically expressed genes identifies disease-relevant  
748 tissues and cell types. *Nature Genetics*, 50(4), 621-629. <https://doi.org/10.1038/s41588-018-0081-4>

749 Finucane, H. K., Reshef, Y. A., Anttila, V., Slowikowski, K., Gusev, A., Byrnes, A., Gazal, S., Loh, P. R.,  
750 Lareau, C., Shores, N., Genovese, G., Saunders, A., Macosko, E., Pollack, S., Brainstorm, C.,  
751 Perry, J. R. B., Buenrostro, J. D., Bernstein, B. E., Raychaudhuri, S., . . . Price, A. L. (2018).  
752 Heritability enrichment of specifically expressed genes identifies disease-relevant tissues  
753 and cell types. *Nat Genet*, 50(4), 621-629. <https://doi.org/10.1038/s41588-018-0081-4>

754 Gabrieli, J. D., Poldrack, R. A., & Desmond, J. E. (1998). The role of left prefrontal cortex in language  
755 and memory. *Proc Natl Acad Sci U S A*, 95(3), 906-913.  
756 <https://doi.org/10.1073/pnas.95.3.906>

757 Gazal, S., Marquez-Luna, C., Finucane, H. K., & Price, A. L. (2019). Reconciling S-LDSC and LDAK  
758 functional enrichment estimates. *Nature Genetics*, 51(8), 1202-1204.  
759 <https://doi.org/10.1038/s41588-019-0464-1>

760 Gluck, M. E., Viswanath, P., & Stinson, E. J. (2017). Obesity, Appetite, and the Prefrontal Cortex.  
761 *Curr Obes Rep*, 6(4), 380-388. <https://doi.org/10.1007/s13679-017-0289-0>

762 Goriounova, N. A., & Mansvelder, H. D. (2019). Genes, Cells and Brain Areas of Intelligence. *Front*  
763 *Hum Neurosci*, 13, 44. <https://doi.org/10.3389/fnhum.2019.00044>

764 Han, X., Zhou, Z., Fei, L., Sun, H., Wang, R., Chen, Y., Chen, H., Wang, J., Tang, H., Ge, W., Zhou, Y.,  
765 Ye, F., Jiang, M., Wu, J., Xiao, Y., Jia, X., Zhang, T., Ma, X., Zhang, Q., . . . Guo, G. (2020).  
766 Construction of a human cell landscape at single-cell level. *Nature*, 581(7808), 303-309.  
767 <https://doi.org/10.1038/s41586-020-2157-4>

768 Islam, A. H., Metcalfe, A. W. S., MacIntosh, B. J., Korczak, D. J., & Goldstein, B. I. (2018). Greater  
769 body mass index is associated with reduced frontal cortical volumes among adolescents  
770 with bipolar disorder. *Journal of Psychiatry and Neuroscience*, 43(2), 120-130.  
771 <https://doi.org/10.1503/jpn.170041>

772 Jha, P., McDevitt, M. T., Gupta, R., Quiros, P. M., Williams, E. G., Gariani, K., Sleiman, M. B., Diserens,  
773 L., Jochem, A., Ulbrich, A., Coon, J. J., Auwerx, J., & Pagliarini, D. J. (2018). Systems Analyses  
774 Reveal Physiological Roles and Genetic Regulators of Liver Lipid Species. *Cell Syst*, 6(6),  
775 722-733 e726. <https://doi.org/10.1016/j.cels.2018.05.016>

776 Kakuschke, N., Lorenzetti, V., Caeyenberghs, K., & Verdejo-Garcia, A. (2019). Impulsivity and body  
777 fat accumulation are linked to cortical and subcortical brain volumes among adolescents  
778 and adults. *Scientific Reports*, 9. <https://doi.org/ARTN 2580>

779 10.1038/s41598-019-38846-7

780 Laurent, J. S., Watts, R., Adise, S., Allgaier, N., Chaarani, B., Garavan, H., Potter, A., & Mackey, S.  
781 (2020). Associations Among Body Mass Index, Cortical Thickness, and Executive Function  
782 in Children. *JAMA Pediatrics*, 174(2), 170-177.  
783 <https://doi.org/10.1001/jamapediatrics.2019.4708>

784 Lee, J. J., Wedow, R., Okbay, A., Kong, E., Maghzian, O., Zacher, M., Nguyen-Viet, T. A., Bowers, P.,

786 Sidorenko, J., Linner, R. K., Fontana, M. A., Kundu, T., Lee, C., Li, H., Li, R. X., Royer, R.,  
787 Timshel, P. N., Walters, R. K., Willoughby, E. A., . . . Consortiu, S. S. G. A. (2018). Gene  
788 discovery and polygenic prediction from a genome-wide association study of educational  
789 attainment in 1.1 million individuals. *Nature Genetics*, 50(8), 1112-+.  
790 <https://doi.org/10.1038/s41588-018-0147-3>

791 Li, L., Wang, Y., Torkelson, J. L., Shankar, G., Pattison, J. M., Zhen, H. H., Fang, F., Duren, Z., Xin, J.,  
792 Gaddam, S., Melo, S. P., Piekos, S. N., Li, J., Liaw, E. J., Chen, L., Li, R., Wernig, M., Wong,  
793 W. H., Chang, H. Y., & Oro, A. E. (2019). TFAP2C- and p63-Dependent Networks  
794 Sequentially Rearrange Chromatin Landscapes to Drive Human Epidermal Lineage  
795 Commitment. *Cell Stem Cell*, 24(2), 271-284 e278.  
796 <https://doi.org/10.1016/j.stem.2018.12.012>

797 Li, W., Duren, Z., Jiang, R., & Wong, W. H. (2020). A method for scoring the cell type-specific  
798 impacts of noncoding variants in personal genomes. *Proc Natl Acad Sci U S A*, 117(35),  
799 21364-21372. <https://doi.org/10.1073/pnas.1922703117>

800 Ma, S., Chen, X., Zhu, X., Tsao, P. S., & Wong, W. H. (2022). Leveraging cell-type-specific regulatory  
801 networks to interpret genetic variants in abdominal aortic aneurysm. *Proc Natl Acad Sci  
802 U S A*, 119(1). <https://doi.org/10.1073/pnas.2115601119>

803 Naqvi, S., Sleyp, Y., Hoskens, H., Indencleef, K., Spence, J. P., Bruffaerts, R., Radwan, A., Eller, R. J.,  
804 Richmond, S., Shriver, M. D., Shaffer, J. R., Weinberg, S. M., Walsh, S., Thompson, J.,  
805 Pritchard, J. K., Sunaert, S., Peeters, H., Wysocka, J., & Claes, P. (2021). Shared heritability  
806 of human face and brain shape. *Nature Genetics*. <https://doi.org/10.1038/s41588-021-00827-w>

807 Neural crest makes a face. (2008). *Development*, 135(23), e2306-e2306.  
808 <https://dev.biologists.org/content/develop/135/23/e2306.full.pdf>

809 Nguyen, P., Leray, V., Diez, M., Serisier, S., Le Bloc'h, J., Siliart, B., & Dumon, H. (2008). Liver lipid  
810 metabolism. *J Anim Physiol Anim Nutr (Berl)*, 92(3), 272-283.  
811 <https://doi.org/10.1111/j.1439-0396.2007.00752.x>

812 Rui, L. (2014). SH2B1 regulation of energy balance, body weight, and glucose metabolism. *World  
813 J Diabetes*, 5(4), 511-526. <https://doi.org/10.4239/wjd.v5.i4.511>

814 Shaw, M. E., Sachdev, P. S., Abhayaratna, W., Anstey, K. J., & Cherbuin, N. (2018). Body mass index  
815 is associated with cortical thinning with different patterns in mid- and late-life.  
816 *International Journal of Obesity*, 42(3), 455-461. <https://doi.org/10.1038/ijo.2017.254>

817 van de Geijn, B., Finucane, H., Gazal, S., Hormozdiari, F., Amariuta, T., Liu, X., Gusev, A., Loh, P. R.,  
818 Reshef, Y., Kichaev, G., Raychauduri, S., & Price, A. L. (2020). Annotations capturing cell  
819 type-specific TF binding explain a large fraction of disease heritability. *Hum Mol Genet*,  
820 29(7), 1057-1067. <https://doi.org/10.1093/hmg/ddz226>

821 van Rheenen, W., Peyrot, W. J., Schork, A. J., Lee, S. H., & Wray, N. R. (2019). Genetic correlations  
822 of polygenic disease traits: from theory to practice. *Nature Reviews Genetics*, 20(10), 567-  
823 581. <https://doi.org/10.1038/s41576-019-0137-z>

824 Westra, H. J., & Franke, L. (2014). From genome to function by studying eQTLs. *Biochim Biophys  
825 Acta*, 1842(10), 1896-1902. <https://doi.org/10.1016/j.bbadi.2014.04.024>

826 Willer, C. J., Schmidt, E. M., Sengupta, S., Peloso, G. M., Gustafsson, S., Kanoni, S., Ganna, A., Chen,  
827 J., Buchkovich, M. L., Mora, S., Beckmann, J. S., Bragg-Gresham, J. L., Chang, H. Y.,  
828 Demirkhan, A., Den Hertog, H. M., Do, R., Donnelly, L. A., Ehret, G. B., Esko, T., . . . Global

830 Lipids Genetics, C. (2013). Discovery and refinement of loci associated with lipid levels.  
831 *Nature Genetics*, 45(11), 1274-1283. <https://doi.org/10.1038/ng.2797>

832 Xiao, Y., Hsiao, T. H., Suresh, U., Chen, H. I., Wu, X., Wolf, S. E., & Chen, Y. (2014). A novel  
833 significance score for gene selection and ranking. *Bioinformatics*, 30(6), 801-807.  
834 <https://doi.org/10.1093/bioinformatics/btr671>

835 Xin, J., Hao, J., Chen, L., Zhang, T., Li, L., Chen, L., Zhao, W., Lu, X., Shi, P., & Wang, Y. (2020).  
836 ZokorDB: tissue specific regulatory network annotation for non-coding elements of  
837 plateau zokor. *Quantitative Biology*, 8(1), 43-50. <https://doi.org/10.1007/s40484-020-0195-4>

838 Xiong, Z. Y., Dankova, G., Howe, L. J., Lee, M. K., Hysi, P. G., de Jong, M. A., Zhu, G., Adhikari, K., Li,  
839 D., Li, Y., Pan, B., Feingold, E., Marazita, M. L., Shaffer, J. R., McAloney, K., Xu, S. H., Jin, L.,  
840 Wang, S. J., de Vrij, F. M. S., . . . VisiGen, I. V. T. G. (2019). Novel genetic loci affecting facial  
841 shape variation in humans. *eLife*, 8. <https://doi.org/ARTN> e49898  
842 10.7554/eLife.49898

843 Xu, P. F., Balczerski, B., Ciozda, A., Louie, K., Oralova, V., Huysseune, A., & Crump, J. G. (2018). Fox  
844 proteins are modular competency factors for facial cartilage and tooth specification.  
845 *Development*, 145(12). <https://doi.org/ARTN> dev165498  
846 10.1242/dev.165498

847 Yang, Y., & Raine, A. (2009). Prefrontal structural and functional brain imaging findings in antisocial,  
848 violent, and psychopathic individuals: a meta-analysis. *Psychiatry Res*, 174(2), 81-88.  
849 <https://doi.org/10.1016/j.psychresns.2009.03.012>

850 Zhu, X., Duren, Z., & Wong, W. H. (2021). Modeling regulatory network topology improves  
851 genome-wide analyses of complex human traits. *Nature Communications*, 12(1), 2851.  
852 <https://doi.org/10.1038/s41467-021-22588-0>

853

854

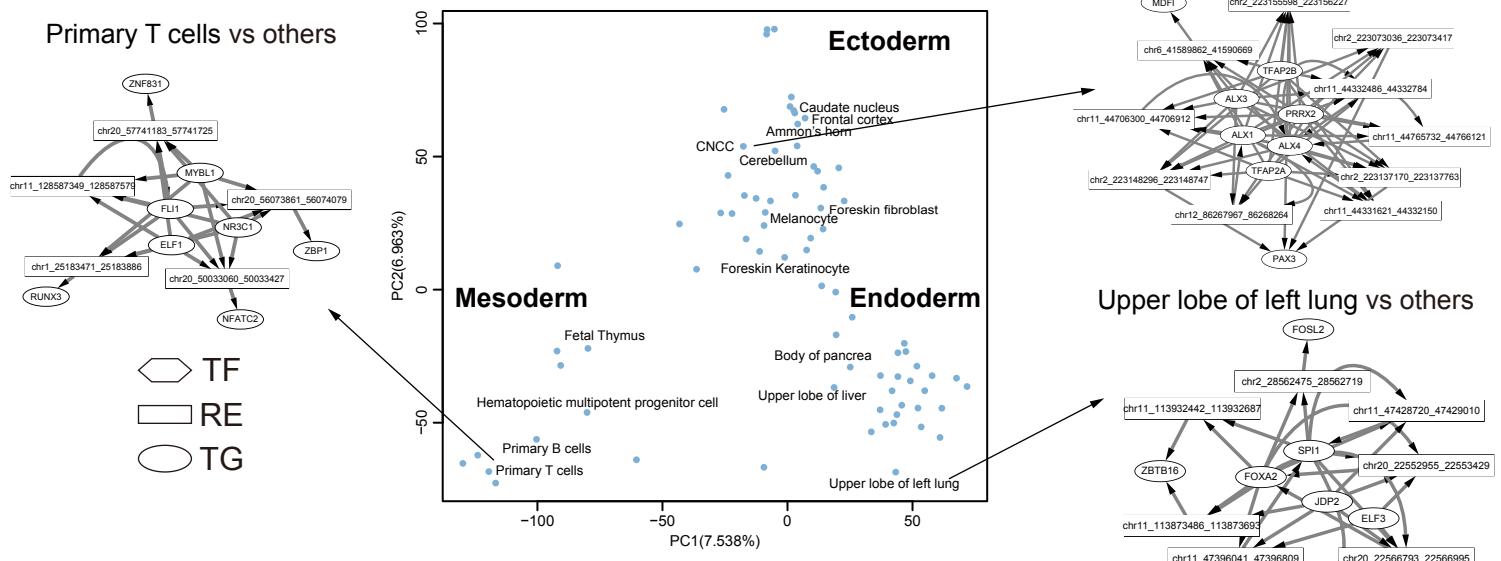


Fig. S1: PCA plot of regulatory network atlas of 77 human tissues. The TRS score across 77 tissues are used for PCA analysis

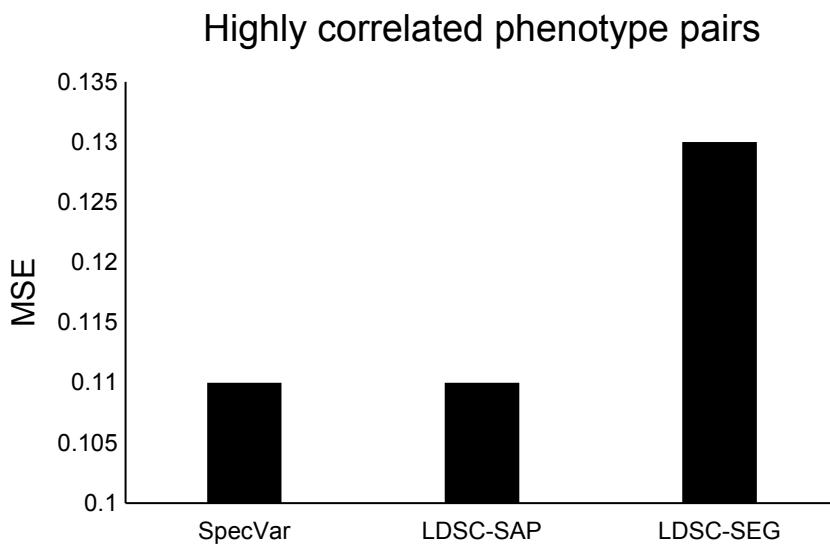
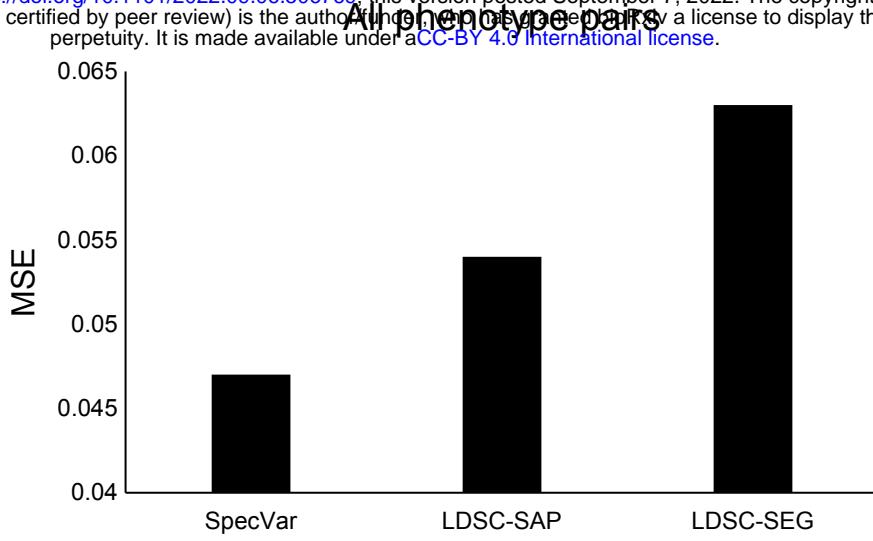
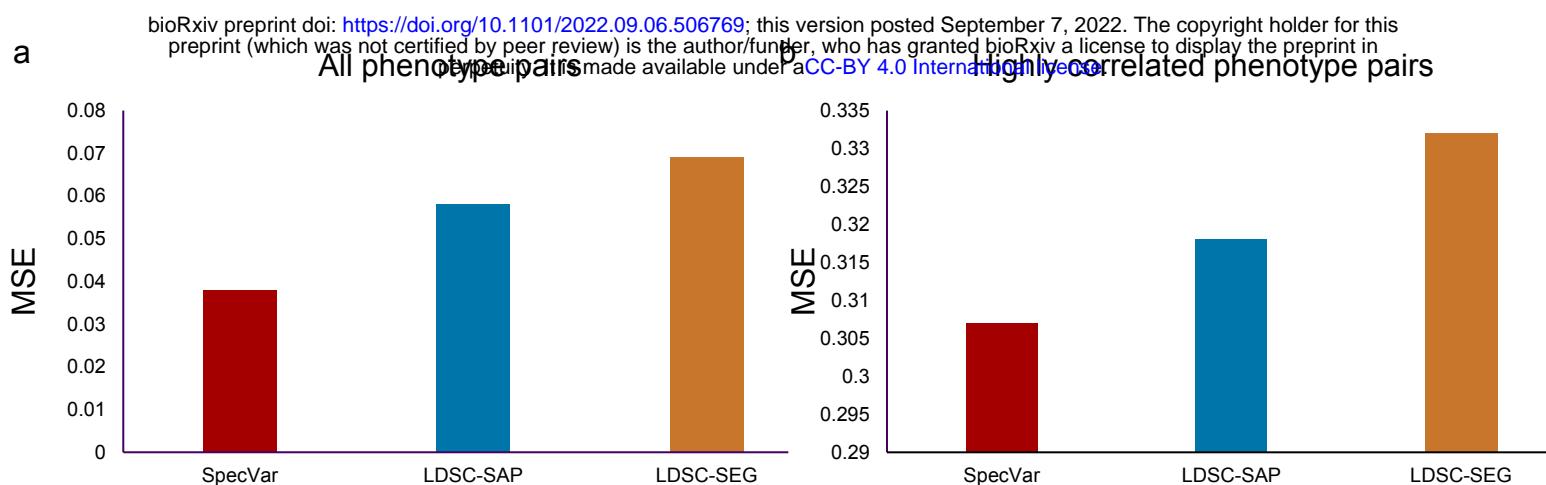
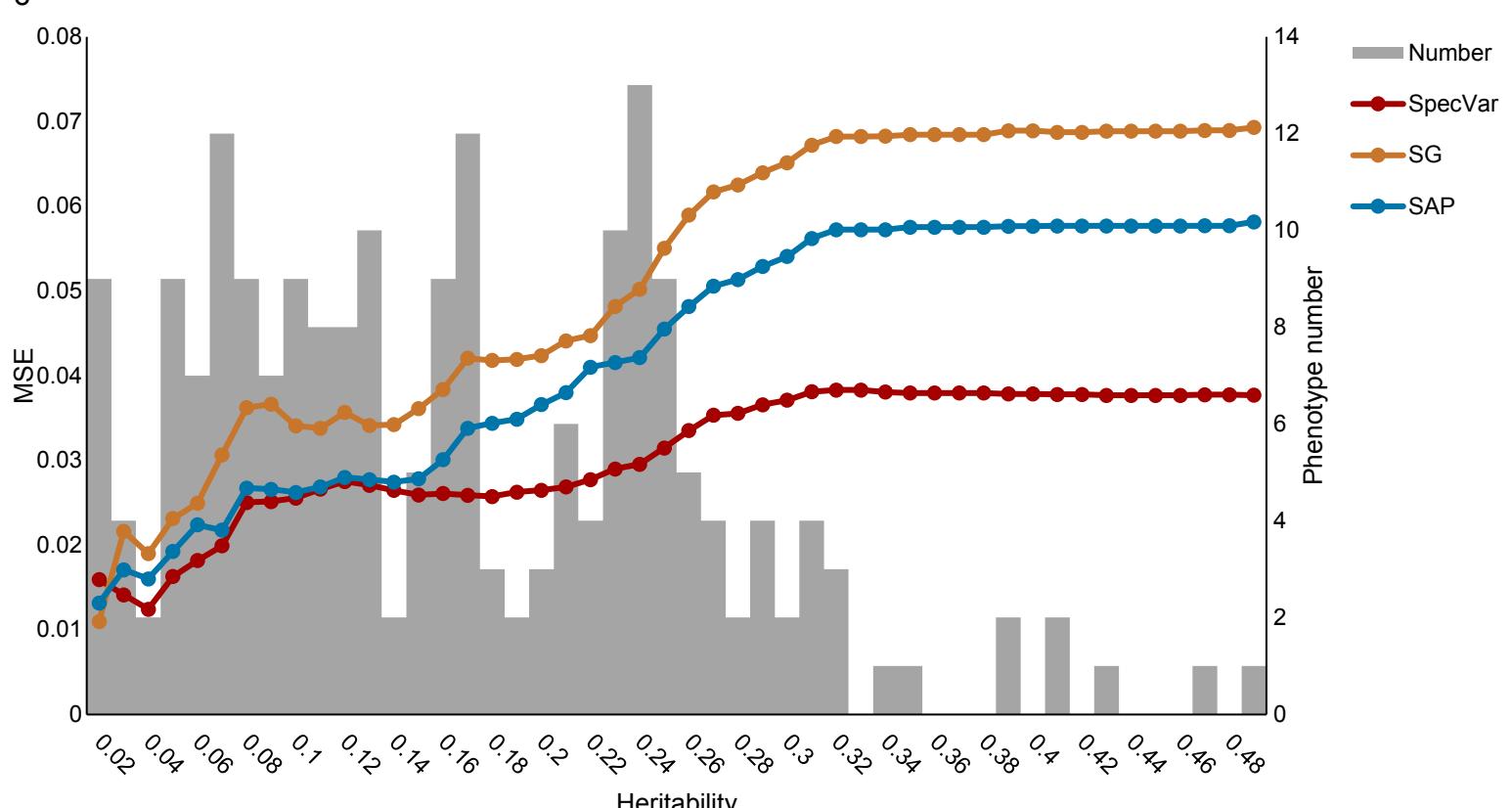


Fig. S2: (s). For all phenotype pairs of facial distances, the MSE between true phenotypic correlation and relevance correlation of SpecVar, LDSC-SAP, and LDSC-SEG. (f). For highly correlated phenotype pairs of facial distances, the MSE between true phenotypic correlation and estimated phenotypic correlation of SpecVar, LDSC-SAP, and LDSC-SEG.

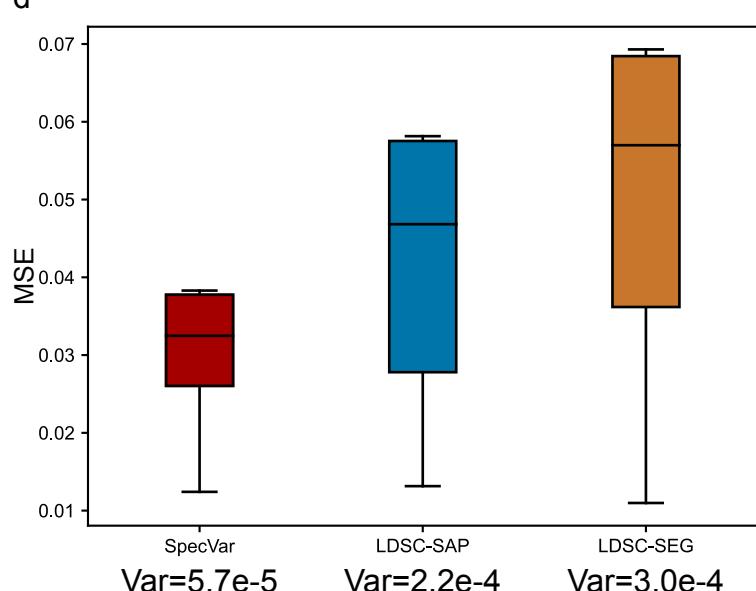
a



c



d



e

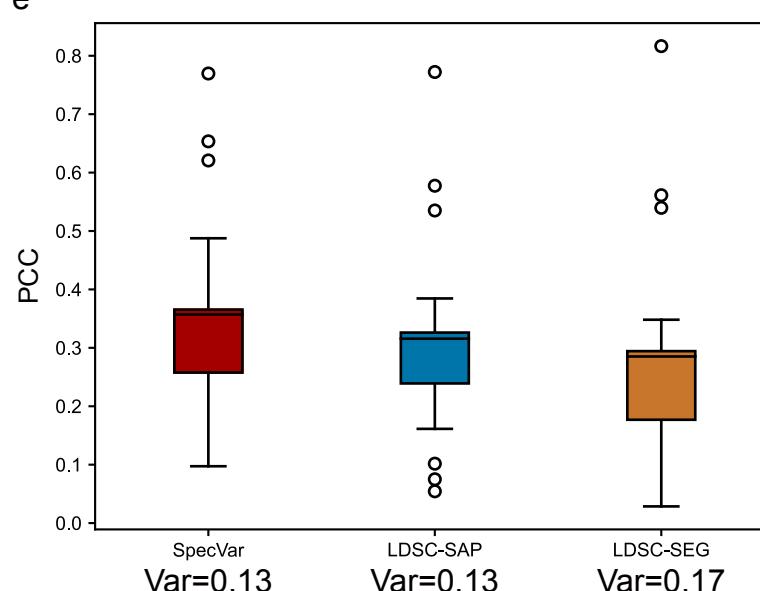


Fig. S3: (a). For all phenotype pairs of facial distances, the MSE between true phenotypic correlation and relevance correlation of three methods. (b). For highly correlated phenotype pairs of facial distances, the MSE between true phenotypic correlation and relevance correlation of three methods. (c) For UKBB phenotype pairs with different heritability thresholds, the MSE between true phenotypic correlation and relevance correlation of three methods. (d). Boxplot of relevance correlation MSE under different threshold of phenotype heritability. Specvar shows the smallest variance. (e). Boxplot of relevance correlation PCC under different threshold of phenotype heritability. Specvar and LDSC-SAP shows the smallest variance.

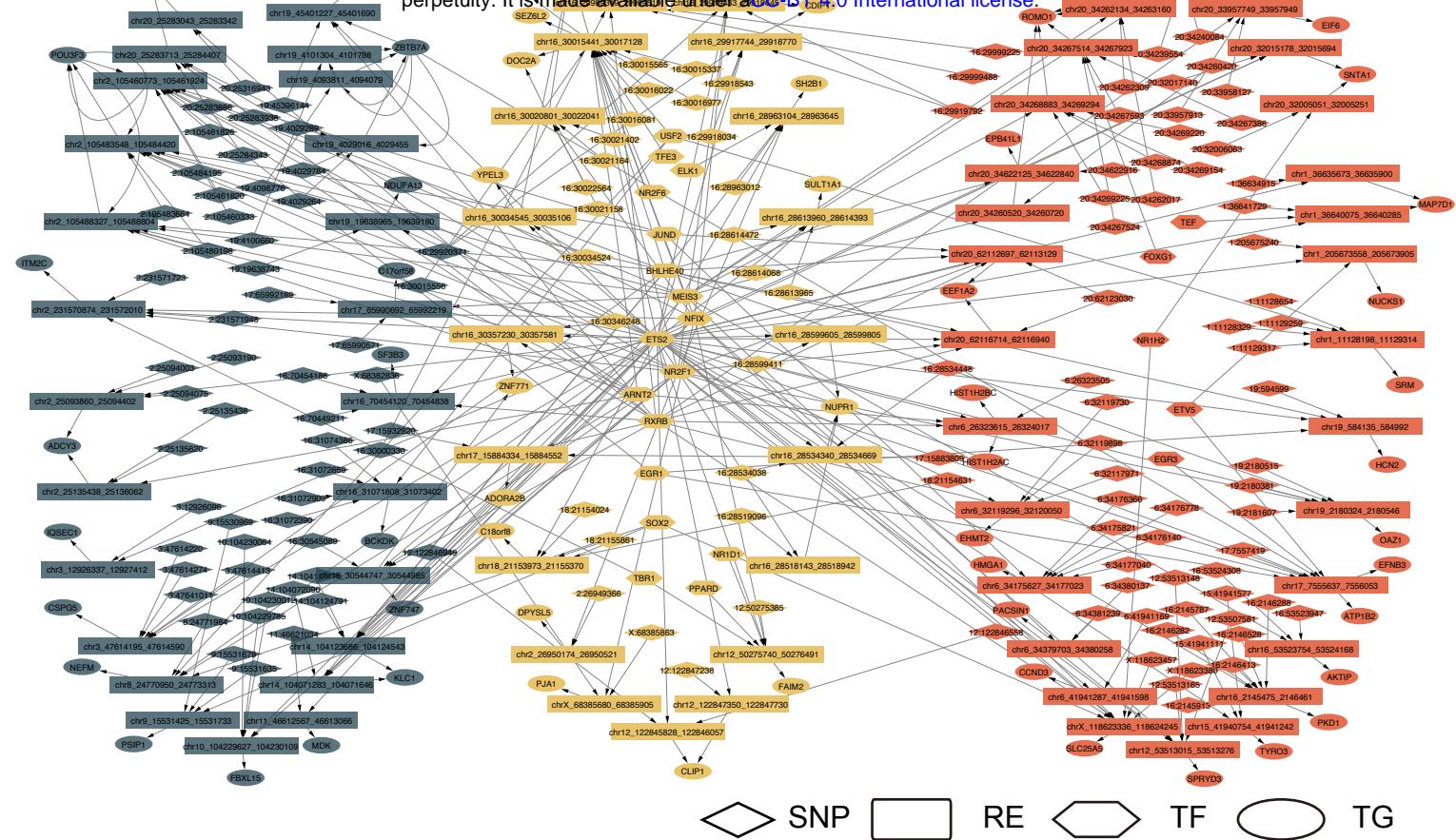
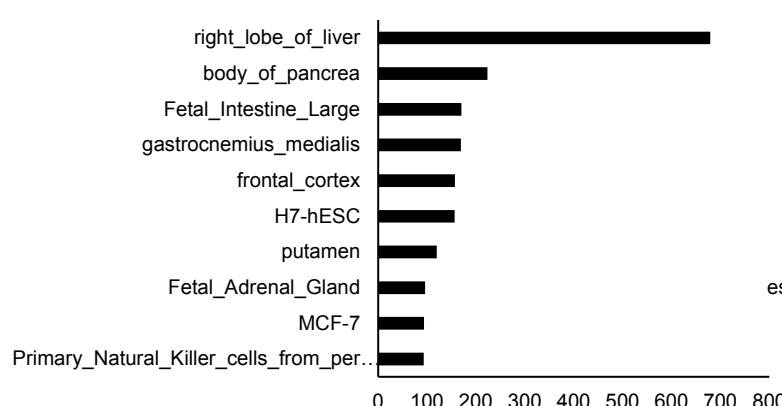
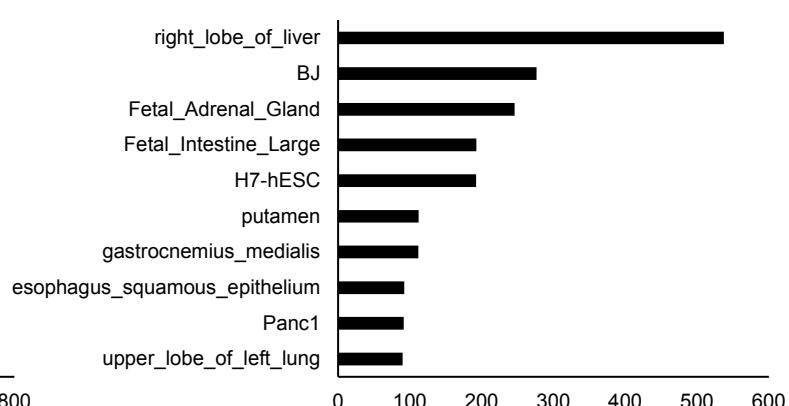


Fig. S4: SNP associated regulatory network of “body mass index” (left) and “right leg fat-free mass” (right) in “frontal cortex”. These two phenotype associated regulatory networks are significantly overlapped (middle).

a

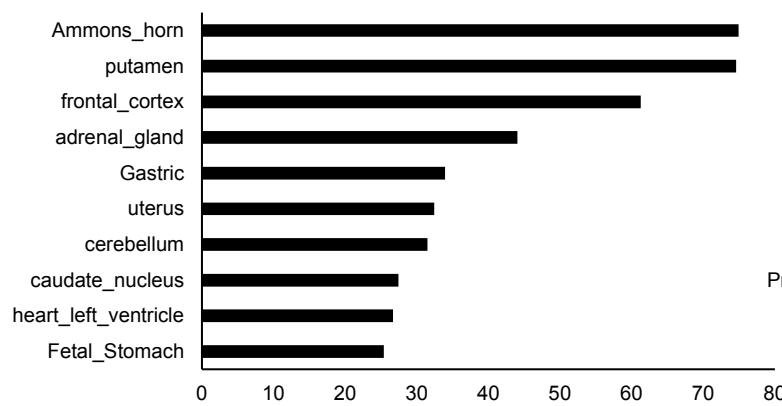


TC



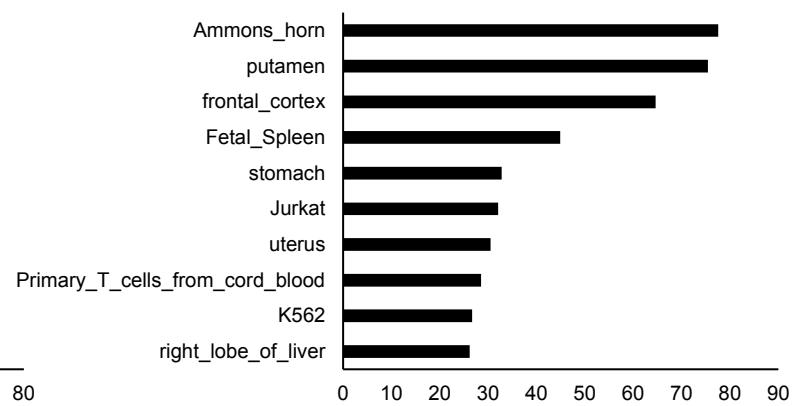
c

EA



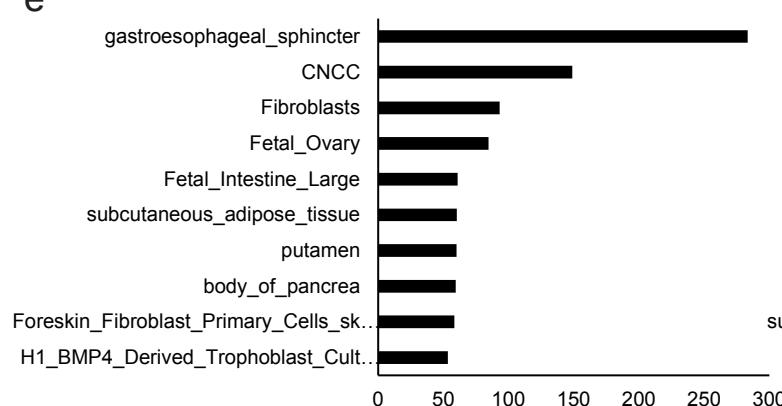
d

CP



e

BrainShape



f

Face

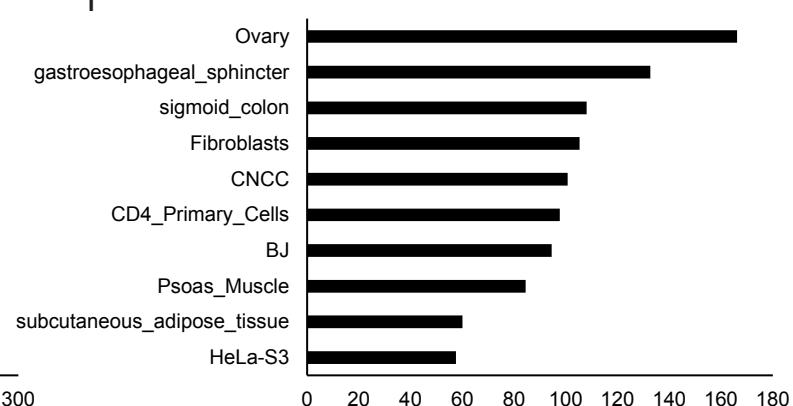


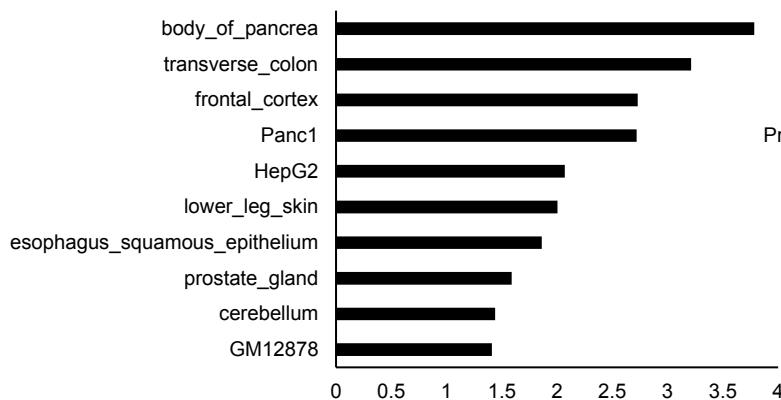
Fig. S5: Top 10 contexts ranked by heritability enrichment in context-specific regulatory elements of (a). LDL, (b). TC, (c). EA, (d). CP, (e). BrainShape, (f). Face.

a



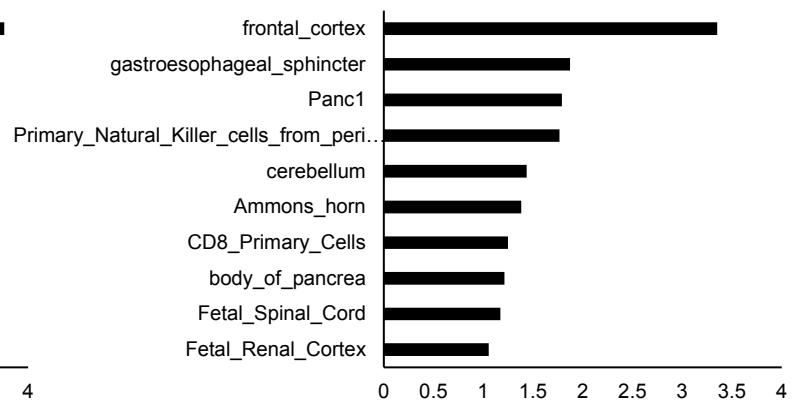
c

EA

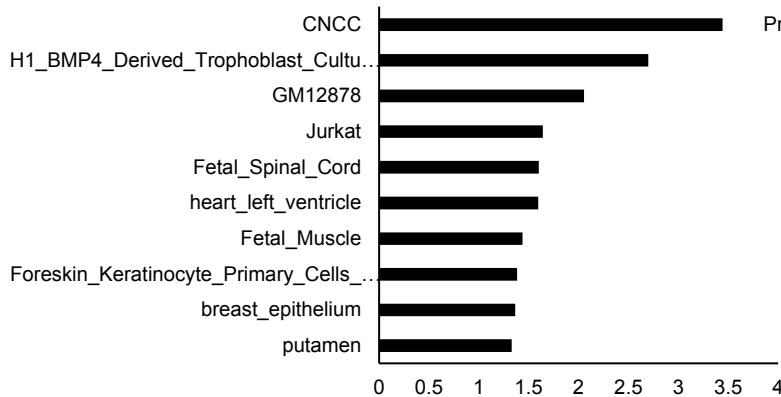


d

CP



e BrainShape



f

Face

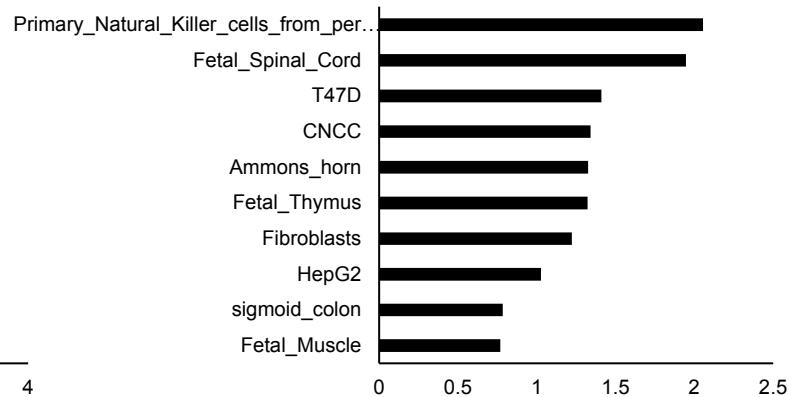


Fig. S6: Top 10 contexts ranked by P-values of heritability enrichment in context-specific regulatory elements of (a). LDL, (b). TC, (c). EA, (d). CP, (e). BrainShape, (f). Face.

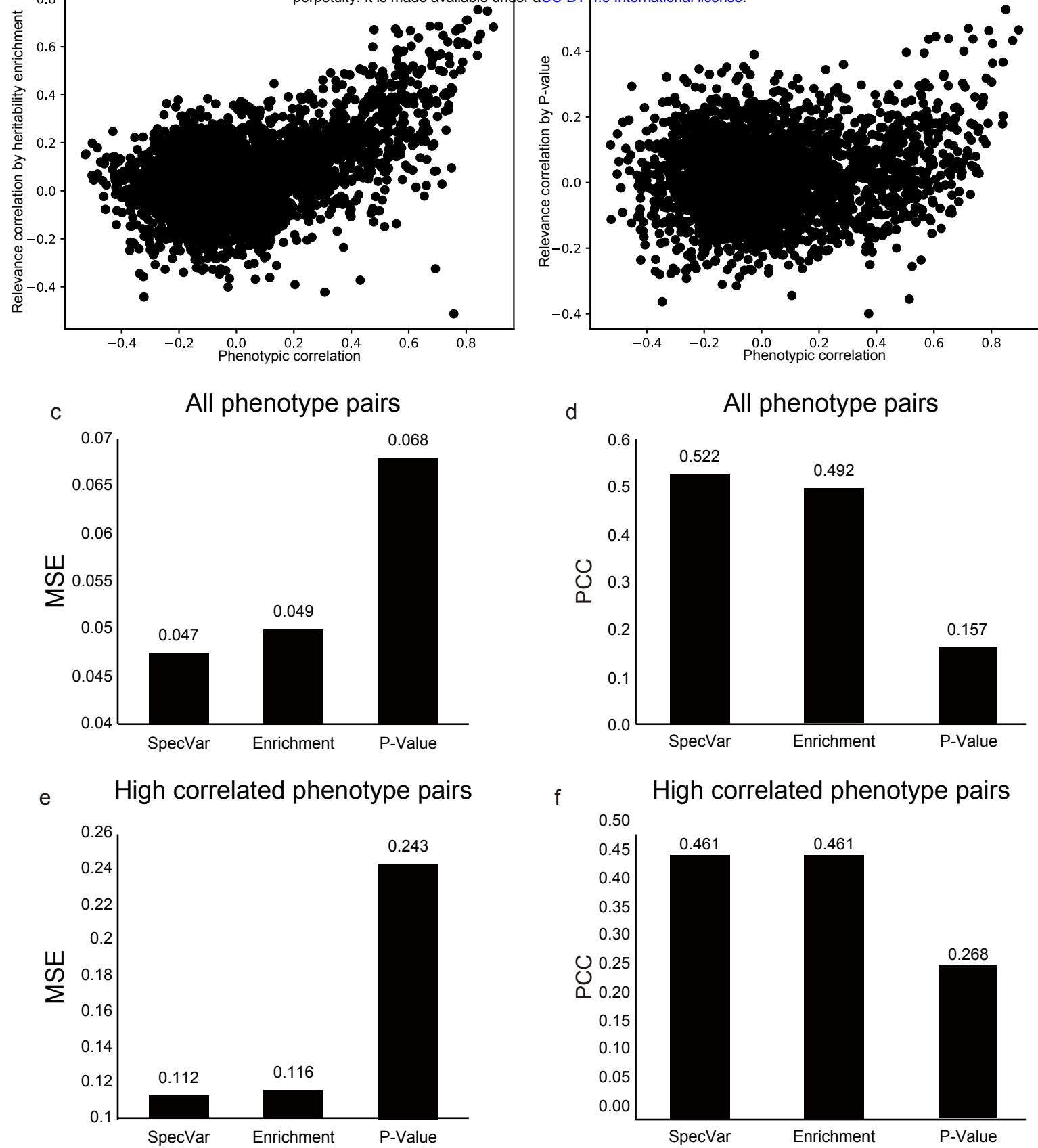


Fig. S7: The scatter plot of true phenotypic correlation and estimated relevance correlation by (a). heritability enrichment, (b).  $-\log(P\text{-value})$ . Each point means a pair of facial distances. (c). For all phenotype pairs, the MSE between phenotypic correlation and relevance correlation of SpecVar, heritability enrichment, and  $-\log(P\text{-value})$ . (d). For all phenotype pairs, the PCC between phenotypic correlation and relevance correlation of SpecVar, heritability enrichment, and  $-\log(P\text{-value})$ . (e). For high correlated phenotype pairs, the MSE between phenotypic correlation and relevance correlation of SpecVar, heritability enrichment, and  $-\log(P\text{-value})$ . (f). For high correlated phenotype pairs, the PCC between phenotypic correlation and relevance correlation of SpecVar, heritability enrichment, and  $-\log(P\text{-value})$ .

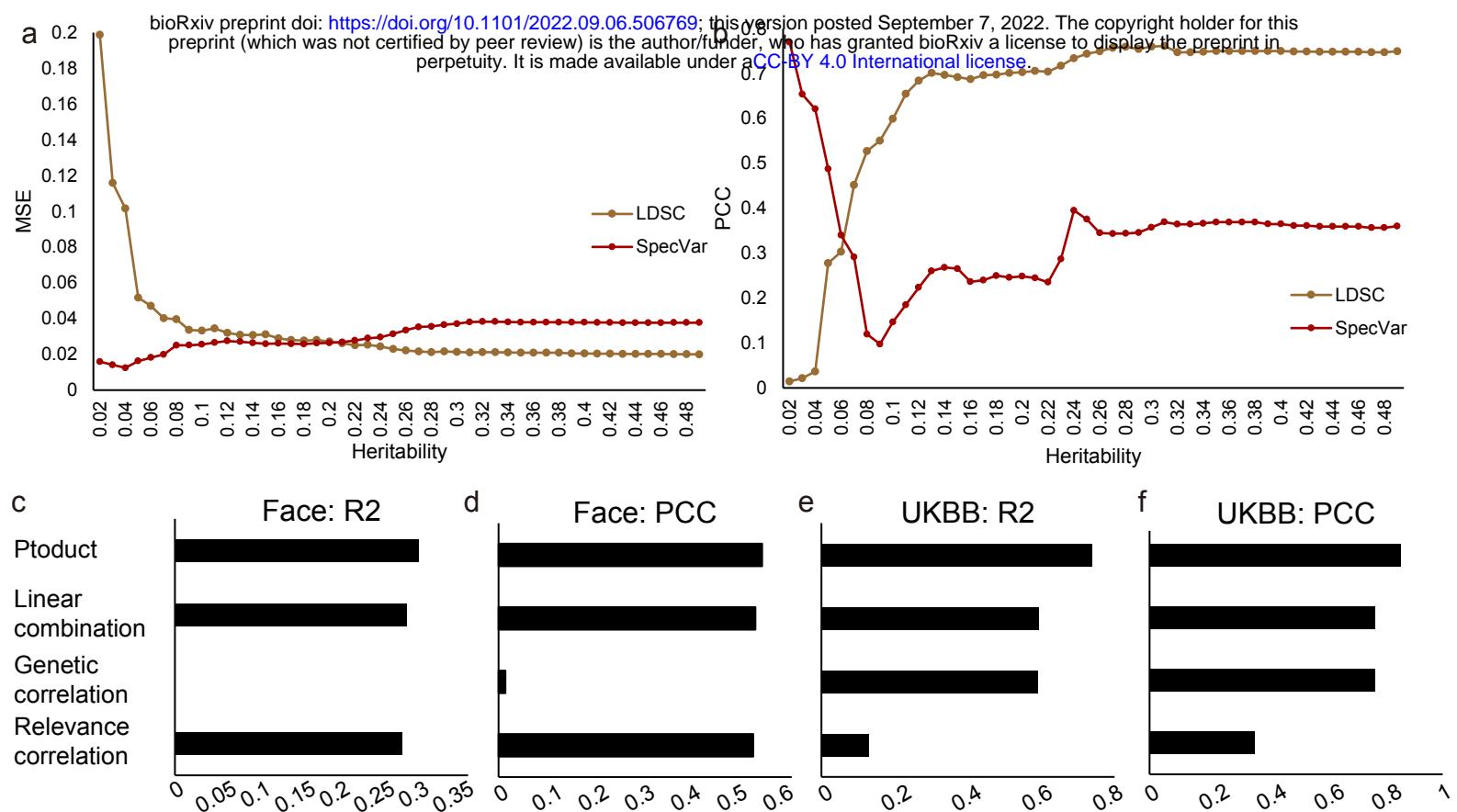


Fig. S8: (a). For phenotype pairs with different heritability thresholds, the MSE between true phenotypic correlation and SpecVar's relevance correlation; and MSE between true phenotypic correlation and LDSC-GC's genetic correlation. (b). For phenotype pairs with different heritability thresholds, the PCC between true phenotypic correlation and SpecVar's relevance correlation; and MSE between true phenotypic correlation and LDSC-GC's genetic correlation. (c). The R2 metric of regression between phenotypic correlation and relevance correlation, genetic correlation, linear combination, product in Face distance phenotypes. (d). The PCC metric of four regression in Face distance phenotypes. (e). The R2 metric of four regression in UKBB phenotypes. (f). The PCC metric of four regression in UKBB phenotypes.

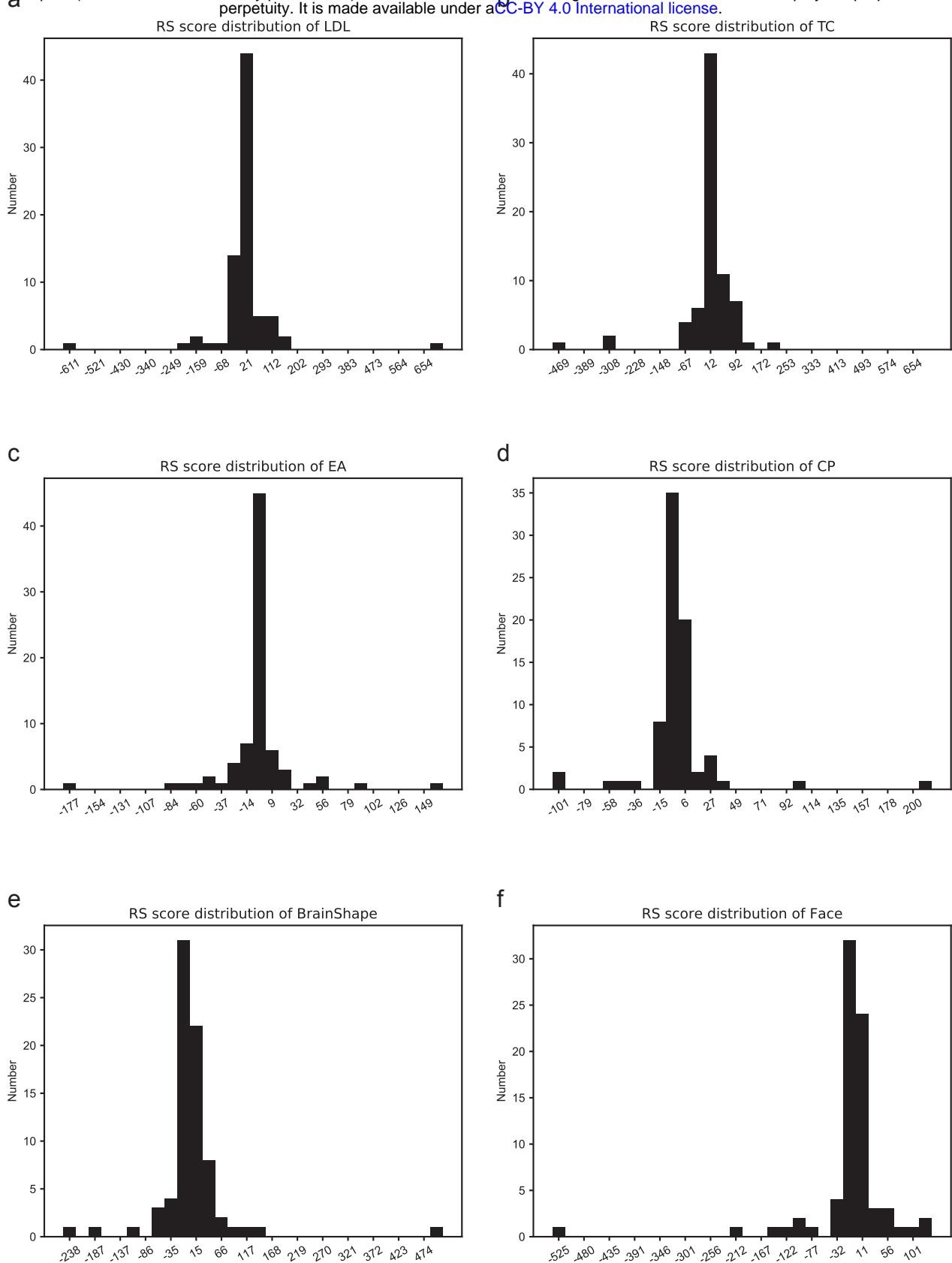
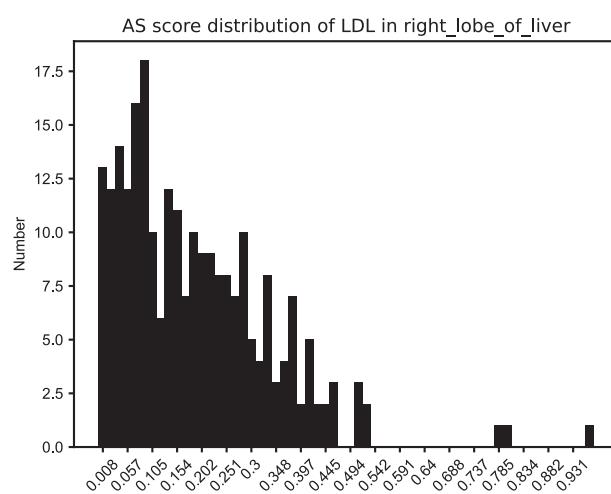
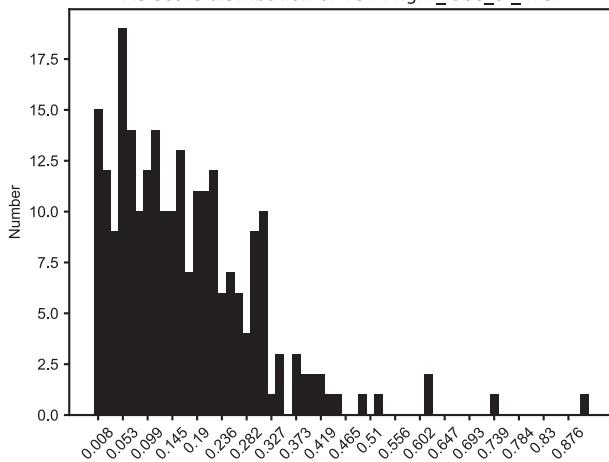


Figure S9: Distribution of *R* score of (a). LDL, (b). TC, (c). EA, (d). CP, (e). Face, (f). BrainShape.

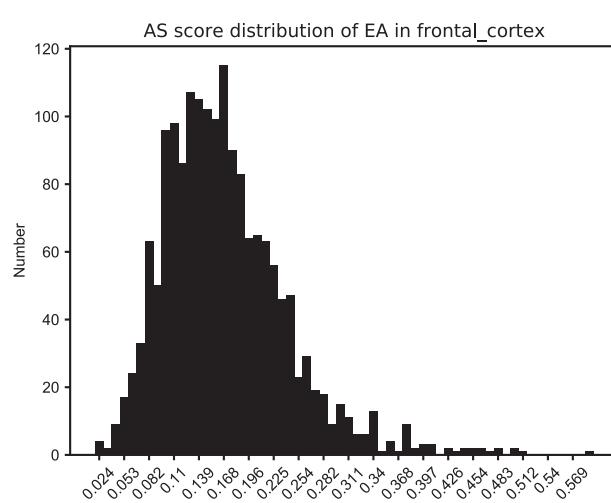
a



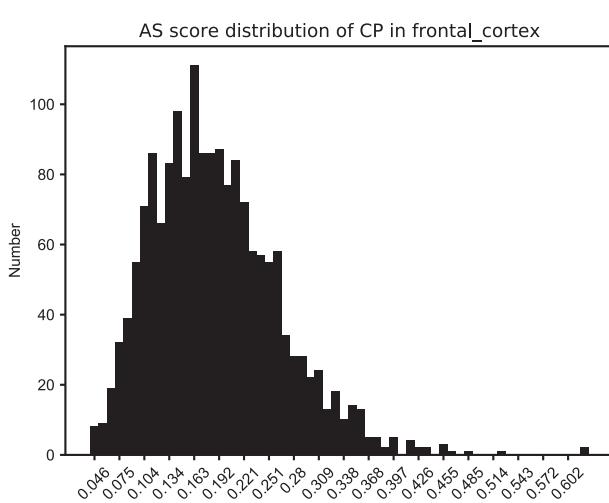
AS score distribution of TC in right\_lobe\_of\_liver



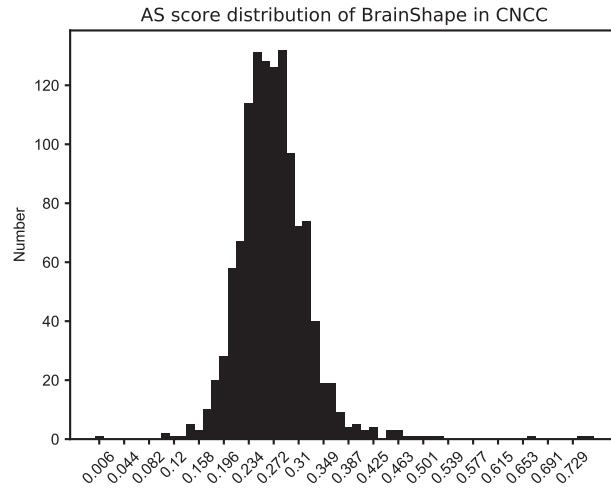
c



d



e



f

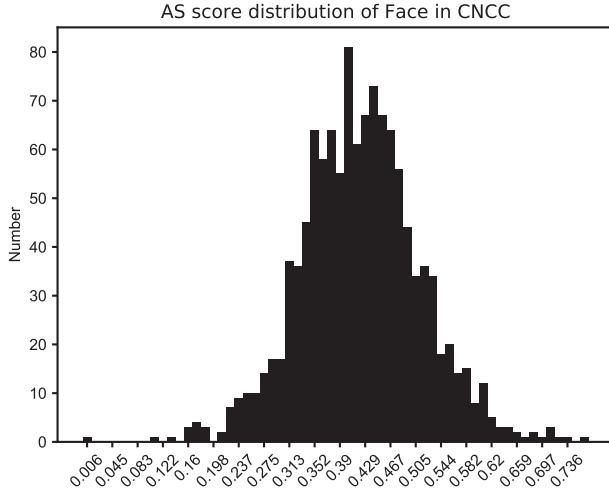


Figure S10: Distribution of A score of (a). LDL in “right lobe of liver”, (b). TC in “right lobe of liver”, (c). EA in “frontal cortex”, (d). CP in “frontal cortex”, (e). BrainShape in “CNCC”, (f). Face in “CNCC”.