

1 Superior colliculus saccade motor bursts do not 2 dictate movement kinematics

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22 Abstract

23
24 The primate superior colliculus (SC) contains a topographic map of space, such that the
25 anatomical location of active neurons defines a desired eye movement vector.
26 Complementing such a spatial code, SC neurons also exhibit saccade-related bursts that are
27 tightly synchronized with movement onset. Current models suggest that such bursts
28 constitute a rate code dictating movement kinematics. Here, using two complementary
29 approaches, we demonstrate a dissociation between the SC rate code and saccade
30 kinematics. First, we show that SC burst strength systematically varies depending on
31 whether saccades of the same amplitude are directed towards the upper or lower visual
32 fields, but the movements themselves have similar kinematics. Second, we show that for the
33 same saccade vector, when saccades are significantly slowed down by the absence of a
34 visible saccade target, SC saccade-related burst strengths can be elevated rather than
35 diminished. Thus, SC saccade-related motor bursts do not necessarily dictate movement
36 kinematics.

37 38 Introduction

39
40 The superior colliculus (SC) plays an important role in saccade generation, as evidenced by
41 the ease with which low-current electrical microstimulation of SC neurons evokes
42 saccades^{1,2}. Anatomically, SC neurons are organized to form a spatial code of eye movement
43 displacement vectors^{1,3,4}, such that the location of an active neuron in the SC defines the
44 amplitude and direction of a desired saccade. Robustness and accuracy of saccade vector
45 representation are ensured through population coding⁴⁻⁶, with the aggregate activity of a
46 large number of simultaneously active neurons defining a given movement's metrics.
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49 The SC spatial code necessarily entails a temporal synchrony of SC activity at the time of
50 saccades. Indeed, saccade-related neurons show a highly characteristic temporal evolution
51 of spiking⁷⁻¹¹, dominated by a burst tightly locked to movement onset. Interestingly, the
52 strength of such a burst can vary, suggesting that SC neurons may encode additional
53 properties beyond the saccadic displacement vector represented by the spatial code. For
54 example, blink-perturbed saccades can have weaker, but prolonged, bursts^{12,13}. Moreover,
55 burst evolution during a saccade may be related to the remaining motor error of an ongoing
56 eye movement^{14,15} (i.e. how much more the eye needs to keep moving), or it may be related
57 to the speed profile of the ensuing saccade¹⁶. Additionally, saccade-related burst strength
58 can be modulated by audio-visual sensory combinations¹⁷. Thus, there is an SC rate code for
59 saccades, the role of which is less well understood than that of the spatial code.

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61 The most recent SC models posit an important role for the rate code in dictating saccade
62 kinematics^{13,16,18}. In these models, the locus of an active neuron (i.e. the spatial code)
63 defines how each individual spike in a motor burst moves the eye along the amplitude
64 dimension; parameters like eye speed or time to movement end would reflect the strength
65 of (i.e. number of spikes in) the motor burst (i.e. the rate code). While appealing in their
66 combination of both spatial and rate codes for movement specification, these models
67 suggest a very tight relationship between saccade-related burst strength and movement
68 kinematics. However, this may not necessarily always be the case. For example, we recently
69 explored a situation in which saccade kinematics were altered by a simultaneity condition
70 between a motor burst somewhere on the SC map and an irrelevant visual burst somewhere
71 else^{19,20}. When we recorded at both the motor and visual burst locations²¹, we found a
72 lawful relationship between the saccade changes and the number of additional spikes
73 injected by the visual burst (consistent with the spatial code); however, critically, the
74 simultaneous motor burst was minimally affected²¹. Thus, the rate code of the original
75 movement commands was essentially unaltered even though the movements themselves
76 were. This, along with other evidence²², motivates investigating whether saccade kinematics
77 are indeed dictated by the SC rate code or not.

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79 We approached this question using two complementary approaches. In the first, we
80 exploited a large asymmetry in how the SC represents the upper versus lower visual fields in
81 its visual sensitivity²³. If such an asymmetry still holds, but now for saccade-related motor
82 burst strength, then there should be (at least according to current models of the rate code)
83 systematic differences in the (amplitude-matched) saccades' kinematics. We confirmed a
84 neural asymmetry in SC motor burst strengths, but found no concomitant kinematic
85 differences between amplitude-matched saccades towards the upper and lower visual fields.
86 In the second approach, we instead used vector-matched saccades, but of clearly different
87 kinematics. Specifically, we exploited the fact that saccades to a blank can have significantly
88 slower speeds than saccades to a clear, punctate visual target²⁴⁻³⁰. We, therefore, compared
89 SC neuron motor bursts in these two conditions, sometimes recording multiple neurons
90 simultaneously in the two behavioral contexts. Surprisingly, we found no correlation
91 between SC motor burst modifications and the kinematic alterations of the saccades. More
92 importantly, approximately one quarter of the neurons actually increased, rather than
93 decreased, their motor burst strengths for the slower saccades. Our observations highlight
94 the need to explore other potential functional roles for the saccade-related SC rate code.

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97 Results

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99 We first identified a dissociation between SC motor burst strengths and their associated eye
100 movements' kinematics. Specifically, we explored how SC motor burst strength might differ
101 as a function of visual field location. When we recently described an asymmetry in how the
102 SC represents the upper and lower visual fields²³, we found that SC visual response
103 properties were different across the fields. We also briefly mentioned that the strength of
104 saccade-related motor bursts may also be asymmetric²³. Here, we investigated the
105 robustness of this saccade-related neural asymmetry in more detail, and we then asked
106 whether it predicted an asymmetry in amplitude-matched saccade kinematics between
107 movements towards the upper and lower visual fields. That is, we were motivated by a
108 common assumption in existing models^{13,16,18} that the relationship between SC motor burst
109 strengths and movement kinematics is directionally symmetric and only depends on
110 movement amplitudes. If so, then amplitude-matched movements of different directions,
111 which have different SC motor burst strengths, should also have different kinematics. In a
112 second set of experiments, we then used the complementary approach: we compared
113 vector-matched saccades (where both the amplitude and direction were the same and
114 towards the response field hotspot), and we asked whether alterations in these saccades'
115 kinematics under different behavioral contexts were systematically related to alterations in
116 the SC motor burst strengths.

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118 In what follows, we first describe the amplitude-matched upper and lower visual field
119 saccade results, and we then turn to the experiments with the vector-matched saccades
120 having different kinematics.

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123 *Difference in superior colliculus motor burst strengths for saccades towards the upper versus*
124 *lower visual fields*

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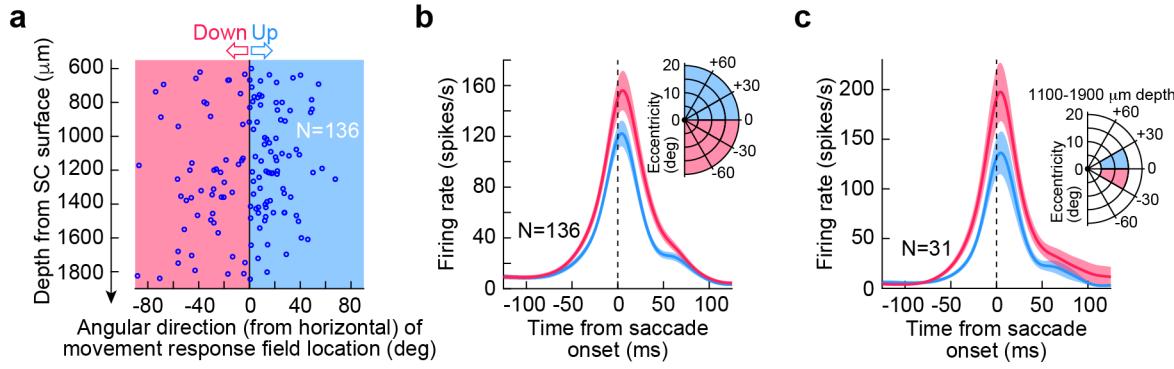
126 Visual sensitivity is significantly stronger in SC neurons representing the upper visual field²³.
127 That is, if a neuron's visual response field has a preferred (hotspot) location above the
128 retinotopic horizontal meridian and we present a stimulus at this location, then the neuron's
129 response is stronger than that of a neuron with a lower visual field hotspot location (and a
130 stimulus presented at its preferred location). Curiously, in our earlier study²³, we noticed
131 that saccade-related motor bursts showed the opposite asymmetry: saccade-related motor
132 bursts (for preferred hotspot locations) were stronger for neurons representing saccades
133 towards the lower visual field than for neurons representing saccades towards the upper
134 visual field. However, in that study²³, we did not control for the depths of the recorded
135 neurons from the SC surface when we analyzed the neurons' motor bursts. Since the
136 strength of SC motor bursts can vary with depth from the SC surface⁶, here, we wanted to
137 first confirm whether the asymmetry alluded to above²³ was still present when carefully
138 controlling for neuron depth (Methods). If this was the case, we could then ask whether
139 saccade kinematics were systematically different or not.

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141 We re-analyzed the neural database of ref. ²³ (monkeys P and N) by first matching the
142 depths of neurons from the SC surface between the upper and lower visual fields (Methods).
143 For each extra-foveal neuron in this database (here referred to as dataset 1), we identified

144 whether the neuron was saccade-related or not²³. We then classified the saccade-related
145 neurons as having a movement-related preferred response field location (or hotspot
146 location) in the upper or lower visual field. Preference was defined as the location for which
147 saccades were associated with the highest firing rates, similarly to how visual preference
148 was defined as the location for which visual stimuli evoked the strongest visual bursts²³.
149 Finally, we picked a range of neural depths from the SC surface that was overlapping
150 between the upper and lower visual field neurons. This final step was the critical step for the
151 present analysis, and it resulted in us having a total of 136 SC neurons with depths from the
152 SC surface between 600 and 1850 μm (Methods). The distribution of these depths is
153 represented in Fig. 1a, where each neuron's depth is plotted against a measure of whether
154 the neurons' preferred movement-related response field location was above or below the
155 horizontal meridian (the x-axis shows the angular direction of the preferred location from
156 the horizontal meridian; positive means above the meridian, and negative means below). As
157 can be seen, we found saccade-related SC activity at a range of depths from the SC surface
158 that was consistent with prior observations^{6-10,31,32}. Critically, the neural depths were
159 overlapping between the upper and lower visual field neurons (Fig. 1a; $p = 0.1257$, t-test, t-
160 statistic: -1.5408, df: 134); note (as an aside) that upper visual field directions were
161 compressed relative to lower visual field directions, which is consistent with the idea of
162 upper visual field neural tissue magnification in the SC²³. Therefore, we were now in a
163 position to check whether an asymmetry of saccade-related burst strengths alluded to
164 earlier²³ still held after controlling for neuron depth.
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166 Having established that we now had a neural database with matched depths from the SC
167 surface, we proceeded to comparing motor burst strengths between the upper and lower
168 visual field neurons. We plotted the peri-saccadic firing rates of the neurons of Fig. 1a, from
169 a delayed, visually-guided saccade task (Methods). We employed such a delayed saccade
170 paradigm to allow analyzing motor bursts in isolation, without the recently occurring visual
171 bursts associated with target onset, which would have come too close to saccade onset in an
172 immediate, visually-guided saccade version of the task (Methods). We picked, for each
173 neuron, the preferred saccades of the neuron and plotted its firing rate for these
174 movements, as we did previously²³. We then averaged across all neurons (Fig. 1b). There
175 was indeed an asymmetry in SC motor burst strengths, such that neurons representing the
176 lower visual field had significantly stronger motor bursts than neurons representing the
177 upper visual field (Fig. 1b). To statistically assess the difference in burst strengths after
178 matching for neural depths from the SC surface, we measured the average firing rate in the
179 final 50 ms before saccade onset for each neuron's preferred saccades²³ (Methods). We then
180 compared the population of measurements for the upper and lower visual field neurons of
181 Fig. 1a using a t-test. Across neurons, average firing rate for the upper visual field neurons
182 was 99 spikes/s, and it was 121 spikes/s for the lower visual field neurons. This difference
183 was statistically significant ($p=0.039$, t-test, t-statistic: -2.0844, df: 134). Therefore, even
184 after controlling for the depths of neurons from the SC surface, we confirmed a potential
185 asymmetry in saccade-related burst strength between upper and lower visual field
186 saccades²³.
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191 **Figure 1 Superior colliculus (SC) saccade-related motor bursts are stronger for downward saccades than for**
192 **upward saccades, even when controlling for depth from the SC surface. (a)** We picked neurons matched for
193 depth from the SC surface (between 600 and 1850 μm) but having movement field hotspot locations in either
194 the upper (light blue) or lower (light red) visual fields (i.e. positive or negative directions from the horizontal
195 meridian, respectively). Note that the upper visual field neurons appear compressed along the direction
196 dimension (i.e. in visual coordinates), likely due to upper visual field neural tissue magnification²³. Such
197 magnification is similar, in principle, to foveal magnification of SC neural tissue³³. **(b)** For the neurons in **a**, we
198 plotted peri-saccadic firing rates for saccades towards each neuron's preferred movement field location²³.
199 Saccade-related bursts were stronger for lower visual field than upper visual field neurons. **(c)** To better constrain
200 errors in depth estimates from the SC surface (due to surface curvature), we further restricted the choice of
201 neurons to those primarily near the horizontal meridian and at an eccentricity range associated with quasi-
202 constant tissue curvature between upper and lower visual field locations³³; the ranges of amplitudes, directions,
203 and depths are shown in the inset. The motor bursts of the resulting 31 neurons were still stronger for lower
204 visual field than upper visual field neurons (left panel). Error bars in all panels denote s.e.m.

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208 A potential concern related to the above interpretation might be the curvature associated
209 with the SC's 3-dimensional shape. Since all electrode paths were constant and defined by
210 the recording chamber's orientation (Methods), it could still be possible that lateral
211 recording sites (representing the lower visual field) could have had systematically different
212 depths from the SC surface than medial recording sites (representing the upper visual field),
213 by virtue of the different SC surface curvature at the two groups of sites. We therefore
214 decided to analyze a stricter grouping of SC neurons. We picked a smaller range of
215 eccentricities (5-15 deg), directions from the horizontal meridian (<30 deg), and depths from
216 the SC surface (1100-1900 μm) for comparing upper and lower visual field neurons' motor
217 bursts. Our prior work on SC surface topography and 3-dimensional anatomical shape³³
218 suggested that this range of selection should reduce potential systematic differences in
219 estimates of depths from the SC surface between the upper and lower visual field groups of
220 neurons. We found 31 neurons (20 upper visual field and 11 lower visual field) satisfying the
221 above strict criteria. When we analyzed their saccade-related firing rates, we still found a
222 similar asymmetry between upper and lower visual field locations (Fig. 1c). The average
223 firing rate (in our same measurement interval) for the upper visual field neurons was 92
224 spikes/s, and it was 147 spikes/s for the lower visual field neurons; this difference was,
225 again, statistically significant ($p=0.0162$, t-test, t-statistic: -2.5524, df: 29). Therefore, it is
226 likely, given both analyses in Fig. 1, that there is indeed a systematic asymmetry in SC motor
227 burst strength between saccades towards the upper and lower visual fields. We were now in
228 a position to ask whether such an asymmetry was reflected in saccade kinematics, as might
229 be predicted from some recent as well as classic models of the SC rate code^{13,14,16}.

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232 *Similarity of movement kinematics for saccades towards the upper and lower visual fields*

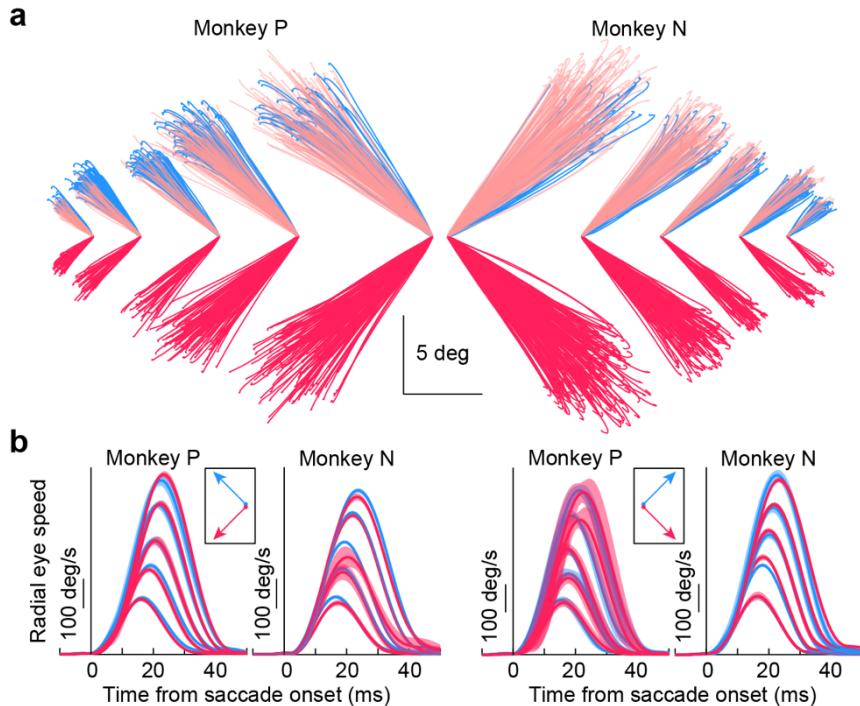
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234 According to existing models, which assume directional symmetry in the SC movement
235 commands, amplitude-matched saccades to the upper and lower visual fields should have
236 different movement kinematics given the different SC motor burst strengths that we saw in
237 Fig. 1. To test this, we analyzed saccades from both monkeys (P and N) from the same
238 delayed, visually-guided saccade task that was used to analyze the peri-saccadic SC firing
239 rates above (Methods). To compare size- and direction-matched movements, we picked, in
240 each monkey, 5 saccade sizes (3, 5, 7, 10, and 13 deg radial amplitude), and two example
241 directions from the horizontal meridian (+45 and -45 deg; i.e. oblique saccades; note that we
242 also made similar observations for example directions that were nearer to or farther away
243 from the horizontal meridian than +/- 45 deg). For each of the saccade sizes, we picked
244 movements landing within a radius of 0.5, 0.8, 1, 2, and 3 deg, respectively for the increasing
245 saccade amplitude categories listed above. Therefore, we ensured that the movement
246 endpoints were matched for landing accuracy. Example such movements are shown in Fig.
247 2a. In this figure, we only plotted rightward movements in monkey N and leftward
248 movements in monkey P, for simplicity, but Fig. 2b shows both rightward and leftward
249 saccades in each of the two monkeys. As can be seen from Fig. 2a, there was no clear
250 difference in the trajectories of upward (light blue) versus downward (light red) oblique
251 saccades, despite the significant SC neural asymmetry in Fig. 1. In fact, the pink upward
252 traces in Fig. 2a are the same as the light red downward traces in the figure, but now
253 reflected across the horizontal meridian for easier comparison to the upward saccades
254 shown in light blue. These pink traces clearly overlapped strongly with the upward saccades.
255

256 Across the population of measurements from the above saccades, we plotted radial eye
257 speed as a function of saccade amplitude and direction (Fig. 2b). This kind of plot
258 summarizes the kinematics of the eye movements^{34,35}. For each saccade size and right/left
259 direction in each monkey, we plotted the radial eye speed for either upward (light blue) or
260 downward (light red) oblique saccades (error bars denote 95% confidence intervals). There
261 were no systematic differences in the saccadic profiles of the two groups of movements
262 (across all sizes tested), despite the systematically stronger SC motor bursts for downward
263 saccades seen in Fig. 1 (compare light blue and light red profiles for each saccade size). For
264 example, stronger motor bursts in Fig. 1 could have predicted systematically higher peak
265 speeds for the saccades directed towards the lower visual field¹⁶. This was clearly not the
266 case (Fig. 2b). In fact, lower visual field neurons possess larger movement fields than upper
267 visual field neurons²³, which should further increase the number of “active” spikes during
268 saccade-related bursting for saccades towards the lower visual field; nonetheless, the
269 kinematics of the movements were largely the same as those of upper visual field saccades
270 (Fig. 2). Therefore, the results so far are consistent with a dissociation between SC saccade-
271 related motor burst strength (Fig. 1) and saccade kinematics (Fig. 2).

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Figure 2 Upward and downward oblique saccades from the same sessions as the neural recordings in Fig. 1 exhibited similar kinematic properties, despite the neural asymmetry of Fig. 1. (a) Oblique saccades of different directions and amplitudes in both monkeys (rightward for N and leftward for P). Each line plots the horizontal and vertical displacement of eye position for a given saccade having a +45 deg (light blue) or -45 deg (light red) direction from the horizontal meridian. Saccades of similar sizes are grouped together (to start from the same origin) and displaced horizontally in the figure from saccades of different size ranges (the scale bars apply to all sizes). The pink traces overlaying the light blue traces are the same as the light red traces of the lower visual field saccades, but now reflected along the vertical dimension for better comparison to the upper visual field saccades. The trajectories of the saccades were largely similar regardless of direction from the horizontal meridian, despite the asymmetry in motor bursts in Fig. 1. **(b)** For each monkey, we plotted radial eye speed as a function of time from saccade onset for leftward (left pair of plots) or rightward (right pair of plots) saccades. In each case, we separated upward and downward movements by color (as in a). The different saccade sizes in a are reflected in the different peak speeds^{34,35}. The kinematic time courses of saccade acceleration, peak speed, and deceleration were largely similar for upward and downward saccades, despite the asymmetry of SC motor bursts in Fig. 1. Error bars denote 95% confidence intervals. The numbers of trials per condition in monkey N ranged from 7 to 362 (mean 121.2), and the numbers of trials per condition in monkey P ranged from 5 to 252 (mean 72.25).

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294 *Similarity of upper and lower visual field saccade kinematics for a variety of behavioral*
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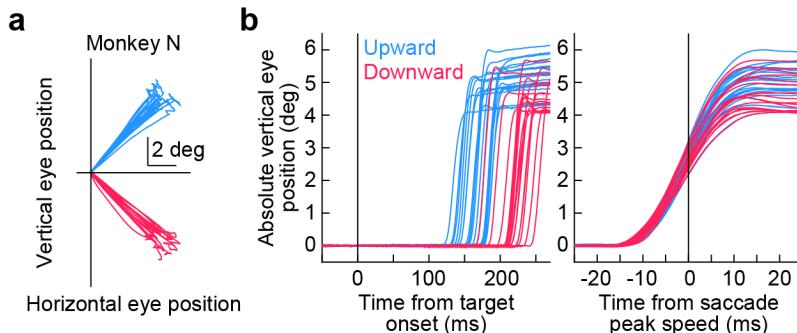
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To further assess the dissociation between upper/lower visual field SC motor burst asymmetries and upward/downward saccade kinematics, we next turned to another, larger database of saccades for analyzing kinematics in more detail (dataset 2; Methods). In this case, we used: 1) immediate, visually-guided, 2) delayed, visually-guided, and 3) memory-guided saccades of different sizes and directions, with the sizes ranging from those associated with fixational microsaccades (approximately 0.1-0.2 deg) to approximately 15-20 deg. Aspects of these movements were analyzed previously for other purposes than movement kinematics^{36,37}. Here, we wanted to confirm that the results of Fig. 2 still held for a larger range of movement amplitudes and directions, and also under different behavioral contexts. In other words, we analyzed the movements' kinematic properties in dataset 2, properties which were not analyzed in the prior publications. Moreover, dataset 2 allowed

308 us to include data from a third monkey, M, when assessing potential differences (or lack
309 thereof) in saccade kinematics between the upper and lower visual fields.

310
311 In our recent work with this dataset³⁶, we reported that saccadic reaction times were
312 systematically shorter for upper visual field target locations when compared to lower visual
313 field target locations, consistent with the asymmetry of SC visual neural sensitivity²³, and
314 also consistent with other behavioral evidence³⁸⁻⁴¹. For example, in Fig. 3a, we plotted
315 example oblique saccades from monkey N from this dataset (but in a format similar to that
316 used in plotting the data of Fig. 2a). In Fig. 3b (left), we plotted the absolute value of vertical
317 eye position from the saccades shown in Fig. 3a (to facilitate comparing the upward and
318 downward movements). Here, we temporally aligned the movements to the time of the go
319 signal for triggering the saccades (the peripheral targets were continuously visible). Even
320 though the saccade trajectories looked similar in Fig. 3a (save for the upward and downward
321 distinction), the reaction times of the movements were markedly different (Fig. 3b, left).
322 Saccades towards the upper visual field were triggered significantly earlier than saccades
323 towards the lower visual field³⁶. We then replotted the same saccades, but this time by
324 aligning them to the time of peak radial eye speed during the movements (Fig. 3b, right). The
325 movement kinematics were largely overlapping, with similar acceleration and deceleration
326 profiles.

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332 **Figure 3 Upward and downward saccades exhibit strong differences in reaction times, but not kinematics.** (a)
333 From the second dataset, we plotted, by way of example, similarly-sized oblique saccades from one monkey, and
334 we separated them as being either upward or downward (as in Fig. 2a). (b) Relative to stimulus onset (left panel),
335 the saccades were very different from each other in terms of their reaction times, as we characterized in detail
336 earlier³⁶; saccades towards the upper visual field (light blue) had significantly shorter reaction times than
337 saccades towards the lower visual field (light red). However, kinematically, the saccades were very similar when
338 aligned to the time of peak intra-saccadic eye speed (right panel). In both panels, we plotted the absolute value
339 of vertical eye position displacement for each saccade (for better comparison of the upward and downward
340 movements). Figures 4, 5 summarize the saccade kinematic results that we obtained for a much larger number
341 of movements, and for two monkeys. N=21 upward saccades and N=18 downward saccades in this figure.

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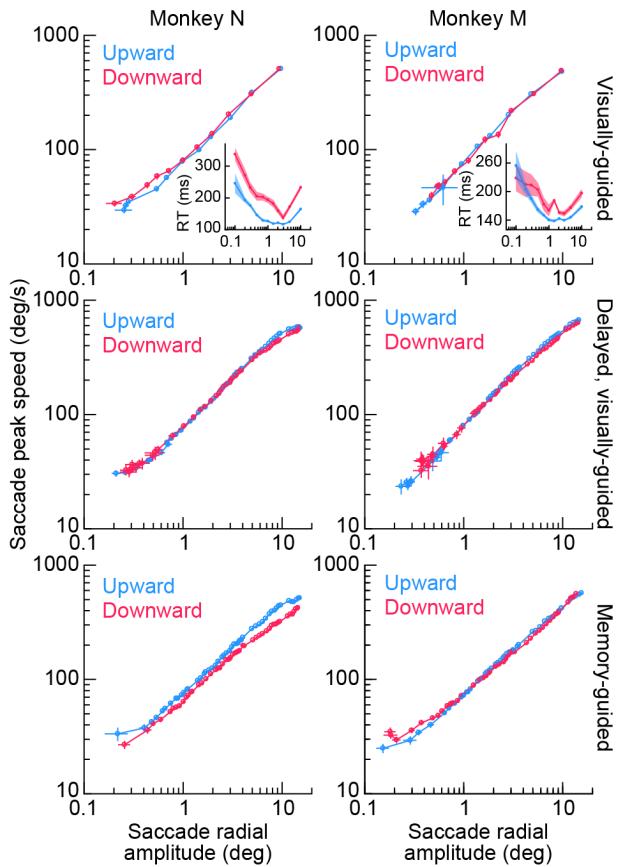
346 To summarize this kinematic similarity across all saccades in this dataset, we generated plots
347 of peak eye speed as a function of saccade amplitude for each monkey^{34,35}. In the first row of
348 Fig. 4, these plots were made for the immediate, visually-guided saccade task, in which the
349 fixation spot was extinguished at the same time as the appearance of the eccentric stimulus

350 (Methods; this task was not used during SC recordings because the visual and motor bursts
351 would occur too close to each other for proper neural analysis). For both monkeys N and M,
352 there was very minimal difference in the main sequence relationship between saccades
353 towards the upper (light blue) or lower (light red) visual fields, and any difference was
354 certainly much smaller than the neural effects in Fig. 1. In fact, the insets in the first row of
355 Fig. 4 show the reaction time results for the very same saccades, which are replicated from
356 our recent work³⁶ for clarity. Despite a large effect of the visual field location on the
357 movements' reaction times (also seen in Fig. 3b, left), there was minimal difference in
358 saccade kinematics. This is again supportive of a dissociation between saccade-related SC
359 motor burst strengths (Fig. 1) and movement kinematics (Figs. 2, 3); also see Figs. 6-8 below.
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361 With an even larger database of visually-guided movements in this dataset, now from the
362 delayed, visually-guided saccade task, the same conclusion could be reached: the middle
363 row of Fig. 4 shows virtually no difference in the saccade kinematics between upward and
364 downward visually-guided saccades, despite a clear effect size for SC motor-related neural
365 responses in Fig. 1 and ref. ²³. The peak speeds in this row were also consistent with the
366 peak speeds in the first row of Fig. 4 obtained with the immediate, visually-guided saccade
367 task, as might be expected given the presence of a visual target for the saccades in both
368 tasks.
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370 We also tested memory-guided saccades. Even though such saccades were generally slower
371 than visually-guided saccades (compare the bottom row of Fig. 4 to the two rows above it;
372 also see Figs. 6-8 below)²⁴⁻³⁰, the above-mentioned kinematic similarity between movements
373 towards the upper and lower visual fields still persisted in the memory-guided saccade task.
374 Only in monkey N (left column of the bottom row of Fig. 4) was there a reduction in
375 downward saccade peak eye speed when compared to upward saccade peak eye speed.
376 However, even in this case, such a reduction was inconsistent with the stronger saccade-
377 related motor bursts for lower visual field saccades seen in the SC neural analyses (Fig. 1). If
378 anything, stronger lower visual field SC motor bursts (along with larger response fields²³)
379 might predict higher, rather than lower, peak speeds for downward saccades.
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Figure 4 The main sequence relationship between peak eye speed and saccade amplitude does not depend on whether saccades are upward or downward for a variety of behavioral task contexts. In each monkey (left and right columns), we plotted the main sequence from dataset 2 but after first separating saccades as being directed towards either the upper visual field (light blue) or lower visual field (light red). The first two rows show visually-guided saccades (immediate for the first row, and delayed based on a task instruction in the second row; Methods). The third row shows memory-guided saccades towards a blank region of the display. The insets in the first row show saccadic reaction time (RT) data (as in Fig. 3b, left) for the same saccades as in the main sequence plots, to highlight the strong presence of a visual field effect on reaction times and a concomitant absence of a visual field effect on saccade kinematics. In all saccade contexts (across rows), the visual field location of the saccade endpoint had minimal effect on saccade kinematics (despite a large effect on saccadic reaction times and despite an asymmetry in SC motor bursts; Fig. 1). The insets in the first row directly replicate the plots in Fig. 4a, c of ref. ³⁶ for easier comparison of effect sizes for reaction times and kinematics. Error bars denote s.e.m. Note that monkey N showed a small reduction of peak eye speed for downward saccades when compared to upward saccades only in the memory-guided condition (bottom row), but this effect is opposite from what would be expected if SC motor bursts (Fig. 1) dictated kinematics. The insets were replotted with permission from ref. ³⁶.

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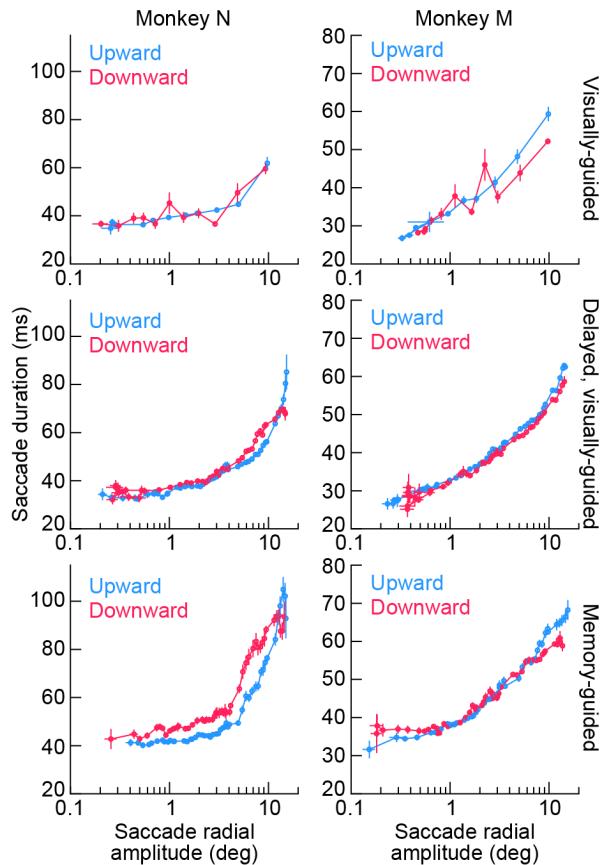
Therefore, across a large range of movement sizes and directions, we found minimal kinematic differences between amplitude-matched upper and lower visual field saccades, even though other aspects of saccade generation (such as reaction times; insets in Fig. 4) were strongly different, and even though SC saccade-related motor bursts were also different (Fig. 1).

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Finally, we also checked saccade durations as a function of saccade amplitudes (Fig. 5), and we reached similar conclusions. Saccade duration versus amplitude curves strongly overlapped for saccades towards the upper (light blue) and lower (light red) visual fields (Fig. 5), and this was true across task contexts. Note how monkey N compensated for the slightly

413 slower downward memory-guided saccade peak speeds (when compared to upward
414 memory-guided saccade peak speeds) with mildly longer durations for these movements
415 (left column of the bottom row of Fig. 5). This might suggest that there was lower drive for
416 generating this monkey's downward memory-guided saccades in general, which was then
417 compensated for by increased movement durations. Nonetheless, as stated above, this is an
418 opposite effect from what might be expected from the neural burst strengths in the SC (Fig.
419 1).

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424 **Figure 5 Saccade durations as a function of saccade amplitude are also largely insensitive to whether saccades**
425 **are directed towards the upper or lower visual field.** Same as Fig. 4 but now plotting saccade duration as a
426 function of saccade amplitude. Similar conclusions were reached concerning the minimal influence of upper
427 versus lower visual field saccade target locations on saccade kinematics, despite asymmetries in SC motor bursts
428 (Fig. 1). For monkey N in the memory-guided condition (left panel of the bottom row), the slower lower visual
429 field saccade peak speeds (Fig. 4) meant slightly longer saccade durations when compared to upper visual field
430 saccades (a speed-duration tradeoff). Error bars denote s.e.m.

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434 *Dissociation between SC motor burst strengths and movement kinematics also for vector-
435 matched saccades*

436
437 In the above experiments, and as stated above, we were motivated by an assumption of
438 directional isotropy in models of saccade control by the SC rate code^{13,16,18}. In such models,
439 saccades are implemented (in terms of efferent connection strengths towards the
440 brainstem) according to their amplitude not vector; as a result, analyses of experimental

441 data often collapse measurements across different directions. We reasoned that if this was
442 indeed the case, then different SC burst strengths for upward and downward saccades (Fig.
443 1) should lead to different saccade kinematics, which we did not observe (Figs. 2-5). Having
444 said that, it may be argued that our observations so far merely suggest a different efferent
445 mapping to the downstream oculomotor control circuitry from the upper and lower visual
446 field SC representations, rather than a dissociation between SC motor burst strengths and
447 movement kinematics. While such a different efferent mapping between the upper and
448 lower visual fields would indeed be interesting, we elected to further test our original
449 hypothesis using a complementary approach, this time by employing vector-matched
450 saccades of different kinematics.

451
452 We exploited the fact that saccades to a blank (as in memory-guided saccades) can be
453 slower than visually-guided saccades²⁴⁻³⁰. We thus instructed 3 monkeys (M, N, and A) to
454 perform delayed, visually-guided saccades and memory-guided saccades towards the
455 response field hotspot locations of SC neurons. This meant that we now had even more SC
456 recording data from monkey N (beyond those shown in Fig. 1), as well as additional SC
457 motor burst measurements from two more monkeys (M and A), always comparing vector-
458 matched visually-guided and memory-guided saccades towards hotspot locations.
459 Moreover, in all 3 monkeys in this additional dataset (referred to here as dataset 3), we also
460 recorded neurons using linear electrode arrays (monkey M also contributed some single-
461 electrode sessions as well; Methods). This meant that we sometimes had simultaneously
462 recorded neurons for the same behavioral trials. For each isolated neuron, we first selected
463 saccades matched by direction and amplitude across the two tasks (data filtering
464 procedures, and minimum trial count requirements, are detailed in Methods). We then
465 checked the movement kinematics across the two tasks, and we evaluated how SC motor
466 bursts were potentially modified.

467
468 Figure 6a shows an example saccade vector from one of our sessions. In purple, we show the
469 delayed, visually-guided saccades from the session, and in green, we show the memory-
470 guided saccades. Despite being matched in direction and amplitude (as per our experimental
471 design), almost all memory-guided saccades from this session were slower than all visually-
472 guided saccades, as can be seen from Fig. 6b. Thus, we had vector-matched saccades with
473 clearly differing kinematics. We then checked how the SC motor bursts were altered. In Fig.
474 6c, we show the spike waveforms of 3 different SC neurons that we recorded simultaneously
475 from the same session in the two tasks. Each sub-plot in Fig. 6c shows the mean and
476 standard deviation of a random sampling of spike waveforms from a given isolated neuron in
477 both tasks (Methods). As can be seen, the waveforms were almost completely overlapping
478 for each neuron, suggesting that isolation quality was sufficiently stable for each of them as
479 we sequentially ran the two behavioral tasks (Methods). Therefore, we were now in a
480 position to compare the motor bursts of the neurons in the two behavioral contexts.

481
482 Surprisingly, there was a large diversity of motor burst modulations between the visually-
483 guided and memory-guided saccades, despite the highly consistent kinematic effects seen in
484 Fig. 6b. For example, Neuron 1 in Fig. 6d had a weaker burst in the memory-guided saccade
485 condition than in the visually-guided saccade condition, consistent with the kinematic effect
486 across the two conditions. However, Neuron 2 was much less affected by the behavioral
487 manipulation, and, most surprisingly, Neuron 3 had a much stronger motor burst in the
488 memory-guided condition instead of the visually-guided condition (Fig. 6d). Thus, there was

489 no systematic reduction in SC motor burst strengths (Fig. 6d) for the systematically slower
490 (but vector-matched) memory-guided saccades (Fig. 6b), as would be predicted by current
491 models of kinematic control by SC motor bursts.

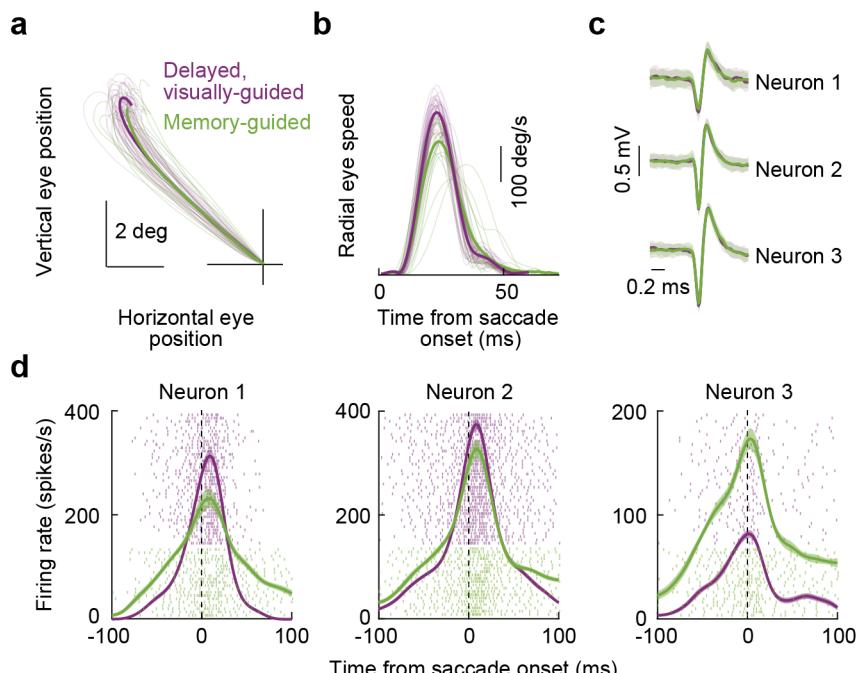
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Figure 6 Superior colliculus motor burst strength is dissociated from saccade kinematics even for vector-matched movements. (a) Example saccade trajectories from one session of the vector-matched experiments. Thin lines show individual movements, and thick lines show averages across trials. Purple denotes delayed, visually-guided saccades, and green denotes memory-guided saccades. The vectors of the two types of saccades were matched (Methods). (b) Memory-guided saccades were systematically slower than their visually-guided counterparts, as might be expected²⁴⁻³⁰. (c) Spike waveforms from 3 example neurons recorded simultaneously during the same session. Each thick line shows the average of a random sampling of waveforms from each of the two tasks. The error bars denote the s.d. across observations. In all cases, the waveforms were stable across the two task types, suggesting that each neuron was successfully recorded in the two tasks. The numbers of waveforms included in the averages for the visually-guided and memory-guided conditions, respectively, are: 70/97 (Neuron 1), 79/74 (Neuron 2), and 42/54 (Neuron 3). (d) The neurons of c had a large diversity of effects, in terms of peri-saccadic motor burst strengths, as a function of saccade type. Neuron 1 had a weaker motor burst strength for memory-guided saccades; Neuron 2 was less affected by the condition; and Neuron 3 had a surprisingly stronger motor burst in the memory-guided condition, despite the significantly slower saccades seen in b. Error bars denote s.e.m. and numbers of trials are evident from the shown individual-trial spike rasters.

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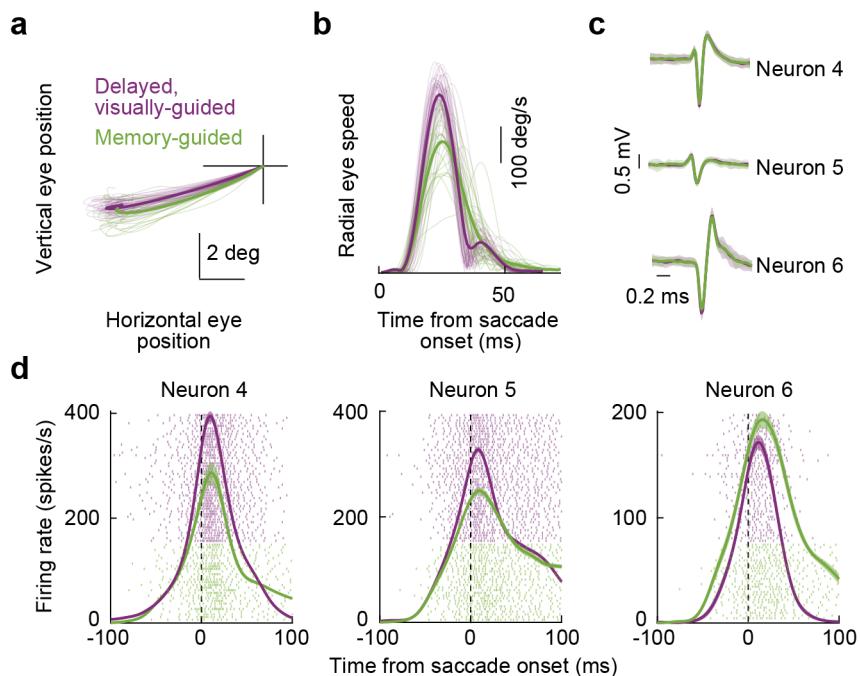
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524 6) that violated the clearly slower saccades observed in Fig. 7b for the memory-guided
525 saccade condition. Thus, this additional example site revealed the very same patterns as
526 those shown in Fig. 6, and it suggests a dissociation between SC motor bursts and saccade
527 kinematics. A similar conclusion was also reached in earlier comparisons of the two tasks²⁴.
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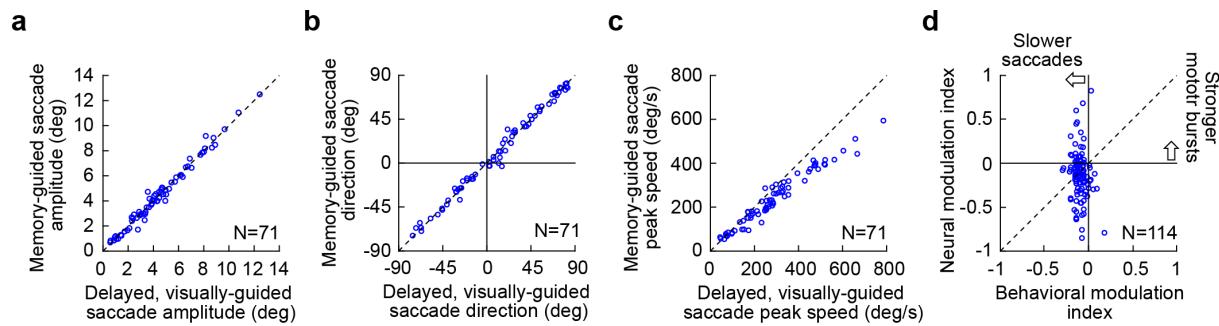


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533 **Figure 7 Similar observations to Fig. 6 from another example SC site.** The figure is formatted identically to Fig.
534 6. The site of this example session was now in the SC's lower visual field representation, as evidenced by the
535 downward oblique saccades in **a**. Note how the saccade speed was clearly different between visually-guided and
536 memory-guided saccades (**b**), but the neurons still had a diversity of effects in terms of motor burst strengths
537 (**c**). The numbers of spike waveforms included in the averages of **c** for the visually-guided and memory-guided
538 conditions, respectively, are: 117/82 (Neuron 4), 76/65 (Neuron 5), and 85/81 (Neuron 6).
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543 In total, we analyzed 114 SC neurons from 71 sites in these vector-matched experiments
544 (from monkeys M, N, and A; Methods). To summarize their results, we first confirmed that
545 all saccades were vector-matched across the visually-guided and memory-guided saccade
546 conditions, as per our experimental design. For each of the 71 sites, each having a unique
547 saccade vector, we collected the average saccade vector from each of the two conditions.
548 We then plotted the amplitude (Fig. 8a) and direction (Fig. 8b) of the memory-guided
549 saccade vector against the amplitude and direction of the visually-guided saccade vector.
550 There was no difference between the two conditions in either amplitude (Fig. 8a) or
551 direction (Fig. 8b) (amplitude comparison: $p = 0.5313$, paired t-test, t-statistic: -0.6292, df:
552 70; direction comparison: $p = 0.9735$, paired t-test, t-statistic: -0.0334, df: 70), as expected
553 (we explicitly matched the vectors of the saccades in these experiments; Methods). We then
554 confirmed that the saccades were significantly slower in the memory-guided condition than
555 in the visually-guided condition²⁴⁻³⁰, and we did so by plotting in Fig. 8c the peak speeds from
556 all experiments against each other, in a fashion similar to the amplitude and direction plots

557 of Fig. 8a, b. Memory-guided saccades were significantly slower than vector-matched
558 visually-guided saccades ($p = 6.21 \times 10^{-13}$, paired t-test, t-statistic: -8.7979, df: 70). Most
559 importantly, we then related the peak speed effect (for the vector-matched movements) to
560 the neural motor burst effect. To do so, we measured each neuron's peak firing rate in the
561 interval -25 to +25 ms from saccade onset (Methods). We then created a neural modulation
562 index as the burst strength in the memory-guided condition minus the burst strength in the
563 visually-guided condition, divided by the sum of the two burst strengths (Methods). Values
564 of the index >0 would indicate that motor bursts were actually stronger in the memory-
565 guided saccade condition than in the visually-guided saccade condition. Similarly, we created
566 a behavioral modulation index as the peak saccade speed in the memory-guided condition
567 minus the peak saccade speed in the visually-guided condition, divided by the sum of the
568 two peak speeds (Methods). Across all neurons, there was no correlation between the
569 neural and behavioral modulation indices (Fig. 8d) (Pearson correlation coefficient: -0.1374,
570 $p = 0.1449$). Rather, there was a more-or-less constant behavioral effect (slower saccades in
571 the memory-guided condition) irrespective of SC neural modulation effect, as evidenced by
572 the vertical scatter of points across all neurons in Fig. 8d.

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577 **Figure 8 Population summary demonstrating how SC motor burst strength is dissociated from saccade**
578 **kinematics even for vector-matched movements. (a)** Average saccade amplitude in the memory-guided saccade
579 task versus the visually-guided saccade task across all unique sessions in this experiment. Each symbol indicates
580 a single session. As per the experimental design, the saccade amplitudes were matched across the two
581 conditions. **(b)** Same as a but for the directions of the saccades. Negative means downward saccades, and
582 positive means upward saccades. Again, there was no difference in saccade angles across the visually-guided and
583 memory-guided conditions. Thus, a and b indicate that the saccades in the two conditions were vector-matched.
584 **(c)** Despite the vector matching, peak speeds were consistently lower for memory-guided saccades. **(d)** For all
585 recorded neurons from the same sessions, we calculated a behavioral modulation index, in which negative values
586 indicated slower saccades in the memory-guided condition. We also created a neural modulation index, in which
587 negative values indicated weaker motor bursts in the memory-guided condition. Note that some neurons were
588 recorded simultaneously during the same trials, as in Figs. 6, 7 (Methods). Thus, there were more neurons than
589 sessions, explaining the different numbers of symbols from a-c; this also meant that there could be multiple
590 symbols with different y-axis values but having the same x-axis value (because multiple neurons were collected
591 for the same behavioral trials). There was no correlation between neural and behavioral modulation indices.

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595 Interestingly, there was a large dynamic range of neural modulation indices. Some neurons
596 were almost completely suppressed in the memory-guided condition. These can qualify as
597 visually-dependent saccade-related neurons^{24,31,37}. Alternatively, 46.49% of the neurons
598 (53/114) were above the diagonal line in Fig. 8d, thus violating the predictions of current
599 models of kinematic control by SC motor bursts. Most intriguingly, almost one quarter of the
600 neurons (23.7%, 27/114) had a neural modulation index >0 , suggesting that these neurons

601 actually exhibited stronger motor bursts for memory-guided saccades than for vector-
602 matched visually-guided saccades (Fig. 8d), despite the significantly slower speeds of the
603 former (Fig. 8c). Thus, the motor bursts were independent of the actual triggered saccades.
604
605 These results, combined with those of Figs. 1-5 above, suggest that there is indeed a
606 dissociation between SC motor burst strengths and saccade kinematics.
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608

609 Discussion

610
611 We described a dissociation between SC saccade-related motor burst strengths and
612 movement kinematics. In particular, we confirmed an asymmetry in motor burst strengths
613 between upper and lower visual field saccade target locations (Fig. 1). We then found that
614 the kinematics of amplitude-matched saccades towards upper and lower visual field
615 locations were not different from each other across a range of movement sizes, directions,
616 and behavioral contexts (Figs. 2-5). Finally, we demonstrated how there was no correlation
617 between SC motor burst effects and kinematic alterations even in vector-matched saccades
618 towards response field hotspot locations (Figs. 6-8).
619

620 Other examples of dissociations between SC motor burst strengths and movement
621 properties are consistent with our interpretation that the SC rate code does not necessarily
622 dictate movement kinematics, as might be suggested by some recent models^{13,16}. For
623 example, and as we have confirmed (Fig. 8d), for memory-guided saccades towards
624 response field hotspot locations, a significant fraction of SC neurons becomes silent at the
625 time of movement onset^{24,31,37}. This, in addition to neurons that exhibit potentially altered
626 response field profiles when making saccades towards a blank²⁹, suggests a significantly
627 modified SC representation during these movements. Indeed, we even found neurons that
628 exhibited stronger, rather than weaker, motor bursts for slower memory-guided saccades
629 (Fig. 8). Therefore, the relationship between movement kinematics and SC motor bursts is
630 relatively loose when making saccades towards a blank, and it was also relatively loose in
631 our analyses of upper and lower visual field target locations.
632

633 Another example of a dissociation between saccade motor burst strength and movement
634 kinematics was observed when saccades were driven by combinations of visual and auditory
635 sensory signals, as opposed to only visual signals¹⁷. Interestingly, it was again the case in this
636 example that a sensory scenario was relevant and critical for revealing a potential separation
637 between the SC rate code and movement kinematics. That is, in both the example above of
638 saccades towards a blank as well as the current example of multi-sensory target
639 specification, it was a modification of a sensory property of saccade targets that has allowed
640 observing a dissociation between motor burst strengths and eye movement properties. This
641 clear context-dependence of the bursts indicates that SC “motor” bursts are likely not pure
642 motor controllers, in the strictest sense of the word. In the current manuscript’s context as
643 well, we were originally motivated by the fact that it was visual sensitivity that was strongly
644 variable between upper and lower visual field locations²³. Indeed, given that stronger visual
645 responses occur in the upper visual field whereas stronger motor responses occur in the
646 lower visual field, it is intriguing to consider the possibility that there might be a general anti-
647 correlation property between visual sensitivity and saccade-related motor burst strength in
648 the SC, for example, in the ubiquitous visual-motor neurons of this structure.

649

650 More recently, Peel and colleagues also identified a dissociation between SC motor burst
651 strength and executed saccade properties²². Specifically, these authors causally perturbed
652 top-down inputs towards the SC through reversible cooling of the cortex, and they found
653 reduced SC burst strengths for metrically similar executed saccades. This study, along with
654 refs. ^{17,24,31,37}, all showed that for the very same saccade vector (i.e. only within the upper
655 visual field SC representation or only within the lower visual field SC representation),
656 sensory^{17,24,31,37} or physiological²² manipulations can indeed significantly alter SC burst
657 strengths without fully accounting for the altered saccade properties. Therefore, whether
658 one considers a single saccade vector like in these studies or a comparison of upper versus
659 lower visual field saccades like in the first half of our study, a dissociation between SC
660 saccade-related motor bursts and saccade execution still exists.

661

662 One potential criticism of our comparison of upper and lower visual field saccades could be
663 that the existing models of the rate code dictating saccade kinematics^{13,16} have primarily
664 focused on a single saccade vector, whereas we compared upward and downward saccades.
665 According to this potential counter argument to our results, by comparing upper and lower
666 visual field saccades, we might have been comparing saccades in which structures
667 downstream from the SC would compensate for the SC asymmetry shown in Fig. 1 and in ref.
668 ²³. Because the above-mentioned studies all showed dissociations between the SC rate code
669 and saccade properties for the very same saccade vector, just like the models of the SC rate
670 code^{13,16}, this counter argument does not seem to be too strong. In addition, we explicitly
671 performed single vector experiments (to response field hotspot locations) in Figs. 6-8, and
672 we found results that were strongly consistent with our original hypothesis. Perhaps most
673 critically, this potential counter argument might imply that the large SC asymmetry in both
674 saccade-related movement burst strengths (Fig. 1) and movement response field sizes²³ just
675 becomes nulled downstream of the SC, which creates the problem of why the asymmetry
676 exists in the SC at all in the first place. It also ignores the fact that the asymmetry has real
677 consequences for saccade latencies, saccade accuracy, and the likelihood of express
678 saccades²³. Rather, we believe that the SC asymmetry motivates investigating what the
679 functional role of SC motor bursts is, and in a more general framework than just one of
680 controlling saccade kinematics.

681

682 Our results also provide complementary evidence to a phenomenon that we recently
683 studied²¹. In that recent study, we altered saccade metrics and kinematics by strategically
684 injecting “visual” bursts into the SC at spatial sites beyond the vector endpoints of the
685 currently executed movements²¹. We found alterations in movement metrics and
686 kinematics²⁰, which were lawfully related to the amounts of visual spikes that we injected
687 onto the SC map around the time of movement triggering²¹. These results were consistent
688 with the spatial code of the SC because the movement metric changes reflected the
689 topographic locations of the injected spikes. However, critically, the movements’ kinematic
690 alterations occurred in the absence of strong alterations in the motor bursts themselves (for
691 the neurons generating the originally planned saccades). This was surprising for a variety of
692 reasons, including ideas related to lateral connectivity patterns in the SC, as we recently
693 discussed²¹. However, it also represented an opportunity for us to explicitly ask, in the
694 current study, whether or not the rate code was indeed as tightly linked to individual
695 movement kinematics. Therefore, here, in the first half of the study (Figs. 1-5), we took the
696 opposite approach from our recent study: we identified a situation in which the motor

697 bursts were different from each other for two different sets of amplitude-matched saccades,
698 and we showed that the saccade kinematics in the two groups of movements were the same
699 (Figs. 1-5). Of course, we also considered the case in which the same saccade vector was
700 made towards the response field hotspot location but with different kinematics (Figs. 6-8).
701 The net result is that either with altered movements and minimally-altered movement
702 commands²¹, or with minimally-altered movements and significantly altered movement
703 commands (Figs. 1-5), or with vector-matched movements of different kinematics and a
704 diversity of SC motor burst effects (Figs. 6-8), there does indeed seem to be a clear
705 dissociation between saccade kinematics and SC motor burst strengths.

706
707 Recent work has suggested that the SC can support high level perceptual and cognitive
708 phenomena^{42,43}. For example, the SC causally influences selective behaviors^{44,45}, and it even
709 shapes object-related visual representations in the ventral visual processing stream⁴⁶. This is
710 in addition to established roles for the SC in target selection⁴⁷⁻⁴⁹. All of this evidence suggests
711 the SC might occupy a functional level that is slightly more abstract than that of specifying
712 individual movement kinematics, consistent with our results. Thus, it might suffice for the SC
713 to specify desired movement metrics, via the spatial code, and also potentially contribute to
714 the decision of when to trigger an eye movement, as recently suggested¹¹. The rest can be
715 handled by downstream oculomotor control structures. If this is indeed the case, then a
716 critical and urgent question for research in the immediate future is: what is, ultimately, the
717 functional role of the SC rate code in visual-motor behavior and perception? One possibility
718 could be that it allows providing a differential gain signal for cortical visual processing. For
719 example, it is known that visual perception⁵⁰⁻⁵³ and attention^{54,55} are better in the lower
720 visual field under conditions of gaze fixation. However, peri-saccadic perceptual
721 mislocalization performance is different for upward saccades⁵⁶. Moreover, when we recently
722 measured perceptual sensitivity in peri-saccadic intervals, at the time of saccadic
723 suppression⁵⁷, we found such sensitivity to be better in the upper visual field instead -
724 consistent with a stronger peri-saccadic suppression of visual sensitivity in the lower visual
725 field⁵⁸. If SC motor bursts contribute to saccadic suppression, perhaps via inhibitory
726 projections to the frontal cortex^{32,59,60}, then a possible functional role for stronger motor
727 bursts in the SC's lower visual field representation could be to differentially modulate
728 cortical visual processing at the time of saccades. It would be interesting to investigate this
729 hypothesis in future studies.

730

731

732 **Methods**

733

734 In this study, we described results from three different sets of experiments, referred to as
735 dataset 1, dataset 2, and dataset 3, respectively.

736

737 In dataset 1, we analyzed data from our previously published study²³. Specifically, neural
738 activity from the SC and saccadic behavior were recorded from two adult, male rhesus
739 macaque monkeys (P and N)²³. We analyzed both neural activity and behavior from that
740 study, using a delayed, visually-guided saccade task.

741

742 In dataset 2, we analyzed saccadic behavior that was recorded from monkey N and a third
743 adult, male monkey (M), again from a previously published experiment³⁶; here, we analyzed
744 additional behavioral parameters from that study that were not previously described. We
745 also analyzed multiple behavioral tasks.

746

747 In dataset 3, we analyzed both saccadic behavior and SC neural activity from adult, male
748 monkeys N, M, and A. The experiments consisted of either single-electrode recordings in
749 monkey M or linear electrode array recordings in all 3 monkeys. The linear electrode array
750 recordings in monkeys N and M were re-analyzed from a previous study³⁷, whereas the
751 linear electrode array recordings from monkey A (aged 10 years and weighing 10 kg), as well
752 as the single-electrode recordings in monkey M, were all newly-performed experiments not
753 previously described in any other publication.

754

755 Thus, we had SC neural recordings from a total of 4 monkeys (M, N, A, and P) and behavior
756 from a total of 3 monkeys (M, N, and P) in this study.

757

758 All experiments were approved by the Regierungspräsidium Tübingen, under licenses
759 CIN3/13 and CIN4/19G, and they were in accordance with the German and European
760 directives on the use of animals in research.

761

762 In what follows, we describe detailed methods relevant for the current work.

763

764

765 *Animal preparation*

766

767 For SC recording, a recording chamber was implanted centered on the midline in all 4
768 monkeys. The midline positioning of the chamber allowed recording from both the right and
769 left SC in each animal. Magnetic resonance images (MRI's) obtained prior to the experiments
770 aided in chamber implant alignment. We aimed for quasi-orthogonal electrode penetrations
771 (relative to the SC curvature) at eccentricities we typically use in experiments (e.g. 5-15 deg).

772

773 Before receiving the chamber implants, the animals were also implanted with head-holding
774 apparatuses and scleral search coils for eye tracking, as described earlier⁶¹⁻⁶³. The scleral
775 search coils allowed using the magnetic induction technique for measuring eye positions^{64,65}.
776 Specifically, a coil of wire was implanted around the sclera of the eye and below the
777 conjunctiva. The animals were then seated near the middle of a cube in which alternating
778 magnetic fields induced electrical current (which depended on ocular position) in the
779 implanted scleral coil; we measured and calibrated this electrical current.

780

781

782 *Behavioral tasks*

783

784 For both neural and behavioral analyses, the monkeys performed classic saccade generation
785 tasks.

786

787 In the immediate, visually-guided saccade task of dataset 2 (which was only used in
788 behavioral experiments and not neurophysiological experiments), the monkey first fixated a
789 central spot. After a variable delay, the spot was jumped to another location, and a saccade
790 to follow the spot was triggered.

791

792 In the delayed version of the same task, during initial fixation, the fixation spot remained
793 visible while an eccentric spot was presented. The monkey was required to maintain gaze
794 fixation and withhold any reflexive orienting towards the eccentric spot for as long as the
795 central fixation spot was visible. After the fixation spot was removed, the monkey generated
796 a saccade towards the (still visible) eccentric spot.

797

798 Finally, in the memory-guided saccade task, during initial fixation, the eccentric spot was
799 only flashed briefly (for approximately 50 ms). A delay period then ensued in which only the
800 fixation spot was visible, and the monkey was required to maintain gaze fixation on it. At the
801 end of this so-called memory period, the fixation spot was extinguished, instructing the
802 monkey to generate a saccade towards the remembered location of the previous flash (i.e.
803 towards a blank location on the display).

804

805 The delayed, visually-guided saccade task was used for all neural analyses reported in this
806 study (dataset 1 and dataset 3). This was important because this task allows dissociating
807 visual burst intervals from the saccade-related motor burst intervals that we were interested
808 in analyzing. The memory-guided saccade task was also used for neural analyses in dataset
809 3. For behavioral analyses, we used the delayed saccade task in dataset 1 (e.g. Fig. 2), as well
810 as all 3 saccade tasks in dataset 2.

811

812 For mapping response fields, we generally employed the delayed, visually-guided and
813 memory-guided saccade tasks. However, in the newly-acquired portions of dataset 3
814 (monkey M single-electrode recordings and monkey A linear electrode array recordings), we
815 first mapped response fields with a fixation variant of the delayed, visually-guided saccade
816 task. That is, at the end of the trial, instead of fixation spot removal to release a visually-
817 guided saccade towards the eccentric target, the monkey was simply rewarded for fixating
818 until trial end. This allowed us to obtain visual response fields, and we then later tested for
819 saccade-related bursts using the delayed, visually-guided and memory-guided saccade tasks.

820

821 In all cases, stimuli were presented on cathode ray tube (CRT) displays, with stimulus
822 luminances and dimensions having been described earlier^{23,36,66}. The timing of trial events in
823 the tasks was also described earlier. For the present study, the primary focus was on the
824 individual saccade kinematics at the ends of all trials, irrespective of timing parameters, such
825 as the length of the delay or memory period, and irrespective of the exact stimulus visual
826 properties. The effects of these factors (such as trial timing or visual stimulus properties)
827 were described earlier^{23,36,67,68}.

828

829

830 *Behavioral data analyses*

831

832 All saccades from datasets 1 and 2 were detected for the previous two studies^{23,36}. Here, we
833 analyzed the kinematic properties of the movements. For dataset 3, the saccades from the
834 electrode array recordings of monkeys M and N were also detected previously³⁷. The
835 saccades from the newly-acquired monkey M and monkey A recordings were detected using
836 our standard approaches^{61,69}.

837

838 For behavioral analyses in dataset 1, we picked saccades having +45 or -45 deg direction
839 from the horizontal meridian (i.e. oblique saccades). We then picked 5 radial amplitude
840 categories to characterize 5 different ranges of saccade sizes (Fig. 2). The categories were: 3,
841 5, 7, 10, and 13 deg. For each of these categories, we picked all saccades landing within a
842 radius of 0.5, 0.8, 1, 2, and 3 deg from the designated amplitude/direction category,
843 respectively. For example, for saccades of 7 deg amplitude and +45 deg direction, we picked
844 all saccades that were upward and oblique, and that were directed towards an eccentricity
845 of 7 deg, and that landed within a radius of 1 deg from this eccentricity. Similarly, for 3 deg
846 saccades of +45 deg direction, we picked all upward oblique movements towards an
847 eccentricity of 3 deg and landing within a radius of 0.5 deg from it. This meant that we had
848 amplitude- and direction-matched saccades for either the oblique upward or the oblique
849 downward movements. We then plotted the trajectories (Fig. 2a) and radial speed profiles
850 (Fig. 2b) of all of these saccades. Since the speeds of temporally-directed saccades could be
851 different from the speeds of nasally-directed saccades for a given tracked eye, we analyzed
852 rightward and leftward saccades separately in this dataset (Fig. 2b). However, in dataset 2,
853 all saccade directions were combined, and with similar conclusions.

854

855 For dataset 2, we had a large range of saccade amplitudes and directions to analyze³⁶. We
856 plotted the main sequence relationship^{34,35} for these saccades after separating them into
857 two groups: saccades towards the upper visual field and saccades towards the lower visual
858 field. We plotted both the main sequence relationship of peak speed versus movement
859 amplitude (Fig. 4) and saccade duration versus movement amplitude (Fig. 5). For
860 comparison, we included a plot of saccadic reaction times for the same saccades in Fig. 4.
861 This was a replotting of the reaction time data already reported earlier³⁶, and we included it
862 here for easier comparison of the difference in effects of visual field location on saccade
863 kinematics and saccade reaction times. In total, we analyzed 1246, 928 visually-guided
864 saccade trials, 6147, 5871 delayed, visually-guided saccade trials, and 6428, 9631 memory-
865 guided saccade trials from monkeys N and M, respectively. The numbers of trials for the
866 behavioral analyses from dataset 1 are reported in the figure legend of Fig. 2.

867

868 For dataset 3, our behavioral analyses consisted of first ensuring vector matching and then
869 checking the movement kinematics to set the stage for neural data analyses. For the
870 previously collected data³⁷ (monkey M and monkey N linear electrode array recordings),
871 response fields were mapped with both the delayed, visually-guided and memory-guided
872 saccade tasks. Therefore, in offline analyses, we obtained the average firing rate in the
873 interval of -25 ms to +25 ms from saccade onset for each movement. We then plotted heat
874 maps of firing rate as a function of saccade horizontal and vertical amplitudes to confirm the
875 response fields. We identified the hotspot location of each neuron from the visually-guided

876 saccade response field, and we then picked all saccades in both tasks landing within 2 deg, 1
877 deg, or 0.5 deg of this location depending on the neuron's preferred eccentricity (within 2
878 deg for neurons with preferred eccentricity > 3 deg, within 1 deg for neurons in the range of
879 2-3 deg preferred eccentricity, and within 0.5 deg for foveal neurons). We only included
880 neurons for which we had at least 5 vector-matched saccades in each of the visually-guided
881 and memory-guided saccade conditions.

882
883 For the newly-collected measurements of dataset 3 (monkey M single-electrode recordings
884 and monkey A linear electrode array recordings), after mapping visual response fields with
885 the fixation task (described above), we ran delayed, visually-guided saccades and memory-
886 guided saccades towards the hotspot location (as assessed online during the experiment),
887 collecting at least 20 trials per task. We then checked for endpoint matching. We found the
888 median landing position from the delayed, visually-guided saccade task. Then, we only
889 included saccades in both tasks that landed within 1 deg from this position. Once again, we
890 only included neurons for which we had at least 5 vector-matched saccades in each of the
891 visually-guided and memory-guided saccade conditions (typically much more).

892
893 After finding vector-matched saccades in dataset 3, we then proceeded to plot radial eye
894 speed for the delayed, visually-guided and memory-guided saccade tasks. We also collected
895 measurements per session as follows: average saccade amplitude, average saccade
896 direction, and average saccade peak speed. This allowed us to plot these parameters across
897 the two tasks (e.g. Fig. 8a-c), to confirm vector matching as well as to confirm different
898 saccade kinematics across the two conditions.

899
900 To obtain a single behavioral modulation index across the two tasks in dataset 3, we
901 measured, in each session, the average peak saccade speed in the memory-guided condition
902 and the average peak saccade speed in the delayed, visually-guided condition. We
903 subtracted the latter from the former, and then divided by the sum of the two. This gave us
904 an index that ranged in values from -1 to +1, with indices >0 indicating that peak saccade
905 speed was higher in the memory-guided condition and indices <0 indicating that peak
906 saccade speed was higher in the delayed, visually-guided saccade condition. This gave us a
907 single number that we could relate to a similar single number for SC motor burst strength
908 modulation by the behavioral task (as described later below).

909

910

911 *Dataset 1 neural data analyses (Fig. 1)*

912

913 We analyzed peri-saccadic firing rates, as we did previously²³. We obtained firing rates by
914 convolving individual spike times with a gaussian kernel of 40 ms σ . For each neuron in the
915 database of the previous study (containing >400 neurons), we had identified (for saccade-
916 related neurons) the saccades towards the neuron's preferred movement-related response
917 field location (i.e. the locations for which the neuron's saccade-related bursts were the
918 strongest). In the present study, we analyzed the firing rates for these preferred saccades.
919 However, we constrained the choice of neurons according to the needs of the current study.
920 Specifically, besides only considering extra-foveal neurons with saccade-related bursts, we
921 matched neural depths between neurons from the upper and lower visual field
922 representations of the SC (e.g. Fig. 1a). Specifically, since saccade-related motor bursts in the
923 SC can vary in strength as a function of depth of the neurons from the SC surface⁶, we only

924 compared motor bursts after selecting neurons from the upper and lower visual field
925 representations that had matched depths.

926

927 To do so, we first considered all neurons in the upper and lower visual field representations
928 having a depth of 600-1850 μm from the SC surface. This range of depths is consistent with
929 known depths of saccade-related activity in the SC⁶. Importantly, for the present purposes,
930 this range of depths contained clear overlap between neurons in the upper and lower visual
931 field SC representations (Fig. 1a). This allowed comparing the strengths of motor bursts
932 between the selected depth-matched neurons. The resulting neural database had 136
933 neurons (Fig. 1).

934

935 To further confirm that there was no confound of neural depth from the SC surface in
936 interpreting a visual field asymmetry in motor burst strength, we were concerned that the
937 curvature of the SC surface could introduce systematic biases in depths of upper versus
938 lower visual field neurons from the SC surface. For example, it could potentially be the case
939 that the 3-dimensional SC surface curvature combined with a constant electrode approach
940 angle dictated by the recording chamber might systematically skew depth estimates: medial
941 (upper visual field) electrode locations might potentially have depth estimates that could be
942 systematically different from lateral (lower visual field) electrode locations in the chamber.
943 This could simply be a function of whether or not a given electrode track was more or less
944 perpendicular to the local SC surface topography at a given site. In our second analysis of
945 neural activity, we therefore picked a range of electrode locations in which we expected
946 minimal changes in SC curvature between upper and lower visual field representations. For
947 example, mapping the SC surface topography on the anatomical SC³³ might suggest a similar
948 relationship between electrode angle and SC surface for upper and lower visual field
949 representations near the horizontal meridian and within a specific range of movement
950 amplitudes. We therefore specifically picked neurons with movement-related response field
951 hotspots near the horizontal meridian (within 30 deg direction in either the upper or lower
952 visual fields) and with radial eccentricities of only 5-15 deg. We also picked a narrower depth
953 of neurons for the comparison (1100-1900 μm from SC surface). With this stricter neural
954 database (31 neurons), we again plotted peri-saccadic firing rates for neurons in the upper
955 and lower visual field representations (Fig. 1c).

956

957 In all cases, a neuron was considered to be part of the upper or lower visual field
958 representation if its preferred saccade (i.e. the movement-related response field hotspot
959 location) was in the upper or lower visual field, respectively. This was also consistent with
960 the known SC topographic representation^{1,3,23,33}, and it was already done in our previous
961 study²³.

962

963 To statistically compare saccade-related activity strength between the upper and lower
964 visual field representations in the SC, we measured the average firing rate in the final 50 ms
965 before saccade onset for each neuron. We then statistically compared the firing rates of all
966 neurons having movement-related response field hotspot locations in the upper visual field
967 to the firing rates of all neurons having response field hotspot locations in the lower visual
968 field (using t-tests). Note that measuring average firing rates is equivalent to counting spikes,
969 which has been the standard method to analyze the rate code^{13,18}. Also note that in our
970 analyses of dataset 3 recordings (described below), we also picked a peri-movement burst

971 measurement (that is, including epochs also after saccade onset) rather than only a pre-
972 movement measurement as in dataset 1, with similar conclusions to this dataset's results.
973

974

975 *Dataset 3 neural data analyses (Figs. 6-8)*

976

977 We collected 25 sessions of linear electrode array recordings in monkey N, 16 sessions of
978 linear electrode array recordings and 32 sessions of single-electrode recordings in monkey
979 M, and 12 sessions of linear electrode array recordings in monkey A (all array recordings
980 were performed with V-probes from Plexon, Inc.). The linear electrode array recordings from
981 monkeys N and M were a subset of those described for a previous study³⁷.
982

983

984 We used offline sorting to identify single neurons. For the single-electrode recordings, we
985 used Plexon's Offline Sorter utility. The visually-guided and memory-guided saccade tasks
986 were collected (in sequence) together in the same file, and we sorted both tasks together.
987 For the linear electrode array recordings, we performed offline sorting using Kilosort⁷⁰,
988 followed by manual curation using the phy software. For the data from ref. ³⁷, we used the
989 same sorting results that were obtained for the original study. Isolated neurons that
990 exceeded an estimated false positive rate (ISI violation) of 10% or had an isolation distance
991 below 30 were excluded from further analysis. We sorted linear electrode array recording
992 data from an entire session simultaneously, thus tracking neurons across the different tasks
993 that we ran (typically much more than the visually-guided and memory-guided saccade
994 tasks). To check isolation stability (e.g. for Fig. 6c), we collected 2000 spike waveforms
995 selected randomly from the same session. For our two tasks of interest, we took the
996 waveforms from this sampling of waveforms that happened to come from either of the two
997 tasks, and we plotted their distributions. Because the two tasks were typically run in
998 succession, it was usually very likely that isolation was stable throughout both of them. This
999 was also the case in the single-electrode recordings.

1000

1001 For each of the vector-matched saccades, we defined a motor interval as the 50-ms interval
1002 centered on saccade onset (that is, the interval spanning -25 to +25 ms from saccade onset).
1003 We also defined a baseline interval as the final 50-ms interval before stimulus onset (at trial
1004 beginning). We then statistically compared the baseline interval firing rate to the motor
1005 interval firing rate using either a t-test (for all the newly-collected data) or a ranksum test
1006 (for the data from ref. ³⁷). The choice of test was dictated by the fact that the old data had
1007 fewer numbers of trials because we selected saccades from response field mapping data,
1008 whereas in the newly-collected sessions, we explicitly collected repeated saccades from the
1009 same response field hotspot location. We only included a neuron if it had a significantly
1010 elevated average firing rate in the motor interval relative to the average firing rate in the
1011 baseline interval ($p < 0.05$) in either the delayed, visually-guided saccade task or the memory-
1012 guided saccade task or both.

1013

1014 To check for changes in SC motor bursts across visually-guided and memory-guided
1015 saccades, we calculated the peak firing rate in the motor interval (-25 to +25 ms from
1016 saccade onset) in each condition. We then calculated a neural modulation index similar to
1017 how we computed the behavioral modulation index above. That is, we subtracted peak firing
rate in the visually-guided saccades from peak firing rate in the memory-guided saccades,

1018 and we divided by the sum of peak firing rates. Thus, a neural modulation index >0 indicated
1019 stronger SC motor bursts for memory-guided than visually-guided saccades.

1020

1021

1022 *Statistics and reproducibility*

1023

1024 We analyzed SC recording data from 4 different monkeys, with consistent results. Similarly,
1025 we analyzed behavioral measurements from 3 monkeys. These numbers of animals increase
1026 confidence in the generalizability of the results, especially given how some observations
1027 were highly consistent with a large literature on SC saccade-related bursts (e.g. the depth
1028 profile shown in Fig. 1a).

1029

1030 For neural analyses, we statistically compared upper and lower visual field motor bursts on a
1031 neuron per neuron basis (Fig. 1). Similarly, in Figs. 6-8, we compared burst strengths on a
1032 neuron per neuron basis. In all cases, we collected a large enough sample of neurons to
1033 increase statistical confidence in the observations.

1034

1035 For eye movement analyses, we employed minimum count requirements (e.g. for the vector
1036 matching in the experiments of Figs. 6-8) to ensure enough replicates. Similarly, we used
1037 large numbers of replicates in the behavioral measurements of Figs. 2-5.

1038

1039 All relevant statistical tests are indicated in the figure legends or the associated Results text.
1040 Also, numbers of observations are indicated in the figures, in the figure legends, in Results,
1041 or in the Methods text.

1042

1043

1044 **Data availability**

1045

1046 The datasets generated during and/or analysed during the current study are available from
1047 the corresponding author on reasonable request.

1048

1049

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1259 **Author contributions**

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1261 ZMH collected and analyzed datasets 1 and 2. TZ, TM, MPB, and ZMH collected and analyzed
1262 dataset 3. All authors wrote the manuscript.

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1265 **Declaration of interests**

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1267 The authors declare no competing interests.

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