

# 1 Unsupervised seizure localisation

## 2 with attention-based graph neural

### 3 networks

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18 **Abstract** Graph neural networks (GNNs) and the attention mechanism are two of the most  
19 significant advances in artificial intelligence methods over the past few years. The former are  
20 neural networks able to process graph-structured data, while the latter learns to selectively focus  
21 on those parts of the input that are more relevant for the task at hand. In this paper, we propose  
22 a methodology for seizure localisation which combines the two approaches.

23 Our method is composed of several blocks. First, we represent brain states in a compact way by  
24 computing functional networks from intracranial electroencephalography recordings, using  
25 metrics to quantify the coupling between the activity of different brain areas. Then, we train a  
26 GNN to correctly distinguish between functional networks associated with interictal and ictal  
27 phases. The GNN is equipped with an attention-based layer which automatically learns to identify  
28 those regions of the brain (associated with individual electrodes) that are most important for a  
29 correct classification. The localisation of these regions is fully unsupervised, meaning that it does  
30 not use any prior information regarding the seizure onset zone.  
31 We report results both for human patients and for simulators of brain activity. We show that the  
32 regions of interest identified by the GNN strongly correlate with the localisation of the seizure  
33 onset zone reported by electroencephalographers. We also show that our GNN exhibits  
34 uncertainty on those patients for which the clinical localisation was also unsuccessful,  
35 highlighting the robustness of the proposed approach.

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#### 37 **Introduction**

38 Epilepsy is a neurological disorder characterised by recurrent episodes of excessive neuronal firing  
39 (*Stafstrom and Carmant, 2015*). In approximately a third of the patients, epilepsy cannot be treated  
40 with anti-seizure drugs and resective surgery can be considered as a possible treatment (*Kwan and*

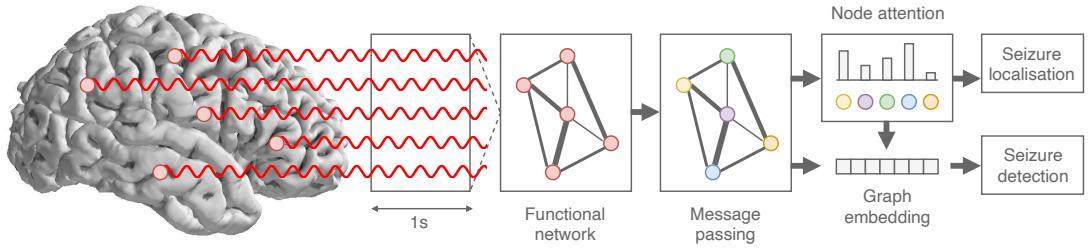
41 **Brodie, 2000**). The outcome of surgery is crucially dependent on the successful localisation of the  
42 seizure onset zone (SOZ) (**Burns et al., 2014; Van Mierlo et al., 2014**).

43 Electroencephalography (EEG) is the mainstay for studying and diagnosing epilepsy, and it is  
44 widely used to detect, classify, and localise seizures by recording and processing the electrical ac-  
45 tivity of groups of neurons (**Nunez et al., 2006**). However, due to their low spatial resolution, scalp  
46 EEG recordings in some cases are not informative enough to successfully localise seizures (**Shah**  
47 **and Mittal, 2014**). In these cases, intracranial EEG recordings (iEEG), in which electrodes are placed  
48 directly on or within the brain, provide better spatio-temporal resolution to capture the dynamics  
49 of seizure generation and propagation (**Hashiguchi et al., 2007**). However, the high temporal res-  
50 olution of iEEG and the complex functional interaction of distant brain areas, especially during  
51 seizures, make the interpretation and processing of raw iEEG data a non-trivial task for clinicians.  
52 For this reason, a significant branch of epilepsy research is concerned with summarising iEEG data  
53 by considering the pairwise (statistical) dependencies between the activity of different brain ar-  
54 eas over time (**Van Mierlo et al., 2014**). These dependencies are usually represented by *functional*  
55 *networks* (FNs), in which each node represents a sensor and edges are weighted by a *functional*  
56 *connectivity* (FC) metric (**Bastos and Schoffelen, 2016**).

57 FNs are a widespread tool to study seizure localisation, with early approaches dating back to the  
58 1970s (**Gersch and Goddard, 1970; Brazier, 1972**). Seizures have been observed to affect the func-  
59 tional organisation of brain activity at the meso-scale, both from a node-centric (**Burns et al., 2014**)  
60 and an edge-centric (**Khambhati et al., 2015**) perspective. In particular, **Burns et al. (2014)** identified  
61 sets of brain states that emerge by clustering FNs, consistent in interictal and ictal periods for in-  
62 dividual patients. They observed that changes in node centrality in FNs accurately predict the SOZ.  
63 **Khambhati et al. (2015)** observed a strengthening of FC in the SOZ during seizures, also coinciding  
64 with a topological tightening of the connections (i.e., strong connections also become physically  
65 closer). **Khambhati et al. (2016)** proposed *virtual cortical resection*, i.e., the removal of nodes from  
66 FNs, in order to study changes in network synchronizability, which is a known predictor for the  
67 spread of seizures (**Schindler et al., 2008**). **Lopes et al. (2017)** also observed that the resection of  
68 brain areas associated to *rich-club* hubs in FNs is correlated with a good post-operative outcome.  
69 Seizure localisation has also been studied in FNs obtained from functional magnetic resonance  
70 imaging (fMRI) (**Lee et al., 2014; Weaver et al., 2013**) and scalp EEG (**Staljanssens et al., 2017**) data.  
71 Recent work by **Covert et al. (2019)** introduced the use of spatio-temporal graph convolutional net-  
72 works (ST-GCNs) (**Yu et al., 2017**) to perform seizure detection, and conducted an *ex post* analysis  
73 similar to the one of **Khambhati et al. (2016)** to quantify the importance of a node by observing  
74 the effect of its removal on the downstream detection accuracy. **Gadgil et al. (2020)** also proposed  
75 a methodology based on ST-GCNs that allows identifying high-interest areas in fMRI by learning  
76 to estimate edge importance, although they did not apply it to seizure localisation. For a more  
77 in-depth review of approaches to seizure localisation with FNs, we refer the reader to **Van Mierlo**  
78 **et al. (2014)**.

79 The aim of this paper is to use the representation of brain states as FNs in order to automate  
80 the localisation of seizures using deep learning. Advances in deep learning techniques over the  
81 past decade have revolutionised how high-dimensional, high-volume data can be used in the con-  
82 text of artificially intelligent systems. In particular, deep learning techniques for computer vision  
83 have shown how artificial intelligence can be successfully adopted in clinical settings to aid human  
84 experts in their decision making (**Litjens et al., 2017**). Despite these successes, traditional deep  
85 learning methods are limited to processing regular structures like images and time series, and  
86 cannot naturally consider the relations that exist in a complex system with multiple interacting  
87 components, such as those described by FNs evolving over time. For this reason, recent literature  
88 has seen the rise of Graph Neural Networks (GNNs) (**Battaglia et al., 2018; Bronstein et al., 2017**)  
89 as a generalisation of deep learning techniques to process data represented as arbitrary graphs.

90 In this paper, we introduce a GNN-based methodology for seizure localisation, using FNs to effi-  
91 ciently represent brain states. The core of our algorithm is a GNN equipped with an *attention-based*



**Figure 1.** Schematic view of our GNN-based pipeline for seizure detection and localisation. Starting from raw iEEG data, we compute a functional network to represent the spatio-temporal dynamics of the signals in a compact way. The FN is then given as input to a GNN composed of an edge-aware message passing operation followed by an attention-based readout to compute a graph-level embedding. The embedding is then classified to perform seizure detection, while the attention scores are analysed to perform seizure localisation.

92 *readout*. By training such a GNN to perform seizure detection, the readout automatically learns to  
 93 assign a higher attention to those nodes that are more important for a correct classification. Then,  
 94 we propose a simple and fast way of analysing the attention coefficients over time, so that we  
 95 obtain a ranking of the nodes based on their overall importance in detecting a seizure. Crucially,  
 96 our methodology does not require *a priori* information regarding the SOZ, but only weak supervi-  
 97 sion in the form of annotated seizure onsets and offsets. The localisation procedure is, therefore,  
 98 unsupervised. A schematic representation of our approach is shown in Figure 1.

99 We validate the proposed methodology on clinical iEEG data collected from eight human sub-  
 100 jects and show that the electrode rankings computed with our localisation procedure are highly  
 101 correlated with the true SOZs. We also validate our algorithm on simulated data, using a simple  
 102 model of seizure initiation (**Benjamin et al., 2012**) and a more complex brain simulator (**Sanz Leon**  
 103 **et al., 2013**) based on the Epileptor model (**Jirsa et al., 2014**). Our main contributions and results  
 104 are summarised as follows:

- 105 • We present a new algorithm for unsupervised seizure localisation based on GNNs, which uses  
 106 FN to represent brain states in a compact form and requires no explicit supervision on the  
 107 SOZ;
- 108 • We show that the attention coefficients learned by the GNN correlate with clinically-identified  
 109 SOZs and accurately predict the presence of ictal activity;
- 110 • We show that, when electroencephalographers were not able to identify the SOZ from the  
 111 iEEG data, the GNN also shows uncertainty in the localisation;
- 112 • We show that, as expected, the choice of FC metric used to estimate FNs is important for an  
 113 accurate localisation;
- 114 • Finally, we show that our methodology performs well on very imbalanced datasets, achieving  
 115 a good localisation accuracy even on patients for which we observe as few as five seizures  
 116 during training.

## 117 Methods

118 **Notation.** We denote a time series  $x_i(t)$  to represent the  $i$ -th iEEG channel at time  $t$ . We define  
 119 a graph as a tuple  $\mathcal{G} = (\mathcal{V}, \mathcal{E})$ , where  $\mathcal{V} = \{v_1, \dots, v_N\}$  represents the set of attributed nodes with  
 120 attributes  $v_i \in \mathbb{R}^F$ , and  $\mathcal{E} = \{e_{i \rightarrow j} | v_i, v_j \in \mathcal{V}\}$  represents the set of attributed edges with attributes  
 121  $e_{i \rightarrow j} \in \mathbb{R}^S$  indicating a directed edge between the  $i$ -th and the  $j$ -th node. We indicate the neighbour-  
 122 hood of node  $i$  with  $\mathcal{N}(i) = \{v_k | e_{k \rightarrow i} \in \mathcal{E}\}$ . We say that a graph is undirected if  $e_{i \rightarrow j} \in \mathcal{E} \iff e_{j \rightarrow i} \in \mathcal{E}$ .  
 123 Note that in the text, for simplicity, we refer to nodes by means of their index, e.g., node  $i$ .

124 **Functional networks**

125 Choosing a suitable FC metric to model the pairwise interaction between brain areas is a non-trivial  
 126 challenge, as there exist a large variety of methods with their own advantages and disadvantages.  
 127 FC metrics can be characterised according to several properties, including whether they are in the  
 128 time or frequency domain, whether they are directed or undirected (*i.e.*, if they model asymmetric  
 129 or symmetric couplings), or whether they are model-free or model-based (**Bastos and Schoffelen**,  
 130 **2016**). Here, we focus on undirected FC metrics to simplify the GNN computation, and on model-  
 131 based approaches to reduce the computational costs of estimating the FC metrics directly from  
 132 data. We do, however, consider two different metrics to highlight the practical differences that  
 133 emerge between time- and frequency-domain metrics.

134 FNs are generated by computing a FC value for each pair of iEEG channels  $x_a(t)$  and  $x_b(t)$  over a  
 135 time window of length  $T$ . For the time-domain metric, we consider Pearson's correlation coefficient:

136

$$\mathbf{e}_{a \rightarrow b} = \mathbf{e}_{b \rightarrow a} = \frac{\sum_{t=1}^T (x_a(t) - \bar{x}_a)(x_b(t) - \bar{x}_b)}{\sqrt{\sum_{t=1}^T (x_a(t) - \bar{x}_a)^2} \sqrt{\sum_{t=1}^T (x_b(t) - \bar{x}_b)^2}}, \quad (1)$$

137 where  $\bar{x}_a = \frac{1}{T} \sum_{t=1}^T x_a(t)$  and analogously for  $\bar{x}_b$ . Correlation allows to quantify symmetric linear in-  
 138 teractions, it is easy to compute and, as such, it is often used in the literature. For the frequency  
 139 domain, we consider the phase-locking value (PLV) (**Lachaux et al.**, 1999):

$$\mathbf{e}_{a \rightarrow b} = \mathbf{e}_{b \rightarrow a} = \left| \frac{1}{T} \sum_{t=1}^T e^{i(\varphi_a(t) - \varphi_b(t))} \right|, \quad (2)$$

140 where  $\varphi_a(t)$  indicates the instantaneous phase of signal  $x_a(t)$  obtained via Hilbert transform (and  
 141 similarly for  $\varphi_b(t)$ ). A significant advantage of PLV over correlation is that it is less sensitive to arti-  
 142 facts in the iEEG signals (such as those caused by the patient's movements). After computing the  
 143 FC metrics for each pair of channels, we sparsify the resulting FNs by removing those edges for  
 144 which  $|\mathbf{e}_{i \rightarrow j}| < 0.1$ , *i.e.*, those indicating weak coupling.

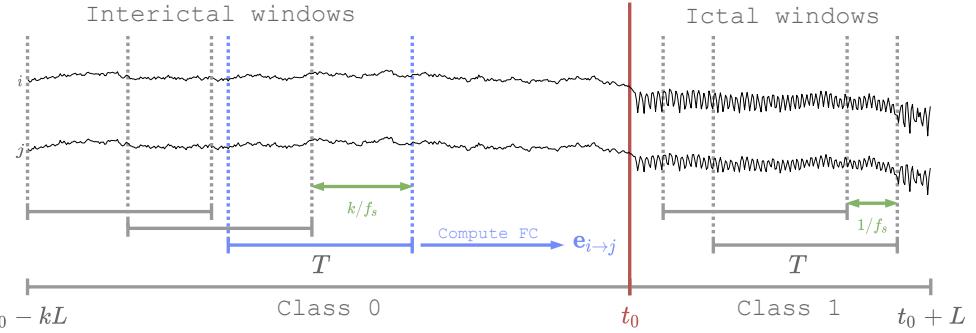
145 We generate a dataset of FNs for each patient, dividing the FNs into ictal and interictal classes  
 146 and proceeding in a per-seizure fashion. Let  $f_s$  be the sampling rate of the iEEG signal,  $L$  the  
 147 duration of a seizure,  $t_0$  the time indicating the seizure onset,  $k \geq 1$  a subsampling factor, and  $T$   
 148 the length of the time windows. Additionally, let  $y(t) \in \{0, 1\}$  be a binary signal indicating whether  
 149 the patient is having a seizure at time  $t$  (*i.e.*,  $y(t) = 1$  if  $t \geq t_0$  and 0 otherwise). Note that we consider  
 150 each seizure to end at time  $t_0 + L$  and we do not compute FNs for the data immediately following  
 151 a seizure offset.

152 Given a time window  $[t - T, \dots, t]$ , we compute a FN  $\mathcal{G}^{(t)}$  and label it with class

$$\mathcal{Y}^{(t)} = \begin{cases} 1, & \text{if } \sum_{\tau=t-T}^t y(\tau) > T/2 \\ 0, & \text{otherwise.} \end{cases} \quad (3)$$

153 To generate the FNs associated with seizures (class 1), we consider the data interval  $[t_0 - T/2, \dots, t_0 +$   
 154  $L]$  and take overlapping windows of size  $T$  with a stride of  $1/f_s$ . For the interictal FNs (class 0), in-  
 155 stead, we consider a longer period preceding the seizure onset,  $[t_0 - kL, \dots, t_0 + T/2]$ , and we take  
 156 windows at a larger stride of  $k/f_s$ . In this work, we consider  $k = 10$  and  $T = 1$ s for all experiments,  
 157 although other values are possible.

158 This procedure to generate the FNs (summarised in Figure 2) results in a balanced dataset and  
 159 has two advantages. First, it allows us to fully use all the available (and rare) ictal events. Second, it  
 160 allows us to consider a more diverse sample for the interictal class. The small differences between  
 161 consecutive FNs of the positive class, due to the small stride at which windows are taken, can be  
 162 seen as a form of sample weighting to account for the class unbalance characterising the problem.



**Figure 2.** Schematic representation of the procedure used to generate FNs. For each seizure of length  $L$  starting at  $t_0$  (marked in red), we consider an interictal interval of length  $kL$ . Interictal FNs are generated taking windows of length  $T$  at stride  $k/f_s$ , while ictal windows are taken with stride  $1/f_s$  (in green). For each window and each pair of electrodes  $i$  and  $j$ , we compute the FC value  $e_{i \rightarrow j}$  (in blue) to obtain the full FN. This figure is only meant to represent the procedure and is not shown in any physical temporal scale.

163 In order to have initial node features that can be processed by the GNN, we consider dummy  
 164 attributes set to 1 for all nodes. Other choices that depend on the actual iEEG signals are possible  
 165 (e.g., the signal power or wavelet coefficients) but were not explored in this work.

166 **Attention mechanism**

167 Attention (*Bahdanau et al., 2014; Vaswani et al., 2017*) is a processing technique for neural net-  
 168 works to learn how to selectively focus on parts of the input. Originally developed for aligning  
 169 sentences in neural machine translation (*Bahdanau et al., 2014; Vaswani et al., 2017*), the atten-  
 170 tion mechanism has been used to achieve state-of-the-art results on different tasks like language  
 171 modelling (*Brown et al., 2020*), image processing (*Xu et al., 2015*), and even learning on graphs  
 172 (*Velickovic et al., 2018*).

173 In this paper, we focus on the concept of *self*-attention, which indicates a class of attention  
 174 mechanisms that learn to attend to the output of a layer using the output itself (in contrast to  
 175 classical attention, which uses the output of one layer to focus on the output of another – e.g., the  
 176 sentence of the source language is used to focus on the target language). At its core, self-attention  
 177 consists of computing a compatibility score  $\alpha_{ij} \in [0, 1]$  between two vectors  $\mathbf{h}_i, \mathbf{h}_j \in \mathbb{R}^F$  (both part  
 178 of the same sequence, image, graph, etc.):

$$\alpha_{ij} = \text{Softmax}_j(e_{ij}) = \frac{\exp(e_{ij})}{\sum_{k=1}^N \exp(e_{ik})}, \quad (4)$$

179 where

$$e_{ij} = a(\mathbf{h}_i, \mathbf{h}_j) \quad (5)$$

180 and  $a$  is called an *alignment* model, which is usually learned end-to-end along with the other pa-  
 181 rameters of the neural network. The compatibility score is then used to compute a representation  
 182 of element  $i$  as:

$$\mathbf{z}_i = \sum_j \alpha_{ij} \mathbf{h}_j. \quad (6)$$

183 Intuitively, the attention mechanism learns the importance of element  $j$  to describe element  $i$ , and  
 184 computes score  $\alpha_{ij}$  to quantify this importance. The alignment model can be seen as a similarity  
 185 function between the two elements, which is then normalised via the Softmax function. Different  
 186 implementations of the alignment model are possible, although often it is implemented as a multi-  
 187 layer perceptron.

188 Attention mechanisms are usually trained without direct supervision and automatically learn to  
 189 focus on different parts of the data according to the loss of the given task. By optimising the overall  
 190 task loss, the attention layers in a neural network learn to compute the optimal compatibility scores.

191 This is a key aspect of our proposed methodology, where we use self-attention to automatically  
 192 detect those brain areas (monitored via different iEEG channels) that are important to detect a  
 193 seizure.

194 **Graph neural networks for seizure localisation**

195 Graph Neural Networks (GNNs) are a class of neural networks designed to perform inference on  
 196 graph-structured data (*Battaglia et al., 2018*). At their core, GNNs learn to represent the nodes  
 197 of a graph by propagating information between connected neighbours, whereas a global repre-  
 198 sentation of the entire graph is usually obtained by computing a *readout* of the nodes, like a sum,  
 199 average, or component-wise maximum vector. In this work, we focus on the family of *message-  
 200 passing* networks (*Gilmer et al., 2017*), in which the  $l$ -th layer maps the attributes  $\mathbf{h}_i^{(l-1)} \in \mathbb{R}^{F^{(l-1)}}$  of  
 201 the  $i$ -th node to:

$$\mathbf{h}_i^{(l)} = \gamma \left( \mathbf{h}_i^{(l-1)}, \square_{j \in \mathcal{N}(i)} \phi \left( \mathbf{h}_i^{(l-1)}, \mathbf{h}_j^{(l-1)}, \mathbf{e}_{j \rightarrow i} \right) \right), \quad (7)$$

202 where  $\mathbf{h}_i^{(l)} \in \mathbb{R}^{F^{(l)}}$ ,  $\mathbf{h}_i^{(0)} = \mathbf{v}_i$ , and  $\phi$  and  $\gamma$  are differentiable functions equivariant to node per-  
 203 mutations, respectively called the *message* and *update* functions, while  $\square$  is a permutation-invariant  
 204 function (such as the sum or the average) to aggregate incoming messages.

205 Many recent papers have introduced methods for graph representation learning based on this  
 206 general scheme, with different implementations ranging from polynomial (*Defferrard et al., 2016*)  
 207 or rational (*Bianchi et al., 2019*) graph convolutional filters, to attentional mechanisms (*Velickovic  
 208 et al., 2018*). In most of these works the creation of messages is only dependent on the node  
 209 attributes, although some methods have been proposed that also explicitly take edge attributes  
 210 into account (*Simonovsky and Komodakis, 2017; Schlichtkrull et al., 2018*). In particular, the Edge-  
 211 Conditioned Convolutional (ECC) operator proposed by Simonovsky and Komodakis (*Simonovsky  
 212 and Komodakis, 2017*) incorporates edge attributes into the message-passing scheme by using a  
 213 *kernel-generating network*  $f^{(l)}(\cdot)$  that dynamically computes messages between each pair of con-  
 214 nected nodes. An ECC layer is thus defined as:

$$\mathbf{h}_i^{(l)} = \mathbf{h}_i^{(l-1)} \cdot \mathbf{W}_{\text{root}}^{(l)} + \sum_{j \in \mathcal{N}(i)} \mathbf{h}_j^{(l-1)} \cdot f^{(l)}(\mathbf{e}_{j \rightarrow i}), \quad (8)$$

215 where  $\mathbf{W}_{\text{root}}^{(l)} \in \mathbb{R}^{F^{(l-1)} \times F^{(l)}}$  is a learnable kernel applied to the root node itself and the kernel-generating  
 216 network is usually a multi-layer perceptron  $f^{(l)} : \mathbb{R}^S \rightarrow \mathbb{R}^{F^{(l-1)} \times F^{(l)}}$ .

217 Our method for seizure localisation can be summarised as follows. First, we train a GNN with  
 218 an attention-based readout to detect seizures from FNs. This is a graph-level classification problem  
 219 where a label (ictal or interictal) is assigned to each FN. Then, we analyse the compatibility scores  
 220 learned by the attentional mechanism to identify those nodes that the model consistently consid-  
 221 ers as important. Although we train the GNN to do seizure detection in a supervised way, *i.e.*, it  
 222 requires manually-annotated seizure onsets and offsets, the localisation is fully unsupervised. This  
 223 is one of the main strengths of the proposed method, as significantly less manual work is required  
 224 to annotate the temporal boundary for each individual seizure, rather than the SOZ.

225 There are two main components in our GNN architecture. First, the connectivity information  
 226 is propagated to the node attributes via an edge-aware message-passing operation like ECC. A  
 227 single layer is sufficient because the input FNs are densely connected, and most nodes will receive  
 228 information from the whole graph in a single step of message passing.

229 Then, we use a self-attentional mechanism to compute the graph readout:

$$\mathbf{z} = \text{Attn-RO}(\mathbf{h}) = \sum_{j=1}^N \alpha_j \mathbf{h}_j \quad (9)$$

230 where

$$\alpha_j = \frac{\exp(\mathbf{h}_j \cdot \mathbf{a})}{\sum_{k=1}^N \exp(\mathbf{h}_k \cdot \mathbf{a})}, \quad (10)$$

231  $\mathbf{h}_j \in \mathbb{R}^{F^{out}}$  is the embedding of the  $j$ -th node computed by the ECC layer, and  $\mathbf{a} \in \mathbb{R}^{F^{out}}$  is a vector of  
 232 learnable weights. Note that, compared to Equation (6), here index  $i$  is left implicit as the attention  
 233 is only computed once for all nodes, to reduce the graph to a vector. This is also reflected in the  
 234 fact that the alignment model is a function of only one node at a time, e.g.,  $\mathbf{h}_j \cdot \mathbf{a}$ . For a more general  
 235 way of applying attention to every possible pair of nodes (while maintaining the graph structure),  
 236 see (Velickovic et al., 2018).

237 Finally, a multi-layer perceptron  $\text{MLP}(\cdot)$  with sigmoid activation computes the probability that  
 238 the input FN represents an ictal window of iEEG data.

239 The full architecture is written as:

$$\hat{y} = \text{MLP}(\text{Attn-RO}(\text{ECC}(\mathcal{G}))) \quad (11)$$

240 where  $\mathcal{G}$  represents an input FN (cf. Figure 1).

241 By training the GNN to correctly distinguish the ictal FNs from the non-ictal ones, we also implicitly  
 242 train the attentional readout Attn-RO to assign higher attention to those nodes of the FNs that  
 243 maximise the confidence in the prediction. We then analyse how the attention scores assigned  
 244 to nodes change over time, and rank the nodes according to the overall amount of attention that  
 245 they receive before and during a seizure. The localisation procedure is described in the following  
 246 section.

### 247 Localising the seizure onset zone

248 For each seizure in the data, we consider symmetric intervals of length  $2L$  centred at the seizure  
 249 onset, so that the first  $L$  timesteps are pre-ictal and the remaining  $L$  cover the beginning of the  
 250 seizure. For each of the  $2L$  timesteps, we compute a FN  $\mathcal{G}^{(t)}$  from a  $T = 1$ s window ending at time  
 251  $t$ , obtaining a sequence of FNs  $[\mathcal{G}^{(1)}, \dots, \mathcal{G}^{(2L)}]$  (this is equivalent to how we generate the training  
 252 datasets, except that the subsampling is set at  $k = 1$ ). For each FN in the sequence, we use the  
 253 GNN to compute the attention scores over the nodes according to Equation (10). We thus compute  
 254 a sequence of attention scores  $[\alpha_i^{(1)}, \dots, \alpha_i^{(2L)}]$  for each node  $i$ .

255 We then sum the sequence of attention scores to obtain the overall *importance* of the node  
 256 over the considered time interval:

$$\sigma_i = \sum_{t=1}^{2L} \alpha_i^{(t)}, \quad (12)$$

257 and normalise the importance scores to the  $[0, 1]$  interval as:

$$s_i^{(s)} = \frac{\sigma_i^{(s)} - \min_{j \in \mathcal{V}} \sigma_j^{(s)}}{\max_{j \in \mathcal{V}} \sigma_j^{(s)} - \min_{j \in \mathcal{V}} \sigma_j^{(s)}}. \quad (13)$$

258 Finally, we rank the nodes according to their importance and predict the SOZ accordingly.

## 259 Results

260 We report the results obtained on real iEEG data collected from eight patients. Additional results on  
 261 two brain activity simulators (a simple network model (Benjamin et al., 2012) and *The Virtual Brain*  
 262 simulator (Sanz Leon et al., 2013)) and all experimental details regarding the GNN are reported in  
 263 the appendix.

### 264 Data collection and pre-processing

265 We used iEEG data recorded from eight human subjects with medically refractory epilepsy, the  
 266 recordings obtained as part of their standard clinical pre-surgical investigations. The study was  
 267 approved by the Research Ethics Board at the University Health Network (ID number 12-0413) and  
 268 written consent for data collection was obtained from all participants. Each patient had a varying  
 269 number of recorded clinical seizures and the number of electrodes also varied from patient to  
 270 patient (cf. Table 1). The data was recorded from subdural or intracerebral depth electrodes at

**Table 1.** Summary of the patients considered for this study. The columns indicate (left-to-right): the number of recorded seizures, the number of implanted electrodes, the presence of ictal activity (IA) marked by electroencephalographers on one or more channels, whether the patient had surgery, and the outcome of the surgery.

Patient	Seizures	Electrodes	IA identified	Surgery	Outcome
66	15	100	Yes, low confidence	No	-
70	9	96	Yes	Yes	Seizures reduced
75	10	23	Yes	No	-
76	5	74	No	No	-
77	11	38	Yes	Yes	Seizures reduced
78	18	45	Yes, poorly defined	No	-
85	5	45	Yes	No	-
87	16	69	Yes	No	-

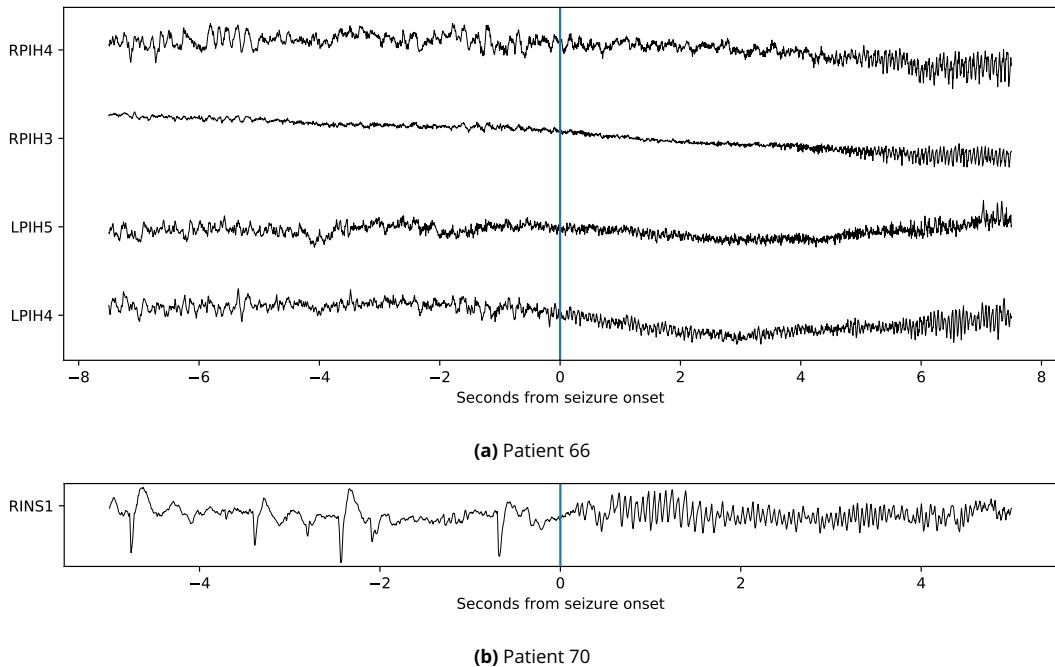
<sup>271</sup>  $f_s = 500\text{Hz}$  over the course of several days per patient, and seizures were manually annotated by  
<sup>272</sup> electroencephalographers, inspecting both raw iEEG and video recordings of the patient. The iEEG  
<sup>273</sup> signal was notch-filtered at 60Hz and related harmonics to remove powerline trends, and then  
<sup>274</sup> filtered with an order-3 low-pass filter at 100Hz to remove any high-frequency noise. Then, each  
<sup>275</sup> electrode channel was independently re-referenced to have zero mean and rescaled to have unit  
<sup>276</sup> variance.

<sup>277</sup> Before pre-processing, we visually inspected the raw data of each patient and each seizure to  
<sup>278</sup> assess the presence of bad channels: we considered symmetric windows around each labelled  
<sup>279</sup> seizure onset and we removed from the data any channels that exhibited abnormal (*i.e.*, either flat  
<sup>280</sup> or excessive) activity in at least one seizure.

### <sup>281</sup> **Per-patient analysis of the SOZ**

<sup>282</sup> This section reports the available clinical data for the patients considered in our study. For all pa-  
<sup>283</sup> tients, both the seizure onset time instants and the SOZ annotations were provided by electroen-  
<sup>284</sup> cephalographers.

<sup>285</sup> Patient 66 demonstrated ictal activity in both the left and right posterior interhemispheric re-  
<sup>286</sup> gions (Figure 3a), with interictal epileptiform discharges recorded independently from the left an-  
<sup>287</sup> terior frontal and right middle frontal lobes. The patient did not undergo resective surgery due to a  
<sup>288</sup> low confidence in the identification of the SOZ. Patient 70 showed clear seizures originating in the  
<sup>289</sup> right posterior insular region (Figure 3b). The patient underwent laser interstitial thermal therapy  
<sup>290</sup> targeting a focal cortical dysplasia in the area. The patient continued to have some post-operative  
<sup>291</sup> seizures, although these were reduced in frequency and intensity, indicating that the SOZ was iden-  
<sup>292</sup> tified correctly. Patient 75 had seizure onsets recorded independently from both temporal lobes  
<sup>293</sup> and thus was not a candidate for surgery. Patient 76 had no clear ictal activity identified by elec-  
<sup>294</sup> troencephalographers in the iEEG recordings and was thus not a candidate for surgery, the SOZ  
<sup>295</sup> evidently not captured by the intracranial electrode placements. Patient 77 demonstrated ictal ac-  
<sup>296</sup> tivity in the left hippocampal body, and underwent a left anterior temporal resection. The patient  
<sup>297</sup> continued to have seizures after the surgery, but of reduced frequency and intensity, indicating a  
<sup>298</sup> successful localisation of the SOZ. Patient 78 had multiple seizures recorded with poorly defined,  
<sup>299</sup> inconsistent ictal onsets over temporoparietal sensory cortex and was deemed not a candidate  
<sup>300</sup> for surgical resection due to uncertainty on the SOZ. Patient 85 had seizures recorded in the left  
<sup>301</sup> hemisphere, with onsets involving a broad region of temporal lobe neocortex. The patient was not  
<sup>302</sup> subject to resection due to the epileptogenic zone being too large, and near eloquent language  
<sup>303</sup> cortex. Patient 87 exhibited abnormal activity in the left amygdala and hippocampus. The patient  
<sup>304</sup> had already undergone contralateral right anterior temporal resective surgery years prior to the



**Figure 3.** Examples of raw iEEG traces for patients 66 and 70. The two plots show the activity of electrodes that were identified as SOZs by electroencephalographers. The vertical line marks the seizure onset, as reported in the patients' clinical records.

305 collection of the iEEG data and was not a candidate for further resections.

306 Table 1 summarises the relevant details of the eight patients. In particular, six patients had  
307 clinically-identified, well-defined information regarding the SOZ, whereas in two patients the SOZ  
308 could not be clearly identified in the iEEG data by electroencephalographers.

### 309 **Results on seizure detection and localisation**

310 Table 2 reports the average Area Under the Receiver Operating Characteristic Curve (ROC-AUC) and  
311 the Area Under the Precision-Recall Curve (PR-AUC) obtained by the GNN on the seizure detection  
312 task. We report the results obtained using both FC metrics (correlation and PLV) to generate the  
313 FNs. We also report the detection performance of a baseline convolutional neural network for time  
314 series classification (details in the Appendix).

315 The GNN achieved an average ROC-AUC score of 79.56 and an average PR-AUC of 81.24 (the aver-  
316 age is computed over all patients) when using correlation as FC metric. These results are aligned  
317 with the performance of the baseline, which our method slightly outperformed on average, and  
318 indicate that 1) our choice of architecture was reasonable and 2) using graph-structured data is  
319 an interesting direction for future research on efficient seizure detection. We also recall that the  
320 detection task is only meant to provide a weak supervision for the more interesting challenge of  
321 localisation, and that better detection results could be achieved by increasing the capacity of the  
322 GNN or collecting more training data.

323 Tables 3 and 4 report the performance of the model on the patients with a known SOZ, respec-  
324 tively using correlation and PLV to generate FNs. In particular, we report three main performance  
325 measures:

326 (a) the average precision at  $K$  (AP@ $K$ ) (Sanderson *et al.*, 2010) obtained by the GNN when com-  
327 puting an average ranking of the electrodes. Each electrode is re-ranked by considering five  
328 models trained on the same data and taking the average score assigned to each electrode  
329 over all models and all seizures. This measure quantifies the GNN's ability to correctly identify

**Table 2.** Average ROC-AUC score and average PR-AUC score for seizure detection on unseen test data. These scores represent the model's ability to correctly classify the FNs as interictal or ictal. The last row reports the average score over all patients. The highest ROC-AUC and PR-AUC scores are reported in bold for each patient.

Patient	Baseline		GNN Corr.		GNN PLV	
	ROC	PR	ROC	PR	ROC	PR
<b>66</b>	$62.54 \pm 22.5$	$70.06 \pm 17.8$	$68.63 \pm 11.43$	$75.20 \pm 10.30$	<b><math>75.68 \pm 23.3</math></b>	<b><math>77.51 \pm 20.1</math></b>
<b>70</b>	$80.19 \pm 15.5$	$85.96 \pm 10.6$	<b><math>86.87 \pm 9.07</math></b>	<b><math>89.04 \pm 9.35</math></b>	$65.36 \pm 20.1$	$72.91 \pm 14.8$
<b>75</b>	$82.32 \pm 14.19$	$87.25 \pm 9.24$	<b><math>93.35 \pm 3.12</math></b>	<b><math>94.34 \pm 2.72</math></b>	$71.50 \pm 14.8$	$71.02 \pm 16.3$
<b>76</b>	$67.81 \pm 8.75$	$69.83 \pm 13.12$	<b><math>60.40 \pm 14.41</math></b>	<b><math>61.11 \pm 14.82</math></b>	$53.83 \pm 6.6$	$51.67 \pm 6.4$
<b>77</b>	$76.18 \pm 15.41$	$80.42 \pm 14.26$	<b><math>77.04 \pm 11.98</math></b>	<b><math>76.39 \pm 13.03</math></b>	$71.46 \pm 12.1$	$71.45 \pm 12.9$
<b>78</b>	<b><math>76.32 \pm 17.2</math></b>	<b><math>80.94 \pm 13.5</math></b>	$73.72 \pm 17.14$	$76.02 \pm 14.53$	$63.81 \pm 17.2$	$71.06 \pm 12.4$
<b>85</b>	$76.46 \pm 11.24$	$81.22 \pm 7.65$	<b><math>85.52 \pm 10.95</math></b>	<b><math>85.92 \pm 13.65</math></b>	$69.32 \pm 2.6$	$65.55 \pm 1.8$
<b>87</b>	$85.60 \pm 14.6$	$89.29 \pm 10.7$	<b><math>90.97 \pm 5.51</math></b>	<b><math>91.89 \pm 3.49</math></b>	$77.69 \pm 11.5$	$78.32 \pm 11.3$
<b>Avg.</b>	$75.93 \pm 7.06$	$80.62 \pm 6.86$	<b><math>79.56 \pm 10.82</math></b>	<b><math>81.24 \pm 10.37</math></b>	$68.58 \pm 7.08$	$69.94 \pm 7.86$

330 the SOZ for a patient in general, which is the most clinically relevant scenario.

331 (b) The mean AP@K (MAP@K) obtained by the GNN on different individual seizures. In this case,

332 the ranking for each seizure is compared to the ground truth independently of the others (*i.e.*,

333 without averaging the scores), and the scores are averaged *a posteriori* (also considering five

334 repetitions of the experiments). This measure quantifies the GNN's ability to correctly identify

335 target electrodes in a given seizure.

336 (c) The MAP@K obtained by the GNN on different individual seizures, but considering groups of

337 electrodes belonging to the same strip (implying spatial locality of the electrodes). This allows

338 us to evaluate the performance of the model at a coarser scale.

339 From the results we see that, while correlation was a clearly better metric for the task of seizure

340 detection, the localisation performance can vary depending on the particular FC metric used. In

341 particular, the localisation for patients 66 and 77 was better when using correlation networks, but

342 PLV yielded better results for patients 75, 85, and 87.

343 In general, however, we note that the (M)AP@5 score is positive for both FC metrics, for all

344 performance measures and for all patients, meaning that at least one SOZ-associated electrode

345 was ranked in the top five every time. We also note that the GNN achieves a perfect AP@2 score

346 (average rankings) in six out of eight cases when using PLV, indicating a high chance of localising

347 at least two relevant electrodes per patient.

348 Remarkably, we see that these results were obtained even when considering small datasets,

349 *e.g.*, down to only five seizures for patient 85 (*cf.* Table 1).

### 350 Comparison with clinical information

351 Figure 5 summarises our results and provides an overview of the importance scores, their variabil-

352 ity across different models and seizures, and their agreement with the ground truth.

353 The results for patient 77 can be considered a complete success, with the highest AP@K scores

354 among all patients and very little uncertainty in the ranking by the GNN. Crucially, the successful

355 post-operative outcome confirms that the localisation of the SOZ for this patient was accurate

356 and points to a strong localisation ability of the GNN. For patient 70, ictal activity was evident and

357 well-localised on a specific depth electrode placed in the right insular complex (RINS1). The clinical

358 localisation of the SOZ was therefore likely accurate, even if the outcome of the surgery was not

359 completely successful. More importantly, we notice that the GNN was strongly aligned with the

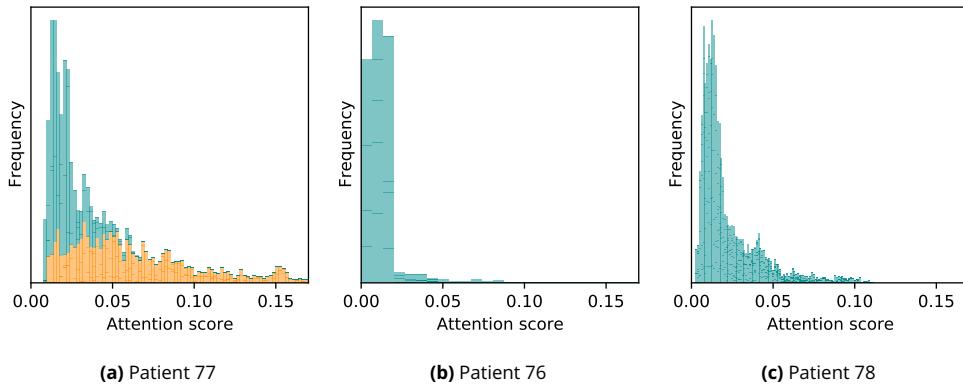
360 human analysis given the same information, and similarly focused on the same electrode (which

**Table 3.** Localisation performance for patients with a known SOZ, when using Pearson's correlation as FC metric. We report: **(a)** the average precision at  $K$  for averaged rankings, which evaluates the localisation for the patient overall; **(b)** the mean average precision at  $K$  for single rankings, which evaluates the localisation for a given seizure; **(c)** the mean average precision at  $K$  for single rankings and groups of electrodes, which is equivalent to (b) but at a coarser scale. We report scores for  $K = 2, 5, 10$ . Bold indicates that the results are better than the ones obtained with PLV as FC metric (cf. Table 4).

Patient	(a) AP@K - Avg. rank			(b) MAP@K - Single			(c) MAP@K - Groups		
	$K = 2$	$K = 5$	$K = 10$	$K = 2$	$K = 5$	$K = 10$	$K = 2$	$K = 5$	$K = 10$
66	<b>50.00</b>	<b>20.00</b>	<b>12.50</b>	<b>22.31</b>	<b>12.0</b>	<b>7.24</b>	<b>26.92</b>	<b>21.48</b>	31.64
70	<b>100.00</b>	<b>100.00</b>	<b>100.00</b>	<b>51.11</b>	<b>54.8</b>	<b>56.71</b>	<b>53.33</b>	<b>58.48</b>	<b>60.73</b>
75	0.00	16.67	38.96	20.37	26.51	28.98	36.11	45.09	50.07
77	<b>100.00</b>	<b>55.00</b>	<b>55.00</b>	<b>97.73</b>	<b>48.55</b>	<b>54.71</b>	<b>99.09</b>	<b>99.09</b>	<b>99.09</b>
85	0.00	0.00	0.00	0.00	2.71	5.43	25.00	53.75	64.42
87	0.00	6.67	5.56	<b>19.69</b>	<b>13.00</b>	<b>7.42</b>	<b>20.00</b>	<b>36.43</b>	<b>44.07</b>

**Table 4.** Localisation performance for patients with a known SOZ, when using PLV as FC metric. Bold indicates that the results are better than the ones obtained with correlation as FC metric (cf. Table 3).

Patient	(a) AP@K - Avg. rank			(b) MAP@K - Single			(c) MAP@K - Groups		
	$K = 2$	$K = 5$	$K = 10$	$K = 2$	$K = 5$	$K = 10$	$K = 2$	$K = 5$	$K = 10$
66	0.00	5.00	5.83	8.67	5.97	4.67	16.67	18.82	<b>31.78</b>
70	<b>100.00</b>	<b>100.00</b>	<b>100.00</b>	50.00	54.33	56.65	50.00	58.04	60.21
75	<b>100.00</b>	<b>55.00</b>	<b>45.46</b>	<b>60.00</b>	<b>40.82</b>	<b>32.58</b>	<b>66.88</b>	<b>45.16</b>	<b>51.36</b>
77	<b>100.00</b>	40.00	48.57	66.82	38.28	45.27	91.82	93.48	93.48
85	<b>100.00</b>	<b>40.00</b>	<b>28.29</b>	<b>70.00</b>	<b>40.40</b>	<b>25.43</b>	<b>66.00</b>	<b>65.02</b>	<b>78.35</b>
87	<b>50.00</b>	<b>20.00</b>	<b>10.00</b>	15.62	9.15	6.43	16.56	20.07	32.30



**Figure 4.** Histograms of the attention scores over a 2-second window starting from a seizure onset. Each bin represents the frequency with which the corresponding attention score is assigned to ten randomly-selected electrodes. Figure **(a)** shows a patient with a known SOZ, while Figures **(b)** and **(c)** show patients without a known SOZ. For Figure **(a)**, the contribution to each bin of those electrodes that are part of the SOZ ground truth are highlighted in orange. Note how the score distribution for SOZ-associated electrodes is spread out towards higher values, while for patients with no known SOZ the scores are similar for all channels.

361 is ranked first using either of the FC metrics). Our methodology also confirms the conclusions  
362 reached by electroencephalographers for patients 75, 85 and 87, although further studies would  
363 be required to give a more precise interpretation of the results (including, possibly, the outcome of  
364 future surgeries). The results for patient 87 are particularly uncertain, despite the GNN achieving a  
365 good detection accuracy (*cf.* Table 2). In general, however, the rankings provided by the GNN show  
366 a high agreement with the medical assessment in those cases where the SOZ was successfully  
367 identified.

368 For patients with no known SOZ (76, 78) the GNN has a low detection performance and the av-  
369 erage attention scores assigned by the GNN are uniformly distributed across all electrodes around  
370 an average score of 0.5. On the contrary, patients with a known SOZ have a few electrodes that are  
371 assigned a majority of the attentional budget. This difference between the two cases is more clearly  
372 visualised in Figure 4, which shows the distribution of the scores given to different electrodes at  
373 the seizure onset (patient 77 is taken as representative of the case in which the SOZ is known).

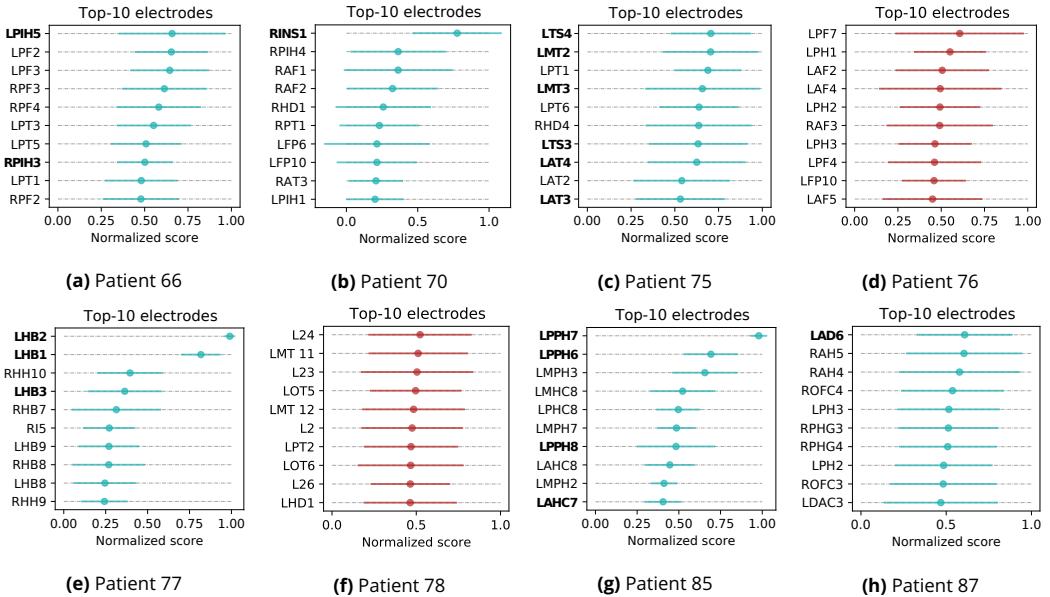
374 For patient 66, the GNN did not identify any particularly important regions despite there being  
375 some clinical evidence of ictal activity in the posterior interhemispheric region. Two posterior inter-  
376 hemispheric electrodes are indeed ranked in the top ten (averaged rankings) by the GNN when us-  
377 ing correlation FNs, although with a very high uncertainty. We note, however, that the uncertainty  
378 showed by the GNN was also reflected clinically in the electroencephalographers' interpretations  
379 and in the final decision to not operate this patient.

Our analysis for patients 66, 76, and 78 shows that the uncertainty of the GNN correlates with uncertainty or inability on the part of electroencephalographers to identify the SOZ in iEEG, and can still be useful to support their decision making (e.g., deciding to not operate a patient can be just as valuable as a successful localisation).

384 Discussion

385 Our work introduces a methodology for automated and unsupervised seizure localisation using  
386 graph-based machine learning. Our approach does not require any manual annotation of the SOZ  
387 in order to work, making it cheaper to train and easier to scale to a larger number of patients. Our  
388 method is also data-efficient: we were able to provide a good – and clinically verified – localisation  
389 using as little as five annotated seizures per patient.

390 The goal of the proposed approach is to provide a support tool for clinicians to allocate pre-  
391 cious resources in the analysis of iEEG data, and to improve the efficiency of the decision-making



**Figure 5.** Top ten electrodes when considering the averaged rankings. We report the ranking obtained with the best-performing FC metric for each patient, according to the AP@10 score for average rankings reported in Tables 3 and 4. The two plots in red indicate those patients for which the SOZ was not identified clinically. Bold labels indicate that the corresponding electrode was marked as a potential SOZ by electroencephalographers.

392 process. Crucially, in this regard, we note that our algorithm is conservative in scoring potential  
 393 SOZ candidates. When the SOZ was not identifiable by electroencephalographers, the GNN also  
 394 showed uncertainty in the scoring (rather than making high-confidence predictions). Contrarily,  
 395 a high importance score consistently correlated with clinically-identified SOZs. With this premise,  
 396 we believe that our approach could have practical value if deployed to epilepsy monitoring units  
 397 to provide a real-time analysis of iEEG recordings.

### 398 Future work

399 There are several directions for future research that could stem from this work. First, we note that  
 400 by 1) increasing the capacity of the network (in terms of parameters and depth), 2) performing a  
 401 patient-specific hyperparameter search, and 3) having more seizures on which to train the model,  
 402 it is likely that both the detection and localisation performance would significantly improve. Also,  
 403 a possible extension of the proposed methodology could be to explicitly introduce a supervised  
 404 objective to train the attentional readout using the available information on the SOZ. This would  
 405 require a per-seizure annotation of every electrode (or, even better, an annotation over time), but  
 406 could lead to a more accurate localisation. An interesting application of this methodology could  
 407 also be to provide a patient-agnostic localisation, by training the GNN concurrently on seizures of  
 408 different patients.

409 Future work could also explore more in-depth the use of different, combined FC metrics and  
 410 their impact on the detection and localisation performance. In fact, our results show that this  
 411 choice could lead to significantly different outcomes (as we showed with correlation and PLV). A  
 412 way to identify *a priori* the best FC metric to build FNs for a specific patient could bring significant  
 413 benefits.

### 414 Conclusion

415 We presented a methodology for unsupervised seizure localisation based on GNNs with an atten-  
 416 tion mechanism. Our approach takes advantage of a compact representation of brain states as

417 FNs, and uses machine learning methods for graph-structured data to automatically detect those  
418 regions of the brain that are important for localising seizure onsets. To train the GNN, it is suf-  
419 ficient to have seizure onset annotations, but no information regarding the SOZ is needed. We  
420 showed the effectiveness of our method in localising the SOZ on real-world data consisting of iEEG  
421 recordings from eight human subjects, using two different FC metrics to compute FNs. Our results  
422 show a very high accuracy in localising the SOZ. However, we also observed that the GNN exhibits  
423 uncertainty in those cases where human analysis was also uncertain, indicating a reliable and safe  
424 behaviour to support decision-making.

425 We believe that this work represents a step towards AI-aided analysis of iEEG data and could  
426 potentially lead to faster and more accurate treatment of epilepsy.

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## 518 Experiments on Simulated Data

### 519 Seizure generator from *Benjamin et al. (2012)*

520 In this experiment we considered a simple network model of seizure initiation presented by *Ben-*  
 521 *jamin et al. (2012)*, and also used by *Lopes et al. (2017, 2020)* to study the effect of network structure  
 522 on the generation of seizures. The model consists of a network of  $N$  bi-stable oscillators

$$\dot{z} = f(z) = (\lambda - 1 + i\omega)z + 2z|z|^2 - z|z|^4 \quad (14)$$

where  $z \in \mathbb{C}$ . Equation (14) describes a dynamical system with a stable fixed point at the origin of the complex plane (which we consider as interictal), and an oscillating attractor with frequency  $\omega$  (which we consider as ictal). Parameter  $\lambda$  controls the location of the oscillator in phase space. Nodes are interconnected in a graph described by adjacency matrix  $\mathbf{A}$  with a coupling factor  $\beta$ , such that the dynamic of a single node reads:

$$dz_i(t) = (f(z_i) + \beta \sum_{j \neq i} \mathbf{A}_{ji}(z_j - z_i)) + \alpha dW_i(t)$$

523 where  $W_i(t)$  is a stochastic Wiener process rescaled by a factor of  $\alpha$ .

524 All nodes in the model are initialised at the fixed point and, due to the presence of noise and  
 525 the interaction between nodes, eventually switch to the oscillation state. We identify the activity of  
 526 the whole system as ictal if any of the nodes meets the condition  $|\text{Re}(z_i)| > 1$ , and the SOZ as the  
 527 first node that escapes the fixed regime.

528 We consider a complete graph without self-loops to describe the interaction of the nodes. The  
 529 configuration of the parameters is summarised in Table 5. The hyperparameters used for creating  
 530 the FNs and training the GNN are the same ones that we used for the real iEEG data, and we only  
 531 report results obtained using PLV as FC metric.

**Appendix 0 Table 5.** Configuration used for the simulator by *Benjamin et al. (2012)*.

Parameter	Value
$N$	3
$\omega$	20
$\lambda$	0.5
$\beta$	0.1
$\alpha$	0.05

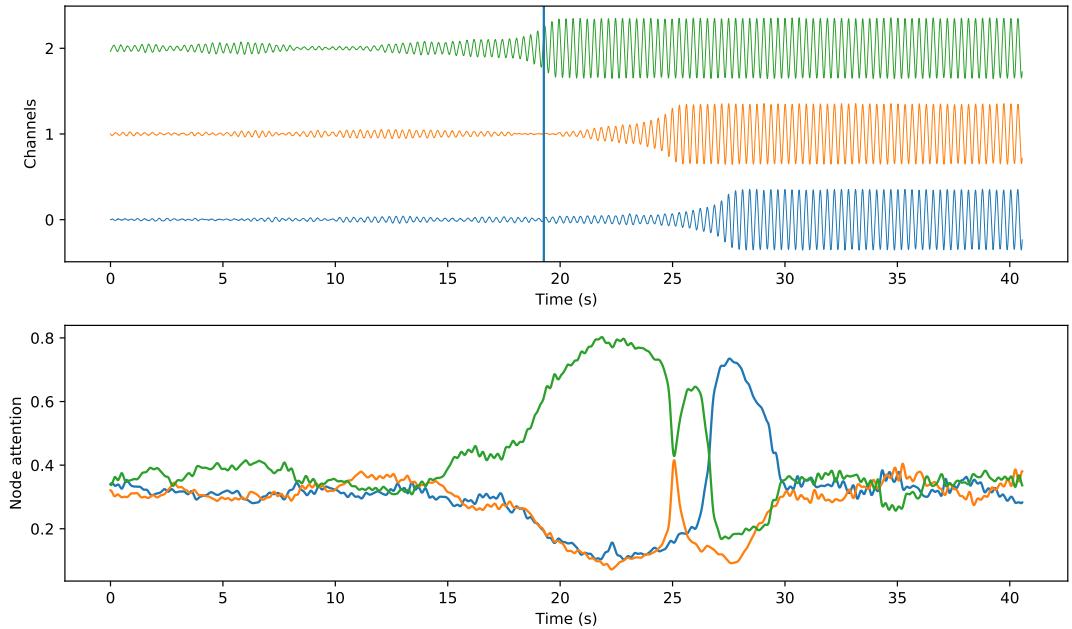
532 The GNN achieves an almost perfect detection score with a ROC-AUC of  $99.61 \pm 0.0$  and a PR-  
 533 AUC of  $99.69 \pm 0.0$  (averaged over five runs, evaluated on hold-out test data). Figure 6 compares  
 534 the generated node activity with the attention scores assigned by the GNN over time. The SOZ chan-  
 535 nel (green) is assigned the highest attention since the beginning of the seizure until all nodes are  
 536 simultaneously oscillating, at which point the attention scores converge to be evenly distributed. A  
 537 similar even distribution is observed in the interictal state, indicating that the network has correctly  
 538 learned to identify the SOZ electrode without defaulting to assign a high score to just one electrode.  
 539 This behaviour is confirmed by the spikes in attention assigned to channels 0 and 1, which happen  
 540 as soon as the node dynamics escape the fixed-point attractor.

## 541 The Virtual Brain Simulator

542 In this experiment we use The Virtual Brain simulator (TVB) (*Sanz Leon et al., 2013*) to model a  
 543 patient with temporal lobe epilepsy.

544 We follow the same approach described in TVB's documentation to configure the simulator.<sup>1</sup>  
 545 We assign the Epileptor neural mass model (*Jirsa et al., 2014*) to all the controllable brain regions of

<sup>1</sup>[https://github.com/the-virtual-brain/tvb-root/blob/master/tvb\\_documentation](https://github.com/the-virtual-brain/tvb-root/blob/master/tvb_documentation)



**Appendix 0 Figure 6.** Top: a clip showing the generated activity of a 3-node simulator, compared to the attention coefficient assigned by the GNN at each node over time. Colors indicate the same node in both plots.

546 TVB. We set the epileptogenicity of the right limbic areas (rHC, rPHC and rAMYG) to  $-1.6$ , the super-  
 547 rior temporal cortex (rTCI) and the ventral temporal cortex (rTCV) to  $-1.8$ , while for all other areas  
 548 to  $-2.2$ . The remaining parameters are kept as default. The hyperparameters used for creating the  
 549 FNs and training the GNN are the same ones that we used for the real iEEG data.

550 We select a subset of 34 sEEG virtual sensors among the ones provided for the default subject  
 551 of TVB. Of this subset, electrode 33 shows strong epileptogenic activity, while electrodes 18, 19, and  
 552 20 show mild activity. We generate clips of roughly 1 minute at 20Hz so that there is a simulated  
 553 onset in the middle of each clip. An example of a generated clip is shown in Figure 7.

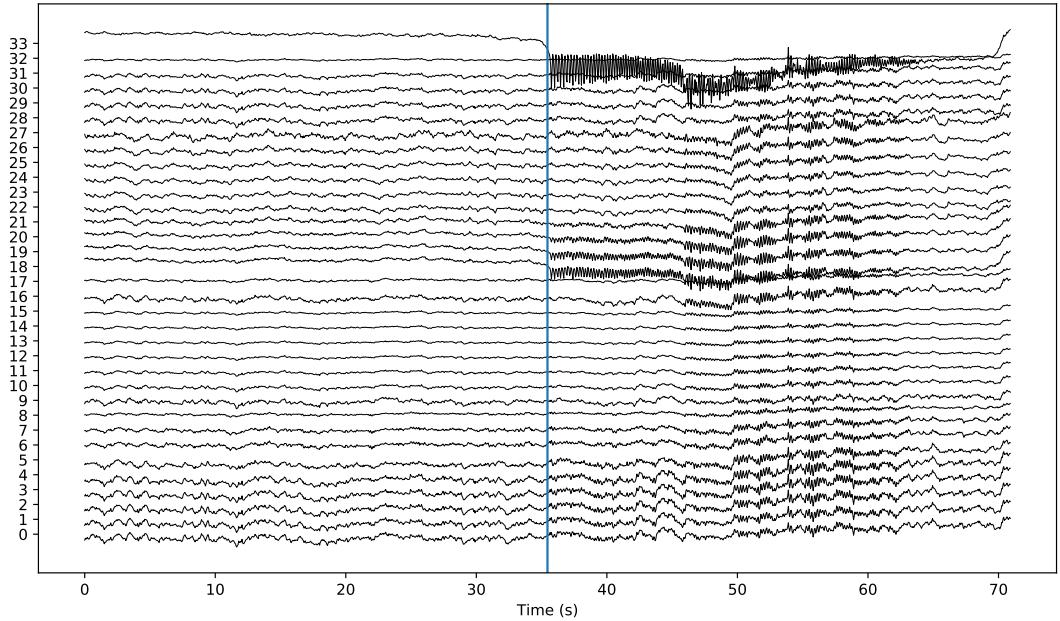
554 The GNN achieved an average detection ROC-AUC of  $98.87 \pm 0.18$  and an average PR-AUC of  
 555  $99.18 \pm 0.07$  (averaged over five runs, evaluated on hold-out test data). The electrode with a strong  
 556 ictal activity is consistently assigned a maximum score of 1 by all models and electrode 19 is also  
 557 ranked in the top-5 electrodes (see Figure 8).

### 558 **GNN training details**

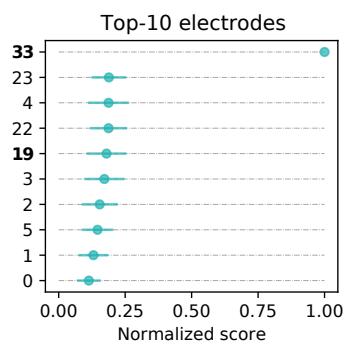
559 We consider each patient separately and train a GNN from scratch to build patient-specific models.  
 560 The GNN architecture is the one given in Equation (11). The ECC layer has 32 output units with  
 561 ReLU activation and a kernel-generating network  $f(\cdot)$  consisting of a two-layer MLP with 32 hidden  
 562 units and ReLU activation. All parameters of the layer are regularised with an  $L_2$  penalty with a  
 563 factor of  $10^{-5}$ .

564 The MLP classifier following the Attn-RO readout has 2 layers, with the hidden one having 32  
 565 units and ReLU activation and with 25% dropout in-between. Both layers are regularised with an  
 566  $L_2$  penalty with factor  $10^{-5}$ .

567 The model is trained using Adam, with a learning rate of  $10^{-3}$  and a batch size of 32 graphs. The  
 568 model is trained to convergence with 10 epochs of patience, using the data from  $[0.2 \cdot n]$  seizures  
 569 selected randomly ( $n$  being the overall number of available seizures) for early stopping.



**Appendix 0 Figure 7.** A virtual seizure generated with TVB. The vertical line denotes the annotated seizure onset in time.



**Appendix 0 Figure 8.** Top-10 electrodes with averaged rankings. Bold labels indicate that the corresponding electrode showed ictal activity. As desired, electrode 33 shows strong epileptogenic activity.

## 570 Baseline training details

571 The baseline is a simple 1D convolutional neural network (CNN) based on the architecture de-  
572 scribed by *Wang et al. (2017)*. The CNN operates directly on iEEG time series and hence does  
573 not take into account any graph-based representation for the data. Similarly to how we create the  
574 input-output pairs for the GNN, here we consider windows of size  $T$  taken at a stride of  $k/f_s$  for  
575 the interictal class and stride  $1/f_s$  for the ictal class, and we associate to each window a class label  
576 corresponding to the majority class of  $y(t)$  in the corresponding window.

577 In particular, we shrink the model to make it comparable in terms of number of parameters and  
578 depth to the GNN one, and also to prevent overfitting (which we experimentally encountered as a  
579 significant problem with the model). We consider a single convolutional layer with a kernel of size  
580 3, 8 output channels, and ReLU activations, followed by a global average pooling and a single-layer  
581 MLP to output the classification decision. We train the model using Adam with learning rate 0.001,  
582 batch size of 32 and early stopping with a patience of 5 epochs.