1 **Correlating fluorescence microscopy, optical and magnetic tweezers to study single chiral**
2 **biopolymers, tested on DNA plectoneme formation dynamics**

3

4 Jack W Shepherd[1,2]*, Sebastien Guilbaud[1]*, Zhaokun Zhou[3]*, Jamieson Howard[1]*, Matthew
5 Burman[1], Charley Schaefer[1], Adam Kerrigan[4], Clare Steele-King[5], Agnes Noy[1], and Mark C Leake[1,2, †]

6 [1] School of Physics, Engineering and Technology, University of York, York, YO10 5DD
7 [2] Department of Biology, University of York, York, YO10 5DD
8 [3] Guangdong Provincial Key Lab of Robotics and Intelligent System, Shenzhen Institute of Advanced
9 Technology, Chinese Academy of Sciences, China
10 [4] The York-JEOL Nanocentre, University of York, York, YO10 5BR
11 [5] Bioscience Technology Facility, University of York, York, YO10 5DD

12 [†] For correspondence. Email mark.leake@york.ac.uk
13 * Authors contributed equally

14

Abstract

16 Biopolymer topology is critical for determining interactions inside cell environments, exemplified by
17 DNA where its response to mechanical perturbation is as important as biochemical properties to its
18 cellular roles. The dynamic structures of chiral biopolymers exhibit complex dependence with
19 extension and torsion, however the physical mechanisms underpinning the emergence of structural
20 motifs upon physiological twisting and stretching are poorly understood due to technological
21 limitations in correlating force, torque and spatial localization information. We present COMBI-
22 Tweez (Combined Optical and Magnetic BIomolecule TWEEZers), a transformative tool that
23 overcomes these challenges by integrating optical trapping, time-resolved electromagnetic
24 tweezers, and fluorescence microscopy, demonstrated on single DNA molecules, that can
25 controllably form and visualise higher order structural motifs including plectonemes. This technology
26 combined with cutting-edge MD simulations provides quantitative insight into complex dynamic
27 structures relevant to DNA cellular processes and can be adapted to study a range of filamentous
28 biopolymers.

29

Keywords

31 Optical tweezers, Magnetic tweezers, Fluorescence microscopy, Plectonemes, DNA topology, Single-
32 molecule

33

34 Multiple cell processes involve chiral biopolymers experiencing pN scale forces[1] and torques of tens
35 of pN.nm[2], exemplified by molecular machines on DNA[3] where torsion is a critical physical factor[4].
36 Although lacking torsional information, optical tweezers (OT) combined[5] with fluorescence
37 microscopy of dye-labelled DNA was used to image DNA extension in response to fluid drag[6], and
38 though missing topological details from fluorescence visualisation, magnetic tweezers (MT)
39 experiments have demonstrated how DNA molecules respond to force combined with supercoiling[7].
40 Developments in OT and MT have enabled molecular study of DNA over-stretching[8], protein
41 binding[9], dependence of mechanical properties to ionicity[10], and DNA-protein bridge formation[11].
42 Fluorescence microscopy combined with OT have enabled super-resolved measurement of extended
43 DNA in the absence of torsional constraints[12,13], with angular OT enabling torque control[14]. High-
44 precision MT has facilitated single-molecule DNA study of over- and undertwisting, including twist-
45 stretch coupling[15], dependence of torsion on temperature[16] and salt[17], and binding of filament-
46 forming proteins such as RecA[18]. MT has enabled single-molecule torsion dependence
47 measurements of non-canonical DNA structures including P-DNA[19], left-handed DNA[20] and higher-

48   order motifs of the G-quadruplex[21] and plectonemes[22], applying vertical geometries to extend
49   molecules orthogonal to the focal plane. DNA plectonemes have been visualised using fluorescence
50   microscopy combined with MT, by reorienting molecules almost parallel to the focal plane, limited
51   to observations *following* but not *during* plectoneme formation[20]. Plectoneme formation has also
52   been induced through intercalator binding to DNA combed onto surfaces then imaged with
53   fluorescence microscopy to track plectonemes[23].

54   OT combined with fluorescence have been used to study DNA over-stretching in torsionally
55   unconstrained DNA[24], revealing S-DNA structures by measuring polarized emissions from bound
56   fluorophores[25]. Later developments using torsional constraints were implemented by stochastic
57   stretch-unbind-rebinding applied to single optically trapped DNA molecules, with a caveat that
58   supercoiling cannot be controlled in advance, or reversed[26].

59   Simulations have enabled insight into DNA structural transitions, coarse-grained approaches using
60   oxDNA[27] on mechanically[28–30] and thermally perturbed DNA[15], and all-atom methods which predict
61   sequence-dependence to torsionally-constrained stretching[31] and explore the denaturing pathways
62   of torsionally unconstrained stretching[32]. Simulations have also been used with single-molecule MT
63   via space-filling algorithms to predict P-DNA formation[19] and molecular dynamics (MD) simulations
64   to study stretch/twist coupling[15]. More recently, DNA minicircles comprising just a few hundred base
65   pairs (bp) have been used as computationally tractable systems to investigate supercoiling[33] and
66   using AFM imaging[34].

67   Single-molecule experiments used to probe DNA mechanical dependence on structural
68   conformations have advantages and limitations. OT enables high forces beyond the ~65 pN
69   overstretching threshold up to ~1 nN [35]. However, they cannot easily control torque of extended
70   molecules without non-trivial engineering of trapping beams and/or the trapped particle's shape[36],
71   and establishing stable torque comparable to MT using readily available microbeads is not feasible.
72   While MT can enable reversible supercoiling of single molecules at ~pN forces[7,19], mechanical
73   vibrations over ~seconds introduced during rotation of nearby permanent magnets places
74   limitations on structural transitions probed.

75   We present Combined Optical and Magnetic Biomolecule TWEEZers (COMBI-Tweez), which
76   overcomes these challenges. COMBI-Tweez is a bespoke, correlative single-molecule force and
77   torsion transduction technology colocating low stiffness near infrared (NIR) OT with laser excitation
78   fluorescence microscopy on DNA molecules in a ~mT B field, generated by pairs of Helmholtz coils,
79   rotated in orthogonal planes independently under high-precision control (Supplementary Movie 1).
80   OT and MT can be operated independently, while a trapped fluorescently-labelled DNA molecule,
81   which we use as well-characterized test chiral biopolymer, can be extended parallel to the focal
82   plane to enable fluorescence imaging in real time with sub-nm displacement detection via laser
83   interferometry. To our knowledge, this is the first report of stable optical trapping of magnetic beads
84   at physiologically relevant temperatures.

85   We demonstrate this technology through time-resolved formation and relaxation of higher-order
86   structural motifs including plectonemes in DNA; these emergent features comprise several open
87   biological questions which relate to plectoneme size, position and mobility. We measure changes to
88   the buckling transition[37] due to binding of the fluorescent dye SYBR Gold[38], and controlled
89   quantification of interactions between two "braided" DNA molecules. We discuss these findings in
90   the context of modelling structural motifs using MD simulations. The unique capability of COMBI-
91   Tweez is the correlative application of several single-molecule techniques on the same biopolymer
92   molecule, not attainable with a subset of techniques alone. OT enables high-bandwidth force
93   measurement, while MT generates magnetic microbead rotation to induce controlled torque with
94   no mechanical noise or lateral force. Control software enables precise tuning of supercoiling density
95   σ, with bead rotation verified using fluorescence imaging of conjugated reporter nanobeads. We
96   demonstrate COMBI-Tweez using high-sensitivity fluorescence detection whose utility can be easily

97 extended to multiple fluorescence excitation and surface functionalization methods, with future
98 applications to study several generalised biopolymers.

99 **Results**

100 **Decoupling force and torque**

101 COMBI-Tweez OT control of force and displacement, with MT control of torque (Fig. 1a,b,
102 Supplementary Movie 1) is simple and robust. No modifications to NIR laser trapping beams are
103 required, such as Laguerre-Gaussian profiles to impart angular momentum[39], nor nanoscale
104 engineering such as cylindrical birefringent particles[40]. Since COMBI-Tweez OT controls bead
105 displacement, dynamic B field gradients that update continuously to reposition the bead, common in
106 MT-only systems[41], are not required. We use a uniform B field via two pairs of coils carrying
107 sinusoidal currents to rotate an optically trapped magnetic bead (Fig. 1c, online methods,
108 Supplementary Note 1 and Supplementary Figs. 1-8). Decoupling force and torque allows COMBI-
109 Tweez to exert arbitrary combinations of sub-pN to approximately 10 of pN and of sub-pN·nm to
110 tens of pN·nm, relevant for cellular processes involving DNA such as plectoneme formation[42].
111 COMBI-Tweez also exploits rapid 50 kHz quantification of bead positions using back focal plane (bfp)
112 detection of the NIR beam via a high-bandwidth quadrant photodiode (QPD) not limited by camera
113 shot noise[43] (online methods). In MT-only setups, camera-based detection is often used to track
114 beads with ~kHz sampling; our high-speed detection permits faster sampling to probe rapid
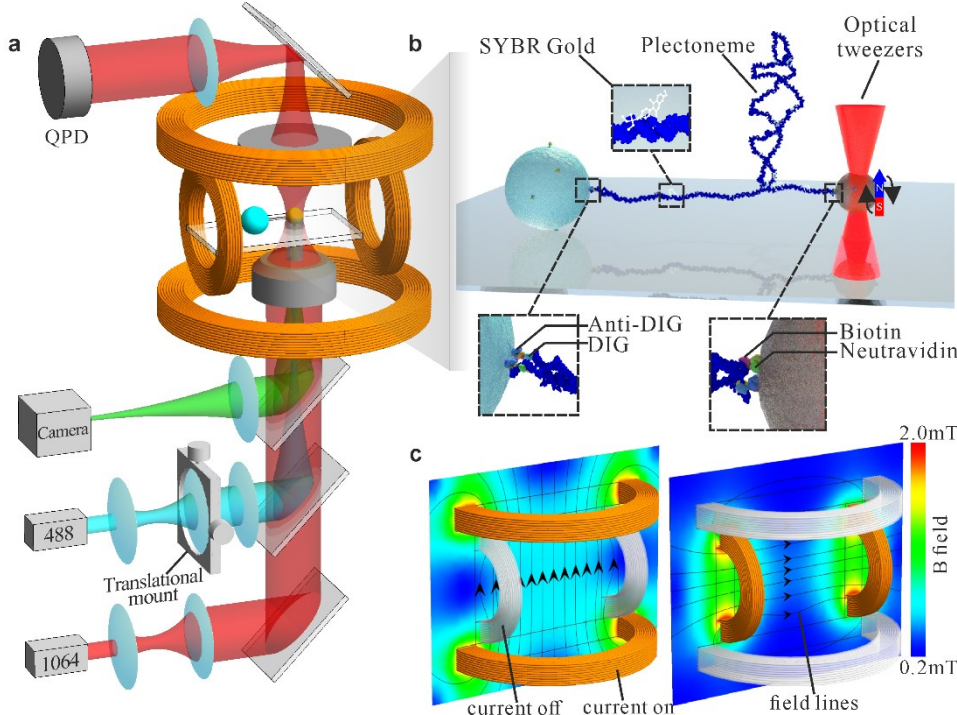115 structural dynamics.

Figure 1 Principle of COMBI-Tweez. (a) An NIR OT is colocated with MT generated from a pair of orthogonal Helmholtz coils enabling a single tethered DNA molecule to be visualised simultaneously in the focal plane using a variety of light microscopy modes, to observe DNA structural dynamics when the molecule is mechanically perturbed. (b) Cartoon of a plectoneme formed in COMBI-Tweez, using chemical conjugation to tether one end of a DNA molecule to a surface-immobilised "anchor" bead with the other tethered to an optically trapped magnetic microbead. SYBR Gold fluorophores[38] label the DNA via intercalation between adjacent base pairs. (c) Simulation of B field when vertical and horizontal coil pairs are separately activated, indicating a highly uniform field in the region of a trapped bead. Generalised magnetic field vectors can be generated by combining outputs from each coil; it is simple to generate stable B field rotation in a plane perpendicular to the microscope focal plane resulting in rotation of the trapped bead that enables torque to be controllably applied to a tethered DNA molecule.

Stretching/twisting label-free DNA

129   We first assessed COMBI-Tweez to perform torsionally unconstrained stretch-release (MT module
130   off) using a 15.6 kbp test double-stranded DNA (dsDNA) construct in the absence of fluorescent tags
131   (online methods, Supplementary Fig. 9), generated as a fragment from λ DNA digestion and
132   functionalised with concatemer repeats of biotin or digoxigenin "handles" on either end, since the
133   results can be directly compared with several previous OT/MT molecular studies on similar
134   constructs. Our handles were 500 bp leaving a 14.6 kbp central region. We surface-immobilised
135   5 μm "anchor" beads with non-specific electrostatic adsorption by flowing diluted anti-digoxigenin
136   (DIG) beads into a flow cell before BSA passivation then introducing DNA in ligase buffer. Following
137   incubation and washing we introduced 3 μm Neutravidin-functionalised magnetic beads, sealed the
138   flow cell and imaged immediately. To form tethers, we hold an optically-trapped magnetic bead 500
139   nm from an anchor bead to allow a tether to form through *in situ* incubation. Each tether's
140   mechanical properties could then be studied via stretch-release through nanostage displacement at
141   a ~1 Hz frequency and ~5 μm amplitude (online methods and Supplementary Movie 2).

142   Since it is well established that strong B fields induce above physiological temperature increases in
143   magnetic nanoparticles and also that previous attempts using optically trapped magnetic beads
144   were limited by temperature increases due NIR laser absorption by magnetite[44] (and personal
145   communication Nynke Dekker, University of Delft), we characterized trapped bead temperature
146   extensively. Performing transmission electron microscopy (TEM) on dehydrated resin-embedded
147   70 nm thick sections of the magnetic beads (online methods) indicated electron opaque
148   nanoparticles distributed in a ~100 nm thin surface just inside the outer functionalisation layer
149   (Fig. 2a,b) while electron diffraction was consistent with an iron (II/III) oxide magnetite mixture as
150   expected (Fig. 2c). We estimated temperature increase near trapped beads by measuring the
151   distance dependence on melting alkane waxes (online methods). By positioning a trapped bead
152   adjacent to a surface-immobilised wax particle, we observed the melting interface using brightfield
153   microscopy (Fig. 2d-f), enabling distance measurement to the bead surface (Fig. 2g). Modelling heat
154   generation analytically suggested ~1/x dependence for small x (distance from the bead surface) less
155   than the bead radius (Supplementary Note 2). We used the data corresponding to small x to show
156   that increasing the distance of the magnetite from the bead centre significantly reduces the bead
157   surface temperature (Supplementary Fig. 10), resulting in 45˚C in our case (Supplementary Note 3).
158   Finite element modelling of heat transfer outside the bead confirmed deviation of 1/x for larger x
159   (Fig. 2h), fitting all wax data points within experimental error, indicating a range of 45-30˚C for
160   distances from the bead surface from zero through to the ~5 μm DNA contour length. The mean
161   ~37-38˚C over this range is serendipitously perfectly aligned for physiological studies. This
162   acceptable temperature increase limits our trapping force to approximately 10 pN, well within the
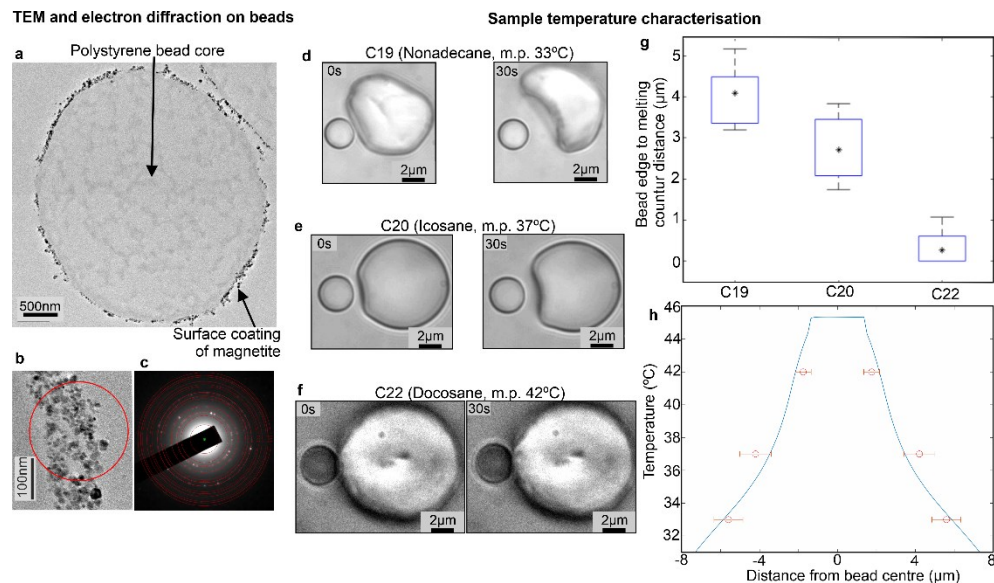163   physiological range we want to explore for DNA.

Figure 2 Absorption of NIR laser by magnetite results in physiological temperatures surrounding trapped beads. a) TEM of 70 nm thick section of resin-embedded dehydrated magnetic bead (JEOL 2100+ TEM 200 kV). b) Zoom-in on the bead surface showing red circled electron-dense nanoparticles produce a c) selected area diffraction pattern consistent with iron (II,III) oxide. d)-f) Brightfield of trapped magnetic bead positioned adjacent to solid ~10 μm surface immobilised alkane wax particle, shown for waxes C19, C20 and C22, indicating formation of melting interface at 30 s timepoint. C22 often either did not visibly melt or had interface less than a radius from bead edge. g) Boxplot indicating mean (*) distance from bead edge to melting interface for the three waxes (blue box interquartile range). h) Finite element model (blue, Supplementary Note 3) for heat transfer predicts that the temperature stays constant inside the bead at ~45°C and decreases with distance away from the bead (experimental datapoints overlaid in red, s.d. errorbars). The temperature dependence beyond bead surface becomes shallower than the ~$1/x$ predicted from analytical modelling (Supplementary Note 2) due to heat transfer into the glass coverslip from the surrounding water.

The estimated DNA persistence length determined from wormlike chain (WLC)[45] fits to force-extension data (online methods) was comparable to previous studies[46] with mean of approximately 50 nm (Fig. 3a) with no significant difference between stretch and release half cycles indicating minimal hysteresis due to stress-relaxation[47] (Extended Data Fig. 1). Mean contour length was approximately 5 μm (Fig. 2a), comparable to sequence expectations. We configured OT stiffness to be low (10 pN/μm) compared to earlier DNA studies that probed overstretch, allowing instead stable trapping up to a few pN relevant to physiological processes while avoiding detrimental heating.

We tested COMBI-Tweez to twist torsionally constrained DNA, first keeping the OT stationary as a trapped bead was continuously rotated at 1 Hz. We found that force increased as DNA is wound, until high enough to pull the bead from the trap, towards the anchor bead at which point meaningful measurement ends (Supplementary Movie 3). As reported by others, we observed that DNA force does not increase linearly with torsional stress but undergoes buckling[37] at which DNA no longer absorbs torsional stress without forming secondary structures which shorten its end-to-end length (Fig. 3b). Utilising the 50 kHz QPD sampling, we monitored rapid fluctuations in conformations between individual rotation cycles which would not be detectable by the slower video rate sampling (Fig. 3b inset). For the example shown, there is an initial 1.7 pN force at 4.5 μm extension (bead image inset, 36 s). Force increased non-linearly during rotation with corresponding decrease in extension to 4.3 μm (inset, 72 s) prior to buckling at 2.2 pN and exiting the trap (75 s). Modelling twist for an isotropic rod suggests torque τ per complete DNA twist is approximately C/L where C is the torsional modulus and L the DNA length. Using C = 410 pN.nm obtained previously on DNA using MT single-molecule twist experiments[2] indicated torque of 0.08 pN.nm per bead rotation.

We next sought to reproduce "hat curves" which map relations between DNA extension versus twist when positively and negatively supercoiled (online methods). At forces less than a critical value F_c of 0.6-0.7 pN [48], DNA supercoiling was approximately symmetric around σ = 0 [49]. At higher forces,

201 negative supercoiling no longer leads to plectonemes but instead to melting bubbles[48]. We selected
202 forces either side of F_c, fixed in real time using bead position feedback to the nanostage. As
203 anticipated, high-force hat curves (Fig. 3c left panel, 1.1 pN) indicate asymmetry with a high
204 extension plateau from σ = 0 to σ < 0 (blue trace) and σ > 0 to σ = 0 (green trace), with decreasing
205 extension as DNA is overtwisted (red). At lower force (Fig. 3c right panel and Fig. 3d, 0.5 pN)
206 negative supercoiling, indicated by green and red traces, comprised 200 rotations for each trace
207 equivalent to maximum negative torque of -1.6 pN.nM, was broadly symmetrical with the positive
208 supercoiling pathway, indicated by blue and yellow traces, which comprised 200 rotations per trace
209 equivalent to maximum positive torque of +1.6 pN.nM. Lateral (15 nm/s) and axial (7 nm/s) drift was
210 effectively negligible for individual rotation cycles by allowing COMBI-Tweez to reach a stable
211 temperature following coil activation, however, over longer duration hat curve experiments
212 comprising several hundred seconds we performed drift correction on bead positions (online
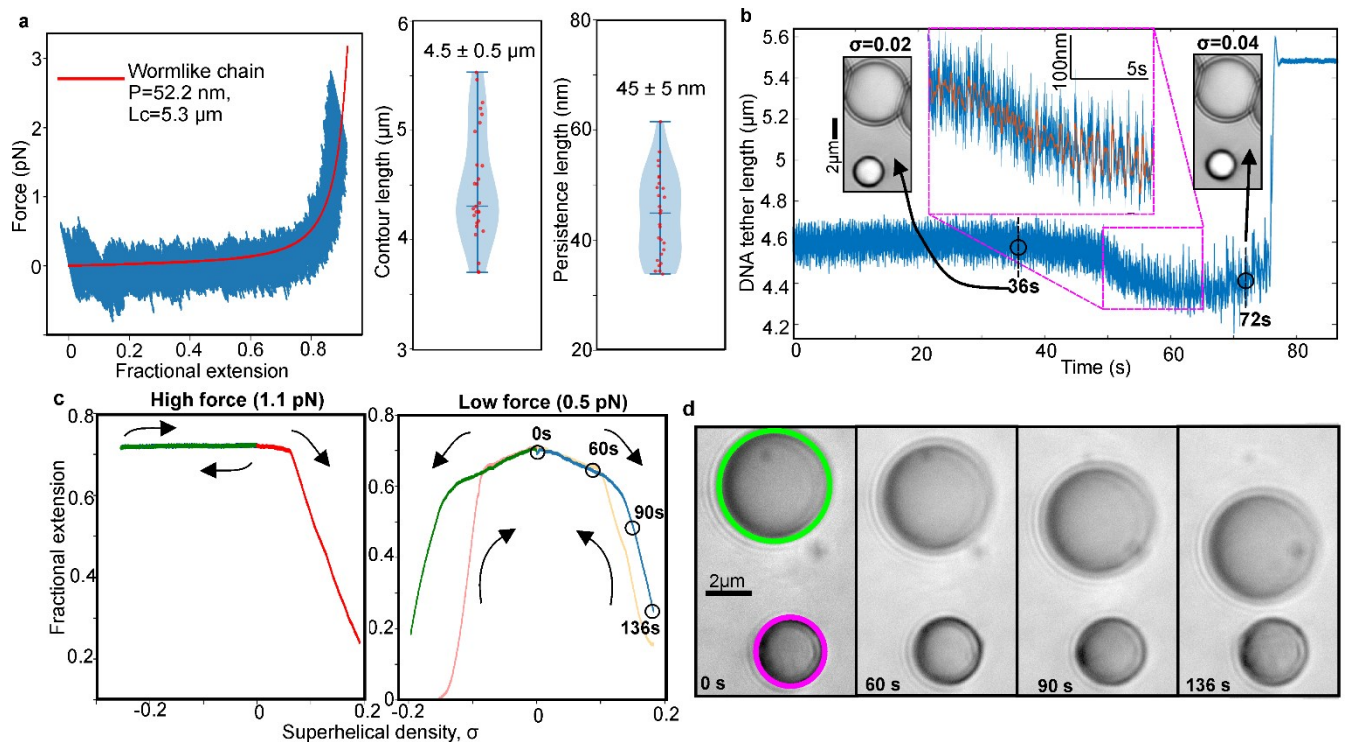213 methods).

214

215
216 **Figure 3 COMBI-Tweez in brightfield quantifies key features of supercoiling**. a) Left: (Blue) representative DNA force vs
217 fractional extension showing no obvious stress-relaxation[47], WLC fit indicated (red) Lc = 5.3 μm and persistence length P =
218 52 nm obtained as mean from n = 44 consecutive stretch-release half cycles, s.d. 13%, error on individual fits <0.002%
219 estimated from 1,000 bootstrapped fits from 1% of data per bootstrap. Right: violin plot of WLC fitted mean Lc and P for
220 n = 27 separate tethers. b) End-to-end extension measured from QPD tracking of trapped bead (blue) plotted as function of
221 time during continuous overtwist for fixed trap, initially 1.7 pN. Inset: brightfield of bead pair at σ values of 0.02 and 0.04
222 taken at 36 s and 72 s respectively before magnetic bead is lost from trap at 75 s. Zoom-in of extension measured using
223 QPD 50 kHz sampling (blue) plus indicative running median overlaid (red, 5,000-point window), showing same trend in
224 decreasing extension as video analysis but revealing additional conformational heterogeneity between individual rotation
225 cycles. c) Left: Hat curve for force clamp experiment, 1.1 pN (green "outward" trace is almost entirely overlaid onto blue
226 "inward" trace indicating negligible hysteresis); Right: hat curve, 0.5 pN. Both curves corrected for drift between different
227 sections taken at timepoints which span up to 25 min. Apparent hysteresis between blue/yellow sections at low force due
228 to 1-2 s response time of force clamp, while that between green/red sections is due both to this effect and bead pair
229 transiently adhering for a few seconds following formation of tether extension reduction upon negative supercoiling.
230 Arrows indicate path taken during the experiment (blue outward and yellow inward overtwist, followed by green outward
231 and red inward undertwist). d) Brightfield from low force clamp experiment of c) at indicated timepoints, with nanostage
232 moving anchor bead (green) relative to optically trapped bead (magenta) to maintain constant force (see also
233 Supplementary Movie 4).

234

DNA dynamics during stretch/twist visualized by correlative fluorescence imaging
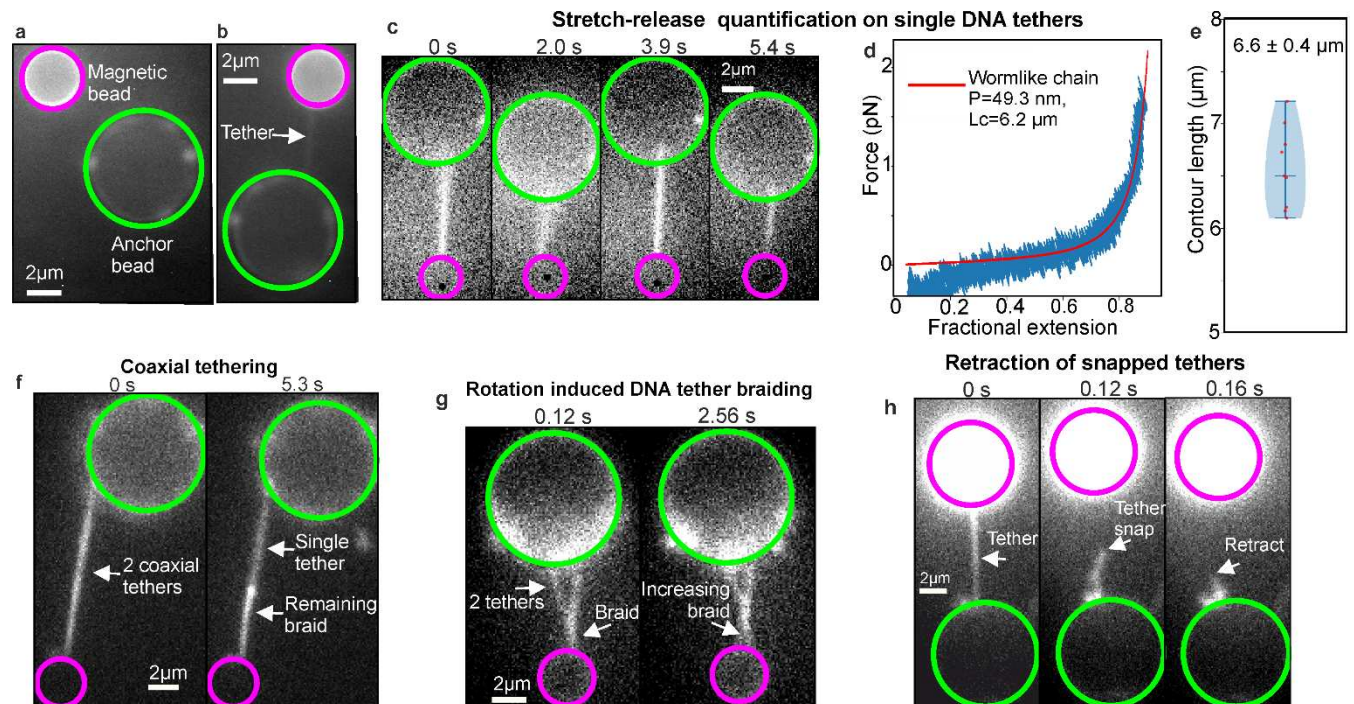
236

Figure 4 Correlative fluorescence imaging and torsional manipulation of DNA enables visualisation of tether dynamics. a) Optically trapped bead (magenta) next to surface-immobilised anchor bead (green). Multiple DNA molecules clearly visible on anchor bead as distinct foci since entropic compaction of untethered DNA results in ~500 nm end-to end length (also see Supplementary Fig. 11). b) Tether is formed between the two beads in a), indicated by white arrow. c) Image frames extracted from continuous stretch-release experiment performed in fluorescence. d) Representative force-extension data compiled from n = 8 consecutive stretch-release half cycles obtained from same tether by WLC fits (red). Mean persistence length determined from n = 9 separate tethers was 53 ± 15 nm (± s.e.), comparable with that obtained for unlabelled DNA construct while e) mean contour length larger by >30% consistent with reports of SYBR Gold interactions[38]. f) Two DNA molecules formed between anchor and trapped bead in which the tethers are coaxial. After one tether breaks (right), it retracts along the second leaving a bright still-braided region and a dimmer single-tether region. g) Two DNA molecules have formed a Y shape with "braided" section and two single tethers meeting anchor bead at different points. After rotation the braided section grows (see also Extended Data Fig. 2). h) Tether snapping and retracting to anchor bead, indicated by white arrow.

We tested the fluorescence capability using several illumination modes including widefield epifluorescence, Slimfield[50] (a narrowfield microscopy enabling millisecond imaging of single fluorescent molecules), and an oblique-angle variant of Slimfield that combines narrowfield with highly inclined and laminated optical sheet microscopy (HILO)[51], using 488 nm wavelength laser excitation (online methods). To visualize tether formation, we pre-incubated DNA-coated anchor beads with intercalating dye SYBR Gold[38] at one molecule per 1-2 μm² (Fig. 4a, online methods and Supplementary Movie 5), enabling inter-bead tethers to be visualized, using oxygen scavengers to mitigate photodamage (Fig. 4b). Low power widefield epifluorescence allowed single tethers to be observed at video rate for ~100 s before tether breakage due to photodamage (Fig. 4c). Repeating the same torsional unconstrained stretch-release protocol as for unlabelled DNA (Fig. 4d and Supplementary Movie 6) indicated a mean persistence length comparable to unlabelled of approximately 50 nm, whereas the contour length increased over 30% (Fig. 4e), consistent with earlier reports at comparable stoichiometry values of SYBR Gold:DNA[38] if at least half available SYBR Gold intercalation sites are occupied.

Experimenting with DNA concentration also demonstrated potential for studying interactions between multiple molecules, e.g. "braided" double tethers that can be controllably unwound by bead rotation to reform separated single tethers (Fig. 4f, Extended Data Fig. 2, online methods and

268 Supplementary Movie 7), including studying two fully braided coaxial DNA molecules (Fig. 4g and
269 Supplementary Movie 8) in some instances resulting in visible entropic retraction when one of these
270 snaps (Fig. 4h and Supplementary Movie 9). These unique features of COMBI-Tweez allowed high-
271 precision control of DNA-DNA interactions as a function of supercoiling.

272 **Time-resolved visualization of DNA structural motifs**

273 To explore the capability to study complex structural dynamics, we investigated DNA plectonemes,
274 higher-order structural motifs that emerge in response to torque[46]. Applying constant force to a
275 SYBR Gold labelled tether using the same protocol as for unlabelled DNA of 1-2 pN, above the critical
276 F_c of 0.6-0.7 pN [48], and rotation to control σ , resulted in a similar asymmetrical hat curve (online
277 methods) – in the example shown in Fig. 5a starting from σ = 0 and overtwisting (blue trace) to σ > 0
278 with associated drop in fractional extension, then undertwisting through to σ = 0 (yellow trace) then
279 to σ < 0 with characteristic plateau in fractional extension (green/red traces), high-frequency QPD
280 sampling enabling detection of rapid structural fluctuations over ~100 nm in this region (Fig. 5a
281 inset). We measured a small difference to σ at which extension begins to decrease during
282 continuous overtwisting; for SYBR Gold labelled DNA this occurred at σ close to zero, whereas for
283 unlabelled DNA this was between 0.05-0.1, likely caused by DNA mechanical changes due to SYBR
284 Gold intercalation[38].

285 To measure longer timescale structural dynamics, we redesigned data acquisition using stroboscopic
286 imaging to expose just 10 consecutive images in fluorescence between 50 continuous bead rotations
287 to minimise photodamage, allowing 1 min equilibration between 50 rotation segments – the
288 example of Fig. 5b obtained below F_c using this discontinuous imaging protocol showed the same
289 qualitative features of an approximately symmetrical hat curve at low force for unlabelled DNA, with
290 the caveat of negligible hysteresis following equilibration between rotation segments.

291 Using the stroboscopic illumination protocol, high forces for relaxed or negatively supercoiled DNA
292 caused no differences in terms of tether shortening from the fluorescence images and no evidence
293 of the formation of higher-order structures (Fig. 5c left and centre panels), though negatively
294 supercoiled DNA exhibited image blur in localized tether regions, absent from relaxed DNA, manifest
295 in a higher average full width at half maximum (FWHM) intensity line profile taken perpendicular to
296 the tether axis (Fig. 5d and online methods). Conversely, overtwist resulted in visible tether
297 shortening along with the appearance of a higher intensity fluorescent puncta along the tether itself
298 (Fig. 5c right panel and inset, indicated as a plectoneme, see also Supplementary Movie 10.
299 Significant overtwisting leads eventually to sufficient DNA shortening which pulls the magnetic bead
300 out of the optical trap, shown in a different tether in Supplementary Movie 11).

301 At low force, fluorescence images of positively supercoiled DNA indicated similar tether shortening
302 and formation of a fluorescent punctum (Fig. 5e and inset, σ = 0.11 and 0.14). Conversely, although
303 relaxed DNA showed no evidence of higher-order localized structures, negatively supercoiled DNA
304 indicated both tether shortening and the appearance of a fluorescent punctum (Fig. 5e and inset,
305 σ = -0.14), albeit dimmer than puncta observed for positively supercoiled DNA. Notably, we find that
306 tethers formed by undertwisting appeared at different locations from those created through positive
307 supercoiling.

308 Similar experiments on full length λ DNA (48.5 kbp) resulted in more than one plectoneme (online
309 methods), the example of Fig. 5f following positive bead rotations (Supplementary Movie 12) having
310 three puncta per tether. Using Gaussian fitting to track puncta to 20 nm precision and summing
311 background-corrected pixel intensities enabled estimation of bp content, indicating 2.6-3.1 kbp per
312 plectoneme whose rate of diffusion decreased with increasing bp content (Fig. 5g). In this example,
313 there was a step-like increase in DNA extension of ~400 nm at approximately 860 ms, consistent
314 with a single-strand nick. Following this, each plectoneme then disappeared in sequence between
315 approximately 900-1,000 ms (Fig. 5h) indicative of a torsional relaxation wave diffusing from the
316 nick[52].

317 Estimating the proportion of bp associated with puncta in the shorter 15 kbp construct for positively
318 supercoiled DNA indicated up to ~50% of bp for the brightest puncta (σ = 0.14) and ~40% for the
319 σ = 0.11 case are associated with plectonemes, while for negatively supercoiled DNA the brightest
320 puncta contained closer to ~10% of the number of bp in the total tether length, broadly comparable
321 with the range of bp per plectoneme in λ DNA. Puncta tracking indicated displacements of
322 approximately 100 nm per frame equivalent to an apparent 2D Brownian diffusion coefficient in the
323 focal plane of 310-1,900 nm^2/s (Table 1 and Fig. 6a). Note, that these 2D diffusion coefficient
324 estimates give indications of the local mobility of plectonemes in the lateral focal plane of a DNA
325 tether, though the physical processes of plectoneme mobility parallel (possible sliding movements)
326 and perpendicular (likely to be lateral tether fluctuations in addition to plectoneme mobility relative
327 to tether) to a tether are likely to be different, which we do not explore here. We found that puncta
328 for positively supercoiled DNA have higher mean diffusion coefficients than for negatively
329 supercoiled by a factor of ~6.

330 We next predicted plectoneme location using a model based on localized DNA curvature[53] and the
331 stress-induced destabilization (SIDD) during undertwist algorithm[54] to model the likelihood of
332 forming melting bubbles and plectonemes at each different bp position along the DNA (online
333 methods), using the same sequence of the 15 kbp construct and so presenting an excellent
334 opportunity for cross-validation between experiment and simulation. This analysis showed
335 agreement for bubble formation to the location of puncta observed during negative supercoiling at
336 low force off-centre at ~4.5 kbp (within 3.6% of our predictions, Fig. 6b). SIDD focuses on locating
337 denaturation bubbles and has limitations in assuming torsional stress is partitioned into twist,
338 therefore over-predicting bubble prevalence in systems in which plectonemes are present, and
339 failing to account for influences of DNA curvature on plectonemes, and by extension, bubble
340 formation. The presence of a predicted peak in the centre 7 kb region was likely an artifact of over-
341 prediction, borne out by the integrated area under the suite of ~6 peaks pooled around ~4.5 kbp
342 being over five times greater than the 7 kbp peak; it is likely this secondary bubble might have
343 effectively been "replaced" by the plectoneme. Considering the high energy cost associated with
344 initialisation of a run of strand separation of 10.84 kcal/mol[55], which is independent of bubble size,
345 the formation of a single bubble is favourable in this regime.

346 Conversely, plectonemes under the same conditions are predicted to form at the DIG-functionalised
347 end of the DNA, opposite to that observed experimentally (Fig. 6c), although the plectoneme
348 prediction algorithm was developed for exclusively positively supercoiled DNA and we are not aware
349 of studies using it for negative supercoiling. The analysis predicted that plectoneme formation
350 during positive supercoiling was most likely located at the midpoint of the DNA tether, consistent
351 with experimental observations of puncta (Fig. 6c).

352 Formation of a localized bubble is a precursor of dsDNA melting, leaving two regions of single-
353 stranded DNA (ssDNA) with high local flexibility which can form the tip of a plectoneme, a scenario
354 which is energetically and entropically favourable compared to forming a second bubble. We
355 therefore hypothesise that bubbles generated through low negative supercoiling act as subsequent
356 nucleation points for plectonemes as negative supercoiling increases. SYBR Gold is capable of
357 binding to ssDNA in addition to dsDNA, with the result that during the sampling time used
358 experimentally, rapidly fluctuating ssDNA conformations will result in localized image blur, which is
359 what we observed experimentally (Fig. 5d). However, fluorescence imaging of cy3b-SSB (online
360 methods), which indicated binding to ssDNA oligos, showed no binding at comparable levels in
361 tethers, which may mean that the typical bubble size is smaller than the probe ~50 nt footprint[56];
362 although SIDD modelling indicated bubble sizes of ~60 nt these are limited by not considering
363 plectoneme dependence, which may result in smaller effective bubble sizes. For positive

364 supercoiling, considering only the intrinsic curvature and sequence accurately predicted the
365 plectoneme location, as described previously.

366 To better understand bubble/plectoneme coupling, we performed MD simulations of DNA
367 fragments held at constant force with varying σ (Fig. 6d,e, online methods and Supplementary
368 Movies 13-16). We found that plectoneme formation was always accompanied by bubbles forming
369 at or near plectoneme tips, caused by significant bending in this region, while relaxed DNA showed
370 no evidence for bubble or plectoneme formation. However, the nature of these bubbles varied
371 between over- and undertwisted fragments. For overtwisted, bubbles remained relatively close to a
372 canonical conformation, with bases on opposite strands still pointing towards each other. For
373 undertwisted, the structural damage was catastrophic; base pairs were melted and bases face away
374 from the helical axis, leaving large ssDNA regions. In addition, bubbles in undertwisted DNA tended
375 to be longer (up to 12 bp) and more stable (lasting for up to 2,200 ns in our simulations, though
376 since simulations were performed in implicit solvent there is no direct mapping to experimental
377 timescales) than the ones formed in overtwisted DNA (maximum of 5 bp and 100 ns) resulting in a
378 significantly higher prevalence of bubbles for negatively supercoiled vs positively supercoiled DNA
379 (Fig. 6d and Extended Data Fig. 3). This agrees with previous experimental studies: while the
380 presence of defects has been widely reported in negatively supercoiled DNA, they have only been
381 detected recently in strongly positive supercoiling with σ > 0.06 [57]. We hypothesise that the differing
382 nature, size and frequency of these bubbles accounts for the relative mobilities of plectonemes we
383 observe; for the less disturbed positively supercoiled plectonemes, motions away from bubbles have
384 a lower energy barrier than for undertwisted plectonemes which would need to form a large highly
385 disrupted site during motion.

386

σ	$rmsd_\parallel$ (nm)	$rmsd_\perp$ (nm)	$rmsd_{tot}$ (nm)	D_{tot} (nm^{2}s^{-1})
0.14	108 ± 37	96 ± 58	144 ± 47	1,900 ± 1,200
0.11	76 ± 52	72 ± 50	105 ± 41	990 ± 770
-0.14	49 ± 35	37 ± 14	62 ± 28	310 ± 280

387 **Table 1 Plectoneme mobility is supercoiling-dependent.** 1-dimensional root mean square
388 displacements parallel ($rmsd_\parallel$) and perpendicular to tether ($rmsd_\perp$), and combined total 2-
389 dimensional rmds (rms_{tot}) and diffusion coefficient D for the puncta shown in Fig. 5e. The
390 perpendicular thermal motion of the same tether without applied supercoiling was found to be
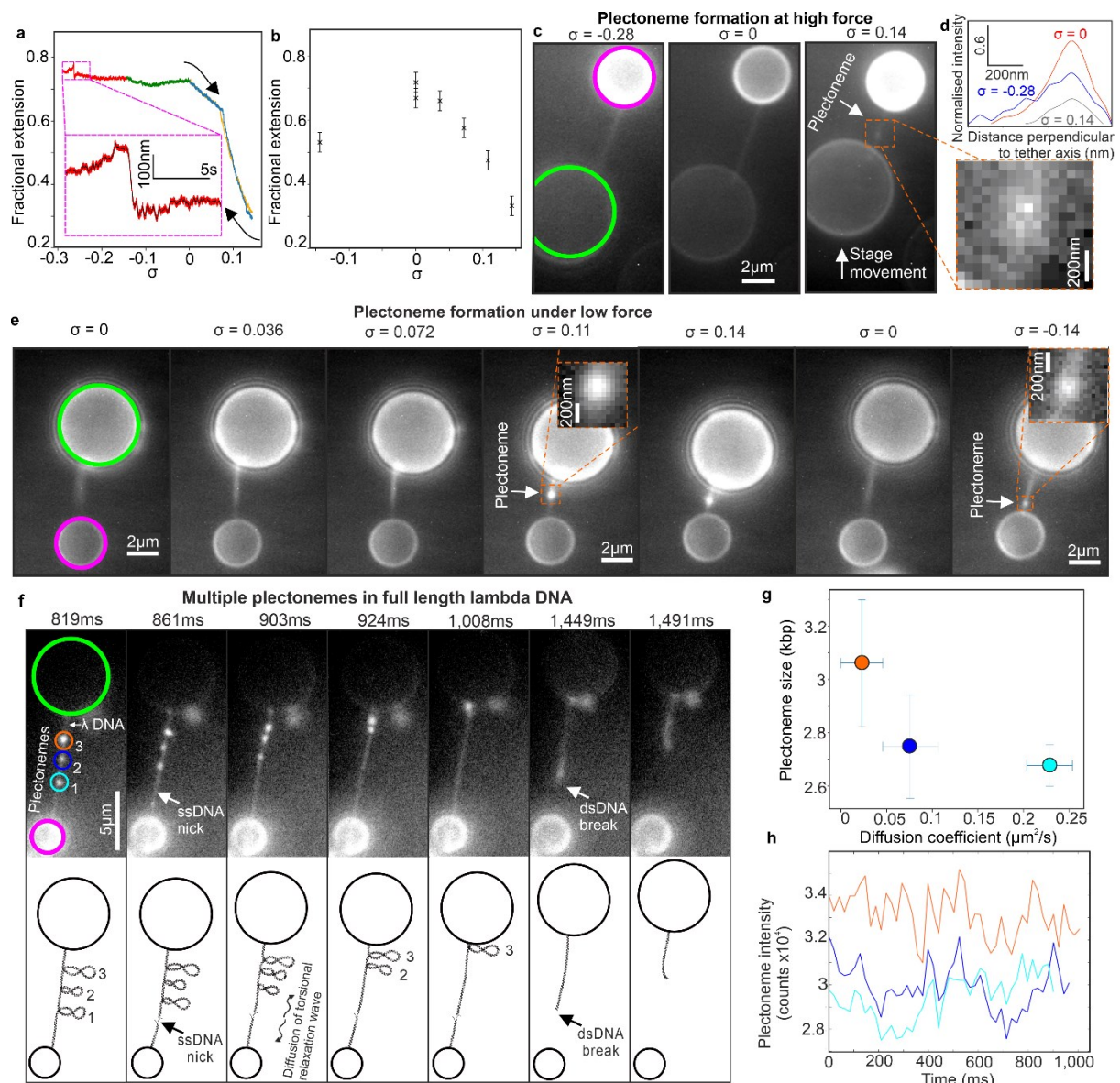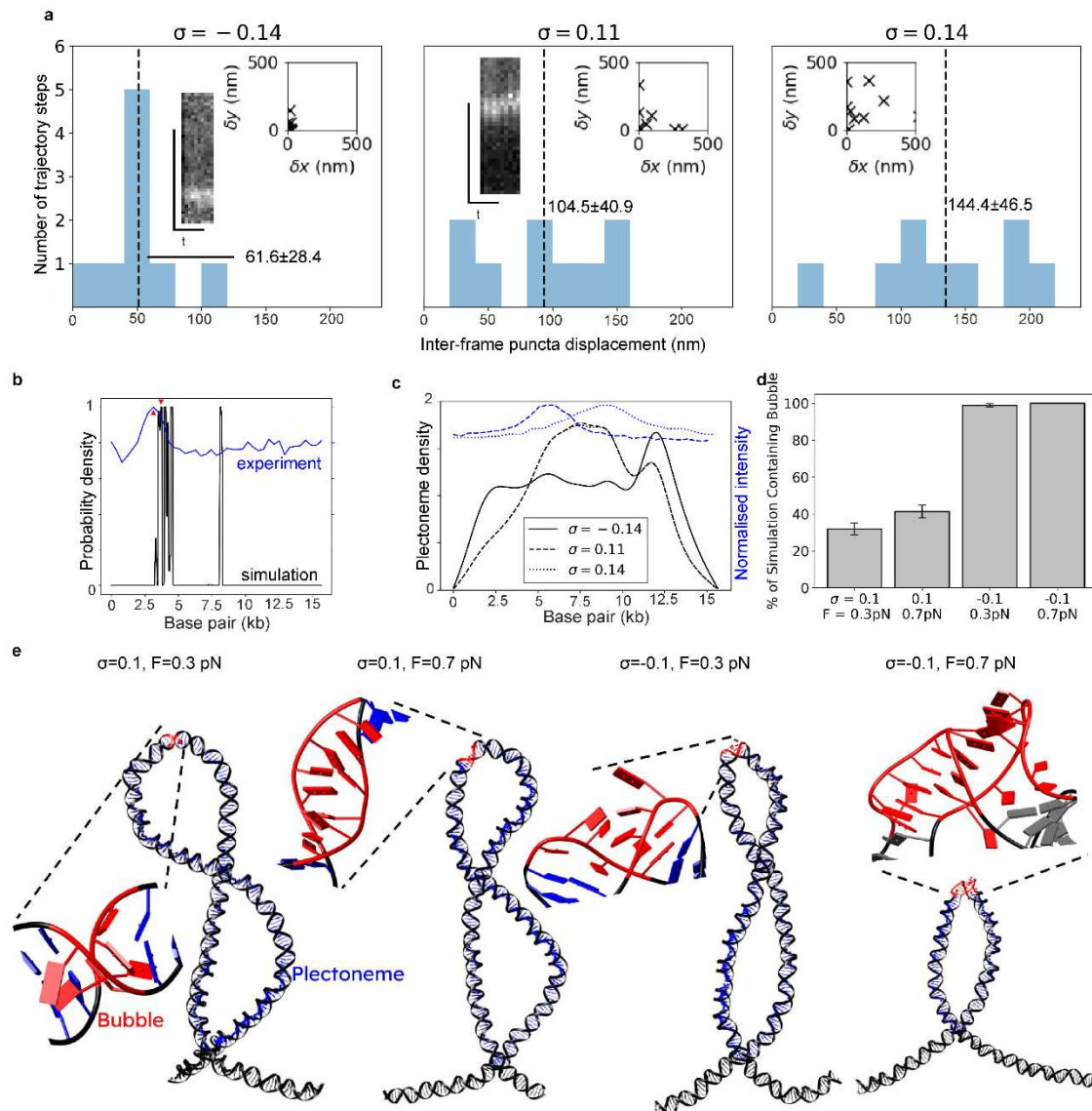391 66 ± 46 nm, s.d. errors.

392

393

394

Figure 5 Plectoneme dynamics in single molecules can be quantified at positive and negative supercoiling. a) Continuously acquired hat curve at 1.0 pN using QPD tracking of trapped bead showing asymmetric behaviour in presence of SYBR Gold dye labelling (arrows indicate direction of overtwist red-green-blue followed by undertwist yellow, paths corrected for experimental drift). Inset: 50 kHz QPD sampling of DNA extension (red) plus black indicative running median filter window 1,500 points showing steep but finite negative gradient. b) Low force (approximately 0.5 pN) discontinuous hat curve showing extension reduction during positive and negative supercoiling (distances measured with ImageJ and indicative error bars shown equivalent to width of a point spread function for the microscope). c) Fluorescence microscopy of high force (approximately 1 pN) plectoneme formation at σ = -0.28 (no plectoneme), 0 (no plectoneme) and 0.14 (inset plectoneme). d) Intensity line profiles for tethers of c) normalized to σ = 0 spanning blur region of σ = -0.28 tether using same size region for σ = 0 and σ = 0.14 tethers but excluding plectonemes, indicating FWHM widths of 251, 214 and 205 nm for σ = -0.28, 0 and 0.14 respectively (s.d. error ~0.2% estimated using bootstrapping, see online methods). e) Fluorescence microscopy of low force plectoneme formation, anchor and magnetic bead indicated with green and magenta circles respectively: when DNA is overtwisted a plectoneme forms and grows (inset, with altered display settings to match local background). Removing positive supercoiling allows DNA to relax, extend to its original length, and removes the plectoneme. After negative supercoiling is applied, extension decreases and a plectoneme is formed (inset). See also Supplementary Movie 6. f) In longer 48.5 kbp λDNA, in the example shown here extended to ~70% fractional extension (approximately 0.3 pN), more plectonemes form upon torsional manipulation, three indicated here (small circles); single-strand nick forms at ~860 ms (relative to the start of the fluorescence acquisition at 0 ms) resulting a torsional relaxation wave which diffuses along the tether to remove the positive supercoiling of the plectonemes which then disappear sequentially. g) The rate of plectoneme diffusion in this example decreases with increasing bp content. h) The integrated fluorescence intensity of plectonemes remain roughly stable before the nick (no net turnover of bp content), though with qualitative evidence of some anticorrelation between the cyan and blues traces whose plectonemes are separated by a few microns. g) and h) same colour code as circled plectonemes in f).

419

420

421 **Figure 6 Plectonemes are mobile but form at preferred locations.** a) Distribution of inter-frame displacements for puncta
422 mobility as assessed by 2D Gaussian tracking and calculating frame-to-frame displacement for tether with σ = -0.14, 0.11,
423 and 0.14 respectively. Inset: scatter plots of frame-to-frame displacement in parallel to (*y*) and perpendicular to (*x*) the
424 tether in nm, kymographs taken from a profile along the centre of the tether axis. b) Bubble forming probability density
425 function as predicted by Twist-DNA[58], σ = -0. Plotted in blue on same axes is the normalised, background-corrected
426 intensity of the plectoneme imaged from a single tether in fluorescence microscopy (Fig. 4c). Red triangles indicate the
427 closest agreement between experimental and predicted peaks (within 3.6%). c) Plectoneme formation probability as
428 predicted by the probabilistic model of Kim et al[53] with modified average plectoneme sizes. Solid line: -200 turns (σ = -
429 0.14), dashed line: +150 turns (σ = 0.11), dotted line: +200 turns (σ = 0.14). Dotted and dashed line overlap so they cannot
430 be distinguished in the plot. d) Percentage of each simulation over which bubbles are seen, with errors representing s.d.
431 Lack of error in σ=-0.1, F=0.7 pN case indicates presence of at least one bubble in every frame. e) Representative structures
432 of our simulations highlighting plectonemes in blue and denaturation bubbles in red.

433

Discussion

435 Three existing approaches of molecular manipulation correlated with fluorescence visualisation
436 enable DNA supercoiling to be studied: 1) utilising stochastic biotin-avidin unbinding[26] between an
437 optically trapped bead and DNA molecule, followed by transient torsional relaxation and religation
438 which introduces negative supercoils. Fluorescence microscopy is applied to visualize DNA. The
439 approach is valuable in not requiring engineering of precise magnetic tweezers as with COMBI-
440 Tweez, however, the introduction of supercoils is stochastic and limited to negative superhelical

441   density, whilst COMBI-Tweez enables more scope to explore positive and negative supercoiling
442   dependence on DNA topology with higher reproducibility; 2) permanent magnetic tweezers[22] in a
443   vertical geometry to twist a magnetic bead conjugated to the free end of surface-tethered dye-
444   labelled DNA to form plectonemes through positive supercoiling, followed by orthogonal rotation of
445   magnets to create an obliquely oriented tether which is almost but not entirely parallel to the
446   microscope focal plane due to imprecision with knowing the exact position of the surface relative to
447   the bead, but which can enable plectoneme dynamics visualisation via epifluorescence. This method
448   reports visualisation of mechanically induced plectonemes though not visualization of mechanically
449   controlled bubbles nor of mechanically induced plectonemes directly correlated in real time to the
450   mechanical driving torque; it does not require accurate engineering of coils nor optical tweezers,
451   however, there is no high-precision force measurement and control compared to COMBI-Tweez,
452   there are potential issues with surface interference and uncertainty in the angle between tether and
453   coverslip leading to imprecision concerning plectoneme mobility and, importantly, it does not enable
454   observation of plectoneme formation at the same time as twisting DNA, so it is not possible to study
455   early onset plectoneme dynamics but only several seconds following mechanical perturbations; 3)
456   intercalation of Sytox Orange dye[23] by surface-tethered DNA induces torsional stress which is
457   resolved by plectoneme formation through positive supercoils, but under certain concentration
458   regimes can also enable negative supercoils to be added. This approach is relatively easy to
459   configure, allows for simultaneous visualization of tethers and plectonemes, and can be performed
460   with higher throughput than COMBI-Tweez. However, a key advantage of COMBI-Tweez is that it can
461   control the state of DNA supercoiling directly, reversibly and consistently without relying on
462   stochastic intercalating dye binding/unbinding which, unavoidably, varies from tether to tether.
463   COMBI-Tweez is also able to precisely exert biologically relevant force regimes to DNA whilst
464   observing plectoneme formation and dynamics. The independent control of torque and force over a
465   physiological range with high-speed data acquisition coupled to high-precision laser interferometry
466   is also a unique capability which can enable biological insights in real time structural dynamics of
467   DNA and processes that affect its topology over a more rapid timescale than is possible with existing
468   approaches, such as DNA replication, repair and transcription. Also, COMBI-Tweez can monitor how
469   torsional dynamics affects plectonemes in real time, and can quantify torsional interactions between
470   two DNA molecules to high-precision, which has not to our knowledge been reported with these
471   earlier technologies. Being based around a standard inverted microscope, it is cost-effective to
472   implement offering access to interchangeable widefield and narrowfield illumination modes. These
473   modes can be multiplexed with trivial engineering adaptations to enable multicolour excitation or
474   combined with techniques such as polarization microscopy[25,59,60] to extract multidimensional data
475   concerning biopolymer molecular conformations.

476   Although a previous report indicated the single-molecule fluorescence imaging of plectonemes in
477   DNA using intercalators to change σ with both DNA ends attached to a coverslip[23], we report here to
478   our knowledge the first transverse single-molecule fluorescence images of mechanically controlled
479   supercoiling-induced higher-order DNA structural motifs including both plectonemes and bubbles. In
480   the same earlier report it was indicated that plectonemes had high mobility equivalent to a diffusion
481   coefficient of ~0.13 $\mu m^2 s^{-1}$, which contrasts our observation using COMBI-Tweez of a lower mobility
482   equivalent at its highest to ~0.002 $\mu m^2 s^{-1}$ for the shorter 15 kbp construct, but is comparable to that
483   observed for full length λ DNA. Aside from these length differences, there are also differences in
484   intercalating dye used, in that the previous study used Sytox Orange dyes, whereas we focus on
485   SYBR Gold. We speculate that the different observed diffusion response may also result from the
486   interplay between applied supercoiling, axial force on differently sized plectonemes. The
487   plectonemes reported previously were relatively small, equivalent to ~0.15-4 kbp, and were
488   generated by relatively small supercoiling changes of σ ~-0.025 at forces typically <0.5 pN.
489   Conversely, in our study we used a higher σ and forces closer to the physiological scale, resulting in
490   larger plectonemes which we find does affect their mobility, since it is known that DNA in general
491   responds to external mechanical stresses by preserving stretches of B-DNA while other regions are

492 highly distorted[19,59]. Also, as our previous MD simulations of the emergence of structural motifs in
493 DNA in response to stretch and twist indicates[31], we find that sequence differences make significant
494 impacts to DNA topological responses to mechanical stress and damage.

495 The model we applied involves the SIDD algorithm[54] which is limited in its ability to accurately
496 predict where bubbles form since 1) it assumes torsional stress is partitioned into twist, effectively
497 that the DNA is fully extended, therefore over-predicting bubble prevalence if plectonemes are
498 present; 2) it does not consider DNA curvature on plectoneme or bubble formation. With these
499 caveats, our calculations perform well in the context of single-molecule experiments and previous
500 modelling studies in which we saw excellent agreement to AFM data[34,61] for bending angles and radii
501 of gyration in addition to validation against bulk elastic properties of DNA demonstrated by the
502 SerraNA algorithm we reported previously[62].

503 The agreement between predictions of bubbles and plectonemes with the observed positions of
504 puncta for negatively supercoiled DNA raises several questions. Firstly, do bubbles nucleate
505 plectonemes? This would be entropically and energetically favourable compared to forming two
506 bubbles – one at the melting site and one at the plectoneme tip. Previous studies indicate a balance
507 between denatured and B-DNA that depends on torsional stress[19,63], and utilising a pre-existing
508 bubble to nucleate plectonemes drives this balance towards more B-DNA, that may be
509 physiologically valuable in maintaining overall structural integrity. Secondly, is the smaller bp
510 content measured for puncta during undertwisting compared to overtwisting a consequence of the
511 seeding of plectoneme nucleation by a bubble? Future studies using dyes sensitive to both ssDNA
512 and dsDNA such as Acridine Orange[64] may delineate the kinetics of bubble from plectoneme
513 formation, since if initial bubble formation takes a comparable time to form compared to
514 subsequent plectoneme nucleation this may explain the time-resolved differences observed in
515 plectoneme content between under- and overtwisted DNA. Thirdly, can a bubble act as a "staple",
516 providing an entropic and energetic barrier to plectoneme diffusion, holding it in place at the
517 plectoneme tip – as mismatched/unpaired regions have been shown to do in experiment[23] and
518 simulation[30]? If so, since predictions indicate sequence dependence on bubble formation, could
519 plectoneme formation serve a role to regulate DNA topology at "programmed" sites in the genome?
520 Given that in *E. coli* the genome is negatively supercoiled with a mean σ ~-0.05 could sequence
521 repeats with enhanced likelihoods for bubble formation serve as a hub for plectonemes that prevent
522 mechanical signal propagation along DNA, in effect defining genetic endpoints of "topological
523 domains" that have roles in protein binding and gene expression[57]?

524 To our knowledge, this is the first time that size, position, and mobility of higher-order structural
525 motifs in DNA under mechanical control have been *directly* measured in real time simultaneously
526 with the driving mechanical perturbation. The dependence of DNA shape and mechanics on its
527 interactions with its local environment represents a divergence from traditional views of DNA seen
528 through the lens of the Central Dogma of Molecular Biology; COMBI-Tweez has clear potential to
529 facilitate mechanistic studies of DNA topology dependence on the interactions with binding partners
530 such as enzymes, transcription factors and other nucleic acid strands. And, with trivial adaption, the
531 technology can be implemented to study other filamentous chiral biopolymers; RNA is an obvious
532 candidate, but also modular proteins such as silk show evidence for interesting torsional properties[65]
533 which have yet to be explored at the single-molecule level in regards to their response to twist. It
534 may also be valuable to use COMBI-Tweez to explore specific mechanistic questions relating to
535 emergent features of DNA topology, including the dependence on force and ionic strength on DNA
536 buckling, to further probe the source of very rapid fluctuations we observe in DNA supercoiling using
537 bfp detection, of putative long-range rapid plectoneme hopping mobility reported previously[22], as
538 well as investigating the role of DNA topology in crucial cell processes involving interaction with DNA
539 binding proteins, such as DNA repair mechanisms[66]. The collation of single-molecule tools in COMBI-
540 Tweez around a single optical microscope also presents valuable future opportunities to integrate
541 even more single-molecule biophysics tools, many of which are developed around optical
542 microscopy [67–69].

543

544

References

546

547   1.   Leake, M. C. The physics of life: one molecule at a time. *Philos Trans R Soc Lond B Biol Sci* **368**, 20120248 (2013).

549   2.   Bryant, Z. *et al.* Structural transitions and elasticity from torque measurements on DNA. *Nature* **424**, 338–341 (2003).

551   3.   Wuite, G. J. L., Smith, S. B., Young, M., Keller, D. & Bustamante, C. Single-molecule studies of the effect of template tension on T7 DNA polymerase activity. *Nature* **404**, 103–106 (2000).

553   4.   Wen, Y., He, M. Q., Yu, Y. L. & Wang, J. H. Biomolecule-mediated chiral nanostructures: a review of chiral mechanism and application. *Adv Colloid Interface Sci* **289**, (2021).

555   5.   J. M Wollman, A. *et al.* Tetrameric UvrD Helicase Is Located at the E. Coli Replisome due to Frequent Replication Blocks. *J Mol Biol* **436**, 168369 (2024).

557   6.   Smith, S. B., Finzi, L. & Bustamante, C. Direct mechanical measurements of the elasticity of single DNA molecules by using magnetic beads. *Science* **258**, 1122–6 (1992).

559   7.   Strick, T. R., Allemand, J. F., Bensimon, D. & Croquette, V. Behavior of supercoiled DNA. *Biophys J* **74**, 2016–2028 (1998).

561   8.   Smith, S. B., Cui, Y. & Bustamante, C. Overstretching B-DNA: The Elastic Response of Individual Double-Stranded and Single-Stranded DNA Molecules. *Science (1979)* **271**, 795–799 (1996).

564   9.   Heller, I., Hoekstra, T. P., King, G. A., Peterman, E. J. G. & Wuite, G. J. L. Optical tweezers analysis of DNA-protein complexes. *Chem Rev* **114**, 3087–3119 (2014).

566   10.   Baumann, C. G., Smith, S. B., Bloomfield, V. A. & Bustamante, C. Ionic effects on the elasticity of single DNA molecules. *Proc Natl Acad Sci U S A* **94**, 6185–6190 (1997).

568   11.   Brouwer, I. *et al.* Sliding sleeves of XRCC4-XLF bridge DNA and connect fragments of broken DNA. *Nature* **535**, 566–569 (2016).

570   12.   Whitley, K. D., Comstock, M. J. & Chemla, Y. R. High-Resolution 'Fleezers': Dual-Trap Optical Tweezers Combined with Single-Molecule Fluorescence Detection. *Methods Mol Biol* **1486**, 183–256 (2017).

573   13.   Meijering, A. E. C. *et al.* Imaging unlabeled proteins on DNA with super-resolution. *Nucleic Acids Res* **48**, (2020).

575   14.   Sheinin, M. Y., Forth, S., Marko, J. F. & Wang, M. D. Underwound DNA under tension: structure, elasticity, and sequence-dependent behaviors. *Phys Rev Lett* **107**, (2011).

577   15.   Lionnet, T., Joubaud, S., Lavery, R., Bensimon, D. & Croquette, V. Wringing out DNA. *Phys Rev Lett* **96**, (2006).

579   16.   Kriegel, F. *et al.* The temperature dependence of the helical twist of DNA. *Nucleic Acids Res* **46**, 7998–8009 (2018).

17. Kriegel, F. *et al.* Probing the salt dependence of the torsional stiffness of DNA by multiplexed magnetic torque tweezers. *Nucleic Acids Res* **45**, 5920–5929 (2017).

18. Lipfert, J., Kerssemakers, J. W. J., Jager, T. & Dekker, N. H. Magnetic torque tweezers: measuring torsional stiffness in DNA and RecA-DNA filaments. *Nat Methods* **7**, (2010).

19. Allemand, J. F., Bensimon, D., Lavery, R. & Croquette, V. Stretched and overwound DNA forms a Pauling-like structure with exposed bases. *Proc Natl Acad Sci U S A* **95**, 14152–14157 (1998).

20. Vlijm, R., Mashaghi, A., Bernard, S., Modesti, M. & Dekker, C. Experimental phase diagram of negatively supercoiled DNA measured by magnetic tweezers and fluorescence. *Nanoscale* **7**, 3205–3216 (2015).

21. Long, X., Parks, J. W., Bagshaw, C. R. & Stone, M. D. Mechanical unfolding of human telomere G-quadruplex DNA probed by integrated fluorescence and magnetic tweezers spectroscopy. *Nucleic Acids Res* **41**, 2746–2755 (2013).

22. van Loenhout, M. T. J., de Grunt, M. V & Dekker, C. Dynamics of DNA supercoils. *Science* **338**, 94–7 (2012).

23. Ganji, M., Kim, S. H., Van Der Torre, J., Abbondanzieri, E. & Dekker, C. Intercalation-Based Single-Molecule Fluorescence Assay To Study DNA Supercoil Dynamics. *Nano Lett* **16**, 4699–4707 (2016).

24. King, G. A. *et al.* Revealing the competition between peeled ssDNA, melting bubbles, and S-DNA during DNA overstretching using fluorescence microscopy. *Proc Natl Acad Sci U S A* **110**, 3859–3864 (2013).

25. Backer, A. S. *et al.* Single-molecule polarization microscopy of DNA intercalators sheds light on the structure of S-DNA. *Sci Adv* **5**, (2019).

26. King, G. A., Burla, F., Peterman, E. J. G. & Wuite, G. J. L. Supercoiling DNA optically. *Proc Natl Acad Sci U S A* **116**, 26534–26539 (2019).

27. Ouldridge, T. E., Louis, A. A. & Doye, J. P. K. Structural, mechanical, and thermodynamic properties of a coarse-grained DNA model. *J Chem Phys* **134**, (2011).

28. Wang, Q. & Pettitt, B. M. Modeling DNA thermodynamics under torsional stress. *Biophys J* **106**, 1182–1193 (2014).

29. Mosayebi, M., Louis, A. A., Doye, J. P. K. & Ouldridge, T. E. Force-Induced Rupture of a DNA Duplex: From Fundamentals to Force Sensors. *ACS Nano* **9**, 11993–12003 (2015).

30. Matek, C., Ouldridge, T. E., Doye, J. P. K. & Louis, A. A. Plectoneme tip bubbles: coupled denaturation and writhing in supercoiled DNA. *Sci Rep* **5**, (2015).

31. Shepherd, J. W., Greenall, R. J., Probert, M. I. J., Noy, A. & Leake, M. C. The emergence of sequence-dependent structural motifs in stretched, torsionally constrained DNA. *Nucleic Acids Res* **48**, 1748–1763 (2020).

32. Harris, S. A., Sands, Z. A. & Laughton, C. A. Molecular dynamics simulations of duplex stretching reveal the importance of entropy in determining the biomechanical properties of DNA. *Biophys J* **88**, 1684–1691 (2005).

33. Mitchell, J. S., Laughton, C. A. & Harris, S. A. Atomistic simulations reveal bubbles, kinks and wrinkles in supercoiled DNA. *Nucleic Acids Res* **39**, 3928–3938 (2011).

34. Pyne, A. L. B. *et al.* Base-pair resolution analysis of the effect of supercoiling on DNA flexibility and major groove recognition by triplex-forming oligonucleotides. *Nat Commun* **12**, (2021).

35. Schakenraad, K. *et al.* Hyperstretching DNA. *Nat Commun* **8**, (2017).

36. Friese, M. E. J., Nieminen, T. A., Heckenberg, N. R. & Rubinsztein-Dunlop, H. Optical alignment and spinning of laser-trapped microscopic particles. *Nature 1998 394:6691* **394**, 348–350 (1998).

37. Forth, S. *et al.* Abrupt buckling transition observed during the plectoneme formation of individual DNA molecules. *Phys Rev Lett* **100**, (2008).

38. Kolbeck, P. J. *et al.* Molecular structure, DNA binding mode, photophysical properties and recommendations for use of SYBR Gold. *Nucleic Acids Res* **49**, 5143–5158 (2021).

39. Simpson, N. B., Allen, L. & Padgett, M. J. Optical tweezers and optical spanners with Laguerre–Gaussian modes. *J Mod Opt* **43**, 2485–2491 (1996).

40. Bustamante, C. J., Chemla, Y. R., Liu, S. & Wang, M. D. Optical tweezers in single-molecule biophysics. *Nature reviews. Methods primers* **1**, (2021).

41. Miller, H., Zhou, Z., Shepherd, J., Wollman, A. J. M. M. & Leake, M. C. Single-molecule techniques in biophysics: a review of the progress in methods and applications. *Reports on Progress in Physics* **81**, 024601 (2017).

42. Gao, X., Hong, Y., Ye, F., Inman, J. T. & Wang, M. D. Torsional Stiffness of Extended and Plectonemic DNA. *Phys Rev Lett* **127**, (2021).

43. Gittes, F. & Schmidt, C. F. Interference model for back-focal-plane displacement detection in optical tweezers. *Opt Lett* **23**, 7 (1998).

44. Fatima, H., Charinpanitkul, T. & Kim, K. S. Fundamentals to Apply Magnetic Nanoparticles for Hyperthermia Therapy. *Nanomaterials* **11**, (2021).

45. Marko, J. F. & Siggia, E. D. Stretching DNA. *Macromolecules* **28**, 8759–8770 (1995).

46. Kriegel, F., Ermann, N. & Lipfert, J. Probing the mechanical properties, conformational changes, and interactions of nucleic acids with magnetic tweezers. *J Struct Biol* **197**, 26–36 (2017).

47. Linke, W. A. A. & Leake, M. C. C. Multiple sources of passive stress relaxation in muscle fibres. *Phys Med Biol* **49**, 3613–27 (2004).

48. Meng, H., Bosman, J., Van Der Heijden, T. & Van Noort, J. Coexistence of twisted, plectonemic, and melted DNA in small topological domains. *Biophys J* **106**, 1174–1181 (2014).

49. Strick, T. R., Allemand, J.-F., Bensimon, D., Bensimon, A. & Croquette, V. The Elasticity of a Single Supercoiled DNA Molecule. *Science (1979)* **271**, 1835–1837 (1996).

50. Plank, M., Wadhams, G. H. & Leake, M. C. Millisecond timescale slimfield imaging and automated quantification of single fluorescent protein molecules for use in probing complex biological processes. *Integrative Biology* **1**, 602–612 (2009).

658   51.   Tokunaga, M., Imamoto, N. & Sakata-Sogawa, K. Highly inclined thin illumination enables
659   clear single-molecule imaging in cells. *Nat Methods* **5**, 159–161 (2008).

660   52.   Gutiérrez Fosado, Y. A., Landuzzi, F. & Sakaue, T. Twist dynamics and buckling instability of
661   ring DNA: the effect of groove asymmetry and anisotropic bending. *Soft Matter* **17**, 1530–
662   1537 (2021).

663   53.   Kim, S. H. *et al.* DNA sequence encodes the position of DNA supercoils. *Elife* **7**, (2018).

664   54.   Benham, C. J. & Bi, C. The analysis of stress-induced duplex destabilization in long genomic
665   DNA sequences. *J Comput Biol* **11**, 519–543 (2004).

666   55.   Benham, C. J. Energetics of the strand separation transition in superhelical DNA. *J Mol Biol*
667   **225**, 835–847 (1992).

668   56.   Bell, J. C., Liu, B. & Kowalczykowski, S. C. Imaging and energetics of single SSB-ssDNA
669   molecules reveal intramolecular condensation and insight into RecOR function. *Elife* **4**,
670   (2015).

671   57.   Fogg, J. M., Judge, A. K., Stricker, E., Chan, H. L. & Zechiedrich, L. Supercoiling and looping
672   promote DNA base accessibility and coordination among distant sites. *Nat Commun* **12**,
673   (2021).

674   58.   Jost, D. Twist-DNA: computing base-pair and bubble opening probabilities in genomic
675   superhelical DNA. *Bioinformatics* **29**, 2479–2481 (2013).

676   59.   Backer, A. S. *et al.* Elucidating the Role of Topological Constraint on the Structure of
677   Overstretched DNA Using Fluorescence Polarization Microscopy. *J Phys Chem B* **125**, 8351–
678   8361 (2021).

679   60.   Shepherd, J. W., Payne-Dwyer, A. L., Lee, J. E., Syeda, A. & Leake, M. C. Combining single-
680   molecule super-resolved localization microscopy with fluorescence polarization imaging to
681   study cellular processes. *Journal of Physics: Photonics* **3**, 034010 (2021).

682   61.   Yoshua, S. B. *et al.* Integration host factor bends and bridges DNA in a multiplicity of binding
683   modes with varying specificity. *Nucleic Acids Res* **49**, 8684–8698 (2021).

684   62.   Velasco-Berrelleza, V. *et al.* SerraNA: a program to determine nucleic acids elasticity from
685   simulation data. *Phys Chem Chem Phys* **22**, 19254–19266 (2020).

686   63.   Randall, G. L., Zechiedrich, L. & Pettitt, B. M. In the absence of writhe, DNA relieves torsional
687   stress with localized, sequence-dependent structural failure to preserve B-form. *Nucleic Acids*
688   *Res* **37**, 5568–5577 (2009).

689   64.   Miller, H. *et al.* Biophysical characterisation of DNA origami nanostructures reveals
690   inaccessibility to intercalation binding sites. *Nanotechnology* **31**, (2020).

691   65.   Emile, O., Le Floch, A. & Vollrath, F. Biopolymers: shape memory in spider draglines. *Nature*
692   **440**, 621 (2006).

693   66.   J. M Wollman, A. *et al.* Tetrameric UvrD Helicase Is Located at the E. Coli Replisome due to
694   Frequent Replication Blocks. *J Mol Biol* **436**, 168369 (2024).

695   67.   Shashkova, S. & Leake, M. C. Single-molecule fluorescence microscopy review: shedding new
696   light on old problems. *Biosci Rep* **37**, (2017).

68. Leake, M. C. C. Analytical tools for single-molecule fluorescence imaging in cellulo. *Phys Chem Chem Phys* **16**, 12635–47 (2014).

69. Harriman, O. L. J. & Leake, M. C. Single molecule experimentation in biological physics: exploring the living component of soft condensed matter one molecule at a time. *J Phys Condens Matter* **23**, (2011).

70. Zhou, Z., Miller, H., Wollman, A. & Leake, M. Developing a New Biophysical Tool to Combine Magneto-Optical Tweezers with Super-Resolution Fluorescence Microscopy. *Photonics* **2**, 758–772 (2015).

71. Leake, M. C. *et al.* Stoichiometry and turnover in single, functioning membrane protein complexes. *Nature* **443**, 355–358 (2006).

72. Paul, T. & Myong, S. Protocol for generation and regeneration of PEG-passivated slides for single-molecule measurements. *STAR Protoc* **3**, 101152 (2022).

73. Shashkova, S. & Leake, M. C. Single-molecule fluorescence microscopy review: shedding new light on old problems. *Biosci Rep* **37**, (2017).

74. Leake, M. C., Wilson, D., Gautel, M. & Simmons, R. M. The elasticity of single titin molecules using a two-bead optical tweezers assay. *Biophys J* **87**, 1112–35 (2004).

75. Dillingham, M. S. *et al.* Fluorescent single-stranded DNA binding protein as a probe for sensitive, real-time assays of helicase activity. *Biophys J* **95**, 3330–3339 (2008).

76. Modesti, M. Fluorescent labeling of proteins. *Methods Mol Biol* **783**, 101–120 (2011).

77. Dresser, L. *et al.* Amyloid-β oligomerization monitored by single-molecule stepwise photobleaching. *Methods* **193**, 80–95 (2021).

78. Badrinarayanan, A., Reyes-Lamothe, R., Uphoff, S., Leake, M. C. & Sherratt, D. J. In vivo architecture and action of bacterial structural maintenance of chromosome proteins. *Science* **338**, 528–31 (2012).

79. Shepherd, J. W., Higgins, E. J., Wollman, A. J. M. & Leake, M. C. PySTACHIO: Python Single-molecule TrAcking stoiCHiometry Intensity and simulatiOn, a flexible, extensible, beginner-friendly and optimized program for analysis of single-molecule microscopy data. *Comput Struct Biotechnol J* **19**, 4049–4058 (2021).

80. Macke, T. J. & Case, D. A. Modeling Unusual Nucleic Acid Structures. *ACS Symposium Series* **682**, 379–393 (1998).

81. Watson, G. D., Chan, E. W., Leake, M. C. & Noy, A. Structural interplay between DNA-shape protein recognition and supercoiling: The case of IHF. *Comput Struct Biotechnol J* **20**, 5264–5274 (2022).

82. Roe, D. R. & Cheatham, T. E. PTRAJ and CPPTRAJ: Software for Processing and Analysis of Molecular Dynamics Trajectory Data. *J Chem Theory Comput* **9**, 3084–3095 (2013).

Correlating fluorescence microscopy, optical and magnetic tweezers to study single chiral biopolymers, tested on DNA plectoneme formation dynamics

Jack W Shepherd[1,2]*, Sebastien Guilbaud[1]*, Zhaokun Zhou[3]*, Jamieson Howard[1]*, Matthew Burman[1], Charley Schaefer[1], Adam Kerrigan[4], Clare Steele-King[5], Agnes Noy[1], and Mark C Leake[1,2, †]

[1] School of Physics, Engineering and Technology, University of York, York, YO10 5DD

[2] Department of Biology, University of York, York, YO10 5DD

[3] Guangdong Provincial Key Lab of Robotics and Intelligent System, Shenzhen Institute of Advanced Technology, Chinese Academy of Sciences, China

[4] The York-JEOL Nanocentre, University of York, York, YO10 5BR

[5] Bioscience Technology Facility, University of York, York, YO10 5DD

[†] For correspondence. Email mark.leake@york.ac.uk

* Authors contributed equally

ONLINE METHODS

Instrumentation

Optical tweezers (Supplementary Fig. 1) were built around an inverted microscope (Nikon Eclipse Ti-S, Nikon Instruments Inc.) with NIR trapping laser (opus 1064, Laser Quantum), to overfill objective aperture (100x, NA 1.45, oil immersion, MRD01095, Nikon Instruments Inc.). Oil immersion condenser (NA 1.4, Nikon Instruments Inc.) recollimated beam, back focal plane imaged onto a QPD[43] (QP50-6-18u-SD2, First Sensor) and digitized (NI 9222 and NI cDAQ-9174). For most fluorescence microscopy, a 488nm wavelength laser provided excitation, detection via a -80°C air-cooled EMCCD (Prime 95B, Photometrics, or iXon Ultra 897, Andor Technology Ltd, 55 and 69 nm/pixel respectively). Magnetic tweezers were generated using Helmholtz coils (Supplementary Fig. 2) on an aluminium platform. B field measurements indicated uniformity over several mm (maximum DC force 4.2×10^{-5} pN, Supplementary Note 1). SWG20 copper wires (05-0240, Rapid Electronics Ltd.) were wound onto 3D printed spools (Autodesk Inventor, Object30, material: VeroWhitePlus RGD835), 95 turns for two smaller spools, 100 turns for two larger spools[70]. LabVIEW signals were generated (NI 9263 and NI cDAQ-9174); two bipolar 4-quadrant linear operational amplifiers (BOP 20-5M, Kepco, Inc.) received voltages to convert to coil currents. COMBI-Tweez was optical table mounted (PTQ51504, Thorlabs Inc.) in aluminium walls/card lids, ±0.1 °C climate controlled with air conditioning (MFZ-KA50VA, Mitsubishi Electric). Custom LABVIEW software (Supplementary Fig. 3) enabled instrument control/data acquisition. Phased/modulated currents were sent to generate a 2D rotating B field; QPD (2 axes), current (2 coils), nanostage (3 axes) and camera fire signal were sampled at 50kHz.

Characterising tweezers. 40nm beads were incubated with 3μm magnetic beads to impart morphological asymmetry detectable on the QPD as a magnetic bead rotated. A 0.54A sinusoidal 1-8Hz current was sent to the larger coil pair, 1.5A to the smaller pair (Supplementary Fig. 5a). We evaluated phase shifts between coil input and bead rotation by taking QPD voltage correlated with its time-reversed signal to reduce noise for peak detection. Supplementary Fig. 5b plots phase shift as peak vs rotation frequency. Data were fitted using linear regression to yield gradient -0.429 rad Hz^{-1}, angular stiffness $k_\theta = 8\pi\eta R^3/|\text{gradient}| = 1.1 x 10^3 \text{pN} \cdot \text{nm} \cdot \text{rad}^{-1}$. To confirm no OT/MT interdependence we intermittently switched a rotating 1 Hz B field on/off for 10s intervals and monitored QPD signals in the absence of beads, confirming no 1Hz peak (Supplementary Fig. 5c). We could entirely remove any driving 1Hz signal from QPD responses of rotating trapped beads using narrow bandpass filtering, indicating no intrinsic influence of bead rotation on QPD signals.

781 We measured trapping force as displacement of a magnetic bead from the trap centre (estimated
782 from mean-filtered QPD signals[42], using prior 2D raster scanning of surface-immobilised beads as
783 calibration) multiplied by trap stiffness (determined from corner frequency of a Lorentzian fitted to
784 the trapped bead power spectrum), Supplementary Fig. 5.

785 **Force clamping.** A Proportional Integral Derivative (PID) feedback loop was enabled between QPD
786 and nanostage to keep tether force constant parallel to its axis (defined as *x*) by dynamically
787 repositioning the nanostage by the difference between set and measured force divided by trap
788 stiffness (10pN/μm), using PID optimisation to prevent overshooting/discontinuities. The clamp
789 response time was ~1s (Supplementary Fig. 6) with set force constant ±0.1pN throughout entire
790 over-/undertwisting experiments (Supplementary Fig. 7). Small forces detected parallel to *y*- and *z*-
791 axes due to angular constraints in trapped beads were minimised by manual nanostage adjustment.

792 **DNA preparation.** A ~15kbp DNA construct was synthesised by ligating functionalized handles,
793 containing biotin-16-dUTP or digoxigenin-11-dUTP (Roche, 1093070910/11277065910 respectively),
794 to a λ DNA fragment (Supplementary Fig. 8). Two PCR reactions were performed using primers
795 NgoMIV forward/NheI reverse, amplifying a 498bp region of plasmid pBS(KS+) generating a 515bp
796 handle. For biotinylation, the ratio of dTTP to biotin-16-dUTP was 1:1 generating ~120 handle
797 nucleotides. For digoxigenin-labelling, the ratio of dTTP to digoxigenin-11-dUTP was 6.5:1 generating
798 ~32 digoxigenin-11-dUTPs. PCR reactions were monitored by gel electrophoresis and handles
799 purified using a Qiaquick PCR kit before digestion with NgoMIV (biotinylation) or NheI-HF
800 (digoxigenin-labelling). The remaining tether comprises a 14.6kb fragment, purified using the
801 Monarch gel extraction kit from a 0.5% agarose TBE gel at 2V/cm for 36h. Handles were mixed with
802 cut λ in 5:1 λ:handle ratio (two compatible sticky ends for each handle), ligated using T4 DNA ligase
803 (NEB). 48.5kbp λ DNA was also created using a previously reported protocol[26], removing
804 phosphorylation steps using T4 polynucleotide kinase as already supplier-phosphorylated (IDT
805 N3011S).

806 **Bead functionalisation.** To suppress bead brightness in fluorescence (Supplementary Fig. 9), beads
807 were functionalised; 250μL of 50mg/mL solution of Micromer or Micromer-m (Micromod 01-02-
808 503/08-55-303 respectively), were incubated with 62.5μL of 5x MES (Alfa Aesar J61587), 2mg of EDC
809 Hydrochloride (Fluorochem 024810-25G), and 4mg *N*-Hydroxysuccinimide (Sigma 130672-5G) at
810 room temperature for 45min while vortexing. Beads were pelleted by centrifugation at 12,000xg and
811 resuspended in 200μL of 200μg/mL anti-digoxigenin (Merck Life Sciences 11333089001) or 200μL of
812 200μg/mL NeutrAvidin (Thermo Scientific 31000), then further incubated 3h. Beads were pelleted
813 and resuspended in 100μL PBS and 25mM glycine quench for 30min. Beads were
814 centrifuged/resuspended 3x in 500μL PBS before resuspending in 250μL PBS/ 0.02% azide,
815 generating anti-digoxigenin Micromer beads and NeutrAvidin Micromer-M beads, or the converse at
816 50mg/mL.

817 **Sample preparation/tethering.** A flow cell was prepared using truncated slides by scoring/snapping
818 a 50x26mm glass slide (631-0114, VWR), forming a double-sided tape plus 22x22mm coverslip
819 "tunnel" as described previously[71]. Flow cells were nominally passivated using polyethylene glycol
820 (PEG)[72] variants MeO-PEG-NHS and Biotin-PEG-NHS (Iris biotech PEG1165 and PEG1057
821 respectively). Anchor and trapping beads were commercially carboxylated then functionalized with
822 anti-digoxigenin or NeutrAvidin as above. 5μm anti-digoxigenin anchor beads were diluted to
823 5mg/mL in PBS/0.02% sodium azide and 2mM MgCl$_2$ and vortexed to disaggregate. 10μL was
824 introduced, inverted and incubated in a humidified chamber 15min room temperature for surface
825 immobilisation; for PEG passivated flow cells 5μm NeutrAvidin anchor beads were used. 20μL
826 2mg/mL BSA in PBS was introduced and incubated 5min. Nominally, 10μL DNA 0.12ng/μL in T4 DNA
827 ligase buffer and with 1μL T4 DNA ligase was introduced and incubated 1h, washed 200μL PBS, 20μL
828 imaging buffer introduced, and flow cell was sealed with nail varnish.

829 For stretch-release experiments we used ~1Hz nanostage triangular waves, amplitude ~5μm,
830 acquiring for ≥2 consecutive cycles. For fluorescence, the imaging buffer comprised PBS, 1mg/mL
831 3μm NeutrAvidin-functionalised Micromer-m beads, 6% glucose, 1mM Trolox, 833ng/mL glucose
832 oxidase, 166ng/mL catalase, 25nM SYBR Gold. For brightfield-only experiments, the imaging buffer
833 comprised 1mg/mL 3μm NeutrAvidin functionalised Micromer-m beads in PBS. Fluorescence
834 experiments used 40ms exposure time, maximum camera gain. Oblique-angle Slimfield[73]
835 $0.11kW/cm^2$ was the default mode, but we confirmed compatibility with epifluorescence, TIRF and
836 HILO. We first imaged DNA for a few seconds at 0.1mW to enable focusing but avoiding
837 photobleaching/photodamage, then imaged at 1mW. For continuous imaging, we acquired data for
838 200 rotations. For discontinuous imaging, we recorded 50 bead rotations using no fluorescence,
839 paused 1 min, then10 frames in fluorescence, acquiring ~10 supercoiling states per molecule.
840 Brightfield-only experiments were 40ms exposure time, zero camera gain, no camera cooling. σ was
841 calculated as number of bead rotations divided by number of turns in relaxed DNA (B-DNA twist per
842 base pair multiplied by number of bp in the DNA construct).

843 An anchor bead was selected and nearby free magnetic bead optically trapped. Beads were brought
844 within 500nm and incubated 2min to facilitate tether formation (optimised using fluorescence by
845 acquiring 10 frames to visualise DNA and reposition beads). Beads were separated ~5μm and
846 visualised with fluorescence if appropriate to test if a tether had formed (Supplementary Movies 2,
847 6). A force-extension curve was generated by oscillating the trapped bead and fitted by a wormlike
848 chain to generate persistence and contour lengths. Throughput, dependent on DNA concentration,
849 was nominally one in ~20 attempts (~5min) using 0.24ng/μL, analysis indicating binding fraction for
850 >1 tether was 5% [74]. Using 0.48ng/μL enabled controllable formation of two tethers between bead
851 pairs to explore the effects of braided DNA. Surface drift was quantified from brightfield video-
852 tracked intensity centroid displacements every 30s up to 1h of surface-immobilised beads in the
853 absence of tethering, indicating mean of ~15nm/s and ~7nm/s for lateral and axial drift respectively.
854 Trapping drift was assessed using QPD signals from a trapped untethered magnetic bead but aside
855 from expected rms fluctuations of a few tens of nm no directed drift was detected.

856 **Imaging SSB/hRPA.** Surface-immobilized 100nt ssDNA-cy5 and ssDNA binding proteins (cy3b-
857 SSB[75]and hRPA-eGFP[76]) were imaged on PEG passivated slides, incubated 5min at room temperature
858 with 200μg/mL Neutravidin (Thermofisher Scientific, 31000) in PBS followed by 200μL wash. 10μL
859 500pM ssDNA-cy5 in PBS was introduced and incubated 10min to allow binding of 5' biotin on
860 ssDNA-cy5 to Neutravidin on flow cell surface, excess ssDNA-cy5 washed 2x 100μL PBS. 100μL
861 100nM cy3b-SSB/hRPA-eGFP in PBS was introduced before the flow cell was sealed. A bespoke
862 single-molecule TIRF microscope with ~100nm penetration depth[77] imaged surface-immobilised
863 binding complexes, excitation was by an Obis LS 50 mW 488nm wavelength laser (hRPA-eGFP); Obis
864 LS 50mW 561nm wavelength laser (cy3b-SSB); Obis LX 50mW 640nm wavelength laser (ssDNA-cy5),
865 10mW at $14μW/μm^2$. Both probes showed colocalization when incubated with surface-immobilised
866 ssDNA-cy5 oligo. Since cy3b-SSB was more photostable and less impaired by steric hindrance than
867 hRPA-eGFP we focused on cy3b-SSB to probe DNA tethers. Due to PEG slide passivation, anchor
868 beads were functionalised with NeutrAvidin to bind to PEG-biotin coverslips, so Micomer-M beads
869 were functionalised with anti-digoxigenin. Tether preparation was as before with addition of 10nM
870 cy3b-SSB to the imaging buffer, and alternating 488nm/561nm wavelength laser excitation[78],
871 1mW/10mW respectively.

872 **Wormlike chain fitting.** Force-extension data were fitted by a wormlike chain (WLC) using Python3
873 and numpy's curve_fit to minimise least squares, error estimated from bootstrapping by taking 1%
874 of randomly selected data, WLC fitting, iterating 1,000 times, indicating ~0.2% s.d.

875 **Puncta analysis**. To assess percentage of tether bp in a plectoneme we used ImageJ to integrate
876 background-corrected pixel intensities associated with puncta normalised to the integrated
877 background-corrected intensity for the whole tether. To measure two-dimensional rms puncta

878 displacements, we used single-particle tracking software PySTACHIO[79] with mean square
879 displacement $<r^2> = 4D.\delta t$ where D is the two-dimensional diffusion coefficient, and δt the inter-
880 frame time interval 40ms, to 20nm localization precision.

881 **Plectoneme/bubble calculations**. Predictions for plectoneme loci were made using a model[53]
882 considering DNA curvature as determining factor, modified to increase the largest possible
883 plectoneme to deal with the ~15kbp construct and higher σ levels. Cutoff was increased from 1kbp,
884 as set in the original model, to 8.3kbp for σ=0.14 (or +200 DNA turns), to 6.7kbp for σ=0.11 (+150
885 DNA turns) and to 1.9kbp for σ=-0.14 (or -200 DNA turns); limits were differently established
886 according to experimental estimations of number of plectoneme bp. Predictions for bubble loci were
887 made using the Stress-Induced DNA Destabilization (SIDD) algorithm[54] implemented on the Twist-
888 DNA program to deal with long sequences at genomic scales[58]. Calculations were done at σ=-0.14,
889 0.1M salt, T=310K. For comparison of experimental fluorescence data to bubble predictions, the
890 plectoneme tether line profile was normalised and fitted with a cubic spline, regularised and plotted
891 on the central 14.6kbp.

892 **Control of tension and torsion *in silico***. DNA was modelled under restraints to control tension and
893 torsion mimicking experimental conditions (Fig. 5) using positional and 'NMR' restraints of AMBER[61].
894 One end of the duplex was fixed by restraining coordinates of O3' and O5' atoms of the final bp
895 ('fixed end'). The other ('mobile end') was kept at force 0.3 or 0.7pN by applying a linear distance
896 restraint to each strand, between O3' or O5' of the final bp and two fixed dummy atoms[62] used as
897 reference points (A and B, Supplementary Fig. 12). Angular restraints were applied for confining
898 'mobile end' motion to the tether axis (Supplementary Fig. 12, denoted *z*). To prevent *y* movement,
899 angles θ_1 and θ_2 were constrained. Another pair of reference points and restraints were
900 implemented to prevent *x* movement. Supercoiling was relaxed by passing DNA over either end of
901 the molecule. To prevent 'untying', we applied one angular restraint per phosphorus atom of the
902 bulk of the chain and per end (Supplementary Fig. 12b). Specifically, ψ angles (defined by a
903 phosphorus atom, the last mobile O3' or O5' on that strand and the corresponding reference point)
904 were forced >90°, creating an excluded volume resembling a bead. To ensure excluded volume
905 restraints were triggered as infrequently as possible, we added 60 GC bp to the 'mobile end' as a
906 buffering molecular stretch which were prevented from bending by dihedral restraints applied to
907 each complementary pair of phosphorus atoms (Supplementary Fig. 12c). DNA torsional stress was
908 maintained by ensuring O3' and O5' of the first relevant bp of the 'mobile end' (61st bp) were co-
909 planar with respective reference points A and B, achieved through a dihedral restraint that reduced
910 the angle between ABF and BAE planes to zero. The 'fixed end' was torsionally constrained using an
911 equivalent dihedral angle defined by O3' and O5' of the next-to-last bp and reference points I and J.

912 **DNA *in silico*.** The structure of a linear 300bp DNA molecule was built using Amber18[80] NAB module
913 from a randomly generated sequence with 49% AT surrounded by 2 GC bp at the 'fixed end' and 60
914 GC bp at the 'mobile end', 362bp total; 300bp sequence was:

915 [1]TGCAAGATTT [11]GCAACCAGGC [21]AGACTTAGCG [31]GTAGGTCCTA [41]GTGCAGCGGG [51]ACTTTTTTTC
916 [61]TATAGTCGTT [71]GAGAGGAGGA [81]GTCGTCAGAC [91]CAGATACCTT [101]TGATGTCCTG [111]ATTGGAAGGA
917 [121]CCGTTGGCCC [131]CCGACCCTTA [141]GACAGTGTAC [151]TCAGTTCTAT [161]AAACGAGCTA [171]TTAGATATGA
918 [181]GATCCGTAGA [191]TTGAAAAGGG [201]TGACGGAATT [211]CGCCCGGACG [221]CAAAAGACGG
919 [231]ACAGCTAGGT [241]ATCCTGAGCA [251]CGGTTGCGCG [261]TCCGAATCAA [271]GCTCCTCTTT [281]ACAGGCCCCG
920 [291]GTTTCTGTTG

921 To determine the default twist, we performed a σ=0 simulation. We used the 3DNA algorithm in
922 CPPTRAJ[64] as a reference to build under- and overtwisted straight DNA, σ=±0.1.

923 **MD.** Simulations were done in Amber18, performed using CUDA implementation of AMBER's
924 pmemd. DNA molecules were implicitly solvated using a generalised Born model, salt concentration
925 0.2M with GBneck2 corrections, mbondi3 Born radii set and no cutoff for better reproduction of

926 molecular surfaces, salt bridges and solvation forces. Langevin dynamics was employed using similar
927 temperature regulation as above with collision frequency 0.01 ps to reduce solvent viscosity[81]. The
928 BSC1 forcefield was used to represent the DNA molecule[70]. A single simulation was calculated for
929 each combination of force and σ (=±0.1, force F=0.3, 0.7pN), following our protocols for
930 minimisation and equilibration. In addition, we performed a control simulation at σ=0 . We
931 performed 40ns re-equilibration, applying the above restraints with exception of tensile force, for
932 allowing plectoneme formation; restraints on the canonical WC H-bonds were added to avoid
933 premature double helix disruption and allow distributions of twist and writhe to equilibrate.
934 Simulations were extended 500ns-2.3μs depending on convergence, measured by cumulative end-
935 to-end distance over time (Extended Data Fig. 3b), calculated using a single NVIDIA Tesla V100 GPU
936 from the local York Viking cluster at 40ns/day.

937 **Determination of bubbles *in silico*.** Melting bubbles were easily identifiable by visual inspection. To
938 quantify and ensure we only captured significant denaturation, we assumed a bubble was formed by
939 ≥3 consecutive bp that didn't present WC H-bonds, whose angular bp parameters (propeller twist,
940 opening and buckle) were ≥2 s.d. from the average obtained from relaxed DNA and that disruption
941 lasted for more than 1ns. This information was acquired using the nastruct routine of CPPTRAJ[82].
942 Percentages of simulations where DNA presented bubbles were calculated considering the last
943 400ns. Standard deviations were calculated using bootstrapping, sampling 1% of each simulation
944 200 times.

945 **Wax melting.** A 1% w/v suspension of each of three different alkane waxes was made, warmed in a
946 water bath 10°C hotter than the alkane melting point and sonicated 1min before plunge cooling in
947 an ice bath, injected into a flow cell and incubating 20min prior to 100μL PBS washing, introducing
948 50μg/mL magnetic beads, and sealing the flow cell. The experiment comprised selecting a surface-
949 immobilized wax particle, trapping a nearby magnetic bead and bringing it in contact with the wax,
950 then leaving it in position for 3min, recording brightfield timelapse movies.

951 **TEM/electron diffraction.** 3μm diameter magnetic beads at initial concentration 50mg/ml
952 were pelleted by centrifugation 1,000xg 1min, washed in 100% Ethanol by
953 resuspension/centrifugation, then infiltrated over 48h in LR White resin (Agar Scientific), and
954 subsequent polymerisation at 60°C for 48h. 70nm sections were cut (Leica Ultracut UCT7
955 ultramicrotome and Diatome diamond knife). TEM was carried out on a JEOL 2100+, 200 kV using a
956 150μm diameter condenser aperture, brightfield imaging achieved with a 120μm objective lens
957 aperture. Simulated electron diffraction was performed for Fe_3O_4 nanoparticles using a standard Al
958 diffraction sample for calibration at camera length $25cm^{-1}$ compared to Selected Area Electron
959 Diffraction (SAED) images taken from the edges of beads where nanoparticles were present. SAED
960 was also taken from within beads and showed no crystal structure.

961 **Data availability**

962 Data used are publicly available at DOI:10.5281/zenodo.7786636

963 **Code availability**

964 All code used for instrument design/control, data acquisition/processing/analysis and figure
965 generation directly relied on: Matlab, LabVIEW, Mathematica, Autodesk Inventor, Jupyter,
966 Matplotlib, NumPy, Pandas, SciPy. COMBI-Tweez source code available at https://github.com/york-
967 biophysics under Creative Commons Attribution-NonCommercial-ShareAlike 4.0 International
968 License (CC-BY-NC-SA; https://creativecommons.org/licenses/by-nc-sa/4.0/).

969 **Acknowledgements**

974   **Author contributions**

975   M.L. conceived the study. J.Z. developed tweezers/imaging instrumentation and control software,
976   which in the following years of development S.G., J.S. expanded. J.H. developed DNA chemistry. J.S.,
977   J.H., S.G. collected data which J.S. analysed. A.N. conceived theoretical molecular dynamics
978   simulations, M.B. performed them. C.S. developed an analytical temperature model. C.S-K, A.K.
979   performed TEM and electron diffraction. J.S., M.L wrote the bulk of the manuscript, with
980   contribution, discussion and revision from all of the authors. M.L. was the project administrator.

981   **Competing interests**

982   All authors declare that they have no competing interests.

983

984

985