

# Phenylketonuria: modelling cerebral amino acid and neurotransmitter metabolism

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## 1 ABSTRACT

### 2 Objective

3 Phenylketonuria (PKU) is caused by a deficiency of the hepatic enzyme phenylalanine  
4 hydroxylase, which primarily converts phenylalanine into tyrosine. Despite a phenylalanine-  
5 deprived diet, many adult PKU patients display deficits of executive functions. These are  
6 hypothesised to be caused by high cerebral phenylalanine and a shortage of monoaminergic  
7 neurotransmitters.

### 8 Method

9 To better understand the relationship between plasma and brain amino acid levels and  
10 monoaminergic neurotransmitter biochemistry, we constructed a computational model. The  
11 model comprises the transport of large neutral amino acids (LNAA) across the blood-brain  
12 barrier as well as cerebral amino acid and monoaminergic neurotransmitter metabolism and  
13 was validated by direct measurements of brain amino acid concentrations in PKU mice on  
14 various diets.

### 15 Results

16 The model predicts that brain amino acids are positively controlled by the concentrations of  
17 the corresponding amino acids in the blood, and to a lesser extent negatively by other amino  
18 acids competing for the transport systems. The model suggests that brain levels of

19 monoaminergic neurotransmitters are controlled more by phenylalanine, probably through  
20 non-competitive inhibition of the hydroxylases rather than by their precursor amino acids.  
21 Therefore, the model predicts that the decrease of neurotransmitters in PKU cannot be fully  
22 rescued by the addition of tyrosine and tryptophan alone, but also benefits from a reduction of  
23 the phenylalanine level. Thereby, the model substantiates the experimental data of the  
24 synergistic effect of both brain phenylalanine reduction and increased precursor amino acid  
25 availability to improve brain neurotransmitters in PKU mice.

26 Conclusion

27 We present the first complete model of the LNAA transport through the blood-brain barrier  
28 and subsequent brain neurotransmitter metabolism in PKU. The model leads to a better  
29 understanding of the pathophysiological mechanisms and the influence of individual amino  
30 acids in the diet on the underlying brain dysfunction in PKU. Moreover, it identifies gaps in  
31 our current knowledge about the LNAA transport across the blood-brain barrier. Furthermore,  
32 the model can be readily applied in studies of other neurological disorders in which the relation  
33 between diet, gene activities, brain amino acids, and neurotransmitters is important.

34 **KEY WORDS**

35 Phenylketonuria, phenylalanine, blood-brain-barrier, large neutral amino acids,  
36 neurotransmitters, model

37 **INTRODUCTION**

38 Phenylketonuria (PKU; OMIM 261600) is the classic example of an inborn error of amino acid  
39 metabolism. It is caused by a deficiency of the hepatic phenylalanine hydroxylase (PAH),  
40 which converts phenylalanine into tyrosine [1]. As the distinction between 'PKU',  
41 'classical PKU' and other forms of PAH deficiency is rather unclear, we here refer to PAH  
42 deficiency causing cerebral pathophysiology referred to as 'PKU'. If left untreated, high  
43 plasma phenylalanine rather than low tyrosine concentrations have been associated with PKU  
44 symptomatology. The latter is almost exclusively restricted to brain functioning, including  
45 severe intellectual disability, seizures, motor deficits, and psychiatric problems. Today,  
46 neonatal screening allows PKU diagnosis and initiation of treatment shortly after birth. The  
47 cornerstone of the treatment is to reduce phenylalanine concentrations in blood and brain by a  
48 severe phenylalanine-restricted diet. This diet consists of three parts: 1) a diet very low in  
49 natural protein; 2) a protein substitute, supplementing all amino acids except phenylalanine  
50 (and tyrosine-enriched) and other micronutrients that are normally present in high natural

51 protein containing food, and 3) low-protein food (that especially supplies patients with energy)  
52 [2].

53 Additionally, some patients respond to tetrahydrobiopterin supplementation.  
54 Tetrahydrobiopterin is a natural co-substrate of hepatic PAH, and of (cerebral) tyrosine and  
55 tryptophan hydroxylases. In addition, to being their redox co-substrate, it may act as a  
56 pharmaceutical chaperone of PAH, supporting its conformational stability and preventing  
57 degradation [3]. While the phenylalanine-restricted diet and tetrahydrobiopterin treatment can  
58 prevent severe intellectual disability [4], the clinical outcome remains suboptimal and warrants  
59 additional/alternative pathophysiology-based treatment strategies [1].

60 In PKU pathophysiology, the blood-brain barrier (BBB) is considered to play a central role  
61 [5,6]. Phenylalanine, as well as all other large neutral amino acids (LNAA), such as tyrosine  
62 and tryptophan, are exchanged across the BBB by the large neutral amino acid transporter 1  
63 (LAT1) [7]. This causes competition between the different LNAA for LAT1. Consequently,  
64 excessive plasma phenylalanine concentrations may not only lead to increased brain  
65 phenylalanine levels but also outcompete the transport of other LNAA across the BBB and  
66 thereby impair their brain availability [8–10]. While high brain phenylalanine levels are  
67 neurotoxic and affect brain metabolism [11–15], insufficient brain availability of non-  
68 phenylalanine LNAA has been related to impaired cerebral protein synthesis [10,16].  
69 Moreover, tyrosine and tryptophan are the precursors for the cerebral monoaminergic  
70 neurotransmitters dopamine, norepinephrine, and serotonin, respectively [17]. High cerebral  
71 phenylalanine content is known to inhibit (cerebral) tyrosine and tryptophan hydroxylases,  
72 which are the enzymes performing the rate-limiting steps in the synthesis of dopamine and  
73 serotonin [18–21]. Thus, a combination of high phenylalanine and low tyrosine and tryptophan  
74 may lead to low concentrations of monoaminergic neurotransmitters. This has been suggested  
75 to play an important role in the mood and psychosocial problems of PKU patients [22–24].  
76 However, while phenylalanine neurotoxicity, impaired cerebral protein synthesis and reduced  
77 cerebral monoaminergic neurotransmitter synthesis have all been associated with brain  
78 dysfunction in PKU patients [5]. Both cerebral protein synthesis and cerebral monoaminergic  
79 neurotransmitter synthesis show correlations with the plasma phenylalanine concentration that  
80 comprises the main treatment target and biomarker in today's PKU management.

81 Based on this pathophysiological concept, supplementation of non-phenylalanine LNAA  
82 instead of restricting dietary phenylalanine intake has been suggested as a possible alternative  
83 non-pharmaceutical treatment strategy [5,25]. Such LNAA treatment has been shown in PKU  
84 mice to (1) reduce brain phenylalanine, (2) increase brain non-phenylalanine LNAA, and (3)  
85 increase brain monoaminergic neurotransmitter concentrations [26]. To ultimately establish the

86 adequate dose of different LNAA, a better understanding of the pathophysiology of brain  
87 dysfunction in PKU, and especially of the relationships between plasma and brain amino acid  
88 concentrations, and between these amino acid and monoamine concentrations, is essential.  
89 The competition of amino acids for the LAT1 transporter and the involvement of additional  
90 amino acid transporters complicate the understanding of the effect of different diets on the  
91 brain amino acid and neurotransmitter composition. Such complex systems can be studied  
92 holistically using computational models. Two distinct modelling approaches exist that allow  
93 mechanistic studies of metabolic networks: 1) genome-scale constraint-based models, and 2)  
94 kinetic, ordinary differential equation (ODE)-type models. The genome-scale models comprise  
95 the entirety of the known metabolic network, including reaction stoichiometry and mass and  
96 charge balance. However, due to their scale and in contrast to kinetic models, they lack kinetic  
97 information and regulation [27]. Kinetic models usually represent only smaller pathways, due  
98 to their increased mechanical complexity and difficulty of obtaining accurate kinetic  
99 parameters [28].  
100 To address the problem of substrate competition for LAT1 amino acid transport in PKU,  
101 several computational models have been constructed that describe the kinetic behaviour of  
102 pathways involved in neurotransmitter metabolism or LNAA transport across the BBB [29–  
103 34]. However, none of these models integrates the dopaminergic and serotonergic pathways in  
104 the brain with the amino acid transport across the BBB. Constraint-based stoichiometric  
105 reconstructions of human metabolism, such as Recon 2 and Recon 3D, do include amino acid  
106 and neurotransmitter metabolism. Recon 2 correctly reproduced the elevated phenylalanine  
107 levels in PKU patients [35]. Recon 2 and its successor Recon 3D [36], however, lack the kinetic  
108 information that is required to grasp the impact of substrate competition for the LAT1 exchange  
109 transporter and the possible existence of other transporters or exchangers. Therefore, to study  
110 the consequences of the substrate competition for the LAT1 transporter, we decided to  
111 construct a kinetic, ODE-type model.  
112 Here we present the first, detailed, kinetic model of LNAA transport across the BBB, together  
113 with the brain dopaminergic and serotonergic metabolic pathways. In this model, we studied  
114 the effects of dietary interventions on brain amino acid composition, neurotransmitter  
115 metabolism, and protein synthesis in PKU, as related to experimental studies in PKU mice.  
116 The model was validated by comparison to a comprehensive dataset from our own research  
117 group consisting of plasma and brain amino acid and monoaminergic neurotransmitter levels  
118 in PKU mice subjected to several dietary interventions. Furthermore, we simulated the impact  
119 of modulating individual dietary amino acids concentrations and the way this could alleviate  
120 the pathophysiological cascade towards brain dysfunction as observed in PKU. Since the model

121 is generic, it can be readily applied to other inherited defects of amino acid metabolism and  
122 neurological disorders in which the relation between amino acid and neurotransmitter  
123 metabolism and the transport across the BBB is important, such as Tyrosinemia type 1 [37],  
124 maple syrup urine disease, urea cycle defects, depression [38], autism [39], Alzheimer's [40],  
125 and Parkinson's disease [41].

## 126 MATERIALS AND METHODS

### 127 ETHICS STATEMENT

128 Experiments were approved by the Ethics Committees for Animal Experiments of the  
129 University of Groningen (Permit Number: 6504D).

### 130 COMPUTATIONAL METHODS

131 The computational model, consisting of a set of 26 Ordinary Differential Equations (ODEs),  
132 was built and analysed in Copasi 4.39 [42]. COPASI is a widely used open open-source  
133 software package used in modelling biological systems, because it enables easy construction,  
134 simulation, and analysis of the models. It has a graphical user interface (GUI) that enables non-  
135 expert programmers to study metabolic networks behaviours using many built-in tools for the  
136 optimisation, parameter scans, steady state analysis, local sensitivity analysis and metabolic  
137 control analysis. Time simulations were performed using the LSODA algorithm for a duration  
138 of 100 s simulation time, with relative tolerance of  $1 \cdot 10^{-6}$ , absolute tolerance of  $1 \cdot 10^{-12}$ , and  
139 maximally 10,000 internal steps. Steady states were calculated using a combination of  
140 methods, according to the default settings in Copasi. The solutions fulfilled the criterion that  
141 all-time derivatives of metabolite concentrations approached zero ( $< 10^{-11}$ ). No alternative  
142 steady states were found when different initial metabolite concentrations were used. As an  
143 input for the steady-state algorithm, the endpoint of the time simulation was used. The detailed  
144 model description is available in Text S1. Copasi's 'Sensitivities' algorithm was used to  
145 calculate the response coefficients of brain metabolite concentrations to changes in model  
146 parameters and blood amino acid concentrations. The model is publicly available together with  
147 all the supplementary data in our GitHub repository (<https://github.com/WegrzynAB/Papers/>  
148 in the folder "2024\_mouse\_PKU\_model\_diets").

### 149 INDEPENDENT TEST AND VALIDATION

150 As a part of our standard quality control procedures, the model was independently tested by  
151 another researcher to assure that the results are reproducible, and the model description (Text  
152 S1) agrees to the Copasi script. A thorough comparison between model description and Copasi

153 file was made to check the correctness of all equations and parameter values. Subsequently, a  
154 subset of important model simulations was repeated to check if the output reproduced the  
155 presented results.

156 **DIETARY INTERVENTIONS IN MICE**

157 Experiments were performed in BTBR *Pah-enu2* (PKU) and corresponding WT mice, as  
158 previously described [18]. In brief, male and female PKU mice received 1 of 5 different LNAA  
159 supplemented diets beginning at postnatal day 45. Control groups included PKU mice  
160 receiving an isonitrogenic and isocaloric high-protein diet, and PKU and WT mice receiving  
161 normal chow. After 6 weeks, brain and plasma amino acid profiles and brain monoaminergic  
162 neurotransmitter concentrations were measured.

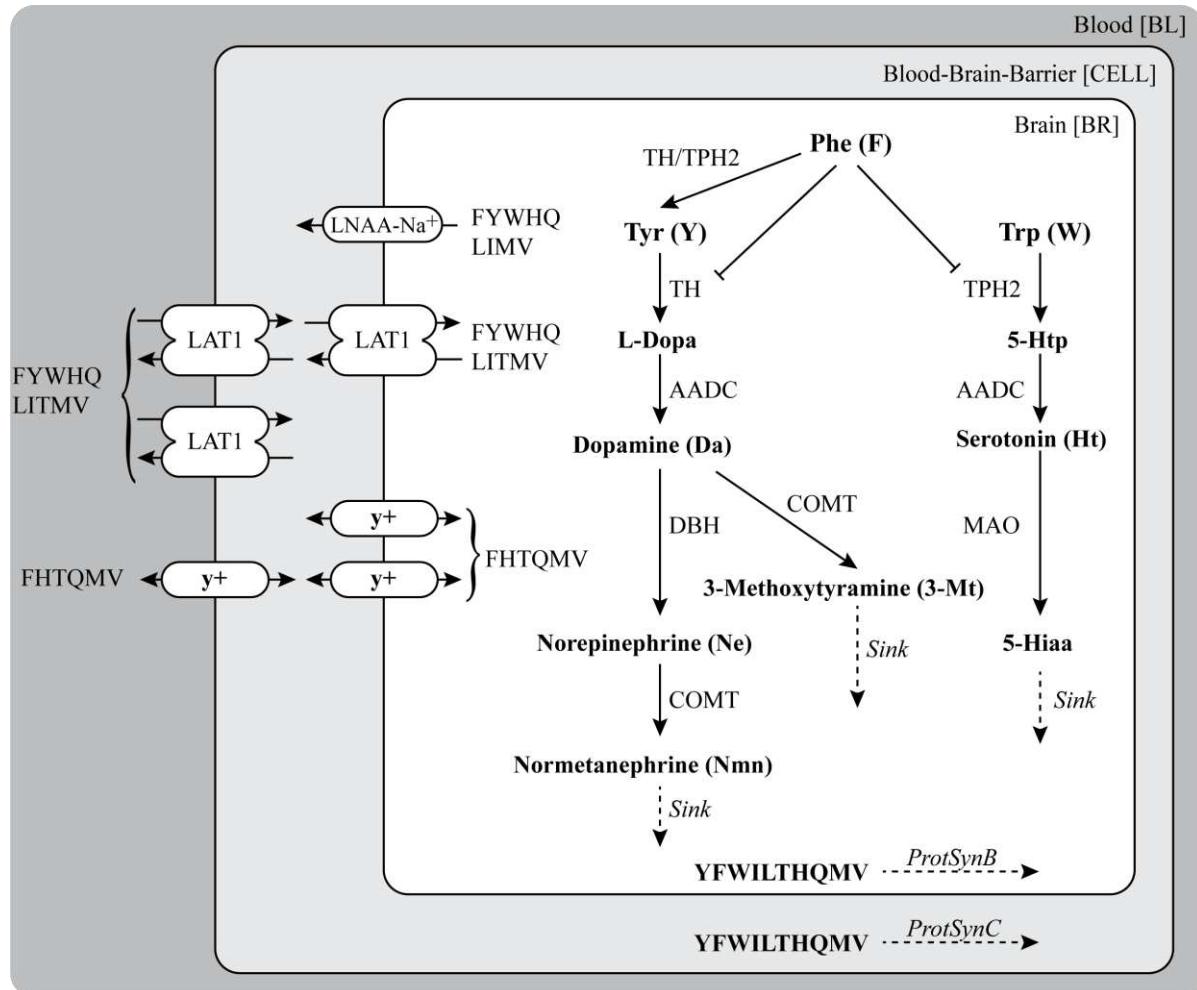
163 **BIOCHEMICAL ANALYSIS**

164 Cerebrum and blood samples were processed for the analyses of brain and plasma amino acid  
165 and monoamine concentrations, as described previously [26]. Monoamines and related  
166 metabolites analysed in the brain included dopamine, norepinephrine, 3-methoxytyramine and  
167 normetanephrine in the catecholamine pathway, and serotonin and 5-hydroxyindoleacetic acid  
168 (5-HIAA) in the serotonergic pathway.

169 **RESULTS**

170 **MODEL CONSTRUCTION**

171 We constructed a computational model that describes the transport of LNAA across the BBB  
172 and the metabolism of cerebral amino acid and monoamines in mice (Fig.1). The computational  
173 model consists of ordinary differential equations (ODEs) and is based on biochemical rate  
174 equations. It is focused on the transport of phenylalanine, tyrosine, and tryptophan between  
175 blood and brain and on their cerebral metabolism, but also includes the transport of other  
176 LNAA to fulfil the requirements for cerebral protein synthesis. We defined three  
177 compartments: 1) blood, with fixed amino acid concentrations; 2) the BBB, a cell layer with  
178 active protein synthesis, transport processes, and variable amino acid concentrations; and 3)  
179 brain, with active protein synthesis [10], transport reactions, monoamine metabolism, and  
180 variable metabolite concentrations. Fig.1 gives an overview of all enzymatic reactions and  
181 transport processes in the model.



182

183 **Figure 1. Model of amino acid transport via the blood-brain-barrier and neurotransmitter**  
184 **metabolism inside the brain.** The transporter LAT1 is twice as abundant on the luminal (blood-cell)

185 side than on the abluminal (cell-brain) side of the blood-brain-barrier, while the y<sup>+</sup> transporter displays  
186 a reversed distribution. F – phenylalanine, Y – tyrosine, W – tryptophan, H- histidine, Q – glutamine,  
187 L – leucine, I -isoleucine, M – methionine, V – valine, T – threonine, 5-Hiaa – 5-Hydroxyindoleacetic  
188 acid.

189

190 The primary LNAAs transporter at the BBB is LAT1. LAT1 is a Na<sup>+</sup>- and pH-independent  
191 antiporter, which forms a heterodimeric complex with CD98 glycoprotein and exchanges one  
192 amino acid for another. According to Napolitano et al., LAT1 binds the two amino acids on the  
193 opposite sides of the membrane in a random order [33]. In the model, the mechanism of LAT1  
194 is described by random-order two-substrates two-products kinetics. This kinetic equation has  
195 been extended to account for competition between all LAT1 substrates (Eq. 1 and 2 in Text  
196 S1). Since LAT1 is an antiporter, it does not lead to a net import of amino acids. However, due  
197 to the different affinities of LAT1 for specific amino acids, it leads to an altered composition  
198 of the amino acid pool. In contrast, the so-called y<sup>+</sup> system is a facilitated diffusion transporter,  
199 which catalyses the net transport of LNAAs. This transporter shows the highest affinity towards  
200 cationic amino acids, but at the same time, it is inhibited by various LNAAs [43]. Since no exact

201 mechanism is known, reversible Michaelis-Menten kinetics with an equilibrium constant of 1  
202 and competition between the various substrates was used (Eq. 3 and 4 in Text S1). Finally, we  
203 included the  $\text{Na}^+$ -dependent large neutral amino acid transporter ( $\text{Na}^+$ -LNAA), which actively  
204 transports amino acids out of the brain. It transports a range of substrates similar to that of  
205 LAT1, but in contrast to LAT1,  $\text{Na}^+$ -LNAA is only expressed on the abluminal side of the  
206 BBB. Together with the  $\text{y}^+$  system,  $\text{Na}^+$ -LNAA controls the total LNAA content of the brain  
207 [44]. In our model, the  $\text{Na}^+$ -LNAA kinetics are described by an irreversible Michaelis-Menten  
208 equation with competition between the various substrates (Eq. 5 in Text S1).

209 To account for the imbalance of cerebral monoamines, including neurotransmitters, in PKU  
210 patients, we included monoamine metabolism in the model (Fig.1). It consists of two main  
211 pathways: 1) tyrosine metabolism to L-dopa, dopamine (DA), norepinephrine (NE), 3-  
212 methoxytyramine (3-MT), and normetanephrine (NMN); and 2) tryptophan metabolism to 4-  
213 hydroxytryptophan (4-HTP), serotonin (HT) and 5-hydroxyindoleacetic acid (5-HIAA). The  
214 first step in both pathways is catalysed by an amino acid hydroxylase. Both tyrosine  
215 hydroxylase and tryptophan hydroxylase (TH and TPH2, respectively in Fig.1) are inhibited  
216 non-competitively and competitively by phenylalanine [45]. Since phenylalanine is not only  
217 an inhibitor, but also a substrate for these enzymes, it can be converted at a low rate to tyrosine  
218 in the brain [46]. We modified the kinetic mechanism proposed by Ogawa and Ichinose [45]  
219 to include not only the role of phenylalanine, but also competitive inhibition by L-dopa [47],  
220 NE, and DA [48] for tyrosine hydroxylase, and by 4-HTP [49], L-dopa, and DA [50] for  
221 tryptophan hydroxylase (Eq. 6 and 7 in Text S1). Tetrahydrobiopterin was assumed to be  
222 available at a saturating concentration for both hydroxylases and therefore not included in the  
223 model. Subsequent metabolic steps were described by Michaelis-Menten kinetics, with  
224 substrate competition where applicable (see detailed description in Text S1).

225 Lastly, brain-protein synthesis is affected both in PKU patients [10] and in PAH-deficient  
226 mouse models [16]. We included the synthesis of protein starting from the amino acids that  
227 were already in the model. Implicitly, we thereby assumed the other amino acids to be present  
228 in excess. The amino acid stoichiometry in protein synthesis was calculated from the mouse  
229 exome [51]. The affinity constants ( $K_m$  values) used in the protein-biosynthesis equation reflect  
230 the affinity of each of the amino acids to its cognate tRNA-ligase.

231 All parameters used in the model, except for the  $V_{max}$  of LAT1, were taken from the literature.  
232 Where available, we prioritised murine data, as specified in Table S2 in Text S1. All enzyme  
233 rates were normalised per total mouse brain. The value of  $V_{max}$  of LAT1 enzyme was found  
234 by a manual fitting to the WT data, since no value was available that could be related reliably  
235 to total mouse protein. Based on the above, we constructed a model of 26 variable metabolite

236 concentrations, 105 reactions, and 89 parameters. Model simulations predicted fluxes and  
237 metabolite concentrations both as functions of time and at steady state. Detailed information  
238 about the parameter values and their source can be found in the model description (Text S1).

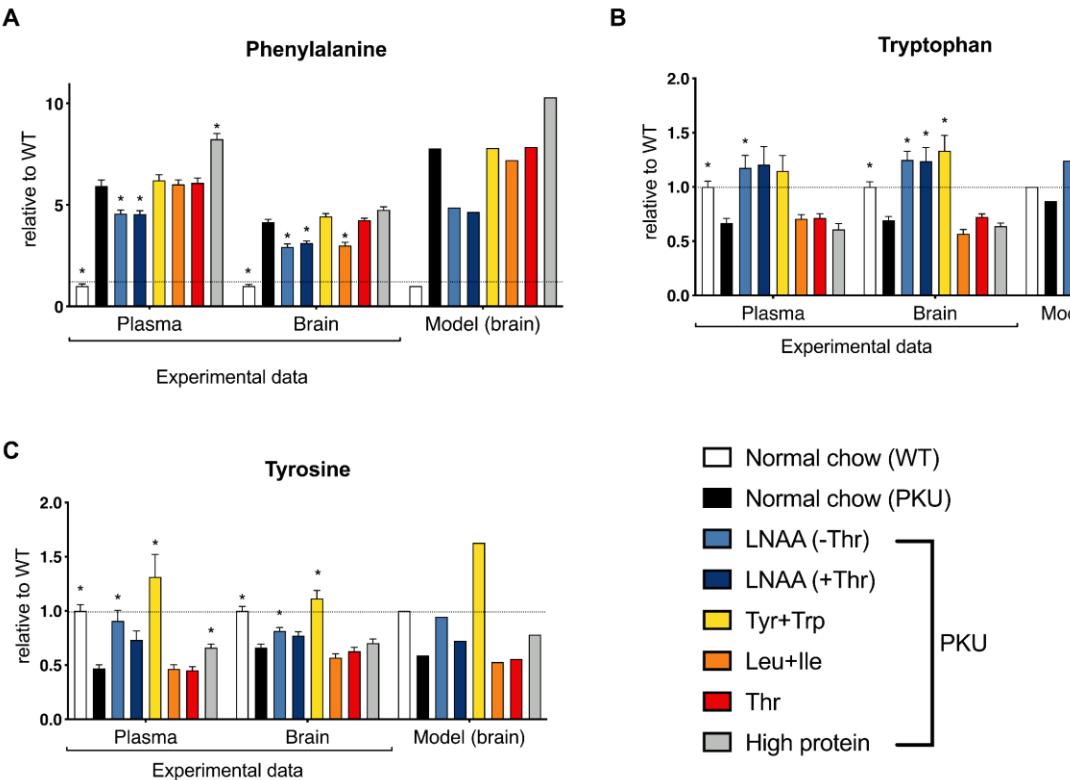
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240 **EXPERIMENTAL VALIDATION OF THE MODEL: THE EFFECT OF DISEASE AND DIET**  
241 **ON BRAIN AMINO ACIDS**

242 To better understand the relationship between plasma amino acids and brain biochemistry in  
243 PKU, we simulated the effect of different diets that were previously given to PKU mice [52].  
244 The blood concentrations in the model were fixed and set to the values measured in the specific  
245 mice groups (see Table S3 in Text S1). PAH, the defective enzyme in PKU, is expressed in the  
246 liver and kidney, but not in the brain. The PKU model is therefore distinguished from the WT  
247 model by the altered concentrations of amino acids in the blood compartment. Notably, blood  
248 phenylalanine is high and blood tyrosine low in PKU compared to WT mice on normal chow  
249 diet

(Table

S4).



250

251 **Figure 2. Comparison between experimental data and model predictions for changes in the brain**  
252 **levels of (A) phenylalanine, (B) tryptophan, and (C) tyrosine, in PKU mice with dietary**  
253 **interventions, relative to the WT values.** For the experimental data, each bar represents a mean (ns =  
254 16) with a standard error of the mean. Significant differences between diets and normal chow PKU mice  
255 have been marked with \*.

256

257 Our model distinguishes between the BBB compartment (called CELL) and the brain itself  
258 (BR) (Fig. 1). The experimental data used for model optimisation and validation, however, had

259 been obtained from total brain samples that also included the BBB. Therefore, we calculated  
260 as model output a weighted average of the concentrations in the CELL and BR compartments,  
261 considering the difference in the volume of these two compartments (for details see Text S1).  
262 Furthermore, since the modelled and experimental data for brain concentrations had different  
263 units ( $\mu\text{mol/g}$  wet weight and  $\mu\text{M}$ , respectively), we compared only values relative to the WT  
264 in both experimental data, and model predictions.

265 The simulated data resembled the experimental data for cerebral amino acid concentrations,  
266 based on low normalised difference scores. The most accurate predictions were obtained for  
267 glutamine, tyrosine and tryptophan (Fig.S1). The model simulations correctly predicted that  
268 cerebral phenylalanine accumulated in PKU mice compared to WT, when both were kept on a  
269 non-supplemented chow diet (black bars in Fig.2A). The accumulation of phenylalanine was  
270 larger in the model than in the experiment, which is also visible in its large relative difference  
271 score (Fig.S1). Nevertheless, the relative increase predicted by the model was within the values  
272 reported in the literature (Table 1). Furthermore, we observed a 17% decrease in the protein  
273 synthesis rate in the brain compartment and a 27% decrease in the BBB compartment in the  
274 PKU model compared to WT, in line with previously published experimental data in PKU mice  
275 [16] (Fig.S3).

276 **Table 1. Comparison between the model predictions and literature data on cerebral amino acid**  
277 **and neurotransmitter levels.** Relative (PKU/WT) values are shown. BTBR and C57BL/6 denote the  
278 background mice strain, M and F are used to describe males and females, respectively.

model	van Vliet <i>et al.</i> [25]	Pascucci <i>et al.</i> [46]	Scherer <i>et al.</i> [47]	Berguig <i>et al.</i> [48]	Winn <i>et al.</i> [49]	
	BTBR	BTBR	C57BL/6	C57BL/6	C57BL/6	
					M	F
Phenylalanine	778%	414%	469%	609%	684%	648%
Tyrosine	59%	66%	60%		69%	78%
Tryptophan	87%	69%			70%	70%
Dopamine	48%	85%	60%		75%	103%
Norepinephrine	47%	61%	50%		59%	
Serotonin	23%	46%	35%	reduced	33%	57%
5-HIAA	23%	28%		reduced	11%	43%
						33%

279  
280 Dietary supplementation of PKU mice with all LNAA (with or without threonine) reduced  
281 phenylalanine levels in the brain, similarly to what is seen in the experiment (light and dark  
282 blue versus black bars in Fig.2A). Furthermore, this intervention restored the protein synthesis  
283 rate in the model to the WT levels (Fig.S3). This may suggest that the other LNAs compete  
284 effectively with phenylalanine for transport by LAT1 and other transporters, both in the model  
285 and the experiment. We note, however, that the blood concentrations of phenylalanine were

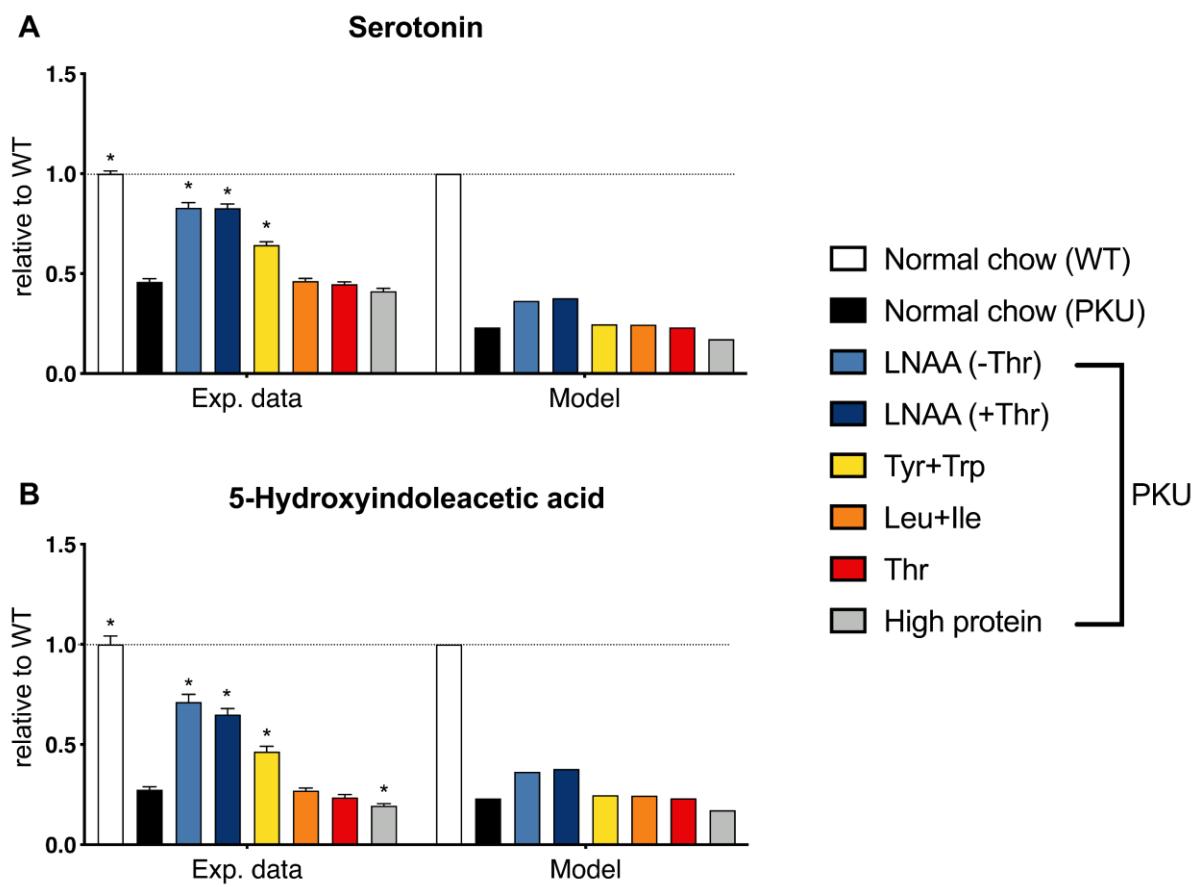
286 also lower in the LNAAs supplemented groups (Table S4.4 and [26])). Supplementation of only  
287 tyrosine and tryptophan had no effect on brain phenylalanine, neither in the model nor in the  
288 experiment (yellow versus black bars in Fig.2A). Experimentally, supplementation of leucine  
289 plus isoleucine reduced the phenylalanine concentration in the brain. This effect was attenuated  
290 in the model (orange bars, Fig.2A). Previously, the strong impact of leucine and isoleucine was  
291 attributed to their high affinities for LAT1 [53]. We have implemented these affinities in the  
292 model. In line with this, supplementation of leucine and isoleucine increased their brain  
293 concentrations substantially (Fig.S2.). Apparently, however, their high affinities are not  
294 sufficient to explain their impact on brain phenylalanine in the experiments, suggesting that  
295 leucine and isoleucine act at least in part via another unknown mechanism. Next, threonine  
296 supplementation has been given in one study showing a decrease of phenylalanine in blood  
297 hypothesising that this decrease in blood phenylalanine levels would also result in a decrease  
298 in cerebral phenylalanine [54]. However, this effect was neither seen in experimental data nor  
299 in model simulations (red bars, Fig.2A). Finally, a high protein diet served as a positive control  
300 in which all amino acids are abundant. Experimental data, as well as model simulations,  
301 showed a further increase in the brain phenylalanine levels in PKU mice on a high protein diet  
302 (grey bars, Fig.2A).

303 Subsequently, the impact of the different diets on tryptophan and tyrosine in the brain was  
304 accurately predicted by the model (Fig.2B and C). In both model and experiment, tryptophan  
305 and tyrosine were most increased by the addition of these amino acids to the diet, while  
306 selective supplementation of threonine or leucine plus isoleucine had no effect on the brain  
307 concentrations of tryptophan or tyrosine. The brain concentrations of the other amino acids are  
308 shown in Fig.S2. First, the concentration of glutamine did not change much on any of the  
309 experimental diets in either model or experiment (Fig.S2A). The model missed, however, the  
310 increased brain concentration of histidine that was experimentally found in the PKU mice  
311 (Fig.S2B). The brain concentrations of leucine and isoleucine did not respond very strongly to  
312 either PKU or dietary supplementation of other amino acids. This was qualitatively reproduced  
313 by the model (Fig.S2C and D). However, the model predicted a much higher response of brain  
314 leucine and isoleucine to supplementation with these amino acids (leucine+isoleucine diet)  
315 than the experimental data showed. Finally, the brain concentrations of methionine plus valine  
316 (MV) and threonine (Fig.S2E and F) showed similar profiles in the model simulations and the  
317 mouse experiment. Particularly, the threonine concentration increased strongly in the brain if  
318 supplemented in the diet, either with or without other LNAAs (dark blue and red bars in  
319 Fig.S2). Furthermore, except for glutamine and histidine, we observed a correlation between

320 plasma and brain levels of all amino acids, both in the experimental data and in the model  
321 predictions (Fig.S2).

322 **EXPERIMENTAL VALIDATION OF THE MODEL: THE EFFECT OF DISEASE AND DIET**  
323 **ON NEUROTRANSMITTERS**

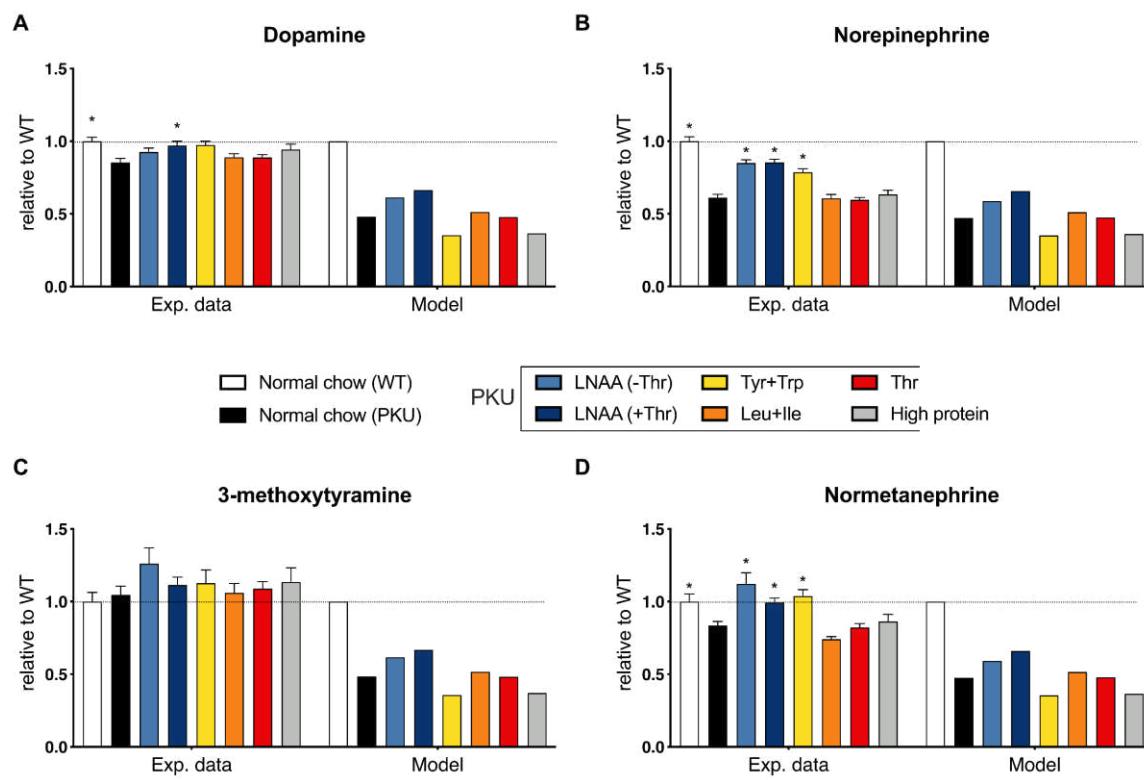
324 Subsequently, we compared the brain monoaminergic neurotransmitter levels between model  
325 and experiments. The computational model correctly predicted the decrease in both tryptophan-  
326 and tyrosine-derived neurotransmitter levels in PKU mice compared to the wild-type controls  
327 (Fig.3,4, and Table 1). In general, the decrease was stronger in the model than in the  
328 experiments, especially in the dopaminergic pathway (Fig.4, and Table 1). The experimental  
329 data shows only a mild decrease in the dopamine levels, followed by a stronger response in the  
330 norepinephrine and normetanephrine levels, whilst no change was seen in the 3-  
331 methoxytyramine levels. This contrasts with our model predictions where all the dopaminergic  
332 metabolites show the same decline in their levels in the PKU model compared with the WT  
333 (Fig.4, and Table 1).



334

335 **Figure 3. Model validation for the levels of the tryptophan-derived neurotransmitter serotonin**  
336 **(A), and its metabolite 5-HIAA (B) in PKU mice with dietary interventions, relative to the WT**  
337 **values.** For the experimental data, each bar represents a mean (ns = 16) with a standard error of the  
338 mean. Significant differences between diets and normal chow PKU mice have been marked with \*.

339 Subsequently, we analysed the response of the neurotransmitter concentrations to different  
340 diets. Qualitatively, the tryptophan-derived neurotransmitters showed the same dietary profiles  
341 in experiments and simulations, but in the simulations the response was attenuated compared  
342 to the experiments (Fig.3). In both experiments and simulations serotonin and 5-  
343 hydroxyindoleacetic acid levels were effectively increased by supplementation with LNAA  
344 plus threonine (Fig.3). In the model, the LNAA diet with threonine increased these  
345 neurotransmitters slightly more than the LNAA diet without threonine. The difference was  
346 smaller, however, than the experimental error.



347

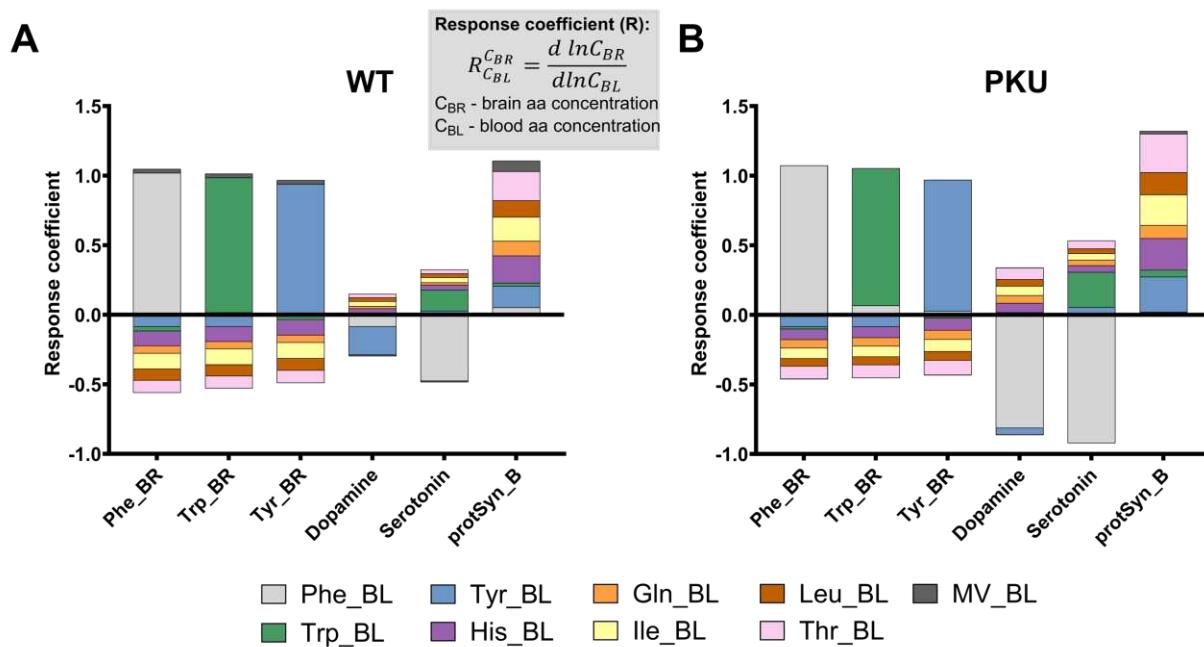
348 **Figure 4. Model validation for the levels of the tyrosine-derived neurotransmitters: (A) dopamine,**  
349 **and (B) norepinephrine, as well as their metabolites: (C) 3-methoxytyramine, and (D)**  
350 **normetanephrine in PKU mice with dietary interventions, relative to the WT values.** For the  
351 experimental data, each bar represents a mean (ns = 16) with a standard error of the mean. Significant  
352 differences between diets and normal chow PKU mice have been marked with \*.

353  
354 According to the model, the LNAA diet with threonine was the only diet with a strong  
355 stimulatory effect on the dopamine pathway (Fig. 4). The simulated tyrosine- plus tryptophan-  
356 enriched diet even further decreased the levels of the dopaminergic metabolites slightly if  
357 compared to the PKU without treatment. This is, however, not seen in the experimental data,  
358 which showed a modest increase over normal chow (PKU) in brain dopamine and  
359 norepinephrine on the tyrosine- plus tryptophan-enriched diet compared to normal chow. This

360 suggests that we miss a mechanism in the model that buffers the dopaminergic neurotransmitter  
361 concentrations in mice *in vivo*.

362 BRAIN AMINO ACID AND NEUROTRANSMITTER LEVELS, AND PROTEIN  
363 SYNTHESIS RATES ARE SENSITIVE TO THE BLOOD CONCENTRATIONS OF AMINO  
364 ACIDS

365 *In vivo*, it is not feasible to assess the impact of each individual amino acid in the blood  
366 systematically. Since the model provided a fairly good representation of the *in vivo* situation,  
367 we calculated the response coefficients (Fig. 5A) of the clinically relevant output variables  
368 towards changes in the concentrations of individual amino acids in the blood. A positive  
369 response coefficient means that an increase of the blood amino acid concentration increases  
370 the output variable, whereas a negative response coefficient would decrease it.



371

372 **Figure 5. Brain levels of phenylalanine, tryptophan, and tyrosine are susceptible to the changes**  
373 **in the corresponding blood levels of these amino acids in both (A) WT, and (B) PKU models.** Bars  
374 represent positive and negative response coefficients of brain phenylalanine, tyrosine, tryptophan, as  
375 well as dopamine, serotonin, and protein synthesis, to the changes in the blood amino acid  
376 concentrations.

377 The response coefficients were qualitatively similar between WT and PKU model predictions  
378 (Fig. 5) as well as in the different diets (Fig. S5). However, in the PKU model, the dopamine  
379 and serotonin levels responded more sensitively to the changes in individual amino acid  
380 concentrations (cf. Fig. 5A and B). In the following, we will focus on the PKU model (Fig.  
381 5B).

382 Blood phenylalanine had by far the strongest impact on its own brain concentration as well as  
383 on that of the neurotransmitters. The brain tyrosine and tryptophan levels responded only  
384 weakly to blood phenylalanine. Surprisingly, these amino acid levels were even increased by  
385 increased blood phenylalanine (Fig 5 and Fig. S10). Furthermore, LAT1 reactions showed only  
386 a minor concentration control coefficient for brain amino acid levels (Fig. S11). This suggests  
387 that competition for LAT1, at least in the present model, is not a dominant factor for these  
388 amino acids. The sensitive response of the neurotransmitters, but not of their precursors,  
389 suggests that their synthesis is mostly affected by phenylalanine inhibition, rather than by the  
390 lack of precursors, at least in the model.

391 Supplementation of tyrosine or tryptophan had a positive impact on their own brain levels, as  
392 indicated by the relatively large, positive response coefficients. Neither had a strong effect on  
393 the phenylalanine concentration, confirming that the interaction between phenylalanine on the  
394 one hand and tyrosine and tryptophan on the other, was weak. Tryptophan had a positive impact  
395 on serotonin, albeit less than the negative effect of phenylalanine. In contrast, the precursor  
396 tyrosine had little effect on dopamine. Dopamine is overall less sensitive to blood amino acid  
397 levels than serotonin. This may explain why the impact of PKU on dopamine is less than on  
398 serotonin in the first place, both in experiments and model. A counterintuitive finding was the  
399 negative response of dopamine to plasma tyrosine concentration in the WT, caused by substrate  
400 inhibition of tyrosine hydroxylase by tyrosine (Fig. 5B and Fig. S6C). Tyrosine titration  
401 showed that this effect was not present in the PKU model since the latter operated at the point  
402 where substrate stimulation and substrate inhibition were just balanced (Fig. S6C).

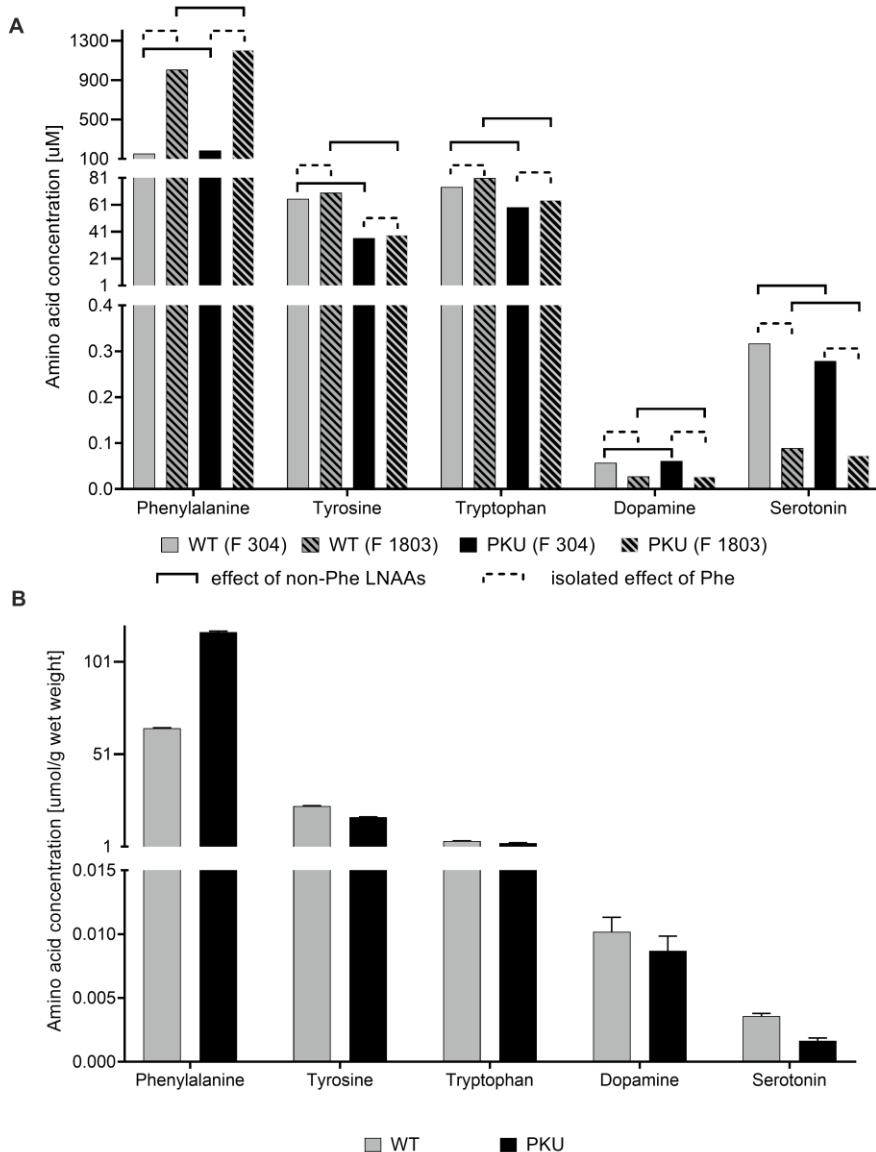
403 The other amino acids, notably threonine, histidine, leucine, and isoleucine, reduced the brain  
404 phenylalanine concentration. Individually they had a low response coefficient, but together  
405 they could have a substantial impact (Fig. 5B). They also impacted positively on dopamine and  
406 serotonin, presumably through alleviating the inhibition by phenylalanine. To test this  
407 hypothesis, we modelled the impact of doubling the plasma concentrations of threonine,  
408 histidine, leucine, and isoleucine (THLI perturbation) in the PKU normal chow diet.  
409 Furthermore, we tested scenarios where only one of these AAs was increased so that the sum  
410 of threonine, histidine, leucine, and isoleucine was the same as in the THLI perturbation.  
411 Similarly, we tested the effect of a proportional increase in all non-phenylalanine LNAAs. Last,  
412 we tested extension of THLI perturbation by additional supplementation of tyrosine and  
413 tryptophan to their WT normal chow plasma levels. As response coefficient analysis suggested,  
414 THLI perturbation was able to substantially decrease the brain phenylalanine levels more than  
415 any of the amino acids alone (Fig. S12A). However, the effect of THLI perturbation on brain

416 levels of neurotransmitters was only minimal (Fig. S12J-O). Since the leucine only diet showed  
417 the least improvement, we decided to test a scenario where only threonine, histidine, and  
418 isoleucine (THI perturbation) were added (maintaining the sum of threonine, histidine, and  
419 isoleucine equal to the one in THLI perturbation). With THI only supplementation, we saw an  
420 even bigger decrease in phenylalanine levels as well as an increase in neurotransmitter levels  
421 (Fig S12A and J-O). Additional supplementation of tyrosine and tryptophan in both THLI and  
422 THI perturbations showed a further decrease in phenylalanine and an increase in  
423 neurotransmitter levels (Fig S12A and J-O).

424 Furthermore, all amino acids are shown to stimulate protein synthesis in the brain with histidine  
425 and isoleucine having the biggest impact in the PKU model (Fig 5B). A drawback of  
426 supplementation of these amino acids, however, would be their negative impact on the brain  
427 concentrations of tyrosine and tryptophan, most likely through competition for LAT1.  
428 However, this may be alleviated by an increase in the tyrosine and tryptophan in the diet  
429 (Fig.S12). Interestingly, histidine-only perturbation showed that at high brain histidine  
430 concentrations the weak inhibition of DBH enzyme by histidine could lead to a reduction of  
431 norepinephrine and normetanephrine levels while dopamine levels remain stable Fig. S12J-M).

432 INCREASE IN THE BLOOD PHENYLALANINE LEVELS ALONE DOES NOT DECREASE THE  
433 BRAIN TYROSINE AND TRYPTOPHAN LEVELS, BUT IT DOES INHIBIT THE SYNTHESIS  
434 OF NEUROTRANSMITTERS.

435 In PKU mice, the blood concentrations of multiple amino acids were changed simultaneously  
436 compared to the WT. To disentangle the effect of the increased phenylalanine concentration  
437 from that of the other amino acids, we performed an *in silico* experiment. To this end, all blood  
438 amino acid concentrations were fixed at the levels measured in either WT or PKU mice without  
439 dietary supplementation. Then, Phe was increased to PKU level in the WT (Phe 1803,  
440 corresponding to 1803  $\mu$ M), or to WT level in the PKU model (Phe 304, corresponding to 304  
441  $\mu$ M) (Fig. 6). Brain phenylalanine accumulates in response to the change in the blood  
442 phenylalanine levels as expected (cf. WT Phe 304 to WT 1803; or PKU Phe 304 to PKU 1803  
443 in Fig. 6A). In contrast, brain phenylalanine did not respond to other amino acids that were  
444 altered in PKU (cf. WT Phe 304 to PKU Phe 304; or WT Phe 1803 to PKU Phe 1803 in Fig.  
445 6A). Tyrosine and tryptophan hardly responded to the change in phenylalanine but decreased  
446 in response to alterations of the other amino acids in PKU (cf. WT to PKU at either Phe  
447 concentration in Fig. 6A).



448

449 **Figure 6. Changes to the brain phenylalanine, tyrosine, tryptophan, dopamine, and serotonin**  
450 **levels in response to the blood phenylalanine increase/decrease in WT and PKU model**  
451 **simulations (A), in comparison with the experimental data from mice (B).** WT or PKU indicate that  
452 all blood amino acid concentrations except those of phenylalanine were equal to those measured in WT  
453 or PKU, respectively. Phe 304 indicates that the WT phenylalanine concentration of 304 μM was used,  
454 whereas Phe 1803 indicates that the PKU phenylalanine concentration of 1803 μM was used.  
455

456 The brain neurotransmitters decreased strongly in response to the increased blood  
457 phenylalanine levels (Fig. 6A and Fig. S7C and D) in line with the experimental data (Fig. 6B).  
458 However, the dopamine to serotonin ratio in the model was opposite to that of the one seen in  
459 the experimental data (Fig. 6B). Even when the blood concentrations of tyrosine and  
460 tryptophan were doubled or quadrupled, the strong inhibition of dopamine and serotonin levels  
461 by phenylalanine synthesis persisted (Fig. S7-S9). Only when blood phenylalanine  
462 concentration was lowered to 750 μM (Phe 750, halfway between WT and PKU values) the

463 combined addition of tyrosine and tryptophan had a positive effect on serotonin, while  
464 dopamine levels were still lower than in the WT (Phe 750, Fig. S9).

## 465 DISCUSSION

466 In this work, we present the first dynamic model that links the LNAA transport system across  
467 the BBB to the subsequent brain neurotransmitter metabolism and protein synthesis (Fig. 1).  
468 In particular, we included extensive competition between the substrates of the LAT1  
469 transporter across the BBB. The model was designed to ultimately understand and optimise  
470 how dietary treatment affects the brain biochemistry in PKU patients.

471 As the mouse brain is experimentally more accessible than the human brain, and PKU mouse  
472 models closely resemble the genetics, biochemistry, and neurobiology of human PKU, the  
473 detailed mechanism of PKU pathophysiology has mostly been studied in PKU mice. Therefore,  
474 the model was based on data from the BTBR mouse strain and validated against data of the  
475 PKU mice in the same background strain. Considering the large number and heterogeneity of  
476 the kinetic parameters (Table S2) the correspondence between model predictions and  
477 experimental data was remarkably good. Moreover, while not all metabolic fates of Phe,  
478 tyrosine and tryptophan were included in the model, we included the most important metabolic  
479 pathways. Kinetic parameters were not fitted to the desired outcome but based on biochemical  
480 data of specific enzymes. Models of this type give insight in how complete our biochemical  
481 knowledge is to understand functional properties, such as the neurotransmitter levels [55,56].

482 Qualitatively, the model largely reproduced the impact of PKU and most of the dietary  
483 treatments on brain biochemistry (Figures 2-4, and Table 1) as seen in the mice with PKU. The  
484 most conspicuous exception was the leucine plus isoleucine diet, which reduced phenylalanine  
485 levels in PKU mouse experiments, but barely in the PKU model. The affinity of LAT1 for  
486 leucine and isoleucine in the model was high, in accordance with the biochemical data, and  
487 these amino acids readily crossed the BBB. Yet, their calculated impact on phenylalanine  
488 uptake was limited. This discrepancy led us to conclude that leucine and isoleucine probably  
489 affect brain phenylalanine levels via another mechanism besides the simple competition for  
490 LAT1. So far, existing research on the metabolic role of branched-chain amino acids shows  
491 that leucine can stimulate protein synthesis and decrease protein breakdown [57,58]. Indeed,  
492 in our simulations, we saw a small increase in protein synthesis rate in leucine and isoleucine  
493 diet (Fig. S3). Since phenylalanine is more abundant than tyrosine and tryptophan in mouse  
494 protein [51], stimulation of protein synthesis could decrease free phenylalanine levels, without  
495 depleting the free tyrosine and tryptophan levels. Another possibility might be that LAT1 is

496 not the only transporter but that other transporters - such as LAT2 of which the function and  
497 the location of in brain is still debated - are not sufficiently considered.

498 Another qualitative discrepancy between model and experiment was the finding that the  
499 tyrosine plus tryptophan diet increased the neurotransmitter levels experimentally, but not in  
500 the model. This might well be explained by the fact that, in the model, brain phenylalanine  
501 levels in PKU compared to WT were much more increased than seen in the PKU mouse  
502 experiments. On the contrary, the reduction of brain tyrosine and tryptophan levels in PKU  
503 compared to WT in the model was less than observed in the mouse experiments.

504 Quantitatively, the calculated effect of PKU on most brain metabolites in the model was larger  
505 than the measured effects in the mouse experiments, with was especially true for brain  
506 phenylalanine levels. The fundamental reason why a quantitative agreement is beyond reach at  
507 this stage could be the compartmentation of the brain. The available validation data are in  
508  $\mu\text{mol/g}$  wet weight of the total brain, whereas the model predicts local concentrations in  
509  $\mu\text{mol/L}$ . The model already includes some compartmentation, specifically the blood  
510 compartment, the endothelial cells of the BBB, and the brain itself. To relate the model  
511 outcome to the validation dataset, a weighted average between the BBB and the brain  
512 compartment was made and an estimate of the cytosolic volume relative to the brain wet  
513 weight. Most likely, the uncertainty in this conversion is an important reason for the  
514 quantitative discrepancy. Naturally, uncertainties in the biochemical parameters may also play  
515 a role, taken into account that only few of the parameters were mouse specific. However, not  
516 all the parameters exert strong control on the brain concentrations of neurotransmitters and  
517 amino acids, and in general, we found the biochemical literature of high quality. Further  
518 progress could be made by using an intermediate experimental system that is closer to the  
519 model. Taslimifar et al. [29,34] proposed further compartmentation of their brain model into  
520 blood, endothelial cells, cerebral spinal fluid, and dopaminergic and serotonergic neurons. To  
521 validate such a model experimentally, novel organ-on-chip technology holds great promise,  
522 particularly since different tissue- and or cell-type-specific chips can be coupled functionally  
523 [59,60].

524 At this stage, the qualitative agreement between model and mice experiments already allows  
525 us to interrogate the model. For many mechanistic and clinical questions, it is sufficient to rank  
526 the impact of different interventions and to predict in which direction they could work. Given  
527 the complexity of the system, modelling can provide non-trivial answers. A particular  
528 advantage is that, in a model, the impact of individual amino acids in the blood can be

529 investigated one by one, in contrast to the different diets which change multiple amino acid  
530 levels in the blood at the same time.

531 Firstly, the model correctly predicted the altered brain levels of amino acids in PKU (Fig. 2).  
532 Notably, the phenylalanine concentration was increased, whereas tyrosine and tryptophan were  
533 decreased in the brain. The model suggests that the decrease of cerebral tyrosine and tryptophan  
534 is not primarily due to competition with the high phenylalanine concentration for the LAT1  
535 transporter. Rather, tyrosine and tryptophan were already decreased in the blood (Table S4).  
536 According to the model, this decrease of blood tyrosine and tryptophan appeared to be a  
537 prerequisite for the decrease of their cerebral concentrations (Fig. 6). The lower blood levels  
538 of tyrosine in PKU mice and patients can be attributed to impaired production in the liver due  
539 to the PAH deficiency, but may also be caused by alterations the intestinal uptake, altered  
540 microbiota composition or metabolism [61,62]. The lower blood levels of tryptophan in PKU  
541 mice and patients are less well understood, but altered metabolism of tryptophan via the  
542 kynurenine pathway has been suggested to play a role [63].

543 Second, the model qualitatively reproduced the decline of brain neurotransmitter levels that  
544 was observed in PKU mice [18,64]. The fact that the dopamine pattern mimics that of tyrosine,  
545 while the serotonin pattern mimics that of tryptophan, may seem to suggest that  
546 neurotransmitter levels are controlled by precursor levels. However, the response coefficients  
547 in the model (Fig. 5) showed the opposite: both cerebral serotonin and dopamine were strongly  
548 negatively controlled by blood phenylalanine, most likely via the strong negative inhibition of  
549 tyrosine and tryptophan hydroxylases by phenylalanine (Fig. 1).

550 Third, the response coefficients showed that isoleucine, leucine, histidine, threonine, and  
551 tyrosine all contributed individually to a reduction of the phenylalanine levels and an increase  
552 of neurotransmitter levels in the brain of PKU mice (Fig. 5, Fig. S12). This is surprising since  
553 neither the leucine plus isoleucine nor the threonine diet affected brain phenylalanine and  
554 neurotransmitter levels in the model (Fig. 2). We should keep in mind, however, that the effect  
555 of individual amino acids that compete for LAT1 was very small compared to that of  
556 phenylalanine. When supplemented together, however, as in the complete LNAA  
557 supplementation, they have a strong impact (Fig. 2 and 3, Fig. S12).

558 A final striking result was the weak, but significantly positive, effect of blood phenylalanine  
559 on the brain concentrations of tyrosine and tryptophan in the model. This was seen in the  
560 positive response coefficients of blood phenylalanine on tryptophan in PKU (Figure 5B) as  
561 well as in a minor increase of tryptophan and tyrosine when the impact of elevated

562 phenylalanine in PKU was simulated without the concomitant decrease of the other amino  
563 acids (Figure 6A). The effect can be explained from the fact that LAT1 is an antiporter;  
564 phenylalanine does not only compete for LAT1 at the blood side but also serves as a counter  
565 metabolite at the brain side as seen in the increased rates of tyrosine and tryptophan transport  
566 to the brain with an increase of phenylalanine (Figure S10). The inverse effect was not  
567 observed: when tryptophan or tyrosine were increased separately in the model, their negative  
568 effect through competition for LAT1 dominated the uptake of phenylalanine (Figure 5B).

569 What do these results mean for a clinical application of the LNAA diet? To answer this  
570 question, we must emphasise that we did not simulate the altered diets used in the PKU mice  
571 per se, but rather the impact of altered blood concentrations of amino acids on the brain in the  
572 PKU mice. For a more complete insight into the impact of diets, we should also include  
573 intestinal uptake and passage through the liver. Nevertheless, the model may help to pinpoint  
574 blood amino acids that are important to monitor and optimise in LNAA treatment.

575 Our present modelling confirmed that the clinical importance of reduction of blood  
576 phenylalanine is not only to avoid direct phenylalanine toxicity in the brain but also - albeit to  
577 an unknown degree of importance - to reduce the inhibition of tyrosine and tryptophan  
578 hydroxylases by cerebral phenylalanine. Furthermore, we gave a theoretical underpinning of  
579 the LNAA diet: even though each individual amino acid had a small effect on brain  
580 phenylalanine, together they had a strong impact. On the other hand, some discrepancies have  
581 been identified between our previous experimental data and the current modelling. These  
582 discrepancies reveal the gaps in our current understanding of the pathophysiological  
583 mechanisms underlying brain amino acid and neurotransmitter deficiencies in PKU. Our work  
584 suggests that future studies should focus on the mechanism through which the leucine plus  
585 isoleucine diet reduces brain phenylalanine, on brain compartmentation, and on the kinetic  
586 regulation of neurotransmitter biosynthesis. Increased future understanding of these  
587 mechanisms should aim to provide an even more solid advice on the optimal LNAA content  
588 for trials in PKU patients.

589 In conclusion, this first detailed, dynamic model of the LNAA transport and subsequent brain  
590 neurotransmitter metabolism gives a good, albeit qualitative, description of the impact of  
591 dietary treatment of PKU mice. In the future, it may be optimised towards the human patient  
592 situation. This can be readily done by changing the model parameters to be human-specific,  
593 since the biochemical architecture of the network is thought to be the comparable between mice  
594 and man [65]. Moreover, its generic nature makes it applicable to other diseases in which the

595 balance of amino acids and neurotransmitters is affected, such as Alzheimer's [40] or  
596 Parkinson's Disease [41], depression [38], and autism [39].

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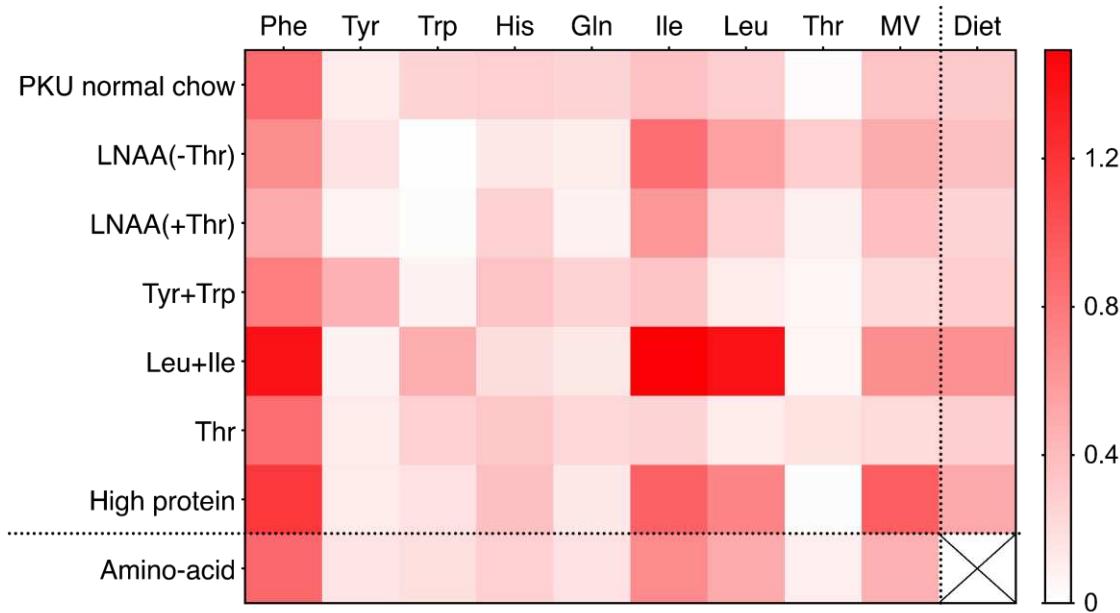
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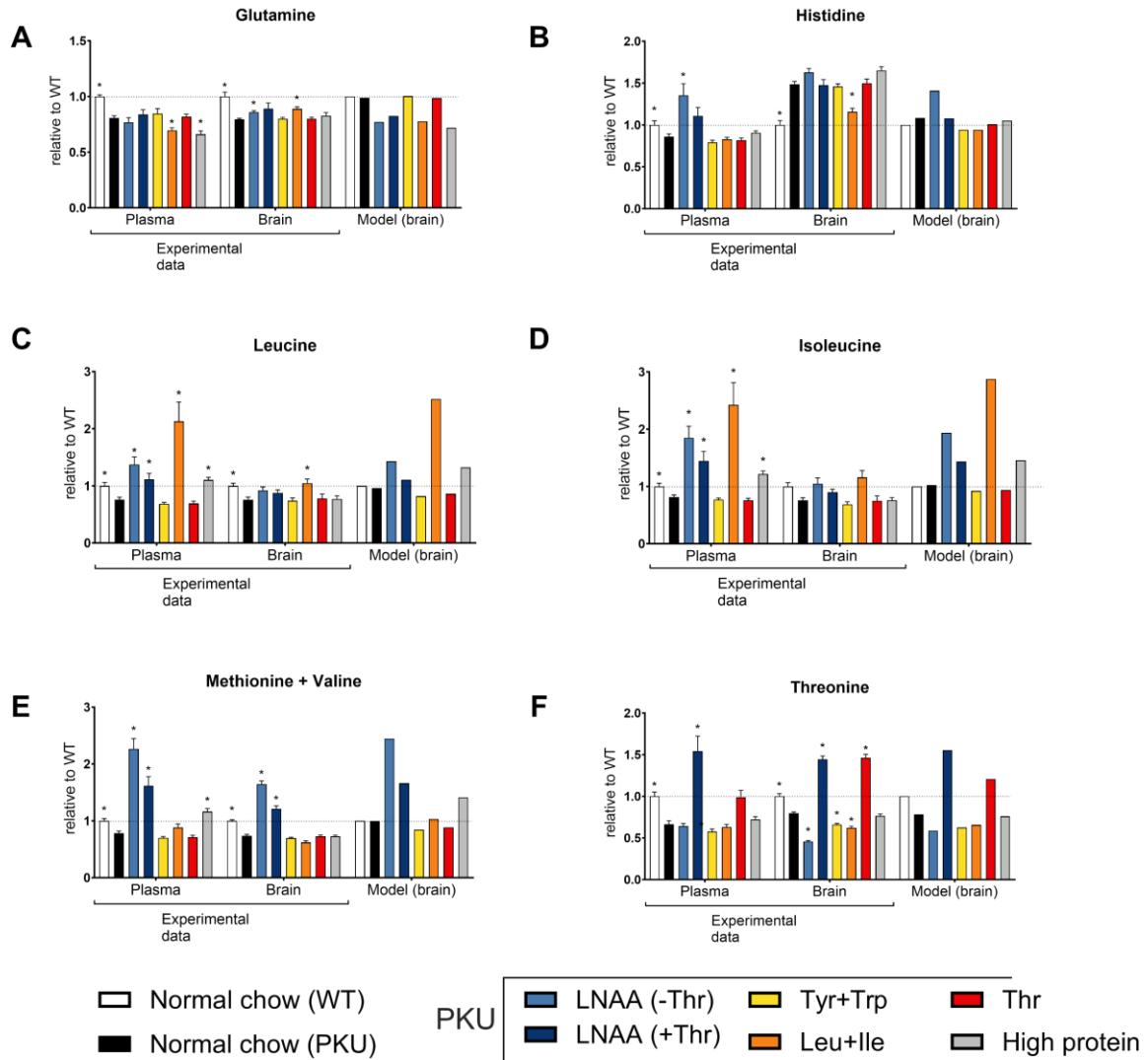
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812 SUPPLEMENTARY INFORMATION



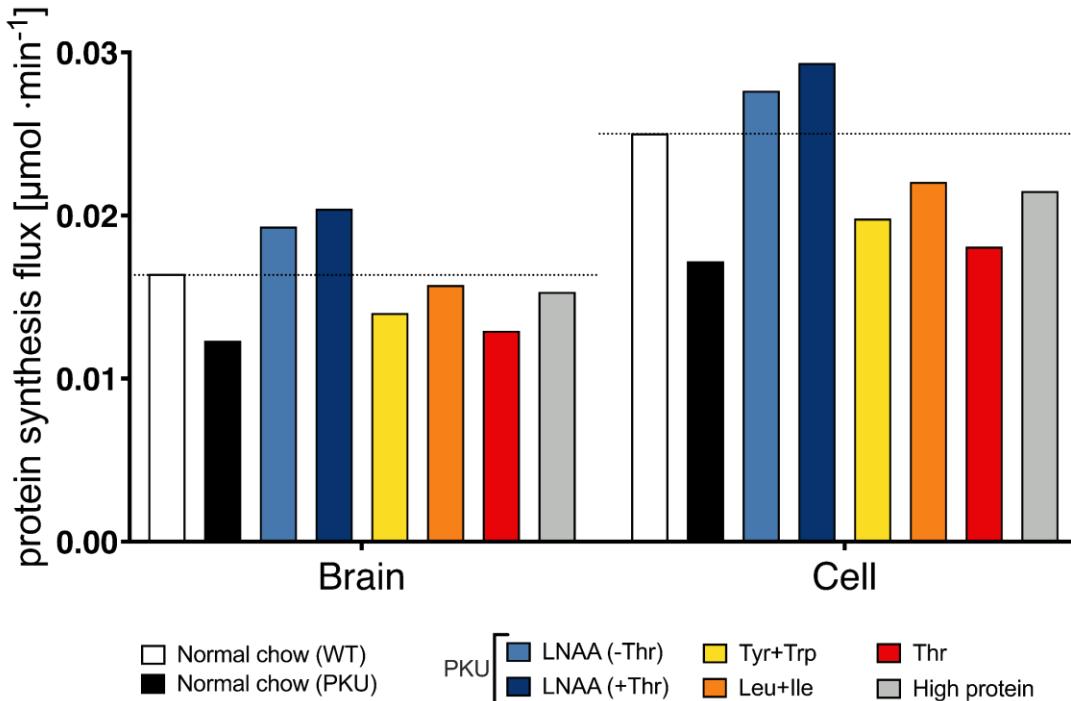
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814 **Figure S1. A detailed comparison between model prediction and experimental data.**  
815 Heatmap shows normalised difference scores between the model prediction for a specific amino acid  
816 value relative to WT, and its experimental value relative to WT, for each diet.  
817  $\text{Normalised difference score}_{n,m} = (|\text{norm. simulation}_{n,m} - \text{norm. data}_{n,m}|) \cdot \text{norm. data}_{n,m}^{-1}$ , where n  
818 = specific amino acid, m = specific diet. If normalised difference score = 0 data and simulation are identical.

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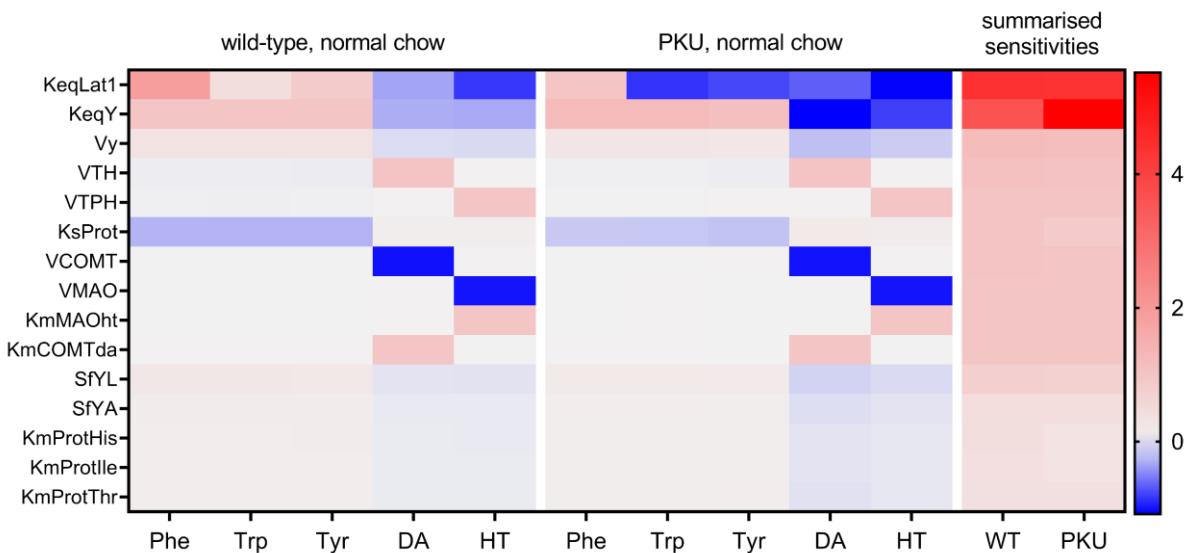
**Figure S2. Comparison between experimental data and model predictions for changes in other amino acid levels after the dietary intervention.** For the experimental data, each bar represents a mean (ns = 16) with a standard error of the mean.



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825 **Figure S3. Comparison between the protein synthesis flux in the model in response to different**  
826 **diets.**

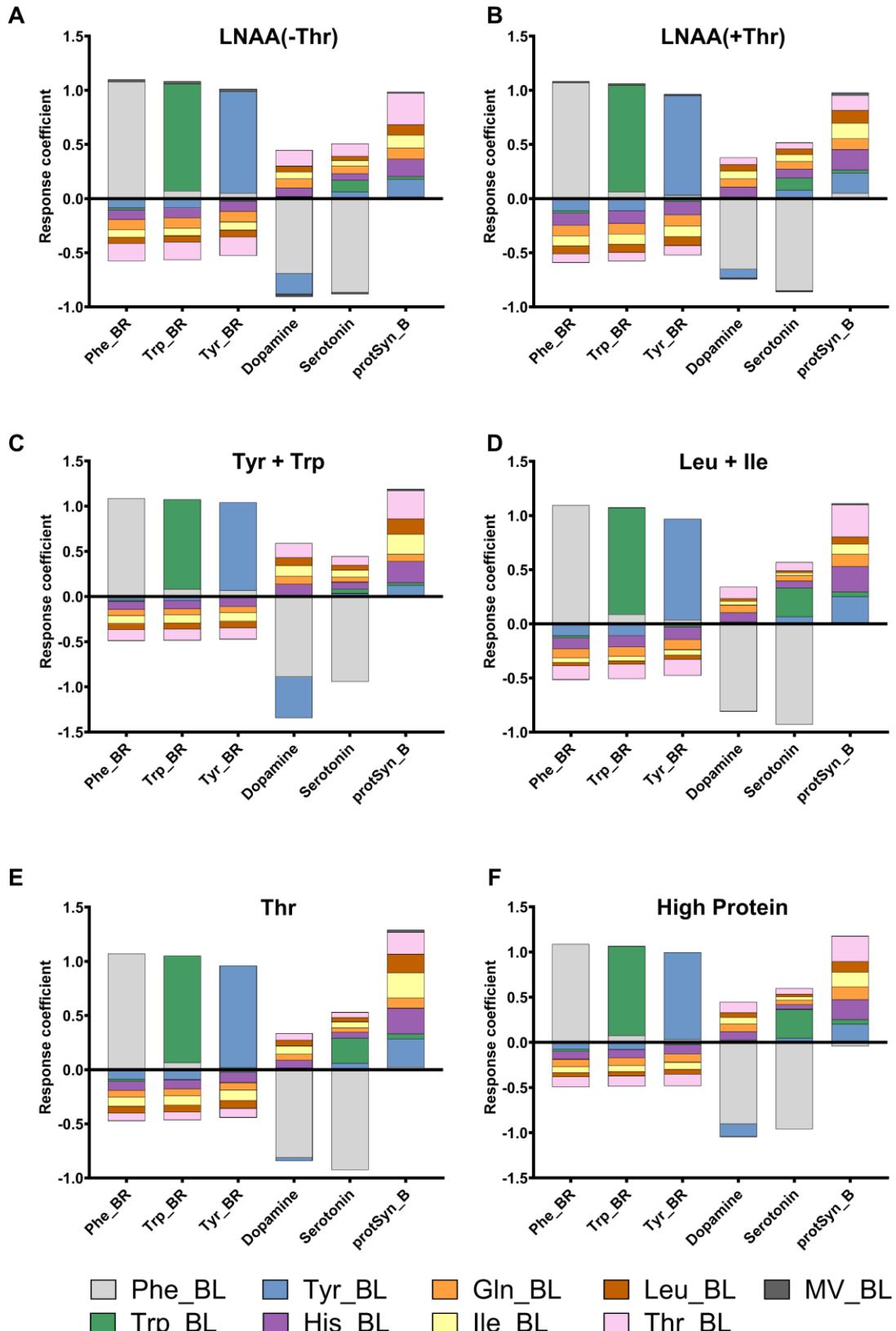
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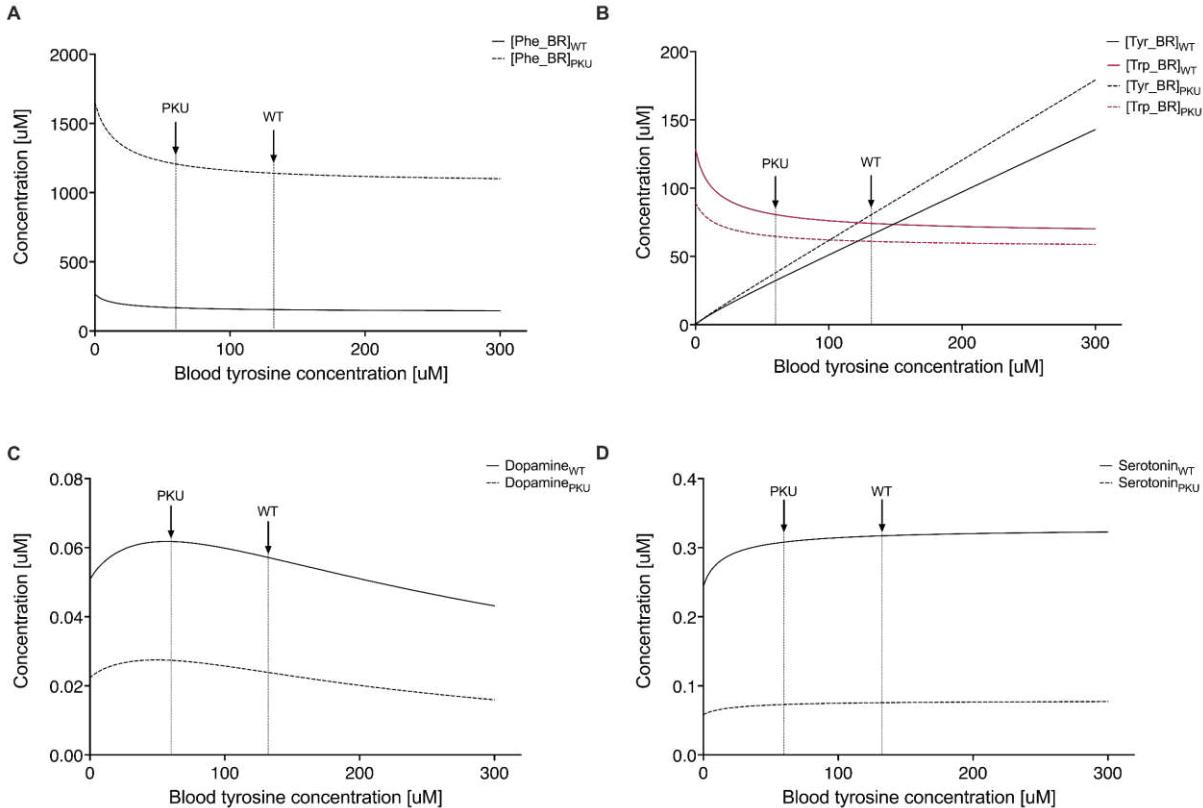
829 **Figure S4. Sensitivities of the brain amino acids to the changes in the model parameters.** Top 15  
830 parameters with the most control over the amino acids and neurotransmitters concentrations in WT mice  
831 are shown.

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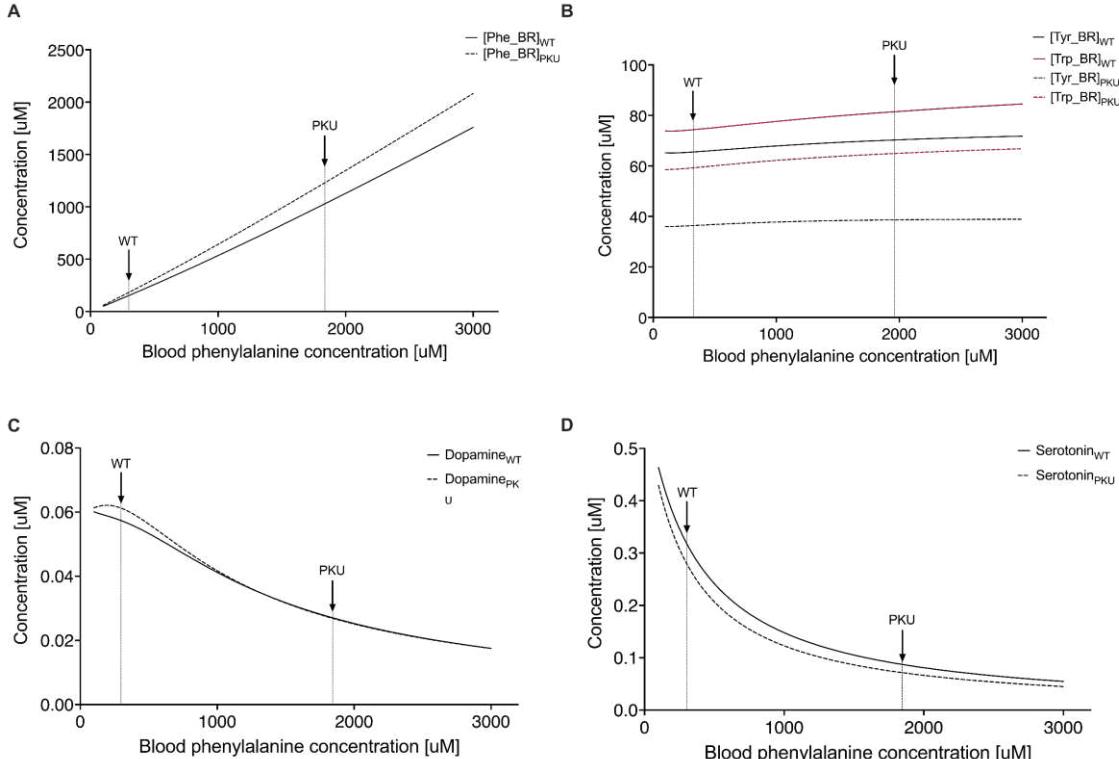
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834 **Figure S5. Brain levels of phenylalanine, tryptophan, and tyrosine are susceptible to the changes**  
835 **in the corresponding blood levels of these amino acids in other diets.** Bars represent positive and  
836 negative response coefficients of brain Phe, Tyr, Trp, as well as dopamine, serotonin, and protein  
837 synthesis in the brain (protSyn\_B), to the changes in the blood amino acid concentrations. Each graph  
838 represents response coefficients calculated based on different dietary conditions as starting points.



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840 **Figure S6. Changes to the amino acid and neurotransmitters concentrations in response to the**  
 841 **increasing concentration of tyrosine in the brain.** All other amino acid concentrations were fixed at  
 842 the levels measured in WT or untreated PKU mice, respectively. The arrows indicate the blood  
 843 concentrations of tyrosine and tryptophan in WT and PKU mice.

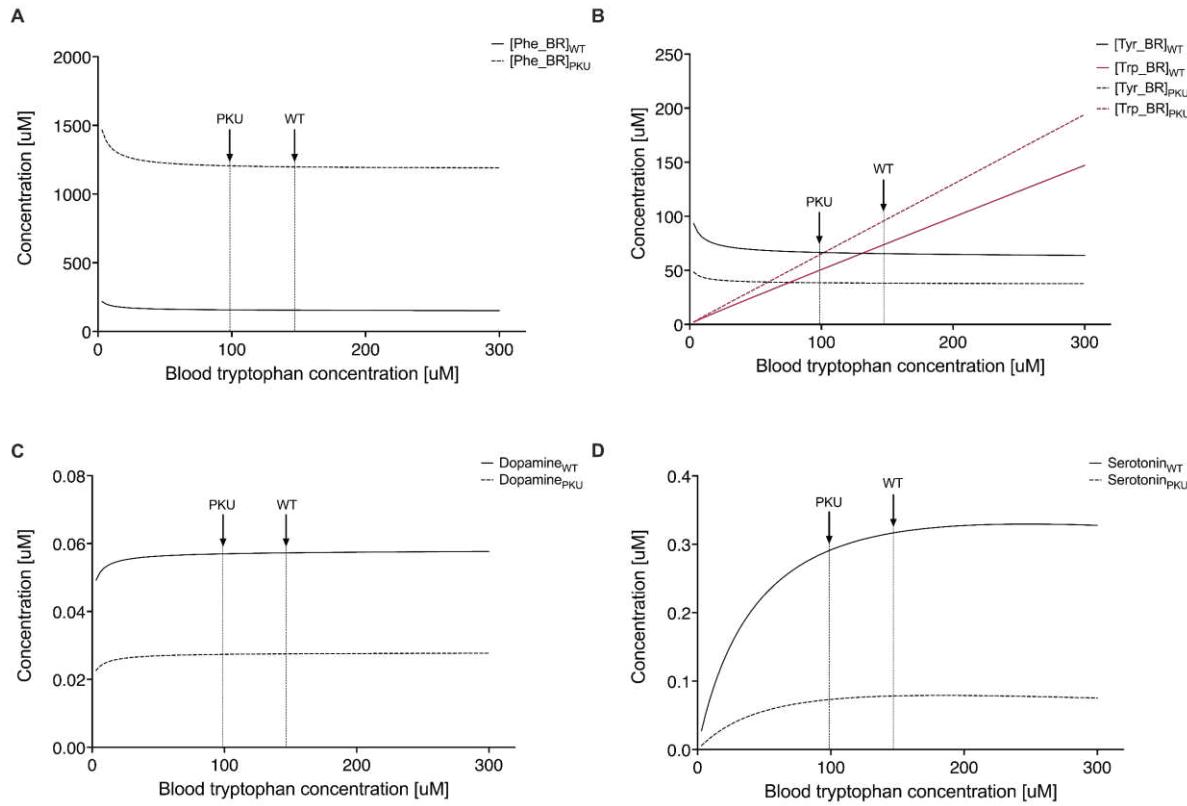


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845 **Figure S7. Changes to the amino acid and neurotransmitters concentrations in response to the**  
 846 **increasing concentration of phenylalanine in the brain.** All other amino acid concentrations were

847 fixed at the levels measured in WT or PKU mice, respectively. The arrows indicate the blood  
848 concentrations of tyrosine and tryptophan in WT and PKU mice.

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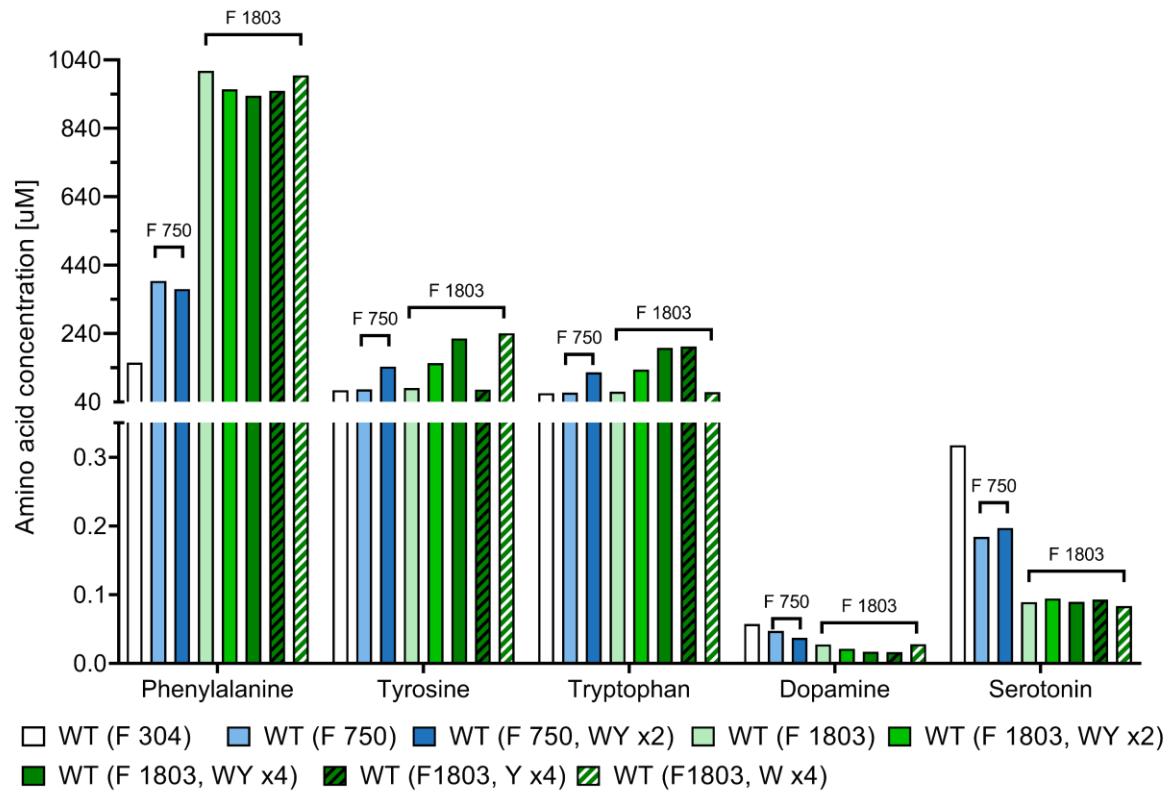


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851 **Figure S8. Changes to the amino acid and neurotransmitters concentrations in response to the**  
852 **increasing concentration of tryptophan in the brain.** All other amino acid concentrations were fixed  
853 at the levels measured in WT or PKU mice, respectively. The arrows indicate the blood concentrations  
854 of tyrosine and tryptophan in WT and PKU mice.

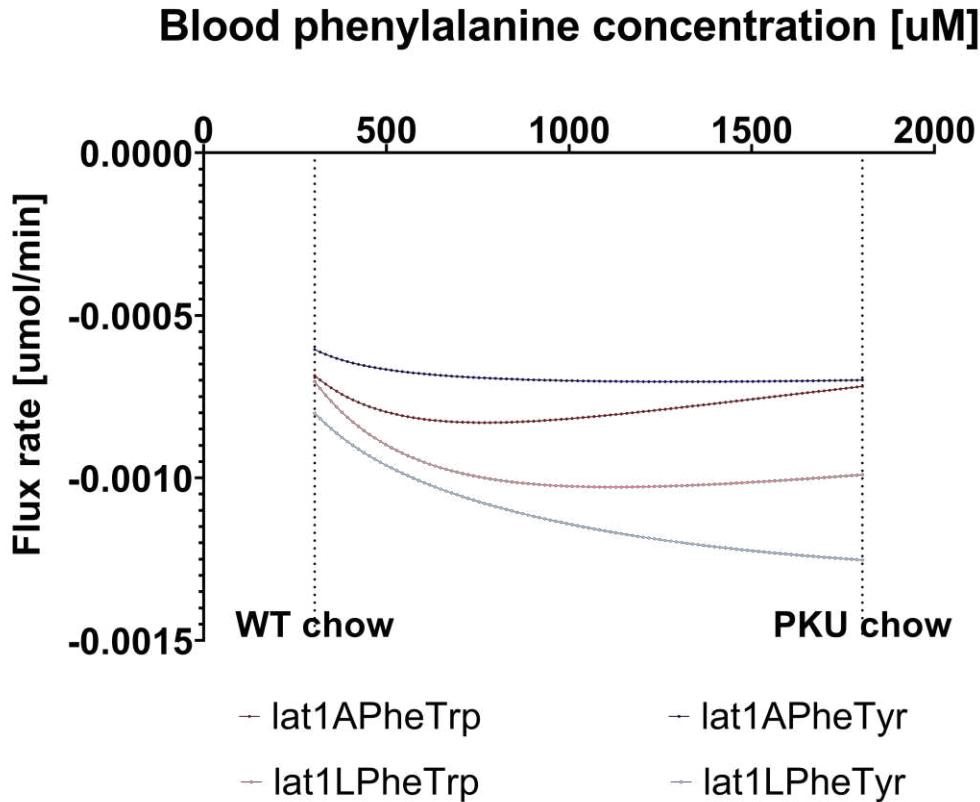
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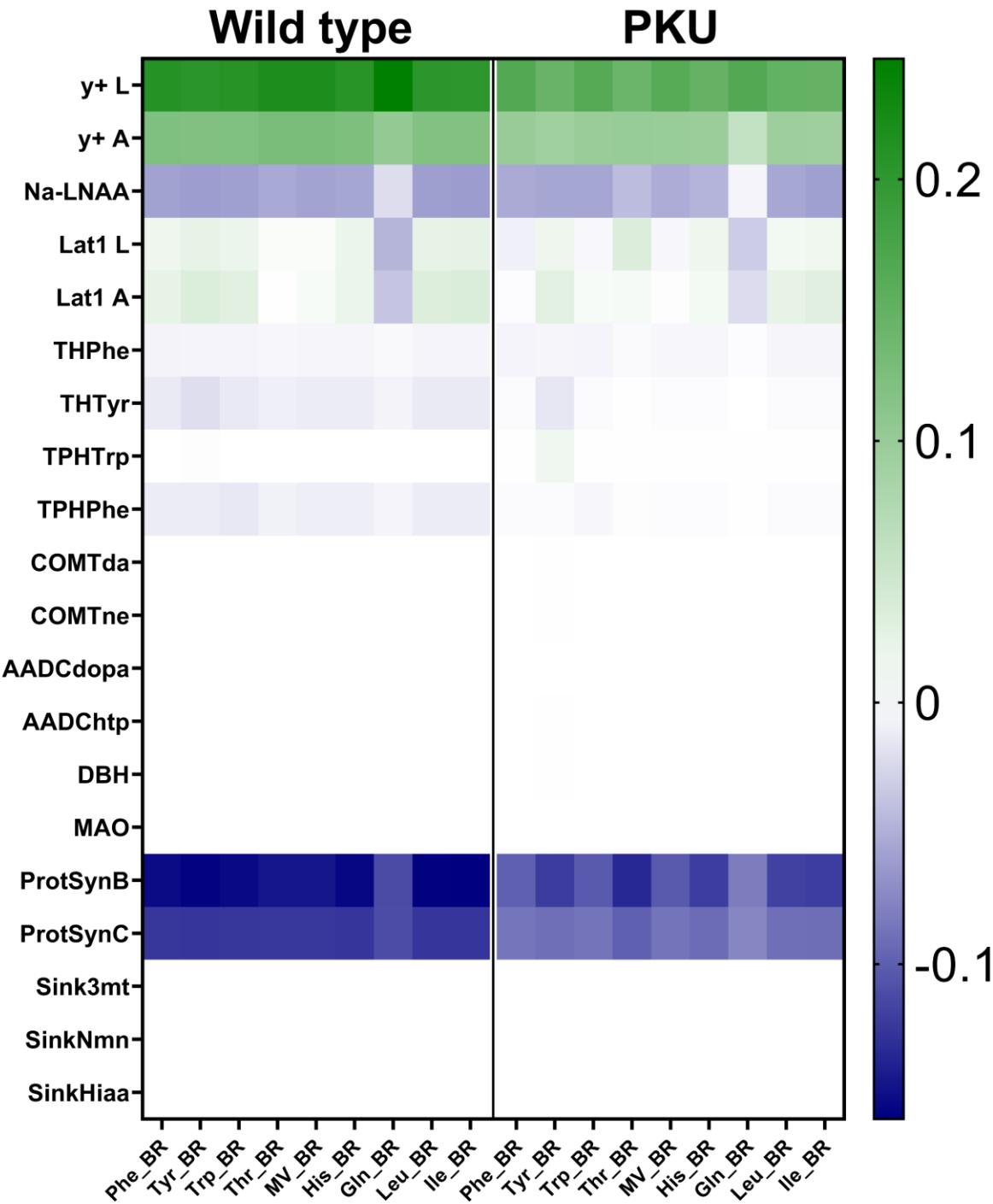
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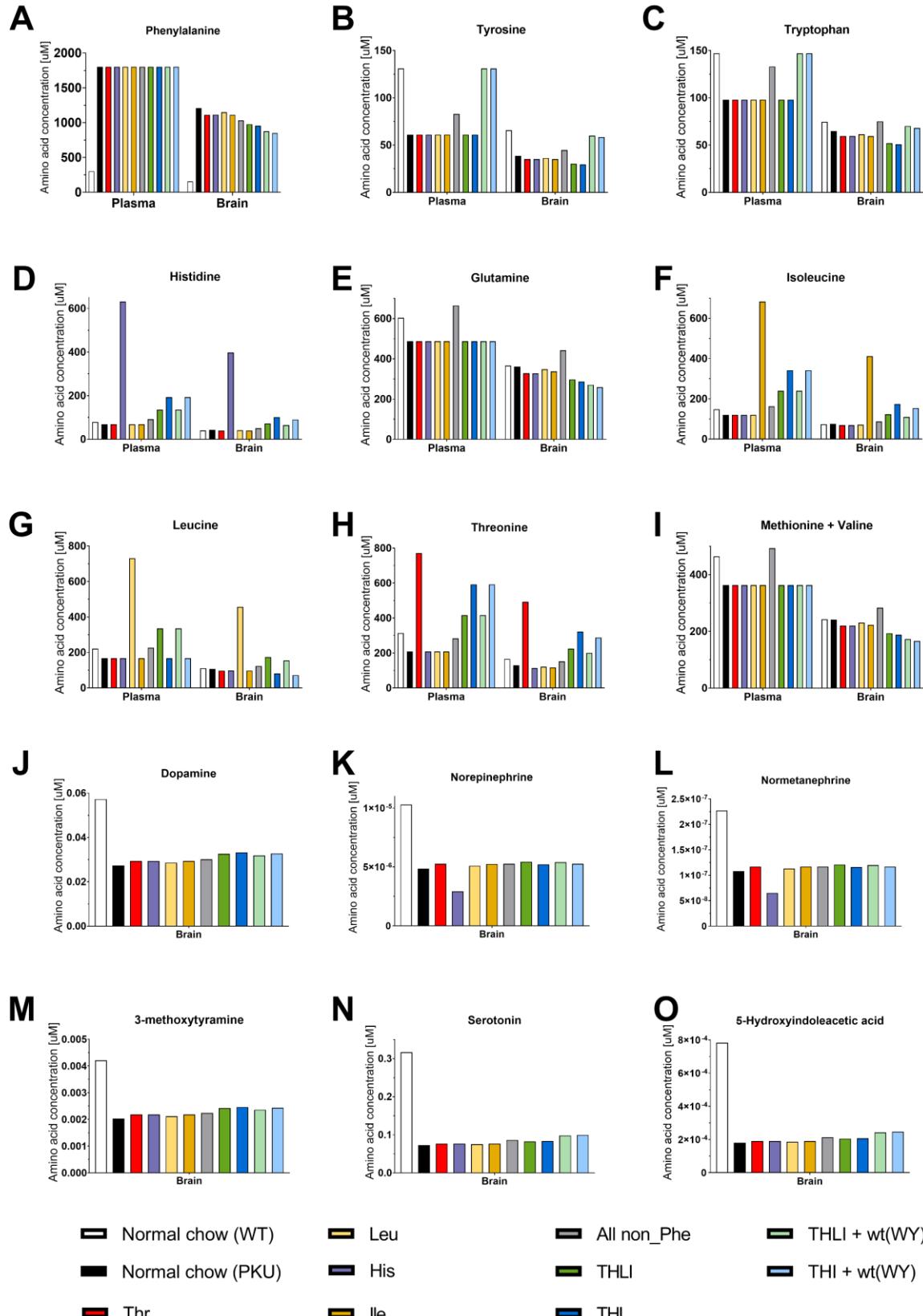
**Figure S9. Changes to the amino acid and neurotransmitters concentrations in response to phenylalanine (F) increase and addition of tyrosine (Y) and tryptophan (W) in the WT background.**



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**Figure S10. Flux rates of LAT1 exchange between phenylalanine and tryptophan and tyrosine at increasing blood phenylalanine concentrations in WT background.**





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**Figure S12. Changes to the amino acid concentrations in response to changes in the plasma amino acid composition.** All non\_Phe – non-Phe LNAA; THLI – threonine, histidine, leucine, isoleucine; THI -threonine, histidine, isoleucine; THLI + wt(WY) – THLI with wild type levels of tyrosine and tryptophan; THI + wt(WY) – THI with wild type levels of tyrosine and tryptophan

## Text S4.1. Model description

### 1 Glossary

**Table S1. Glossary of all abbreviations used in the text**

Abbreviation	Full name
3-Mt, Mt	3-methoxytyramine
5-Hiaa, Hiaa	5-Hydroxyindoleacetic acid
5-Htp, Htp	5-Hydroxytryptophan
AA	Amino acid
AADC	Aromatic L-amino acid decarboxylase
COMT	Catechol-O-methyltransferase
Da	Dopamine
DBH	Dopamine beta-hydroxylase
F, Phe	Phenylalanine
H, His	Histidine
Ht	Serotonin
I, Ile	Isoleucine
$K_{eq}$	Equilibrium constant
$K_i$	Inhibitory (dissociation) constant
$K_{ic}$	Inhibitory (dissociation) constant, competitive inhibitor
$K_{inc}$	Inhibitory (dissociation) constant, non-competitive inhibitor
$K_{is}$	Inhibitory (dissociation) constant of a substrate
$K_m$	The Michaelis-Menten constant
L, Leu	Leucine
L-dopa	L-3,4-dihydroxyphenylalanine
LAT1	Large neutral amino acid transporter 1
LNAA- $Na^+$	$Na^+$ -dependent large neutral amino acid transporter
MAO	Monoamine oxidase
MV	Total pool of methionine and valine
Ne	Norepinephrine
Nmn	Normetanephrine
Q, Gln	Glutamine
sc	Stoichiometric coefficient
sf	Specificity factor
T, Thr	Threonine
TPH2	Tryptophan monooxygenase 2
TH	Tyrosine 3-monooxygenase
$v$	Net rate of the reaction
$V$	Maximum velocity of an enzyme
W, Trp	Tryptophan
Y, Tyr	Tyrosine
$y^+$	Cationic amino acid transporter, $y^+$ system

### 2 Kinetic rate equations

In our model, the majority of enzymes catalyze the conversion of multiple substrates (see Fig.1). However, each enzyme is characterized by its unique rate equation, with variable, substrate-specific(indicated by the subscript), rats  $v$ . Furthermore, LAT1 and  $y^+$  transporters are present on both sides of the blood-brain barrier at different concentrations. To address this, we use L for the luminal side ('blood') and A for the abluminal side ('brain') in the rate equations. In the abbreviations CELL indicates metabolites in the endothelial cell compartment (blood-brain barrier), BR indicates brain concentrations, and BL indicates blood concentrations. Additionally, the abbreviation AA is used for a general amino acid, and MV for a combined pool of methionine (Met, M) and valine (Val, V) to simplify the equation nomenclature. Most of the equations used in the model are of (ir)reversible Michaelis-Menten type. Exceptions to this rule are the rate equations for the transporter LAT1,

and two hydroxylases: TH and TPH2.

The model for LAT1 transporter follows the ping-pong bi-bi kinetics. It is known, that for each amino acid, LAT1 transporter displays different maximum velocities (specificity factor  $s f_{AA}$ ). Therefore a mean of  $s f$  factors was used for each exchange reaction. Additionally, LAT1 is known to have 2 x higher abundance on the luminal side  $s f_{latL}$  of the blood-brain-barrier than on the abluminal side  $s f_{latA}$ , which was reflected in the rate equation. Tyrosine and tryptophan hydroxylases are known to follow non-reversible Michaelis-Menten kinetics with substrate [1] and product inhibition.

The unit for the rates in the model description is  $\mu\text{mol} \cdot \text{min}^{-1} \cdot \text{mouse}^{-1}$ . The rate equations for the sink reactions, and consumption of the end products 3-Mt, Nmn, and 5-Hiaa, were constructed so that the sink reactions do not control the flux.

$$v_{lat1L(AA1)(AA2)} = \frac{V_{LAT1} \cdot s f_{latL} \cdot \frac{s f_{AA1} + s f_{AA2}}{2} \cdot \left( \frac{AA1_{BL}[t] \cdot AA2_{CELL}[t]}{Km_{AA1} \cdot Km_{AA2}} - \frac{AA1_{CELL}[t] \cdot AA2_{BL}[t]}{Km_{AA1} \cdot Km_{AA2} \cdot K_{eq}} \right)}{\text{subUnit1} \cdot \text{subUnit2}}$$

where:

$$AA \rightarrow Phe, Tyr, Trp, His, Ile, Leu, Thr, Gln, MV \quad (1)$$

$$\text{subUnit1} = 1 + \frac{AA1_{BL}[t]}{Km_{AA1}} + \frac{AA2_{BL}[t]}{Km_{AA2}} + \frac{AA3_{BL}[t]}{Km_{AA3}} + \frac{AA4_{BL}[t]}{Km_{AA4}} + \frac{AA5_{BL}[t]}{Km_{AA5}} + \frac{AA6_{BL}[t]}{Km_{AA6}} + \frac{AA7_{BL}[t]}{Km_{AA7}} + \frac{AA8_{BL}[t]}{Km_{AA8}} + \frac{AA9_{BL}[t]}{Km_{AA9}}$$

$$\text{subUnit2} = 1 + \frac{AA1_{CELL}[t]}{Km_{AA1}} + \frac{AA2_{CELL}[t]}{Km_{AA2}} + \frac{AA3_{CELL}[t]}{Km_{AA3}} + \frac{AA4_{CELL}[t]}{Km_{AA4}} + \frac{AA5_{CELL}[t]}{Km_{AA5}} + \frac{AA6_{CELL}[t]}{Km_{AA6}} + \frac{AA7_{CELL}[t]}{Km_{AA7}} + \frac{AA8_{CELL}[t]}{Km_{AA8}} + \frac{AA9_{CELL}[t]}{Km_{AA9}}$$

$$v_{lat1A(AA1)(AA2)} = \frac{V_{LAT1} \cdot s f_{latA} \cdot \frac{s f_{AA1} + s f_{AA2}}{2} \cdot \left( \frac{AA1_{CELL}[t] \cdot AA2_{BR}[t]}{Km_{AA1} \cdot Km_{AA2}} - \frac{AA1_{BR}[t] \cdot AA2_{CELL}[t]}{Km_{AA1} \cdot Km_{AA2} \cdot K_{eq}} \right)}{\text{subUnit1} \cdot \text{subUnit2}}$$

where:

$$AA \rightarrow Phe, Tyr, Trp, His, Ile, Leu, Thr, Gln, MV \quad (2)$$

$$\text{subUnit1} = 1 + \frac{AA1_{CELL}[t]}{Km_{AA1}} + \frac{AA2_{CELL}[t]}{Km_{AA2}} + \frac{AA3_{CELL}[t]}{Km_{AA3}} + \frac{AA4_{CELL}[t]}{Km_{AA4}} + \frac{AA5_{CELL}[t]}{Km_{AA5}} + \frac{AA6_{CELL}[t]}{Km_{AA6}} + \frac{AA7_{CELL}[t]}{Km_{AA7}} + \frac{AA8_{CELL}[t]}{Km_{AA8}} + \frac{AA9_{CELL}[t]}{Km_{AA9}}$$

$$\text{subUnit2} = 1 + \frac{AA1_{BR}[t]}{Km_{AA1}} + \frac{AA2_{BR}[t]}{Km_{AA2}} + \frac{AA3_{BR}[t]}{Km_{AA3}} + \frac{AA4_{BR}[t]}{Km_{AA4}} + \frac{AA5_{BR}[t]}{Km_{AA5}} + \frac{AA6_{BR}[t]}{Km_{AA6}} + \frac{AA7_{BR}[t]}{Km_{AA7}} + \frac{AA8_{BR}[t]}{Km_{AA8}} + \frac{AA9_{BR}[t]}{Km_{AA9}}$$

$$v_{yL(AA1)} = \frac{V_y \cdot s f_{yL} \cdot \left( \frac{AA1_{BL}}{Km_{AA1}} - \frac{AA1_{CELL}}{Km_{AA1} \cdot K_{eq}} \right)}{\left( 1 + \frac{AA2_{BL} + AA2_{CELL}}{Km_{AA1}} + \frac{AA1_{BL} + AA1_{CELL}}{Km_{AA2}} + \frac{AA3_{BL} + AA3_{CELL}}{Km_{AA3}} + \frac{AA4_{BL} + AA4_{CELL}}{Km_{AA4}} + \frac{AA5_{BL} + AA5_{CELL}}{Km_{AA5}} \right)} \quad (3)$$

where:

$$AA \rightarrow Phe, His, Thr, Gln, MV$$

$$K_{eq} = 1$$

$$v_{yA(AA1)} = \frac{V_y \cdot s f_{yA} \cdot \left( \frac{AA1_{CELL}}{Km_{AA1}} - \frac{AA1_{BR}}{Km_{AA1} \cdot K_{eq}} \right)}{\left( 1 + \frac{AA2_{CELL} + AA2_{BR}}{Km_{AA1}} + \frac{AA1_{CELL} + AA1_{BR}}{Km_{AA2}} + \frac{AA3_{CELL} + AA3_{BR}}{Km_{AA3}} + \frac{AA4_{CELL} + AA4_{BR}}{Km_{AA4}} + \frac{AA5_{CELL} + AA5_{BR}}{Km_{AA5}} \right)} \quad (4)$$

where:

$$AA \rightarrow Phe, His, Thr, Gln, MV$$

$$K_{eq} = 1$$

$$v_{lnaa(AA1)} = \frac{V_{lnaa} \cdot \frac{AA1_{BR}[t]}{Km_{AA1}}}{1 + \frac{AA1_{BR}[t]}{Km_{AA1}} + \frac{AA2_{BR}[t]}{Km_{AA2}} + \frac{AA3_{BR}[t]}{Km_{AA3}} + \frac{AA4_{BR}[t]}{Km_{AA4}} + \frac{AA5_{BR}[t]}{Km_{AA5}} + \frac{AA6_{BR}[t]}{Km_{AA6}} + \frac{AA7_{BR}[t]}{Km_{AA7}} + \frac{AA8_{BR}[t]}{Km_{AA8}}} \quad (5)$$

where:

$$AA \rightarrow Phe, Tyr, Trp, His, Ile, Leu, Gln, MV$$

$$v_{TH(Tyr)} = \frac{V_{TH} \cdot \frac{\text{Tyr}_{BR}[t]}{Km_{Tyr}}}{Den}$$

where:

(6)

$$Den = 1 + \frac{\text{Phe}_{BR}[t]}{Km_{Phe}} + \frac{\text{Ne}_{BR}[t]}{Km_{Ne}} + \frac{\text{lDopa}_{BR}[t]}{Km_{lDopa}} + \frac{\text{Da}_{BR}[t]}{Km_{Da}} + \text{Tyr}_{BR} \cdot \frac{1 + \frac{\text{Phe}_{BR}[t]}{Km_{Phe}}}{Km_{Tyr}}$$

$$+ \text{Tyr}_{BR}[t]^2 \cdot \frac{1 + \frac{\text{Phe}_{BR}[t]}{Km_{Phe}} + \frac{\text{Ne}_{BR}[t]}{Km_{Ne}} + \frac{\text{lDopa}_{BR}[t]}{Km_{lDopa}} + \frac{\text{Da}_{BR}[t]}{Km_{Da}}}{Km_{Tyr} \cdot Kis_{Tyr}}$$

$$v_{TH(Phe)} = \frac{V_{TH} \cdot \frac{\text{Phe}_{BR}[t]}{Km_{Phe}}}{Den}$$

where:

(7)

$$Den = 1 + \frac{\text{Tyr}_{BR}[t]}{Km_{Tyr}} + \frac{\text{Ne}_{BR}[t]}{Km_{Ne}} + \frac{\text{lDopa}_{BR}[t]}{Km_{lDopa}} + \frac{\text{Da}_{BR}[t]}{Km_{Da}} + \text{Phe}_{BR} \cdot \frac{1 + \frac{\text{Phe}_{BR}[t]}{Km_{Phe}}}{Km_{Phe}}$$

$$+ \text{Phe}_{BR}[t]^2 \cdot \frac{1 + \frac{\text{Tyr}_{BR}[t]}{Km_{Tyr}} + \frac{\text{Ne}_{BR}[t]}{Km_{Ne}} + \frac{\text{lDopa}_{BR}[t]}{Km_{lDopa}} + \frac{\text{Da}_{BR}[t]}{Km_{Da}}}{Km_{Phe} \cdot Kis_{Phe}}$$

$$v_{TPH(Trp)} = \frac{V_{TPH} \cdot \frac{\text{Trp}_{BR}[t]}{Km_{Trp}}}{Den}$$

where:

(8)

$$Den = 1 + \frac{\text{Phe}_{BR}[t]}{Km_{Phe}} + \frac{\text{Htp}_{BR}[t]}{Km_{Htp}} + \frac{\text{lDopa}_{BR}[t]}{Km_{lDopa}} + \frac{\text{Da}_{BR}[t]}{Km_{Da}} + \text{Trp}_{BR} \cdot \frac{1 + \frac{\text{Phe}_{BR}[t]}{Km_{Phe}}}{Km_{Trp}}$$

$$+ \text{Trp}_{BR}[t]^2 \cdot \frac{1 + \frac{\text{Phe}_{BR}[t]}{Km_{Phe}} + \frac{\text{Htp}_{BR}[t]}{Km_{Htp}} + \frac{\text{lDopa}_{BR}[t]}{Km_{lDopa}} + \frac{\text{Da}_{BR}[t]}{Km_{Da}}}{Km_{Trp} \cdot Kis_{Trp}}$$

$$v_{TPH(Phe)} = \frac{V_{TPH} \cdot \frac{\text{Phe}_{BR}[t]}{Km_{Phe}}}{Den}$$

where:

(9)

$$Den = 1 + \frac{\text{Trp}_{BR}[t]}{Km_{Trp}} + \frac{\text{Htp}_{BR}[t]}{Km_{Htp}} + \frac{\text{lDopa}_{BR}[t]}{Km_{lDopa}} + \frac{\text{Da}_{BR}[t]}{Km_{Da}} + \text{Phe}_{BR} \cdot \frac{1 + \frac{\text{Phe}_{BR}[t]}{Km_{Phe}}}{Km_{Phe}}$$

$$+ \text{Phe}_{BR}[t]^2 \cdot \frac{1 + \frac{\text{Trp}_{BR}[t]}{Km_{Trp}} + \frac{\text{Htp}_{BR}[t]}{Km_{Htp}} + \frac{\text{lDopa}_{BR}[t]}{Km_{lDopa}} + \frac{\text{Da}_{BR}[t]}{Km_{Da}}}{Km_{Phe} \cdot Kis_{Phe}}$$

$$v_{AADC(s)} (s \rightarrow lDopa | Htp) = \frac{V_{AADC} \cdot s f_s \cdot \frac{S1[t]}{Km_{S1}}}{1 + \frac{S1[t]}{Km_{S1}} + \frac{S2[t]}{Km_{S2}}}$$

(10)

$$v_{COMT(s)} (s \rightarrow Da | Ne) = \frac{V_{COMT} \cdot \frac{S1[t]}{Km_{S1}}}{1 + \frac{S1[t]}{Km_{S1}} + \frac{S2[t]}{Km_{S2}}}$$

(11)

$$v_{DBH} = \frac{V_{DBH} \cdot \frac{\text{Da}[t]}{Km_{Da}}}{1 + \frac{\text{Da}_{BR}[t]}{Km_{Da}} + \frac{\text{Ne}_{BR}[t]}{Km_{Ne}} + \frac{\text{His}_{BR}[t]}{Km_{His}}}$$

(12)

$$v_{MAO} = \frac{V_{MAO} \cdot \frac{\text{Ht}[t]}{Km_{Ht}}}{1 + \frac{\text{Ht}[t]}{Km_{Ht}}}$$

(13)

$$sink_S (S \rightarrow 3-Mt, Nmn, 5-Hiaa) = Ks_S \cdot \frac{S[t]}{Km_S} \quad (14)$$

$$protSynB = Ks_{prot} \cdot \frac{\frac{AA1_{BR}}{AA1_{BR} + Km_{AA1}} \cdot \frac{AA2_{BR}}{AA2_{BR} + Km_{AA2}} \cdot \frac{AA3_{BR}}{AA3_{BR} + Km_{AA3}} \cdot \frac{AA4_{BR}}{AA4_{BR} + Km_{AA4}}}{\frac{AA5_{BR}}{AA5_{BR} + Km_{AA5}} \cdot \frac{AA6_{BR}}{AA6_{BR} + Km_{AA6}} \cdot \frac{AA7_{BR}}{AA7_{BR} + Km_{AA7}} \cdot \frac{AA8_{BR}}{AA8_{BR} + Km_{AA8}}} \cdot \frac{AA9_{BR}}{AA9_{BR} + Km_{AA9}} \quad (15)$$

where:

AA → Phe, Tyr, Trp, His, Ile, Leu, Thr, Gln, MV

$$protSynC = Ks_{prot} \cdot \frac{\frac{AA1_{CELL}}{AA1_{CELL} + Km_{AA1}} \cdot \frac{AA2_{CELL}}{AA2_{CELL} + Km_{AA2}} \cdot \frac{AA3_{CELL}}{AA3_{v} + Km_{AA3}} \cdot \frac{AA4_{CELL}}{AA4_{CELL} + Km_{AA4}}}{\frac{AA5_{CELL}}{AA5_{CELL} + Km_{AA5}} \cdot \frac{AA6_{CELL}}{AA6_{v} + Km_{AA6}} \cdot \frac{AA7_{CELL}}{AA7_{CELL} + Km_{AA7}} \cdot \frac{AA8_{CELL}}{AA8_{CELL} + Km_{AA8}}} \cdot \frac{AA9_{CELL}}{AA9_{CELL} + Km_{AA9}} \quad (16)$$

where:

AA → Phe, Tyr, Trp, His, Ile, Leu, Thr, Gln, MV

### 3 Ordinary differential equations

Based on the reaction scheme in Figure 1, a set of 26 ordinary differential equations was created. As seen in Fig.1, many enzymes/transporters have broad substrate specificity, and many substrates can be converted by different enzymes/transporters. Furthermore, some transporters are localized in two different membranes, luminal (L) and abluminal(A). For instance,  $v_{lat1LPheTyr}$  is the net rate of the luminal (L) transport of the Phe (phenylalanine) from the blood to the cell compartment, in exchange for the Tyr (tyrosine) which is transported by the LAT1 transporter in the opposite direction. In the abbreviations CELL indicates endothelial cell metabolite pool (blood-brain barrier), BR indicates total brain metabolite pool.

$$\frac{dPheCELL \cdot V_{CELL}}{dt} = v_{lat1LPheTyr} + v_{lat1LPheTrp} + v_{lat1LPheHis} + v_{lat1LPheGln} + v_{lat1LPheIle} + v_{lat1LPheLeu} + v_{lat1LPheThr} + v_{lat1LPheMV} + v_{lnaaPhe} + v_{yLPhe} - v_{lat1APheTyr} - v_{lat1APheTrp} - v_{lat1APheHis} - v_{lat1APheGln} - v_{lat1APheIle} - v_{lat1APheLeu} - v_{lat1APheThr} - v_{lat1APheMV} - v_{yAPhe} - sCPhe \cdot v_{ProtSynC} \quad (17)$$

$$\frac{dTyrCELL \cdot V_{CELL}}{dt} = v_{lat1APheTyr} + v_{lat1LTyrTrp} + v_{lat1LTyrHis} + v_{lat1LTyrGln} + v_{lat1LTyrIle} + v_{lat1LTyrLeu} + v_{lat1LTyrThr} + v_{lat1LTyrMV} + v_{lnaaTyr} - v_{lat1LPheTyr} - v_{lat1ATyrTrp} - v_{lat1ATyrHis} - v_{lat1ATyrGln} - v_{lat1ATyrIle} - v_{lat1ATyrLeu} - v_{lat1ATyrThr} - v_{lat1ATyrMV} - sCTyr \cdot v_{ProtSynC} \quad (18)$$

$$\frac{dTrpCELL \cdot V_{CELL}}{dt} = v_{lat1LTTrpHis} + v_{lat1LTTrpGln} + v_{lat1LTTrpIle} + v_{lat1LTTrpLeu} + v_{lat1LTTrpThr} + v_{lat1LTTrpMV} + v_{lat1APheTrp} + v_{lat1ATyrTrp} + v_{lnaaTrp} - v_{lat1LPheTrp} - v_{lat1LTTrpTrp} - v_{lat1ATTrpHis} - v_{lat1ATTrpGln} - v_{lat1ATTrpIle} - v_{lat1ATTrpLeu} - v_{lat1ATTrpThr} - v_{lat1ATTrpMV} - sCTrp \cdot v_{ProtSynC} \quad (19)$$

$$\begin{aligned} \frac{d\text{HisCELL} \cdot V_{\text{CELL}}}{dt} = & v_{lat1LHisGln} + v_{lat1LHisIle} + v_{lat1LHisLeu} + v_{lat1LHisThr} + v_{lat1LHisMV} \\ & + v_{lat1APheHis} + v_{lat1ATyrHis} + v_{lat1ATrpHis} + v_{lnaaHis} + v_{yLHis} \\ & - v_{lat1LPheHis} - v_{lat1LTyrHis} - v_{lat1LTrpHis} - v_{lat1AHisGln} - v_{lat1AHisIle} \\ & - v_{lat1AHisLeu} - v_{lat1AHisThr} - v_{lat1AHisMV} - v_{yAHis} - s_{CHis} \cdot v_{ProtSynC} \end{aligned} \quad (20)$$

$$\begin{aligned} \frac{d\text{IleCELL} \cdot V_{\text{CELL}}}{dt} = & v_{lat1LIleLeu} + v_{lat1LIleThr} + v_{lat1LIleMV} + v_{lat1APheIle} + v_{lat1ATyrIle} \\ & + v_{lat1ATrpIle} + v_{lat1AHisIle} + v_{lat1AGlnIle} + v_{lnaaIle} - v_{lat1LPheIle} \\ & - v_{lat1LTyrIle} - v_{lat1LTrpIle} - v_{lat1LHisIle} - v_{lat1LGlnIle} - v_{lat1AIleLeu} \\ & - v_{lat1AIleThr} - v_{lat1AIleMV} - s_{CIle} \cdot v_{ProtSynC} \end{aligned} \quad (21)$$

$$\begin{aligned} \frac{d\text{LeuCELL} \cdot V_{\text{CELL}}}{dt} = & v_{lat1LLeuThr} + v_{lat1LLeuMV} + v_{lat1APheLeu} + v_{lat1ATyrLeu} + v_{lat1ATrpLeu} \\ & + v_{lat1AHisLeu} + v_{lat1AGlnLeu} + v_{lat1AIleLeu} + v_{lnaaLeu} - v_{lat1LPheLeu} \\ & - v_{lat1LTyrLeu} - v_{lat1LTrpLeu} - v_{lat1LHisLeu} - v_{lat1LGlnLeu} - v_{lat1LIleLeu} \\ & - v_{lat1ALeuThr} - v_{lat1ALeuMV} - s_{CLeu} \cdot v_{ProtSynC} \end{aligned} \quad (22)$$

$$\begin{aligned} \frac{d\text{ThrCELL} \cdot V_{\text{CELL}}}{dt} = & v_{lat1LThrMV} + v_{lat1APheThr} + v_{lat1ATyrThr} + v_{lat1ATrpThr} + v_{lat1AHisThr} \\ & + v_{lat1AGlnThr} + v_{lat1AIleThr} + v_{lat1ALeuThr} + v_{lnaaThr} + v_{yLThr} \\ & - v_{lat1LPheThr} - v_{lat1LTyrThr} - v_{lat1LTrpThr} - v_{lat1LHisThr} - v_{lat1LGlnThr} \\ & - v_{lat1LIleThr} - v_{lat1LLeuThr} - v_{lat1AThrMV} - v_{yATHr} - s_{CThr} \cdot v_{ProtSynC} \end{aligned} \quad (23)$$

$$\begin{aligned} \frac{d\text{GlnCELL} \cdot V_{\text{CELL}}}{dt} = & v_{lat1LGlnIle} + v_{lat1LGlnLeu} + v_{lat1LGlnThr} + v_{lat1LGlnMV} + v_{lat1APheGln} \\ & + v_{lat1ATyrGln} + v_{lat1ATrpGln} + v_{lat1AHisGln} + v_{yLGln} \\ & - v_{lat1LPheGln} - v_{lat1LTyrGln} - v_{lat1LTrpGln} - v_{lat1LHisGln} - v_{lat1AGlnIle} \\ & - v_{lat1AGlnLeu} - v_{lat1AGlnThr} - v_{lat1AGlnMV} - v_{yAGln} - s_{CGln} \cdot v_{ProtSynC} \end{aligned} \quad (24)$$

$$\begin{aligned} \frac{d\text{MVCELL} \cdot V_{\text{CELL}}}{dt} = & v_{lat1APheMV} + v_{lat1ATyrMV} + v_{lat1ATrpMV} + v_{lat1AHisMV} + v_{lat1AGlnMV} \\ & + v_{lat1AIleMV} + v_{lat1ALeuMV} + v_{lat1AThrMV} + v_{lnaaMV} + v_{yLMV} \\ & - v_{lat1LPheMV} - v_{lat1LTyrMV} - v_{lat1LTrpMV} - v_{lat1LHisMV} - v_{lat1LGlnMV} \\ & - v_{lat1LIleMV} - v_{lat1LLeuMV} - v_{lat1LThrMV} - v_{yAMV} - s_{CMV} \cdot v_{ProtSynC} \end{aligned} \quad (25)$$

$$\begin{aligned} \frac{d\text{PheBR} \cdot V_{\text{BR}}}{dt} = & v_{lat1APheTyr} + v_{lat1APheTrp} + v_{lat1APheHis} + v_{lat1APheGln} + v_{lat1APheIle} \\ & + v_{lat1APheLeu} + v_{lat1APheThr} + v_{lat1APheMV} + v_{yAPhe} - v_{lnaaPhe} \\ & - v_{THPhe} - v_{TPHPhe} - s_{CPhe} \cdot v_{ProtSynB} \end{aligned} \quad (26)$$

$$\begin{aligned} \frac{d\text{TyrBR} \cdot V_{\text{BR}}}{dt} = & v_{lat1ATyrTrp} + v_{lat1ATyrHis} + v_{lat1ATyrGln} + v_{lat1ATyrIle} + v_{lat1ATyrLeu} \\ & + v_{lat1ATyrThr} + v_{lat1ATyrMV} + v_{TPHPhe} - v_{lat1APheTyr} \\ & - v_{lnaaTyr} - v_{THTyr} - s_{CTyr} \cdot v_{ProtSyn} \end{aligned} \quad (27)$$

$$\begin{aligned} \frac{d\text{TrpBR} \cdot V_{\text{BR}}}{dt} = & v_{lat1ATrpHis} + v_{lat1ATrpGln} + v_{lat1ATrpIle} + v_{lat1ATrpLeu} + v_{lat1ATrpThr} \\ & + v_{lat1ATrpMV} - v_{lat1APheTrp} - v_{lat1ATyrTrp} - v_{lnaaTrp} - v_{TPHTrp} \\ & - s_{CTrp} \cdot v_{ProtSyn} \end{aligned} \quad (28)$$

$$\begin{aligned} \frac{d\text{HisBR} \cdot V_{\text{BR}}}{dt} = & v_{\text{lat1AHisGln}} + v_{\text{lat1AHisIle}} + v_{\text{lat1AHisLeu}} + v_{\text{lat1AHisThr}} + v_{\text{lat1AHisMV}} \\ & + v_{\text{yAHis}} - v_{\text{lat1APheHis}} - v_{\text{lat1ATyrHis}} - v_{\text{lat1ATrpHis}} - v_{\text{lnaaHis}} \\ & - \text{SCHis} \cdot v_{\text{ProtSyn}} \end{aligned} \quad (29)$$

$$\begin{aligned} \frac{d\text{IleBR} \cdot V_{\text{BR}}}{dt} = & v_{\text{lat1AIleLeu}} + v_{\text{lat1AIleThr}} + v_{\text{lat1AIleMV}} - v_{\text{lat1APheIle}} - v_{\text{lat1ATyrIle}} \\ & - v_{\text{lat1ATrpIle}} - v_{\text{lat1AHisIle}} - v_{\text{lat1AGlnIle}} - v_{\text{lnaaIle}} \\ & - \text{SCIle} \cdot v_{\text{ProtSyn}} \end{aligned} \quad (30)$$

$$\begin{aligned} \frac{d\text{LeuBR} \cdot V_{\text{BR}}}{dt} = & v_{\text{lat1ALeuThr}} + v_{\text{lat1ALeuMV}} - v_{\text{lat1APheLeu}} - v_{\text{lat1ATyrLeu}} - v_{\text{lat1ATrpLeu}} \\ & - v_{\text{lat1AHisLeu}} - v_{\text{lat1AGlnLeu}} - v_{\text{lat1AIleLeu}} - v_{\text{lnaaLeu}} \\ & - \text{SCLeu} \cdot v_{\text{ProtSyn}} \end{aligned} \quad (31)$$

$$\begin{aligned} \frac{d\text{ThrBR} \cdot V_{\text{BRAIN}}}{dt} = & v_{\text{lat1AThrMV}} + v_{\text{yAThr}} - v_{\text{lat1APheThr}} - v_{\text{lat1ATyrThr}} - v_{\text{lat1ATrpThr}} \\ & - v_{\text{lat1AHisThr}} - v_{\text{lat1AGlnThr}} - v_{\text{lat1AIleThr}} - v_{\text{lat1ALeuThr}} - v_{\text{lnaaThr}} \\ & - \text{CThr} \cdot v_{\text{ProtSyn}} \end{aligned} \quad (32)$$

$$\begin{aligned} \frac{d\text{GlnBR} \cdot V_{\text{BR}}}{dt} = & v_{\text{lat1AGlnIle}} + v_{\text{lat1AGlnLeu}} + v_{\text{lat1AGlnThr}} + v_{\text{lat1AGlnMV}} + v_{\text{yAGln}} \\ & - v_{\text{lat1APheGln}} - v_{\text{lat1ATyrGln}} - v_{\text{lat1ATrpGln}} - v_{\text{lat1AHisGln}} \\ & - \text{CGln} \cdot v_{\text{ProtSyn}} \end{aligned} \quad (33)$$

$$\begin{aligned} \frac{d\text{MVBR} \cdot V_{\text{BR}}}{dt} = & v_{\text{yAMV}} - v_{\text{lat1APheMV}} - v_{\text{lat1ATyrMV}} - v_{\text{lat1ATrpMV}} - v_{\text{lat1AHisMV}} \\ & - v_{\text{lat1AGlnMV}} - v_{\text{lat1AIleMV}} - v_{\text{lat1ALeuMV}} - v_{\text{lat1AThrMV}} - v_{\text{lnaaMV}} \\ & - \text{CMV} \cdot v_{\text{ProtSyn}} \end{aligned} \quad (34)$$

$$\frac{d\text{Htp} \cdot V_{\text{BR}}}{dt} = v_{\text{TPHTrp}} - v_{\text{AADChtp}} \quad (35)$$

$$\frac{d\text{Ht} \cdot V_{\text{BR}}}{dt} = v_{\text{AADChtp}} - v_{\text{MAO}} \quad (36)$$

$$\frac{d\text{Hiaa} \cdot V_{\text{BR}}}{dt} = v_{\text{MAO}} - \text{sinkHiaa} \quad (37)$$

$$\frac{d\text{Dopa} \cdot V_{\text{BR}}}{dt} = v_{\text{THTyr}} + v_{\text{THPhe}} - v_{\text{AADCdopa}} \quad (38)$$

$$\frac{d\text{Da} \cdot V_{\text{BR}}}{dt} = v_{\text{AADCdopa}} - v_{\text{DBH}} - v_{\text{COMTda}} \quad (39)$$

$$\frac{d\text{Mt} \cdot V_{\text{BR}}}{dt} = v_{\text{COMTda}} - \text{sink3Mt} \quad (40)$$

$$\frac{d\text{Ne} \cdot V_{\text{BR}}}{dt} = v_{\text{DBH}} - v_{\text{COMTne}} \quad (41)$$

$$\frac{d\text{Nmn} \cdot V_{\text{BR}}}{dt} = v_{\text{COMTne}} - \text{sinkNmn} \quad (42)$$

## 4 Simulations of diets - model validation

Parameters used in the model are summarized in Table S2. For the  $y+$  and LAT1 transporters, the equilibrium constants were assumed to be 1, as these are not driven by any external Gibbs-energy input. All maximum enzyme velocities from the literature were normalized to the total brain protein content ( $47.5 \text{ mg prot} \cdot \text{brain}^{-1}$ ), taking into account different expression levels of each enzyme in the brain where needed. To this end, we calculated weighted means of transcript levels for each enzyme based on the differential expression levels in the mouse brain and then normalized them to LAT1 (see Table S3).

**Table S2. Kinetic parameters.**

Parameter	Value	Reference
<b>LAT1 transporter</b>		
$V_{LAT1}$	1.9665	$\mu\text{mol} \cdot \text{min}^{-1} \cdot \text{mouse}^{-1}$
$sf_{Phe}$	1	[2]
$sf_{Tyr}$	2.341	[2]
$sf_{Trp}$	0.854	[2]
$sf_{His}$	1.488	[2]
$sf_{Gln}$	1.049	[2]
$sf_{Ile}$	1.463	[2]
$sf_{Leu}$	1.439	[2]
$sf_{Thr}$	0.415	[2]
$sf_{MV}$	1.042	[2]
$sf_{LatL}$	2	2x higher expression on the luminal site [3]
$sf_{LatA}$	1	
$K_{eq}$	1	
$Km_{Phe}$	11	$\mu\text{M}$
$Km_{Tyr}$	64	$\mu\text{M}$
$Km_{Trp}$	15	$\mu\text{M}$
$Km_{His}$	100	$\mu\text{M}$
$Km_{Gln}$	880	$\mu\text{M}$
$Km_{Ile}$	56	$\mu\text{M}$
$Km_{Leu}$	29	$\mu\text{M}$
$Km_{Thr}$	220	$\mu\text{M}$
$Km_{MV}$	165.59	$\mu\text{M}$
weighted average for methionine and valine [2] (based on their abundance in the brain in WT mice)		
<b><math>y+</math> transporter</b>		
$V_y$	0.1045	$\mu\text{mol} \cdot \text{min}^{-1} \cdot \text{mouse}^{-1}$
$sf_{yL}$	1	
$sf_{yA}$	2	2x higher expression on the abluminal site [3]
$K_{eq}$	1	
$Km_{Phe}$	590	$\mu\text{M}$
$Km_{His}$	630	$\mu\text{M}$
$Km_{Gln}$	620	$\mu\text{M}$
$Km_{Thr}$	670	$\mu\text{M}$
$Km_{MV}$	687	$\mu\text{M}$
<b>LNAA-<math>\text{Na}^+</math> transporter</b>		
$V_{LNAA}$	0.005415	$\mu\text{mol} \cdot \text{min}^{-1} \cdot \text{mouse}^{-1}$
$Km_{Leu}$	21	$\mu\text{M}$
$Km_{Phe}$	26.11	$\mu\text{M}$
$Km_{Tyr}$	25.87	$\mu\text{M}$
$Km_{Trp}$	24.33	$\mu\text{M}$
$Km_{His}$	30.57	$\mu\text{M}$
$Km_{Ile}$	21.32	$\mu\text{M}$
rough estimates based on the reported changes in the apparent Vmax due to the substrate competition [5]		

**Table S2. Kinetic parameters (continued).**

Parameter	Value	Reference
$Km_{Thr}$	30.91	$\mu\text{M}$
$Km_{MV}$	27.00	$\mu\text{M}$
<b>TH</b>		
$V_{TH}$	0.001425	$\mu\text{mol} \cdot \text{min}^{-1} \cdot \text{mouse}^{-1}$
		original value: $30 \text{ pmol} \cdot \text{min}^{-1} \cdot \text{mg prot}^{-1}$ , rat midbrain slices [6]
$Km_{Tyr}$	17	$\mu\text{M}$
$Kis_{Tyr}$	227	$\mu\text{M}$
$Km_{Phe}$	103	$\mu\text{M}$
$Kinc_{Phe}$	736	$\mu\text{M}$
$Kis_{Phe}$	1375.3529	$\mu\text{M}$
		unknown, value based on the $Km_{Tyr}/Kis_{Tyr}$ ratio from [1]
$Kis_{Ne}$	280	$\mu\text{M}$
$Kis_{Da}$	600	$\mu\text{M}$
$Kis_{lDopa}$	56	$\mu\text{M}$
<b>TPH2</b>		
$V_{TPH}$	0.00115	$\mu\text{mol} \cdot \text{min}^{-1} \cdot \text{mouse}^{-1}$
		original value: $0.0242 \text{ nmol} \cdot \text{min}^{-1} \cdot \text{mg prot}^{-1}$ , rat brain extract [9]
$Km_{Trp}$	13.2	$\mu\text{M}$
$Kis_{Trp}$	1030	$\mu\text{M}$
$Km_{Phe}$	72.7	$\mu\text{M}$
$Kinc_{Phe}$	257	$\mu\text{M}$
$Kis_{Phe}$	5672.8030	$\mu\text{M}$
		unknown, value based on the $Km_{Trp}/Kis_{Trp}$ ratio from [1]
$Kis_{Htp}$	35	$\mu\text{M}$
$Kis_{Da}$	94	$\mu\text{M}$
$Kis_{lDopa}$	17	$\mu\text{M}$
<b>AADC</b>		
$V_{AADC}$	0.2831	$\mu\text{mol} \cdot \text{min}^{-1} \cdot \text{mouse}^{-1}$
		original value: $5.96 \text{ nmol} \cdot \text{min}^{-1} \cdot \text{mg prot}^{-1}$ , human [12]
$Sf_{lDopa}$	1	$\mu\text{M}$
$Sf_{Htp}$	0.0435	$\mu\text{M}$
$Km_{lDopa}$	70	$\mu\text{M}$
$Km_{Htp}$	47	$\mu\text{M}$
<b>DBH</b>		
$V_{DBH}$	0.8102	$\mu\text{mol} \cdot \text{min}^{-1} \cdot \text{mouse}^{-1}$
		original value: $1500 \text{ nmol} \cdot \text{min}^{-1} \cdot \text{mg prot}^{-1}$ , Rat, purified protein [16], normalized to LAT1
$Keq$	$1 \cdot 10^6$	$\mu\text{M}$
		arbitrary number, the reaction is virtually irreversible, however, the product does slightly inhibit the enzyme
$Km_{Da}$	200	$\mu\text{M}$
$Km_{Ne}$	5000	$\mu\text{M}$
$Ki_{His}$	410	$\mu\text{M}$
<b>MAO</b>		
$V_{MAO}$	0.1501	$\mu\text{mol} \cdot \text{min}^{-1} \cdot \text{mouse}^{-1}$
		original value: $3.16 \text{ nmol} \cdot \text{min}^{-1} \cdot \text{mg prot}^{-1}$ , Rat, cell lysates, at $100 \mu\text{M}$ serotonin [19]
$Km_{Ht}$	99	$\mu\text{M}$
<b>COMT</b>		
$V_{COMT}$	0.0494	$\mu\text{mol} \cdot \text{min}^{-1} \cdot \text{mouse}^{-1}$
		original value: $1.04 \text{ nmol} \cdot \text{min}^{-1} \cdot \text{mg prot}^{-1}$ , rat liver extract [21]
$Km_{Da}$	3.3	$\mu\text{M}$
$Km_{Ne}$	5.28	$\mu\text{M}$
		human [22]
		human, based on the ratio of $Km_{Ne}/Km_{Da}$ in recombinant Sf9 cells, and $Km_{Da}$ in human brain [22]

**Table S2. Kinetic parameters (continued).**

Parameter	Value	Reference
<b>protSyn</b>		
$V_{protSyn}$	0.265	$\mu\text{mol} \cdot \text{min}^{-1} \cdot \text{mouse}^{-1}$
$Km_{Phe}$	2.6	$\mu\text{M}$
$Km_{Tyr}$	34	$\mu\text{M}$
$Km_{Trp}$	7.4	$\mu\text{M}$
$Km_{His}$	30	$\mu\text{M}$
$Km_{Gln}$	114	$\mu\text{M}$
$Km_{Ile}$	52	$\mu\text{M}$
$Km_{Leu}$	45.6	$\mu\text{M}$
$Km_{Thr}$	110	$\mu\text{M}$
$Km_{MV}$	7.87877	$\mu\text{M}$
$sc_{Phe}$	0.039	
$sc_{Tyr}$	0.029	
$sc_{Trp}$	0.012	
$sc_{His}$	0.026	
$sc_{Gln}$	0.046	
$sc_{Ile}$	0.045	
$sc_{Leu}$	0.105	
$sc_{Thr}$	0.055	
$sc_{MV}$	0.053	
<b>Sinks</b>		
$Ks_{Hiaa}$	30	$\mu\text{mol} \cdot \text{min}^{-1} \cdot \text{mouse}^{-1}$
$Km_{Hiaa}$	49	$\mu\text{M}$
$Ks_{3-Mt}$	10	$\mu\text{mol} \cdot \text{min}^{-1} \cdot \text{mouse}^{-1}$
$Km_{3-Mt}$	50	$\mu\text{M}$
$Ks_{Nmn}$	20	$\mu\text{mol} \cdot \text{min}^{-1} \cdot \text{mouse}^{-1}$
$Km_{Nmn}$	48	$\mu\text{M}$
<b>Volumes</b>		
$V_{BL}$	0.00126	$1 \cdot \text{mouse}^{-1}$
$V_{CELL}$	$7.47 \cdot 10^{-6}$	$1 \cdot \text{mouse}^{-1}$
$V_{BR}$	0.004532	$1 \cdot \text{mouse}^{-1}$
		own data
		surface area of microvessels: $150 \text{cm}^2 \cdot \text{g tissue}^{-1}$ [35]; brain mass = 475 mg [own data]; average endothelial cell volume: $1009 \mu\text{m}^3$ [36]; average area of ecapillary endothelial cell: $962 \mu\text{m}^3$ [37]
		[38]
		arbitrary values estimated to not display any metabolic control over the system

**Table S3. Protein expression levels in the brain.**

Protein	A	B	C	D	E	F	G	H	I	J	Weight. mean	Rel. to LAT1
LAT1	19.50	22.58	23.45	33.86	17.60	18.05	21.34	27.94	13.80	29.33	24.89	1
TPH2	0.01	0.03	0.05	0.02	-	-	0.03	0.03	0.01	0.01	0.03	0.001
TH	-	-	-	-	-	-	-	6.43	-	32.30	0.48	0.019
AADC	-	-	-	-	-	-	-	0.91	-	2.67	0.05	0.002
DBH	-	-	-	1.2	-	-	-	-	-	-	0.28	0.011
MAO-A	11.68	10.57	9.52	3.19	19.96	9.68	7.94	13.29	11.66	12.18	9.91	0.398
COMT	13.35	11.93	10.78	11.82	13.27	13.06	13.39	12.60	12.97	14.98	12.02	0.483
LNAA	1.92	3.13	4.33	2.94	2.20	1.99	2.17	4.67	2.03	2.41	3.16	0.127
y+	4.85	8.76	9.81	9.64	4.45	3.73	6.69	8.64	4.03	6.28	8.34	0.335

A-Amygdala, B-Anterior cingulate cortex, C-Frontal cortex, D-Cortex, E-Caudate, F-Putamen, G-Hippocampus, H-Hypothalamus, I-Nucleus accumbens, J-Substantia nigra

The blood concentrations of amino acids were set, as fixed values, according to the measured values in mice (see Table S4). The initial concentrations (in  $\mu M$ ) for the variables were first assigned arbitrarily, and then a time-course simulation was performed to acquire a set of initial concentrations close to the steady-state values for WT diet. This newly acquired set of initial concentrations was then used for all the simulations.

**Table S4. Average amino-acid concentrations in the blood, as used in the model (in  $\mu M$ ).**

Amino-acid	WT	PKU	LNAA (-Thr)	LNAA (+Thr)	Tyr+Trp	Leu+Ile	Thr	High protein
<i>Phe</i>	304	1803	1387	1381	1886	1826	1848	2503
<i>Tyr</i>	131	61	119	96	172	61	59	86
<i>Trp</i>	147	98	172	177	168	104	105	89
<i>His</i>	79	68	107	87	63	66	65	72
<i>Gln</i>	604	487	464	507	511	420	494	399
<i>Ile</i>	148	120	273	213	114	358	112	180
<i>Leu</i>	221	167	303	246	151	470	153	243
<i>Thr</i>	314	208	202	484	182	198	311	227
<i>MV</i>	464	363	1052	752	325	410	330	539

WT - wild-type mice, standard chow; PKU - C57Bl/6 Pah-enu2 (PKU) mice, standard chow; LNAA(-Thr) - PKU mice, standard chow with LNAA(-Thr) supplementation; LNAA(+Thr) - PKU mice, standard chow with LNAA(+Thr) supplementation; Tyr+Trp - PKU mice, standard chow with Tyr and Trp supplementation; Leu+Ile - PKU mice, standard chow with Leu and Ile supplementation; Thr - PKU mice, standard chow with Thr supplementation; High protein - PKU mice, an isonitrogenic/isocaloric high-protein control diet

The simulation values represented in figures 2, 3, 4, 6, S2, S3, S9, and S12 were calculated as a weighted average of concentrations of amino acids in the BRAIN and CELL compartments as in the following equation:

$$AA_{total} = \frac{V_{CELL}}{V_{CELL} + V_{BR}} \cdot AA_{CELL} + \frac{V_{BR}}{V_{CELL} + V_{BR}} \cdot AA_{BR}$$

This approach reflects better the experimental data available, which does not distinguish between blood-brain-barrier and brain compartments.

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