

## ALGORITHMIC RECONSTRUCTION OF GBM NETWORK COMPLEXITY

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## SUMMARY

Glioblastoma (GBM) is a complex disease that is difficult to treat. Establishing the complex genetic interactions regulating cell fate decisions in GBM can help to shed light on disease aggressivity and improved treatments. Networks and data science offer alternative approaches to classical bioinformatics pipelines to study gene expression patterns from single-cell datasets, helping to distinguish genes associated with control of differentiation and thus aggressivity. Here, we applied a host of data theoretic techniques, including clustering algorithms, Waddington landscape reconstruction, trajectory inference algorithms, and network approaches, to compare gene expression patterns between pediatric and adult GBM, and those of adult glioma-derived stem cells (GSCs) to identify the key molecular regulators of the complex networks driving GBM/GSC and predict their cell fate dynamics. Using these tools, we identified critical genes and transcription factors coordinating cell state transitions from stem-like to mature GBM phenotypes, including eight transcription factors (OLIG1/2, TAZ, GATA2, FOXG1, SOX6, SATB2, YY1) and four signaling genes (ATL3, MTSS1, EMP1, and TPT1) as clinically targetable novel putative function interactions differentiating pediatric and adult GBMs from adult GSCs. Our study provides strong evidence of the applicability of complex systems approaches for reverse-engineering gene networks from patient-derived single-cell datasets and inferring their complex dynamics, bolstering the search for new clinically relevant targets in GBM.

**Keywords:** Glioblastoma; Complex Systems; Networks; Data Science; Waddington Landscape Reconstruction; Computational Oncology; Pediatric Glioblastoma

1    **1. INTRODUCTION**

2

3    Glioblastoma (GBM) is the most lethal pediatric and adult brain tumour. Despite advances in  
4    treatment, recurrence will occur in all GBM patients, and mean survival is only 15 months  
5    (Alifieris and Trafalis, 2015). GBM is a morbid disease that is driven by a high degree of  
6    heterogeneity and phenotypic plasticity in response to the interactions with their tumor  
7    microenvironment (Jung et al., 2019). The cell fate transitions and cellular decision-making in  
8    GBM cell populations are regulated by the dynamics of complex signaling networks (Suvà et al.,  
9    2014; Jia et al., 2017). Recent advances linking single-cell datasets and computational  
10   algorithms have improved our understanding of these complex networks and their orchestration  
11   of cell fate decisions of GBM transcriptional states (phenotypes) (Jin et al., 2018; Iacono et al.,  
12   2019). Despite this progress, quantitative approaches that reconstruct the information flow and  
13   dynamics of these complex networks remain under-applied. Pediatric GBM exhibits molecular  
14   patterns and collective behaviors which are fundamentally different from those of adult GBM  
15   (Paugh et al., 2010; Jones et al., 2017; Schwartzenruber et al., 2012; Sturm et al., 2012). There  
16   is a greater epigenetic burden in pediatric GBM marked by specific histone H3.3 modifications  
17   and aberrant DNA methylation profiles (Schwartzenruber et al., 2012; Sturm et al., 2012; Lulla et  
18   al., 2016; Harutyunyan et al., 2019). However, the complex signaling dynamics distinguishing  
19   pediatric and adult GBM subgroups, and the similarities within the molecular networks driving  
20   their cancer stemness, remain poorly investigated (Paugh et al., 2010; Jones et al., 2017).  
21   Answering the question of whether the reconfiguration of these underlying signaling networks in  
22   both GBM groups steers their cell fate dynamics would allow for the prediction of causal  
23   patterns in the disease progression and therapeutic responses.

24

25   Glioma-derived stem cells (GSCs) are believed to be a small subset of GBM cancer cells that  
26   largely contribute to emergent GBM adaptive behaviors such as phenotypic plasticity, clonal

27 heterogeneity, self-renewal, aggressiveness (resilience), relapse/recurrence, and therapy  
28 resistance (Jung et al., 2019, Xiong et al., 2019). However, many different phenotypes in the  
29 tumor microenvironment, including immune cells, healthy cells, extracellular matrices, and blood  
30 vessels, form complex feedback loops with malignant GBM cells (Jung et al., 2019, Xiong et al.,  
31 2019). GSCs form complex networks with their tumor microenvironment. Signaling dynamics  
32 within this microenvironment and its reconfiguration govern the fitness and stemness of GSCs.  
33 A lack of quantitative understanding of the causal mechanisms (gene expression patterns)  
34 underlying GSC cell fate choices and transitions to their mature phenotypes hinders successful  
35 clinical interventions in the treatment of GBM (Jung et al., 2019, Xiong et al., 2019; Yabo et al.,  
36 2021).

37  
38 Statistical approaches are traditionally used to study cell fate dynamics and infer complex  
39 networks from large-scale single cell transcriptomics by differential expression analysis through  
40 a combination of single cell data processing and clustering algorithms (Iacono et al., 2019).  
41 However, these algorithmic pipelines are inadequate for capturing the complex patterns and  
42 emergent behaviors of cancer network dynamics. Further, fundamental limitations associated  
43 with the raw counts of the scRNA-Seq complicate the inference of networks in complex  
44 diseases like GBM. These limitations include drop out events (zero counts), and the inherent  
45 noise and sparsity of single cell data. To extract quantitatively meaningful differences between  
46 GSC and GBM networks, while retaining the essential information representative of their  
47 complex dynamics, requires tools from the interdisciplinary paradigm of *complex systems*  
48 *theory*.

49  
50 Complex systems theory, or complexity science, is the study of irreducible systems composed  
51 of many interacting parts in which the systems exhibit emergent behaviors. Emergence denotes  
52 systems in which the nonlinear interactions between the system and its environment give rise to

53 complex patterns and unpredicted collective dynamics (Wolfram, 1988; Shalizi, 2006). Some  
54 general properties of complex systems include nonlinear dynamics, adaptive processes, self-  
55 organized structures, interconnectedness, collective behaviors, pattern formation, fractality,  
56 sudden phase-transitions, computational irreducibility, non-locality, long-term unpredictability,  
57 undecidability and multi-scaled, multi-nested feedback loops (Wolfram, 1988; Shalizi, 2006).  
58 The presence of multi-scaled feedback loops, in particular, is the defining feature of complex  
59 networks (Thurner et al., 2018). Traditional reductionist approaches are inadequate to quantify  
60 the properties and temporal behaviors of complex networks (Wolfram, 1988; Shalizi, 2006).  
61 Complex systems theory advocates the use of computational algorithms and tools from network  
62 science to dissect these complex networks (Thurner et al., 2018; Huang et al., 2009; Barabási  
63 and Oltvai, 2004).

64  
65 The molecular networks coordinating the emergence of GSC and GBM phenotypes are such  
66 complex networks. To reveal the mechanisms underlying GSC cell fate decisions and  
67 transitions to their mature GBM phenotypes, we deployed several approaches from complex  
68 systems theory on data from single-cell RNA Sequencing (scRNA-Seq) count matrices. We  
69 compared pediatric GBM to adult GBM to identify the signaling network patterns distinguishing  
70 pediatric and adult GBM from GSCs. For this, we relied upon clustering algorithms, Waddington  
71 landscape reconstruction, multivariate information theory, network science (graph theory), and  
72 machine learning algorithms to map possible *cell fate dynamics* and identify robust expression  
73 markers (critical TFs and genes) driving the complex networks underlying GBM/GSC cell fate  
74 control and regulation. We found that distinct gene expression signatures regulate the cell fate  
75 decisions in the GBM and GSC patient groups we studied. In particular, we identified a set of  
76 key gene targets as master regulators of cell fate decision dynamics in all patient groups, and  
77 the critical drivers of GSC stemness networks. Mapping their energy landscape dynamics and  
78 cell fate trajectories in pseudotime (cellular transition dimension), we represented the GSC/GBM

79 cell fate decisions as dynamical systems which allowed us to identify genes such as GATA2,  
80 FOXG1, SATB2, YY1, and SOX6, amidst others, as master regulators of information flow in  
81 their signaling networks. Our results help to understand how cellular fate decisions in GBM,  
82 identify potential drug targets for precision oncology, and provide a roadmap for data theoretic  
83 approaches to other such complex systems.

84

85 **2. METHODS**

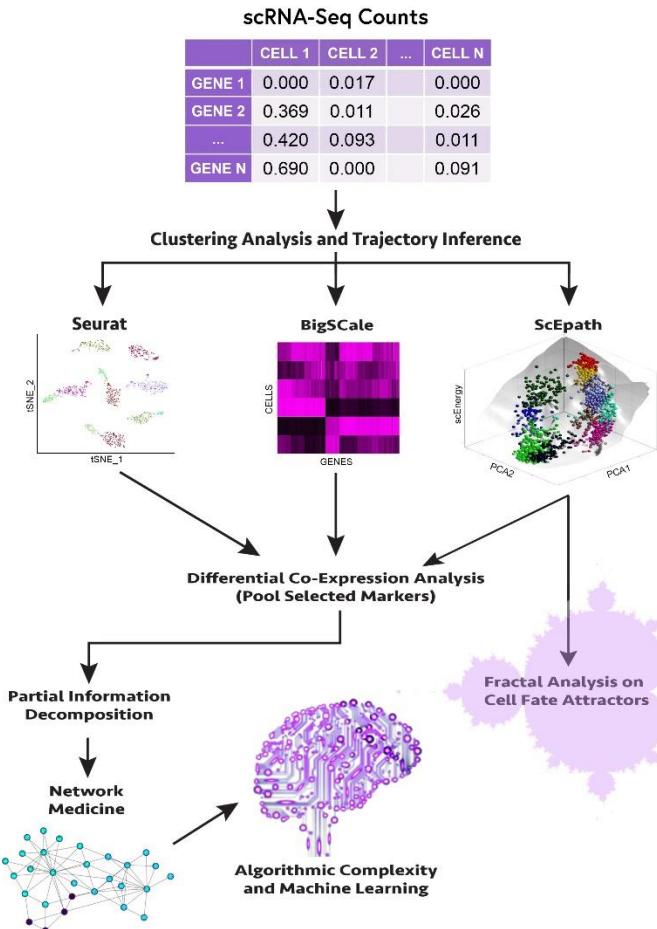
86 **2.1. General methodological framework**

87 To understand GBM network complexity, we integrated several pediatric and adult IDH-wt  
88 GBM single-cell RNA-Seq (scRNA-Seq) datasets in an analytical pipeline that combines  
89 several network reconstruction and analysis tools (see subsections below). Details of the  
90 datasets used are provided in Table 1. Single-cell datasets were first filtered and normalized  
91 in a quality control step, and patient samples were removed from the scRNA-Seq counts  
92 expression matrix due to low unique molecular identifier (UMI)/high drop-out rates.

93

94 Next, gene expression matrices were analyzed independently using the various clustering  
95 and trajectory inference algorithms discussed below. Here we provide a short summary  
96 (Figure 1). For the Seurat algorithm, the top 10 principal component analysis (PCA) loadings  
97 were used for the differential marker discovery; the top 25 PC loadings were used for the  
98 BigScale analysis. To identify the differential markers expressed in all clusters, the top 10  
99 markers within these PC loadings were pooled and analyzed on the UMAP/tSNE patterning  
100 space of the cell fate clusters for each patient group. Similarly, the top 2 PCA loadings were  
101 used by the scEpath pseudotime analysis. The normalized scRNA-Seq counts of the  
102 discovered markers from the Seurat and BigScale algorithms were pooled together, and  
103 separately analyzed for each patient group. The expression counts of these markers were  
104 then run through the PIDC Network Inference algorithm to obtain gene receptor networks.

105 The differential transcription factors identified in the pseudotemporal progression heatmaps  
106 were selected for scEpath analysis. Only the markers specific to each patient group were  
107 selected for the PIDC network inference. Lastly, complex networks analysis was performed  
108 on the reconstructed networks using transitivity and centrality scores to assess the network  
109 structure and dynamics (information flow) to identify key regulators of GBM/GSC cell fate  
110 decisions. Further, algorithmic complexity measures, as provided in the Supplementary  
111 Material, were used to identify gene markers which could accurately discriminate the patient  
112 groups by machine learning classifiers. Within the established gene networks, algorithmic  
113 complexity was used to identify robust discriminants that could accurately distinguish the  
114 three patient groups (i.e., pediatric GBM, adult GBM, and adult GSC), based on the  
115 performance of machine learning classifiers on their algorithmic complexity scores (see  
116 Supplementary Information).



117

118 **FIGURE 1. Workflow schematic of gene expression network pattern discovery.**  
119 Flowchart summarizing the methodological approach to differential marker discovery and  
120 cell fate dynamics inference (see Methods section 2.1).  
121

122 **2.2. Single-cell datasets:** Gene expression matrices for pediatric GBM, adult GBM, and  
123 adult GSC were obtained from the SingleCell Portal repositories from Neftel et al., 2019 and  
124 Richards et al., 2021 (Table 1). Briefly, GBM patient samples from Neftel et al. (2019)  
125 contained the single cell RNA-Seq counts of four phenotypes (or cellular states):  
126 macrophages, malignant GBM cells, oligodendrocytes, and T-cells. Adult GSC consisted  
127 only of stem cells. Overall, our dataset included 28 adult GSC datasets, 7 pediatric GBM,  
128 and 18 adult GBM scRNA-Seq expression count matrices.

129

130 As a quality control measure for the Seurat and BigSCale clustering, two adult GBM  
131 samples and one pediatric GBM sample were dropped in the filtering process (prior to  
132 clustering) due to high zero-counts (i.e., low UMI). Importantly, we confirmed that our  
133 findings were insensitive to the number of patient samples within each patient group:  
134 including these removed samples did not change the differential expression analysis. To  
135 further validate this finding, one sample was randomly chosen and dropped from the total  
136 number of samples from each patient group to verify whether the clustering analysis  
137 changed (i.e., leave-out-one cross-validation) and we confirmed the clustering results were  
138 identical. Beyond 2500 cells, the computational time complexity of the scEpath algorithm  
139 increased. Thus, the total cell counts of all three patient groups were kept at the maximum  
140 computational threshold for the scEpath analysis (see Section 2.3.3). Further, to visualize  
141 the cell fate attractor dynamics at the same fine-scale resolution for all patient groups, cell  
142 counts were kept roughly the same for each GBM type. Selecting a different combination of  
143 adult GSC samples did not change the scEpath landscape or results, as the trial of multiple  
144 random selections (> 6 distinct combinations) reproduced identical results. A complete  
145 description of the experimental approaches used to derive these datasets from their original  
146 studies is provided in the Supplementary Information.

147

148 **2.3. Clustering techniques.** Clustering algorithms were used to identify differential markers  
149 co-expressed within all patient groups and distinguish a robust network regulating the cell  
150 fate dynamics across all phenotypes.

Patient Group	Single-Cell Dataset	# Patient Samples (n) and Single-Cells (N) for Seurat/BigSCale	# Patient Samples (n) and single-cells (N) for scEpath Analysis	# of Cell Fate Trajectories in scEpath Waddington Landscape
Pediatric GBM	Neftel et al. (18)	n = 7 N = 1850	n = 7 N= 1850	2

<b>Adult GBM</b>	Neftel et al. (18)	n = 18 N ~ 21,500	n = 7 N = 2221	4
<b>Adult GSC</b>	Richards et al. (19)	n = 28 N ~ 69, 000	n= 13 N = 1504	2

151 **TABLE 1. Summary of single-cell datasets.** The total number of patient samples (n) and  
152 number of single-cells within each patient group (N) used for each step of the clustering and  
153 single-cell trajectory inference process are shown.

154

155 **2.3.1. Seurat algorithm:** scRNA-Seq count matrices were pre-processed to obtain normalized  
156 and binarized count expressions. Seurat initially performs a cluster analysis by principal  
157 component analysis (PCA) dimensionality reduction followed by a graph-based  
158 clustering (k-nearest neighbor (kNN) graph) based on the Euclidean distance of the 10  
159 PCA loadings using the FindNeighbors function and Louvain community detection  
160 algorithm (modularity optimization) using the FindClusters function (parameter can be  
161 tuned between 0.4-1.2 for optimal results), to cluster cells by their Jaccard index-  
162 expression similarity (see Seurat Clustering tutorial in GitHub code). All clustering  
163 parameters were kept to their default settings. Next, the cells within the graph-based  
164 clusters were visualized on Uniform Manifold Approximation and Projection (UMAP) or t-  
165 Distributed Stochastic Neighbor Embedding (TSNE) space (i.e., unsupervised nonlinear  
166 dimensionality reduction techniques) (Stuart et al., 2019). Differential markers from the  
167 top 10 PCA loadings were visualized in UMAP space (analysis does not vary for TSNE  
168 space) using the FindAllMarkers function with parameters: min.pct = 0.25 and  
169 logfc.threshold = 0.25. We clustered similarly expressed cells together in the low  
170 dimensional space by finding differentially expressed features/markers corresponding to  
171 the highest ten PCA loadings in the graph-based clusters. To identify markers that  
172 govern disease progression and transcriptional dynamics, we imposed the condition that  
173 selected markers for the network reconstruction must be expressed in all clusters of the  
174 three patient groups (pediatric GBM, adult GBM, and adult GSC).

175 **2.3.2. BigSCale algorithm:** BigSCale is a framework for clustering, phenotyping,  
176 pseudotiming, and inferring gene regulatory and protein-protein interaction networks  
177 from single-cell data (Iacono et al., 2019). A SingleCellExperiment class was created  
178 from the scRNA-Seq raw count matrices for BigSCale processing, and counts were  
179 replaced by z-scores. Cellular clustering was established by first computing all pairwise  
180 cell distances using the Pearson correlation to generate a distance matrix. Following,  
181 cells were assigned to cluster groups via the Ward's linkage/method (an agglomerative  
182 hierarchical clustering algorithm). Iterative differential expression analysis was  
183 performed between the clusters of cells and the differential markers within the identified  
184 clusters were assessed using the getMarkers function (see BigSCale 2 tutorial in Github  
185 code). The markers specific to a cluster were sorted from the highest (most significant)  
186 to the lowest (least significant) z-score for the selection of cluster-specific differential and  
187 co-expressed gene markers within the top 25 PCA components. A z-score threshold of  
188 5.0 was used as a cut-off threshold while the min\_ODscore parameter was kept default  
189 at 2.33. This imposed cut-off acts as a filtering mechanism to retain only the markers  
190 with significant expression changes per cluster. As in the Seurat analysis, we imposed  
191 the condition that selected markers for the network reconstruction must be expressed in  
192 all clusters of the three patient groups.

193  
194 **2.3.3. ScEpath algorithm:** We applied single cell Energy path (scEpath) to reconstruct the 3D-  
195 energy landscape of cells and infer regulatory relationships from their transcriptional  
196 dynamics (Jin et al., 2018). scEpath is a Waddington Landscape reconstruction  
197 algorithm with an unsupervised clustering framework for cell lineage hierarchy mapping  
198 and studying the pseudotemporal transcriptional dynamics in cell fate decisions. In this  
199 trajectory inference algorithm, information flow and network reconfiguration underlying  
200 the cellular decision-making steer the topography of cell populations' energy landscapes

201 (also referred to as a cell fate landscape, attractor landscape, or Waddington's  
202 epigenetic landscape (Waddington, 1957)). A cell state (cell fate) corresponds to a  
203 specific transcriptional (gene expression) program and phenotype of a given cellular  
204 population. Cell clusters higher on the energy landscape correspond to stem-cell like  
205 states (unstable attractors) with higher differentiation potency, while cell states stuck in  
206 lower energies (valleys, or stable attractors) correspond to differentiated (mature)  
207 phenotypes with lower potency/plasticity (Figure 2).

208  
209 scEpath allows for the visualization of cell fate transition probabilities in the population,  
210 mapping of cell lineage trajectories in pseudotemporal ordering, and inference of cell  
211 fate decisions from patient-derived scRNA-Seq datasets using the following steps: (i)  
212 preprocessing of scRNA-seq count matrix, (ii) gene regulatory network (GRN) inference,  
213 (iii) single cell energy (scEnergy) calculation, (iv) 3D energy landscape reconstruction via  
214 principal component analysis and structural clustering; (v) Transition probabilities  
215 calculation, (vi) Inference of cell lineage hierarchy via a probabilistic directed graph, (vii)  
216 pseudotime trajectory inference and, (viii) downstream analyses of identifying critical  
217 transcription factors (TFs) governing the cell-fate commitments (Jin et al., 2018). A  
218 detailed description of the scEpath algorithm is provided in the Supplementary  
219 Information.

220  
221 To perform the scEpath analysis on our data, we first pre-processed the log-normalized  
222 (within patient-groups) count matrices with respect to their gene expression values by  
223 filtering out zero counts. The differential markers were selected from the first two  
224 significant PCA components. We then ran the scEpath MATLAB code from (Jin et al,  
225 2018) on these processed datasets. GSC patient samples BT127, BT48, and BT84 from  
226 Richards et al. (2021) were used for all scEpath analyses on GSC. Seven pediatric GBM

227 samples from (Neftel et al., 2019) and seven adult GBM samples, selected to match the  
228 cell count of the pediatric patient group, from (Neftel et al., 2019), were analyzed. We  
229 confirmed that the number of patients did not influence the results and analysis by  
230 selecting different random sets of adult GBM samples. We then ran energy  
231 (Waddington) landscapes reconstruction on the following population sizes: pediatric  
232 GBM: n= 7, N= 1850 cells; adult GBM: n = 7, N= 2221 cells; adult GSC: n=3, N=1504  
233 cells.

234

235 scEpath smooths the average normalized expression of each gene using cubic  
236 regression splines to map the pseudotemporal gene expression dynamics along the  
237 inferred trajectories of the cell fates on the landscape, leading to smoothed gene  
238 expression along a lineage path (Jin et al., 2018). Leveraging this, we inferred key  
239 regulatory TFs for the cell fate differentiation by considering all PDG genes with a  
240 standard deviation > 0.5 and a Bonferroni-corrected p-value below a significance level  $\alpha$   
241 = 0.01 for the expression greater than a threshold (e.g.,  $\log_2(\text{fold-change}) > 1$ ). The  
242 probabilistic-directed graph network and the cell lineage hierarchy inference parameters  
243 were kept at default settings (quick\_construct = 1; tau = 0.4; alpha = 0.01; theta1 = 0.8).  
244 The pseudotime-dependent genes were identified using parameters sd\_thresh = 0.5;  
245 sig\_thresh = 0.01; nboot (see hyperparameter-optimized code in GitHub link).

246

247 **2.3.4. Fractal and multifractal analysis:** We applied fractal analysis to quantify the  
248 complexity of the phenotypic patterns on the scEpath cell fate attractor landscape.  
249 Fractals are signatures of complex systems (Mandelbrot, 1982), and the fractal  
250 dimension is a non-integer, fractional dimension characterizing the statistical self-  
251 similarity and roughness of a pattern. A higher fractality in tumor structures may imply  
252 that the tumor is more complex, resilient (i.e., withstands environmental perturbations),

253 aggressive, and difficult to treat (Coffey, 1998; Baish and Jain, 1998). As such, the  
254 fractal index provides a quantitative measure of the cell fates' phenotypic plasticity (i.e.,  
255 higher for stem cell-like fates) and disease progression.

256

257 We used ImageJ plugin FracLac (v2.5) to compute the fractal dimension (FD) of  
258 analyzed samples using the BoxCount algorithm on the cell state attractors (patterns of  
259 cellular distributions on the scEpath energy landscapes). To calculate the fractal  
260 dimension, landscape images were converted to black and white. Attractor fractal  
261 dimensions reconstructed from the cell fate landscapes found to be non-integer were  
262 considered to exhibit a fractional dimension in phase-space. Higher fractal indices  
263 indicate more complex dynamics that are irregular and asymptotically unpredictable,  
264 since in dynamical systems theory, patterns of systems exhibiting deterministic chaos  
265 have a fractal dimension (i.e., strange attractors) (Strogatz, 2015).

266

267 **2.3.5. Partial Information Decomposition and Context network inference:** Using the  
268 differential expression markers identified by the various approaches discussed above,  
269 we reconstructed the underlying complex networks driving the GBM/GSC cell state  
270 dynamics on the Waddington energy landscapes. Network inference tools study the  
271 statistical dependencies between genes amidst distributions of expression levels in  
272 populations of sampled cells (Chan et al., 2017) by inferring a graph-theoretic  
273 representation of the functional relationships between the drivers of complex behaviors  
274 such as cell fate transitions, thus allowing for the quantification of the relationships  
275 between identified differential transition markers and tracking how these relationships  
276 change across distinct phenotypes. Partial Information Decomposition and Context  
277 (PIDC) networks have been suggested to outperform traditional gene regulatory network  
278 inference approaches using correlation metrics, mutual information, Boolean networks,

279 or Bayesian inference methods for network reconstruction (Chan et al., 2017). We used  
280 this PIDC network inference algorithm to obtain a network structure of GBM and GSC  
281 samples.

282

283 The Julia packages *InformationMeasures.jl* and *NetworkInference.jl* were used to  
284 reconstruct the GRN networks. PIDC network inference uses partial information  
285 decomposition (PID) to infer regulatory interaction networks from gene expression  
286 datasets. We used the *NetworkInference.jl* package to establish the (undirected)  
287 networks from the multivariate information measure (PID) calculated from the gene  
288 expression matrices. Gene expression counts were first discretized via Bayesian blocks  
289 discretization and the maximum likelihood estimator (Chan et al., 2017). The PIDC  
290 network pattern is the simplest network the algorithm can construct such that the  
291 distance between the nodes (genes or TFs) are minimized given their weights (PID  
292 score). Network measures characterizing the structure, properties, and information flow  
293 of these complex networks were then computed and the most differentially expressed  
294 genes were identified by the clustering algorithms using PID scores.

295

296 **2.3.6. Block Decomposition Method Calculations:** We evaluated the algorithmic complexity  
297 of key nodes (genes) of the inferred signaling networks to further identify robust markers  
298 distinguishing GBM and GSC. Algorithmic complexity is a complementary measure that  
299 identifies the minimal amount or set of information in our inferred complex networks  
300 which regulate the phenotypic plasticity dynamics across the patient groups, and as  
301 such the genes/TFs with highest algorithmic complexity could be robust disease  
302 screening tools in precision oncology. The K-complexity of a string  $s$ ,  $K(s)$ , also known  
303 as Kolmogorov or algorithmic complexity, is the shortest computer program length  
304 needed to output that string. This can also alternatively be interpreted as the length of

305 the shortest description of a system (Zenil et al., 2016). Since  $K(s)$  does not depend on  
306 a choice of probability distribution like Shannon entropy, it is more robust for the  
307 assessment of system complexity (Zenil et al., 2016, Zenil et al., 2019). Formally, the  
308 Kolmogorov complexity of a discrete dynamical system is given by

309 
$$K(s|e) = \min \{|p|: U(p, e) = s\},$$

310 for a string or array  $s$ , where  $p$  is the program that produces  $s$  and halts running on a  
311 universal Turing machine  $U$  with input  $e$ . Then,  $K(s)$  is a function that takes a string or  
312 matrix  $s$  to be the length of the shortest program  $p$  that generates  $s$ . However,  $K(s)$  is in  
313 principle incomputable and must be approximated using the coding theorem method  
314 (Zenil et al., 2019). We therefore used the Block Decomposition Method (BDM) to  
315 approximate the  $K(s)$  of a dataset, which provides local estimates of the algorithmic  
316 complexity (Zenil et al., 2016). BDM is available in the online algorithmic complexity  
317 calculator [OACC] and its R-implementation (see Availability of Data and Material). The  
318 BDM is defined as

319 
$$BDM = \sum_{i=1}^n K(block_i) + \log_2(|block_i|),$$

320 where the block size must be specified for the n-number of blocks. When the block sizes  
321 are higher, better approximations of the K-complexity are obtained (Zenil et al., 2016,  
322 Zenil et al., 2019).

323  
324 To calculate the BDM, we selected scRNA-Seq counts of seven randomly chosen  
325 patient samples from each of the three patient groups. String length was kept the same  
326 for all gene candidates from each sample. Accordingly, we chose the cell count  
327 expressions of 46 cells from each patient sample for this analysis. The R-implementation  
328 of the Online Algorithmic Complexity Calculator was used to compute the BDM  
329 estimates of K-complexity for each expression string. scNA-Seq counts of the top gene

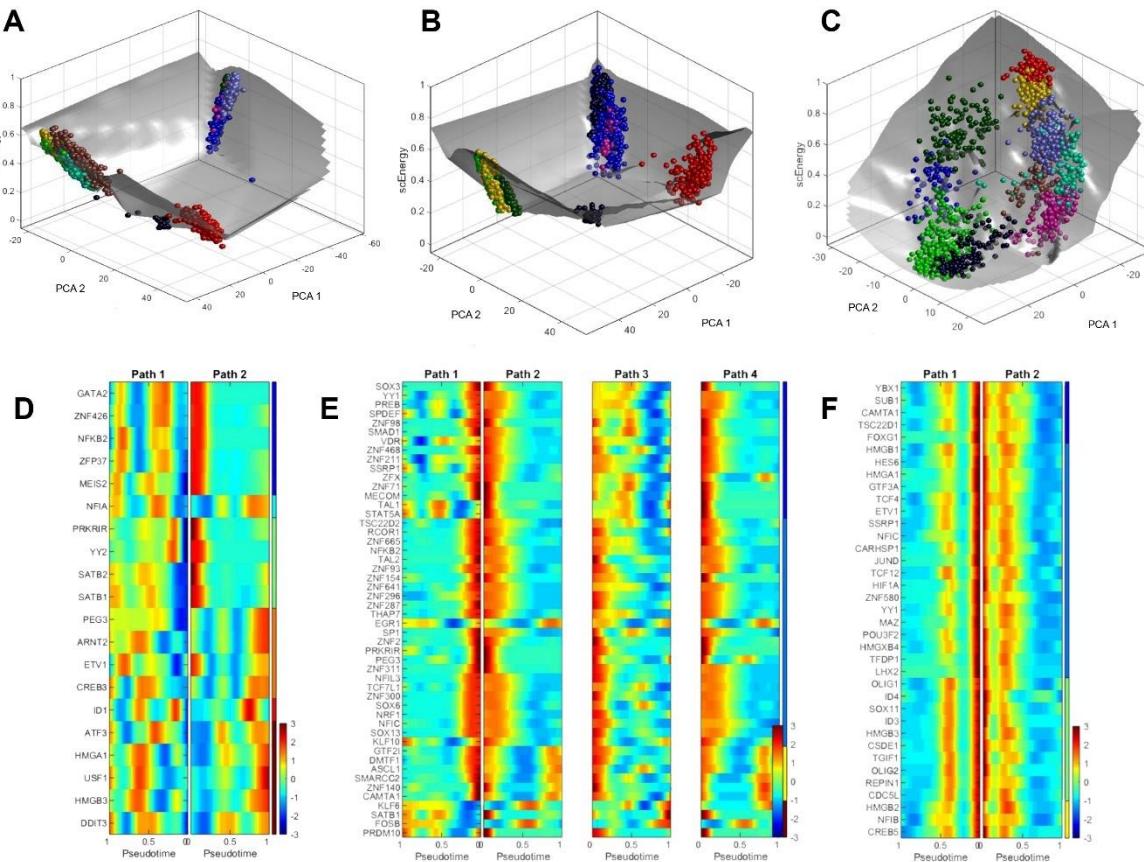
330 interactions with highest PID scores were selected from each network and binarized.  
331 We then performed BDM on these binarized strings using a block size of 12 and  
332 alphabet size of 2 bits to estimate the K-complexity (i.e., BDM score) (see  
333 Supplementary Information for BDM Results).

334

335 **3. RESULTS**

336 **3.1. *Key driver genes mediating the cell fate transition dynamics in GBM/GSC***  
337 ***epigenetic landscapes are identified using the scEpath algorithm.***

338 The Waddington landscape reconstruction identified causal patterns (attractors) to which the  
339 distinct transcriptional states within each patient group cluster (Fig 2A-C). Distinct patient group  
340 clusters were determined by the scEpath algorithm (colored by similarity in gene expression  
341 (i.e., phenotypes) in Figure 2). Three and four meta-clusters were identified in the pediatric GBM  
342 (Fig 2A) and adult GBM (Fig 2B), respectively while sub-populations are observed within each  
343 meta-cluster indicating the presence of phenotypic heterogeneity and epigenetic plasticity. Many  
344 genes encoding transcription factors (TFs) were identified as the transition genes required for  
345 cells to transition from one attractor to another. We mapped the expressions of these transition  
346 genes across the inferred cell fate trajectories (Fig 2D-F) and found similarities in the gene  
347 expression signatures and similar oscillatory patterns in EMP1, MTSS1, PHGDH and OLIG1/2  
348 (Fig 3). These markers were selected in the clustering and trajectory inference process as  
349 explained above. Their similarity was assessed by their expression variation along the cell fate  
350 trajectories in pseudotime (Figure 3). We also identified OLIG1/2 as critical transcription factors  
351 in the adult GSC phenotypic transitions (Fig 2F).



352

353 **FIGURE 2. Waddington landscape reconstruction differentiates adult and pediatric GBM,**  
 354 **and adult GSC critical genes and transcription factors for cell fate transitions.** A-C) The  
 355 distinct phenotypes of each patient group were clustered on the Waddington energy landscape  
 356 by their similarity in gene expression. The cell clustering patterns on the landscape are referred  
 357 to as **attractors**. Balls represent the transcriptional states (cell fates) and paths correspond to  
 358 the cell fate differentiation trajectories on the Waddington landscape. A) Pediatric GBM. B) Adult  
 359 GBM. C) Adult GSC. D-F) Heat maps of the critical transcription factors involved in the  
 360 differentiation and cell fate transitions between the distinct attractors (phenotype clusters) of the  
 361 GBM/GSC Waddington landscape. The color gradient represents the intensity of the gene  
 362 expression in pseudotime trajectory, where blue implies low expression and red implies high  
 363 expression of the gene (TF) during the cell fate choices along the cell differentiation trajectories.  
 364 The path corresponds to the inferred trajectories in between the cell state attractors on the  
 365 Waddington landscape. D) Pediatric GBM. E) Adult GBM. and F) Adult GSC.

366  
 367  
 368

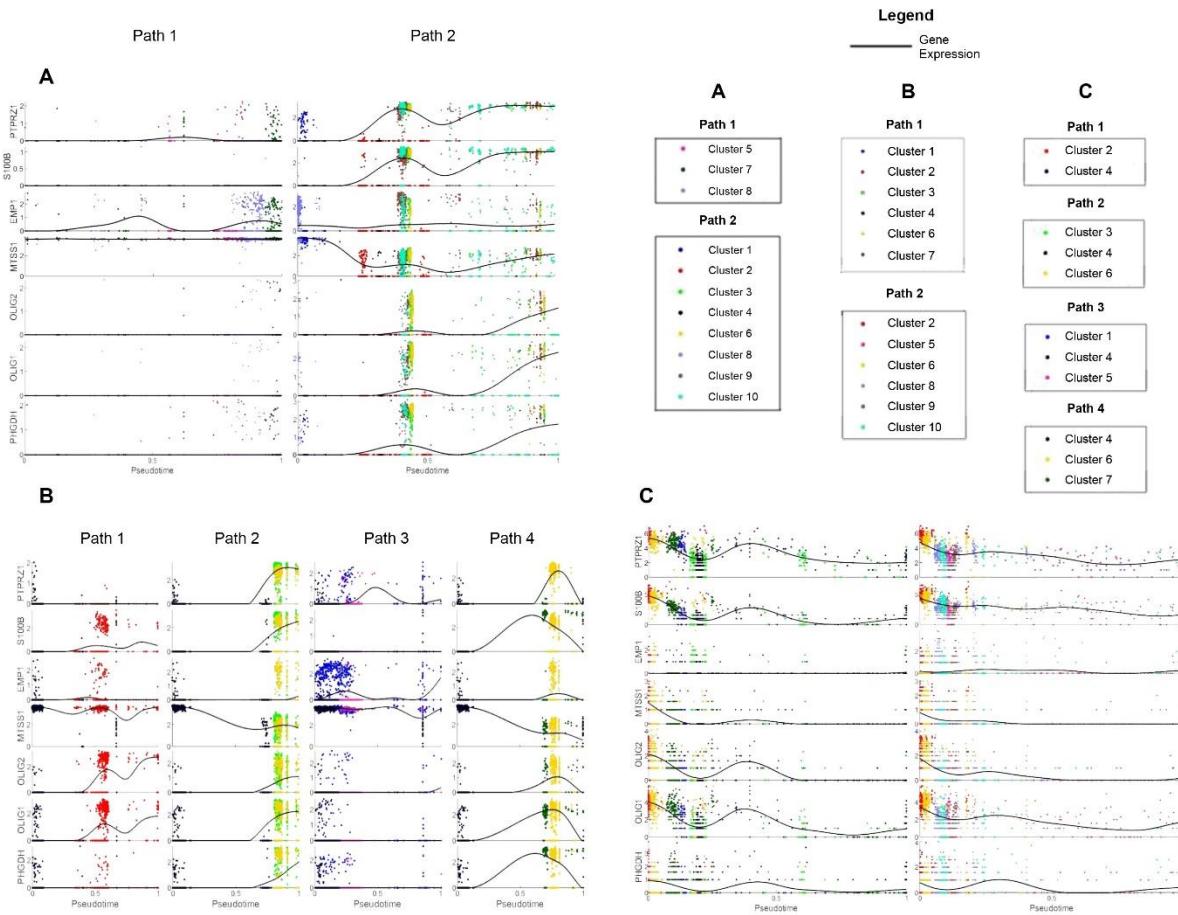
369 **3.2. Pseudotime expression dynamics identifies oscillatory patterns in critical gene  
370 targets.**

371 Given the key driver genes and transcription factors identified by scEpath trajectory inference,  
372 we next sought to infer similarities in gene expression dynamics during cell fate transitions  
373 within each patient group amidst the identified critical gene markers. Using clustering algorithms  
374 (see Methods), we found that PTPRZ1 and S100B showed nearly identical expression  
375 dynamics in pediatric GBM along both cell fate trajectories on the Waddington landscape,  
376 whereas genes such as EMP1, MTSS1, and PHGDH had more complex dynamics and  
377 exhibited oscillations during cell fate dynamics in pediatric GBM and adult GSC (Fig 3A and Fig  
378 3C). The expression metric used to compare the dynamics of the different pseudotime-  
379 dependent genes correspond to the cubic spline smoothed average normalized expression  
380 along the pseudotime interval of [0,1].

381  
382 In adult GBM, NACA and PABPC1, and TPT1 and PSAP had similar expression patterns across  
383 all four differentiation paths (Fig 3B). S100B, OLIG1, and PHGDH all had a broad expression  
384 profile in path 4 (Fig 3B). Furthermore, the presence of four cell clusters in adult GBM  
385 landscape (Fig 2B) is in good agreement with previous classifications of four molecular  
386 subtypes of adult GBM (Verhaak et al., 2010). The expression of EGFR and PDGFRA were  
387 distinctly higher in one of the four cell fate clusters/attractors (Figure S4B). However, the  
388 expression of IDH1 exhibited oscillatory dynamics in all four paths/attractors (data not shown).  
389 In adult GSC, many of the identified markers had similar gene expression profiles in  
390 pseudotemporal ordering (Fig 3C). For instance, PTPRZ1, NACA and PABPC1, were all found  
391 to have similar expression dynamics in both transition paths (Fig 3C). Notably, OLIG 1 and  
392 OLIG2 were found to have similar expression patterns in all three patient groups across all cell  
393 fate transition trajectories of the landscape (Fig 3A-C).

394

395 Notably, we identified that genes such as STMN3, MTSS1 and TAZ are critical regulators in one  
396 transition pathway, while PSAP, TPT1, and PTPRZ1 are relevant for the other transition  
397 trajectory on the pediatric GBM's Waddington landscape (Fig 3A and S4A). The same trends in  
398 pseudotemporal gene expression patterns in STMN3 and PTPRZ1 have also been found in the  
399 adult GSC cell fate trajectories (see Fig S4C in the Supplementary Information). In all three  
400 patient groups, OLIG1, OLIG2, PHGDH, and TIMELESS had similar expression profiles within  
401 the distinct cell fate transition paths indicating potentially some network coordination or  
402 collective oscillations. Some signals (e.g., BCAN and CLU) were found to exhibit oscillations  
403 that may be indicative of complex dynamics with time-series expression analysis  
404 (Supplementary Information). These findings suggest that the identified markers involved in  
405 GBM/GSC cell fate decisions exhibit similar patterns in their expression dynamics, and that the  
406 identified critical genes are functionally putative master orchestrators of cell fate  
407 transitions/differentiation of the heterogeneous phenotypes within a GBM patient's tumor.



408

409 **FIGURE 3. Reconstructing pseudotime dynamics in GBM/GSC cell fate decisions of the**  
 410 **Waddington landscape.** Average normalized gene expression in cells plotted along  
 411 pseudotime after fitting with a cubic smoothing spline (black line). Cells are colored according to  
 412 cell clusters defined by scEpath. The expression patterns of the top genes identified by scEpath  
 413 and BigSCale algorithms (via correlation metrics) showed significant changes along the  
 414 pseudotime trajectory inferred by scEpath algorithm. Selected gene markers in A) pediatric  
 415 GBM, B) adult GBM, C) adult GSC.

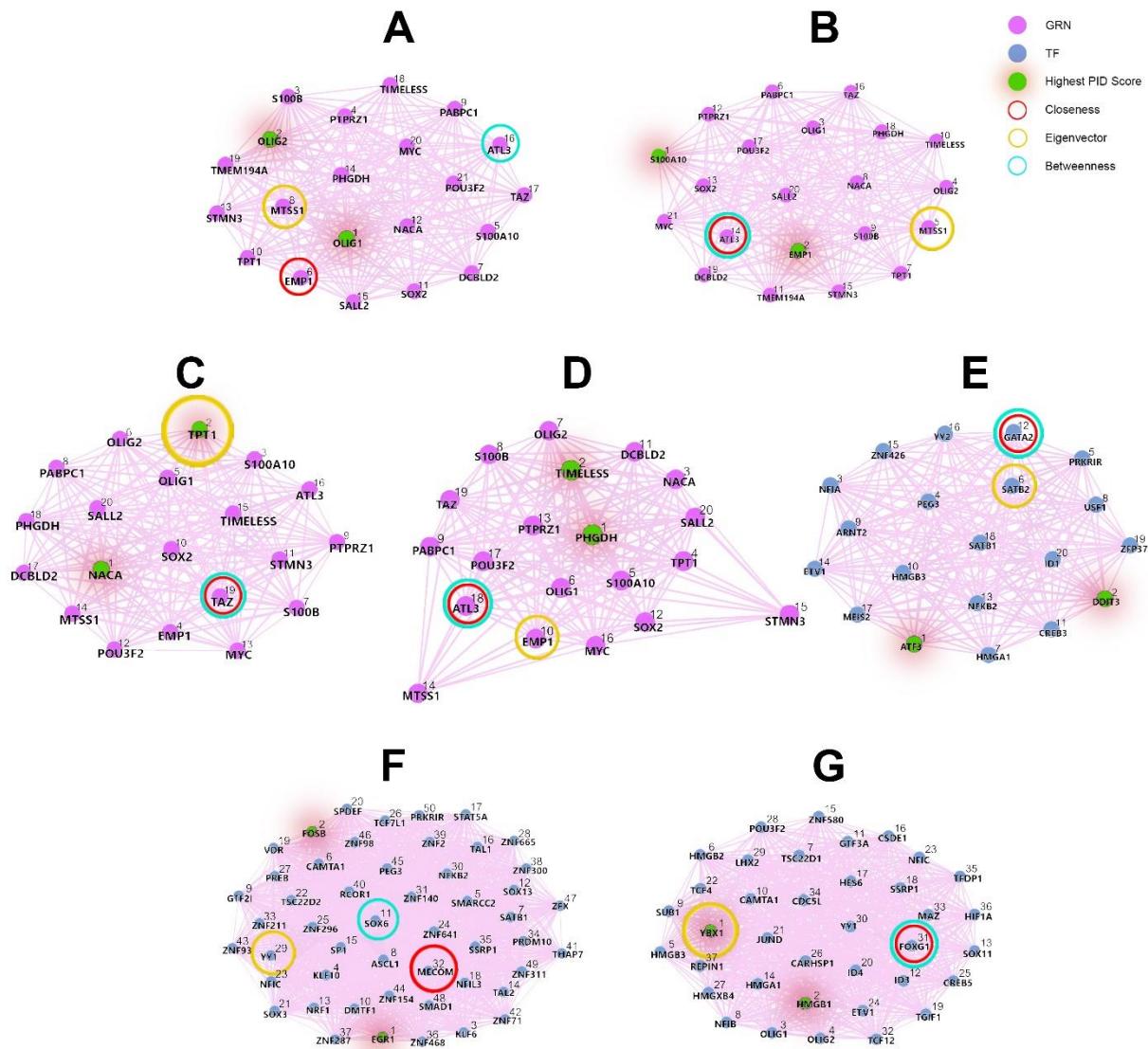
416

417 **3.3. PIDC Network Inference algorithm reconstructs the regulatory network**

418 **configurations driving GBM/GSC cell fate transitions.**

419 We next reverse engineered the signaling networks coordinating the information flow in GBM  
 420 and GSC using Partial Information Decomposition and Context (PIDC). Though the network  
 421 topography may seem similar, the arrangement of the interactions from highest influence on the  
 422 information flow (i.e., top PID scores) to those of the weakest interactions (lowest PID scores)

423 vary for each patient group. As seen in Figure 4A, OLIG1 and OLIG2 have the highest PID  
424 score of 1.9508, followed by S100B and PTPRZ1 interaction with a PID score of 1.9303 in  
425 pediatric GBM, suggesting a strong relationship between these two genes in the complex  
426 network steering their cell fate decisions (Fig 4A). We found that S100A10 and EMP1 have the  
427 highest interaction in adult GBM with a PID score of 1.9517 (Fig 4B), whereas NACA and TPT1  
428 had the highest interaction in adult GSC with a PID score of 1.9628 (Fig 4C). A distinct pattern  
429 was observed in the PIDC regulatory network of adult GSC sample BT127 (highest quality GSC  
430 cells). The highest interaction was observed between PHGDH and TIMELESS at a PID score of  
431 2.762. Other top interactions identified for the TF networks (Fig 4E-G) had similar  
432 pseudotemporal expression dynamics (Figure S4 A-C in the Supplementary Information). ATF3  
433 and DDIT3 were the top interaction markers from the critical TFs identified for pediatric GBM  
434 with a PID score of 1.971 (Fig 4E). EGR1 and FOSB in the adult GBM group (Fig 4F), and  
435 YBX1 and HMGB1 were identified as the top interaction TF markers, with PID score of 1.992  
436 (Fig 4G). These results suggest the reconfiguration of the nodes within the same complex  
437 signaling network may characterize GSC cells from GBM cells and distinguish pediatric GBM  
438 from adult GBM cell fate dynamics.



439

440 **FIGURE 4. Mathematical modelling identifies key regulatory genes driving GBM**  
441 **networks.** Gene regulatory networks of A) pediatric GBM, B) adult GBM, C) adult GSC, D) adult  
442 GSC sample BT127, E) pediatric GBM transcription factors, F) adult GBM transcription factors,  
443 and G) adult GSC transcription factors. In each, the signaling networks show the information  
444 flow between critical signals required for the complex cell fate dynamics. The GRN networks  
445 identified by Seurat and BigSCale are colored in violet nodes (Fig 4A-D) while the scEpath TF  
446 networks are colored in teal (Fig 4E-G). The ranks were assigned a priority index by the PID  
447 content as indicated by the numbers on the nodes. A high PID content implies a high mutual  
448 information (dependence) of those gene interactions in the information flow network. The  
449 number index on the nodes of the network correspond to the PID score in a decreasing order,  
450 where rank 1 denotes the top (highest) value. As shown in the legend, the nodes with the  
451 highest PID score are colored in green with a red shadow. Additionally, three different colored  
452 rings are used to identify the nodes of the networks with the highest network centrality  
453 measures as identified in Figure 5.

454 **3.4. Network centrality measures identify master regulators of information flow across**  
455 **the regulatory networks underlying GBM/GSC cell fate decision-making.**

456 Centrality is a key property of complex networks that influences the network dynamics and  
457 information flow (Iacono et al., 2019). The nodes (genes or TFs) with the highest centrality in the  
458 regulatory networks are the most biologically important signals. By measuring network  
459 centrality, we identified the primary genes regulating communication flow across each of the  
460 pediatric and adult GBM, and adult GSC networks (Table 2). In particular, we calculated the  
461 global clustering coefficient that measures the total number of closed triangles (link density) in a  
462 network. A clustering coefficient at its maximal value of 1 indicates that the neighbors of the  
463 gene (node)  $i$  form a complete graph (i.e., they all connect to each other) versus the converse  
464 for a clustering coefficient of 0 (Barabási and Posfai, 2016). We observed a lower clustering  
465 coefficient of 0.94 for the BT127 network in Figure 4D. In the transcription factor networks  
466 reconstructed from the scEpath heatmaps (italic columns, Table 2), the GSC TF network had  
467 the highest diameter, while the GBM networks (both pediatric and adult) had smaller diameters.  
468 The diameter is relatively in the same order of magnitude for the PIDC networks reconstructed  
469 from the Seurat-BigSCale markers (bold columns, Table 2) as they correspond essentially to the  
470 same set of genes interactions. The degree of centrality of all networks in Figure 4 was 1.0 at all  
471 nodes, except for the BT127 PIDC network which had a degree centrality of value of 1.0 only at  
472 nodes 1, 5, 10, 12, 13, and 16, and a clustering coefficient of value 0.96. The degree centrality  
473 of nodes 2, 7, and 8 were 0.89, the degree centrality of nodes 14 and 15 were roughly 0.5, and  
474 the remaining nodes had a degree centrality of 0.95.

475  
476 The closeness centrality identified genes/TFs occupying a central position in a network (Iacono  
477 et al., 2019). The nodes corresponding to the highest closeness centrality for each GRN  
478 network were found to be Node 6 (EMP1) for pediatric GBM, Node 14 (ATL3) for adult GBM,

479 Node 18 (ATL3) for GSC BT127, and Node 19 (TAZ) for GSC with closeness values of 1.398,  
480 1.361, 1.006, and 1.184, respectively (Fig 5A).

481

482 Nodes corresponding to the maximal closeness in the pediatric GBM, adult GBM, and adult  
483 GSC TF networks were found to be node 12 (GATA2), node 32 (MECOM), and node 31  
484 (FOXG1), respectively with closeness measures of 1.761, 2.563, and 1.478 respectively (Fig  
485 5B).

486 Betweenness centrality indicates the presence of regulatory bottlenecks (Iacono et al., 2019;  
487 Latora et al., 2017; Rodrigues, 2019). In our analyses, the highest betweenness measures for  
488 the pediatric GBM, adult GBM, BT127 adult GSC, and adult GSC GRN networks were node 16  
489 (ATL3), node 14 (ATL3), node 18 (ATL3), and node 19 (TAZ), respectively with betweenness  
490 values of 0.3947, 0.5842, 0.2690, and 0.4678, respectively (Fig 5C). The trends in maximal  
491 betweenness values (Fig 5C) were in good agreement with the nodes contributing to the  
492 maximal closeness values discussed in Fig 5A, indicating that identified nodes are critical  
493 targets governing the information flow in these complex networks. The highest betweenness  
494 values for the TF networks were found to be to node 12 (GATA2) for pediatric GBM, node 11  
495 (SOX6) for adult GBM, and node 31 (FOXG1) for adult GSC, with values of 0.3801, 0.2279, and  
496 0.1539, respectively (Fig 5D). The highest values of eigenvector centrality, a measure of  
497 information flow across the network, for the GRNs were found to be node 8 (MTSS1) for  
498 pediatric GBM, node 5 (MTSS1) for adult GBM, node 10 (EMP1) for BT127, and node 2 (TPT1)  
499 for GSC, with measures of 0.2796, 0.2827, 0.2909, and 0.2805, respectively.

500

501 The maximal eigenvector is a measure of the hub-score, i.e., the highest authority node of hub  
502 networks (Latora et al., 2017; Rodrigues, 2019). The maximal eigenvector centrality of the TF  
503 networks was found to be node 6 (SATB2) for pediatric GBM, and node 29 (YY1) for adult GBM,

504 and node 1 (YBX1) for GSC, with values of 0.2594, 0.1874, and 0.2322, respectively. SATB2 is  
505 a nuclear matrix-associated protein involved in chromatin remodelling and transcription  
506 regulation during neuronal differentiation (Gyorgy et al., 2008). Interestingly, all transition genes  
507 with high centrality measures identified in our network analyses, including EMP1, MTSS1,  
508 ATL3, and TPT1 have a TF-binding site for YY1 (Stelzer et al., 2016; GeneCards, 2021) (see  
509 Table 3).

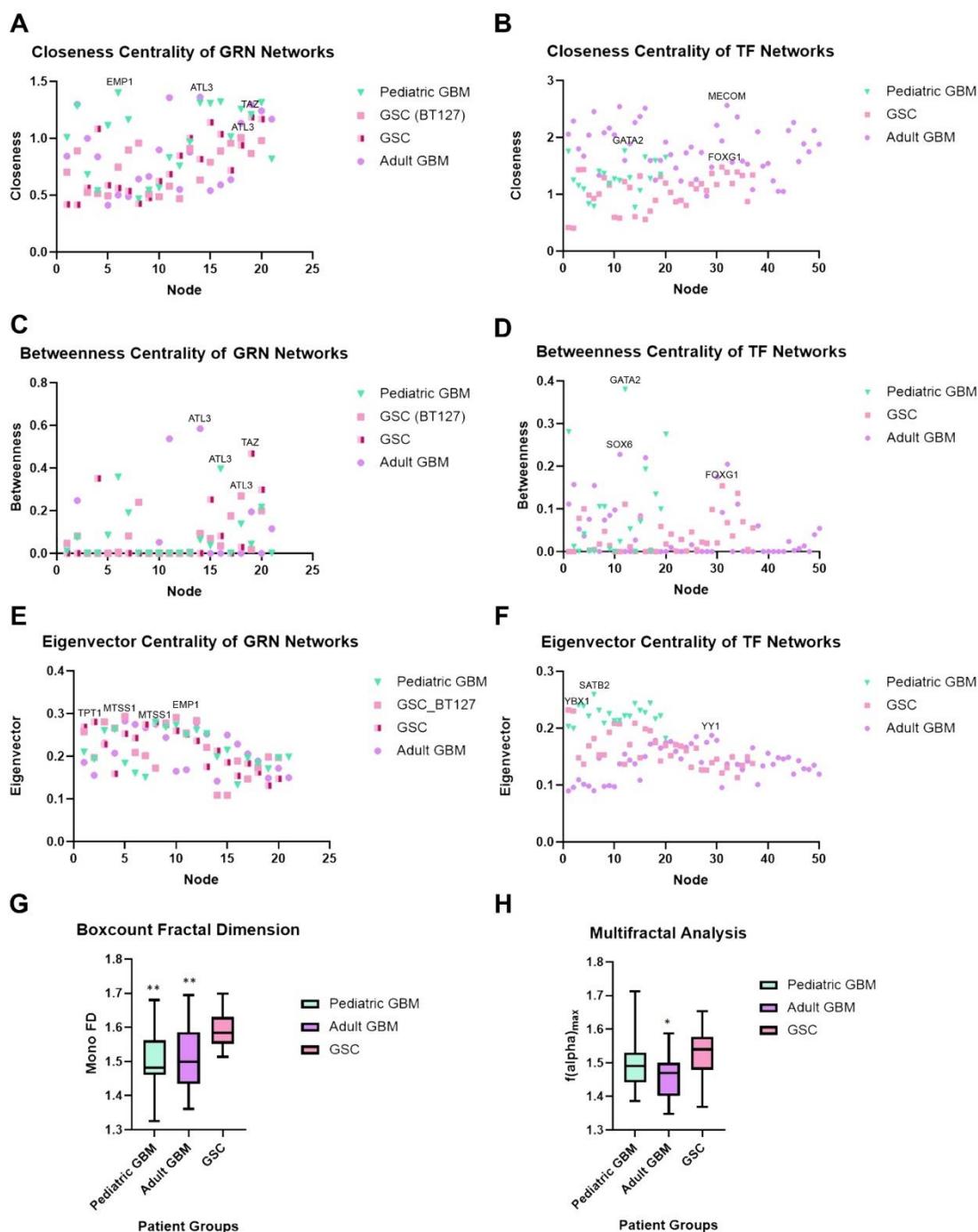
510

511 We also performed fractal analysis on the attractors (cell clustering patterns) in the scEpath  
512 Waddington landscapes. The fractal dimension scores obtained on the cell state attractors on  
513 the energy landscape were compared across all groups (pediatric GBM (n=7), adult GBM (n =  
514 18), and GSC (n=28)). The mean fractal dimension scores of the pediatric GBM, adult GBM,  
515 and adult GSC groups were  $1.502 \pm 0.099$ ,  $1.509 \pm 0.091$ , and  $1.588 \pm 0.051$ , respectively  
516 (Figure 5G). The FD scores of the two GBM groups were nearly identical, while a statistically  
517 significant difference was observed from the GSC group. The multifractal spectrum  $f(\alpha)$  was  
518 extracted from the multifractal spectra of the individual cancer samples energy landscape  
519 (n=54) (Fig 5H). Only the difference between GSC versus adult GBM was found to be  
520 statistically significant ( $p=0.0201$ ) by a Kolmogorov-Smirnov test. The pediatric GBM, and adult  
521 GBM and GSC groups had a maximal multifractal spectrum  $f(\alpha)$  value of  $1.499 \pm 0.092$ ,  $1.462$   
522  $\pm 0.066$ , and  $1.521 \pm 0.075$ , respectively.

Network Properties	Pediatric GBM	Adult GBM	Adult GSC	BT127 (Adult GSC)	Pediatric GBM (TF Network)	Adult GBM (TF Network)	Adult GSC (TF Network)
$G(V, E)$	(21,210)	(21,210)	(20,190)	(20,174)	(20,190)	(50, 1225)	(37,666)
Center	16	14	19	18	8	15	31
Diameter	3.037	3.283	3.490	3.106	1.869	1.474	3.936
Global Clustering Coefficient	1.00	1.00	1.00	0.94	1.00	1.00	1.00

523

524 **TABLE 2. General Properties of Inferred Complex Networks.**  $G(V, E)$  denotes the graph with  
 525 the number of vertices  $V$  (the genes) and number of edges  $E$  for each inferred GRN network.  
 526 The center values designate to the node index (gene) acting as the center of the simple  
 527 weighted network. The clustering coefficient captures the degree to which the neighbors of a  
 528 given node link to each other.



530 **FIGURE 5. Centrality measures distinguish master regulators of information flow in GBM**  
531 **networks.** Three network centrality measures are assessed on the reconstructed GBM/GSC  
532 networks. Three different network centralities were computed on the reconstructed networks:  
533 closeness, betweenness, and eigenvector centrality. The genes (nodes) occupying the highest  
534 of these centrality measures correspond to critical nodes steering the information flow in the  
535 complex signaling networks governing GBM/GSC cell fate transition dynamics. A) Closeness  
536 centrality of inferred GRNs. B) Closeness centrality of TF networks. C) Betweenness centrality  
537 of gene regulatory networks. D) Betweenness centrality of transcription factor networks. E)  
538 Eigenvector centrality of gene regulatory networks. F) Eigenvector centrality of transcription  
539 factor networks. G) Fractal dimension of cell state attractors on scEpath energy landscapes. A  
540 p-value of 0.0031 between the adult GSC and adult GBM, and p= 0.0011 between adult GSC  
541 and pediatric GBM was calculated for the box-count algorithm's fractal dimension scores using  
542 the Kolmogorov-Smirnov test. Multifractal analysis of cell fate attractors on scEpath Waddington  
543 landscapes.

544

#### 545 4. DISCUSSION

546 Here we applied a collection of data theoretic and complexity science approaches to single cell  
547 RNA-seq data from pediatric and adult GBM, and adult GSCs to distinguish genes regulating  
548 communication within these cellular populations. Our findings demonstrate the application of  
549 these tools for deciphering GBM/GSC signaling networks to understand how network  
550 configuration orchestrates information flow and determines cell fate dynamics.

551

552 Multiple clustering algorithms were deployed to cross-validate their findings and ensure that the  
553 differential markers extracted for network analysis were robust, complementary, and of high  
554 importance in cell fate transition/differentiation mapping. There is a high degree of heterogeneity  
555 displayed by GBM stem cells. The complementarity of our results in our independent and  
556 orthogonal approaches are outlined in Table 3 by the associations identified between the  
557 transition genes and the scEpath TFs. Our approach using distinct clustering techniques and  
558 verifying their matching or complementary results was deployed to minimize the effects of  
559 expression heterogeneity and validate our findings (Krieger et al., 2020).

TRANSITION GENES	TRANSCRIPTION FACTORS
ATL3	YY1, FOSB, SOX6, GATA2, ATF3, EGR1, MYC
MTSS1	YY1, ATF3, MYC

EMP1	YY1, FOSB, GATA2, ATF3, MYC
TPT1	YY1, ATF3, FOSB, SOX6, EGR1, OLIG1/2
PTPRZ1	YY1, YY2, EGR1, NANOG, POUF51
S100B	YY1, GATA2, EGR1, SOX6, MYC

560 **TABLE 3. Interactions between transition genes and transcription factors identified in**  
561 **network analysis.** Amidst the critical transition genes listed, the first four were identified as the  
562 central regulators of information flow across the GBM/GSC regulatory networks, while PTPRZ1  
563 and S100B were other differential markers identified in our analyses. The list is not inclusive of  
564 all possible gene-TF interactions but restricted to the analysis of only the high importance (i.e.,  
565 highest network centrality measures) scEpath TFs identified in our findings. The TF-gene  
566 interactions were identified using the GeneCards human gene database (GeneCards, 2021).

567  
568 Using scEpath, we identified three and four meta-clusters in the pediatric GBM (Fig 2A) and  
569 adult GBM (Fig 2B), respectively, while sub-clusters within each meta-cluster indicated the  
570 presence of phenotypic heterogeneity and plasticity. However, the number of meta-clusters was  
571 ambiguous in the adult GSC landscape (Fig 2C), as shown by the continuous progression from  
572 the higher energy state clusters (stem-like fates) to the lower energy states indicating the  
573 potential presence of a complex attractor. An alternative measure to assess the significance of  
574 the scEpath clustering is the transition paths (cell fate trajectories). We predicted that the  
575 number of clusters identified in the pediatric GBM group corresponds to the neuronal, astrocytic-  
576 mesenchymal, and oligodendrocytic lineages, mirroring the healthy brain's neurodevelopmental  
577 hierarchy (Jessa et al., 2019; Couturier et al., 2020). Similarly, the four clusters identified in the  
578 adult GBM group correspond to the four groups identified by Neftel et al. (2019), namely the  
579 OPC-like (oligodendrocytic progenitor cell), NPC-like (neuronal progenitor cell-like), AC-like  
580 (astrocytic cell-like), and MES-like (mesenchymal cell) lineages. Further, the infiltrated immune  
581 cells (i.e., T-cells and macrophages) grouped into the MES-like state (Neftel et al., 2019).  
582 Pediatric GBM cells showed less differentiation than the adult GBM samples, as indicated by  
583 the higher energy cell-states, suggesting a closer resemblance to the GSC sample. The two cell  
584 fate trajectories observed in the adult GSC sample may correspond to the transcriptional  
585 gradient of two cellular states observed in the original study by Richards et al. (Fig 2C), which

586 were shown to mirror normal neurodevelopment and inflammatory wound responses (Richards  
587 et al., 2021).

588

589 The cell fate trajectories along the scEpath Waddington landscape (Figure 2A-C) were  
590 determined by the transition probabilities of the probabilistic directed graph reconstructed from  
591 the cell fate clusters, where the weighted edges of the networks correspond to the average  
592 normalized gene expression (see Supplementary Information for additional details). scEpath  
593 used the minimum directed spanning tree to find the maximum probability flow and minimal  
594 number of edges along the network, since cell fates transition to lower energy states during  
595 differentiation. The resulting tree approximates the cell state transition network and infers the  
596 observed developmental trajectories/lineage structures. The weighted edges of the cell state  
597 transition network were found to be proportional to the gene expression values seen in Figure 3,  
598 where the number of developmental trajectories inferred are indicated by the path numbers in  
599 Figure 2. Thus, two cell fate trajectories were detected in the pediatric GBM and adult GSC  
600 samples while four developmental trajectories were observed in adult GBM.

601

602 In pediatric GBM, the expression of transcription factors in pseudotime was shown to be highly  
603 nonlinear. Certain genes, including GATA2, were even found to be oscillatory in one trajectory  
604 while demonstrating an increasing or decreasing gradient of expression along the other cell fate  
605 trajectory. Likewise, patterns of other critical transition genes (TFs) were identified along the  
606 attractor dynamics between the distinct transcriptional states of adult GBM and adult GSC cells.  
607 Further, we found that genes such as EMP1, MTSS1, PTPRZ1 and S100B exhibited distinct  
608 gene expression oscillations in one differentiation trajectory (path) over the other(s) (Figure 3).  
609 These genes were also found to have TF-binding sites for the scEpath identified TFs with the  
610 highest network centrality measures in our downstream analysis (Figure 4). Together, these  
611 findings are indicative of a highly interconnected network of gene-TF interactions governing

612 GBM/GSC cell fate decisions, and further suggest that the information flow across the inferred  
613 networks may steer cell fate decisions towards complex attractors on the GBM/GSC  
614 Waddington landscape.

615

616 Using network centrality measures, we identified OLIG1/2, TAZ, GATA2, FOXG1, SOX6,  
617 SATB2, YY1, and gene targets ATL3, MTSS1, EMP1, and TPT1 as critical genes governing the  
618 cell fate dynamics of GBM and GSC cells (Fig 5A-F). Many of these signals are  
619 neurodevelopmental transcription factors involved in healthy brain development, essential for  
620 conferring and maintaining cancer stem cells (GSCs). Maximal centrality scores indicated that  
621 they are key regulators of the network information flow in both GBM groups and GSCs. The  
622 functional significance of these transcription factors (see Supplementary Information) suggests  
623 their critical role in stem cell decision-making and differentiation dynamics. Our findings indicate  
624 that these genes may be strong candidates for therapeutic interventions points for the treatment  
625 of GBM. Other signaling interactions such as PTPRZ1 and S100B were identified in our  
626 analyses as potent clinically druggable targets in the treatment of GBM. Furthermore, we  
627 predicted that GATA2 and MTSS1 may provide a common ground for interlinking  
628 leukemogenesis, the complex signaling dynamics of leukemia/lymphoma affecting children, and  
629 pediatric glioma/GBM (Menendez-Gonzalez et al., 2019, Schemionek et al., 2015).

630

631 BDM was used to distinguish which of the differential markers can accurately  
632 classify/differentiate the three patient group samples (see Supplementary Information). We  
633 identified FOSB, HMGB1 and EGR1 as differential signatures which can accurately predict the  
634 patient groups in our single-cell analyses (see SI). The algorithmic complexity measured by the  
635 BDM allowed for the identification of critical network genes differentiating GBM and GSC  
636 phenotypes with the minimal information. The rationale for using gene/TF markers' BDM as a  
637 phenotypic discriminant is that the algorithmic complexity denotes the shortest algorithm or

638 minimal set of information within the complex networks inferred required to classify the distinct  
639 patient groups. As such, the identified genes/TFs may be useful biomarkers for prognostic  
640 screening and disease phenotyping in clinical medicine.

641

642 From the transcription factor (TF) networks identified by scEpath (Table 3), we distinguished  
643 some TFs to form interactions with some of the differential gene markers, suggesting cellular  
644 reprogramming targets for controlling GBM cell fate dynamics. Our study therefore quantifies  
645 how these markers' expression vary in the cell fate transitions from stem-like to mature  
646 phenotypes. For a discussion on the biological significance of key genes and transcription  
647 factors identified in our analyses, see the Supplementary Results in the Supplementary  
648 Information.

649

650 The cell fate transition markers identified in our study, including PTPRZ1, EMP1, S100B, and  
651 MTSS1, are in good agreement with the findings from the original studies (SCP393 and  
652 SCP503). Although some of the signatures we identified overlap with the differential expression  
653 patterns of the original studies, they did not compare the co-expression of these markers  
654 between GSC and GBM. Markers differentiating distinct cellular states have been previously  
655 investigated (for instance, the original study by Neftel et al. identified copy number  
656 amplifications of the CDK4, EGFR, and PDGFRA loci and mutations of the NF1 locus, each  
657 favoring one of the four GBM phenotypes (Neftel et al., 2019)). Our study instead analyzed the  
658 expression patterns which fluctuate or form a differentiation gradient across the distinct cell  
659 states. Further, while previous studies have associated the differentiation markers of GBM  
660 progression identified here, our study demonstrates their novel integrated application to  
661 elucidate the roles of these network biomarkers in GBM cell fate decisions and differentiation  
662 dynamics. Indeed, while many of the identified genes or TFs have been previously studied in  
663 the context of neurodevelopmental regulation and glioma cell fate dynamics, most of those

664 selected in our analyses are not yet documented in glioblastoma cell fate control. As such, we  
665 propose the identified interactions in Table 3 may provide clinically relevant GBM-specific  
666 precision therapeutics, and that our network analyses provide a quantitative tool to characterize  
667 which of the markers were of high importance (i.e., high centrality measures) in cell fate control,  
668 plasticity regulation, and transition dynamics. Future studies should exploit tools from  
669 algorithmic complexity theory including algorithmic network perturbation analysis (i.e., quantify  
670 the BDM changes across a network by node or link deletion) to better elucidate the inferred  
671 network dynamics in cancer cell fate control and regulation.

672

673 While previous GBM gene regulatory network inference methods vary from our approaches, our  
674 findings are consistent with their results. For example, Sun et al. found 15 hub genes in GBM-  
675 specific miRNA-TF networks, including PDGFRA and SOX11, and 6 hub TFs (including GATA1)  
676 as key regulators of GBM dynamics (Sun et al., 2012). In our study, we also identified PDGFRA  
677 and SOX11 as hub genes of the inferred GBM networks, and found that GATA2, an alternate  
678 isoform, overlapped with these findings. However, Sun et al. (2012) did not compare GBM of  
679 different age groups nor consider GBM-derived stem cells for reconstruct their differentiation  
680 networks. Similarly, a network inference study by Ping et al. (2015) revealed 17 hub genes in  
681 GBM networks, including EGFR and PDGFRA, as gene signatures of the proneural GBM  
682 subtype, both of which were identified in our analyses. In another study, GSEA and IPA-based  
683 gene enrichment pathway analysis discovered TAZ as a key regulator of GBM networks  
684 (Bozdag et al., 2014), which was also identified as a master regulator of GBM differentiation  
685 dynamics in our analyses.

686

687 Using multi-omic analyses, Suva et al. distinguished OLIG2, POU3F2 SALL2, and SOX2 as hub  
688 genes of GBM stemness networks critical for their tumor-propagation potential (Suvà et al.,  
689 2014). Our findings identified OLIG2 as a master control gene of GBM differentiation dynamics

690 and established a connection between SOX2 expression and the critical hub gene FOXG1.  
691 Further, some epigenetic profiling studies have shown that aberrant histone modifications and  
692 methylation profiles are molecular signatures driving pediatric GBM and distinguishing them  
693 from their adult counterparts (Jones et al., 2017, Lulla et al., 2016, Sturm et al., 2012). Sturm et  
694 al. (2012) revealed that the TFs OLIG1, OLIG2 and FOXG1 are the master regulators of the hub  
695 gene networks driving these oncohystone pediatric GBM variants (i.e., K27M and G34V/R).  
696 Similar findings were recently reported by Wang et al. (2021), who identified the same set of  
697 TFs as critical drivers of pediatric high-grade gliomas' epigenetic landscapes. We identified all  
698 three TFs reported by Sturm et al. and Wang et al. in our network approaches as critical  
699 regulators of GBM cell fate dynamics. Thus, our findings recapitulate the complex network  
700 dynamics driving the oncohystone variants of pediatric GBM and validate and extend previous  
701 findings.

702  
703 It should be noted that there is a good deal of heterogeneity within the single-cell datasets  
704 across and with the patient groups. The original datasets contained 8 pediatric GBM samples,  
705 20 adult GBM samples, and 28 adult GSC samples. For the initial clustering (i.e., differential  
706 discovery using Seurat and BigSCale), samples--two adult GBM and one pediatric GBM-- with  
707 the highest drop-out rate (i.e., zero counts) were removed as a data filtering and quality control  
708 step prior to normalization. Subsequently, the number of adult GBM samples in the scEpath  
709 analysis was randomly selected to closely match the cell count numbers of the adult GSC  
710 patient groups. The down-sampling of GSC samples was necessary since scEpath analysis has  
711 a computational limitation on the number of samples which can be processed (roughly 2500  
712 cells). As noted in the Methods, selecting a different combination of GSC samples did not  
713 change the results and including the removed samples did not change the differential marker  
714 discovery or expression analyses. Indeed, the global clustering patterns remained the same  
715 although there was greater dispersion in the local sub-clusters in the Seurat and BigSCale

716 pattern space. However, including all n=8 pediatric GBM patient samples generated a shorter  
717 list of transition genes with abrupt transitions between the distinct phenotypes.

718

719 A limitation of our study is that we did not have access to pediatric GSC cells, given that adult  
720 GSC data have only recently been described (Richards et al., 2021). There may be other hidden  
721 causal interactions interconnecting the nodes of the complex networks we inferred that were not  
722 identified due to lack of data. Further, the lack of time-series scRNA-Seq counts is a barrier to  
723 understanding the complex dynamics of GBM/GSC networks. The pseudotemporal dynamics  
724 consist of inferred cell fate trajectories in a dimensionality-reduced data space (i.e., PCA space)  
725 by transcriptional similarity of cell fates. Ribosomal proteins and certain cytoskeletal markers  
726 (housekeeping genes) were also not pooled with the differential expression signatures for  
727 network inference (Figure S1).

728

729 This proof-of-concept study provides a comprehensive method to dissect the cybernetics of  
730 cancer cellular ecosystems and their cell fate dynamics. Current bioinformatic pipelines in  
731 cancer data science largely fail to reconcile the complex dynamics and temporal features of  
732 GBM transcriptional states, as they either take a reductionist approach to inferring gene  
733 expression patterns or rely on statistical correlation methods. In contrast, our framework  
734 provides a pipeline for causal pattern discovery and thereby allows the prediction/forecasting of  
735 how the differentially expressed transition genes control and regulate cell fate decision-making.  
736 Further, our approach allows for the mapping of these cancer cell fate behaviors to information  
737 flow across the inferred complex networks. Thus, these causal inference tools shed light on  
738 emergent behaviors in cell fate decisions such as transcriptional heterogeneity from a dynamical  
739 systems perspective. As such, we propose our methodological framework may provide a  
740 complementary and potentially more useful means to assess how the heterogeneous cancer

741 phenotypes exhibit adaptive (emergent) behaviors and help forecast their dynamic response to  
742 drug/therapeutic perturbations at the level of molecular interactions.

743

## 744 **6. CONCLUSION**

745 This study demonstrates the use of complex systems approaches in deciphering the cybernetics  
746 of GBM/GSC networks, and shows how signaling dynamics differ between pediatric GBM, adult  
747 GBM, and adult GSC populations. By identifying transcription factors and genes, our combined  
748 approach serves as one part of the precision medicine toolbox for the treatment of GBM,  
749 suggesting both precision therapeutic targets and GBM reprogramming factors.

750

751 Prospective studies should explore the use of artificial neural networks, including Deep Learning  
752 algorithms, for single-cell transcriptomic analyses. Further, causal inference-based network  
753 inference methods such as Bayesian networks and algorithmic information dynamics should be  
754 investigated for GBM regulatory networks reconstruction. The epigenetic regulation of our  
755 identified transcriptional networks must be explored using high-throughput multi-omics datasets.  
756 Our network approaches should be extended to protein-protein interaction networks, epigenetic  
757 networks, and metabolic networks to investigate multi-omic levels of GBM heterogeneity,  
758 including oncohistone variants (i.e., K27M, K36M, G34V/R) and IDH1/2-mutants observed in  
759 pediatric gliomas (GBM).

## 760 **DECLARATIONS**

761 **DECLARATIONS STATEMENT:** The authors declare no competing interests.

762 **ETHICS APPROVAL AND CONSENT TO PARTICIPATE:** Not Applicable

763 **AUTHOR CONTRIBUTIONS:** AU performed the algorithms, wrote, and edited the manuscript.  
764 MC supervised, wrote, and edited the manuscript.

765 **FUNDING:** MC was funded by Natural Science and Engineering Research Council of Canada  
766 Discovery Grant RGPIN-2018-04546 and an FRQS Research Scholar grant (J1).

767 **DATA AND CODE AVAILABILITY:**

768 The datasets supporting the conclusions of this article are available in the Single Cell Portal  
769 repository:

770 [https://singlecell.broadinstitute.org/single\\_cell/study/SCP393/single-cell-rna-seq-of-adult-and-pediatric-glioblastoma#study-summary](https://singlecell.broadinstitute.org/single_cell/study/SCP393/single-cell-rna-seq-of-adult-and-pediatric-glioblastoma#study-summary)

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773 [https://singlecell.broadinstitute.org/single\\_cell/study/SCP503/gradient-of-developmental-and-injury-reponse-transcriptional-states-define-functional-vulnerabilities-underpinning-glioblastoma-heterogeneity#study-download](https://singlecell.broadinstitute.org/single_cell/study/SCP503/gradient-of-developmental-and-injury-reponse-transcriptional-states-define-functional-vulnerabilities-underpinning-glioblastoma-heterogeneity#study-download)

774  
775  
776

777 All Codes and Algorithms used for the single-cell data analysis are available in the project  
778 GitHub page:

779 [https://github.com/Abicumaran/GBM\\_Complexity\\_I](https://github.com/Abicumaran/GBM_Complexity_I)

780

781 **Software/Algorithms:**

782 **Seurat**

783 Project name: Seurat V3

784 Project home page: <https://github.com/satijalab/seurat/>

785 Archived version: 10.1016/j.cell.2019.05.031

786 Operating system(s): Platform independent

787 Programming language: R

788 Other requirements: Not Applicable

789 License: GNU Public License (GPL 3.0)

790 Any restrictions to use by non-academics: Not Applicable

791

792 **BigScale**

793 Project name: BigScale V2

794 Project home page: <https://github.com/iaconogi/BigSCale2>

795 Archived version: 10.1186/s13059-019-1713-4

796 Operating system(s): Platform independent

797 Programming language: R

798 Other requirements: C++

799 License: Not Applicable

800 Any restrictions to use by non-academics: Not Applicable

801

802 **scEpath**

803 Project name: single-cell Energy path (scEpath)

804 Project home page: <https://github.com/sqjin/scEpath>

805 Archived version: 10.1093/bioinformatics/bty058

806 Operating system(s): Platform independent

807 Programming language: MATLAB

808 Other requirements: C++

809 License: Not Applicable

810 Any restrictions to use by non-academics: Not Applicable

811

812

813 **OACC**

814 Project name: Online Algorithmic Complexity Calculator V3  
815 Project home page: <https://github.com/algorithmicnaturelab/OACC>  
816 Archived version: 10.1016/j.isci.2019.07.043  
817 Operating system(s): Platform independent  
818 Programming language: R  
819 Other requirements: Not Applicable  
820 License: GNU Public License (GPL 3.0)  
821 Any restrictions to use by non-academics: Not Applicable  
822

### **Network Inference**

823 Project name: NetworkInference.jl and Partial Information Decomposition (PID)  
824 Project home page: <https://github.com/Tchanders/NetworkInference.jl>  
825 Archived version: 10.1016/j.cels.2017.08.014  
826 Operating system(s): Platform independent  
827 Programming language: Julia  
828 Other requirements: Not Applicable  
829 License: MIT "Expat" License  
830 Any restrictions to use by non-academics: Not Applicable  
831  
832

### **Julia LightGraphs**

833 Project name: LightGraphs.jl V1.3  
834 Project home page: <https://github.com/JuliaGraphs/SimpleWeightedGraphs.jl>  
835 Archived version: Not Applicable  
836 Operating system(s): Platform independent  
837 Programming language: Julia  
838 Other requirements: Jupyter Notebook and HTML  
839 License: MIT "Expat" License  
840 Any restrictions to use by non-academics: Not Applicable  
841  
842

### **SciKit-learn:**

843 Project name: Scikit-learn  
844 Project home page: <https://scikit-learn.org/> or <https://github.com/scikit-learn/scikit-learn>  
845 Archived version: <http://jmlr.org/papers/v12/pedregosa11a.html>  
846 Operating system(s): Platform independent  
847 Programming language: Python ( $\geq$  V3.7)  
848 Other requirements: NumPy ( $\geq$  1.14.6), SciPy ( $\geq$  1.1.0), joblib ( $\geq$  0.11), threadpoolctl ( $\geq$  2.0.0),  
849 Google Colab or Jupyter Notebook  
850 License: 3-Clause BSD license  
851 Any restrictions to use by non-academics: Not Applicable  
852  
853

### **FracLac**

854 Project name: FracLac V2.5  
855 Project home page: <https://imagej.nih.gov/ij/plugins/fraclac>  
856 Archived version: Not Applicable  
857 Operating system(s): Platform independent  
858 Programming language: Java  
859 Other requirements: Not Applicable  
860 License: National Institute of Health (NIH) Public License  
861 Any restrictions to use by non-academics: Not Applicable  
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