

The heart rate discrimination task: a psychophysical method to estimate the accuracy and precision of interoceptive beliefs

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Abstract (150 words):

Interoception - the physiological sense of our inner bodies - has risen to the forefront of psychological and psychiatric research. Much of this research utilizes tasks that attempt to measure the ability to accurately detect cardiac signals. Unfortunately, these approaches are confounded by well-known issues limiting their validity and interpretation. At the core of this controversy is the role of subjective beliefs about the heart rate in confounding measures of interoceptive accuracy. Here, we recast these beliefs as an important part of the causal machinery of interoception, and offer a novel psychophysical “heart rate discrimination” method to estimate their accuracy and precision. By applying this task in 223 healthy participants, we demonstrate that cardiac interoceptive beliefs are more biased, less precise, and are associated with poorer metacognitive insight relative to an exteroceptive control condition. Our task, provided as an open-source python package, offers a robust approach to quantifying cardiac beliefs.

Highlights (85 chars each):

- Current interoception tasks conflate cardiac beliefs with accuracy.
- We introduce a Bayesian method for estimating cardiac belief accuracy and precision.
- Individuals underestimate their heart rate by -7 BPM (95% CI [-8.6 -5.3]) on average.
- Cardiac beliefs are associated with reduced precision and metacognitive insight.
- The task and modelling tools are provided in the Python Cardioception Package.

keywords: heart rate discrimination, heartbeat tracking, interoception, psychophysics, metacognition

1 Introduction

2 Interoception denotes the ability to sense, perceive, and regulate internal visceral states (Chen
3 et al., 2021; Sherrington, 1952). This ability is thought to depend on unique neurobiological
4 pathways, which underpin the affective and somatic axes of selfhood (Craig, 2002; Critchley
5 & Garfinkel, 2017; Seth & Tsakiris, 2018; Strigo & Craig, 2016). Measuring the individual
6 interoceptive capacity to detect visceral signals, such as those arising from the lungs, heart, or
7 stomach has recently come to the forefront of psychological and psychiatric research (Khalsa
8 et al., 2018; Khalsa & Lapidus, 2016). A critical objective of this work is to determine the
9 mechanisms by which interoception interacts with cognition and emotion, to ultimately derive
10 sensitive and specific neuropsychiatric biomarkers from individual indices of visceral
11 sensitivity. The majority of studies along these lines attempt to measure “interoceptive
12 accuracy” (iACC) in the cardiac domain, as measured by the Heartbeat Counting (HBC) task
13 (Dale & Anderson, 1978; Schandry, 1981), and similar heartbeat tracking or tapping tasks
14 (Flynn & Clemens, 1988). While easy to implement, these tasks suffer from serious
15 methodological challenges that obscure their interpretation. To overcome these challenges, we
16 developed a novel psychophysical approach to measure the accuracy, bias, and precision of
17 interoceptive beliefs in the cardiac domain.

18 The measurement of interoceptive accuracy presents a unique challenge compared to that
19 of exteroception: unlike vision or touch, the heart is not typically amenable to direct
20 experimental control. The inability to control the information present in the stimulus (e.g., the
21 heartbeat) places hard constraints on interoception research, such that most extant tasks ask
22 participants to count uncontrolled endogenous states (e.g., heartbeats) or to determine whether
23 exteroceptive stimuli are synchronized with said states. While these tasks are widely used, they
24 suffer from several confounds which place strong limitations on their reliability,
25 interpretability, and validity (for review see Brener & Ring, 2016; Desmedt et al., 2018;
26 Desmedt, Corneille, et al., 2020; Ring & Brener, 2018; Zamariola et al., 2018).

27 A central issue associated with the use of the HBC or similar tasks concerns the role of
28 subjective beliefs about one's heart rate. These simple measures require participants to silently
29 attend to and count their heartbeats for various intervals, or to tap in rhythm to felt beats. Several
30 authors point out that participants could exploit various strategies to increase their accuracy
31 (Clemens, 1979; Flynn & Clemens, 1988; Pennebaker & Hoover, 1984). Crucially, even when
32 the heart rate is directly modulated by as much as 60 beats per minute (BPM) via pacemaker,
33 counted heartbeats showed little alteration beyond expectations about different sitting or

34 standing postures on the heart rate (Windmann et al., 1999). Accordingly, participants'
35 subjective prior beliefs about the heart rate have been repeatedly found to be more predictive
36 of counts than actual heartbeats (Ring & Brener, 1996), and it has been shown that these beliefs
37 can be manipulated via false feedback independently of any true change in heart rate (Ring et
38 al., 2015). A more accurate prior knowledge about one's heart rate, e.g. amongst medical
39 practitioners or athletes, can influence HBC accuracy scores (Murphy et al., 2018), such that
40 when explicitly instructing participants not to estimate beats, but to instead count felt ones, this
41 bias is reduced (Desmedt et al., 2018). More recently, the validity of the HBC task has been
42 further questioned by reports showing that interoceptive accuracy scores are largely driven by
43 under-counting (Zamariola et al., 2018), suggesting that HBC-derived scores are merely a
44 rough reflection of subjective beliefs about the heart rate (Desmedt, Luminet, et al., 2020).

45 These reports raise serious concerns given the rising interest in interoceptive
46 measurements as potential psychiatric biomarkers (Eggart et al., 2019; Forkmann et al., 2019;
47 Paulus & Stein, 2010). This poor construct validity could also explain why little to no
48 relationship between HBC-derived scores and various psychiatric symptom measures has been
49 found at the meta-analytic level (Desmedt, Houte, et al., 2020). Here, we argue that the
50 inconsistencies between these HBC-derived scores and interoceptive ability could be better
51 handled by more rigorous measurement and modelling of the role of subjective beliefs in
52 cardiac interoception. Although these tasks were originally designed to be objective and
53 selective measures of the ability to detect afferent cardiac sensory information, they fail to
54 account for factors confounding score variances, such as prior beliefs about the heart rate and
55 other common introspective or self-report biases. In particular, these approaches struggle to
56 dissociate interoceptive sensitivity, bias, and accuracy, confounding the role of subjective vs.
57 objective performance in interoceptive measures.

58 Another commonly used task, the Heartbeat Discrimination (HBD) task (Whitehead et
59 al., 1977), suffers from different, but similarly serious drawbacks. This method presents
60 participants with a series of tones whose onset times are delayed at different intervals relative
61 to the R-wave. Tones presented approximately at systole (typically, R + 170 ms) are treated in
62 signal theoretic terms as the “signal plus”, while tones presented at a variable time after systole
63 (typically, R + 300 ms) are treated as “signal minus”. This design is based on strong
64 assumptions about when, relative to the cardiac phase, participants are most likely to feel the
65 heartbeat. These assumptions have been challenged by results obtained using a similar task
66 based on a method of constant stimuli (MCS), where tones are presented at 5 different intervals
67 with respect to the R-wave.

68 Using this MCS-based method, Brener and colleagues demonstrated that individuals vary
69 substantially in terms of when relative to r-wave, heartbeats are perceived (Brener et al., 1993;
70 Brener Jasper & Ring Christopher, 2016; for review see Ring & Brener, 2018) and that
71 calibrating the HBD offset intervals to each subject improves detection scores to above chance,
72 seriously undermining the notion that the HBD can be used as a signal theoretic measure to
73 delineate cardiac sensitivity and bias. However, while the MCS likely improves the
74 quantification of single-beat detection when compared to the HBD, both tasks require
75 participants simultaneously to attend to exteroceptive and interoceptive multi-sensory inputs, a
76 difficult cognitive task that further obscures the relationship to interoception. Moreover, the
77 MCS requires long testing times (as much as 1 hour), which can be problematic for clinical
78 populations, and further requires sophisticated equipment capable of achieving precise cardiac-
79 tone synchrony and stimulus time. As such, there is a need for robust, accessible measures that
80 are amenable to clinical settings, and which can flexibly dissociate the bias, sensitivity, and
81 precision of cardioceptive decisions.

82 To achieve this, we developed the heart rate discrimination task (HRD), a novel
83 psychophysical approach to quantifying cardioceptive decisions. Through Bayesian modelling
84 of cardiac psychophysics, the HRD delineates the accuracy of cardiac beliefs into the bias (i.e.,
85 the error between the perceived HR versus ground truth), and precision (i.e., the uncertainty
86 around this estimate) of trial by trial cardiac decisions. By presenting stimuli dynamically
87 across trials, titrated to the current heart rate, this approach estimates psychometric perceptual
88 and metacognitive curves indicating participants' ability to update and monitor cardiac beliefs
89 under different conditional manipulations.

90 To demonstrate the utility of the HRD for measuring cardiac beliefs, characterize the
91 overall interoceptive psychometric function, and establish the face validity of this approach, we
92 measured HRD performance in 223 participants at a resting heart rate while seated upright in a
93 standard testing booth, together with heartbeat counting scores. To further quantify internal
94 (test-retest) reliability, we re-tested HRD performance in the same participants following 6
95 weeks. Our results demonstrate that cardioceptive beliefs are reliably and robustly measured by
96 the task across both sessions. Further, we find that cardioceptive beliefs are more negatively
97 biased, imprecise, and associated with poorer metacognitive insight relative to an exteroceptive
98 control condition.

99 Methods

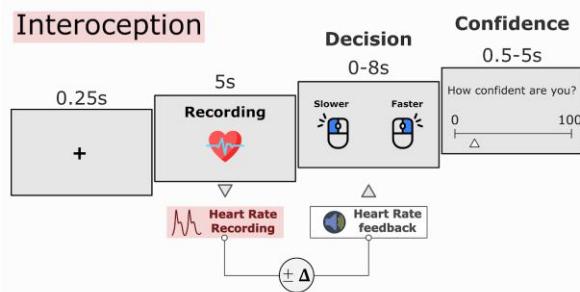
100 Heart Rate Discrimination task

101 Task Overview

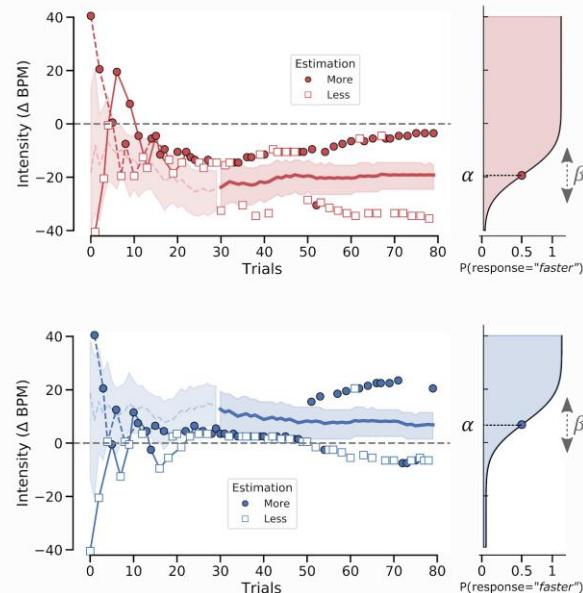
102 To measure the bias, precision, and metacognitive calibration of interoceptive beliefs, we
103 created the Heart Rate Discrimination task (HRD) (See **Fig. 1**). The goal of the HRD is to
104 provide an efficient method for measuring the influence of subjective beliefs, viscerosensory
105 inputs, and other possible contextual factors on interoceptive decisions about heart rate. The
106 task asks participants to first attend to their cardiac sensations and then to decide on each trial
107 whether a “feedback” tone series is faster or slower than their heart rate in a 2-Interval Forced
108 Choice design (2-IFC). To control for possible non-interoceptive processes such as working
109 memory or general temporal estimation biases, we also implemented an exteroceptive control
110 condition, in which participants had to discriminate whether a series of tones was faster or
111 slower than another “reference” sequence of tones.

112

a. Heart Rate Discrimination task



b. Slope and threshold estimates of interoceptive and exteroceptive psychometric functions



113

114 **Legend Figure 1: A. Heart Rate Discrimination Trial Design (Session 1).** Participants were presented with 160 trials testing their exteroceptive (blue) and interoceptive (red) bias and precision (80 in each condition in randomised interleaved order). During interoceptive trials, participants were instructed to attend to their heart rate for 5 seconds, while it was recorded using a pulse oximeter. The average heart rate for the trial was then computed and used to select the frequency of the tones presented during the decision phase, increased or decreased by an intensity value generated by the staircase, i.e. Δ -BPM. During exteroceptive trials, a sequence of tones was

120 presented to the participant with a frequency between 40 and 100 BPM, drawn randomly from a uniform
121 distribution. This value then determined the frequency of the tones presented during the decision phase, increased
122 or decreased by a value generated by the staircase procedure. Δ -BPM values were controlled by separate staircases
123 for each condition. To estimate metacognitive ability for each modality, at the end of each trial, participants were
124 asked to rate their subjective decision confidence (from 0 - guess to 100 - certain). **B. Staircases for each**
125 **condition from an exemplary subject.** Trials classified by participants as faster or slower are depicted with
126 circles or squares respectively. The shaded area represents the 95% CI of the threshold posterior distribution. On
127 the right panel, the resulting cumulative normal distribution is plotted using the final parameters estimated by the
128 Psi procedure.

129

130 To estimate psychometric functions for both conditions, we applied a well-established adaptive
131 Bayesian psychophysical method (“Psi”) (Kingdom & Prins, 2016; Kontsevich & Tyler, 1999;
132 Prins & Kingdom, 2018). This technique adaptively estimates the probability of a participant
133 responding that the feedback tones were “faster” or “slower” than the true heart rate
134 (interoception), or the reference tone (exteroception) on each trial, given the frequency
135 difference between the two stimuli, or Δ -Beats Per Minute (Δ -BPM). This procedure estimates
136 the point of subjective equality (PSE) both for interoceptive and exteroceptive decision
137 processes in the same Δ -BPM units. The PSE is henceforth referred to as the threshold of the
138 psychometric function. This threshold represents the difference between the true frequency of
139 the heart rate and the estimated cardiac frequency by the participant (see **Fig. 1.** the threshold
140 is denoted α). A negative threshold, therefore, indicates the degree to which a participant
141 underestimates their cardiac frequency, while a positive threshold indicates an overestimation.
142 In addition to the threshold measure, the procedure further estimates the slope of the
143 psychometric function (denoted β in **Fig. 1.**), which represents the precision, or uncertainty,
144 around this estimated perceptual bias, also in units of Δ -BPM. A larger slope value reflects a
145 less steep psychometric curve, indicating increased uncertainty (i.e. reduced precision) in the
146 cardioceptive decision process.

147 HRD Trial Design

148 During interoceptive trials, participants silently attend to their heart rate for 5 seconds, e.g., in
149 a “heart listening” phase (see **Fig.1**), during which the heart rate is monitored using a soft-clip
150 pulse oximeter placed on one of the fingers of the non-dominant hand. The raw signal is
151 analyzed in real-time using a systolic peak detection algorithm, and the heart rate is calculated
152 as the average of the inter-pulse interval (see **Physiological Analyses**, below). After this
153 listening phase another sequence of five auditory tones was presented (frequency: 440 Hz;

154 duration: 200 ms). This “two-interval” design is a deliberate choice so that participants attend
155 solely to their cardiac sensation before the presentation of auditory feedback.

156 At any point during the auditory feedback, the participant can press the right or left mouse
157 button to indicate whether the feedback sequence was faster or slower than their estimated
158 average heart rate, terminating the response and feedback period. The maximum response time
159 for the type 1 decision task was 8 seconds. Following the decision interval, participants provide
160 a subject confidence rating (from 0 - uncertain to 100 - certain, minimum possible response
161 time: 0.5 seconds; maximum: 5 seconds), and the next trial begins. To prevent motor
162 preparation of the confidence rating, the starting point of the rating scale cursor is randomly
163 jittered around the midpoint by about +/- 70% of the scale length.

164 Crucially, the frequency of the second tones was adjusted to the frequency of the first
165 tones (exteroceptive modality) or the recorded cardiac frequency (interoceptive modality). This
166 difference is denoted Δ -BPM and corresponds to the stimulus intensity manipulated by the
167 staircases (see the *Staircase procedure* section below). For example, if the heart rate recorded
168 during the listening condition is 60 BPM, and the Δ -BPM value is -15, the feedback tone
169 frequency will be set to 45 BPM. In this example, if the participant answers “Slower”, this is
170 considered a correct answer, otherwise, this is considered an incorrect answer. In this way, the
171 staircase procedure hones in on the point of subjective equality, or threshold (α), at which the
172 participant is equally likely to respond “Faster” or “Slower”.

173 During exteroceptive trials, participants compared two sequences of tones, instead of
174 comparing their heart rate with the feedback tone sequence. Here, the first (“reference”) tone
175 sequence frequency was randomly selected from a uniform distribution (lower bound = 40
176 BPM, upper bound = 100 BPM, signal frequency: 440 Hz; tone duration: 200 ms), and the
177 second tone sequence frequency presented at a BPM above or below this value as determined
178 by the staircase procedure. After this listening phase, the participants underwent the same
179 decision and confidence task as in the interoceptive trials, that is, to decide whether the second
180 sequence was faster or slower than the first one. The tone presentation ceased when the response
181 was provided (maximum response time: 8 seconds). As in the interoceptive condition, the
182 intensity Δ -BPM was adjusted across trials using the same adaptive Bayesian approach for
183 estimating threshold and slope.

184 Adaptive Staircase Procedure

185 The primary aim of the HRD task is to estimate the difference between the objective heart rate
186 and the participant's subjective perception of this heart rate (i.e., the threshold α), as well as the

187 precision or uncertainty around this perceptual belief (i.e., the slope β). The HRD achieves this
188 via an adaptive staircase procedure which manipulates the Δ value that was added to the true
189 BPM to produce the feedback tone frequency. This psychophysical procedure can be described
190 as an appearance-based 2-Interval Forced Choice (2-IFC) similar to the 2-Alternative Forced
191 Choice procedure implemented in the Vernier-alignment task, (Kingdom & Prins, 2016,
192 Chapter 3.3), where varying the degree of difference between two stimuli allows estimating the
193 threshold (α) and the slope (β) of the underlying decision process. In our implementation, HRD
194 thresholds are adaptively estimated using either two interleaved standard n-up/n-down
195 staircases (the first steps were manually fixed to: {20, 12, 12, 7, 4, 3, 2, 1}; starting value: -40.5
196 and 40.5) (Dixon & Mood, 1948), or using an adaptive method known as Psi (Kontsevich &
197 Tyler, 1999).

198 Psi is a Bayesian adaptive psychophysical method that manipulates the Δ -BPM deviation
199 values and estimates the slope and the threshold of the underlying sensory psychometric
200 function (Kingdom & Prins, 2016; Prins & Kingdom, 2018). The psychometric function relates
201 the deviation Δ to the proportion of “Faster” decisions using the following formula:

202
$$\psi(\Delta; \alpha, \beta, \gamma, \lambda) = \gamma + (1 - \gamma - \lambda)F(\Delta; \alpha, \beta)$$

203 in which Δ refers to stimulus intensity, ψ refers to the proportion of trials rated as faster by the
204 participant, and γ and $1 - \lambda$ are nuisance parameters corresponding to the lower and upper
205 asymptote, respectively. F is the cumulative normal distribution parameterized using threshold
206 α and slope β . The parameter λ is often referred to as the *lapse rate* and describes the probability
207 of a stimulus-independent negative response (here, the probability of answering “slower”
208 regardless of the frequency of the tones). In appearance-based 2-IFC tasks like the HRD, the
209 lapse rate determines both γ and $1 - \lambda$. Here, this parameter was fixed, because it is assumed that
210 responses obtained from this kind of task only contain limited information on the real value of
211 this parameter. Further, the estimation of the lapse rate as a free parameter can potentially
212 introduce bias (Prins, 2012). Here, we assumed that $\gamma = \lambda = 0.02$.

213 Irrespective of the staircase procedure (i.e., n-up/n-down or Psi), it should be noted that
214 the psychometric function was not fitted to the proportion of correct trials given the Δ intensity,
215 but on the probability of a participant making a “Faster” response given the Δ intensity (see
216 **Fig. 1b**). This procedure is known as an appearance-based staircase and entails that the
217 probability of a participant answering “Faster” given an increasing Δ -BPM value is expected
218 to follow a monotonic psychometric function. However, this is not the case for the probability

219 that the response is correct relative to the ground truth HR. Here, the probability of answering
220 correctly increases with Δ -BPM increments towards either positive or negative infinity and is
221 0.5 around the threshold. As a consequence, the online estimation of an accuracy-based
222 staircase requires dedicated adaptive methods for non-monotonic psychometric functions
223 (García-Pérez, 2014).

224 **Python Cardioception Package**

225 We implemented two interoception tasks using Psychopy v3.2.3 (Peirce et al., 2019), the classic
226 Schandry Heartbeat Counting Task (Dale & Anderson, 1978; Schandry, 1981), and the Heart
227 Rate Discrimination task. The code for the two interoception tasks is made publicly available
228 in the Cardioception Python Package (<https://github.com/embodied-computation-group/Cardioception>). The package natively supports recording and processing pulse rate
229 activity as recorded by the Nonin 3012LP Xpod USB pulse oximeter together with a Nonin
230 8000SM “soft-clip” fingertip sensor (<https://www.nonin.com/>) by interfacing with the Systole
231 python package for pulse oximetry (Legrand & Allen, 2021).
232

233

234 **Participants**

235 223 participants between the ages 18 and 56 (130 females, 93 males, 1 other, age = 25.0 ± 5.50)
236 participated in the study. They were recruited through the Center of Functionally Integrative
237 Neuroscience (CFIN) SONA system participant pool, local advertisements and flyers, social
238 media, and the aarhusbrain.org website. All measures took place at Aarhus University Hospital,
239 Denmark, and were performed on a computer in a behavioural testing room. All participants
240 had normal or corrected to normal vision, and were of at least average proficiency in both
241 Danish and English. All participants were healthy and did not take psychoactive, psychiatric,
242 or cardiovascular medications. Participants who could potentially be pregnant or were
243 breastfeeding had MRI contraindications (e.g., claustrophobia), or reported that they were not
244 able to abstain from alcohol and drugs 48 hours before study participation, were not included
245 in the study. All participants took part in a larger experiment including multiple brain scans,
246 psychiatric inventories, and other behavioural measures (data not reported here). Participants
247 were invited to complete two separate experimental sessions of the HRD task (henceforth
248 referred to as “Session 1” and “Session 2”), separated by 46.89 days on average (min=10;
249 max=97; std=23.87, statistics from participants that completed both sessions). Among the 223

250 participants, 218 participants completed session 1 and data were lost for 5 of them due to
251 technical difficulties. 192 participants (86% of the total sample) completed session 2. 11
252 participants were excluded from session 1 due to poor signal quality and/or for not having
253 performed the HRD task correctly (detail concerning the exclusion of participants based on
254 insufficient staircase convergence are provided in Supplementary Material). 1 participant was
255 excluded from session 1 and 2 due to a prior psychiatric diagnosis. After exclusion, 206
256 participants had completed Session 1 and 191 participants had completed Session 2. Among
257 the 191 participants that completed session 2, 179 had also completed session 1 (5 were
258 removed due to technical difficulties, and 7 were removed due to signal quality). When
259 analysing confidence ratings, 1 participant from Session 1 and 1 participant from session 2 were
260 dropped due to insufficient variance for estimation of M-ratio (see **Analysis**). 214
261 participants completed the HBC task, and 7 of them were removed due to poor physiological
262 signal quality. 193 participants had completed both the HBC task and the HRD task during
263 session 1. Participants received monetary compensation for each session (350 DKK). The study
264 was conducted in accordance with the Declaration of Helsinki and was approved by the Region
265 Midtjylland Ethics Committee.

266

267 **Physiological recordings**

268 Physiological signals in both sessions were recorded using the Nonin 3012LP Xpod USB pulse
269 oximeter together with a Nonin 8000SM “soft-clip” fingertip sensor (<https://www.nonin.com/>)
270 by interfacing with the “Systole” python package (v0.1.3) for pulse oximetry (Legrand & Allen,
271 2021). Previous work reported that the pressure exerted by some pulse oximeters on the surface
272 of the skin could provide sensory feedback to some participants, therefore potentially biasing
273 the estimation of interoceptive accuracy (Murphy et al., 2019). We selected the Nonin Pulse
274 softouch pulse oximeter as Murphy and colleagues demonstrated that this device did not elicit
275 fingertip pulse sensations. We further attempted to mitigate this effect by asking the participants
276 to move the device from the index finger to another fingertip if they felt any such sensory
277 feedback, although we did not record the proportion of participants for which this adjustment
278 was made. Participants were further asked to keep their hand still on the table or on their thighs
279 so as to not introduce heart rate measurement errors, due to movements.

280 Heartbeat Counting Task

281 The Heartbeat Counting (HBC) task is perhaps the most widely used and easily implemented
282 task for measuring interoceptive accuracy (Dale & Anderson, 1978; Schandry, 1981). However,
283 this procedure has been previously criticized, in part because it could be confounded by beliefs
284 about one's heart rate (Desmedt, Corneille, et al., 2020). To better validate and interpret our
285 new HRD measure, we implemented a revised version of the HBC (Garfinkel et al., 2015),
286 together with specialized instructions to reduce the role of bias in the derived interoceptive
287 accuracy (iACC) scores. Considering the substantial evidence that HBC scores are influenced
288 by beliefs in the heart rate, we expected to observe significant correlations between HBC iACC
289 scores and individual HRD thresholds. Participants were asked to count their heartbeats for
290 various periods of time while sitting silently. The HBC task consisted of 6 trials and lasted 25,
291 30, 35, 40, 45 or 50 seconds. The order of the trials was randomized across participants. The
292 HBC task was measured only in Session 1.

293 HRD Task Procedure - Session 1

294 At Session 1, the task comprised 160 trials, equally distributed between the interoceptive and
295 the exteroceptive conditions. For each condition, the first 30 trials were run using an adaptive
296 1-up/1-down staircase procedure, and the remaining 50 trials were run using a Psi procedure
297 (Kontsevich & Tyler, 1999). Our intention in combining these two staircase procedures was to
298 ensure that each experiment started with a mixture of trials that would be clearly perceived as
299 “Faster” or “Slower” by the participant. The initial up/down staircases consisted of 2 randomly
300 interleaved 1-up 1-down staircases per condition initialized at high (Δ -BPM = 40) and low (Δ -
301 BPM = -40) starting values following the recommendations of Cornsweet (Cornsweet, 1962).
302 The Psi staircases were initialized at starting values informed by the 1-up 1-down staircases,
303 achieved by updating Psi in the background with the intensity values and responses recorded
304 during the first 30 up/down trials. Based on our pilot studies, Psi was initialized such that the
305 prior for α was uniformly distributed between -40.5 and 40.5 and the prior for β was uniformly
306 distributed between 0.1 and 20. The α precision was 1 BPM to ensure that the intensity Δ -BPM
307 = 0 was excluded a priori and never presented. The β precision was set to 0.1.

308 The main task was preceded by a tutorial phase, which comprised 5 interoception and
309 5 exteroception trials with accuracy feedback after the decision and without confidence ratings,
310 as well as 5 interoception trials without feedback, but with confidence ratings, as in the main
311 experiment. For these trials, we fixed the absolute Δ value to 20 BPM and randomly selected

312 for negative or positive differences at each trial. This was intended to clarify the instructions,
313 to provide the participant with an easier version of the task, and ensure that they had an
314 opportunity to practice and adapt before the staircase procedure, which can be biased by initial
315 lapses. All auditory tones in Session 1 were presented through the stimulus PC speakers. The
316 total duration of the HRD task was 31.31 minutes on average ($SD = 3.32$, $MIN = 24.27$, MAX
317 = 42.46).

318 **HRD Task Procedure - Session 2**

319 To assess the internal (test-retest) reliability of HRD performance, all participants were invited
320 back for a second testing session. Here, all aspects of the HRD were as in Session 1, minus the
321 following, detailed below.

322 The total duration of the HRD at Session 2 was 22.69 minutes on average ($SD = 2.45$,
323 $MIN = 18.81$, $MAX = 31.81$). Due to a change in our testing environment, which exposed
324 participants to additional MRI noise, we opted to deliver auditory stimuli via over-the-ear
325 headphones to limit external distractions. We also decreased the maximum decision time from
326 8 to 5 seconds. To optimize psychometric estimation, we made the following changes to the
327 parameters and overall adaptive procedure. In particular, we observed a ceiling effect in the
328 Session 1 slope parameters (See Supplementary **Fig. 2.b**), likely induced by an overly
329 restrictive range on the slope prior distribution. To improve the estimation of this parameter,
330 we increased this range from 0.1-20 in Session 1, to 0.1-25 in Session 2. The range of the
331 threshold was increased from [-40.5, 40.5] in Session 1 to [-50.5, 50.5] in Session 2. We also
332 simplified the staircase procedure in Session 2, running only the Psi staircase instead of the
333 dual staircase approach described earlier. As the 1-up/1-down staircase initialization was
334 intended to ensure participants heard a sufficient number of positive and negative Δ -BPM trials
335 (i.e., trials in which the feedback was truly faster or slower than their true heart rate), we instead
336 implemented “catch” trials presented at fixed intervals above and below zero Δ -BPM. The catch
337 trial responses were not used to update the Psi staircases, yet ensured that once the staircase
338 had converged, subjects still occasionally received faster or slower ground-truth trials. In
339 Session 2, for each modality (Interoception, Exteroception) we used 12 catch trials, along with
340 48 Psi trials, for a total of 60 trials. In general, these changes improved the stability and
341 reliability of staircase convergence (see Supplementary **Fig. 2.e**).

342 Analysis

343 Statistical Analysis and Software

344 For both Session 1 and 2, we conducted planned statistical comparisons of threshold, slope,
345 confidence ratings, meta-d and SDT parameters (d' & M-ratio), across the two modalities using
346 paired-samples t-tests at each timepoint separately. We further conducted an apriori assessment
347 of test-retest reliability using the Pearson correlation coefficient for threshold and slope
348 between Session 1 and 2. We further hypothesized that HRD thresholds would correlate with
349 heartbeat counting scores, assessed via a priori correlation analysis. In addition to these planned
350 analyses, we conducted exploratory group by time repeated measures ANOVAs on HRD
351 parameters to assess possible interaction effects, and also estimated exploratory cross-
352 correlation matrices for all HRD and HBC parameters at both time points.

353 Statistical analyses were conducted using Pingouin v0.3.9 (Vallat, 2018). The Bayes
354 Factors were computed using a Cauchy scale of 0.707 and the p-values for the 2-way repeated
355 measure ANOVAs were adjusted using the Greenhouse-Geisser correction. Correlation
356 coefficients were tested using skipped correlations as implemented in Pingouin, which are
357 robust to outliers (Pernet et al., 2013). We controlled for multiple comparisons in the correlation
358 matrices using FDR correction ($p_{FDR} < 0.01$). Where applicable, outliers were detected and
359 rejected using the absolute deviation around the median rule (Leys et al., 2013). Test-retest
360 reliability was tested using the Pearson correlation from the same package. Figures were created
361 using Matplotlib (Hunter, 2007), Seaborn (Waskom et al., 2020) and Arviz (Kumar et al.,
362 2019). Distributions for repeated measures are represented using an adaptation of raincloud
363 plots (Allen et al., 2021). All preprocessed data and analysis scripts supporting the results
364 described in this paper are available at <https://github.com/embodied-computation-group/CardioceptionPaper>.

366 Bayesian Modelling of Psychometric Functions

367 Although Psi adaptively estimates slope and threshold parameters at each trial, we elected to
368 apply a post hoc modelling approach to improve psychometric estimation. The post hoc
369 modelling was applied after rejecting trials with extremely fast (< 100ms) responses or during
370 epochs containing unreliable cardiac signals. In general, this approach yielded highly similar
371 results as the Psi estimates - see supplementary materials (**Supp Fig. 1 & 2**) for a
372 comprehensive analysis. We used the absolute deviation around the median rule (Leys et al.,

373 2013) to identify and reject outliers in the instantaneous heart rate time series. Trials were
374 rejected if the average of the heart rate was considered an outlier, or if the standard deviation
375 of the pulse-to-pulse intervals was detected as outliers when compared to the other trials. This
376 ensured that we only included responses in which the participant was in principle able to
377 correctly estimate their cardiac frequency. We implemented Bayesian modelling of the
378 psychometric functions using PyMC3 (Salvatier et al., 2016, p. 3). We used the NUTS sampling
379 algorithm (Hoffman & Gelman, 2011) to update and estimate the posterior probability of the
380 slope (β) and threshold (α) parameters ($n_{\text{chains}}=2$, $n_{\text{tuning}}=4000$, $n_{\text{samples}}=1000$) for each subject
381 and modality separately. We used a cumulative normal function so the results can be compared
382 to what is estimated by the Psi staircase (see Supplementary Material **Fig. 2**). The psychometric
383 model parameters were defined as:

$$\begin{aligned} 384 \quad \alpha &\sim \text{Uniform}(-40.5, 40.5) \\ 385 \quad \beta &\sim \text{Uniform}(0, 40) \\ 386 \quad \theta_i &= \Phi(x_i, \alpha, \beta) \\ 387 \quad r_i &= \text{Binomial}(\theta_i, n_i) \end{aligned}$$

388 Considering the i th intensity levels, for the trials with a stimulus intensity x_i we observed a total
389 of n_i responses, among which r_i were “Faster” responses. Here, Φ is the cumulative normal
390 function defined by:

$$\Phi(x, \alpha, \beta) = \frac{1}{2} + \frac{1}{2} * \text{erf}\left(\frac{x - \alpha}{\beta * \sqrt{2}}\right)$$

391 Because we aimed to correlate the resulting scores with other variables and were not interested
392 in group-level means, we fitted the model for each subject and each modality separately in a
393 non-hierarchical manner. These post hoc models are included in the cardioception toolkit, and
394 future releases will provide easy to use hierarchical group estimation, to facilitate for example
395 between groups analyses (Valton et al., 2020). All subsequent psychometric behavioural
396 analyses were performed on the post hoc estimated parameters.

398 **Signal Theoretic Modelling of Perceptual and Metacognitive Sensitivity**

399 For these analyses, accuracy was coded such that a “Faster” response was correct only when
400 the intensity Δ -BPM was greater than 0, and a “Slower” response was correct only when the
401 intensity Δ -BPM was smaller than 0. Confidence ratings were binned into 4 equally spaced bins
402 before modelling using the `discreteRatings()` functions from `metadPy`, a custom python package
403 for metacognition modelling (<https://github.com/LeGrandNico/metadPy>). We used a standard

404 Signal Detection Theory (SDT) approach to estimate type 1 (i.e., perceptual) and type 2 (i.e.,
405 metacognitive) bias and sensitivity from the binned confidence ratings. Briefly, this model
406 operationalizes metacognitive “insight” as the sensitivity of subjective confidence ratings to
407 ground truth accuracy; e.g., by defining a receiver-operating characteristic (ROC) curve relating
408 metacognitive “hits” - $p(Confidence = High | Response = Correct)$ - and “misses” -
409 $p(Confidence = High | Response = Incorrect)$ - (Fleming & Lau, 2014; Maniscalco
410 & Lau, 2012a). This measure is known as meta- d' , and is an index of metacognitive sensitivity
411 akin to d' . However, as meta- d is known to be influenced by overall d' , and interoceptive
412 accuracy is generally lower than exteroceptive on our task, we analyzed the parameter M-ratio
413 (meta- d'/d'), also known as “metacognitive efficiency”. This parameter operationalizes
414 metacognitive insight in signal theoretic units; e.g., the proportion of available sensory evidence
415 utilized by the subjective confidence response. Perceptual and Metacognitive parameters were
416 estimated using an adapted hierarchical Bayesian model from the HMeta-d toolbox (Fleming,
417 2017). We reparameterized this model to implement a paired-samples t-test estimating the
418 within-subject impact of modality (interoceptive vs. exteroceptive) on M-ratio. The
419 significance of this effect was then assessed by checking if the 94% highest density interval
420 (HDI_{94%}) includes zero or not.

421

422 **Physiological Analysis**

423 The time-series recorded through photoplethysmography (PPG) were analysed using Systole
424 v0.1.3 (Legrand & Allen, 2021). The PPG signal, sampled at 75 Hz, is a measure of peripheral
425 blood oxygenation level, in which cardiac cycles can be tracked by detecting abrupt increases
426 following cardiac contraction and blood circulation (i.e., systolic peaks). The signal was first
427 resampled to 1000Hz using linear interpolation. This procedure simplifies the measurement of
428 the pulse-to-pulse intervals and can refine the peak detection precision, and the resulting heart
429 rate when the initial sampling rate is low (Quintana et al., 2016). Clipping artefacts were
430 removed using cubic spline interpolation (van Gent et al., 2019), the signal was then squared
431 for peak enhancement and normalized using the mean + standard deviation using a rolling
432 window (window size: 0.75 seconds). All positive peaks were labelled as systolic (minimum
433 distance: 0.2 seconds). This procedure was applied both for the online heart rate recording
434 during the Heart Rate Discrimination task (segments of 5 seconds) and for the Heartbeat
435 Counting task. If any interbeat interval higher than 120 BPM or lower than 40 BPM was

436 detected during the online recording of the Heart Rate Discrimination task, an error message
437 was presented on the screen to ask the participant to stay still, and the trial was started again,
438 up to 5 times consecutively before dropping the trial. As the correct detection of heartbeats is
439 critical for the Heartbeat Counting task, we ran additional artefacts correction steps to control
440 for erroneous or missed detection of some heartbeats. Extra heartbeats (i.e., erroneous labelling
441 of peaks in PPG signal) were automatically removed using an artefact correction algorithm
442 (Lipponen & Tarvainen, 2019) implemented in Systole (Legrand & Allen, 2021). All raw time
443 series were manually inspected to ensure correct systolic peak detection. The HTML reports
444 detailing these preprocessing steps of the HRD and the HBC tasks are made available online
445 with the GitHub Repository associated with this paper.

446 Heartbeat Counting Analysis

447 We derived an accuracy score following previous recommendations (Garfinkel et al., 2015;
448 Hart et al., 2013) as follows:

$$449 \quad Score = 1 - \frac{|N_{real} - N_{reported}|}{\frac{N_{real} + N_{reported}}{2}}$$

450 This score has a maximum of 1 and indicates the similarity between the objective recorded
451 number of heartbeats and the number reported by the participant (a score of 1 indicating a
452 perfect match). We used the absolute deviation around the median rule (Leys et al., 2013) to
453 automatically detect and remove extreme responses that are more likely to reflect erroneous
454 numbers provided by the participant. The remaining scores were subsequently averaged for
455 each participant.

456 Results

457 Characterizing the Interoceptive and Exteroceptive Psychometric Function

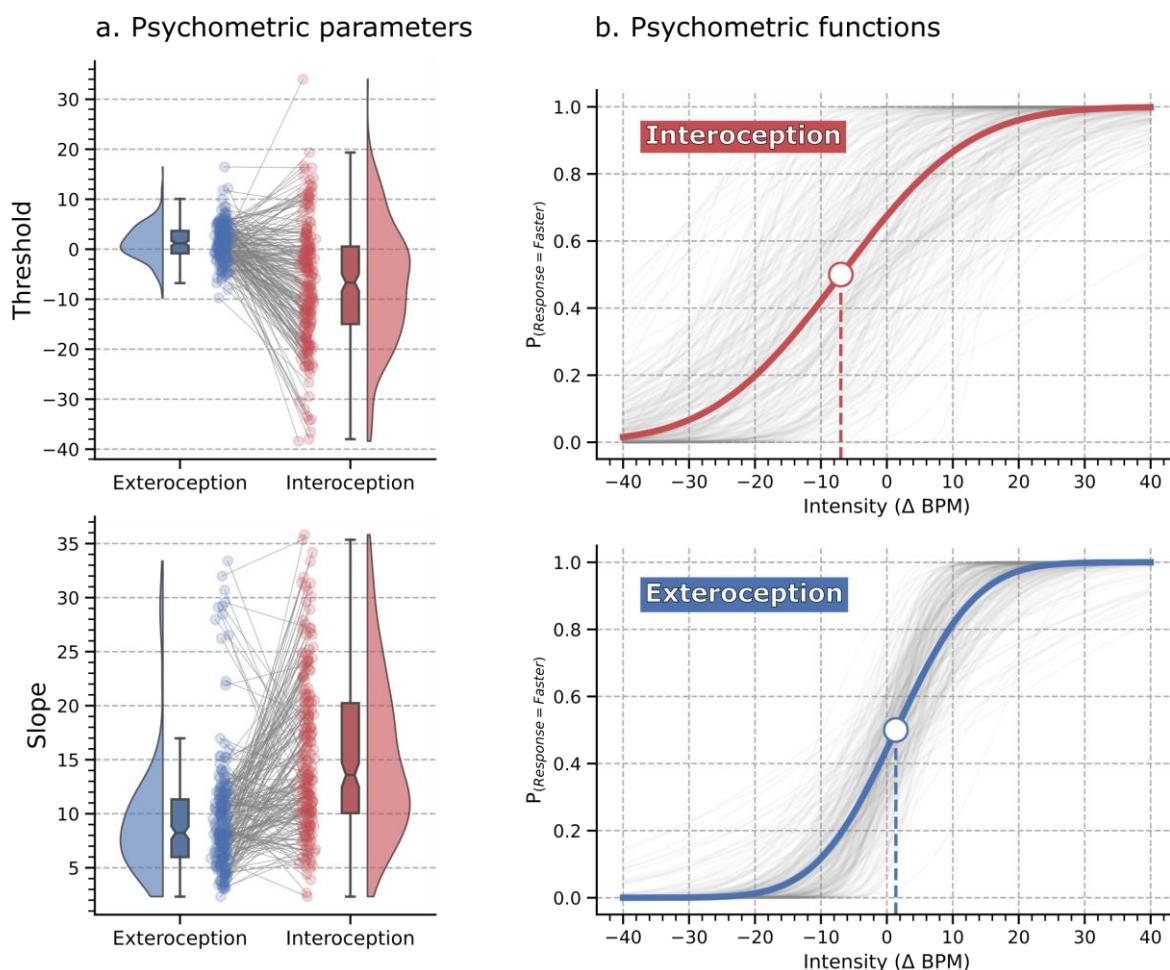
458 We first analyzed the threshold (α) and slope (β) psychometric parameters using the estimates
459 from the post hoc Bayesian model, separately for both sessions (see **Methods** for more details
460 and **Supplementary Results** for comparison of Psi and post hoc parameters). These analyses
461 serve to both characterize the overall shape of the two psychometric functions, which can
462 inform the setting of prior parameters in future experiments, and assess how belief accuracy,
463 bias, and precision differed between the two conditions. Further, to explore possible Session by
464 Modality interactions, we fit repeated measures ANOVAs to each parameter of interest.

465 A paired sample *t-test* at Session 1 revealed that threshold was significantly lower in
466 the interoceptive condition than in the exteroceptive condition (mean_{Intero} = -6.97, CI_{95%} [-8.59,
467 -5.37], mean_{Extero} = 1.36, CI_{95%} [0.9, 1.85], $t_{(205)} = -9.89, p < 0.001, BF_{10} = 1.15e+16, d = -0.93$),
468 indicating a robust negative bias; i.e., heart rate underestimation. This effect was replicated at
469 Session 2 (mean_{Intero} = -8.50, 95% CI_{95%} [-10.09, -6.91], mean_{Extero} = 0.008, 95% CI [-0.48,
470 0.50], $t_{(190)} = -11.15, p < 0.001, BF_{10} = 2.85e+19, d = -1.03$). We further noted a marked increase
471 in inter-subject variance for interoceptive thresholds, range_{Intero} = [-38.3, 34.0] vs. exteroceptive
472 thresholds, range_{Extero} = [-9.8, 16.39], indicating substantially more inter-individual variance in
473 the magnitude of interoceptive biases. In contrast, when compared to a null hypothesis of 0
474 bias, follow-up one-sample *t-tests* on exteroceptive thresholds revealed a slight but highly
475 significant positive bias at Session 1 (mean = 1.39, CI₉₅ = [0.9, 1.89], $t_{(203)} = 5.58, p < 0.001,$
476 $BF_{10} = 1.28e+05, d = 0.99$), which was not present at Session 2, in which we observed instead
477 a strong evidence for an absence of difference (mean = 0.01, CI₉₅ = [-0.48, 0.52], $t_{(189)} = 0.06, p$
478 = 0.94, $BF_{10} = 0.08, d = 0.05$). Finally, exploratory repeated measures ANOVA revealed
479 significant main effects of Session ($F_{(1,178)} = 13.20, \eta_p^2 = 0.06, p < 0.001$) and Modality ($F_{(1,178)} = 127.53, \eta_p^2 = 0.41, p < 0.001$), indicating that thresholds were significantly reduced across
480 sessions for both modalities, and that interoception was more biased across both sessions, but
481 with no Session by Modality interaction ($F_{(1,178)} = 0.60, \eta_p^2 = 0.003, p = 0.43$). See **Fig. 2** and
482 **6B** for illustration of these effects. Collectively these results show that interoceptive heart rate
483 beliefs are robustly biased towards underestimation, and show greater inter-individual variance,
484 than the exteroceptive control condition.

486 We next consider the slope of the interoceptive and exteroceptive functions. While the
487 threshold indicates the overall accuracy and bias of the decision-making process, the slope
488 characterizes the precision or uncertainty of this process. A higher slope indicates a less steep
489 (i.e., more shallow) psychometric function, indicating lower precision (higher uncertainty) for
490 that condition. A paired sample *t-test* revealed that slope was significantly higher in the
491 interoceptive condition as compared to the exteroceptive (mean_{Intero} = 15.34, CI_{95%} [14.39,
492 16.36], mean_{Extero} = 9.58, CI_{95%} [8.89, 10.39], $t_{(205)} = 9.05, p < 0.001, BF_{10} = 4.97e+13, d = -$
493 0.88). This effect was reproduced in Session 2, with interoceptive slope again greater than
494 exteroceptive slope at retest (mean_{Intero} = 11.96, 95% CI [11.17, 12.76], mean_{Extero} = 8.69, 95%
495 CI [8.11, 9.26], $t_{(190)} = 7.29, p < 0.001, BF_{10} = 9.12e+08, d = 0.67$). Exploratory repeated
496 measures ANOVA further revealed main effects of Session ($F_{(1,178)} = 31.27, \eta_p^2 = 0.14, p <$
497 0.001) and Modality ($F_{(1,178)} = 106.29, \eta_p^2 = 0.37, p < 0.001$), as well as an interaction between
498 these two factors ($F_{(1,178)} = 9.46, \eta_p^2 = 0.05, p = 0.002$). Thus, interoceptive slope showed a

499 greater reduction across sessions ($t_{(178)} = -5.35, p < 0.001, \text{BF}_{10} = 4.13+04, d = -0.53$) than
500 exteroceptive slope ($t_{(178)} = -2.19, p = 0.029, \text{BF}_{10} = 0.875, d = -0.20$). Collectively, these results
501 demonstrate that interoceptive beliefs are less precise than exteroceptive. Further, we could
502 hypothesize that interoceptive precision is more sensitive to practice and training effects than
503 exteroceptive precision. This notion cannot be fully tested here due to the methodological
504 differences that we introduced between the two sessions. See, however, **Fig. 2** and
505 **Supplementary Fig. 1** for the comparison between the two conditions.

506



507

508 **Legend Figure 2: Psychometric parameter estimates and fitted interoception and exteroception**
509 **psychometric functions (Session 1).** **A.** Repeated measures raincloud plots visualizing threshold and slope
510 parameters of the psychometric functions across the two modalities (interoception and exteroception). Data points
511 for every individual are connected by a grey line to highlight the repeated measure effect. **B.** The grey lines show
512 individual subject fits. The dark red and blue lines show the grand mean psychometric function, depicting averaged
513 threshold and slope. Grand mean thresholds are marked by the large point, where the psychometric function
514 crosses 0.5 on the ordinate axis. We observed a strong effect of interoception on both slope and threshold as
515 compared to the exteroceptive control condition. The negative bias observed on threshold demonstrates that
516 participants underestimated their heart rate on average. The greater slope indicates a less precise decision process.

517 Perceptual and Metacognitive Sensitivity

518 In addition to the psychometric function underlying the subjective decision process, we also
519 compared objective overall perceptual and metacognitive sensitivity between interoception and
520 exteroception. To assess between condition differences on these indices, we performed paired-
521 sample t-tests comparing interoceptive and exteroceptive performance on each key type 1 and
522 type 2 measure (d' , average confidence, and M-ratio), as well as exploratory Modality by
523 Session repeated measures ANOVAs on these variables.

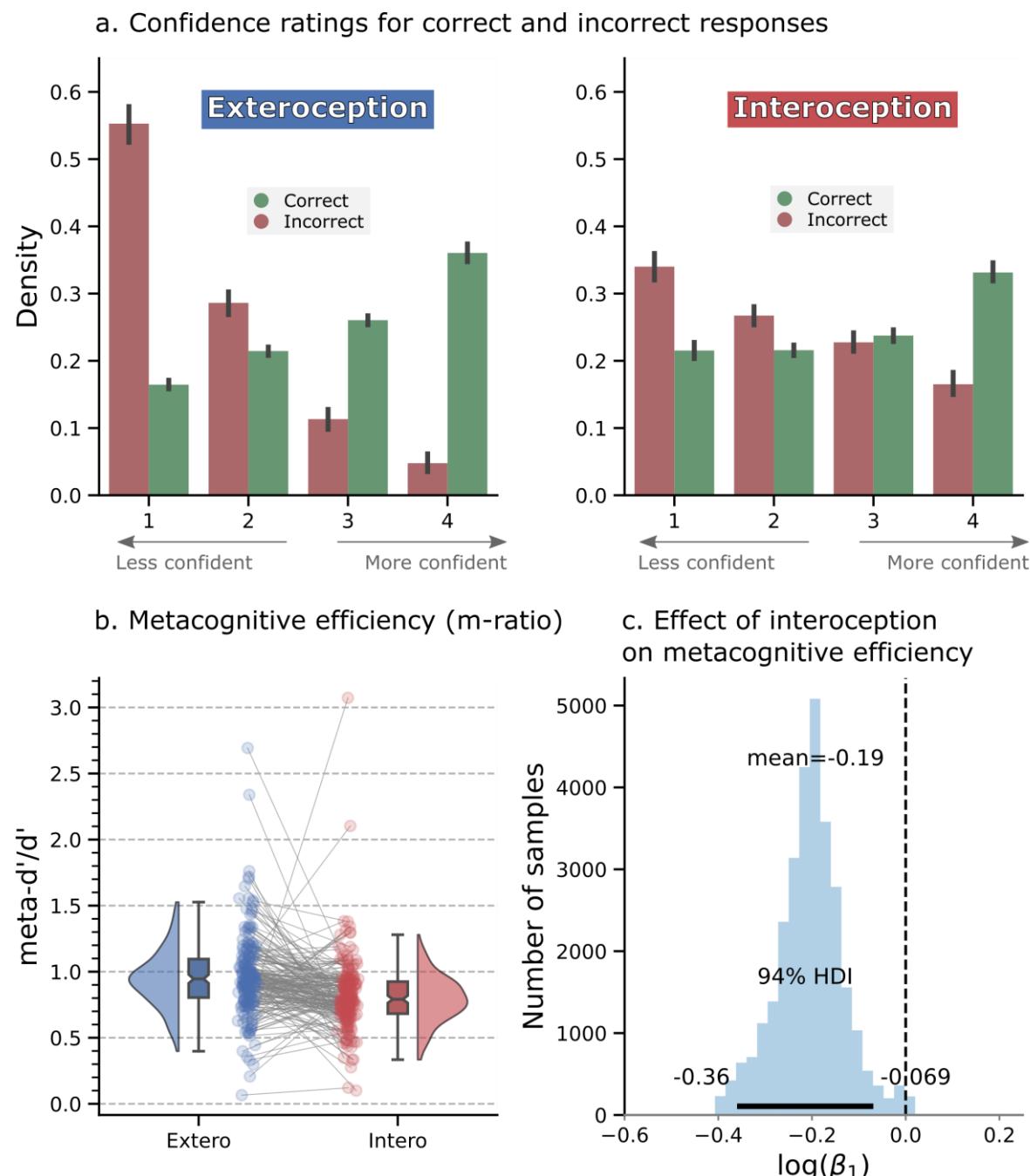
524 The d' , which reflects discrimination sensitivity, was significantly lower in the
525 interoception condition as compared to the exteroception condition during Session 1 (mean_{Intero}
526 = 1.43, CI_{95%} = [1.34, 1.52], mean_{Extero} = 2.05, CI_{95%} = [1.96, 2.14]), $t_{(203)} = -9.42$, $p < 0.001$,
527 $BF_{10} = 5.06e+17$, $d = -0.97$). We replicated this effect in Session 2 (mean_{Intero} = 1.87, CI_{95%} =
528 [1.79, 1.96], mean_{Extero} = 2.25, CI_{95%} = [2.21, 2.3], $t_{(185)} = -7.98$, $p < 0.001$, $BF_{10} = 4.45e+10$, d
529 = -0.77). We also performed an exploratory Session by Modality repeated measures ANOVA
530 on these measures to assess overall interactions between these factors. We observed significant
531 effects of both Session ($F_{(1,176)} = 59.82$, $\eta_p^2 = 0.25$, $p < 0.001$), Modality ($F_{(1,176)} = 114.81$, η_p^2
532 = 0.39, $p < 0.001$), and a Session by Modality interaction ($F_{(1,176)} = 7.19$, $\eta_p^2 = 0.03$, $p = 0.008$).
533 This result shows that across both conditions, sensitivity increased from Session 1 to 2, with
534 the greatest increase being observed in the interoceptive condition.

535 We next analyzed average subjective confidence, an indicator of metacognitive bias.
536 We found that confidence ratings were significantly lower during the interoception condition
537 as compared to the exteroception condition, both during the first session (mean_{Intero} = 51.52,
538 CI_{95%} = [49.16, 53.87], mean_{Extero} = 61.44, CI_{95%} = [59.51, 63.57], $t_{(203)} = -10.01$, $p < 0.001$, BF_{10}
539 = 2.3e+16, $d = -0.62$) and the second session (mean_{Intero} = 57.47, CI_{95%} = [55.41, 59.77],
540 mean_{Extero} = 64.27, CI_{95%} = [62.4, 66.03], $t_{(189)} = -7.15$, $p < 0.001$, $BF_{10} = 4.18e+08$, $d = -0.49$).
541 An exploratory repeated measures ANOVA revealed a main effect of Session ($F_{(1,176)} = 26.37$,
542 $\eta_p^2 = 0.13$, $p < 0.001$), Modality ($F_{(1,176)} = 101.37$, $\eta_p^2 = 0.36$, $p < 0.001$) and a Session by
543 Modality interaction ($F_{(1,176)} = 8.72$, $\eta_p^2 = 0.04$, $p < 0.003$). The average confidence was higher
544 in the second session as compared to the first one ($t_{(176)} = 5.13$, $p < 0.001$, $BF_{10} = 1.52e+04$, $d =$
545 0.30), and this increase was larger for the interoceptive condition ($t_{(176)} = 6.02$, $p < 0.001$, $BF_{10} = 9.68e+05$, $d = 0.36$) than for the exteroceptive condition ($t_{(176)} = 2.54$, $p < 0.01$, $BF_{10} = 1.93$, $d = 0.18$). Overall, confidence was generally lower for interoceptive vs. exteroceptive confidence.

548 To assess metacognitive sensitivity for both modalities, we estimated metacognitive
549 efficiency using hierarchical modelling of M-ratio (meta- d'/d') (Fleming & Lau, 2014;

550 Maniscalco & Lau, 2012a). We observed that the individual estimated M-ratio values, as
551 estimated by the repeated measure model, were lower during the interoception condition
552 ($\text{mean}_{\text{Intero}} = 0.81$, $\text{CI}_{95\%} = [0.78, 0.86]$) as compared to the exteroception condition ($\text{mean}_{\text{Extero}} = 0.96$,
553 $\text{CI}_{95\%} = [0.92, 1.01]$, see **Fig. 3.b**). This tendency is confirmed by inspecting the
554 posterior distribution of the log-transformed repeated measure effect ($\text{mean} = -0.19$, $\text{HDI}_{94\%} =$
555 $[-0.36, -0.06]$, see **Fig. 3.c**). Because the M-ratio reflects the relation between the amount of
556 evidence for metacognitive judgement and the amount of evidence for the objective decision,
557 our results suggest that 19% of the interoceptive evidence used for decision in the type 1 task
558 is lost during the metacognitive evaluation of confidence, compared to just 4% evidence loss
559 for exteroception.

560 We replicated this finding in Session 2, where interoception M-ratio estimates were
561 again lower ($\text{mean}_{\text{Intero}} = 0.83$, $\text{CI}_{95\%} = [0.8, 0.87]$) than those for exteroception ($\text{mean}_{\text{Extero}} = 0.96$,
562 $\text{CI}_{95\%} = [0.92, 1.01]$), as well as in the posterior distribution of the repeated measure effect
563 ($\text{mean} = -0.17$ $\text{HDI}_{94\%} = [-0.26, -0.03]$, see **Supplementary Material, Fig. 3**).



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Legend Figure 3: Visualization of metacognitive performance for interoception and exteroception conditions (Session 1). A. Histogram showing the distribution of binned confidence ratings for correct (green) vs. error (red) trials. Higher bins represent higher confidence ratings. Overall, participants were significantly less confident in the interoceptive condition and showed reduced metacognitive sensitivity as indicated by the flattening of the confidence distributions. **B.** To quantify this effect, we estimated “metacognitive efficiency”, a signal theoretic model of introspective accuracy which controls for differences in type 1 (discrimination) performance. Here, an M-ratio of 1 indicates optimal metacognition according to an ideal observer model, whereas values lower than this indicate inefficient use of the available perceptual signal. This model demonstrated that metacognitive efficiency was substantially decreased for interoceptive relative to exteroceptive judgements. **C.** Histogram of posterior samples from the beta value encoding the difference of interoception-exteroception in the repeated measures hierarchical model.

576 Cross-modal Correlations

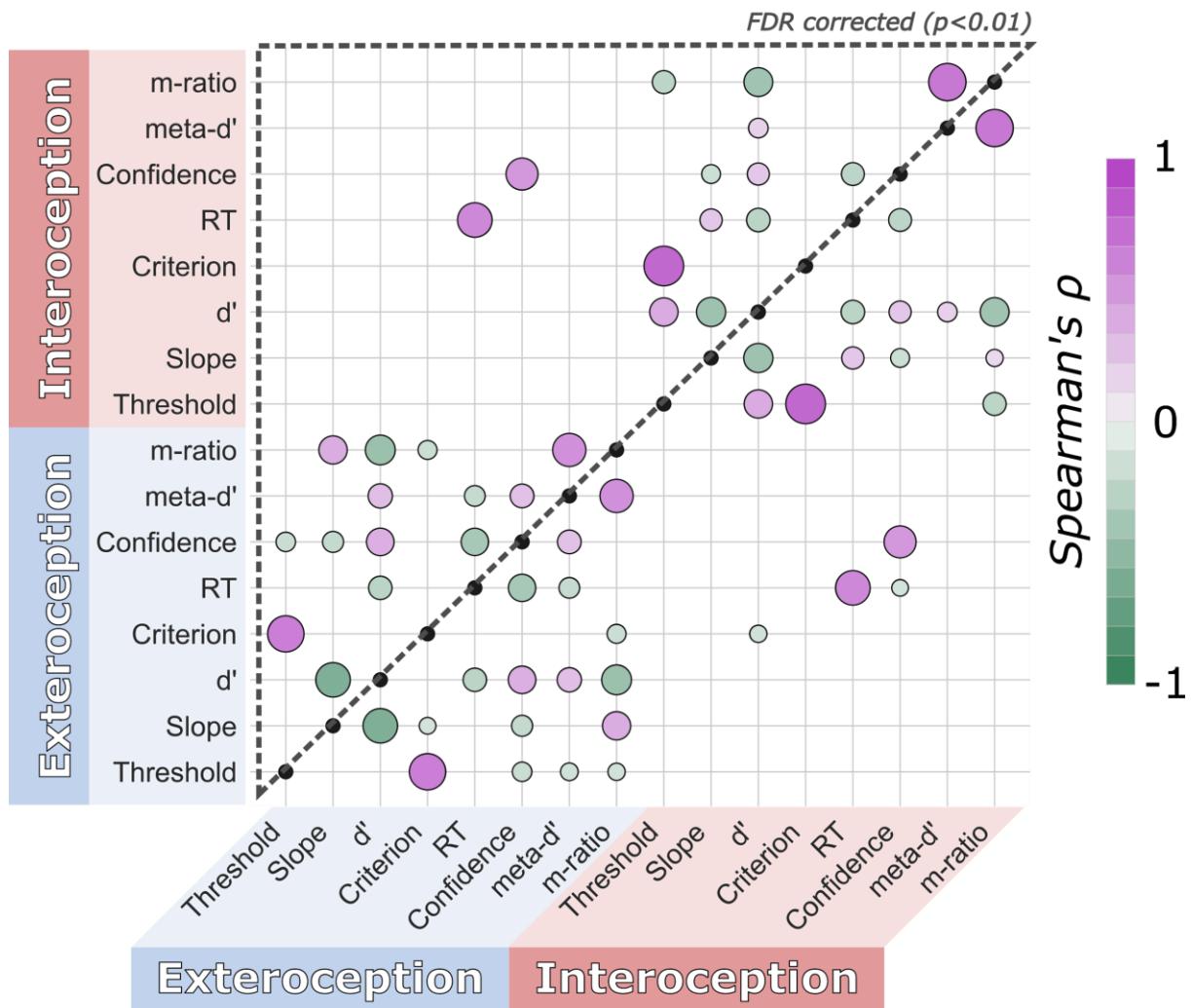
577 To investigate the construct validity of HRD performance measures, we conducted an
578 exploratory correlation analysis relating individual differences in perceptual and metacognitive
579 performance within and between the interoceptive and exteroceptive modalities. For this
580 analysis, we refitted the meta- d' model (Fleming, 2017) separately to each participant (i.e., in
581 a non-hierarchical model), and extracted individual M-ratio values. Here, we sought to verify
582 whether threshold, slope, or other type 1 or type 2 parameters were correlated across the two
583 conditions. For example, if HRD performance primarily indexed general temporal estimation
584 ability, we would expect a high correlation between interoceptive and exteroceptive thresholds,
585 as well as with other type 1 performance variables. Alternatively, if participants used additional
586 information, such as afferent cardiac sensory information and/or prior beliefs specifically about
587 the heart rate, then we would expect little to no correlation between these parameters.
588 Additionally, previous studies found that interoceptive metacognition is typically uncorrelated
589 to exteroceptive metacognition, suggesting unique inputs for these self-estimates (Garfinkel et
590 al., 2016). However, more recent work suggested the existence of a “metacognitive g-factor”
591 indexed by high inter-modal correlations in metacognitive ability (Mazancieux et al., 2020;
592 Rouault et al., 2018). We, therefore, included both type 1 measures (i.e., threshold, slope, d' ,
593 response time, and criterion) and type 2 measures (confidence, meta- d' , M-ratio) in one
594 exploratory between-subject correlation analysis to probe the degree of within and between
595 modality overlap in parameter estimates. To do so, we performed robust pairwise correlation
596 tests between exteroception and interoception task parameters (Pernet et al., 2013), using a
597 skipped correlation approach and correcting for multiple comparisons using a false-discovery
598 rate (FDR, $p_{FDR} < 0.01$) correction. The resulting Spearman’s r coefficients for Session 1 are
599 summarized in **Fig. 4**.

600 We observed more robust and consistent correlations between task parameters within
601 each modality (interoception or exteroception), but few significant correlations between task
602 modalities, indicating a high degree of independence between performance on the two task
603 conditions. Interestingly, with the exception of reaction time, type 1 performance was largely
604 uncorrelated between modalities, whereas at the metacognitive level only subjective confidence
605 was highly correlated ($r_s = 0.60$, $CI_{95\%} = [0.52, 0.69]$, $p < 0.001$, $n = 204$, $n_{outliers} = 5$). These
606 results may suggest that individuals use similar “self-beliefs” about their performance on both
607 task modalities (Fleming & Daw, 2017). A similar overall pattern was observed in Session 2,
608 albeit with a modest but significant relationship between interoceptive and exteroceptive

609 thresholds ($r_s = 0.26$, $CI_{95\%} = [0.13, 0.39]$, $p < 0.001$, $n = 190$, $n_{\text{outliers}} = 6$, see **Supplementary Results** for the full correlation matrix).

611

Cross-modal correlations matrix



612

613 **Legend Figure 4: Cross-modal correlation heatmap of task parameters for interoception and exteroception**
614 **conditions (Session 1).** Overall, we observed that behavioural results were correlated within modalities but with
615 limited dependence across modalities, the only exceptions were confidence and response time (RT). Only
616 significant skipped Spearman correlations are represented. **The upper triangle only shows results surviving**
617 **FDR correction ($p_{\text{FDR}} < 0.01$), while the lower right triangle of the matrix shows the uncorrected**
618 **comparisons.** Colour and size of individual points indicate the sign and strength of estimated correlation
619 coefficients. See supplementary Fig. 4 for Session 2 cross-correlations.

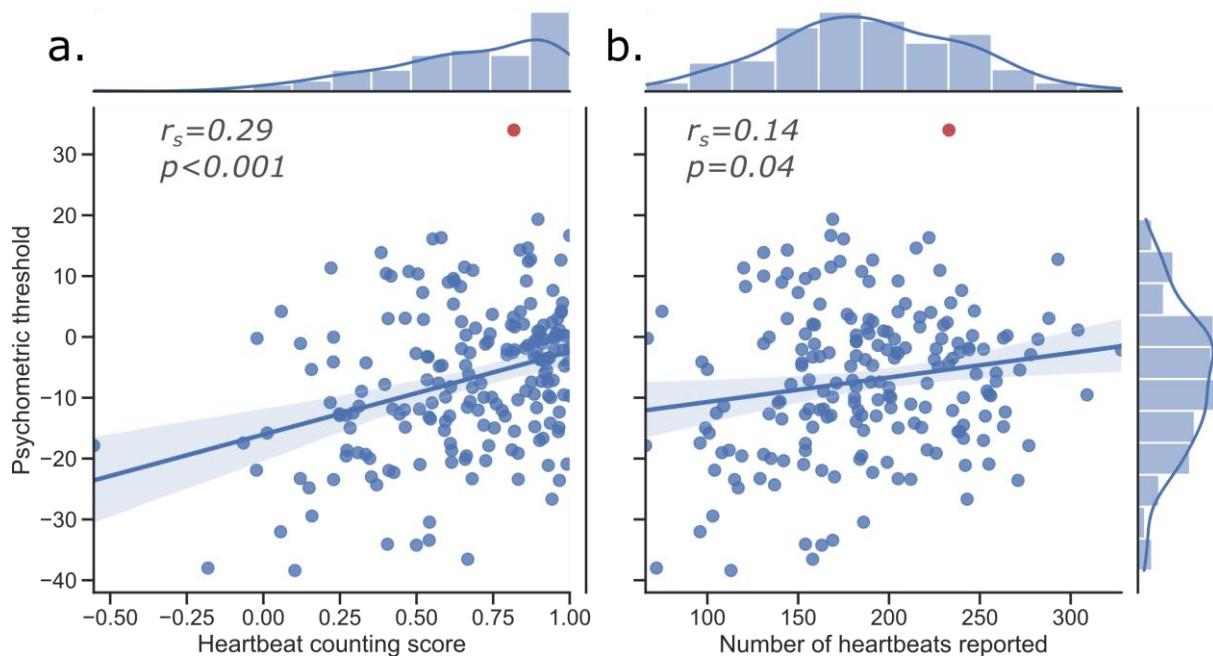
620 Correlation with the heartbeat counting task parameters

621 As a final check of construct validity, we assessed how our new task relates to the standard
622 heartbeat counting task. We thus correlated HRD performance variables (psychometric
623 thresholds and slopes) with the HBC scores. We found that the interoceptive thresholds from

624 Session 1 were positively correlated with the global heartbeat counting score (see **Fig. 5.a**; $r_s =$
 625 0.29 , $CI_{95\%} = [0.16, 0.42]$, $p < 0.001$, $n = 193$, $n_{outliers} = 1$). No significant correlation was found
 626 between the heartbeat counting score and the exteroceptive threshold ($r_s = -0.04$, $CI_{95\%} = [-0.18,$
 627 $0.1]$, $p = 0.58$, $n = 193$, $n_{outliers} = 13$). We further replicated the correlation between HRD
 628 threshold and HBC iACC scores in Session 2 ($r_s = 0.19$, $CI_{95\%} = [0.05, 0.33]$, $p = 0.01$, $n = 178$,
 629 $n_{outliers} = 0$).

630

Correlation with the heartbeat counting task parameters



631

632 **Legend Figure 5: Correlation between the psychometric threshold and heartbeat counting performance.**
 633 **(Session 1) A.** We found that heart rate discrimination (HRD) thresholds correlate positively with heartbeat
 634 counting (HBC) interoceptive accuracy scores. A lower threshold (i.e., a more negative bias) on the HRD task was
 635 associated with lower performance on heartbeat counting. We suggest that low scores on the heartbeat counting
 636 task are associated with a tendency to undercount the number of heartbeats. **B.** The psychometric threshold was
 637 associated with the total number of heartbeats reported during the heartbeat counting task. The correlation was
 638 also found while controlling for the heart rate during the task (not shown). These results suggest that participants'
 639 inability to reliably count their heartbeats is partially explained by lower interoceptive thresholds. Outliers detected
 640 by the skipped correlation are reported in red. The r_s and p values are from the bootstrapped Spearman coefficient.
 641 The regression line is only fitted to non-outlier data points. The shaded area represents the bootstrapped confidence
 642 interval (95%).

643

644 The previous results suggest that the bias observed in the heartbeat counting task might be at
 645 least partially explained by the participants' tendency to underestimate their own heart rate. To
 646 corroborate this notion, we attempted to verify the association between the psychometric

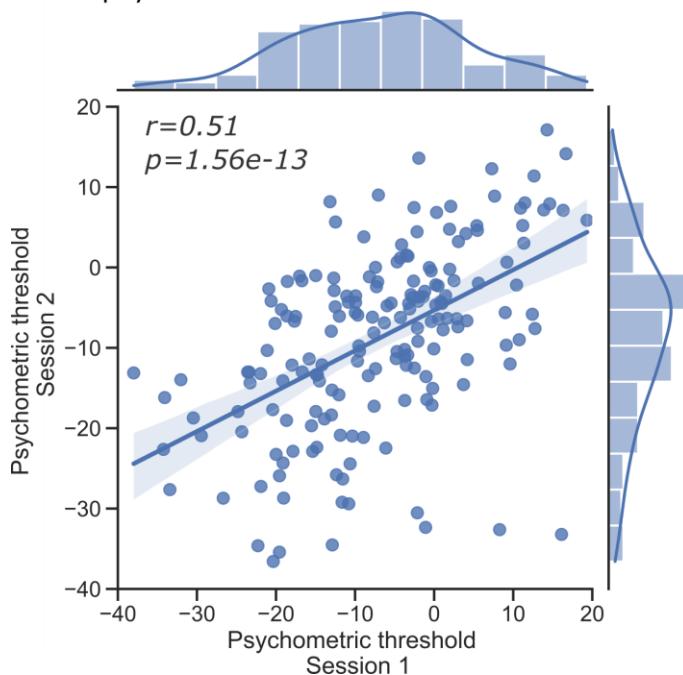
647 threshold obtained during the HRD task, which quantifies the heart rate underestimation, and
648 the total number of heartbeats reported by the participant during the HBC task (see **Fig. 5.b**).
649 The psychometric threshold was positively correlated with the total number of heartbeats
650 counted by the participants ($r_s = 0.14$, $CI_{95\%} = [0.01, 0.28]$, $p = 0.04$, $n = 193$, $n_{outliers} = 1$). It
651 could be argued here that the actual heart rate of the participant may directly influence the total
652 number of counted heartbeats, as the number of heartbeats that can be potentially counted
653 naturally increases with increments in heart rate frequency. To control for this possible
654 confound, we performed a semi-partial correlation between the psychometric threshold and the
655 total number of counted heartbeats while controlling for the relation between the number of
656 counted heartbeats and the number of actual heartbeats detected in the PPG signal. This analysis
657 revealed a positive correlation between these two variables ($r_s = 0.20$, $CI_{95\%} = [0.07, 0.34]$, $p =$
658 0.004 , $n = 193$, $n_{outliers} = 2$).

659 **Reliability of psychometric parameters**

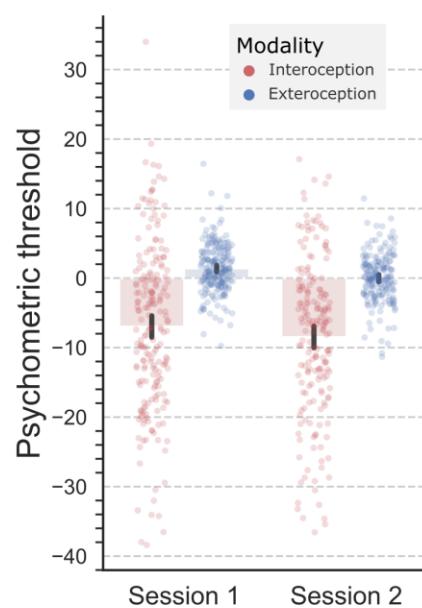
660 Intrinsic or test-retest reliability is a critical feature of any measurement, in particular, if it is to
661 be useful for clinical diagnostic or intervention purposes. To evaluate reliability, we calculated
662 the correlation coefficient for Session 1 and 2 interoceptive thresholds and slopes, obtained on
663 average 46.79 days apart from each other. Threshold was highly correlated between sessions,
664 showing good reliability ($r = 0.51$, $p < 0.001$, $BF_{10} = 5.04e+10$, see **Fig. 6**). In contrast, Slope
665 was not correlated across sessions ($r = 0.10$, $p = 0.15$, $BF_{10} = 0.25$), potentially indicating a
666 poor reliability of this parameter.

667

a. Test re-test reliability of the psychometric threshold



b. Psychometric threshold estimates across modalities and sessions



668

669 **Legend Figure 6: Test-retest reliability of the psychometric threshold.** The psychometric threshold estimated
670 using a Bayesian post hoc approach provided correct test-retest reliability. **A.** Correlation between the
671 interoception threshold estimates in Sessions 1 and 2. Outliers detected by the skipped correlation were removed
672 and the reliability was tested using a Pearson correlation. The r_s and p values were calculated using the
673 bootstrapped Spearman coefficient. The regression line was only fitted to non-outlier data points. The shaded area
674 represents the bootstrapped confidence interval (95%, 1000 iterations). **B.** Distribution of threshold Bayesian
675 estimates across sessions and modalities (n=204 for Session 1; n=190 for Session 2). The error bars represent the
676 bootstrapped confidence interval (95%, 1000 iterations).

677

678

679

680 Discussion

681 The measurement of cardiac interoception is a methodological puzzle that has challenged
682 generations of psychologists and psychophysicists (Ainley et al., 2020; Brener Jasper &
683 Ring Christopher, 2016; Chen et al., 2021; Zamariola et al., 2018; Zimprich et al., 2020). Here,
684 we suggest that this difficulty arises in part from a reluctance to treat subjective perceptual
685 beliefs about the heart rate as a core component of interoception. To remedy this gap, we
686 introduce a new Heart Rate Discrimination (HRD) task, which incorporates a Bayesian
687 psychophysical procedure for measuring the accuracy, precision, and metacognitive sensitivity
688 of cardiac decisions. In a study of 223 healthy participants, we observed robust and consistent
689 heart rate underestimation. We also found that interoceptive beliefs and metacognition are more
690 imprecise as compared to the exteroceptive control condition. Our results indicate that
691 interoceptive beliefs as measured by the HRD are not strongly correlated with other
692 exteroceptive temporal beliefs, but share some variability with indexes of interoception
693 measured by the Heartbeat Counting task. In general, these effects were robustly replicated
694 across two testing sessions, with interoceptive thresholds, in particular, exhibiting good within-
695 participant test-retest reliability. These features make the HRD well-suited for the measurement
696 of interoceptive biomarkers in clinical populations, and for basic research probing the
697 underlying mechanisms underlying cardiac beliefs and their influence on behaviour.

698 Our principal finding is that participants consistently underestimate their resting heart
699 rate by 7 BPM on average, with substantial inter-individual variation around this value (Δ -BPM
700 threshold range = [-39, 30]) (Fig. 2). This finding is consistent with repeated reports that
701 heartbeat counting scores are driven by undercounting (Zamariola et al., 2018) - for discussion,
702 see (Ainley et al., 2020; Corneille et al., 2020; Zimprich et al., 2020). We also find that
703 interoceptive HRD thresholds are moderately correlated with HBC iACC scores, such that
704 fewer counted heartbeats correlate with a lower HRD threshold (see Fig. 5). When comparing
705 interoceptive and exteroceptive thresholds, we further found a similar positive correlation at
706 session 2 (see Supp Fig. 4). These results highlight the unique sources of variance influencing
707 interoceptive beliefs, such that HRD thresholds (and by extension, HBC scores) are likely to be
708 driven by a combination of general temporal estimation ability, bottom-up cardio-sensory
709 inputs, and top-down beliefs about the heart rate.

710 The ability to distinguish these contributions is a unique strength of the HRD. Future
711 clinical investigations will benefit from including both interoceptive and exteroceptive
712 conditions to tease apart these different potential causes of apparent interoceptive dysfunction.

713 For example, if a participant group shows general cross-domain main effects on both
714 interoceptive and exteroceptive thresholds, this would indicate a general deficit in temporal
715 estimation rather than an alteration of interoceptive beliefs. In contrast, group or conditional
716 interaction effects on the interoceptive threshold or slope, in the absence of any exteroceptive
717 effects, would indicate a specific deficit in monitoring bodily sensations and updating cardiac
718 beliefs. In this way, investigating conditions by group interactions on HRD parameters should
719 hopefully improve the specificity of interoception research.

720 Another important finding is that interoceptive precision, as measured by the slope of
721 the psychometric function, was substantially lower than exteroceptive precision (**Fig. 2 and**
722 **Supp Fig. 1**). This is an interesting finding in light of recent theoretical and computational
723 models which hypothesize that interoceptive sensory signals in the brain may generally be more
724 imprecise than their exteroceptive counterparts (Ainley et al., 2016; Allen et al., 2019; Allen &
725 Tsakiris, 2018). This hypothesis is based on influential “interoceptive predictive processing”
726 models which emphasize the top-down, belief-driven nature of embodied self-perception. On
727 these accounts, subjective interoceptive sensations are more likely to reflect the integration of
728 top-down, prior expectations about the bodily self with ascending sensory inputs, with each
729 signal weighted by their respective precision or confidence (Allen, 2020; Allen & Friston, 2018;
730 Barrett & Simmons, 2015; Seth, 2013). The finding that interoceptive decisions are associated
731 with lower precision may thus indicate that ascending cardiac signals are themselves inherently
732 imprecise, or those prior beliefs encoding expected interoceptive precision are themselves more
733 uncertain.

734 It should be noted however that “precision” as measured by the HRD indicates the
735 uncertainty of the psychological decision process, and should not yet be treated as a direct read-
736 out or measurement of the computational process by which prediction error signals are
737 “precision-weighted”, which is thought to depend on neurobiological gain control (Bastos et
738 al., 2012; Feldman & Friston, 2010). While previous investigations in the exteroceptive domain
739 demonstrated a link between behavioural variability of this sort and neurocomputational
740 precision (Eldar et al., 2013; Hénaff et al., 2020; van Bergen et al., 2015; Warren et al., 2016),
741 in advance of direct evidence in the interoceptive domain this link should be interpreted with
742 caution. Nevertheless, a unique benefit of our approach is that future studies could combine the
743 HRD with computational modelling and direct neuronal recordings to conclusively establish
744 the potential link between these parameters, and to tease apart the contributions of prior versus
745 sensory precision to the imprecision observed here in heart-rate decisions (see e.g. Allen et al.,
746 2019; Smith et al., 2020, 2021 for potential modelling applications).

747 Finally, we observed a robust reduction in metacognitive efficiency for interoceptive
748 versus exteroceptive decisions. Although individual levels of subjective confidence (i.e.,
749 metacognitive bias) were highly correlated between modalities, metacognitive efficiency itself
750 was not. This speaks to ongoing debates about the modularity of metacognition (Rouault et al.,
751 2018), indicating that metacognitive ability in the interoceptive domain is largely unrelated to
752 exteroceptive self-monitoring, in line with previous findings on this topic (Beck et al., 2019;
753 Garfinkel et al., 2016). In light of these results, it is interesting to speculate as to the divergent
754 mechanisms that might underlie metacognition in these two domains.

755 Numerous computational accounts emphasize that accurate metacognitive self-
756 monitoring is likely to depend on a process by which the precision of the sensory signals
757 underlying the type 1 decision is “read-out” by a higher-order metacognitive module, such that
758 noisy, imprecise signals can be expected to degrade both perceptual performance and
759 metacognitive sensitivity (Fleming et al., 2012; Maniscalco & Lau, 2016). However, other
760 accounts emphasize that top-down “self-beliefs” may play a crucial role in shaping the
761 interaction between low-level precision and higher-order metacognition (Allen et al., 2020;
762 Fleming & Daw, 2017). Speculatively, our findings may suggest that in the cardiac domain,
763 metacognition is largely dominated by top-down beliefs, rather than pure sensory read-out.
764 Alternatively, if the reduced interoceptive precision observed here relates primarily to the
765 uncertainty of cardiac sensory afferents, then this effect may be simply a result of the
766 metacognitive system accurately reading out the low sensory precision. Teasing apart these
767 different hypotheses through targeted causal manipulations of cardiac sensory signals and prior
768 beliefs will hopefully shed new light on metacognitive insight into the bodily self.

769 **Strengths of the Heart Rate Discrimination Task**

770 The HRD has several important methodological and practical strengths that support its utility
771 in both basic and clinical research. First, the psychometric curve is estimated across trials
772 relative to the ground truth heart rate. This allows us to differentiate the bias and precision of
773 cardiac beliefs, in a way in which previous tasks such as HBC and HBD cannot. For example,
774 it could be expected that the overall shape of the psychometric function may change under
775 cardiovascular arousal, and the magnitude of this change could be an important marker of inter-
776 individual differences in interoceptive reactivity.

777 A second feature of the HRD is the inclusion of an exteroceptive control condition,
778 enabling measurements in the same units (Δ -BPM) in both modalities. This provision of

779 sensible, easy to interpret units enables precise, meaningful comparisons across different
780 studies, improving metric interpretability. The exteroceptive control condition itself has several
781 additional benefits; it facilitates the use of the task in neuroimaging studies aiming to isolate
782 more specific neural correlates of cardioceptive beliefs and allows for the differentiation of
783 clinical symptoms into specific interoceptive deficits and more general temporal estimation
784 deficits.

785 A third strength is that up to 100 HRD trials can be collected in as little as 25 minutes
786 using standard physiological recording equipment. This is critical for clinical studies where
787 testing time is often limited. A core contribution of the HRD is that it provides a novel decision
788 axis through which researchers can probe interoceptive beliefs and percepts: the moment to
789 moment decision of how fast one's heart is beating. This trial design means that the HRD is
790 amenable to a variety of quantitative modelling techniques such as hierarchical modelling of
791 psychometric functions, or through computational modelling using reinforcement learning and
792 similar approaches (Mathys et al., 2014; Petzschner et al., 2021). This feature facilitates testing
793 mechanistic hypotheses about how cardioceptive beliefs are formed and updated and could be
794 paired with, for example, the probabilistic manipulation of attention or performance feedback
795 to delineate the role of prior beliefs and sensory prediction errors.

796 In general, we believe the HRD will be particularly useful as a clinical biomarker when
797 comparing how specific populations update their cardiac beliefs under differing contexts - for
798 example, one could test whether participants with anxiety show a tendency towards
799 overestimating the heart rate at rest, or instead exhibit larger shifts in threshold and/or precision
800 when comparing aroused vs. resting state performance.

801 **Limitations**

802 The HRD offers several improvements to existing cardioceptive measures, including increased
803 face validity, adaptability, and amenability to signal theoretic and other computational
804 approaches to quantifying cardiac decisions. However, there are a few potential limitations of
805 the task, and the results demonstrated here.

806 First, the HRD depends upon the online estimation of the heart rate within a five-second
807 interval. While instantaneous measures of heart rate are generally robust, even within this time
808 window there are likely to be within-trial shifts in high-frequency heart rate variability (HRV).
809 Effectively this means that there is a theoretical lower bound on the precision with which one
810 can estimate HRD thresholds, below which their interpretation becomes suspect. To control for

811 this effect, we ensured that HRD step sizes (e.g., in terms of the minimum increment on Δ -
812 BPM) are never lower than 1 BPM intervals, and also excluded trials with an extreme standard
813 deviation of within-trial beat to beat intervals.

814 Another limitation is related to our implementation of the task as a two-interval forced-
815 choice response. On each trial, participants first attended to their cardiac sensations and were
816 then immediately presented with auditory feedback during the choice interval. This is a
817 deliberate design decision, as the 2-IFC structure both ensures that participants have a window
818 of interoception-only focus on each trial and renders the underlying behaviour more amenable
819 to the signal theoretic assumptions of the metacognitive model (Galvin et al., 2003; Lee et al.,
820 2018; Maniscalco & Lau, 2012b). We see this as an improvement over measures such as the
821 heartbeat discrimination task, where subjects must perform a difficult simultaneous
822 multisensory judgement, and it makes the task more amenable for identifying the neural or
823 physiological correlates of HRD measures in the interoception-only time window. However, as
824 a trade-off, this does induce a slight working-memory component to the task, as participants
825 must form a belief about the heart rate and then hold it in mind while comparing it to the
826 auditory feedback tones. This may be a limitation for studies comparing, for example, clinical
827 populations with known working memory deficits. In this case, a variant of the task could easily
828 be implemented in which the feedback tone is presented simultaneously with the listening
829 interval, similar to recent tasks using a method of adjustment (Palmer et al., 2019).

830 The HRD task also includes an exteroceptive condition that has been designed to
831 correspond as closely as possible to the interoceptive condition in terms of trial structure, timing
832 and cognitive content that makes it appropriate for contrast-based analyses, e.g., in
833 neuroimaging or physiological studies. It should be noted however that across trials, the
834 frequency of the first “reference” stimulus is not derived from the heart rate but rather a random
835 uniform distribution from 40 to 100 bpm. This means that the range of presented tones is greater
836 in the exteroceptive vs interoceptive condition and that the exteroceptive psychometric function
837 is essentially averaged across relatively slow and fast stimuli. If a participant has a large
838 difference in responses across these bins, it could potentially limit the interpretation of the
839 relative difference in interoceptive versus exteroceptive thresholds. One could alternatively
840 generate these stimuli from a distribution matching that of the participants own heart rate, albeit
841 with the trade-off of potentially feeding the participant implicit information about their heart
842 rate. Future work should rigorously compare these possibilities to achieve optimal control over
843 temporal and other cognitive confounds.

844 Finally, we do not present the HRD as measuring the objective sensitivity to ascending
845 (i.e., baroreceptor mediated) cardiac sensations specifically. In the absence of further empirical
846 data, interoceptive thresholds and/or precisions obtained by the HRD method should not be
847 interpreted as a straightforward measure of the objective ability to discriminate viscerosensory
848 sensations, as a variety of different strategies utilizing, for example, semantic beliefs or tactile
849 inputs are likely to underlie decisions on the task, in particular under resting conditions (Khalsa
850 et al., 2009). For researchers targeting specifically visceral ascending sensitivity, we would
851 recommend approaches such as the MCS (Brener et al., 1993). Our task instead measures the
852 bias and precision of subjective beliefs about the heart rate, which are likely to combine prior
853 beliefs, contextual factors, and ascending (interoceptive and exteroceptive) sensory information
854 where available. Future studies will pair causal manipulations of ascending cardiac signals with
855 threshold measurement, to better delineate the degree to which these sensory inputs shape
856 cardiac beliefs.

857 **Conclusion**

858 In this study, we reported observations from the experimental use of the Heart Rate
859 Discrimination task to measure the bias and precision of cardiac beliefs among a group of 223
860 individuals in a test-retest design. Our results have documented a robust tendency across
861 participants to underestimate their heart rate, and have shown that interoceptive decisions are
862 imprecise as compared to an exteroceptive control condition. We argue that the ability to
863 objectively quantify these perceptual beliefs is a powerful tool for both basic and clinical
864 interoception research. As this procedure is supported by psychophysics and Bayesian
865 modelling of metacognition, it also calls for future methodological refinement and hypothesis-
866 driven investigation to delineate the computational and physiological sources of cardiac beliefs.
867

868

869 Acknowledgements

870 NL, NN, CMCC, MB, AS, NK, MN, and MA are supported by a Lundbeckfonden Fellowship
871 (under Grant [R272-2017-4345]), and the AIAS-COFUND II fellowship programme that is
872 supported by the Marie Skłodowska-Curie actions under the European Union's Horizon 2020
873 (under Grant [754513]), and the Aarhus University Research Foundation. FF is supported by
874 an European Research Council Starting Grant, under the European Union's Horizon 2020
875 research and innovation programme (Grant agreement No. 948838). The authors further thank
876 Benjamin Vincent for insightful discussions on the psychometric approach implemented here.

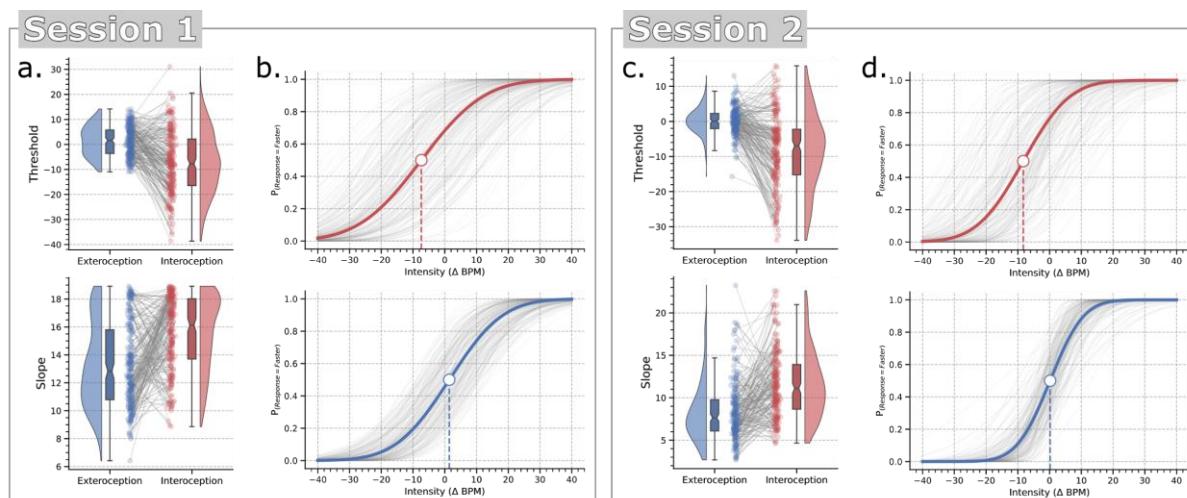
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878 Supplementary material

879 Psychometric estimates using the Psi method

880 During Session 1, we used a 1-up/1-down procedure together with a Psi staircase to estimate
881 the threshold of the psychometric function. During the first 30 trials of each condition, the
882 intensity value was controlled by a 1-up/1-down staircase (Dixon & Mood, 1948) and the
883 results were provided to the Psi staircase for initialization. We used this procedure to control
884 for threshold convergence between the two techniques (results non reported here). During
885 Session 2, we used only a Psi staircase procedure (Kontsevich & Tyler, 1999). The
886 experimental setup was also slightly optimized between Sessions 1 and 2 (see **Material and**
887 **Methods**). All these points could impact the efficiency and the parameters estimates of the Psi
888 staircases. To check for possible deviation, we report in **Figure 1** of the **Supplementary**
889 **Materials** the psychometric parameters estimates for slope and threshold across the two
890 modalities and across the two sessions.

891



892
893 **Legend Supplementary Material 1: Psychometric parameters and psychometric functions estimated by the**
894 **staircase using the Psi method from Sessions 1 and 2.** Slope and threshold parameters of the psychometric
895 functions for interoception (red) and exteroception (blue) conditions during Session 1 (n=206) (A.) and Session 2
896 (n=191) (C.). Psychometric functions fitted across interoceptive and exteroceptive conditions for Session 1 (B.)
897 and Session 2 (D.). The grey lines show individual subject fits. The dark blue and red lines show the grand mean
898 psychometric function, depicting the average threshold and slope. Both sessions show a strong effect of
899 interoception on slope and threshold as compared to the exteroceptive control condition, with a negative bias and
900 reduced precision for interoception.

901

902 Here, our results mirrored what we observed using the Bayesian estimates and comparing
903 the two modalities conditions. We observed a bias in the interoceptive threshold as compared
904 to the exteroceptive one in both Session 1 ($t_{(205)} = -9.89, p < 0.001, BF_{10} = 1.20e+16, d = -0.90$)
905 and Session 2 ($t_{(190)} = -11.66, p < 0.001, BF_{10} = 8.31e+20, d = -1.06$). The slope, reflecting the
906 imprecision of the decision, was also higher during interoception in both Session 1 ($t_{(205)} = 7.86,$
907 $p < 0.001, BF_{10} = 3.06e+10, d = 0.80$) and Session 2 ($t_{(190)} = 8.92, p < 0.001, BF_{10} = 1.50e+13, d$
908 $= 0.86$). Here, a higher slope reflects a less precise decision process. These results suggest that
909 the two main psychometric effects (i.e., the threshold bias and slope increase during
910 interoception) are robust and are not specific to one analytical approach in particular.

911 **Correlation between psychometric parameters estimated using the**
912 **Psi method and a Bayesian post hoc model**

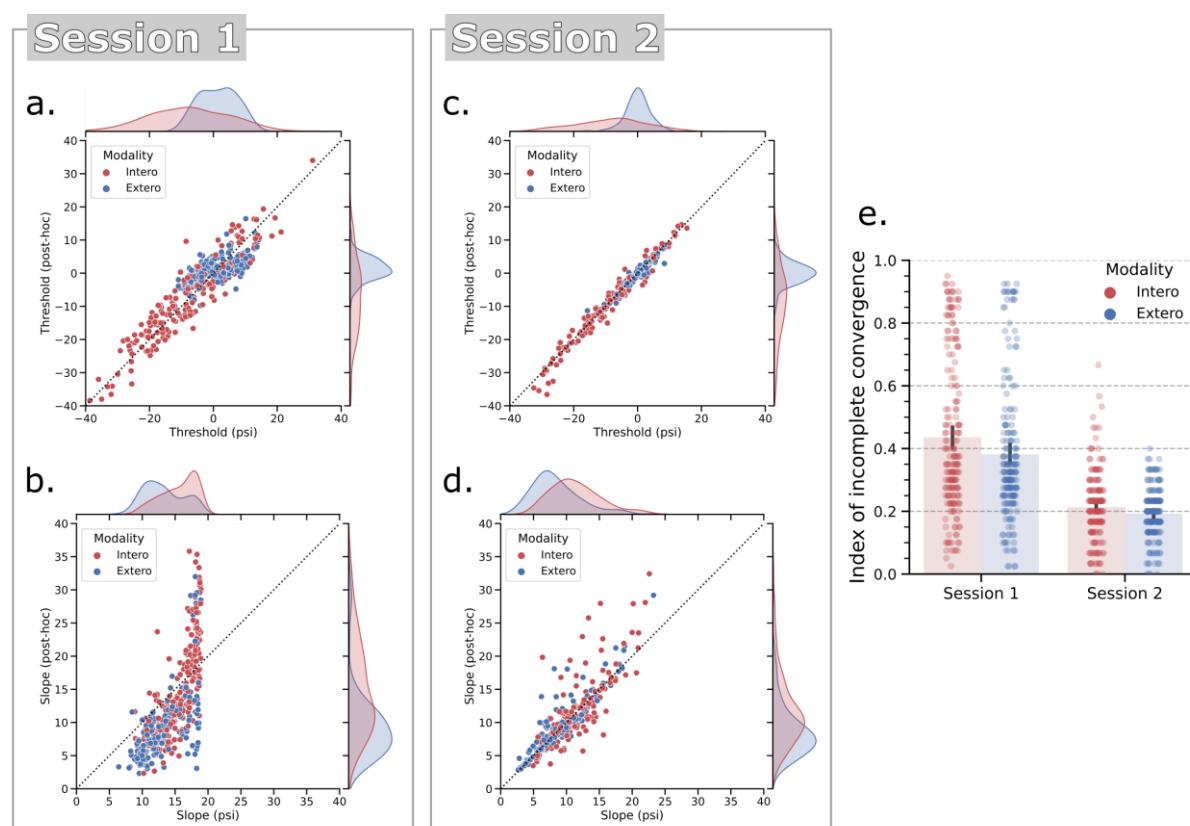
913 In this paper, the psychometric parameters were estimated using a Bayesian model fitted on
914 post-processed response data. This provides, in our opinion, a more robust framework for
915 between session comparisons, and has the advantage to allow for behavioural and physiological
916 data cleaning before model fitting. However, the values of the parameters can also differ
917 between the Psi procedure and the final Bayesian estimates. We report in **Fig. 2** of the
918 **Supplementary Materials** the relation between the values estimated by these two methods for
919 both sessions.

920 When testing covariance using a Pearson correlation, we observed that the threshold
921 estimates were highly consistent across the two estimation methods in both Session 1
922 (Exteroception: $r = 0.63, CI_{95\%} = [0.55, 0.71], n = 206$; Interception: $r = 0.92, CI_{95\%} = [0.91,$
923 $0.94], n = 206$) and Session 2 (Exteroception: $r = 0.96, CI_{95\%} = [0.95, 0.97], n = 154$;
924 Interception: $r = 0.98, CI_{95\%} = [0.98, 0.99], n = 147$). These effects are illustrated in
925 **Supplementary Material Fig. 2. a-c.**

926 We observed more variability in the estimation of slope, as reflected by the slightly
927 lower correlation coefficients in Session 1 (Exteroception: $r = 0.69, CI_{95\%} = [0.62, 0.76], n =$
928 206 ; Interception: $r = 0.80, CI_{95\%} = [0.75, 0.84], n = 206$) compared to Session 2
929 (Exteroception: $r = 0.90, CI_{95\%} = [0.87, 0.93], n = 154$; Interception: $r = 0.78, CI_{95\%} = [0.71,$
930 $0.84], n = 147$). Notably, a ceiling effect and a systematic shift of the slope estimates was
931 observed on Session 1 (see **Supplementary Material Fig. 2. b-d**). The ceiling effect was
932 corrected in Session 2 by using larger parameter ranges. Here, the Bayesian approach included
933 a larger prior range and was able to infer different slope values when the maximum was reached.

934 This analysis illustrates the power of a simple *post hoc* Bayesian modelling approach to
935 improve and correct potential issues in the settings of the Psi staircase. This approach can be
936 further expanded in future works, for example using fully hierarchical (i.e., mixed-effects)
937 Bayesian modelling across participants and groups, improving the estimation of conditional
938 differences in threshold or slope values. This could enhance statistical power by pooling and it
939 further limits the influence of unlikely or outlier responses through group shrinkage effects on
940 the parameter estimates.

941



942

943 **Legend Supplementary Material 2: Comparison between online and post hoc Bayesian estimation of slope**
944 **and threshold parameters of the psychometric functions.** Adaptive Bayesian staircases can be biased if their
945 initial parameter settings poorly fit the underlying generative psychometric function, or if a subject makes
946 unrepresentative responses early in the experiment. For example, in this sample we observed that the prior width
947 [0 - 20] on the slope parameter was too low, resulting in a ceiling effect that biased our estimates in a subset of
948 participants. One solution to control these biases is to implement post hoc Bayesian modelling of the observed
949 psychophysical data. We thus re-analyzed the responses for each participant and each condition separately using
950 a Bayesian model to fit a cumulative normal distribution. **A.** The thresholds estimates remained stable, although
951 with a reduced variance for the exteroceptive condition. **B.** The ceiling effect on the slope was normalized by the
952 post hoc modelling, which shifts the posterior mass away from the extremes. The post hoc procedure can thus
953 improve the estimation of the interoceptive and exteroceptive psychophysical parameters. In session 2, both
954 threshold (**C.**) and slope (**D.**) were more reliably estimated after changes we made on the experimental design and

955 prior ranges of the Psi parameters. **E**. We created an index of staircase convergence to quantify the estimation
956 errors observed in session 1 (see below for details). A higher value reflects more imbalanced intensities around
957 the threshold, which is often associated with improper estimates and convergences of the staircases.

958

959 Another reason for using a Bayesian model was the presence of incomplete convergence
960 of the Psi staircase during the first session. The Psi algorithm (Kontsevich & Tyler, 1999) is
961 designed to test intensity values that would first increase the precision of the posterior density
962 for threshold. When this confidence around the threshold level is high enough, the staircase
963 starts to improve precision for the slope estimate by testing intensity values around the
964 threshold. This results in a recognizable pattern of higher and lower intensities values
965 alternating regularly around the inferred threshold. Interfering with the Bayesian updating
966 during the first 30 trials of the task, as in Session 1, could result in biased estimation of threshold
967 values. Further, erroneous responses during the first trials may hinder convergence.

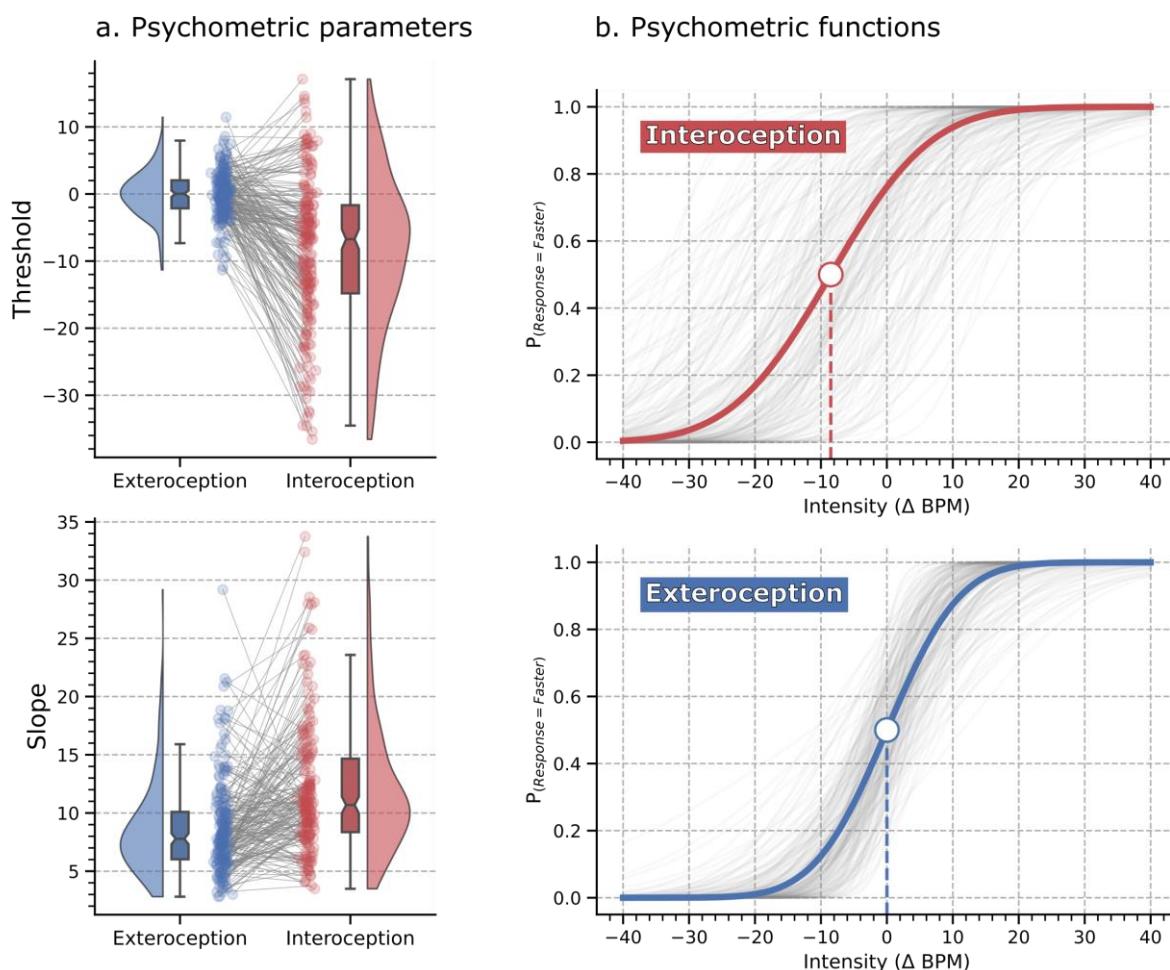
968 Here, we quantified the amount of incomplete Psi staircase convergence through the
969 two sessions. Incomplete convergence is characterized by stimulus intensity values that are
970 consistently higher or lower than the inferred threshold even at the end of the task. To quantify
971 this effect, we calculated an incomplete convergence index using the ratio of high-intensity
972 versus low-intensity values compared to the inferred threshold in the last 40 trials. This ratio
973 was then converted using the following formula:

974
$$\text{IncompleteConvergence} = |\text{ratio} - 0.5| * 2$$

975 This formula returns a real number between 0 and 1. 0 indicates that the intensity values
976 were equally distributed around the inferred threshold in the last 40 trials. Instead, 1 indicates
977 divergence between the tested intensity values and the inferred threshold. The incomplete
978 convergence indexes for Interoception and Exteroception through Session 1 and 2 are reported
979 in **Supplementary Material Fig. 2. e**). These results revealed a high proportion of incomplete
980 convergence in the first session, in both interoception and exteroception conditions. For
981 example, setting an arbitrary threshold for quality assessment at 0.5 revealed that 63 and 41
982 participants had poor convergence for interoception and exteroception, respectively. These
983 numbers dropped radically in Session 2 (see **Material and Method**) and corresponded to only
984 3 and 0 staircases for interoception and exteroception, respectively. The improved convergence
985 in Session 2 is likely due to the introduction of different design choices, aimed at solving the
986 convergence issues observed in Session 1.

987 Psychometric results (Session 2)

988 We reproduced the approach used in the first session and compared threshold and slope values
989 between the interoception and the exteroception conditions. This revealed that during
990 interoception participants had significantly lower psychometric thresholds (mean_{Intero} = -8.50,
991 CI_{95%} [-10.06, -6.92], mean_{Extero} = 0.01, CI_{95%} [-0.47, 0.52], $t_{(190)} = -11.15$, $p < 0.001$, $BF_{10} =$
992 $2.85e+19$, $d = -1.03$) and higher psychometric slopes (mean_{Intero} = 11.96, CI_{95%} [11.22, 12.74],
993 mean_{Extero} = 8.69, CI_{95%} [8.14, 9.28], $t_{(190)} = -7.29$, $p < 0.001$, $BF_{10} = 9.12e+08$, $d = 0.67$). See
994 Fig. 2 and Supplementary Fig. 1 for illustration of these effects. Similarly to the results in the
995 first session, the negative bias of the threshold parameters suggests that participants
996 underestimated their heart rate on average. The greater slope on the other side, indicates a less
997 precise decision process.

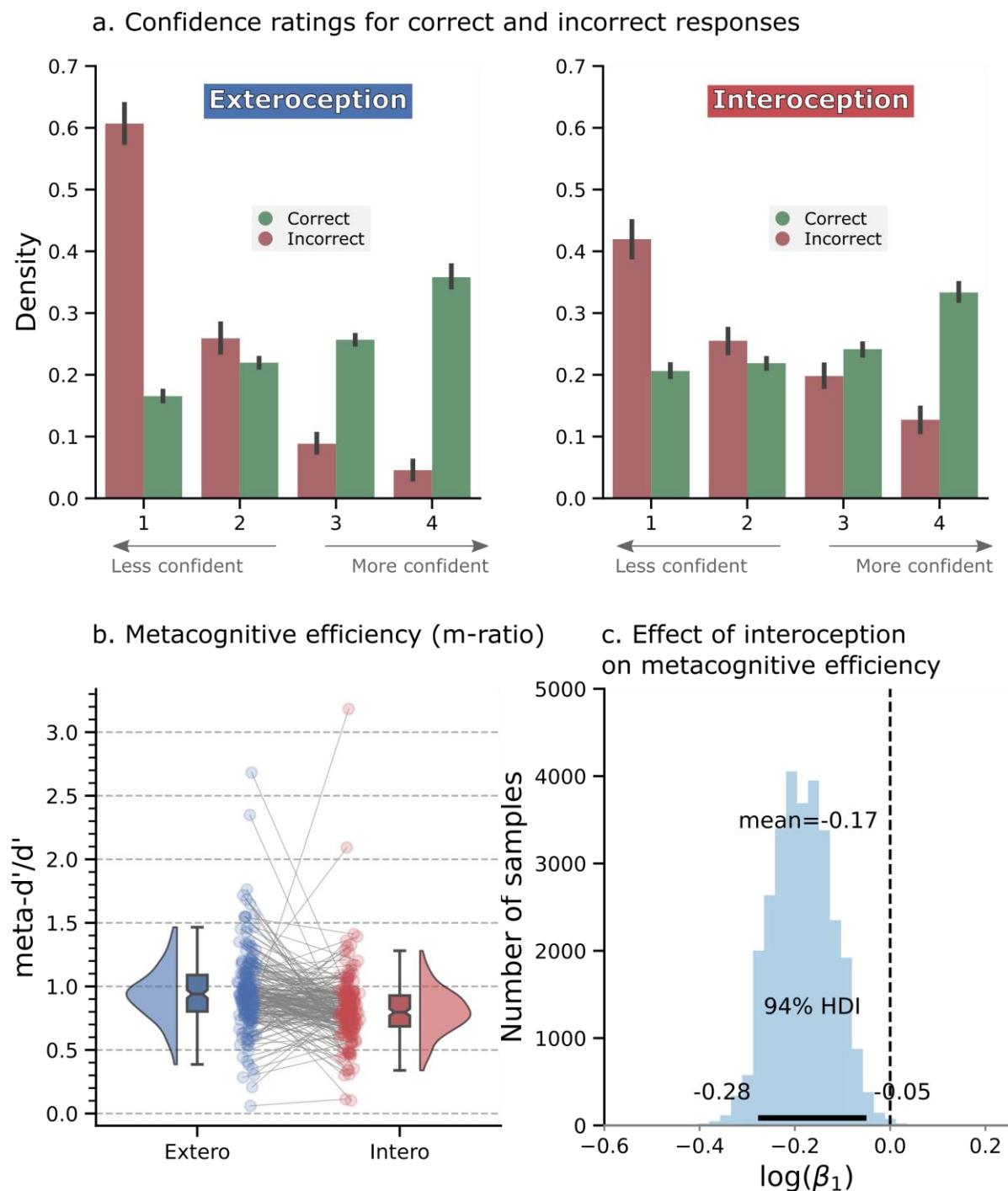


998
999 **Legend Supplementary Material 3: Psychometric parameter estimates and fitted interoception and**
1000 **exteroception psychometric functions (Session 2).** **A.** Repeated measures raincloud plots visualizing threshold
1001 and slope parameters of the psychometric functions across the two modalities (interoception and exteroception).
1002 Data points for every individual are connected by a grey line to highlight the repeated measure effect. **B.** The grey
1003 lines show individual subject fits. The dark red and blue lines show the grand mean psychometric function,

1004 depicting averaged threshold and slope. Grand mean thresholds are marked by the large point, where the
1005 psychometric function crosses 0.5 on the ordinate axis. We observed a strong effect of interoception on both slope
1006 and threshold parameters as compared to the exteroceptive control condition.

1007 **Metacognition results (Session 2)**

1008 The d' , which reflects discrimination sensitivity, was lower in the interoception condition
1009 ($\text{mean}_{\text{Intero}} = 1.88$, $\text{CI}_{95\%} = [1.78, 1.96]$, $\text{mean}_{\text{Extero}} = 2.25$, $\text{CI}_{95\%} = [2.21, 2.3]$, $t_{(189)} = -8.10$, $p <$
1010 0.001 , $\text{BF}_{10} = 9.67\text{e}+10$, $d = -0.77$). Further, as in the first session, we found that metacognitive
1011 sensitivity was significantly lower during interoception. The interoceptive M-ratio estimates
1012 were lower ($\text{mean}_{\text{Intero}} = 0.83$, $\text{CI}_{95\%} = [0.8, 0.87]$) than the exteroceptive ones ($\text{mean}_{\text{Extero}} = 0.96$,
1013 $\text{CI}_{95\%} = [0.92, 1.01]$). The posterior distribution of the repeated measure effect was also lower
1014 ($\text{mean} = -0.17$ $\text{HDI}_{94\%} = [-0.28, -0.05]$).



1015

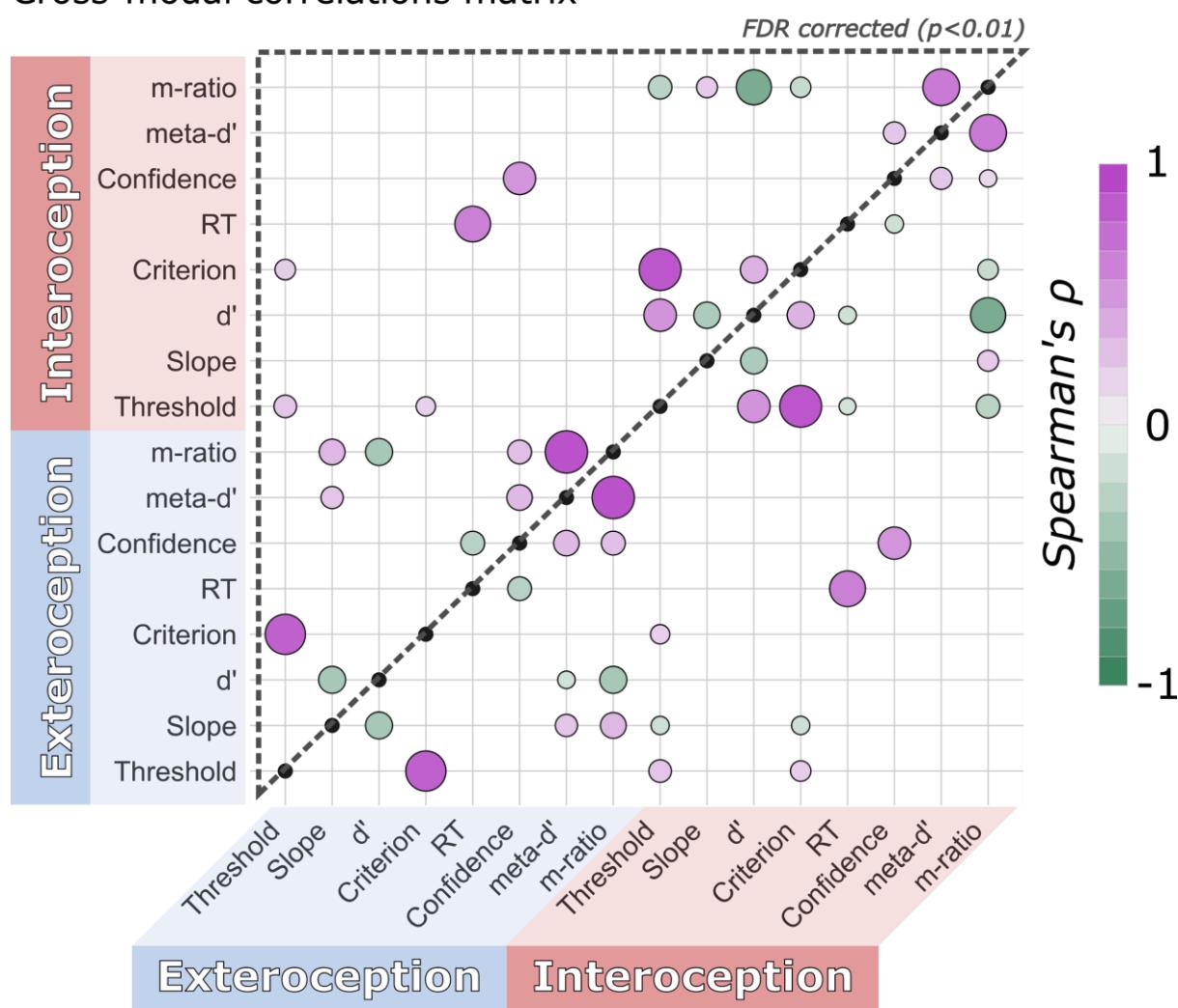
1016 **Legend Supplementary Material 3: Visualization of metacognitive performance for interoceptive and**
 1017 **exteroceptive conditions (Session 2). A.** Histogram showing the distribution of binned confidence ratings for
 1018 correct (green) vs. error (red) trials. Higher bins represent higher confidence ratings. Participants were significantly
 1019 less confident overall in the interoceptive condition and showed reduced calibration as indicated by the flattening
 1020 of the confidence distributions. To quantify this effect, we estimated “metacognitive efficiency”, a signal theoretic
 1021 model of introspective accuracy which controls for differences in type 1 (discrimination) performance. Here, an
 1022 M-ratio of 1 indicates optimal metacognition according to an ideal observer model, whereas values lower than this
 1023 indicate inefficient use of the available perceptual signal. **B.** This model demonstrated that metacognitive

1024 efficiency was substantially decreased for interoceptive relative to exteroceptive judgements. **C.** Histogram of
 1025 posterior samples from the beta value coding the effect of interoception.

1026 Cross-modal correlation (Session 2)

1027 We observed more robust and consistent correlations between task parameters within each
 1028 modality (interoception or exteroception), but few significant correlations between task
 1029 modalities, indicating a high degree of independence between performance on the two task
 1030 conditions. Across modalities, response times during the decision process (type 1 measure)
 1031 were correlated between the interoception and the exteroception conditions ($r_s = 0.66$, $CI_{95\%} =$
 1032 $[0.58, 0.74]$, $p < 0.001$, $n = 190$, $n_{\text{outliers}} = 5$), as well as between confidence ratings ($r_s = 0.54$,
 1033 $CI_{95\%} = [0.44, 0.64]$, $p < 0.001$, $n = 190$, $n_{\text{outliers}} = 3$).

Cross-modal correlations matrix



1034
 1035 **Legend Supplementary Material 4: Cross-modal correlation heatmap of task parameters for interoception**
 1036 **and exteroception conditions (Session 2).** We replicated several of the observations reported in Session 1.
 1037 Behavioural results were correlated within modalities but with limited dependence across modalities. The only

1038 exceptions, already observed in Session 1, were confidence ratings and response times (RT). The figure depicts
1039 significant skipped Spearman correlations. **The upper triangle shows results surviving FDR correction (p_{FDR}**
1040 **< 0.01**). The colour and size of individual points indicate the sign and strength of the estimated correlation
1041 coefficients.

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