

1 DelSIEVE: joint inference of single-nucleotide variants, somatic 2 deletions, and cell phylogeny from single-cell DNA sequencing 3 data

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14 Abstract

15 The swift advancements in single-cell DNA sequencing (scDNA-seq) have enabled quantitative
16 assessment of genetic content in individual cells, allowing downstream analyses at the single-cell
17 resolution. This technology considerably facilitates cancer research, yet its underlying power has
18 not been fully exploited. Specifically, computational methods for variant calling and phylogenetic
19 tree reconstruction struggle due to high coverage variance and allelic dropout. To address these
20 issues, here we present DelSIEVE, a statistical method that directly models the inherent noise
21 in scDNA-seq data for the inference of single-nucleotide variants (SNVs), somatic deletions, and
22 cell phylogeny. In a simulation study DelSIEVE exhibits outstanding performance with respect
23 to the identification of somatic deletions and SNVs. We apply DelSIEVE to three real datasets,
24 where rare double mutant and somatic deletion genotypes are found in colorectal cancer samples.
25 As expected with the more expressive model, for the triple negative breast cancer sample we
26 identify several somatic deletions, with less single and double mutant genotypes as compared to
27 those reported by our previous method SIEVE.

28 Introduction

29 Cancer is a genetic disease driven by somatic mutations in the evolutionary process [1–5], result-
30 ing in highly heterogeneous cell populations. One of the somatic mutations is single nucleotide
31 variants (SNVs), which, through nucleotide substitutions, can activate oncogenes and thus pro-
32 moting tumor proliferation, and can inactivate tumor suppressor genes, resulting in malfunc-
33 tioned proteins. Another type of somatic mutations is *somatic deletions*, which can inactivate
34 tumor suppressor genes by reducing the number of genomic copies through point deletions,
35 small deletions and copy number aberrations (CNAs) [2, 3, 5–8]. Phylogenetic inference is typ-
36 ically used to understand and quantify the underlying complexity, or intra-tumor heterogeneity
37 (ITH) [9–11], which has substantial relevance in the clinical therapy and prognosis of cancer,
38 especially against acquired resistance and relapse of tumor [11–13].

39 Previously, methods have been developed for bulk sequencing data to derive variant allele [14–
40 18] and CNA profiles [19–22] of clones, as well as to reconstruct tumor phylogeny [23–27]. Lately,
41 the rapid development of single-cell DNA sequencing (scDNA-seq) technologies exhibit great
42 potential for the analysis of ITH by profiling genetic materials with fine resolution of individual
43 cells [28–31]. However, despite the strengths, scDNA-seq suffers from a low signal-to-noise
44 ratio, mainly due to the necessity of performing whole genome amplification (WGA) on the
45 limited genetic material present in a single cell [31–35]. A popular WGA method is multiple
46 displacement amplification (MDA) [36–40], which can generate a great amount of DNA copies
47 efficiently without introducing many errors. However, MDA is prone to biases against genomic
48 regions, leading to uneven coverage of the genome. Additionally, it may result in allelic dropout
49 (ADO), where one of the two alleles fails to be amplified during the process. In some cases, the
50 amplification of both alleles may fail, leading to locus dropout, which is a potential source of
51 missing data. Such data is suitable for SNV calling, but not for CNA calling, as it is challenging
52 to differentiate true CNA events from amplification biases [31, 32, 35].

53 Several methods calling SNVs from scDNA-seq have been proposed, which manage to in-
54 crease statistical power in distinct aspects to account for specific errors. For instance, Mono-
55 var [41] pools single cells at each site together, while SCcaller [42], LiRA [43] and SCAN-SNV [44]
56 leverage information on germline single nucleotide polymorphisms. The called SNVs can be used
57 then as input for phylogenetic inference by other methods [45–52], reconstructing the cell phy-
58 logeny with existing cells as leaves and extinct cells as internal nodes in the tree. To share more

59 effectively information among individual cells and to reduce uncertainties introduced by variant
60 callers in phylogenetic inference [53], SCIPhiI [54] and SIEVE (previously developed by us) [55]
61 jointly infer SNVs and cell phylogeny. SCIPhiI considers a cell phylogeny without branch lengths
62 under the infinite-sites assumption (ISA), which is reportedly often violated in reality [56–58]. In
63 contrast, SIEVE models a cell phylogeny with branch lengths corrected for acquisition bias [59,
64] [60] under the finite-sites assumption (FSA) within a statistical phylogenetic model, and models
65 the sequencing coverage using a negative binomial distribution. Accounting for more informa-
66 tion and providing a more flexible model to share information across cells, SIEVE outperforms
67 SCIPhiI in both SNV calling and cell phylogeny reconstruction [55].

68 One assumption of SIEVE’s statistical phylogenetic model is that the genome remains diploid
69 during the evolutionary process of the tumor, overlooking the possible occurrence of somatic dele-
70 tions. Indeed, the inclusion and the accurate identification of somatic deletions for scDNA-seq
71 remains a challenging problem. This difficulty arises because the sequencing data generated by
72 somatic deletions bears a resemblance to and can be mistaken for ADOs or somatic back muta-
73 tions. Nevertheless, to address this issue, innovative methods have explored the incorporation
74 of a cell phylogeny, leveraging the idea that cells residing closely on the evolutionary tree share
75 related information, while ADOs occur independently during the sequencing process. SCAR-
76 LET [61] takes the first step in this direction by refining a copy number tree using read counts
77 for SNVs with a loss-supported phylogeny model. SCIPhiN [62] considers somatic deletions, and
78 allows for mutational losses and recurrent mutations on the cell phylogeny. However, both of
79 them relax the ISA to only a limited extent, which might result in them missing other important
80 events in the evolutionary process, such as double mutations (mutations affecting both alleles
81 at a variant site). In addition, both SCARLET and SCIPhiN ignore the information conveyed
82 by sequencing coverage. However, scDNA-seq data, particularly when coupled with MDA am-
83 plification method, is highly uneven across the genome. Therefore, deliberately disregarding the
84 intricacies of sequencing coverage may result in substantial loss of the information embedded
85 within the dataset.

86 We reasoned that utilizing the additional signal in coverage, combined with the information
87 encoded in the raw read counts and phylogenetic similarities among cells, a model extending
88 SIEVE could account for somatic deletions. Building upon this intuition, here we introduce
89 DelSIEVE (somatic Deletions enabled SIngle-cell EVolution Explorer), a statistical phylogenetic
90 model that includes all features of SIEVE, namely correcting branch lengths of the cell phylogeny

91 for the acquisition bias, incorporating a trunk to model the establishment of the tumor clone,
92 employing a Dirichlet-multinomial distribution to model the raw read counts for all nucleotides,
93 as well as modeling the sequencing coverage using a negative binomial distribution, and extends
94 them with the more versatile capacity of calling somatic deletions. DelSIEVE is capable of
95 modeling locus dropout, where both alleles at a site are allowed to be dropped out during
96 WGA. Importantly, it is the first model leveraging phylogenetic similarities among cells to tell
97 apart the factual deletion genotypes from back mutations or technical artifacts such as ADO
98 or locus dropout. By doing so, DelSIEVE is able to discern 28 types of genotype transitions,
99 associated with 17 types of mutation events, much more than the 12 types of transitions that
100 SIEVE can discern. DelSIEVE is available as a package of BEAST 2 [63] at <https://github.com/szczurek-lab/DelSIEVE>.

102 Methods

103 In the evolution of tumor, both SNVs and somatic deletions play important roles, leading to
104 highly heterogeneous tumor populations. Assuming a diploid genome in a normal cell as the
105 origin of tumor evolution, our DelSIEVE model performs joint inference of cell phylogeny from
106 scDNA-seq and the resulting SNVs and somatic deletions in single cells.

107 DelSIEVE model

108 DelSIEVE takes as input raw read counts for all four nucleotides for cell $j \in \{1, \dots, J\}$ at
109 candidate site $i \in \{1, \dots, I\}$ in the form of $\mathcal{D}_{ij}^{(1)} = (\mathbf{m}_{ij}, c_{ij})$, where $\mathbf{m}_{ij} = \{m_{ijk} \mid k = 1, 2, 3\}$
110 is the read counts of three alternative nucleotides with values in descending order and c_{ij} is the
111 sequencing coverage (Figure 1a; see Kang *et al.* [55] for explanation of how candidate sites are
112 identified). DelSIEVE also optionally takes raw read counts data $\mathcal{D}^{(2)}$ from I' background sites
113 for acquisition bias correction. It is important to note that since DelSIEVE requires preselected
114 candidate variant sites as input, it can only identify somatic deletions at those candidate sites.

115 The model first infers the cell phylogeny, followed by maximum likelihood estimation of the
116 genotype state of each node in the tree (Figure 1a). The power of DelSIEVE lies in the elegantly
117 devised probabilistic graphical model, where the hidden variable describing the genotype for site
118 i in cell j , denoted g_{ij} , is used as the bridge between the statistical phylogenetic model and the
119 model of raw read counts (Figure 1b).

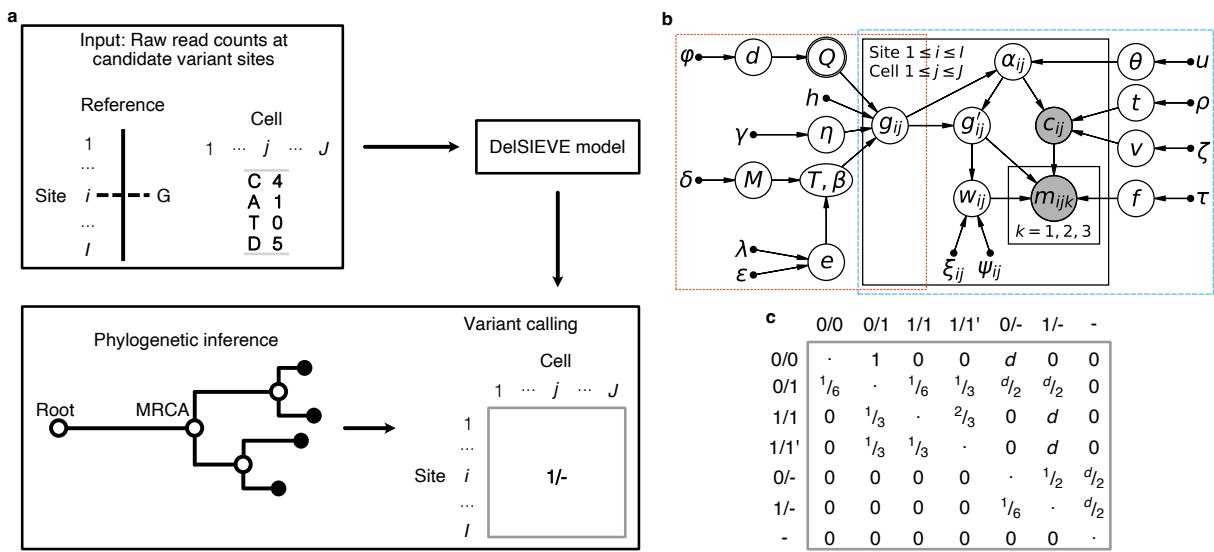


Figure 1: Overview of the DelSIEVE model. **a** Analysis workflow of DelSIEVE with an example of input data. At candidate variant site $i \in \{1, \dots, I\}$, the reference nucleotide is G. For cell $j \in \{1, \dots, J\}$ at site i , observed are sequencing depth being 5 (marked by D) as well as read counts for nucleotide C being 4 and A being 1. Inferred first is the cell phylogeny from the input data by DelSIEVE. Based on the cell phylogeny, determined is the genotype state of each node in the tree through maximum likelihood estimation. For instance, 1/- is inferred as the genotype state of cell j at site i . **b** Probabilistic graphical model of DelSIEVE. The orange dotted frame shows the part corresponding to the statistical phylogenetic model, and the blue dashed frame encloses the part corresponding to the model of raw read counts. Shaded circle nodes represent observed variables, while unshaded circle nodes represent hidden random variables. Nodes with double circles are deterministic random variables, meaning that they are readily fixed once the values of their parents are determined. Small filled circles correspond to fixed hyper parameters. Arrows denote local conditional probability distributions of child nodes given parent nodes. **c** Instantaneous transition rate matrix of the statistical phylogenetic model. The hidden random variable d is the deletion rate, measured relatively to the mutation rate. The elements in the diagonal of the matrix are denoted by dots, and have negative values equal to the sum of the other entries in the same row, ensuring that the sum of each row equals zero.

120 Statistical phylogenetic model

121 DelSIEVE expands the genotype state space defined in SIEVE: on top of 0/0 (*wildtype*), 0/1
 122 (*single mutant*), 1/1 (*double mutant*, where the two alternative nucleotides are the same) and
 123 1/1' (*double mutant*, where the two alternative nucleotides are different), DelSIEVE additionally
 124 considers 0/- (*reference-left single deletion*), 1/- (*alternative-left single deletion*) and - (*double*
 125 *deletion*). Here, 0, 1, 1' and - represent the reference nucleotide, an alternative nucleotide, a
 126 second alternative nucleotide different from that denoted by 1, and deletions, respectively. The
 127 expanded genotype state space $G = \{0/0, 0/1, 1/1, 1/1', 0/-, 1/-, -\}$ enables the addition of somatic
 128 deletions as possible events in the statistical phylogenetic model (Figure 1c). Given the genotype
 129 state space G , DelSIEVE is able to discern 28 types of genotype transitions (16 more than
 130 SIEVE), which can be categorized into 17 types of mutation events (8 more than SIEVE; see

131 Section **Mutation event classification**).

132 With the genotype state space G specified, we define the instantaneous transition rate matrix
 133 Q in **Figure 1c**, which is the key component to the statistical phylogenetic model. We set the
 134 somatic mutation rate to 1, where the relative measurements for back mutation rate and deletion
 135 rate are $1/3$ and d , respectively. Thus, Q is deterministic and depends on the hidden random
 136 variable corresponding to the relative deletion rate d :

$$P(Q | d) = 1. \quad (1)$$

137 Each entry in Q represents the transition rate from the genotype in the row to that in the column
 138 during an infinitesimal time Δt . Besides, each row in Q sums up to 0. The continuous-time
 139 homogeneous Markov chain underlying Q is time non-reversible and reducible. For instance,
 140 genotypes that have both alleles present can transition to genotypes with one or both alleles
 141 lost, but not vice versa. To be specific, genotypes $\{0/0, 0/1, 1/1, 1/1'\}$ and genotypes $\{0/-, 1/-\}$
 142 form two ergodic, transient communicating classes, while genotype $\{\}$ forms a closed communica-
 143 cating class. As a result, the limiting distribution of the Markov chain exists, where the value
 144 corresponding to genotype $-$ is 1, while the others are 0.

145 Based on the well-established theory of statistical phylogenetic models, the joint conditional
 146 probability of the genotype states of all sequenced cells at site i , namely $\mathbf{g}_i^{(L)}$, is

$$P\left(\mathbf{g}_i^{(L)} \mid \mathcal{T}, \boldsymbol{\beta}, Q, h, \eta\right) = \sum_{\mathbf{g}_i^{(A)} \setminus \{g_{i(2J)}\}} P\left(\mathbf{g}_i^{(L)}, \mathbf{g}_i^{(A)} \setminus \{g_{i(2J)}\} \mid \mathcal{T}, \boldsymbol{\beta}, Q, h, \eta\right). \quad (2)$$

147 Intuitively, this means that to compute the likelihood of the genotypes of the variant sites at the
 148 leaves, we marginalize out the genotypes at the ancestor nodes from the total likelihood. The
 149 variables in **Equation (2)** have the same meaning as in SIEVE. Briefly speaking, \mathcal{T} is the rooted
 150 binary tree topology, whose root, representing a normal cell with diploid genome, has only one
 151 child, the MRCA of all sequenced cells. \mathcal{T} has J existing, sequenced cells as leaves, whose
 152 genotypes are $\mathbf{g}_i^{(L)} = (g_{i1}, \dots, g_{ij}, \dots, g_{iJ})^T$, where $g_{ij} \in G$. The J extinct, ancestor cells in \mathcal{T} as
 153 internal nodes have genotypes $\mathbf{g}_i^{(A)} = (g_{i(J+1)}, \dots, g_{ij}, \dots, g_{i(2J)})^T$, where $g_{ij} \setminus \{g_{i(2J)}\} \in G$ and
 154 $g_{i(2J)} = 0/0$. \mathcal{T} also has $2J-1$ branches, whose lengths $\boldsymbol{\beta} \in \mathbb{R}^{2J-1}$ represent the expected number
 155 of somatic mutations per site. h and η are the number of rate categories and shape, respectively,
 156 of a discrete Gamma distribution with mean equal 1 for modeling among-site substitution rate

157 variation. Hidden random variables d in [Equation \(1\)](#) and \mathcal{T}, β, η in [Equation \(2\)](#) are estimated
 158 using MCMC, while the fixed hyperparameter h takes value 4 by default.

159 Given deletion rate d (and thus Q) and branch length β , the seven-by-seven transition
 160 probability matrix $R(\beta)$ is computed as $R(\beta) = \exp(Q\beta)$ [\[53\]](#).

161 **Model of raw read counts**

162 We factorize the probability of observing \mathcal{D}_{ij} for cell j at site i into

$$P(\mathcal{D}_{ij}) = P(\mathbf{m}_{ij} | c_{ij})P(c_{ij}), \quad (3)$$

163 where the former corresponds to the model of nucleotide read counts and the latter to the model
 164 of sequencing coverage.

165 **Model of sequencing coverage.** One of the major, yet often overlooked challenges in scDNA-
 166 seq is the highly uneven sequencing coverage. This happens because the genetic materials are
 167 amplified largely unequally during WGA. Similar to SIEVE, we employ a negative binomial
 168 distribution to capture the overdispersion existing in the sequencing coverage:

$$P(c | p, r) = \binom{c + r - 1}{r - 1} p^r (1 - p)^c, \quad (4)$$

169 where p and r are parameters. To improve interpretability, the distribution is reparameterized
 170 using mean μ and variance σ^2 :

$$\begin{cases} p = \frac{\mu}{\sigma^2}, \\ r = \frac{\mu^2}{\sigma^2 - \mu}. \end{cases} \quad (5)$$

171 We assume that μ_{ij} and σ_{ij}^2 have the same form as in SIEVE, namely

$$\begin{aligned} \mu_{ij} &= \alpha_{ij} t s_j, \\ \sigma_{ij}^2 &= \mu_{ij} + \alpha_{ij}^2 \nu s_j^2. \end{aligned} \quad (6)$$

172 Here, t and ν are the mean and the variance of allelic coverage, respectively. $\alpha_{ij} \in \{0, 1, 2\}$
 173 represents the number of sequenced alleles. With the extended genotype state space G in the
 174 DelSIEVE model, the number of alleles possessed by a cell at a site can either be zero (corre-
 175 sponding to genotype state $\{-\}$), one (genotype states $\{0/-, 1/-\}$), or two ($\{0/0, 0/1, 1/1, 1/1'\}$).

176 On top of that, the possible occurrence of ADOs during scWGA could alter the number of alleles
 177 possessed by a cell at a site. Here, we model two types of ADOs, single ADO and locus dropout.

178 The single ADO mode was previously proposed by us in SIEVE, where at most one ADO is
 179 allowed to happen to cell j at site i . For DelSIEVE, the corresponding prior distribution of α_{ij} ,
 180 $P(\alpha_{ij} | g_{ij}, \theta)$, is defined in [Table 1](#), where θ denotes the probability of the occurrence of single
 181 ADO when both alleles exist. One should consider the "Single ADO occurred" column as value
 182 of an additional hidden random variable corresponding to an ADO occurrence indicator, which
 183 will be marginalized out in the model. For example, the probability of an event of single ADO
 184 occurrence when $g_{ij} = 0/-$ equals $\theta/2$, because there is only one allele left to be dropped out. For
 185 genotype $-$, it is certain that single ADO has not occurred as there is no allele existing.

Table 1: Definition of the distribution of α_{ij} conditional on g_{ij} and θ under single ADO mode for DelSIEVE.

α_{ij}	g_{ij}	Single ADO occurred	$P(\alpha_{ij} g_{ij}, \theta)$
1	0/0	Yes	θ
2	0/0	No	$1 - \theta$
1	0/1	Yes	θ
2	0/1	No	$1 - \theta$
1	1/1	Yes	θ
2	1/1	No	$1 - \theta$
1	1/1'	Yes	θ
2	1/1'	No	$1 - \theta$
0	0/-	Yes	$\theta/2$
1	0/-	No	$1 - \theta/2$
0	1/-	Yes	$\theta/2$
1	1/-	No	$1 - \theta/2$
0	-	No	1
		Others	0

186 To generalize DelSIEVE to model both ADO and locus dropout, we allow more than one
 187 allele to drop out. $P(\alpha_{ij} | g_{ij}, \theta)$ is defined in [Table 2](#), where θ represents the probability of an
 188 allele dropped out. We assume that the ADOs occur to each allele independently. For instance,
 189 when $g_{ij} = 0/0$, the probability of $\alpha_{ij} = 0$ is θ^2 , happening only when both alleles drop out. For
 190 genotype $0/-$, the sole allele drops out with probability θ , resulting in zero sequenced alleles.

191 s_j in [Equation \(6\)](#) is the size factor of cell j , which is estimated exactly in the same way as
 192 in SIEVE:

$$\hat{s}_j = \text{median}_{i:c_{ij} \neq 0} \frac{c_{ij}}{\left(\prod_{\substack{j'=1 \\ c_{ij'} \neq 0}}^{J'} c_{ij'} \right)^{\frac{1}{J'}}}, \quad (7)$$

Table 2: Definition of the distribution of α_{ij} conditional on g_{ij} and θ under locus dropout mode for DelSIEVE.

α_{ij}	g_{ij}	Number of alleles dropped out	$P(\alpha_{ij} g_{ij}, \theta)$
0	0/0	2	θ^2
1	0/0	1	$2\theta(1-\theta)$
2	0/0	0	$(1-\theta)^2$
0	0/1	2	θ^2
1	0/1	1	$2\theta(1-\theta)$
2	0/1	0	$(1-\theta)^2$
0	1/1	2	θ^2
1	1/1	1	$2\theta(1-\theta)$
2	1/1	0	$(1-\theta)^2$
0	1/1'	2	θ^2
1	1/1'	1	$2\theta(1-\theta)$
2	1/1'	0	$(1-\theta)^2$
0	0/-	1	θ
1	0/-	0	$1-\theta$
0	1/-	1	θ
1	1/-	0	$1-\theta$
0	-	0	1
Others			0

193 where J' is the number of cells with non-zero coverage at a site.

194 **Model of nucleotide read counts.** We showed before that the occurrence of ADOs could
195 change the number of alleles possessed by cell j at site i . As a result, the genotype g_{ij} could
196 change to the *ADO-affected genotype*, $g'_{ij} \in G$. The probability of g'_{ij} writes $P(g'_{ij} | g_{ij}, \alpha_{ij})$,
197 which is defined in [Table 3](#) for the single ADO mode and in [Table 4](#) for the locus dropout mode.
198 When $g'_{ij} \in G \setminus \{\}$, we model \mathbf{m}_{ij} , the read counts of three alternative nucleotides, conditional
199 on the sequencing coverage c_{ij} with a Dirichlet-multinomial distribution as

$$P(\mathbf{m}_{ij} | c_{ij}, \mathbf{a}_{ij}) = \frac{F(c_{ij}, a_{ij0})}{\prod_{k=1: m_{ijk} > 0}^3 F(m_{ijk}, a_{ijk}) F(c_{ij} - \sum_{k=1}^3 m_{ijk}, a_{ij4})}, \quad (8)$$

200 with parameters $\mathbf{a}_{ij} = \{a_{ijk} | k = 1, \dots, 4\}$ and $a_{ij0} = \sum_{k=1}^4 a_{ijk}$. F is a function defined as

$$F(x, y) = \begin{cases} xB(y, x), & \text{if } x > 0, \\ 1, & \text{otherwise,} \end{cases} \quad (9)$$

201 where B is the beta function. Note that $c_{ij} - \sum_{k=1}^3 m_{ijk}$ is the read count of the reference
202 nucleotide.

203 Similar to SIEVE, we reparameterize [Equation \(8\)](#) by letting $\mathbf{a}_{ij} = w_{ij} \mathbf{f}_{ij}$. w_{ij} is related to

Table 3: Definition of the distribution of g'_{ij} conditional on g_{ij} and α_{ij} under single ADO mode for DelSIEVE.

g'_{ij}	g_{ij}	α_{ij}	$P(g'_{ij} g_{ij}, \alpha_{ij})$
0/0	0/0	2	1
0/-	0/0	1	1
0/1	0/1	2	1
0/-	0/1	1	$\frac{1}{2}$
1/-	0/1	1	$\frac{1}{2}$
1/1	1/1	2	1
1/-	1/1	1	1
1/1'	1/1'	2	1
1/-	1/1'	1	1
0/-	0/-	1	1
-	0/-	0	1
1/-	1/-	1	1
-	1/-	0	1
-	-	0	1
Others			0

204 the overdispersion. $\mathbf{f}_{ij} = \{f_{ijk} | k = 1, \dots, 4\}$, $\sum_{k=1}^4 f_{ijk} = 1$ is a vector of expected frequencies
 205 of each nucleotide, where the first three elements correspond to the three alternative nucleotides
 206 ordered decreasingly according to their read counts, and the last to the reference nucleotide.
 207 Depending on g'_{ij} , \mathbf{f}_{ij} is given by

$$f_{ij} = \begin{cases} \mathbf{f}_1 = \left(\frac{1}{3}f, \frac{1}{3}f, \frac{1}{3}f, 1-f \right), & \text{if } g'_{ij} = 0/0 \text{ or } 0/-, \\ \mathbf{f}_2 = \left(\frac{1}{2} - \frac{1}{3}f, \frac{1}{3}f, \frac{1}{3}f, \frac{1}{2} - \frac{1}{3}f \right), & \text{if } g'_{ij} = 0/1, \\ \mathbf{f}_3 = \left(1-f, \frac{1}{3}f, \frac{1}{3}f, \frac{1}{3}f \right), & \text{if } g'_{ij} = 1/1 \text{ or } 1/-, \\ \mathbf{f}_4 = \left(\frac{1}{2} - \frac{1}{3}f, \frac{1}{2} - \frac{1}{3}f, \frac{1}{3}f, \frac{1}{3}f \right), & \text{if } g'_{ij} = 1/1', \end{cases} \quad (10)$$

208 where f is the effective sequencing error rate, combining together amplification and sequencing
 209 errors.

210 The parameter w_{ij} also depends on g'_{ij} , where

$$w_{ij} = \begin{cases} w_1, & \text{if } g'_{ij} = 0/0, 0/-, 1/1, \text{ or } 1/-, \\ w_2, & \text{if } g'_{ij} = 0/1 \text{ or } 1/1', \end{cases} \quad (11)$$

211 and w_1 corresponds to wild type overdispersion and w_2 to alternative overdispersion.

Table 4: Definition of the distribution of g'_{ij} conditional on g_{ij} and α_{ij} under locus dropout mode for DelSIEVE.

g'_{ij}	g_{ij}	α_{ij}	$P(g'_{ij} g_{ij}, \alpha_{ij})$
0/0	0/0	2	1
0/-	0/0	1	1
-	0/0	0	1
0/1	0/1	2	1
0/-	0/1	1	$\frac{1}{2}$
1/-	0/1	1	$\frac{1}{2}$
-	0/1	0	1
1/1	1/1	2	1
1/-	1/1	1	1
-	1/1	0	1
1/1'	1/1'	2	1
1/-	1/1'	1	1
-	1/1'	0	1
0/-	0/-	1	1
-	0/-	0	1
1/-	1/-	1	1
-	1/-	0	1
-	-	0	1
Others			0

212 By plugging Equations (10) and (11) into Equation (8), we have

$$P(\mathbf{m}_{ij} | c_{ij}, g'_{ij}, f, w_{ij}) = \begin{cases} P_{0/0} = P(\mathbf{m}_{ij} | c_{ij}, g'_{ij} = 0/0, \mathbf{f}_1, w_1), \\ P_{0/-} = P(\mathbf{m}_{ij} | c_{ij}, g'_{ij} = 0/-, \mathbf{f}_1, w_1), \\ P_{0/1} = P(\mathbf{m}_{ij} | c_{ij}, g'_{ij} = 0/1, \mathbf{f}_2, w_2), \\ P_{1/1} = P(\mathbf{m}_{ij} | c_{ij}, g'_{ij} = 1/1, \mathbf{f}_3, w_1), \\ P_{1/-} = P(\mathbf{m}_{ij} | c_{ij}, g'_{ij} = 1/-, \mathbf{f}_3, w_1), \\ P_{1/1'} = P(\mathbf{m}_{ij} | c_{ij}, g'_{ij} = 1/1', \mathbf{f}_4, w_2), \\ P_- = P(\mathbf{m}_{ij} | c_{ij}, g'_{ij} = -, f, w_{ij}) = 1, \end{cases} \quad (12)$$

213 where we additionally define $P(\mathbf{m}_{ij} | c_{ij}, g'_{ij} = -, f, w_{ij}) = 1$.

214 Although g_{ij} and g'_{ij} share the same genotype state space, it's important to note that some
215 genotype states can arise from distinct evolutionary or technical events. For instance, genotype
216 1/- could be the outcome of evolutionary processes, where one allele was deleted while the
217 other remained intact. Alternatively, it could also be a result of technical artifacts, where
218 both alleles were initially present before scWGA, but one allele experienced dropout during
219 the amplification process. The presence of multiple potential causes for genotypes, such as

220 the genotype 1/-, introduces a significant challenge in disentangling their origins compared
221 to methods like SIEVE, which predominantly attribute such genotypes to technical artifacts.
222 However, an encouraging development is the integration of the statistical phylogenetic model
223 and the model of sequencing coverage. This integration allows for a comprehensive analysis
224 from both evolutionary and technical perspectives, thereby facilitating the disentanglement. By
225 incorporating the statistical phylogenetic model, we gain insights into the evolutionary dynamics
226 underlying genotype development, while the model of sequencing coverage provides valuable
227 information about the technical nuances of the sequencing technique employed. This combined
228 approach offers a more robust framework for disentangling the complex factors contributing to
229 genotypic variations and enhancing our understanding of the underlying biological and technical
230 processes involved.

231 **DelSIEVE likelihood**

232 Combining the statistical phylogenetic model and the model of raw read counts described above,
233 we acquire the likelihood of DelSIEVE, denoted by

$$P\left(\mathcal{D}^{(1)}, \mathcal{D}^{(2)} \mid \mathcal{T}, \boldsymbol{\beta}, Q, h, \eta, t, v, \theta, f, w_1, w_2\right). \quad (13)$$

234 To simplify notation, we denote some variables in the statistical phylogenetic model as
235 $\Theta = \{\mathcal{T}, \boldsymbol{\beta}, Q, h, \eta\}$ and some in the model of raw read counts as $\Phi = \{t, v, \theta, f, w_1, w_2\}$. By
236 taking the logarithm, [Equation \(13\)](#) is further writes

$$\log \mathcal{L}(\Theta, \Phi) = \log \mathcal{L}^{(1)}(\Theta, \Phi) + \log \mathcal{L}^{(2)}(\Theta, \Phi), \quad (14)$$

237 where $\mathcal{L}^{(1)}$ is the tree likelihood corrected for acquisition bias computed for candidate SNV sites
238 in $\mathcal{D}^{(1)}$, while $\mathcal{L}^{(2)}$ is the likelihood computed for background sites in $\mathcal{D}^{(2)}$, referred to as the
239 background likelihood.

240 Acquisition bias refers to the cases where the branch lengths of cell phylogenies are overes-
241 timated when only using data from SNV sites as input [\[59, 60\]](#). Here, it is corrected similarly
242 to SIEVE, following [\[64\]](#):

$$\log \mathcal{L}^{(1)} = \log P\left(\mathcal{D}^{(1)} \mid \Theta, \Phi\right) + I' \log \left(\frac{1}{I} \sum_{i=1}^I C_i\right), \quad (15)$$

243 where the first component is the uncorrected tree log-likelihood for SNV sites, and C_i in the
 244 second component is the likelihood of SNV site i being invariant (see below).

245 To compute $\log P(\mathcal{D}^{(1)} | \Theta, \Phi)$ in [Equation \(15\)](#), we decompose it according to the proba-
 246 bistic graphical model in [Figure 1b](#). Assuming independent and identical evolution of each
 247 candidate variant site, $\log P(\mathcal{D}^{(1)} | \Theta, \Phi)$ writes

$$\begin{aligned}
 \log P(\mathcal{D}^{(1)} | \Theta, \Phi) &= \sum_{i=1}^I \log \sum_{\mathbf{g}_i^{(L)}, \mathbf{g}_i^{(A)} \setminus \{g_{i(2J)}\}} \left[P(\mathcal{D}_i^{(1)} | \mathbf{g}_i^{(L)}, \Phi) \right. \\
 &\quad \left. \times P(\mathbf{g}_i^{(L)}, \mathbf{g}_i^{(A)} \setminus \{g_{i(2J)}\} | \Theta) \right] \\
 &= \sum_{i=1}^I \log \sum_{\mathbf{g}_i^{(L)}, \mathbf{g}_i^{(A)} \setminus \{g_{i(2J)}\}} \left[\prod_{j=1}^J P(\mathbf{m}_{ij}, c_{ij} | g_{ij}, \Phi) \right. \\
 &\quad \left. \times P(\mathbf{g}_i^{(L)}, \mathbf{g}_i^{(A)} \setminus \{g_{i(2J)}\} | \Theta) \right] \\
 &= \sum_{i=1}^I \sum_{j=1}^J \log \sum_{\mathbf{g}_i^{(L)}, \mathbf{g}_i^{(A)} \setminus \{g_{i(2J)}\}} \left[P(\mathbf{m}_{ij}, c_{ij} | g_{ij}, \Phi) \right. \\
 &\quad \left. \times P(\mathbf{g}_i^{(L)}, \mathbf{g}_i^{(A)} \setminus \{g_{i(2J)}\} | \Theta) \right], \tag{16}
 \end{aligned}$$

248 where $P(\mathbf{m}_{ij}, c_{ij} | g_{ij}, \Phi)$, representing the model of raw read counts applied on the leaves of the
 249 phylogenetic tree, is similarly decomposed into

$$\begin{aligned}
 P(\mathbf{m}_{ij}, c_{ij} | g_{ij}, \Phi) &= P(\mathbf{m}_{ij}, c_{ij} | g_{ij}, f, w_{ij}, t, v, \theta) \\
 &= \sum_{\alpha_{ij}, g'_{ij}} P(\mathbf{m}_{ij}, c_{ij}, \alpha_{ij}, g'_{ij} | g_{ij}, f, w_{ij}, t, v, \theta) \\
 &= \sum_{\alpha_{ij}, g'_{ij}} \left[P(\mathbf{m}_{ij} | c_{ij}, g'_{ij}, f, w_{ij}) P(g'_{ij} | g_{ij}, \alpha_{ij}) \right. \\
 &\quad \left. \times P(c_{ij} | \alpha_{ij}, t, v) P(\alpha_{ij} | g_{ij}, \theta) \right]. \tag{17}
 \end{aligned}$$

250 $P(c_{ij} | \alpha_{ij}, t, v)$ in the above equation is defined through [Equations \(4\)](#) to [\(6\)](#), and $P(\mathbf{m}_{ij} | c_{ij}, g'_{ij}, f, w_{ij})$
 251 is defined in [Equation \(12\)](#). Under the single ADO mode, $P(\alpha_{ij} | g_{ij}, \theta)$ and $P(g'_{ij} | g_{ij}, \alpha_{ij})$ are
 252 defined as shown in [Table 1](#) and [Table 3](#), respectively, while under the locus dropout mode in
 253 [Table 2](#) and [Table 4](#), respectively. As a result, [Equation \(17\)](#) takes distinct forms under different
 254 modes of modeling ADOs.

255 For the single ADO mode, [Equation \(17\)](#) is further represented as

$$P(\mathbf{m}_{ij}, c_{ij} | g_{ij}, \Phi) = \begin{cases} P_{0/0} \cdot P(c_{ij} | \alpha_{ij} = 2, t, v) \cdot (1 - \theta) \\ \quad + P_{0/-} \cdot P(c_{ij} | \alpha_{ij} = 1, t, v) \cdot \theta, \text{ if } g_{ij} = 0/0, \\ P_{0/1} \cdot P(c_{ij} | \alpha_{ij} = 2, t, v) \cdot (1 - \theta) \\ \quad + \frac{1}{2}(P_{0/-} + P_{1/-}) \cdot P(c_{ij} | \alpha_{ij} = 1, t, v) \cdot \theta, \text{ if } g_{ij} = 0/1, \\ P_{1/1} \cdot P(c_{ij} | \alpha_{ij} = 2, t, v) \cdot (1 - \theta) \\ \quad + P_{1/-} \cdot P(c_{ij} | \alpha_{ij} = 1, t, v) \cdot \theta, \text{ if } g_{ij} = 1/1, \\ P_{1/1'} \cdot P(c_{ij} | \alpha_{ij} = 2, t, v) \cdot (1 - \theta) \\ \quad + P_{1/-} \cdot P(c_{ij} | \alpha_{ij} = 1, t, v) \cdot \theta, \text{ if } g_{ij} = 1/1', \\ P_{0/-} \cdot P(c_{ij} | \alpha_{ij} = 1, t, v) \cdot (1 - \frac{\theta}{2}) \\ \quad + P \cdot P(c_{ij} | \alpha_{ij} = 0, t, v) \cdot \frac{\theta}{2}, \text{ if } g_{ij} = 0/-, \\ P_{1/-} \cdot P(c_{ij} | \alpha_{ij} = 1, t, v) \cdot (1 - \frac{\theta}{2}) \\ \quad + P \cdot P(c_{ij} | \alpha_{ij} = 0, t, v) \cdot \frac{\theta}{2}, \text{ if } g_{ij} = 1/-, \\ P \cdot P(c_{ij} | \alpha_{ij} = 0, t, v), \text{ if } g_{ij} = -. \end{cases} \quad (18)$$

256 For the locus dropout mode, [Equation \(17\)](#) writes

$$P(\mathbf{m}_{ij}, c_{ij} | g_{ij}, \Phi) = \begin{cases} P_{0/0} \cdot P(c_{ij} | \alpha_{ij} = 2, t, v) \cdot (1 - \theta)^2 \\ \quad + P_{0/-} \cdot P(c_{ij} | \alpha_{ij} = 1, t, v) \cdot 2 \cdot \theta \cdot (1 - \theta) \\ \quad + P_- \cdot P(c_{ij} | \alpha_{ij} = 0, t, v) \cdot \theta^2, \text{ if } g_{ij} = 0/0, \\ P_{0/1} \cdot P(c_{ij} | \alpha_{ij} = 2, t, v) \cdot (1 - \theta)^2 \\ \quad + (P_{0/-} + P_{1/-}) \cdot P(c_{ij} | \alpha_{ij} = 1, t, v) \cdot \theta \cdot (1 - \theta) \\ \quad + P_- \cdot P(c_{ij} | \alpha_{ij} = 0, t, v) \cdot \theta^2, \text{ if } g_{ij} = 0/1, \\ P_{1/1} \cdot P(c_{ij} | \alpha_{ij} = 2, t, v) \cdot (1 - \theta)^2 \\ \quad + P_{1/-} \cdot P(c_{ij} | \alpha_{ij} = 1, t, v) \cdot 2 \cdot \theta \cdot (1 - \theta) \\ \quad + P_- \cdot P(c_{ij} | \alpha_{ij} = 0, t, v) \cdot \theta^2, \text{ if } g_{ij} = 1/1, \\ P_{1/1'} \cdot P(c_{ij} | \alpha_{ij} = 2, t, v) \cdot (1 - \theta)^2 \\ \quad + P_{1/-} \cdot P(c_{ij} | \alpha_{ij} = 1, t, v) \cdot 2 \cdot \theta \cdot (1 - \theta) \\ \quad + P_- \cdot P(c_{ij} | \alpha_{ij} = 0, t, v) \cdot \theta^2, \text{ if } g_{ij} = 1/1', \\ P_{0/-} \cdot P(c_{ij} | \alpha_{ij} = 1, t, v) \cdot (1 - \theta) \\ \quad + P_- \cdot P(c_{ij} | \alpha_{ij} = 0, t, v) \cdot \theta, \text{ if } g_{ij} = 0/-, \\ P_{1/-} \cdot P(c_{ij} | \alpha_{ij} = 1, t, v) \cdot (1 - \theta) \\ \quad + P_- \cdot P(c_{ij} | \alpha_{ij} = 0, t, v) \cdot \theta, \text{ if } g_{ij} = 1/-, \\ P_- \cdot P(c_{ij} | \alpha_{ij} = 0, t, v), \text{ if } g_{ij} = -. \end{cases} \quad (19)$$

257 [Equation \(16\)](#) is computed efficiently using the Felsenstein's pruning algorithm [\[65\]](#). For
258 I candidate SNV sites, J cells and K genotype states in G (for DelSIEVE $K = 7$), the time
259 complexity of the Felsenstein's pruning algorithm is $\mathcal{O}(IJK^2)$.

260 Since in the second component of [Equation \(15\)](#), C_i corresponds to the likelihood of candidate
261 SNV site i being invariant, it is computed as the joint probability of \mathcal{D}_i and $\mathbf{g}_i^{(L)} = 0/0$, writing

$$\begin{aligned} C_i &= P\left(\mathcal{D}_i^{(1)}, \mathbf{g}_i^{(L)} = 0/0 \mid \Theta, \Phi\right) \\ &= P\left(\mathcal{D}_i^{(1)} \mid \mathbf{g}_i^{(L)} = 0/0, \Phi\right) \sum_{\mathbf{g}_i^{(A)} \setminus \{g_{i(2J)}\}} P\left(\mathbf{g}_i^{(L)} = 0/0, \mathbf{g}_i^{(A)} \setminus \{g_{i(2J)}\} \mid \Theta\right) \\ &= \prod_{j=1}^J P(\mathbf{m}_{ij}, c_{ij} | g_{ij} = 0/0, \Phi) \sum_{\mathbf{g}_i^{(A)} \setminus \{g_{i(2J)}\}} P\left(\mathbf{g}_i^{(L)} = 0/0, \mathbf{g}_i^{(A)} \setminus \{g_{i(2J)}\} \mid \Theta\right), \end{aligned} \quad (20)$$

262 which is computed similarly to [Equation \(16\)](#), but with g_{ij} for $j = 1, \dots, J$ fixed to 0/0. In fact,
 263 C_i and $\log P(\mathcal{D}_i^{(1)} | \Theta, \Phi)$ are computed simultaneously in the implementation for optimized
 264 efficiency.

265 To efficiently compute $\log \mathcal{L}^{(2)}$, the background likelihood in [Equation \(14\)](#), we make sev-
 266 eral simplifications similar to SIEVE. Specifically, we assume that each cell at each background
 267 site has the wildtype genotype with both alleles covered during scWGA. We also assume that
 268 $P(c_{ij} | \alpha_{ij}, t, v) = 1$ and $P(\mathbf{g}_i^{(L)} = 0/0, \mathbf{g}_i^{(A)} \setminus \{g_{i(2J)}\} | \Theta) = 1$, thereby ignoring the model of
 269 sequencing coverage and the tree log-likelihood for the background sites i for $i = 1, \dots, I'$. With
 270 an alternative form of the Dirichlet-multinomial distribution, $\log \mathcal{L}^{(2)}$ is approximately and effi-
 271 ciently computed by

$$\begin{aligned}
 \log \mathcal{L}^{(2)}(f, w_1) &= \sum_{i=1}^{I'} \sum_{j=1}^J \log P_{0/0} \\
 &= \sum_{i=1}^{I'} \sum_{j=1}^J \log \left[\frac{\Gamma(w_1) \Gamma(c_{ij} + 1)}{\Gamma(c_{ij} + w_1)} \prod_{k=1}^3 \frac{\Gamma(m_{ijk} + \frac{1}{3}fw_1)}{\Gamma(\frac{1}{3}fw_1) \Gamma(m_{ijk} + 1)} \right. \\
 &\quad \times \left. \frac{\Gamma(c_{ij} - \sum_{k=1}^3 m_{ijk} + (1-f)w_1)}{\Gamma((1-f)w_1) \Gamma(c_{ij} - \sum_{k=1}^3 m_{ijk} + 1)} \right] \\
 &= I' J \left[\log \Gamma(w_1) - 3 \log \Gamma\left(\frac{1}{3}fw_1\right) - \log \Gamma((1-f)w_1) \right] \\
 &\quad + \sum_{c=1}^{\max(c_{ij})} N_c (\log \Gamma(c+1) - \log \Gamma(c+w_1)) \\
 &\quad + \sum_{k=1}^3 \sum_{m_k=1}^{\max(m_{ijk})} N_{m_k} \left(\log \Gamma\left(m_k + \frac{1}{3}fw_1\right) - \log \Gamma(m_k + 1) \right) \\
 &\quad + \sum_{c=\sum_{k=1}^3 m_k=1}^{\max(c_{ij} - \sum_{k=1}^3 m_{ijk})} N_{c-\sum_{k=1}^3 m_k} \left(\log \Gamma\left(c - \sum_{k=1}^3 m_k + (1-f)w_1\right) \right. \\
 &\quad \quad \quad \left. - \log \Gamma\left(c - \sum_{k=1}^3 m_k + 1\right) \right), \tag{21}
 \end{aligned}$$

272 where $P_{0/0}$ is defined in [Equation \(12\)](#). Across I' background sites and J cells, N_c , N_{m_k} for $k =$
 273 1, 2, 3, and $N_{c-\sum_{k=1}^3 m_k}$ represent the unique occurrences of sequencing coverage c , of alternative
 274 nucleotide read counts m_k for $k = 1, 2, 3$, and of reference nucleotide read counts $c - \sum_{k=1}^3 m_k$,
 275 respectively. Some terms, namely $\log \Gamma(c+1)$, $-\log \Gamma(m_k+1)$ for $k = 1, 2, 3$, and $-\log \Gamma(c -$
 276 $\sum_{k=1}^3 m_k + 1)$, are constants, and thus they are not updated in the MCMC iterations.

277 The time complexity of [Equation \(21\)](#) is $\mathcal{O}(c)$, where c is the number of unique values in
 278 the set of values representing sequencing coverage and read counts for all four nucleotides across

279 I' background sites and J cells. Since generally $IJK^2 \gg c$, the overall time complexity of
280 model likelihood is $\mathcal{O}(IJK^2)$. It is worth noting that given I candidate variant sites and J cells,
281 the time complexity of DelSIEVE is around 1.8 times greater than that of SIEVE due to the
282 expanded genotype state space.

283 **Priors**

284 Similar to SIEVE, we use prior distributions predefined and implemented in BEAST 2 for hidden
285 random variables in the DelSIEVE model. For the cell phylogeny given by \mathcal{T} and β , we set a prior
286 following the Kingman coalescent process with an exponentially growing population, denoted

$$P(\mathcal{T}, \beta | M, e), \quad (22)$$

287 where M and e are hidden random variables, representing the scaled population size and the
288 exponential growth rate, respectively. The analytical form of Equation (22) is defined at length
289 in [66].

290 The default prior for M in BEAST 2 is

$$P(M | \delta) = \frac{1}{\delta}, \quad (23)$$

291 where δ is the current proposed value of M .

292 As for e , the default prior is

$$e | \lambda, \epsilon \sim \text{Laplace}(\lambda, \epsilon), \quad (24)$$

293 where the default values of the fixed parameters are mean $\lambda = 10^{-3}$ and scale $\epsilon = 30.7$.

294 For η in Equation (2), an exponential prior distribution is chosen:

$$\eta | \gamma \sim \exp(\gamma), \quad (25)$$

295 where $\gamma = 1$.

296 For the relative deletion rate d in Equation (1), a uniform prior distribution is used:

$$d | \varphi \sim \text{Uniform}(0, \varphi), \quad (26)$$

297 where $\varphi = 1$.

298 For the hidden random variables in the model of sequencing coverage in [Equations \(4\) to \(6\)](#),
299 a weak prior is set for t :

$$t | \rho \sim \text{Uniform}(0, \rho), \quad (27)$$

300 where $\rho = 1000$, while the prior for v is

$$v | \zeta \sim \exp(\zeta), \quad (28)$$

301 where $\zeta = 25$.

302 For the ADO rate θ defined either under the single ADO ([Table 1](#)) or under the locus dropout
303 mode ([Table 2](#)), we use an uninformative prior:

$$\theta | u \sim \text{Uniform}(0, u), \quad (29)$$

304 where $u = 1$.

305 Regarding the hidden random variables in the model of nucleotide read counts in [Equa-](#)
306 [tions \(8\), \(10\) and \(11\)](#), an exponential prior is set for f :

$$f | \tau \sim \exp(\tau), \quad (30)$$

307 where $\tau = 0.025$, and a log normal prior for both w_1 and w_2 :

$$\begin{aligned} w_1 | \xi_1, \psi_1 &\sim \text{Log-Normal}(\xi_1, \psi_1), \\ w_2 | \xi_2, \psi_2 &\sim \text{Log-Normal}(\xi_2, \psi_2), \end{aligned} \quad (31)$$

where we choose for w_1 the log-transformed mean $\xi_1 = 3.9$ (150 for untransformed) and the standard deviation $\psi_1 = 1.5$, and for w_2 the log-transformed mean $\xi_2 = 0.9$ (10 for untransformed) and the standard deviation $\psi_2 = 1.7$. The mean is log-transformed using

$$\xi_{\text{transformed}} = \log(\xi_{\text{untransformed}}) - \frac{\psi^2}{2}.$$

308 These values of the fixed parameters in [Equation \(31\)](#) are chosen to cover a wide range of possible
309 values for w_1 and w_2 .

310 **Posterior and MCMC**

311 The posterior distribution of the hidden random variables writes

$$\begin{aligned}
 & P\left(\mathcal{T}, \boldsymbol{\beta}, M, e, \eta, d, t, v, \theta, f, w_1, w_2 \mid \mathcal{D}^{(1)}, \mathcal{D}^{(2)}\right) \\
 & = \frac{1}{Z} P\left(\mathcal{D}^{(1)}, \mathcal{D}^{(2)} \mid \mathcal{T}, \boldsymbol{\beta}, Q, \eta, t, v, \theta, f, w_1, w_2\right) \\
 & \quad \times P(\mathcal{T}, \boldsymbol{\beta} \mid M, e) P(M \mid \delta) P(e \mid \lambda, \epsilon) \\
 & \quad \times P(\eta \mid \gamma) P(Q \mid d) P(d \mid \varphi) \\
 & \quad \times P(t \mid \rho) P(v \mid \zeta) P(\theta \mid u) P(f \mid \tau) \\
 & \quad \times P(w_1 \mid \xi_1, \psi_1) P(w_2 \mid \xi_2, \psi_2),
 \end{aligned} \tag{32}$$

312 where $Z = P(\mathcal{D}^{(1)}, \mathcal{D}^{(2)})$ is a normalization constant, and the likelihood of the model and priors
 313 for hidden random variables are defined in Section [DelSIEVE likelihood](#) and Section [Priors](#),
 314 respectively. To simplify the notation, we denote the hidden random variables in [Equation \(32\)](#)
 315 as $\Lambda = \{\mathcal{T}, \boldsymbol{\beta}, M, e, \eta, d, t, v, \theta, f, w_1, w_2\}$.

316 Since Z in [Equation \(32\)](#) is intractable to calculate, we employ the MCMC algorithm with
 317 Metropolis-Hastings kernel to sample from the posterior distribution. In this algorithm, a new
 318 state of the hidden random variables Λ^* is proposed based on its current state Λ following a
 319 proposal distribution $q(\Lambda^* \mid \Lambda)$. $q(\Lambda^* \mid \Lambda)$ is designed to ensure the reversibility and ergodicity
 320 of the underlying Markov chain. For DelSIEVE, in each iteration, a new state of a randomly
 321 selected hidden variable is accepted with probability

$$\min \left\{ 1, \frac{P\left(\Lambda^* \mid \mathcal{D}^{(1)}, \mathcal{D}^{(2)}\right) q(\Lambda \mid \Lambda^*)}{P\left(\Lambda \mid \mathcal{D}^{(1)}, \mathcal{D}^{(2)}\right) q(\Lambda^* \mid \Lambda)} \right\}. \tag{33}$$

322 We employ exactly the same proposal distributions as we used in SIEVE, which are defined
 323 in BEAST 2. Briefly, regarding the branch lengths of the tree, the heights of the internal nodes
 324 are adjusted. For the tree topology, we use multiple moves, including subtree swapping, Wilson-
 325 Balding, and subtree sliding, where the last two moves also change branch lengths as a side
 326 effect. With respect to unknown parameters, scaling and random Gaussian walks are used. For
 327 detailed description of the aforementioned moves, refer to Drummond et al. [66] and Kang et
 328 al. [55].

329 To achieve accurate parameter and tree estimates, DelSIEVE employs a two stage sampling
 330 strategy, similarly to SIEVE.

331 **Variant calling, ADO calling and maximum likelihood gene annotation**

332 In the efficient computation of model likelihood using [Equations \(16\)](#) and [\(17\)](#), we marginal-
333 ize out some hidden random variables: $\mathbf{g}_i^{(L)}$, $\mathbf{g}_i^{(A)}$, g'_{ij} and α_{ij} . Hence, the direct results from
334 the MCMC sampling process are the posterior distributions of cell phylogeny and other un-
335 known hidden random variables. We obtain the estimates of those marginalized hidden random
336 variables as a post processing step, similarly to SIEVE. Specifically, we use the max-sum al-
337 gorithm [67], by fixing the maximum clade credibility tree [68] and parameters estimated from
338 the MCMC posterior samples. As a result, the variants, ADO states, as well as the locations
339 of mutated genes on the inferred cell phylogeny are determined by identifying the maximum
340 likelihood states of $\mathbf{g}_i^{(L)}$, g'_{ij} and α_{ij} , as well as $\mathbf{g}_i^{(A)}$, respectively.

341 **Mutation event classification**

342 DelSIEVE is able to discern 28 types of genotype transitions, which are classified into 17 types of
343 mutation events ([Table 5](#)). Each genotype transition is a combinatorial result of single mutations,
344 single back mutations and single deletions. Single mutations happen when 0 mutates to 1, or
345 1 and 1' mutate to each other. Single back mutations occur when 1 or 1' mutates to 0. Single
346 deletions happen when an existing allele is lost during evolution, namely 0 or 1 deleted.

347 Since DelSIEVE encompasses the genotype state space modeled by SIEVE, it is capable of
348 discerning all genotype transitions that SIEVE can handle, namely the first 12 rows in [Table 5](#)
349 (for detailed explanation see Kang et al. [55]). Those mutation events that only DelSIEVE is
350 able to discern are explained as follows.

351 The single deletion which is not loss of heterozygosity (LOH; related to genotype transitions
352 $0/0 \rightarrow 0/-$ and $1/1 \rightarrow 1/-$) takes place when one allele is deleted from genotypes in which
353 both alleles originally contained the same nucleotide, while the single deletion which is LOH
354 ($0/1 \rightarrow 0/-$, $0/1 \rightarrow 1/-$ and $1/1' \rightarrow 1/-$) happens when one allele is deleted from genotypes in
355 which both alleles originally had different nucleotides. The coincident deletion and mutation
356 ($0/0 \rightarrow 1/-$) refers to the case when one allele is deleted, and the other is mutated of the
357 wildtype, while the coincident deletion and back mutation ($1/1 \rightarrow 0/-$ and $1/1' \rightarrow 0/-$) happens
358 when one allele is deleted, and the other is mutated back to the reference nucleotide. The
359 single deletion mutation addition ($0/- \rightarrow 1/-$) takes place when the only allele of the reference-
360 left single deletion genotype is mutated to an alternative nucleotide, while the single deletion
361 back mutation addition happens when the mutated allele of the alternative-left single deletion

Table 5: 28 types of genotype transitions that DelSIEVE is able to identify, with their interpretation as mutation events. The genotype transitions correspond to possible changes of genotypes on a branch from the parent node to the child node. If any of these events occurs on independent branches of the phylogenetic tree, it is also considered as a parallel evolution event. The first 12 genotype transitions are also identifiable with SIEVE. LOH in the table represents loss of heterozygosity.

Genotype transition	Mutation event	Identifiable solely by DelSIEVE
$0/0 \rightarrow 0/1$	Single mutation	No
$0/0 \rightarrow 1/1$	Coincident homozygous double mutation	No
$0/0 \rightarrow 1/1'$	Coincident heterozygous double mutation	No
$0/1 \rightarrow 0/0$	Single back mutation	No
$1/1 \rightarrow 0/1$	Single back mutation	No
$1/1' \rightarrow 0/1$	Single back mutation	No
$1/1 \rightarrow 0/0$	Coincident double back mutation	No
$1/1' \rightarrow 0/0$	Coincident double back mutation	No
$0/1 \rightarrow 1/1$	Homozygous single mutation addition	No
$0/1 \rightarrow 1/1'$	Heterozygous single mutation addition	No
$1/1' \rightarrow 1/1$	Homozygous substitute single mutation	No
$1/1 \rightarrow 1/1'$	Heterozygous substitute single mutation	No
$0/0 \rightarrow 0/-$	Single deletion (not LOH)	Yes
$1/1 \rightarrow 1/-$	Single deletion (not LOH)	Yes
$0/1 \rightarrow 0/-$	Single deletion (LOH)	Yes
$0/1 \rightarrow 1/-$	Single deletion (LOH)	Yes
$1/1' \rightarrow 1/-$	Single deletion (LOH)	Yes
$0/0 \rightarrow 1/-$	Coincident deletion and mutation	Yes
$1/1 \rightarrow 0/-$	Coincident deletion and back mutation	Yes
$1/1' \rightarrow 0/-$	Coincident deletion and back mutation	Yes
$0/- \rightarrow 1/-$	Single deletion mutation addition	Yes
$1/- \rightarrow 0/-$	Single deletion back mutation addition	Yes
$0/- \rightarrow -$	Single deletion addition	Yes
$1/- \rightarrow -$	Single deletion addition	Yes
$0/0 \rightarrow -$	Coincident double deletion	Yes
$0/1 \rightarrow -$	Coincident double deletion	Yes
$1/1 \rightarrow -$	Coincident double deletion	Yes
$1/1' \rightarrow -$	Coincident double deletion	Yes

362 genotype is mutated back to the reference nucleotide. The single deletion addition ($0/- \rightarrow -$ and
 363 $1/- \rightarrow -$) refers to the case when the only allele is deleted of the reference- and alternative-left
 364 single deletion genotypes. Finally, for the coincident double deletion ($0/0 \rightarrow -$, $0/1 \rightarrow -$, $1/1 \rightarrow -$
 365 and $1/1' \rightarrow -$) both of the alleles existing before are deleted.

366 ScDNA-seq data simulator

367 We generated simulated data by modifying the simulator we had used in SIEVE. The first
 368 change we made was to expand the rate matrix, according to which each genomic site evolved

369 along the tree ([Additional file 1: Table S1](#)). The rate matrix contains 14 genotypes encoded
370 with nucleotides, allowing for mutations, back mutations, and deletions. It has one parameter,
371 deletion rate, which is measured relatively to the mutation rate. Another change was that we
372 implemented the locus dropout mode to allow more than one ADO to occur at each site for each
373 cell. The simulator takes the same input configuration as SIEVE does.

374 The simulation process was similar to that in SIEVE. Briefly, with a given number of cells,
375 a binary cell lineage tree was first simulated following the coalescent process under the strict
376 molecular clock. For a given number of genomic sites, each site was initialized by randomly
377 selecting one of four nucleotides to have a reference genotype. Next, with a given mutation rate
378 and a relative deletion rate, each site was evolved independently along the tree following the
379 rate matrix defined in [Additional file 1: Table S1](#). A genomic site is considered as a true SNV
380 site if at least one cell has a genotype that is not wildtype. ADOs were then added on top
381 of the simulated genotypes under either single ADO or locus dropout mode, as long as there
382 were existing alleles. We recorded the true ADO states for all cells at the true SNV sites. Size
383 factors in [Equation \(7\)](#) were generated from a normal distribution with the mean = 1.2 and the
384 variance = 0.2. The sequencing coverage was simulated using a negative binomial distribution
385 following [Equations \(4\) to \(6\)](#). The read counts of each nucleotide were then generated following
386 a multinomial distribution.

387 **Simulation design**

388 We designed a series of simulations to benchmark the performance of DelSIEVE. We reused and
389 modified the benchmarking framework in SIEVE.

390 We assumed that 40 tumor cells were sampled from an exponentially growing population,
391 whose growth rate and effective population size are 10^{-4} and 10^4 , respectively. We used the
392 same mutation rates as in SIEVE, namely 10^{-6} , 8×10^{-6} and 3×10^{-5} . We selected two levels
393 of deletion rate relative to the mutation rate: 0.1 and 0.25.

394 For each mutation rate, we chose such number of genomic sites that DataFilter would produce
395 a certain amount of candidate variant sites or background sites. For mutation rate 10^{-6} , we
396 evolved 10^4 genomic sites to have around $400 \sim 700$ candidate variant sites. For mutation rate
397 8×10^{-6} , 10^4 genomic sites were chosen to have around 4×10^3 background sites. For mutation
398 rate 3×10^{-5} , 1.2×10^5 genomic sites were chosen to have at least 2.5×10^3 background sites.
399 For the higher mutation rates of 8×10^{-6} and 3×10^{-5} , the chosen numbers of genomic sites

400 resulted in $> 5 \times 10^3$ and $> 1.1 \times 10^5$ true SNV sites, respectively. Due to the consideration of
401 runtime efficiency, they were subsetted before piping to downstream methods.

To this end, we first computed a targeted number of true SNV sites n_{target} using

$$n_{\text{target}} = \min(700, \frac{n'}{5}),$$

402 where n' is the number of background sites. Next, we randomly selected n_{target} sites out of
403 the true SNV sites. Together with the n' background sites, the selected n_{target} true SNV sites
404 formed the new simulated data. This ensured that the number of true SNV sites in the final
405 simulated data for different mutation rates were within the same range, and the ratio between
406 the number of background sites and the true SNV sites was at least 5 for mutation rates being
407 8×10^{-6} and 3×10^{-5} .

408 We considered both single ADO and locus dropout mode. The ADO rate for the former was
409 $\theta = 0.163$, and for the latter $\theta = 0.3$.

410 Similar to SIEVE, we had different combinations of t and v in Equations (4) to (6) for various
411 coverage qualities. For simulated data referred to as high coverage quality, we used high mean
412 ($t = 20$) and low variance ($v = 2$) of allelic coverage. For medium coverage quality data, we
413 used high mean ($t = 20$) and medium variance ($v = 10$). For low coverage quality data, we fixed
414 low mean ($t = 5$) and high variance ($v = 20$).

415 Other parameters were fixed when simulating the data. We set w_1 and w_2 in Equation (11)
416 to 100 and 2.5, respectively. Moreover, we set both the amplification and sequencing error rate
417 to 10^{-3} , and thus the effective sequencing error rate in Equation (10) was $f \approx 2 \times 10^{-3}$.

418 Overall, we designed 36 simulation scenarios, each repeated 10 times.

419 Furthermore, for each of those genotypes related to somatic deletions, we filtered out results
420 if the proportion of simulated ground truth was less than 0.1%. We also excluded results from
421 mutation rate being 10^{-6} as too few somatic deletions were generated (less than 0.3%, 0.7%
422 and 0.005% for alternative-left single deletion, reference-left single deletion and double deletion,
423 respectively). For the same reason, results were also excluded from double deletion for mutation
424 rate being 8×10^{-6} (less than 0.2% generated).

425 For double mutant genotype, we excluded results when mutation rate was 10^{-6} as less than
426 0.2% of such genotype was generated.

427 Measurement of the quality of variant calling and cell phylogeny accuracy

428 For assessing the results of variant and ADO calling, standard performance measures such
429 as precision, recall, F1 score, and false positive rate (FPR) were used. DelSIEVE, SIEVE,
430 SCIPhIN and Monovar were evaluated using these measures in the task of single and double
431 mutant genotype calling.

432 Both DelSIEVE and SCIPhIN identify somatic deletions at preselected candidate sites.
433 Hence, we subsetted the true somatic deletions to those at the candidate variant sites when
434 computing the metrics. This barely influenced the recall and F1 score for alternative-left single
435 deletion, as majority of the sites containing such genotype were captured in the selection of the
436 candidate variant sites. For reference-left single deletion and double deletion genotype, however,
437 restricting to candidate sites would inevitably decrease recall and F1 score, as sites having solely
438 those genotypes would be missed in the preselection.

439 To assess the accuracy of cell phylogeny reconstruction, we used the same measurements as
440 in SIEVE, namely the BS distance [69] for both the tree topology and branch lengths, as well as
441 the normalized RF distance [70] for the tree topology only (see Kang *et al.* [55]). For DelSIEVE,
442 SIEVE and SiFit, we computed both the BS and the normalized RF distance in the rooted tree
443 mode. For SCIPhIN, we only computed the normalized RF distance as it only infers a rooted
444 tree without branch lengths. We used R package phangorn to compute BS and normalized RF
445 distance [71].

446 Configurations of methods

447 For Monovar (commit 68fbb68), we used the true values of θ and f as priors for false negative
448 rate and false positive rate and default values for other options.

449 For SCIPhIN (commit 27e5ca6), we gave it the true value of f to avoid estimating its mean
450 error rate (option "wildMean"), and ran it with 10^6 iterations with zygosity learned (option "lz"
451 set to 1). We also set the penalty of computing the loss (option "llp") and parallel score (option
452 "lpp") to 30. The command line is as follows:

```
453 sciphin -l 1000000 --lz 1 --ll 1 --lp 1 --llp 30 --lpp 30 --ese 0 \
454 --wildMean 0.002
```

455 To run SiFit (commit 9dc3774), we fed the required data with variants called by Monovar
456 as a ternary matrix. We used the true values of θ and f as the prior for false negative rate and

457 the estimated false positive rate, respectively. We ran it with 2×10^5 iterations.

458 For SIEVE, originally it only supported single ADO mode. In this contribution, we additionally equipped it with the locus dropout mode, which is now available along with DelSIEVE.

460 On the simulated data, we configured a strict molecular clock model for DelSIEVE and
461 SIEVE, both of which was then run for 2×10^6 and 1.5×10^6 iterations for the first and
462 the second sampling stages, respectively. The deletion rate was also inferred in the second
463 sampling stage as it is related to the branch lengths of the cell phylogeny. Both DelSIEVE and
464 SIEVE were configured to match the ADO type employed during the simulation process. This
465 ensured consistency between the simulation and analysis, allowing for accurate comparisons and
466 evaluations of the methods' performance.

467 On the real datasets, we instead used a log-normal relaxed molecular clock model to account
468 for branch-wise substitution rate variation for DelSIEVE. To obtain better mixed Markov chains,
469 we used an optimized relaxed clock model [72] rather than the default one in BEAST 2. We
470 increased the number of iterations for both stages to 4×10^6 and 3.5×10^6 , respectively. Both
471 the deletion rate and parameters introduced by the relaxed molecular clock model were explored
472 in the second sampling stage. To reduce the uncertainties introduced by the model, DelSIEVE
473 was run in single ADO mode.

474 To run Sequenza on the real datasets, we used the bam2seqz command in the sequenza-utils
475 package to convert bam files for normal and tumor cells to the Sequenza file format, which was
476 subsequently binned with the seqz-binning command, using a window size of 50. With this file
477 as input, we used the sequneza.fit command from Sequenza v3.0.0 to estimate the ploidy.

478 The SNVs were annotated using Annovar (version 2020 Jun. 08) [73]. The cell phylogeny was
479 plotted in R (version 4.2.3) [74] using ggtree [75], and the genotype heatmap was plotted using
480 ComplexHeatmap [76]. Besides, the comparison of sequencing coverages reported by DelSIEVE
481 and Sequenza was performed and plotted using ggstatsplot [77].

482 Results

483 DelSIEVE accurately called somatic deletions

484 First, we used simulated data to benchmark one of DelSIEVE's asset functionalities, namely
485 calling somatic deletions (Methods; Section [Simulation design](#)). DelSIEVE's performance was
486 benchmarked against SCIPhIN [62] ([Figure 2](#), [Additional file 1: Figure S1, S2](#)). Here, SCIPhIN

487 was given an advantage by fixing its mean error rate to the true effective sequencing error rate
488 used in the simulation. DelSIEVE and SCIPhIN were evaluated in the task of calling alternative-
489 and reference-left deletions, while only DelSIEVE was evaluated in the task of calling double
490 deletion genotype, as it is the only method to call such genotype.

491 For calling alternative- and reference-left single deletion, DelSIEVE overall outperformed
492 SCIPhIN, regardless of the type of ADOs (single or locus dropout) used in the simulated data
493 (Figure 2a, b, Additional file 1: Figure S1a-d, Additional file 1: Figure S2a, b). When the
494 data was of medium or high coverage quality (with high mean and low or medium variance
495 of coverage), DelSIEVE achieved F1 scores with medians ≥ 0.87 and ≥ 0.76 for alternative-
496 and reference-left single deletions, respectively (Figure 2a, b). In contrast, SCIPhIN had F1
497 scores with medians ≤ 0.28 for alternative-left single deletion and ≤ 0.01 for reference-left single
498 deletion. The related recall (Additional file 1: Figure S1a, c) and precision (Additional file
499 1: Figure S1b, d) also showed DelSIEVE's superiority. In particular, the high precision (≈ 1)
500 and negligible FPR (≈ 0 , see Additional file 1: Figure S2a, b) of DelSIEVE indicate its high
501 reliability in calling alternative- and reference-left single deletion genotypes.

502 When the data was of low coverage quality (low mean and high variance of coverage), the
503 medians of F1 scores of DelSIEVE dropped to ≥ 0.55 and ≥ 0.29 for calling alternative- and
504 reference-left single deletion genotypes, respectively, but still largely exceeded those of SCIPhIN
505 (Figure 2a, b). The low quality of the data seemed to affect more the performance of DelSIEVE
506 in calling reference-left single deletion compared to that in calling alternative-left single deletion
507 (Additional file 1: Figure S1a-d). This was expected since such low coverage provided very little
508 information for calling reference-left single deletion. Furthermore, the FPR of DelSIEVE was
509 still ≈ 0 for the low quality data.

510 We observed that the performance of DelSIEVE only slightly decreased when applied to
511 data simulated under locus dropout mode, in comparison to the results obtained when it was
512 applied to data simulated under single ADO mode. Given that DelSIEVE explicitly modeled the
513 sequencing coverage, it was anticipated that data simulated under locus dropout mode would
514 introduce additional uncertainties to the model.

515 DelSIEVE was the only method designed for explicitly calling double deletion genotype.
516 Overall, in evaluation on simulated data, DelSIEVE obtained high medians of F1 scores ≥ 0.75
517 (Figure 2c). Its performance decreased as the relative deletion rate increased or the coverage
518 quality of the data decreased (Figure 2c, Additional file 1: Figure S1e, f), but the FPR kept at

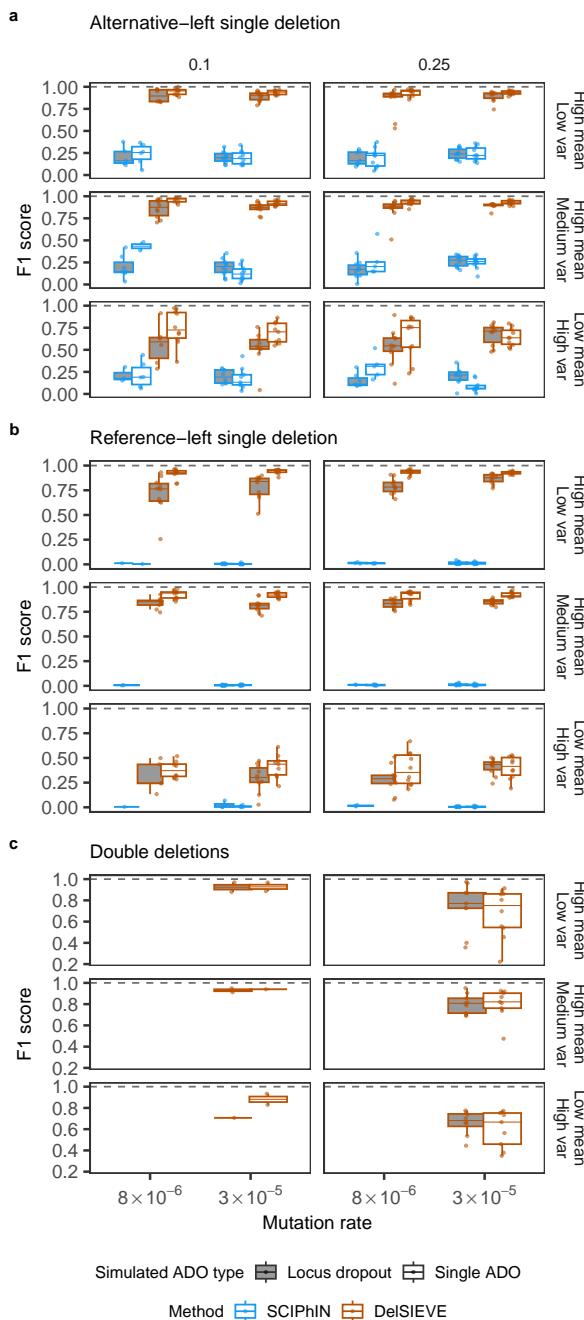


Figure 2: F1 score for the benchmark of calling somatic deletions. Varying are the mutation rate (the horizontal axis), the relative deletion rate (the vertical strip), the coverage quality (the horizontal strip) and the simulated ADO type (the shaded or blank boxes). Each simulation is repeated $n = 10$ times with each repetition denoted by colored dots. The gray dashed lines represent the optimal values of each metric. Box plots comprise medians, boxes covering the interquartile range (IQR), and whiskers extending to 1.5 times the IQR below and above the box. Data points were removed if the proportion of simulated ground truth was less than 0.1%. **a-c**, Box plots of the F1 score for calling alternative-left single deletion (**a**), reference-left single deletion (**b**), and double deletion (**c**). The results in **c** when mutation rate was 8×10^{-6} were omitted as very few double deletion were generated (less than 0.2%; see Section [Simulation design](#)).

519 a negligible level (≈ 0 ; see [Additional file 1: Figure S2c](#)).

520 **DelSIEVE showed boosted performance in calling double mutant genotypes**
521 **compared to SIEVE in the presence of somatic deletions.**

522 We next assessed DelSIEVE's performance in calling single and double mutant genotypes against
523 Monovar, SCIPhIN and SIEVE ([Figure 3](#), [Additional file 1: Figure S3, S4](#)). Regarding calling
524 single mutant genotype, DelSIEVE and SIEVE performed comparatively well (minimum median
525 F1 score of 0.9), and outperformed Monovar and SCIPhIN (minimum median F1 score 0.58 and
526 0.6, respectively; see [Figure 3a](#)). As mutation rate increased, the recall of both DelSIEVE and
527 SIEVE slightly increased ([Additional file 1: Figure S3a](#)), while the precision slightly decreased
528 ([Additional file 1: Figure S3b](#)), resulting in relatively constant F1 scores. In contrast, both
529 Monovar and SCIPhIN experienced a decrease in both recall and precision as the mutation
530 rate increased ([Additional file 1: Figure S3a, b](#)). Consequently, their F1 scores declined, with
531 SCIPhIN being more adversely affected compared to Monovar. Moreover, DelSIEVE and SIEVE
532 had comparable recall ([Additional file 1: Figure S3a](#)), while DelSIEVE showed higher precision
533 ([Additional file 1: Figure S3b](#)) and lower FPR ([Additional file 1: Figure S4a](#)) than SIEVE did,
534 especially when the mutation rate was high ($\geq 3 \times 10^{-5}$). We speculate that this might because
535 SIEVE has to model the evident signal of somatic deletions as ADOs on top of single mutant
536 genotype.

537 Additionally, as the mutation rate increased, the FPR of all methods also increased, with
538 SCIPhIN exhibiting the most significant FPR increase ([Additional file 1: Figure S4a](#)). It was
539 noteworthy that, when the mutation rate was high ($\geq 3 \times 10^{-5}$), methods that incorporated cell
540 phylogeny in variant calling, such as DelSIEVE, SIEVE and SCIPhIN, had slightly higher FPR
541 in calling single mutant genotype compared to other methods, such as Monovar ([Additional file](#)
542 [1: Figure S4a](#)). However, this loss was negligible compared to the advantage that SIEVE and
543 DelSIEVE had over Monovar when precision, recall, and F1 were evaluated.

544 In the task of calling double mutant genotypes, SCIPhIN and Monovar obtained minimum
545 median F1 scores 0.04 and 0.21, respectively, while SIEVE and DelSIEVE exhibited much higher
546 performance with minimum median F1 scores 0.65 and 0.93, respectively ([Figure 3b](#)). More
547 specifically, DelSIEVE and SIEVE had comparable recall ([Additional file 1: Figure S3c](#)), but
548 the former reached much higher precision than the latter (minimum medians 0.75 and 0.61,
549 respectively; see [Additional file 1: Figure S3d](#)). Again, this discrepancy in performance could

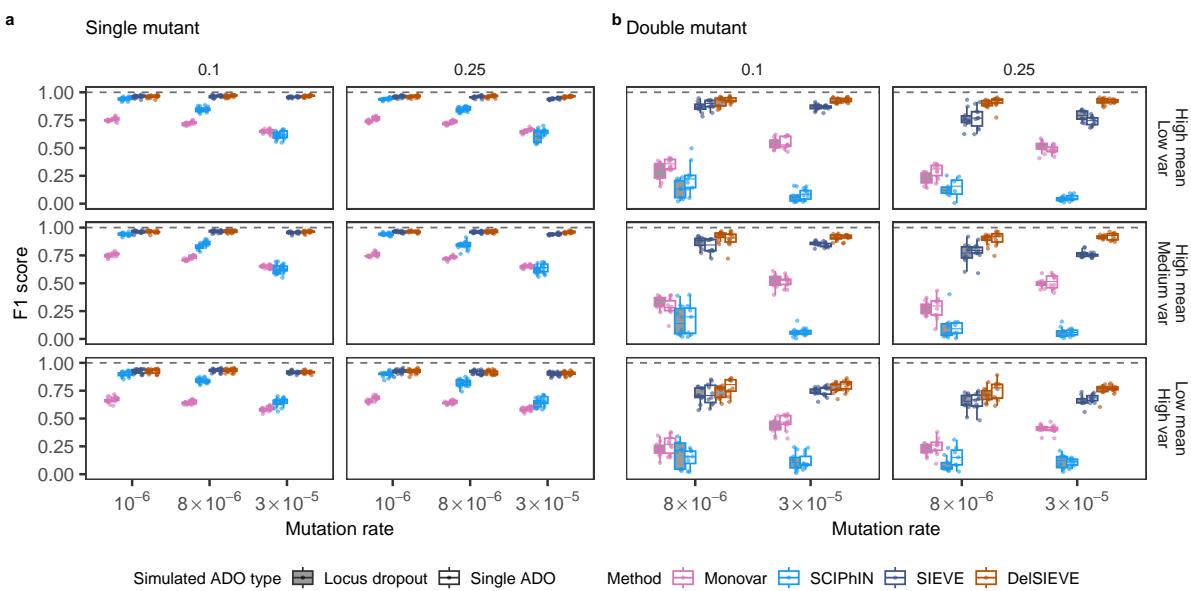


Figure 3: F1 score for the benchmark of calling single and double mutant. Varying are the mutation rate (the horizontal axis), the relative deletion rate (the vertical strip), the coverage quality (the horizontal strip) and the simulated ADO type (the shaded or blank boxes). Each simulation is repeated $n = 10$ times with each repetition denoted by colored dots. The gray dashed lines represent the optimal values of each metric. Box plots comprise medians, boxes covering the interquartile range (IQR), and whiskers extending to 1.5 times the IQR below and above the box. **a-b**, Box plots of the F1 score for calling single mutant (**a**) and double mutant (**b**). The results in **b** for mutation rate was 10^{-6} were omitted as too few double mutant were generated (less than 0.2%; see Section [Simulation design](#)).

550 be due to SIEVE's inclination to explain somatic deletions by modeling them as ADO events
 551 occurring within double mutant genotypes.

552 Besides, DelSIEVE had the lowest FPR (≈ 0) compared to other methods ([Additional file](#)
 553 [1: Figure S4b](#)). These findings highlighted the superior capability of DelSIEVE in accurately
 554 identifying double mutant genotypes in the presence of somatic deletions. On top of that, the
 555 slight advantage of Monovar over methods incorporating phylogeny observed for single mutant
 556 calling was not observed for double mutant calling. In contrast, in this task, Monovar had
 557 significantly elevated FPR compared to all other methods.

558 **DelSIEVE outperformed SIEVE in calling ADOs on data with adequate cov-
 559 erage quality.**

560 We then evaluated DelSIEVE's performance in calling single ADO and locus dropout against
 561 SIEVE ([Figure 4](#), [Additional file 1: Figure S5, S6](#)), which are the only two methods that
 562 can conduct these tasks. Though unsupported originally in SIEVE, locus dropout mode was
 563 implemented by us for the comparison (see Section [Configurations of methods](#)). The ADO

564 type used during the simulation process was taken into consideration when configuring both
 565 DelSIEVE and SIEVE for analysis. As a result, the results of calling single ADO were accessible
 566 for data simulated under both single ADO and locus dropout modes. However, the results of
 567 calling locus dropout were only available for data simulated specifically under the locus dropout
 568 mode.

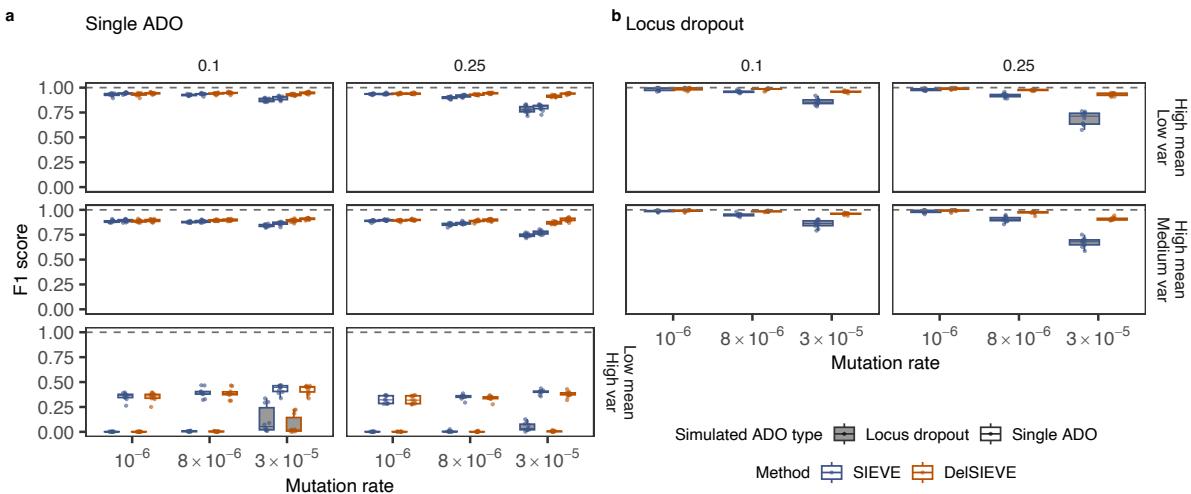


Figure 4: F1 score for the benchmark of calling single ADO and locus dropout. Varying are the mutation rate (the horizontal axis), the relative deletion rate (the vertical strip), the coverage quality (the horizontal strip) and the simulated ADO type (the shaded or blank boxes). Each simulation is repeated $n = 10$ times with each repetition denoted by colored dots. The gray dashed lines represent the optimal values of each metric. Box plots comprise medians, boxes covering the interquartile range (IQR), and whiskers extending to 1.5 times the IQR below and above the box. **a-b**, Box plots of the F1 score for calling single ADO (**a**) and locus dropout (**b**). The F1 score were unavailable in **b** when data was of low coverage quality due to unavailable precision.

569 For calling single ADO, the performance of DelSIEVE and SIEVE were affected by the cov-
 570 erage quality of the data. When the data was of medium or high coverage quality, DelSIEVE
 571 reached a minimum median F1 score 0.9, higher than SIEVE (0.77; see Figure 4a). The per-
 572 formance of DelSIEVE remained consistent regardless of changes in the mutation rate and relative
 573 deletion rate, in contrast to SIEVE. This was anticipated because higher mutation and deletion
 574 rates resulted in an increased number of somatic deletions being generated. DelSIEVE was
 575 capable of differentiating somatic deletions from ADOs by incorporating them into the model.
 576 In contrast, SIEVE wrongly accounted for somatic deletions as ADOs occurring within single
 577 or double mutant genotypes. This behavior of SIEVE reduced the recall and precision, and
 578 increased FPR (Additional file 1: Figure S5a, b, Additional file 1: Figure S6a), similarly to its
 579 inferior performance in calling single and double mutant genotypes compared to DelSIEVE (see
 580 the previous section).

581 The performance of both DelSIEVE and SIEVE in calling single ADO declined when the
582 data had low coverage quality (Figure 4a, Additional file 1: Figure S5a, b, Additional file 1:
583 Figure S6a). This decrease in performance was further exacerbated when the data was simulated
584 under the locus dropout mode, as compared to when it was simulated under the single ADO
585 mode. The decrease in performance can be attributed to two primary factors. Firstly, data
586 of low coverage quality contained more noise compared to that of higher coverage quality. The
587 locus dropouts added even more noise on top of that. Secondly, the more complex model versions
588 operating under the locus dropout mode inherently introduced more uncertainty to the results.

589 For calling locus dropout from data of medium or high coverage quality, DelSIEVE showed
590 a minimum median F1 score of 0.91, higher than SIEVE did (0.68; see Figure 4b). Specifically,
591 DelSIEVE and SIEVE were comparable in terms of recall (Additional file 1: Figure S5c), but the
592 former had a higher precision and lower FPR than the latter as the mutation rate and relative
593 deletion rate increased (Additional file 1: Figure S5d, Additional file 1: Figure S6b). However,
594 when the data was of low coverage quality, both methods reported no locus dropout, resulting
595 in zero recall and FPR as well as unavailable precision and F1 score.

596 Since the quality of the real data resembles more that of low coverage quality, we decided
597 to configure DelSIEVE under the single ADO mode to reduce the amount of uncertainties
598 introduced.

599 **DelSIEVE estimated cell phylogeny with comparable accuracy to SIEVE.**

600 We further benchmarked DelSIEVE's performance in reconstructing the cell phylogeny against
601 SiFit, SCIPhIN and SIEVE (Additional file 1: Figure S7). To account for both tree structure
602 and branch lengths in the evaluation, we used branch score (BS) distance as the metric. The
603 results of SCIPhIN were excluded in the computation of BS score as it only reported the tree
604 structure. Both DelSIEVE and SIEVE outperformed SiFit, showing the advantage of correcting
605 the acquisition bias (Additional file 1: Figure S7a). When the mutation rate was higher (\geq
606 8×10^{-6}), DelSIEVE reported cell phylogenies with longer branch lengths than SIEVE and
607 showed a bit larger BS score. This may be due to the fact that DelSIEVE, as a more complex
608 model, with more considered genotypes, allowed more genotype transitions on the branches.

609 We then used the normalized RF distance as the metric, which only considered the tree
610 structure. The performance of DelSIEVE and SIEVE in tree reconstruction was comparable
611 in estimating the tree structure (maximum medium normalized RF distance 0.29 and 0.28,

612 respectively), and was lower compared to SiFit (maximum median normalized RF distance
613 0.37) and SCIPhIN (0.33; see [Additional file 1: Figure S7b](#)), especially when the mutation rate
614 increased.

615 DelSIEVE reliably identified several somatic deletions in TNBC cells.

616 We applied DelSIEVE to real world scDNA-seq datasets analyzed previously in SIEVE with ex-
617 actly the same input, configuring similarly a relaxed molecular clock model to account for branch-
618 wise rate variation (see Section [Configurations of methods](#)). For scWES dataset TNBC16 [78],
619 DelSIEVE reported a maximum clade credibility (MCC) cell phylogeny with a visually long
620 trunk, supported by high posterior probabilities ([Figure 5](#), [Additional file 1: Figure S8](#)). The
621 cell phylogeny was similar to that reported by SIEVE, with the normalized RF and the BS
622 distances being 0.07 and 3.88×10^{-6} , respectively.

623 DelSIEVE identified the same types of mutation events reported by SIEVE, except for single
624 back mutation. In terms of numbers, DelSIEVE explained the same data with less single muta-
625 tions. Specifically, DelSIEVE identified 31 coincident homozygous double mutations (transitions
626 from 0/0 to 1/1; 44 for SIEVE), eight homozygous single mutation additions (from 0/1 to 1/1;
627 nine for SIEVE) and two parallel single mutations (from 0/0 to 0/1 that occurred more than
628 once in the tree; same for SIEVE). SIEVE identified seven single back mutations (from 0/1 to
629 0/0; *BRD8*, *COL6A5*, *GRB14*, *MYRF*, *RHOJ*, *SEMA3A*, *TMX4*), narrating an evolutionary
630 story of acquiring single mutations in these genes on the trunk of the tree, followed by losing
631 them through single back mutations, resulting in these mutations possessed by only a subgroup
632 of cells (a2, a3, a5 and a7). Reporting the same mutations in the same group of cells, DelSIEVE,
633 however, narrated a more straightforward, parsimonious alternative, where cell a2, a3, a5 and
634 a7 acquired these mutations directly from their most recent common ancestor.

635 In addition, DelSIEVE identified mutation events where somatic deletions were involved,
636 including a large number of 245 coincident deletions and mutations (from 0/0 to 1/-), three
637 single deletions which could be categorized as LOH (from 0/1 to 0/- or 1/-, or from 1/1' to 1/-),
638 ten single deletions which were not LOH (from 0/0 to 0/-, or from 1/1 to 1/-), and finally ten
639 single deletion mutation additions (from 0/- to 1/-). For instance, DelSIEVE inferred that gene
640 *NEK1* and *NEK5*, which had been reported to be related to breast tumors [79], experienced
641 both a deletion and a mutation on the trunk, resulting in all sequenced cells having genotype
642 1/-. Another gene, *LIMCH1*, known to be related to TNBC [80], had an allele deleted first on

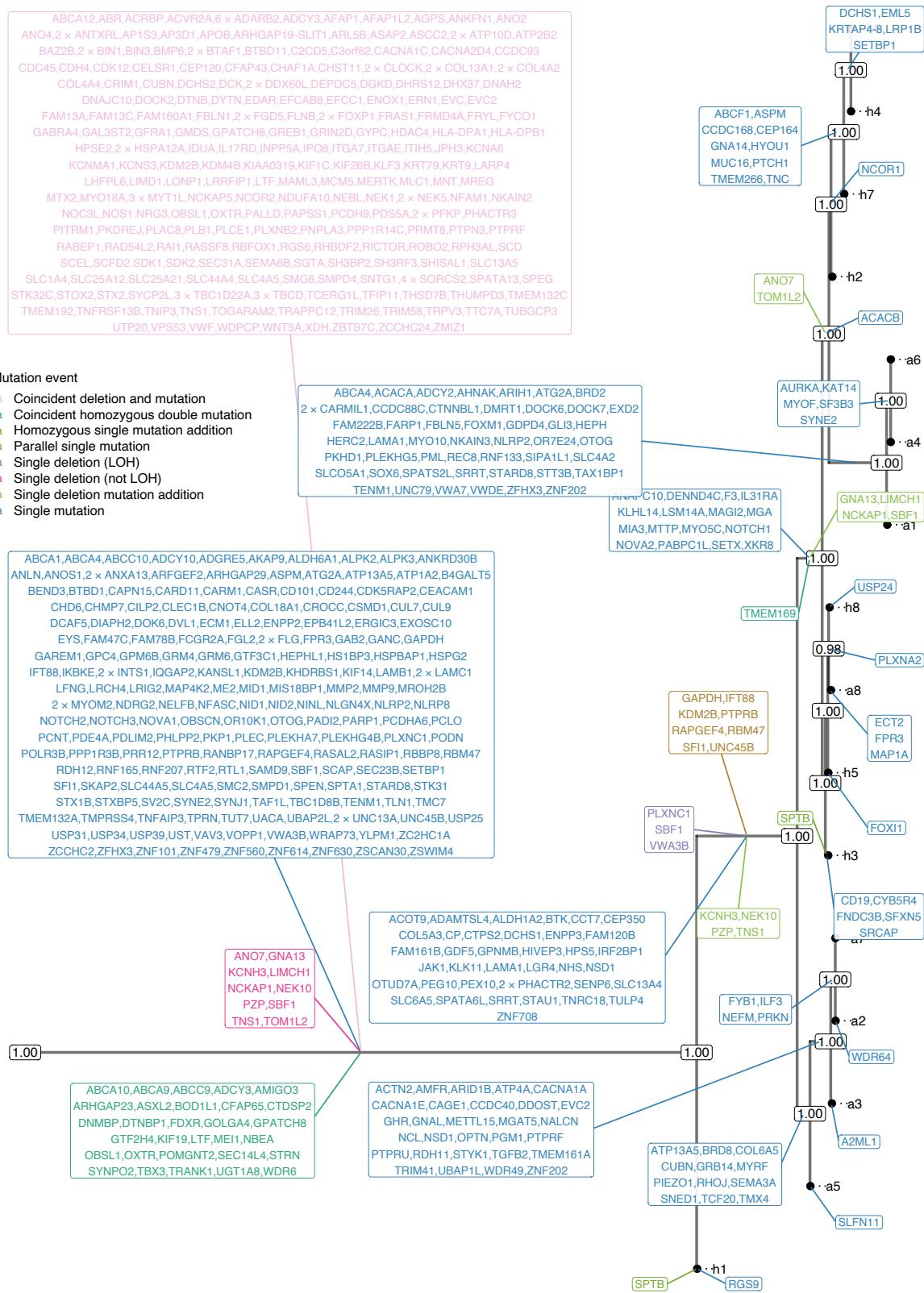


Figure 5: Results of phylogenetic inference for the TNBC16 dataset. Shown is DelSIEVE’s maximum clade credibility tree. Tumor cell names are annotated to the leaves of the tree. The numbers at each node represent the posterior probabilities (threshold $p > 0.5$). At each branch, depicted in different colors are non-synonymous genes that are either TNBC-related single mutations (in blue) or other mutation events (in other colors).

643 the trunk (genotype changed from 0/0 to 0/-), and then the left allele mutated for a subgroup of
644 cells (genotype changed from 0/- to 1/-). The substantial amount of evolutionary events related
645 to deletions highlights the importance of the extended functionality of DelSIEVE as compared
646 to SIEVE.

647 In total, DelSIEVE identified 5,893 variant sites, close to 5,895 variant sites reported by
648 SIEVE (Figure 6). Among the 683 sites inferred by DelSIEVE that contain somatic deletions
649 (mostly 1/-; 11.6% of all variant sites), 377 were previously determined according to SIEVE to
650 have double mutant genotypes and the remaining 306 to have single mutant genotype. This
651 observation was in accordance with the simulation results, where SIEVE inclined to explaining
652 somatic deletions as ADO events within single and double mutant genotypes to accommodate to
653 the characteristics of the data, showing reliability to the results of DelSIEVE. The proportion
654 of genotypes called by DelSIEVE and SIEVE were summarized in Additional file 1: Table S2
655 (same for the following datasets).

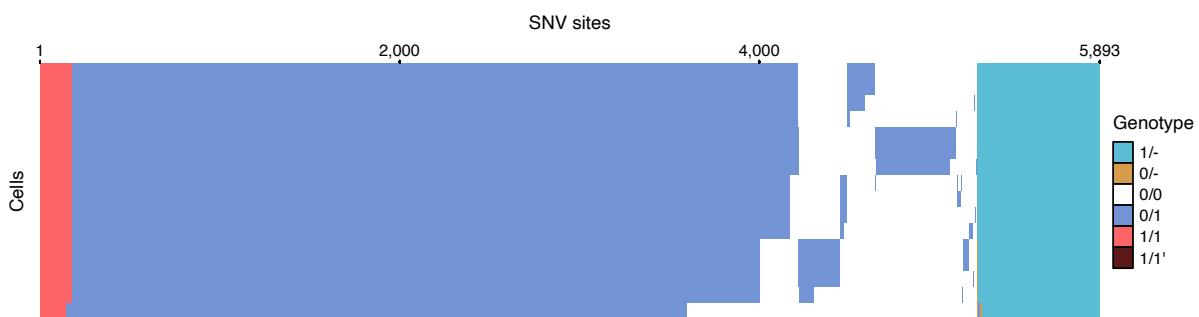


Figure 6: Results of variant calling for the TNBC16 dataset. Cells in the row are in the same order as that of leaves in the phylogenetic tree in Figure 5.

656 To further validate the ability of DelSIEVE to reliably call deletions, we inspected whether
657 the sites identified as deleted displayed also a lower coverage than sites with neutral copy number.
658 We next compared the strength of the coverage reduction effect on deleted sites to a dedicated
659 copy number calling method, Sequenza [22] (Figure 7). The comparison was performed only
660 for the sites shared between the input data of both methods, which, in this case, were all 5,912
661 candidate variant sites. Since Sequenza was designed to apply to bulk-seq data and only reported
662 copy number (CN) at the clone (or subclone) level, we harmonized the resolution of DelSIEVE's
663 results with Sequenza to ensure a fair comparison. To this end, we adjusted DelSIEVE to
664 operate at the clone level as well. In other words, for this comparison, we considered all cells at
665 a given site to contain somatic deletions if at least one cell indicated the presence of a deletion.
666 As expected, we observed that for DelSIEVE the mean value of sequencing coverages (de-

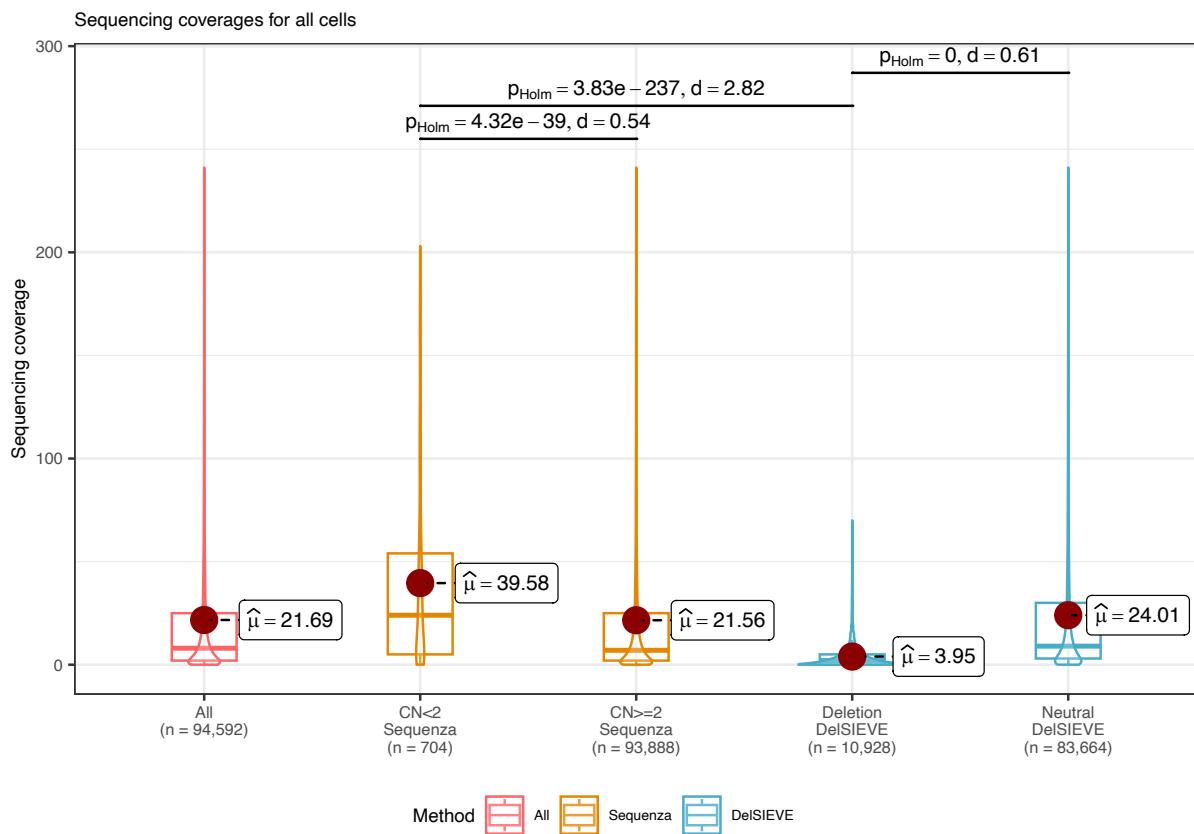


Figure 7: Results of clone-wise sequencing coverage comparison for TNBC16 between DelSIEVE and Sequenza [22]. Compared were the sites shared between the input data of both methods. The resolution of variant calling was clone-wise in order to conduct a fair comparison. For Sequenza, sites were divided into two groups with copy number (CN) < 2 and ≥ 2 , respectively. For DelSIEVE, sites were also divided into two groups, one with somatic deletions, the other copy neutral. Sequencing coverage across all cells at all sites were plotted for reference. In each group, the violin and the box plots matched the color of the method and showed the distribution of the sequencing coverage, while the burgundy dot denoted its mean value $\hat{\mu}$. The total number of dots in each group, which was the product of the number of cells (16) and the number of sites in each group, was marked with n on the horizontal axis. Box plots comprise medians, boxes covering the interquartile range (IQR), and whiskers extending to 1.5 times the IQR below and above the box. Within- and between-group comparisons were conducted between CN < 2 and ≥ 2 of Sequenza, between somatic deletions and copy neutral of DelSIEVE, and between CN < 2 of Sequenza and somatic deletions of DelSIEVE. For each comparison, shown were the p-value corrected by Holm–Bonferroni method and the absolute value of the effect size (Cohen’s d).

667 noted by $\hat{\mu}$ in Figure 7) in the group of sites with somatic deletions (3.95) was significantly lower
 668 compared to the mean for sites without somatic deletions (24.01, respectively), with effect size
 669 Cohen’s d = 0.61. In contrast, the mean coverage for 44 sites identified as containing somatic
 670 deletions by Sequenza was 39.58, significantly larger than 21.56, the mean coverage for sites with
 671 amplifications (Cohen’s d = 0.54), contesting Sequenza’s copy number calls. Furthermore,
 672 a direct comparison revealed that sites identified as deleted by DelSIEVE showed much lower

673 coverage levels than those identified as deleted by Sequenza (Cohen's $d = 2.82$). This indicates
674 that DelSIEVE calls deletions more reliably than Sequenza.

675 **DelSIEVE identified rare somatic mutations in CRC cells.**

676 We then applied DelSIEVE to a scWGS dataset, CRC28 [55]. The estimated cell phylogeny was
677 supported by high posterior probabilities with a long trunk (Additional file 1: Figure S9, S10),
678 which was similar to that reported by SIEVE (the normalized RF and the BS distances were
679 0.08 and 8.03×10^{-7} , respectively). In particular, tumor proximal (TP) and tumor distal (TD)
680 cells also formed a closer clade compared to tumor central (TC) cells in the tree reported by
681 DelSIEVE. This suggested that, like SIEVE, DelSIEVE also inferred regular tumor growth and
682 limited cell migration.

683 Similar to SIEVE, DelSIEVE annotated mutations of known CRC driver genes, for instance,
684 *APC*, and of genes related to the metastatic progression of CRC, such as *ASAP1* and *RGL2* on
685 the trunk of the tree. However, DelSIEVE identified more mutation events than SIEVE, includ-
686 ing two coincident deletions and mutations, one single deletion which was not LOH, and one
687 single deletion mutation addition. For example, DelSIEVE identified that *ACSL5*, potentially
688 related to intestinal carcinogenesis [81], underwent a somatic deletion of one allele (genotype
689 changed from 0/0 to 0/-) on the trunk and a mutation to the left allele (genotype changed
690 from 0/- to 1/-) for the most recent common ancestor of TP and TD cells. Overall, DelSIEVE
691 found very few mutation events that were not single mutations, indicating that single mutations
692 dominated the evolutionary process of this sample.

693 DelSIEVE identified the same number of variant sites as SIEVE (8,029; see Additional file 1:
694 Figure S11), in which 13 sites contained somatic deletions (mostly 1/-; 0.16% of all variant sites).
695 According to SIEVE, nine of those sites were inferred to have double mutant genotypes and four
696 to have single mutant genotype. The contrasting results obtained by DelSIEVE, with multiple
697 somatic deletions identified in TNBC16 but only few in CRC28, underscored an important
698 feature of the method. While DelSIEVE employs a sophisticated modeling approach, it primarily
699 relies on the data for the inference. In other words, the detection of somatic deletions was driven
700 solely by the characteristics of the data itself and is not enforced by the model when the deletions
701 are not there.

702 We further conducted a comparative analysis of the sequencing coverage between sites that
703 were identified to contain somatic deletions and those that did not, using both DelSIEVE and

704 Sequenza ([Additional file 1: Figure S12-S14](#)). Specifically, as CRC28 comprised tumor cells
705 originating from distinct anatomical locations (denoted TP, TC, and TD cells), our comparison
706 was conducted at the subclone resolution. This resolution represented the highest achievable
707 level of detail that Sequenza could provide for this specific dataset, and we adjusted the resolution
708 of DelSIEVE accordingly.

709 For TP cells (cancer tissue 1 in [Additional file 1: Figure S9](#); with nine cells) and TC cells
710 (cancer tissue 3; with 12 cells), we could only inspect the results of DelSIEVE as there is
711 no corresponding bulk sample for Sequenza. We observed noticeable differences of coverage
712 between sites with and without somatic deletions called by DelSIEVE: for TP cells, the mean
713 coverage $\hat{\mu} = 1.54$ for sites with somatic deletions was significantly lower than $\hat{\mu} = 6.37$ for sites
714 without deletions Cohen's $d = 0.59$; [Additional file 1: Figure S12, S14](#)). This difference was
715 also significant for the TC cells ($\hat{\mu} = 2.9$ for sites with somatic deletions, 10.26 for sites without,
716 Cohen's $d = 0.63$; [Additional file 1: Figure S14](#)).

717 For TD cells (cancer tissue 2; with seven cells), both DelSIEVE and Sequenza had lower $\hat{\mu}$ for
718 sites containing somatic deletions compared to sites without deletions ([Additional file 1: Figure
719 S13a](#)). DelSIEVE exhibited a clear distinction, with a significantly lower $\hat{\mu}$ of 1.76 for sites with
720 somatic deletions compared to 7.41 for sites without, resulting in Cohen's $d = 0.5$. Conversely,
721 the difference in $\hat{\mu}$ was negligible for Sequenza, with values of 6.85 and 7.97 for sites with and
722 without somatic deletions, respectively, resulting in Cohen's $d = 0.1$. Additionally, there was
723 an evident difference in $\hat{\mu}$ between sites with somatic deletions identified by DelSIEVE and
724 Sequenza, as indicated by a Cohen's d effect size of 0.5. These findings highlighted the divergent
725 performance of DelSIEVE and Sequenza in calling somatic deletions for TD cells, where the
726 results of the latter might not be reliable from the viewpoint of the conducted comparisons.

727 To further inspect the results from Sequenza, we visualized its reported CNs in TD cells
728 across the entire genome ([Additional file 1: Figure S13b](#)). The visualization clearly revealed that
729 Sequenza inferred a substantial number of CNs other than 2 for each chromosome. Moreover,
730 these CNs frequently exhibited fluctuations in their values, indicating that the method might
731 be fitting to the noise rather than accurately capturing true CN states. These findings indicate
732 that a significant portion of the CNs inferred from Sequenza could potentially be false positives.

733 **DelsIEVE identified rare somatic mutations in CRC samples mixed with nor-**
734 **mal cells.**

735 We finally analyzed another scWES dataset, CRC48 (CRC0827 in [82]). DelsIEVE pinpointed
736 two tumor subclones, associated with their anatomical locations, each subclone containing ex-
737 actly the same cells as in SIEVE (Additional file 1: Figure S15, S16). The rest of the cells
738 collected from tumor biopsies were clustered together with cells from adenomatous polyps, sug-
739 gesting that they might be normal cells residing inside cancer tissues, as pointed out by both
740 the original study [82] and SIEVE. There were some distinctions between the cell phyloge-
741 nies reported by DelsIEVE and SIEVE, with normalized RF and BS distances being 0.33 and
742 1.99×10^{-6} , respectively. This discrepancy is higher than observed for previous datasets, and
743 might be due to the overall lower signal level in the data. Indeed, the CRC48 dataset has a
744 substantially lower ratio between the number of candidate variant sites and the number of cells
745 (707/48 ≈ 14.7) compared to TNBC16 (5912/16 = 369.5) and CRC28 (8470/28 = 302.5).

746 DelsIEVE identified many single mutations on the branch leading to two tumor subclones,
747 including a reported CRC driver mutation in gene *SYNE1* [83], as well as a mutation related
748 to DNA mismatch repair, in gene *MLH3* [84], both of which were also identified on the same
749 branch by SIEVE. Moreover, DelsIEVE found two parallel single mutations (*CHD3* and *PLD2*),
750 which were also reported by SIEVE for the same cells. Furthermore, DelsIEVE identified only
751 one site containing somatic deletions (among 679 variant sites, and only 0/-; see Additional file
752 1: Figure S17), which was previously inferred by SIEVE to have single mutant genotype.

753 We conducted a comparative analysis of the site-wise sequencing coverage between sites
754 that were identified to contain somatic deletions and those that did not, for cancer tissue 1
755 (Additional file 1: Figure S18; with 17 cells) as well as cancer tissue 2 (Additional file 1: Figure
756 S19; with 18 cells). The comparisons were performed at the subclone resolution associated
757 with the anatomic locations. Sites identified by DelsIEVE as containing somatic deletions
758 showed much more pronounced mean coverage differences compared to sites without deletions,
759 both for cancer tissue 1 (Cohen's $d = 0.4$) and for cancer tissue 2 ($d = 0.47$). These mean
760 coverage differences between sites identified as deleted or not by Sequenza were negligible for
761 both subclones (Cohen's $d = 0.06$ for cancer tissue 1; $d = 0.09$ for cancer tissue 2). Moreover,
762 mean coverage was much lower for sites identified to carry somatic deletions by DelsIEVE than
763 for sites identified as such by Sequenza (Cohen's $d = 0.46$ for cancer tissue 1; $d = 0.5$ for
764 cancer tissue 2). For adenomatous polyps, DelsIEVE reported no somatic deletions, so we only

765 compared the results of Sequenza ([Additional file 1: Figure S20](#)). Countering the expected effect
766 of deletions, we observed a higher mean coverage for the sites identified by Sequenza to have
767 $CN < 2$ (37.97) than sites with $CN \geq 2$ (35.76), though the difference was negligible (Cohen's d
768 = 0.03). These findings again validated the deletion calls made by DelSIEVE and raised doubts
769 about the CNs called by Sequenza in the context of the comparisons we performed regarding
770 the sequencing coverages.

771 Discussion

772 We present DelSIEVE, a statistical method designed to jointly infer somatic deletions, SNVs,
773 and the cell phylogeny from scDNA-seq data. Built upon SIEVE, which combines inference
774 of SNVs and cell phylogeny, DelSIEVE takes a step forward by allowing for the occurrence
775 of somatic deletions during the evolution of the tumor. In a nutshell, DelSIEVE features a
776 statistical phylogenetic model with genotypes relating both to somatic deletions and to single
777 and double mutants, a model of raw read counts allowing for both single ADO and locus dropout,
778 a mechanism for acquisition bias correction for the branch lengths, and a trunk in the cell
779 phylogeny for clonal mutations.

780 Somatic deletions often play an essential role in tumor evolution. Although our previous
781 work, SIEVE, does account for the FSA in the statistical phylogenetic model, it only considers
782 somatic mutations with nucleotide substitutions. Thus, it is not versatile enough to apply to
783 data where somatic deletions are present. We have shown that for such data SIEVE tends
784 to explain somatic deletions as a result of ADOs, with an inflated amount of single and double
785 mutant genotypes inferred. The inclusion of somatic deletions in DelSIEVE fills this missing part
786 in the puzzle. In particular, compared to SIEVE, DelSIEVE exhibits boosted performance in
787 terms of calling double mutant genotypes, while performs similarly in estimating cell phylogeny
788 and calling single mutant genotype.

789 The difficulty of identifying somatic deletions is mainly due to the similarity between the
790 sequencing data resulting from somatic deletions and ADOs, as well as the uneven coverage
791 inherent in scDNA-seq. Both DelSIEVE and SCIPhIN deconvolve somatic deletions from ADOs
792 with the help of cell phylogeny. However, unlike SCIPhIN, DelSIEVE explicitly employs a
793 statistical phylogenetic model allowing for both somatic deletions and double mutant genotypes,
794 as well as a model of sequencing coverage using a negative binomial distribution. We have shown
795 that DelSIEVE outperforms SCIPhIN in identifying somatic deletions, including alternative-

796 (1/-) and reference-left single deletion (0/-), as well as in calling single and double mutant
797 genotypes. Furthermore, DelSIEVE is the only method able to explicitly call double deletion
798 genotype.

799 DelSIEVE and SIEVE are the only two methods being able to explicitly call ADOs, working
800 under either single ADO or locus dropout mode. This task is daunting in a similar sense to
801 calling somatic deletions. We have proved that DelSIEVE outperforms SIEVE regarding calling
802 ADOs. However, the results are only reliable when the data is of adequate coverage quality,
803 which is not given for real data yet. We anticipate that the coverage quality of future scDNA-seq
804 data would be suitable for DelSIEVE to make reliable ADO inference.

805 Estimating cell phylogeny from scDNA-seq data is a crucial step as it lays the foundation
806 for downstream analyses. Our previous research demonstrated the superiority of SIEVE over
807 other methods, particularly in accurately estimating branch lengths. Building upon the success
808 of SIEVE, our more sophisticated model, DelSIEVE, exhibits comparable performance in the
809 precise estimation of cell phylogeny. Moreover, DelSIEVE surpasses SIEVE's functionality by
810 discerning 17 types of mutation events, corresponding to 28 distinct types of genotype transi-
811 tions. This expanded capability of mutation event identification makes DelSIEVE a valuable
812 asset in unraveling complex genomic dynamics and understanding evolutionary relationships
813 among cells. We believe that DelSIEVE will greatly benefit researchers in deciphering intricate
814 cellular processes and furthering our understanding of genetic evolution.

815 For now, DelSIEVE demonstrates its proficiency in identifying somatic deletions, SNVs and
816 ADO. One potential improvement would be to add the identification of small insertions and
817 CNAs with CNs greater than two. Another limitation of DelSIEVE lies in the requirement for
818 preselected input data using DataFilter. This step is limited to identifying candidate variant
819 sites that specifically contain nucleotide substitutions. To address this limitation, a possible
820 enhancement would be to enable DataFilter to preselect sites of tumor suppressor genes that
821 are solely associated with somatic deletions. The inclusion of these sites, which are known to
822 elevate the risk of tumor development, could further refine DelSIEVE's precision and clinical
823 relevance in understanding tumorigenesis and potential therapeutic targets.

824 Despite these limitations, DelSIEVE proves to be already now one of the most sophisticated
825 statistical phylogenetics models of its kind and extracts an unprecedented wealth of information
826 on evolution of tumors from scDNA-data. We apply DelSIEVE to three real scDNA-seq datasets
827 from TNBC and CRC samples, which were previously analyzed using SIEVE. DelSIEVE identi-

828 fies rare somatic deletions and double mutant genotypes in the CRC samples, akin to the results
829 of SIEVE. However, for the TNBC sample, DelSIEVE identifies multiple somatic deletions while
830 revealing fewer single and double mutant genotypes compared to SIEVE, consistent with the
831 benchmarking results. Additionally, we demonstrate the higher reliability of somatic deletions
832 called by DelSIEVE than those by Sequenza. These results highlight the precision of DelSIEVE
833 in reconstruction of the phylogenetic tree, as well its enhanced accuracy and effectiveness in
834 identifying genotypes, which holds great potential for advancing our understanding of cancer
835 biology and facilitating precision medicine approaches.

836 **Supplementary Materials**

837 **Supplementary Material 1.**

838 Supplementary Figs. S1-S20 and Tables S1-S2.

839 **Data availability**

840 We analyzed three published single-cell datasets ([55, 78, 82]). Raw sequencing data for these
841 datasets are available from the BioProject database under accession code PRJNA896550 (CRC28),
842 as well as SRA database under accession codes SRA053195 (TNBC16) and SRP067815 (CRC48).

843 **Code availability**

844 DelSIEVE is implemented in Java and is accessible at <https://github.com/szczurek-lab/DelSIEVE>. The simulator is hosted at https://github.com/szczurek-lab/DelSIEVE_simulator,
845 and the reproducible benchmarking framework is available at https://github.com/szczurek-lab/DelSIEVE_benchmark_pipeline. The scripts for generating all figures in this paper are
846 hosted at https://github.com/szczurek-lab/DelSIEVE_analysis. All aforementioned code
847 are freely accessible under a GNU General Public License v3.0 license.
848

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1058 **Author contributions**

1059 S.K. and E.S. conceived the DelSIEVE model - with input and feedback from J.K., N.BE. and
1060 D.P. S.K. implemented the model, performed all model performance analysis and generated
1061 figures. N.BO. and M.V. processed the scDNA-seq datasets. M.M. plotted the copy numbers
1062 across the whole genome. S.K. and E.S. wrote the manuscript with critical comments and input
1063 from all the co-authors. E.S. supervised the study.

1064 **Competing interests**

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