The Utility of Ancestral and Derived Allele Sharing for Genome-Wide Inferences of Introgression

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Abstract

The past decade has ushered in a resurgence of studies highlighting the importance of introgression throughout the Tree of Life. Several methods exist for detecting and quantifying introgression on a genomic scale, yet the majority of these methods primarily utilize signals of derived allele sharing between donor and recipient populations. In this study, we exploit the fact that introgression will not only result in derived allele sharing but also the reintroduction of ancestral alleles to derive new estimators of the admixture proportion. Using coalescent simulations, we assess the performance of our new methods and the methods proposed in *Lopez Fang et al. 2022* to assess the utility of incorporating shared ancestral variation into genome-wide inferences of introgression. Using coalescent theory, simulations, and applying our methods to human and canid data, we find that methods incorporating ancestral allele sharing are comparable to their derived allele sharing counterparts, in turn providing researchers with the opportunity to utilize more of the genomic signature of introgression.

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1 Introduction

The field of evolutionary biology has seen a meteoric rise in the number of studies detecting 2 and quantifying instances of introgression—the integration of foreign genomic blocks into a species' genomic background—throughout the Eukaryotic Tree of Life (Dagilis et al., 2022) since the publishing of the draft Neanderthal genome in 2010 (Green et al., 2010). This is in large part due to the recent feasibility of next-generation sequencing technology, which has initiated a paradigm shift in how evolutionary biologists study introgression from comparing sequence similarity at some genetic markers between species to analyzing the whole genome via statistical methods—e.g., Patterson's D—to make inferences of introgression by using site patterns as a proxy for genealogical relationships (Dagilis et al., 2022; Durand et al., 2011; Edelman & Mallet, 2021; Green et al., 2010). Recent years have ushered in an influx of studies demonstrating that introgression is not only more 11 common than originally thought, but can also provide the raw genetic materials necessary for local adaptations (Hedrick, 2013; Huerta-Sánchez et al., 2014; Jagoda et al., 2022; Jones et al., 2018; Suarez-Gonzalez et al., 2018; Zhang et al., 2021), adaptive radiations (Malinsky et al., 2018; Meier et al., 2017; Pease et al., 2016; Richards & Martin, 2017; Stankowski & Streisfeld, 2015), and 15 speciation (Bierne et al., 2013; Nelson et al., 2021; Rheindt & Edwards, 2011). However, even with 16 keystone studies demonstrating that the evolutionary outcomes of introgression are diverse, it is challenging to assess its significance in evolution because the frequency of introgression across the 18 Tree of Life is still unclear (Dagilis et al., 2022; Edelman & Mallet, 2021). 19 The most popular statistical methods for making genome-wide inferences about introgression 20 exploit asymmetries in observed site patterns (Dagilis et al., 2022). Statistical tests for site pattern 21 asymmetries count the number of segregating sites that have a configuration of shared derived and 22 ancestral alleles which are informative of introgression in a set of taxa. One example of these tests 23 is Patterson's D (Equation 1), where two configurations of derived allele sharing site patterns are used to test for the presence of introgression (Durand et al., 2011; Green et al., 2010). Genome-wide 25 tests of introgression based on observed site patterns are relatively straight-forward to implement, 26 computationally efficient to calculate, and provide a unified approach for detecting and quantifying introgression across the Tree of Life as they can be applied to both phylogenetic and population genetic data sets. Due to the utility of site pattern-based metrics of introgression, recent years have 29 seen a rapid proliferation of site pattern-based statistics designed to detect and quantify genomewide levels of introgression (Durand et al., 2011; Hamlin et al., 2020; Lopez Fang et al., 2022;

Martin et al., 2014; Pease & Hahn, 2015; Pfeifer & Kapan, 2019). However, until recently existing 32 methods have strictly relied on the idea of derived allele sharing—where the donor and recipient 33 populations both harbor the same derived allele—which only captures a small portion of the total genomic signature produced by introgression (Lopez Fang et al., 2022). Notably, Lopez Fang et al. 35 2022 recently proposed the D+ statistic, which leverages both the sharing of derived and ancestral alleles between donor and recipient populations to detect genomic windows harboring introgressed 37 segments in the genome. 38 In this study we aim to assess if ancestral allele sharing site patterns are informative about 39 introgression on a broader genomic scale. We first propose novel metrics to quantify the proportion of introgression that utilize ancestral allele sharing site patterns. Using coalescent simulations we assessed the performance of our newly proposed metrics and the metrics to detect introgression 42 proposed by Lopez Fang et al. 2022. Lastly, we assessed the performance in empirical data by applying all the introgression metrics to publicly available human and canid data sets (1000 Genomes Project Consortium et al., 2015; Freedman et al., 2014). We find that in both simulated and empirical data, all introgression metrics perform comparably, allowing researchers the opportunity to use multiple lines of evidence across more segregating sites throughout the genome to make inferences about introgression.

9 2 New Approaches

In practice, most site pattern-based metrics of introgression assume a four-taxon tree—Newick format: (((P1, P2), P3), O); site pattern format: (P1's allelic state, P2's allelic state, P3's allelic state, O's allelic state)—where P1 and P2 represent potential recipients of introgression from the donor population P3, and O represents an outgroup used to polarize ancestral states, in which A denotes the ancestral allele and B denotes the derived allele. Thus, the ABBA site pattern indicates that the derived allele is shared between P2 and P3, while the BABA site pattern indicates that the derived allele is shared between P1 and P3. Patterson's D (Equation 1) specifically tests for patterns of derived allele sharing between donor and recipient populations and a significant excess of either aforementioned site pattern is suggestive of introgression (Durand et al., 2011; Green et al., 2010)

$$D(P1, P2, P3, O) = \frac{\sum_{i=1}^{n} C_{ABBA}(i) - C_{BABA}(i)}{\sum_{i=1}^{n} C_{ABBA}(i) + C_{BABA}(i)}$$
(1)

where $C_{ABBA}(i)$ and $C_{BABA}(i)$ are indicator variables that take a value of either zero or one conditioned on observing an ABBA or BABA site pattern at site i for all n sites where we have data for 61 all four samples (Durand et al., 2011; Green et al., 2010). Due to its computational efficiency and ability to discriminate between coalescent histories of incomplete lineage sorting (ILS)—the process where two lineages fail to coalesce in their most recent common ancestral population—and introgression, Patterson's D is the most widely used summary statistic to detect introgression (Dagilis et al., 2022). However, there is no theoretical or biological reason to believe that introgression will only result in the sharing of derived alleles. This is because introgressed genomic segments contain 67 both new derived alleles and re-introduced ancestral alleles. Using this logic, Lopez Fang et al. 2022 derived the expected branch lengths where a single mutation would generate a BAAA and ABAA site pattern respectively, which represents the ancestral allele sharing analogs to the ABBA and BABA site patterns. Notably, the authors demonstrated that the expected difference in the 71 number of ABBA and BABA sites is equivalent to the expected difference in the number of BAAAand ABAA sites in the instantaneous unidirectional admixture (IUA) model of introgression—see 73 the Appendix for the model description—providing the motivation to construct D_{anc} (Equation 2), 74 a statistic that leverages ancestral allele sharing to detect local introgressed regions

$$D_{anc}(P1, P2, P3, O) = \frac{\sum_{i=1}^{n} C_{BAAA}(i) - C_{ABAA}(i)}{\sum_{i=1}^{n} C_{BAAA}(i) + C_{ABAA}(i)}$$
(2)

where $C_{BAAA}(i)$ and $C_{ABAA}(i)$ are indicator variables that take a value of either zero or one conditioned on observing a BAAA or ABAA site pattern at site i for all n sites where we have data for all four samples. They also defined D+, a statistic (Equation 3) which leverages both the sharing of derived and ancestral alleles to strengthen inferences for detecting locally introgressed genomic regions

$$D + (P1, P2, P3, O) = \frac{\left(\sum_{i=1}^{n} C_{ABBA}(i) - C_{BABA}(i)\right) + \left(\sum_{i=1}^{n} C_{BAAA}(i) - C_{ABAA}(i)\right)}{\left(\sum_{i=1}^{n} C_{ABBA}(i) + C_{BABA}(i)\right) + \left(\sum_{i=1}^{n} C_{BAAA}(i) + C_{ABAA}(i)\right)}$$
(3)

and found that D+ was a more reliable statistic than D to detect introgression in small genomic windows (Lopez Fang et al., 2022). As researchers are also interested in quantifying the amount

of introgression, here we construct estimators to infer the fraction of the genome shared through introgression—hereafter referred to as the admixture proportion. One approach to infer the ad-84 mixture proportion is to assess the ratio of observed differences in allele sharing between the donor 85 and recipient populations—i.e., the P3 and P2 populations respectively—in the numerator and the expected differences assuming the entire genome was introgressed—i.e., complete homogeniza-87 tion of allele sharing—from P3 to P2 in the denominator (Martin et al., 2014). This approach (Equation 4) was first described only in terms of derived allele sharing between recipient and donor populations in Martin et al. 2015 as an alternative to the original estimator of the admixture proportion described in Durand et al. 2011 where two pseudo-haploid genomes are created by 91 randomly sub-sampling chromosomes from the P3 individual. In the simplest case of only having four whole-genome alignments—which are monoploid—this pseudo-haploid approach is not possible, so Martin et al. 2015 proposed to use the sampled P3 sequence twice in the denominator to circumvent the need for creating pseudo-haploid genomes. The original estimator of the admixture proportion from Martin et al. 2015 is f_{hom} (Equation 4)

$$S(P1, P2, P3, O) = \sum_{i=1}^{n} C_{ABBA}(i) - C_{BABA}(i)$$
(4a)

$$f_{hom}(P1, P2, P3, O) = \frac{S(P1, P2, P3, O)}{S(P1, P3, P3, O)}$$
(4b)

where homogenization is accomplished by replacing P2 with P3 in the assumed underlying species tree—i.e., in Newick format (((P1, P3), P3), O)—when computing the denominator. It should be noted that when written in terms of derived allele frequencies and in the most simplest case of only having four whole-genome sequences, f_{hom} is equivalent to F4-ratio (Patterson et al., 2012). Given that patterns of ancestral allele sharing between donor and recipient populations mirror those of their derived allele sharing counterparts we can re-derive f_{hom} in terms of BAAA and ABAA site patterns resulting in f_{anc} (Equation 5).

$$S_{anc}(P1, P2, P3, O) = \sum_{i=1}^{n} C_{BAAA}(i) - C_{ABAA}(i)$$
 (5a)

$$f_{anc}(P1, P2, P3, O) = \frac{S_{ANC}(P1, P2, P3, O)}{S_{ANC}(P1, P3, P3, O)}$$
(5b)

Lastly, given that introgressed segments are inherited in blocks consisting of both new derived alleles and re-introduced ancestral alleles one can formulate quantification metrics that consider all possible site patterns that represent allele sharing between recipient and donor populations; such as f+ (Equation 6).

$$S + (P1, P2, P3, O) = \left(\sum_{i=1}^{n} C_{ABBA}(i) - C_{BABA}(i)\right) + \left(\sum_{i=1}^{n} C_{BAAA}(i) - C_{ABAA}(i)\right)$$
(6a)

$$f + (P1, P2, P3, O) = \frac{S + (P1, P2, P3, O)}{S + (P1, P3, P3, O)}$$
(6b)

Note that all coalescent based expectations and equations written in terms of derived allele frequencies can be found in the Appendix.

$_{\circ}$ 3 Results

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3.1 Ancestral & Derived Allele Sharing Site Pattern Differences Are Equivalent Across All Admixture Proportions

We first validated the theoretical result proposed by Lopez Fang et al. 2022 that the (ABBA – 113 BABA) and (BAAA - ABAA) site pattern differences are equivalent by simulating whole-genome sequences under an IUA model of introgression using parameters that reflect the demographic 115 history of humans (Figure S1) using the coalescent simulator msprime v1.1.1 (Baumdicker et 116 al., 2022). For each simulation replicate, we sample one chromosome from each population, and 117 computed the difference—i.e., (ABBA - BABA) - (BAAA - ABAA). We simulated 100 replicates 118 under the demographic model to generate a distribution of the difference. We calculated the mean 119 of the difference over the number of replicates and we take the absolute value of the mean—so that 120 the mean difference is always positive. We then test to see if the mean is statistically significantly different from zero. For different values of the admixture proportion ranging from 0% to 50%, 122 we find that the difference of site pattern differences does not significantly differ from zero under 123 the IUA model (see Figure 1 and Table S4). This is also true in the case of a more complex demographic history—e.g. such as the one in Ragsdale and Gravel 2019—or when we consider a 125 larger sample size (n=100), where the variance of the differences gets smaller (see Figure 1; Tables 126 S4-S6 and S19-S20). These results suggest that the theoretical expectation is robust to sampling scheme, demographic history, and the amount of introgression, providing us with justification for constructing introgression metrics that incorporate ancestral allele sharing site patterns.

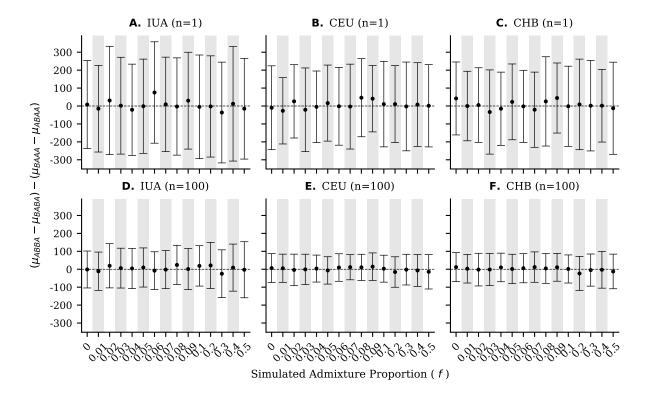


Figure 1: The mean (dots), standard deviation (error bars), and the theoretical expectation (dashed line and y = 0) for the difference of site pattern differences in simulations under an IUA model of introgression (panels **A** and **D**) and a more realistic model of human demography modified from Ragsdale and Gravel 2019 (panels **B-C** and **E-F**) with a sampling scheme of n = 1 and n = 100 genomes from each of the potential recipient populations.

3.2 The Power To Detect Introgression Is Comparable Across All Metrics

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Simulating under the IUA demographic model, we generated distributions of D, D_{anc} , and D+ and subsequently computed the mean simulated value per admixture proportion. Table S10 shows that the mean simulated values for these statistics match the values of D, D_{anc} and D+ calculated using the theoretical expectations of the number of ABBA, BABA, BABA, and ABAA site patterns (Equations A1-A3). We next assessed how the power to correctly detect introgression in simulated data differed between D, D_{anc} , and D+. We define power as the number of replicates

that significantly differ from zero out of 100 total simulated replicates per admixture proportion; to 137 test for statistical significance we constructed 1000 bootstrapped genomes per simulation replicate 138 and calculate each introgression dection metric, which were used to generate a z-distribution and 139 subsequent p-values. Like D, D+ and D_{anc} are able to correctly identify instances of introgression 140 and we observe that the power to correctly identify instances of introgression is largely consistent 141 across all metrics (Figure 2; Tables S7-S9). Notably, in simulations with no introgression (i.e., 142 when f = 0) D+ and D_{anc} either always incorrectly detect introgression at the same rate or lower 143 rate as D, suggesting that on average D+ and D_{anc} have a lower false positive rate (FPR) than 144 D. Under the IUA model of introgression D and D+ are always able to correctly identify intro-145 gression at comparable rates and outperform D_{anc} . For more realistic demographic histories, on 146 average D slightly outperforms D+ for smaller amounts of introgression while both statistics tend 147 to outperform D_{anc} (Tables S8-S9). Additionally, the power to correctly detect introgression always 148 increased when the sample size increases in all models explored (Figure 2; Tables S7-S9).

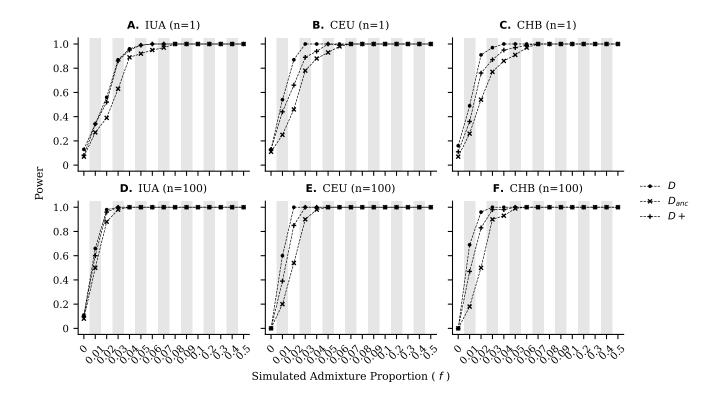


Figure 2: The power to correctly detect introgression in simulations under an IUA model of introgression (panels **A** and **D**) and a more realistic model of human demography modified from Ragsdale and Gravel 2019 (panels **B-C** and **E-F**) with a sampling scheme of n = 1 and n = 100 genomes from each of the potential recipient populations. Note that the power at $f = \theta$ corresponds to the false positive rate since no introgression has occurred.

3.3 The Power To Quantify Introgression Is Nearly Identical Across All Metrics

Simulating under the IUA model with varying admixture proportions from 0% to 50% we generated distributions and computed the simulated mean values of f_{hom} , f_{anc} , and f+. Notably, the coalescent based expectations closely mirror the mean inferred admixture proportions across all simulations, providing evidence that f_{hom} , f_{anc} , and f+ are all accurate metrics for quantifying introgression given the underlying IUA model (Figure 3; Table S16). We next evaluated the power of f_{hom} , f_{anc} , and f+ to infer the true admixture proportion in simulated data under the assumption that a perfect estimator of the admixture proportion would infer the same value as the simulated admixture proportion—i.e., $\hat{f} = f$. Under this assumption we calculated the root-mean-square-error

(RMSE) and mean-absolute-error (MAE) of each quantification metric for all simulated admixture proportions. Despite that f_{hom} , f_{anc} , and f+ all generally underestimate the true admixture proportion for our demographic models, the power to infer the admixture proportion is nearly identical across all metrics (Table S13-S15). In fact, Tables S16-S18 demonstrate that the mean inferred admixture proportions varied at most by 0.1% across all metrics for any given demographic model, sampling scheme, and simulated admixture proportion. However this is to be expected given that f_{hom} , f_{anc} , and f+ all have the same coalescent based expectation—i.e., $\frac{(f) \cdot (T_{P3} - T_{GF})}{T_{P3} + 2N}$ (see equations A7-A9 in the Appendix).

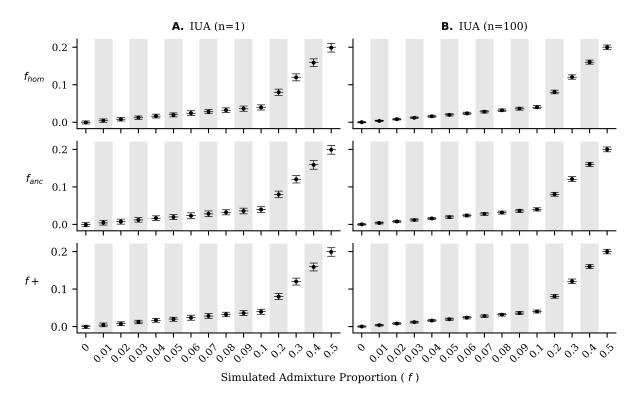


Figure 3: The mean (dots), standard deviation (error bars), and the theoretical expectation (solid horizontal lines) of f_{hom} , f_{anc} , and f_{+} in simulations under an IUA model of introgression with a sampling scheme of n = 1 (panel **A**) and n = 100 (panel **B**) genomes from each of the potential recipient populations.

3.4 All Introgression Metrics Perform Similarly In Human & Canid Data

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Before calculating f_{hom} , f_{anc} , and f_{+} in empirical data, we wanted to investigate the behavior of 168 ancestral and derived allele sharing site patterns. We first calculated ABBA, BABA, BAAA, and 169 ABAA using the modern-day humans in the 1000 Genomes Project (TGP) and the high-coverage 170 Altai Neanderthal genome (1000 Genomes Project Consortium et al., 2015; Prüfer et al., 2014). 171 We first wanted to test if the difference of site pattern differences significantly deviated from zero 172 by calculating site pattern counts for every non-African individual in the TGP and calculating the 173 mean difference of site pattern differences per chromosome for every population. Concordant with 174 our theoretical and simulated results, on average the mean difference of site pattern differences per chromosome was within two standard deviations of the theoretical expectation of zero (Figure 176 4). However, it should be noted that not all chromosomes were within two standard deviations, 177 particularly, this was the case for chromosome 19 in every non-African population (Figure 4). 178 Additionally, we computed the distribution of the difference across the whole genome (Figure 179 5) to assess if the genomic mean difference of site pattern differences significantly differed from 180 zero in each population. After correcting for multiple comparisons, we found that only the CDX 181 population did not meet our theoretical expectation (Figure 5; Table S21). Next, we inferred the 182 Altai Neanderthal admixture proportion in each non-African individual and again concordant with 183 our theoretical and simulated results we find that all estimates of the admixture proportion are 184 concordant among trios with the mean f_{hom} , f_{anc} , and f_{+} values all being within one standard deviation of one another within each non-African population (Figure 6; Table S22). As all the 186 statistics studied here can also be defined as functions of allele frequency (see Equations A4-A6 187 and A10-A12), we also used the derived allele population frequencies to infer the presence and amount of introgression in every non-African population. Remarkably, we find that all D, D_{anc} , 189 and D+ estimates are statistically significant after correcting for multiple comparisons and that 190 estimates of f_{hom} , f_{anc} , and f+ are nearly identical with nearly identical standard deviations (Table 191 S23). Furthermore, estimates of the admixture proportion are in agreement with previous estimates 192 of roughly 1% of Neanderthal introgression (Green et al., 2010; Mafessoni et al., 2020; Prüfer et al., 193 2017; Prüfer et al., 2014). 194 We also sought out to apply our methods in a non-human data set, and we chose canid data 195 to investigate the behavior of ancestral and derived allele sharing site pattern-based introgression

metrics when only one individual per population is sequenced. To do so, we calculated all site 197 patterns and introgression metrics from high-coverage whole-genome sequences for the ((Dingo, 198 Basenji), Israeli Wolf) trio where we used the Golden Jackal as an outgroup—we chose this trio as 199 it has the largest significant Z-score for Patterson's D reported in the original paper (Freedman et 200 al., 2014). It should be noted that it is highly unlikely that any biological system has experienced 201 a demographic history that mirrors the IUA model which the underlying expectations for site 202 pattern differences are based on; to this extent we propose a definition of approximately equivalent, 203 which is defined as site pattern differences having the same sign and same order of magnitude. 204 Notably, even though the demographic history of canids is known to violate the underlying IUA 205 model, the site pattern differences are concordant with our definition of approximately equivalent 206 (Table S24). Additionally, concordant with the original findings from Freedman et al. 2014, we find 207 that all introgression detection metrics are statistically significant and that all inferred admixture 208 proportions varied at most by 1.4% Israeli Wolf ancestry between quantification metrics (Table 209 S24). 210

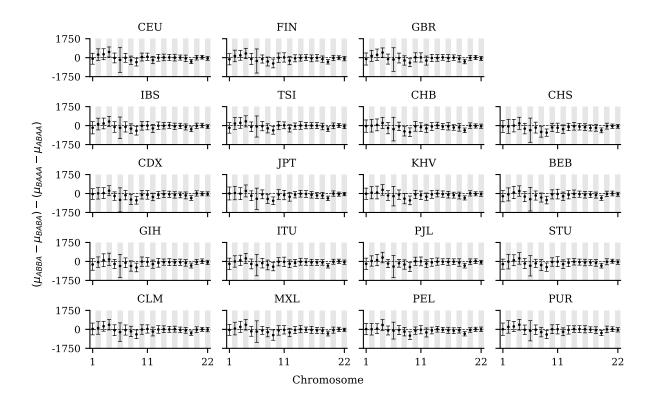


Figure 4: The mean (dots), two standard deviation (error bars), and the theoretical expectation (dashed line and y = 0) for the mean difference of site pattern differences among trios per chromosome for every non-African population in the 1000 Genomes Project.

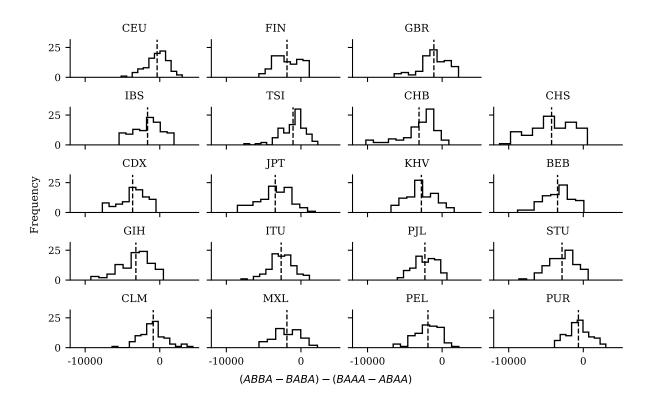


Figure 5: Distributions of difference of site pattern differences among trios for every non-African population in the 1000 Genomes Project. The black dashed line represents the genome-wide mean difference of site pattern differences among trios per non-African population.

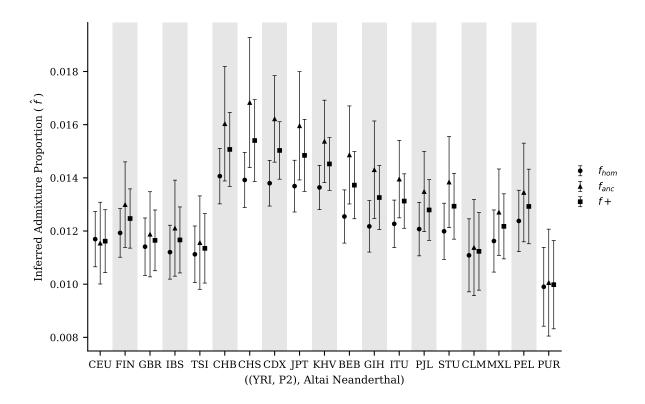


Figure 6: The mean (dots, triangles, and squares) and standard deviation (error bars) of f_{hom} , f_{anc} , and f_{+} among trios for every non-African population in the 1000 Genomes Project.

211 4 Discussion

The genomic era continues to provide evidence that post-divergence gene flow events are much more common than previously appreciated. Characterizing what are the effects and consequences of introgression across the tree of life requires providing robust tools that are able to efficiently and confidently detect and quantify such events. Here, in addition to using derived allele sharing between a putative donor and recipient population, we proposed to also incorporate ancestral allele sharing to construct estimators of the admixture proportion—e.g. f_{anc} and f+. In our study we benchmark D, D_{anc} , D+, f_{hom} , f_{anc} , and f+ which can be used to detect and quantify introgression. In particular, we use coalescent theory, simulations, and publicly available empirical data, to show that genome-wide site pattern-based tests of introgression that rely on ancestral, derived, and both patterns of allele sharing perform comparably, providing researchers the opportunity to corroborate claims of introgression from multiple metrics that exploit different genomic signals.

Our results show that D, D_{anc} , and D+ can detect the presence of introgression. On average 223 D_{anc} has less power to detect introgression when compared to D and D+, but D_{anc} on average also 224 exhibits the lowest FPR (Tables S7-S9). D tends to slightly have more power to detect introgression 225 than D+ but also tends to have higher FPR compared to D+ (Tables S7-S9). In empirical data 226 we found that D, D_{anc} , and D+ gave concordant results, suggesting that all of the aforementioned 227 statistics are appropriate for detecting introgression on genome-wide data sets. The power to 228 correctly infer the admixture proportion suffers from theoretical constraints. Specifically, f_{hom} , 229 f_{anc} , and f_{+} all have the same theoretical expectation of $\frac{(f)\cdot(T_{P3}-T_{GF})}{T_{P3}+2N}$ (see equations A7-A9 in the 230 Appendix), which makes it clear that we will always underestimate the admixture proportion. In 231 simulated data the mean f_{hom} , f_{anc} , and f_{+} values closely mirrored the theoretical expectations 232 (Figure 3; Table S13) and all quantification metrics exhibit nearly identical RMSE and MAE233 with respect to the simulated admixture proportion (Tables S13-S15). Additionally, in human 234 data not only do we observe nearly identical estimates of the admixture proportions between all 235 metrics studied here, but also nearly identical standard deviations for both trio and population 236 level estimates (Figure 3; Table S23 and S22). Taken together we propose that researchers make 237 use of both derived and ancestral allele sharing site pattern-based tests of introgression to make 238 more thorough assessments about the presence and amount of introgression. To this extent we also 239 developed a lightweight python package RIPTA (Re-evaluating Introgression site Patterns Through 240 Ancestral alleles) to calculate all site patterns and introgression metrics studied in here. 241 Our theoretical and simulation results have shown that the expectation of site pattern differences i.e., (ABBA - BABA) - (BAAA - ABAA)—is zero. This is true even when we consider complex 243 demographic histories (Figure 1). When we count these site patterns using human and archaic 244 genomes, we found that most non-African chromosomes in the TGP do not depart from this theo-245 retical expectation (Figures 4-5; Table S21). One exception is chromosome 19 (see Figure 4), where 246 the difference of (BAAA - ABAA) is larger than (ABBA - BABA), and this is true across all 247 non-African populations. We tested to see if more complex demographic histories that have been 248 proposed for human populations could lead to deviations from zero. For example, we tried incor-249 porating population expansions and contractions, multiple pulses of introgression, and a dilution 250 in the recipient population, and none of these models result in a difference that deviates from zero 251

(Tables S5-S6 and S19-S20).

Another explanation for this observation, could be a component of evolution that our simulations 253 ignored, such as natural selection. Studies have shown that Neanderthal alleles were originally costly 254 on the modern human genetic background due to genetic load (Harris & Nielsen, 2016; Kim et al., 255 2018). It has also been shown that the effects of Neanderthal ancestry is negatively correlated with 256 exon density under an additive fitness model (Kim et al., 2018). Given that chromosome 19 has 257 the highest gene density in the genome (Grimwood et al., 2004), we hypothesize that the effects of 258 natural selection may influence these site patterns. However, while some studies have shown that 259 derived archaic alleles were likely mostly deleterious in modern humans, we know very little about 260 what evolutionary forces (if any) acted on ancestral alleles that were re-introduced into modern 261 humans with archaic introgression. We acknowledge that the BAAA and ABAA site patterns are likely to be more sensitive to differences in mutations rate in the two sister populations—i.e., 263 P1 and P2—than ABBA and BABA sites. This might be contributing to observation that the 264 difference of (BAAA - ABAA) is larger than (ABBA - BABA), where more BAAA sites could 265 indicate a higher mutations rate in P1 vs P2. As this is only observed in chromosome 19, we think 266 it is more likely that other evolutionary forces might be contributing to this signature, but more 267 work is needed to characterize what can lead to deviations from zero. 268

In summary, we have provided further evidence that ancestral allele sharing site patterns are 269 informative for detecting introgression on a genome-wide scale and are robust to realistic models 270 of human demography. Additionally, we have derived novel estimators of the admixture propor-271 tion and demonstrated that these methods provide reliable estimates of the admixture proportion. Applying it to empirical data in humans suggests that chromosome 19 is an outlier with respect to 273 the difference in ancestral allele sharing site patterns. None of the demographic histories that we 274 simulated lead to deviations, so we hypothesize that other non-neutral processes may be at play. 275 More work to investigate how natural selection acted on ancestral alleles that were reintroduced 276 into human populations through introgression with archaic humans might provide insights into how 277 evolutionary forces have shaped introgressed genetic variation.

₂₇₉ 5 Materials and Methods

All annotated code to recreate all analyses and annotated Jupyter Notebooks with walkthroughs of how to perform all analyses described in this paper can be found at https://github.com/ David-Peede/anc-der-intro-proj. The RIPTA package to calculate site patterns and all introgression metrics studied here can be found at https://github.com/David-Peede/RIPTA.

5.1 Simulation Design

All demographic models were quality controlled using msprime v1.1.1 and visualized using demesdraw v0.3.0 (Baumdicker et al., 2022; Gower et al., 2022). All demes .yaml files with demographic histories needed to reproduce our results can be found https://github.com/David-Peede/anc-der-intro-proj/tree/main/simulations/yamls.

$_{289}$ 5.1.1 IUA Model

To assess the statistical power of all introgression metrics discussed in this study we simu-290 lated whole-genome sequences based on a three-taxon tree following IUA model described in Du-291 rand et al., 2011, and in Green et al., 2010. Using the coalescent simulator msprime v1.1.1 we 292 simulated 100 Mb genomes under a demographic model with the following parameters: $T_{P3} =$ 293 16,000 generations ago, $T_{P2} = 4,000$ generations ago, $T_{GF} = 1,600$ generations ago, constant 294 and equal $N_e=10{,}000$ for all populations, $r=1e^{-8}$ per bp per generation, and $\mu=1.5e^{-8}$ 295 per bp per generation under a Jukes-Cantor substitution model (Baumdicker et al., 2022). Our 296 parameter space was constructed to reflect a simplified version of human evolution with intro-297 gression from the Neanderthal population into the Eurasian population as was originally described in Racimo et al., 2017. The divergence times, timing and direction of introgression, 290 and mutation and recombination rates are all direct reflections of the original parameter space, 300 and represent plausible parameter values for the well studied case of Neanderthal introgression 301 (Racimo et al., 2016). The only model parameter varied was the simulated admixture propor-302 tion $f \in \{0, 0.01, 0.02, 0.03, 0.04, 0.05, 0.06, 0.07, 0.08, 0.09, 0.1, 0.2, 0.3, 0.4, 0.5\}$ which was used to 303 determine the behavior of the introgression metrics studied here, for both plausible and theoretical 304 amounts of introgression. For each of the 15 admixture proportions, 100 replicate simulations were 305 performed, either n = 1 or n = 100 simulated genomes were sampled per potential recipient popu-306 lation per replicate, and one simulated genome was sampled from the donor population, which were 307 then used to calculate site pattern counts and all introgression metrics described in this paper.

5.1.2 Non-IUA Models

309

To determine the statistical power of all introgression metrics in a more realistic model of human 310 demographic history, we used the used the demographic model proposed by Ragsdale and Gravel 311 2019 implemented in stdpopsim v0.1.2 (Adrion et al., 2020; Ragsdale & Gravel, 2019). To make 312 this model more comparable to our analyses using the IUA model we modified the model (see Figure 313 \$2) to consist of discrete pulses of introgression—one pulse into the Eurasian population, and one 314 pulse into CEU and CHB populations respectively—by taking the midpoint of the two periods of 315 continuous bidirectional gene flow described in the original model. The simulation design for the 316 modified Ragsdale and Gravel 2019 model is the exact same as described in the previous section. Additionally, we ran all sets of analyses on the original model (see Figure S3) using the original 318 estimates of bidirectional gene flow (Ragsdale & Gravel, 2019). Lastly, to assess if the difference of 319 site pattern differences would significantly deviate from zero we chose to simulate multiple pulses of 320 introgression, ghost introgression, and a dilution event from a so called "Basal Eurasian" population 321 (see Figures S4-S5). We used demographic parameters described in Rogers and Bohlender 2015, 322 Villanea and Schraiber 2019, and Ragsdale and Gravel 2019 to run 100 replicate simulations per 323 all pairwise possibilities of plausible Neanderthal $f_{NEA} \in \{0, 0.005, 0.01, 0.015, 0.02\}$ and Denisovan 324 $f_{DEN} \in \{0, 0.005, 0.01, 0.015, 0.02\}$ admixture proportions for sampling schemes of n = 1 and n = 1325 100 simulated genomes from the potential recipient populations, and one simulated genome from 326 the Neanderthal population (Ragsdale & Gravel, 2019; Rogers & Bohlender, 2015; Villanea & Schraiber, 2019). 328

5.2 Assessing Introgression Metrics In Simulated Data

For all 100 replicate simulations per admixture proportion we assessed the theoretical expectation that (ABBA - BABA) is equivalent to (BAAA - ABAA) by computing the difference of site pattern differences—i.e., (ABBA - BABA) - (BAAA - ABAA)—per replicate to construct a z-distribution. We then assessed if the absolute value of the mean difference of site patterns differences significantly differed from the theoretical expectation of zero using the scipy.stats.sf function in scipy v1.7.2, and corrected for multiple comparisons using the Bonferroni correction (Virtanen et al., 2020). To determine the significance of introgression detection metrics—i.e., D, D_{anc} , and D+—for each simulation replicate we built a bootstrapped distribution of 1,000

bootstrapped replicates, where each bootstrapped replicate consists of concatenating 1,000 100 kb 338 windows that were randomly sampled with replacement to build 100 Mb bootstrapped genomes 339 for each focal population. The bootstrapped genomes were then used to construct z-distributions 340 of D, D_{anc} , and D+ per replicate, and a nominal p-value of < 0.05 was used as the significance 341 threshold. The power to detect introgression using D, D_{anc} , and D+ was then determined by the 342 proportion of replicates that were statistically significant per admixture proportion. The power 343 to accurately infer the true—i.e., simulated—admixture proportion using f_{hom} , f_{anc} , and f+ was 344 assessed by calculating root-mean-square-error (RMSE) and mean-absolute-error (MAE) using the 345 following equations: 346

$$RMSE = \sqrt{\frac{\sum_{i=1}^{100} (\hat{f}_i - f_{true})^2}{100}}$$
 (7)

$$MAE = \frac{\sum_{i=1}^{100} \left| \hat{f}_i - f_{true} \right|}{100}$$
 (8)

where \hat{f}_i represents the inferred admixture proportion for the i^{th} replicate simulation out of 100 total 347 replicates and where f_{true} represents the admixture proportion used in the simulation to infer \hat{f} . We 348 chose to assess the performance of each introgression quantification metric using both the RMSE349 and MAE because both values are in the same units as the admixture proportion and because both 350 quantify the amount of dispersion in the estimates of the inferred admixture proportion around the 351 simulated admixture proportion where the RMSE values gives more weight to inferred estimates 352 that have the large amounts of error while MAE values equally weight the amount of error in all 353 inferred estimates. 354

5.3 Human Application

355

The all sites VCF files for the high-coverage genome of the Altai Neanderthal were downloaded from https://www.eva.mpg.de/genetics/genome-projects, the curated and imputed high quality genotypes from the phase three release of the 1000 Genomes Project (TGP) in VCF format was download from http://ftp.1000genomes.ebi.ac.uk/vol1/ftp/release/20130502, and the ancestral allele calls in fasta format for the Hg19 assembly using the Enredo, Pecan, Ortheus (EPO) pipeline was download from http://ftp.ensembl.org/pub/release-74/fasta/ancestral_alleles (1000 Genomes

Project Consortium et al., 2015; Herrero et al., 2016; Prüfer et al., 2014). The autosomal TGP and Altai Neanderthal VCF files were merged using the merge command from the bcftools v1.13 363 package and the resulting merged VCF files were then filtered to only contain sites with no missing 364 data, an ancestral allele call, and bi-allelic SNPs with a mapping quality of 25 or higher and a 365 genotype quality of 40 or higher (Li, 2011). Site patterns and all introgression metrics were then 366 calculated for every non-African individual using the following configuration P1 = NA18486 (a 367 randomly chosen individual from Yoruba in Ibadan, Nigeria), P2 = non-African individual, P3 = non-African individual368 Altai Neanderthal, and O = EPO ancestral allele call. Statistical tests based on the difference 369 of site pattern difference distributions per non-African TGP population were carried out in the 370 same manner as described in previous methods subsection for both individual chromosomes and 371 the entire genome. Next, site patterns and all introgression metrics were additionally calculated 372 from derived allele frequencies using the following configuration P1 = Yoruba in Ibadan, Nigeria 373 (YRI), P2 = non-African population, P3 = Altai Neanderthal, and O = EPO calls. Lastly, for the population level comparisons, the significance of introgression detection metrics—including cor-375 recting for multiple comparisons using the Bonferroni correction—and standard deviations for the 376 introgression quantification metrics were determined from bootstrapped distributions consisting of 377 1,000 replicates, which were generated from 1,000 bootstrapped genomes per population, where 378 a single bootstrapped genome was constructed from concatenating 303 randomly sampled with 379 replacement 10 Mb windows. 380

381 5.4 Canid Application

The merged VCF files for the high-coverage canid data-set were downloaded from https://doi. 382 org/10.5061/dryad.sk3p7 (Freedman et al., 2014). The autosomal VCF files were then filtered by 383 the genomic-feature (GF=1) flag using the view command from the bcftools v1.13 package. Ad-384 ditionally, when performing calculations we only used sites where all focal individuals passed their 385 respective sample filters—i.e., SF=1 flag. We calculated site patterns and all introgression metrics 386 for the configuration P1 = Dingo, P2 = Basenji, P3 = Israeli Wolf, and O = Golden Jackalbecause the aforementioned trio had the highest degree of confidence for a significant Patterson's 388 D reported in the original paper (Freedman et al., 2014). Lastly, the significance of introgres-389 sion detection metrics and standard deviations for the introgression quantification metrics were determined from bootstrapped distributions consisting of 1,000 replicates, which were generated from 1,000 bootstrapped genomes per individual canid, where a single bootstrapped genome was constructed from concatenating 220 randomly sampled with replacement 10 Mb windows.

All annotated code and previously published publicly available data sets needed to reproduce the entirety of this manuscript can be found at the url links described in the methods section.

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