

1 HAPNEST: efficient, large-scale generation and evaluation of  
2 synthetic datasets for genotypes and phenotypes

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14 **Abstract**

15 Existing methods for simulating synthetic genotype and phenotype datasets have limited scalability,  
16 constraining their usability for large-scale analyses. Moreover, a systematic approach for evaluating  
17 synthetic data quality and a benchmark synthetic dataset for developing and evaluating methods  
18 for polygenic risk scores are lacking. We present HAPNEST, a novel approach for efficiently gener-  
19 ating diverse individual-level genotypic and phenotypic data. In comparison to alternative methods,  
20 HAPNEST shows faster computational speed and a lower degree of relatedness with reference pan-  
21 els, while generating datasets that preserve key statistical properties of real data. These desirable  
22 synthetic data properties enabled us to generate 6.8 million common variants and nine phenotypes  
23 with varying degrees of heritability and polygenicity across 1 million individuals. We demonstrate

24 how HAPNEST can facilitate biobank-scale analyses through the comparison of seven methods to  
25 generate polygenic risk scoring across multiple ancestry groups and different genetic architectures.

## 26 1 Introduction

27 With the emergence of large-scale biobanks, methods to analyse common genetic variants (single  
28 nucleotide polymorphisms, or SNPs) across diverse human populations are in growing demand.  
29 This is especially the case for polygenic risk scoring (PRS) methods, which quantify an individual's  
30 genetic risk for a disease or other phenotypic trait [1]. Derived from one's genotype, well-calibrated  
31 PRSs have the potential to be used for risk stratification and prognostic prediction [1]. PRS's utility  
32 has been demonstrated for certain common diseases among European ancestries, on which most  
33 genome-wide association studies (GWAS) were carried out [2], but some studies have highlighted  
34 limitations in PRS's transferability across ancestries and different socio-demographic groups [3].  
35 Thus, the development of methods that can improve the generalisability of PRSs is needed. At the  
36 same time, only a few accessible large-scale biobank datasets exist and most previous PRS methods  
37 have been tested and compared in UK Biobank [4]. More diverse biobank datasets are needed, but  
38 due to the highly sensitive nature of genetics data, accessing and sharing individual-level data raises  
39 privacy concerns. This makes publicly accessible synthetic data a welcome alternative for methods  
40 developers.

41 Broadly, two main approaches have been used to simulate individual level genetic data. Coalescence-  
42 based methods, such as Hudson's ms and msprime [5, 6], use demographic models to generate  
43 genomes including both rare and common variants. Reference-based approaches use real genomic  
44 data (e.g. 1000 genomes or HGDP) to generate synthetic data, but they are not suitable to gen-  
45 erate realistic rare variants. There are also methods, such as simGWAS[7], that directly simulate  
46 GWAS summary statistics. However, many times they do not meet modern demands for methods  
47 development based on individual level data. We will focus on reference-based approaches since for  
48 PRSs we are mostly interested in common genetic variation, which forms the bulk of complex trait  
49 heritability [8]. Moreover, common SNPs, especially Hapmap3 SNPs [9], are widely recommended  
50 for PRS computation [10]. HAPGEN2 [11] is a widely used tool for genotype and phenotype sim-  
51 ulation, which preserves linkage disequilibrium (LD) patterns of real data through a resampling

52 approach based on the Li and Stephens model [12]. However, HAPGEN2 lacks computational scal-  
53 ability and flexibility to simulate certain scenarios of interest for biobank-scale PRS and SNP-based  
54 methods development. Recent alternatives include G2P [13] and Sim1000G [14]. Sim1000G is an  
55 integrated R package, but is limited to genotype simulation. G2P encompasses both genotype and  
56 phenotype simulation, and is highly customisable, but this setup can be challenging for non-expert  
57 users. Without an integrated approach for parameter selection and evaluation of synthetic data  
58 quality, it is difficult for end-users to understand the statistical guarantees and reliability of the  
59 generated datasets. To the best of our knowledge, there does not exist a software tool implementing  
60 an end-to-end pipeline for synthetic data generation, evaluation and optimisation.

61 To address these limitations, we introduce HAPNEST, a user-friendly tool for generating syn-  
62 thetic datasets for genotypes and phenotypes, evaluating synthetic data quality, and analysing  
63 the behavior of model parameters with respect to the evaluation metrics. HAPNEST simulates  
64 genotypes by resampling a set of existing reference genomes, according to a stochastic model that  
65 approximates the underlying processes of coalescent, recombination and mutation. It is, in spirit,  
66 similar to HAPGEN2, but we introduce some innovations to reduce relatedness between synthetic  
67 individuals and the reference panel. Phenotypes are subsequently assigned to each sample by  
68 integrating user-specified genetic, covariate, and environmental effects. Genetic effects are mod-  
69 elled in terms of heritability and polygenicity. HAPNEST enables efficient simulation of diverse  
70 biobank-scale datasets, as well as simultaneously generating multiple genetically correlated traits  
71 with population specific effects under different pleiotropy models. Moreover, the HAPNEST soft-  
72 ware includes an extensive workflow for evaluating synthetic data fidelity and generalisability, as  
73 well as approximate Bayesian computation (ABC) techniques for analysing the posterior distribu-  
74 tions of model parameters to aid model selection.

75 We compare the performance of HAPNEST with current state-of-the-art genotype and pheno-  
76 type simulation tools in terms of data quality and computational speed. Furthermore, as a demon-  
77 stration of the utility of our tool, we show the application of our diverse, biobank-scale synthetic data  
78 for evaluating the performance of various PRS methods under different disease models. Our open-  
79 source software tool is available at [https://github.com/intervene-EU-H2020/synthetic\\_data](https://github.com/intervene-EU-H2020/synthetic_data),  
80 and has also been distributed as Docker and Singularity containers. We have generated 6.8 million  
81 common variants and 9 phenotypes with varying degrees of heritability and polygenicity across 1

82 million individuals and made this large synthetic dataset available at <https://www.ebi.ac.uk/biostudies/studies/S-BSST936> to encourage standardised evaluation of new statistical methods  
83 by the genomic research community.  
84

## 85 2 Results

### 86 2.1 Overview of genotype generation methods

87 Synthetic haplotypes are constructed as a mosaic of segments of various lengths imperfectly copied  
88 from real haplotypes (Figure 1, Panel a). HAPNEST uses an approximate model inspired by the  
89 sequential Markovian coalescent model [15], which makes simplifying assumptions about the coales-  
90 cence and recombination processes. The real haplotypes to copy from are sampled uniformly from a  
91 reference dataset,  $\mathcal{D}_s$ , limited to individuals belonging to a certain ancestry group  $s$ . Alternatively,  
92 users can specify the proportion of real haplotypes to sample from each ancestry group. We refer  
93 to the Discussion section of the paper regarding the complications in interpreting admixed samples.  
94 Segments of length  $\ell$  (in centimorgans) are sampled from the real haplotypes (Figure 1, Panel b)  
95 based on a simplified stochastic model of the coalescent and recombination processes,

$$\ell \sim \text{Exp}(2T\rho_s), T \sim \text{Gamma}(2, N_s/N_{e,s}), \quad (1)$$

96 where  $\rho_s$  is the population-specific recombination rate,  $N_{e,s}$  is the population-specific mean effective  
97 population size, and  $N_s$  is the number of reference samples for population  $s$ . The simulation of  
98 varying, rather than constant, coalescence time  $T$ , is one of two main aspects in which HAPNEST  
99 differs from previous methods such as HAPGEN2. Another feature we introduce is that to reduce  
100 close copying of genotypes from the reference, the presence of a genetic variant at position  $i$  is only  
101 copied if  $T \leq m_i$ , where  $m_i$  is the variant's age of mutation (obtained from [16]). Two synthetic  
102 haplotypes,  $h_i$ ,  $i \in \{1, 2\}$ , constructed in this way are added element-wise to create a synthetic  
103 genotype,  $g$  (Figure 1, Panel c). For experiments in this text, we consider a reference dataset of  
104 4,062 phased genotypes derived from the publicly available 1,000 Genomes Project and Human  
105 Genome Diversity Project datasets for 6 major discrete ancestry groups [17].

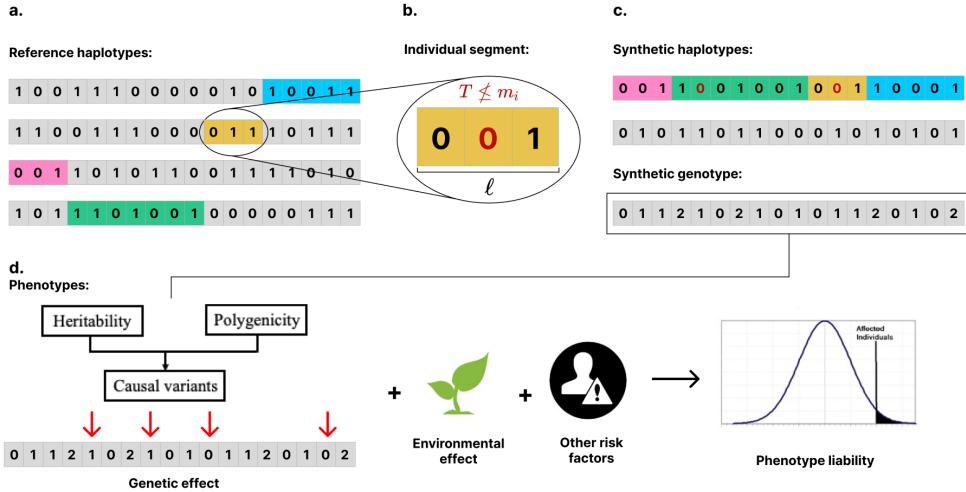


Figure 1: **a.** A reference set of real haplotypes, from which segments (colored) are imperfectly copied to construct a synthetic haplotype. **b.** Detailed view of an individual segment. The segment length,  $\ell$ , and coalescence time,  $T$ , are sampled from a stochastic model. The presence of a genetic variant at position  $i$  is only copied if  $T \leq m_i$ , where  $m_i$  is the variant's age of mutation. Variants that are not copied are shown in red. **c.** Synthetic genotypes,  $g$ , are constructed as pairs of synthetic haplotypes,  $h_i$ ,  $i \in \{1, 2\}$ . **d.** Once the genotype is generated, liability of phenotype will subsequently be assigned to each sample as a summation of genetic effect, covariate effect (if any) and environmental noise.

## 106 2.2 Posterior distributions of model parameters

107 While there is no consensus on universal metrics for evaluating synthetic datasets, the literature  
 108 tends to emphasise the general properties of fidelity (the ability to preserve statistical properties  
 109 of the real data) and generalisability (the extent to which synthetic samples are not direct copies  
 110 of the real data) [18, 19]. For downstream applications such as GWAS and PRS, it is important to  
 111 preserve realistic LD patterns in the synthetic data (fidelity objective). In this work we measure  
 112 generalisability in terms of genetic relatedness (defined by the kinship coefficient), to ensure that  
 113 the samples in large synthetic datasets are not close copies of samples from the much smaller  
 114 reference dataset. We use Approximate Bayesian Computation (ABC) (as explained in the Methods  
 115 section) to estimate model parameters which balance both the fidelity and the generalisability  
 116 objectives. Figure 2 shows the posterior distributions of the parameters that best satisfy these  
 117 criteria. We observe a tradeoff between optimising the fidelity objective (Supplementary, Figure  
 118 10) and optimising the generalisability objective (Supplementary, Figure 11). This tradeoff can  
 119 affect the results of downstream analyses such as GWAS (Supplementary, figure 12, table 6).

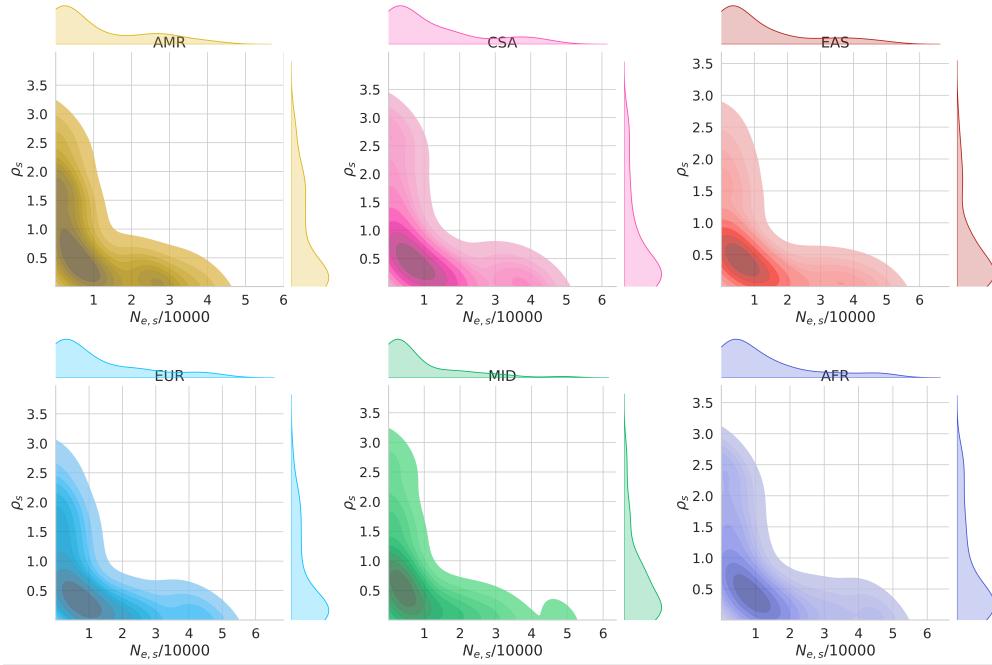


Figure 2: Posterior distributions plotted as marginal and bivariate kernel density estimates for the effective population size,  $N_{e,s}$ , and recombination rate,  $\rho_s$ , for six superpopulation groups,  $s^{-1}$ . The experiment setup used 500 simulations for  $N_{syn} = 1000$  synthetic samples based on a reference of chromosome 21 HapMap3 variants, with uniform priors and a 20 percent rejection rate.

### 120 2.3 Comparison of synthetic genotype quality

121 Synthetic data quality is evaluated based on a workflow implemented in the HAPNEST software  
 122 tool for measuring the fidelity, diversity and generalisability of synthetic datasets. Briefly, fidelity  
 123 is measured as the similarity between the real (reference) and synthetic datasets for 4 properties:  
 124 minor allele frequency (MAF) distribution, population structure in terms of alignment of the prin-  
 125 cipal components (PCs), LD decay and nearest neighbour adversarial accuracy (as explained in  
 126 the Methods section). Diversity is measured by the degree of genetic relatedness (kinship) within  
 127 the synthetic dataset and generalisability is measured by the degree of genetic relatedness between  
 128 the real and synthetic datasets. HAPNEST is compared with three alternative methods (HAP-  
 129 GEN2, G2P and Sim1000G) for  $N_{syn} = 1,000$  synthetic samples, based on a reference dataset  
 130 of  $N_{ref} = 775$  European-ancestry individuals. In this section we compare two parameter sets for  
 131 HAPNEST: HAPNEST-abc, as determined by the ABC procedure for balancing the LD and relat-  
 132 edness objectives (Figure 2) and HAPNEST-equivalent, that is more equivalent to the parameter  
 133 configurations used by the other tools (which do not have built-in optimisation procedures). The

<sup>134</sup> rest of the text generally considers the ABC parameters, unless otherwise stated.

### <sup>135</sup> 2.3.1 Fidelity

<sup>136</sup> The full fidelity results are reported in Supplementary Table 1. The HAPNEST-equivalent and  
<sup>137</sup> G2P methods had the lowest divergence in MAF between the synthetic and reference datasets,  
<sup>138</sup> followed by HAPNEST-abc, Sim1000G and HAPGEN2. The HAPNEST-equivalent method also  
<sup>139</sup> had the LD decay that least diverged from the reference, followed by the G2P and HAPGEN2  
<sup>140</sup> methods. However, we observe that HAPNEST-abc has a faster LD decay (Figure 3, Panel b) and  
<sup>141</sup> more generally, our posterior analysis indicates there is a tradeoff between optimizing the LD and  
<sup>142</sup> relatedness objectives (Supplementary, Figure 10, 11). Nevertheless, GWAS results presented later  
<sup>143</sup> still indicate realistic LD structure at genome-wide significant loci. We evaluate preservation of  
<sup>144</sup> population structure by comparing the PC alignment score, defined as the cosine distance between  
<sup>145</sup> the first 20 PCs obtained from real and synthetic data within European individuals. HAPGEN2 has  
<sup>146</sup> the highest PC alignment score, followed by HAPNEST-equivalent. HAPNEST can also generate  
<sup>147</sup> datasets that preserve population structure across multiple populations (Figure 4, Panel a). Finally,  
<sup>148</sup> we consider privacy-preserving metrics, by calculating the nearest neighbour adversarial accuracy  
<sup>149</sup> score, which averages the true positive rate and true negative rate for distinguishing real and  
<sup>150</sup> synthetic data. Adversarial accuracy scores closest to 0.5 are observed for the G2P and HAPNEST-  
<sup>151</sup> abc methods, indicating that these synthetic samples are more indistinguishable from the real data.  
<sup>152</sup> Our analysis indicates that no one method performs best across all evaluation metrics, but instead  
<sup>153</sup> there are tradeoffs that end users should consider, depending on the priorities of their use case.

### <sup>154</sup> 2.3.2 Generalisability and diversity

<sup>155</sup> HAPNEST-abc reached the best generalisability and diversity of all methods evaluated (Supplemen-  
<sup>156</sup> tary, Table 2, 3) when considering  $N_{syn} = 1000$  synthetic samples. However, it is more appropriate  
<sup>157</sup> to measure generalisability and diversity on larger and more realistic sample sizes. As there is  
<sup>158</sup> a limited number of haplotypes in the reference dataset, one might expect that when generating  
<sup>159</sup> thousands of synthetic samples, some generated genomes might eventually be copies of or highly  
<sup>160</sup> related with genomes in the reference set. As shown in the next section, scalability is an issue  
<sup>161</sup> for Sim1000G and G2P, so in this experiment we only consider HAPNEST and HAPGEN2. To

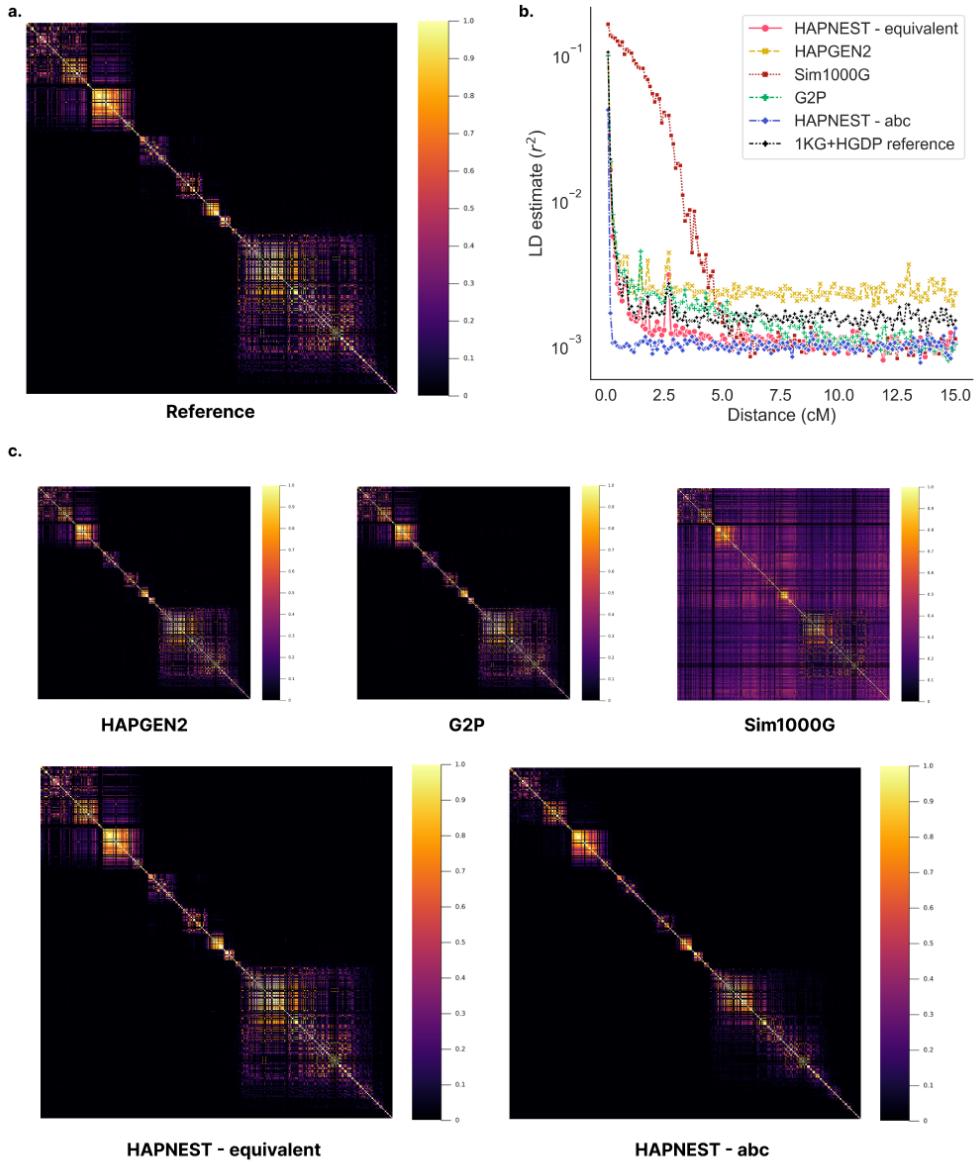


Figure 3: **a.** LD correlation for 500 contiguous SNPs selected at random from chromosome 21 HapMap3 variants, for the European-ancestry reference dataset ( $N_{ref} = 775$ ); **b.** Comparison of LD decay for  $N_{syn} = 1000$  European-ancestry synthetic samples; **c.** Comparison of LD correlation (for same 500 SNPs shown in reference panel) for  $N_{syn} = 1000$  European-ancestry synthetic samples

162 evaluate the impact of the size of the reference panel, we consider both the full reference ( $N = 775$ )  
 163 and a smaller reference ( $N = 100$ ). We observe that HAPNEST outperforms HAPGEN2 for both  
 164 generalisability and diversity on larger sample samples (Figure 5). These results are not a function  
 165 of the synthetic data sample size for either method, due to simplifying assumptions of the statistical  
 166 models used by these methods. However, the generalisability and diversity performance is affected

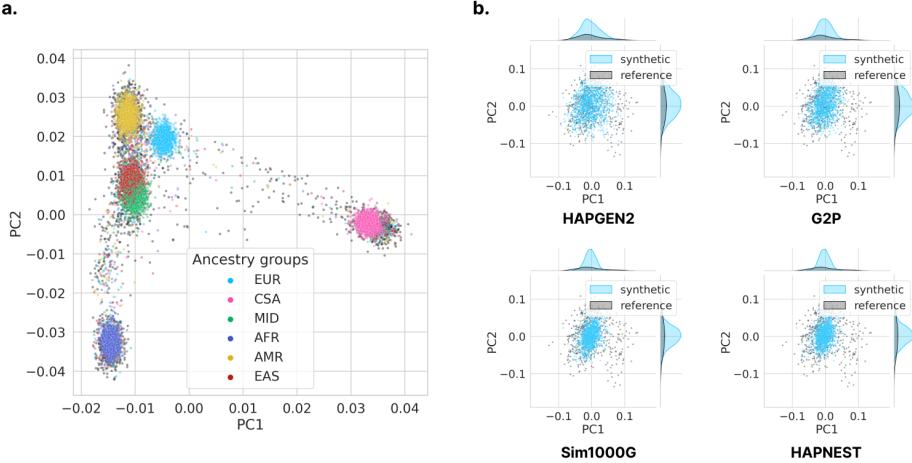


Figure 4: **a.** PCA projection plot for  $N_{syn} = 10000$  synthetic samples generated by the HAPNEST method, for chromosome 21 HapMap3 variants; **b.** Comparison of PCA projection plots and bivariate densities for  $N_{syn} = 1000$  European-ancestry synthetic samples. The highest PC alignment score for preservation of population structure is 0.311 for HAPGEN2, followed by 0.243 (HAPNEST-equivalent), 0.222 (G2P), 0.182 (HAPNEST-abc) and 0.043 (Sim1000G)

167 by the size of the reference data. We also demonstrate that for both methods, generalisability and  
 168 diversity can be improved by increasing the number of reference samples.

#### 169 2.4 Scalability analysis for large sample sizes

170 The scalability of HAPNEST is validated by measuring the computational speed of generating  
 171 genotype datasets for a range of sample sizes, compared with the widely used HAPGEN2 software  
 172 tool. The other two methods (Sim1000G and G2P) are excluded from this comparison as they did  
 173 not scale to the large sample sizes considered here. We observe that while generation times are  
 174 similar for small sample sizes, HAPNEST is increasingly faster than HAPGEN2 for larger sample  
 175 sizes (Figure 6) which approach the size of modern biobank-scale genetic datasets. This gain  
 176 in computational speed is achieved by a more efficient algorithm and its efficient multi-threaded  
 177 implementation in the Julia programming language.

#### 178 2.5 Overview of phenotype generation methods

A continuous or binary phenotype can be assigned to each sample as an aggregation of genetic effect, user-input covariate effect (if any) and environmental noise. The genetic component is generated as

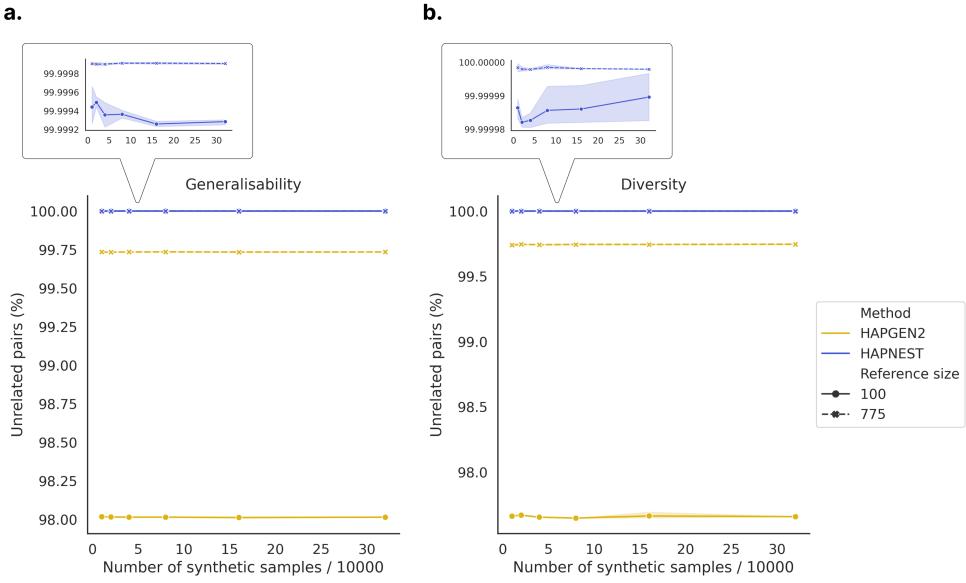


Figure 5: The **a.** generalisability and **b.** diversity scores for two reference sizes ( $N_{ref} = 100$  and  $N_{ref} = 775$ ) and various sample sizes, averaged across five trials for chromosome 21 HapMap3 variants, and the HAPNEST and HAPGEN2 methods. The ratio  $N/N_e$  is fixed to ensure a fair comparison with the same average segment lengths. Generalisability is calculated as  $(1 - \frac{N_{cross}}{N_{syn} * N_{ref}}) \times 100$ , where  $N_{cross}$  is the number of closely related pairs (i.e. twins or first-degree relatives, as determined by the kinship coefficient) between the reference and synthetic datasets. Diversity is calculated as  $(1 - \frac{N_{pairs}}{N_{syn}^2 - N_{syn}}) \times 100$ , where  $N_{pairs}$  is the number of closely related pairs in the synthetic dataset.

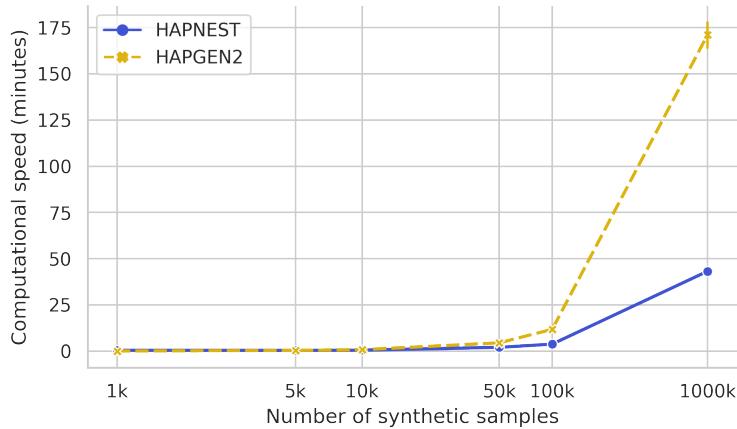


Figure 6: Simulation times for genotype datasets for HAPNEST and HAPGEN2 (other methods are excluded from this comparison due to scalability and compatibility issues), averaged for five trials with error bars plotted, for chromosome 21 HapMap3 variants. The comparison was performed on Intel Xeon Gold 6230 2.1 GHz processors with 8 cores and 32GB RAM. Since the simulation time depends on the input configuration, the experiment is controlled by setting  $\rho$  to the average recombination rate used by HAPGEN2 ( $\rho = 2.185$  for chromosome 21), and using  $N_e = 500$  for both methods (to eliminate bias from mutations).

a weighted sum of causal allele counts (Figure 1, Panel d). For each causal SNP  $\beta_i$ , the effect size is drawn from a Gaussian distribution with 0 mean and variance determined by three well-studied factors impacting heritability of the variants, the minor allele frequency (MAF)  $p_i$ , local linkage structural  $r_i$ , and the functional annotation  $s_i$  of the SNP:

$$\beta_i \sim N(0, [p_i(1 - p_i)]^a r_i^b s_i^c).$$

179 Power parameters  $a$ ,  $b$ , and  $c$  reflect strength of negative selection on each aspect and we used  
180 extensive empirical observations [20, 21, 22] to chose the default parameters. HAPNEST allows  
181 SNP's effect sizes to be drawn from a mixture of distributions with different width, corresponding  
182 to variable level of heritability. Our model also allows flexible assignment of individual components'  
183 contribution to the phenotype (heritability), as well as the number of causal variants constituting  
184 the genetic risk (polygenicity). We run GWASs for 50,000 synthetic individuals and 1,049,096  
185 HapMap 3 SNPs based on phenotypes generated under different genetic architectures. The Man-  
186 hattan plots visually resemble Manhattan plots obtained on real data with similar heritability and  
187 polygenicity (Figures 7, 13 and 14). Figure 7 shows exemplary GWAS results for traits under  
188 two extreme scenarios: low heritability, low polygenicity, and high heritability, high polygenicity.  
189 The former resembles phenotypes such as atrial fibrillation and flutter (Figure 13), and the latter  
190 resembles typically more heterogeneous traits, such as body pain (Figure 14). Our approach allows  
191 us to specify genetic correlations between phenotypes within and, importantly, between ancestry  
192 groups.

## 193 2.6 Application: Comparison of polygenic risk scoring methods

194 We demonstrated the utility of HAPNEST by comparing 7 PRS methods using synthetic data  
195 from 5 ancestry groups. We first generated a synthetic training dataset of 100,000 individuals of  
196 European ancestries, and performed a standard GWAS using software plink2 [23], correcting for top  
197 20 PCs. We subsequently used the summary statistics to build PRSs in a separate synthetic test set  
198 of 25,000 individuals (5,000 samples from each ancestry group). To demonstrate variability across  
199 genetic architectures, GWAS summary statistics are computed for nine continuous phenotypic  
200 traits, with varying heritability (0.03, 0.1, 0.5) and polygenicity (0.0001, 0.005, 0.1). We assumed

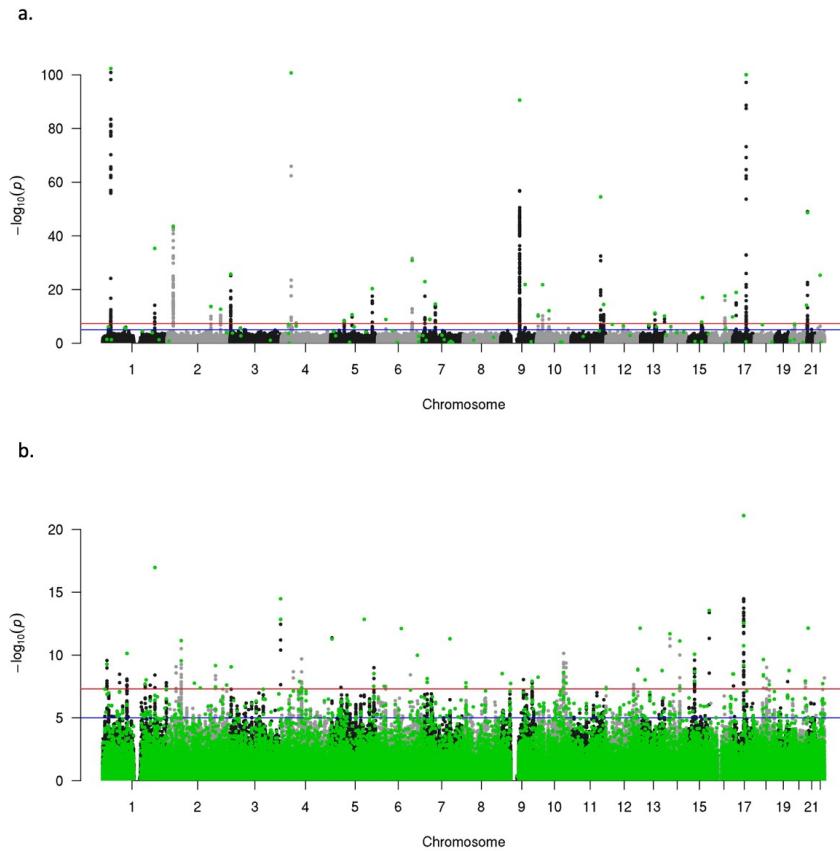


Figure 7: **Example GWAS Manhattan plots for phenotypes under various genetic architectures.** Colored in green are causal SNPs on trait liability under each setup. a. Phenotype with low heritability (0.1) and low polygenicity (0.0001, i.e. approximately 0.01% of total SNPs having causal effects on trait liability); b. Phenotype with high heritability (0.9) and high polygenicity (0.1, i.e. approximately 10% of total SNPs having causal effects on trait liability).

201 a genetic correlation of 1 across all ancestry groups.

202 The evaluation of the PRS methods is based on the reference-standardised framework of Pain  
203 et al. [4], where for continuous traits, the PRS performance is measured in terms of Pearson  
204 correlation between the predicted and observed values. The optimal parameters for each PRS  
205 method are identified using cross validation (CV), or pseudovalidation (PseudoVal), if CV is not  
206 available.

207 Better predictive performance is observed for higher heritability, lower polygenicity architectures  
208 (Supplementary, Figure 15). No single PRS method was observed to perform best across all genetic  
209 architectures. Methods with sparsity-inducing shrinkage priors (e.g. PRScs) were observed to  
210 perform better for higher heritability, lower polygencity architectures, where genetic effects on most

211 SNPs are zero (Figure 8, Panel c), while other approaches such as MegaPRS performed better for  
 212 lower heritability, higher polygenicity architectures (Figure 8, Panel a). Multi-ancestry results  
 213 replicate known issues with transferability of polygenic risk scores based on European-ancestry  
 214 summary statistics (Figure 8, Panels b and d).

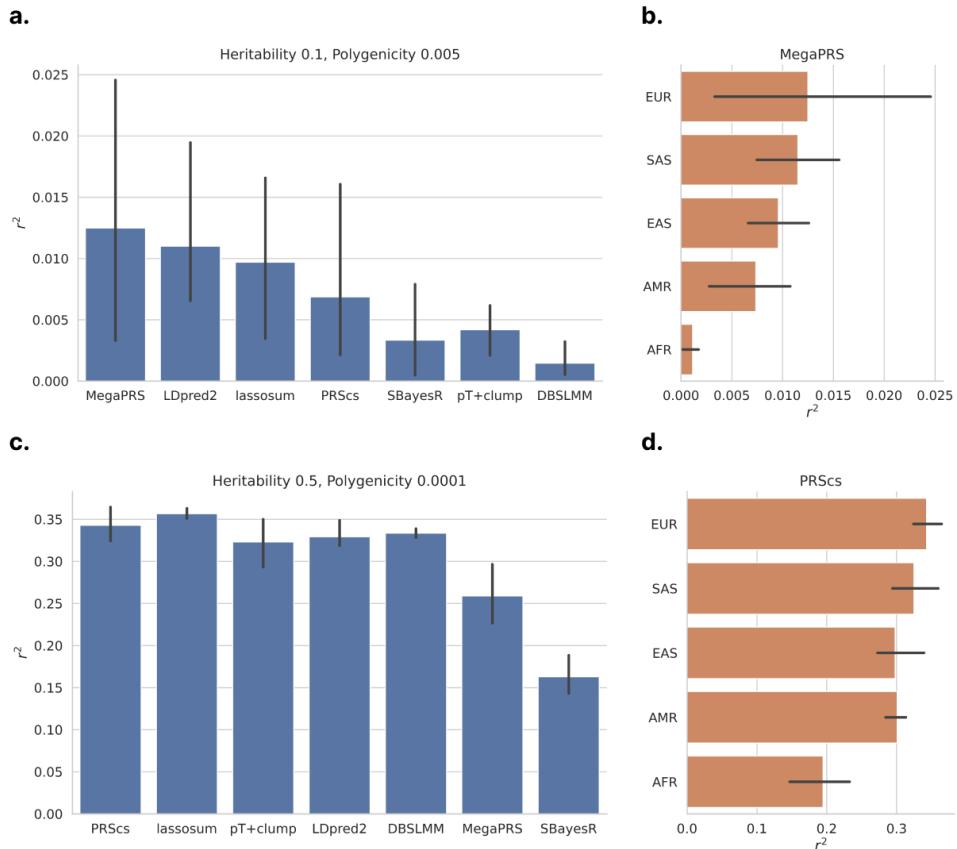


Figure 8: PRS results for two genetic architectures, averaged across 3 experiment trials with error bars showing the range of outcomes, for HapMap3 variants across 22 chromosomes. **a.** Pearson correlation between predicted and observed values, for various PRS methods and a European-ancestry phenotype with heritability 0.1 and polygenicity 0.005. **b.** Pearson correlation for various target ancestry groups for the best-performing PRS method (MegaPRS) for the heritability 0.1 and polygenicity 0.005 phenotype. **c.** Pearson correlation between predicted and observed values, for various PRS methods and a European-ancestry phenotype with heritability 0.5 and polygenicity 0.0001. **d.** Pearson correlation for various target ancestry groups for the best-performing PRS method (PRScs) for the heritability 0.5 and polygenicity 0.0001 phenotype.

### 215 3 Discussion

216 In this study, we proposed HAPNEST, a new algorithm to generate realistic individual-level ge-  
217 netic and phenotypic data and provide an efficient implementation. HAPNEST meets the demand  
218 for diverse, biobank-scale genomic data by improving scalability compared to existing methods.  
219 Users can customise population parameters or use parameter estimates derived from the reference  
220 dataset. Previous studies have been inconsistent in their approach to evaluating the quality of the  
221 generated synthetic data. We provide a comprehensive set of measures to be used for data quality  
222 evaluation that have been proposed in the statistical genetics and differential-privacy literature [24].  
223 Genotype generation, phenotype generation and evaluation modules are wrapped in user-friendly  
224 Docker or Singularity containers, where each module can be run independently.  
225 Synthetic genotypes are generated by copying and assembling haplotype segments from the refer-  
226 ence genome, with distribution of segment length determined by specifics of the target population,  
227 including recombination rates, effective population size and samples in the reference panel. Pa-  
228 rameters are optimised through the ABC algorithm, which typically results in an output dataset  
229 well-balanced across fidelity and generalisability metrics. On top of that, we introduced mutations  
230 to the synthetic genome to reduce similarity across individuals. Our approach is, in spirit, similar  
231 to HAPGEN2, but to improve computational scalability and generalisability we have introduced  
232 modeling of varying, rather than constant, coalescence time, and the use of mutation ages to de-  
233 termine if mutations are present in synthetic samples.  
234 From our systematic evaluations and experiments, we noticed some general trade-offs in synthetic  
235 data quality and in the parameter selection. One trade-off occurs between the preservation of pop-  
236 ulation LD structure and synthetic sample relatedness when constructing large synthetic datasets  
237 from much smaller reference datasets. Our observations indicated that parameters optimising the  
238 preservation of LD usually result in higher levels of sample relatedness, as LD typically comes with  
239 larger average segment length copied from the reference. On the other hand, shortened segments  
240 allow more combinations and higher sample level variability, which results in samples that are less  
241 related to each other but increased fragmentation in the LD structure. Furthermore, smaller seg-  
242 ments lead to more computational input/output operations when constructing synthetic data files  
243 and a slight increase in running time. Segments copied from the reference genome in our algorithm

244 can be conceptually viewed as identity-by-descent (IBD) segments in population genetics [25, 26].

245 As can be seen in equation 2, recombination events ( $\rho_s$ ) happen over time ( $T$ ) in the population.

246 Thus, IBD segments degrade over time, which also shows an impact on LD [27, 28]. Our algorithm

247 also provides an implementation of generating “admixed” samples by sampling from multiple ref-

248 erence populations under user defined compositions. However, we would like to note that this

249 approach does not accurately reflect the process of multi-population diverging and intermixing,

250 therefore it should be used and interpreted carefully.

251 Compared to other methods, HAPNEST-generated genotypes demonstrated better diversity and

252 generalisability which are essential features when scaling to large sample sizes. While the genetic

253 relatedness analysis indicated that the genotypes are sufficiently different from the reference data,

254 a nearest-neighbour adversarial accuracy close to 0.5 indicates that statistically speaking, it would

255 be difficult to discern a synthetic genotype from a real genotype. These properties of synthetic

256 datasets are desirable in the context of data privacy, where we may want to create a synthetic twin

257 of sensitive data that preserves key statistical properties of the real data, but cannot be traced

258 back to real individuals. However, we note that the criteria used in our analysis are not sufficient

259 for differential privacy guarantees, and we advise to use HAPNEST, or any of the reference-based

260 generation methods, only on publicly-available genomics datasets.

261 Once individual level genotypes have been generated, we can subsequently assign phenotypes to

262 each sample as an aggregation of polygenic effects, non-genetic effects and environmental noise. We

263 also implemented population-specific phenotypic effects by assuming shared causal variants across

264 populations with distinct but correlated effect sizes, and multi-trait simulation allowing for different

265 genetic correlation and pleiotropy models.

266 We believe our tool can benefit the community especially for GWAS related method development,

267 for which one of the examples can be PRS computation and evaluation. HAPNEST allows re-

268 searchers to assess the validity of genetic scoring methods under a broad variety of setups, including

269 cross-ancestry, trans-diagnostic, and different genetic architectures. Here, as a demonstration of its

270 utility, we applied PRSpipe<sup>2</sup> to synthetic data generated by HAPNEST and found that our results,

271 to a great degree, replicated what has been observed by Pain et. al [4]. As widely discussed, we

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<sup>2</sup>PRSpipe is a Snakemake pipeline developed to calculate and evaluate polygenic risk scores from GWAS summary statistics. It implements and extends the GenoPred [4] pipeline, a reference standardized framework for the prediction of PRS using various state-of-the-art methods.

272 found lower cross-ancestry portability of PRSs derived in a single ancestry. For a given phenotype,  
273 we set genetic correlations between ancestry groups to 1 and this might be higher than what is  
274 observed in real settings and result in slightly inflated trans-ethnic PRS prediction performance.  
275 Nevertheless, we still observed reduced prediction accuracy in non-European samples, indicating  
276 the synthetic genotype captured the differences of MAF and LD structures across populations. Re-  
277 sults under different genetic architectures are concordant with the general expectation: we observe  
278 better performance of PRS for phenotypes with higher heritability and lower polygenicity due to  
279 the existence of few variants with larger effect that explain large amounts of phenotypic variance.  
280 We also noticed that the best performing method can depend on different genetic architecture,  
281 reflecting the need for careful considerations when choosing a PRS method. As more studies come  
282 online that examine the clinical utility of PRSs, it will be important to have a reference dataset  
283 where old and new PRS methods can be compared and their robustness can be assessed as a func-  
284 tion of the genetic and phenotypic architecture. We used HAPNEST to create one of the largest  
285 genomics synthetic datasets today including 1 million individuals across 6 major continental ances-  
286 try groups, 6.8 million variants and 9 phenotypes. We hope this dataset can generate a reference  
287 set for deriving and testing PRS methods within a unified framework.

## 288 4 Data availability

289 We have made available a pre-simulated synthetic dataset for 1,008,000 individuals and 9 continuous  
290 phenotypic traits for over 6.8 million SNPs and 6 ancestry groups at <https://www.ebi.ac.uk/biostudies/studies/S-BSST936>. There is also a smaller example dataset available at this link.  
291

## 292 5 Code availability

293 The HAPNEST software is available at [https://github.com/intervene-EU-H2020/synthetic\\_data](https://github.com/intervene-EU-H2020/synthetic_data). The software can be used to simulate synthetic datasets and evaluate synthetic data quality.  
294

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