

Detecting shifts in the mode of chromosomal speciation across the cosmopolitan plant lineage *Carex*

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Abstract Recent studies of angiosperm diversification have focused on the role of polyploidy as a driver of diversification. However, we know far less about the effects of single changes in chromosome number—dysploidy, which can mediate lineage diversification by affecting recombination rates, linkage, and/or reproductive isolation. Modeling the effects of dysploidy on diversification is mathematically and computationally challenging because many states and parameters are required to track changes in individual chromosomes, especially in lineages that have high variability in chromosome number. Additionally, we expect the processes of diversification and dysploidy to vary across clades, which requires modeling process variation to disentangle the effects of the observed trait (chromosome number) from the effects of unobserved traits on diversification. In this work, we propose a new state-dependent diversification model of chromosome evolution that includes numerous character states and explicitly models heterogeneity in the diversification process. Our model includes parameters that functionally link diversification rates to dysploidy rates and differentiate between anagenetic and cladogenetic changes. We apply this model to *Carex* (Cyperaceae), a model lineage for understanding dysploidy and diversification, leveraging chromosome number information and the most recent time-calibrated phylogenetic tree for over 700 species and subspecies. We recover distinct modes of chromosomal speciation across *Carex*. In one mode, dysploidy occurs very frequently and drives faster diversification rates. In the other mode, dysploidy is rare and diversification is driven by other factors, unmeasured in our analysis. This study is the first to demonstrate that dysploidy drives diversification in plants while considering unmeasured factors affecting

diversification.

Significance Statement Evolutionary genomic rearrangements via the gain and/or loss of chromosomes without losing DNA may cause new species to form, but how this process plays out over a millions-of-years timescale is unclear. We test if there is a detectable effect of chromosome gains/losses on the rate of species formation in a large, diverse group of plants. We demonstrate decisively for the first time that these rearrangements sometimes drive the formation of new species through two evolutionary modes. In one mode, rearrangements happen rapidly and sometimes cause new species to form. In the other mode, rearrangements happen less frequently and are not associated with new species formation; instead, other factors—unmeasured in our analysis—likely drive the formation of new species.

[keywords—Chromosome number; diversification process variation; diversification; dysploidy; macroevolution; RevBayes; TensorPhylo]

Introduction

1 Unveiling the primary drivers of diversification remains one of the most important goals in evolutionary biology
2 (Sauquet and Magallón, 2018). Hundreds of studies have focused on estimating changes in plant diversification pro-
3 cesses through time (e.g., Magallón and Castillo, 2009), across clades (e.g., Magallón et al., 2019), or in association with
4 trait evolution (e.g., Helmstetter et al., 2023). Chromosome number changes and rearrangements are particularly likely
5 to influence lineage diversification. Most plant diversification studies that address chromosome evolution focus on
6 polyploidy, rather than on localized chromosomal rearrangements that do not involve large DNA content changes (*i.e.*,
7 dysploidy, gains or losses of single chromosomes; Escudero et al., 2014; Mandáková and Lysák, 2018). A recent review
8 of trait-dependent diversification in angiosperms, for example, cites seven studies linking speciation and polyploidy
9 (Helmstetter et al., 2023), only one which considered dysploidy linked to diversification (Freyman and Höhna, 2018).
10 While dysploidy has the potential to influence lineage diversification through effects on recombination or reproductive
11 isolation, far fewer macroevolutionary studies have focused on speciation and extinction as a result of dysploidy.

12 In a recent review, Lucek et al. proposed three contrasting models of chromosomal speciation (see Fig. 4 in Lucek
13 et al., 2022). In the hybrid-dysfunction model, dysploidy is linked to speciation events. Under this model, dysploidy
14 causes an immediate reproductive barrier, as reproduction between individuals with different chromosome numbers
15 would cause problems during meiosis. Thus, most—if not all—dysploidy events across a phylogeny would occur
16 cladogenetically. Alternatively, the recombination-suppression model posits that chromosomal rearrangements may
17 become fixed in lineages via either drift or selection (as some rearrangements may physically link adaptive loci or
18 locally reduce recombination). Under this model, dysploidy would evolve primarily anagenetically across the phy-
19 logeny. The two above-described models are not mutually exclusive. The authors also introduce a third option—the
20 hybrid-dysfunction/recombination-suppression model, under which dysploidy evolves both anagenetically and clado-
21 genetically. While populations may be able to continue interbreeding despite some dysploidy events (which then may
22 be fixed in the lineage), other dysploidy events may cause speciation, either because of an accumulation of differences
23 that eventually leads to incompatibility or because of the genomic signature of the dysploidy event itself. We describe
24 additional theory on dysploidy and macroevolution in Supplemental Section S1.

25 Of the few applied macroevolutionary studies that address the role of dysploidy in lineage diversification, most
26 have focused on monocentric chromosomes, which have a single centromere (e.g., Ayala and Coluzzi 2005; Freyman
27 and Höhna 2018, but see relevant work on Lepidoptera in de Vos et al. 2020, among others), even though approxi-
28 mately 15–20% of eukaryotic species may have holocentric chromosomes. Holocentric chromosomes, instead of having
29 kinetochore activity concentrated in a single point (*i.e.*, at a single centromere in monocentric chromosomes), have cen-
30 tromeric regions distributed along the whole chromosome where the kinetochores assemble in most of the organisms
31 with such chromosome type (Marques et al., 2015; Márquez-Corro et al., 2019b). In monocentric chromosomes, chromo-
32 some fissions are expected to result in a loss of genetic material during meiosis and inviable gametes, as chromosome

33 fragments without centromeres are unable to segregate normally, and fusions are generally inherited by combining two
34 telocentric chromosomes (Robertsonian translocations; Robertson, 1916). Holo-centric chromosomes, by contrast, allow
35 chromosome fragments to segregate normally during meiosis (Faulkner, 1972). Holo-centrism may promote chromo-
36 some number variation via fission and fusion, as these changes are expected to be neutral or nearly so in holo-centric
37 organisms (Márquez-Corro et al., 2019b). Thus, holo-centric organisms provide a unique system in which to study
38 chromosomal speciation (Lucek et al., 2022).

39 Holo-centrism is distributed broadly across the Tree of Life, including 18 different lineages in animals, plants, and
40 rhizaria (Escudero et al., 2016b; Márquez-Corro et al., 2019b), and two particular holo-centric lineages show extraor-
41 dinary chromosome number variation: the insect order Lepidoptera (de Vos et al., 2020) and the angiosperm sedge
42 family Cyperaceae ($2n = 4-224$; Márquez-Corro et al., 2021, 2019a). *Carex*—the largest genus in Cyperaceae—is partic-
43 ularly well suited for studying the effect of dysploidy on plant diversification because it is the third most species-rich
44 monocot family—among the tenth in angiosperms—(POWO, 2023) and there are well-developed phylogenetic and
45 chromosome number datasets for the genus—necessary for macroevolutionary studies—(Márquez-Corro et al., 2021;
46 Martín-Bravo et al., 2019). In *Carex*, karyotype evolves mainly through fusion and fission events, in contrast to in other
47 sedge lineages where karyotype evolves through both dysploidy and polyploidy (Elliott et al., 2022; Márquez-Corro
48 et al., 2019a; Shafir et al., 2023). *Carex* also has exceptional variability in holo-centric chromosome number, ranging from
49 $2n = 10$ to $2n = 132$ (Márquez-Corro et al., 2021). *Carex* has experienced several rapid radiations (Martín-Bravo et al.,
50 2019), and shifts in optimum chromosome number are thought to have played a role in some of these radiations (e.g.,
51 *Carex* sect. *Cyperoideae*; Hipp, 2007; Márquez-Corro et al., 2021).

52 Here, we design a new model that incorporates process variation in chromosome number evolution and disentan-
53 gles the effects of dysploidy from other unobserved factors that may also affect diversification rates (Fig. 1). Previous
54 studies that have tested for a correlation between dysploidy and diversification (e.g., Márquez-Corro et al., 2021) have
55 relied on models that fail to account for alternative sources of variation in diversification rates—e.g., morphologi-
56 cal traits, climatic niche, or biotic interactions—that are not the study’s focal trait (in our case, chromosome number;
57 Beaulieu and O’Meara, 2016). Models that fail to account for alternative sources of variation in diversification rates
58 have high type-I error rates (Rabosky and Goldberg, 2015) because the null hypothesis of those models assume that
59 there is no variation in rates of diversification. This high error rate motivated the development of hidden-state models
60 with null hypotheses that account for underlying diversification-rate variation (Beaulieu and O’Meara, 2016; Caetano
61 et al., 2018). These hidden state models not only more accurately test for associations between the focal trait and diver-
62 sification, but also provide an opportunity to model how focal evolutionary processes vary across the phylogeny. For
63 example, does chromosome number evolution occur uniformly across *Carex*? Our proposed model differs from other
64 SSE-type models with or without hidden states (e.g., Helmstetter et al., 2023) in that we are testing differences in the
65 speciation rates associated with types of transitions rather than with the states themselves. In the case of chromosomes,
66 the goal is not to test whether $n = 15$ or $n = 16$ have different modes of diversification, but rather if the type of kary-
67 otype change (i.e., increase: $n = 15$ to $n = 16$ vs. decrease: $n = 15$ to $n = 14$) carries significant diversification signal

68 compared to heterogeneity (or noise) in the diversification process. Thus, our approach addresses critical issues in the
69 role of heterogeneity in the diversification process as discussed in Caetano et al. (2018). We apply our model to the most
70 recent *Carex* time-calibrated phylogeny with chromosome number information that contains over 700 taxa and more
71 than 50 states (Márquez-Corro et al., 2021; Martín-Bravo et al., 2019).

72 Modeling cladogenesis, chromosome number evolution, and hidden rate variation

73 We developed the ChromoHiSSE model (Chromosome number and Hidden State-dependent Speciation and Extinction
74 model) as an extension of the ChromoSSE model (Freyman and Höhna, 2018). Under the ChromoSSE model, lineages
75 evolve independently under a continuous-time Markov chain (CTMC) that describes changes in chromosome numbers,
76 speciation events, and extinction events; each of these events occurs at a particular rate (interpreted as the expected
77 number of events per lineage per unit time). The ChromoHiSSE model includes an additional hidden trait with m
78 states. The states of this hidden trait correspond to different sets of ChromoSSE parameters, and lineages evolve among
79 hidden states as a Markov process with a given rate.

80 Under the ChromoHiSSE model, the state of a lineage is both the chromosome number, n , and the hidden state,
81 *i*. For numerical stability (Freyman and Höhna, 2018; Mayrose et al., 2010), we place an upper bound on the possible
82 number of chromosomes (k ; transitions to $n > k$ are prohibited, *i.e.*, have rate 0). We denote the two hidden states as *i*
83 and *ii*. For example, the state for a lineage could be $10i$, indicating that the lineage has 10 chromosomes and is in the
84 hidden state *i*.

85 The ChromoHiSSE model is a stochastic process that begins with two lineages at the root, which evolve indepen-
86 dently forward in time. As the process evolves, a lineage can experience anagenetic events (changes in chromosome
87 number or hidden state that do not involve speciation, denoted with superscript ^a), cladogenetic events (speciation
88 events that may also involve changes in the number of chromosomes or hidden state for one of the daughter lineages,
89 denoted with superscript ^c), and extinction events. As in all continuous time Markov chain models, each event happens
90 at an instantaneous point in time and multiple events cannot happen concurrently. The anagenetic events are:

91 (1) n increases by one ($n + 1$ increasing dysploidy) but the hidden state stays the same, which occurs at rate γ_i^a ;
92 (2) n decreases by one ($n - 1$ decreasing dysploidy) but the hidden state stays the same, which occurs at rate δ_i^a ,
93 and;
94 (3) n stays the same, but the hidden state changes (*e.g.*, *i* to *ii*), which occurs at rate χ^a .

95 Cladogenetic events produce two daughter lineages that then evolve independently. The states of the daughters depend
96 on the type of event:

97 (4) both daughters inherit the state of the ancestor, which occurs at rate ϕ_i^c ;
98 (5) one daughter inherits n , the other inherits $n + 1$ (increasing dysploidy), and both inherit the same hidden state
99 *i*, which occurs with rate γ_i^c ;

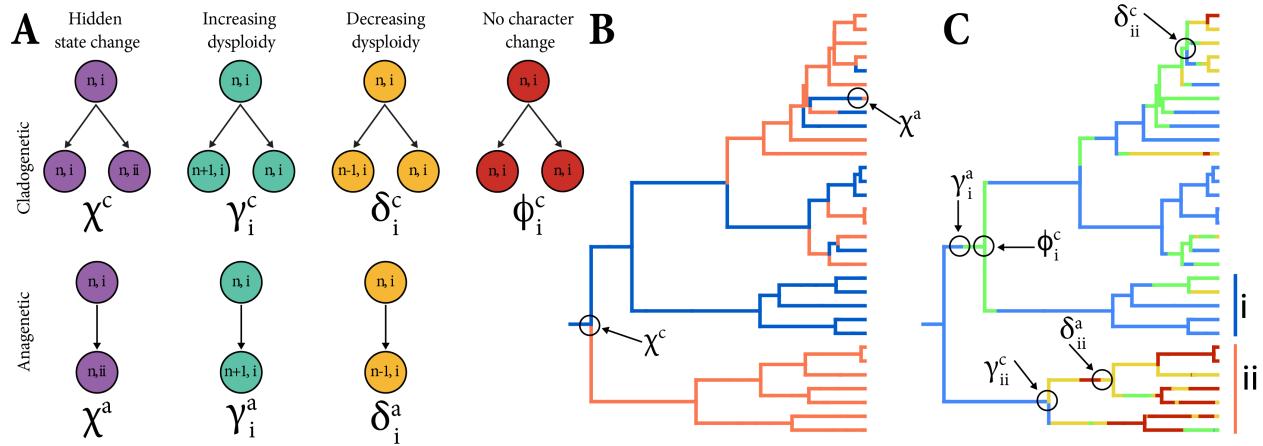


Figure 1: The ChromoHiSSE model. Panel (A) describes the event rates allowed in the model for both cladogenetic (top) and anagenetic (bottom) events. Panels (B) and (C) demonstrate those rates on a tree simulated under ChromoHiSSE. Panel (B) shows the anagenetic and cladogenetic changes in the hidden states, indicated by blue (*i*) vs. orange (*ii*). Panel (C) shows the anagenetic and cladogenetic gains and losses of chromosomes, as well as speciation with no corresponding change in chromosome numbers. More red colors in (C) correspond to more chromosomes. The vertical blue and orange bars in (C) indicate clades in the blue (*i*) vs. orange (*ii*) hidden states, displaying that chromosome number changes are less frequent in the blue hidden state than in the orange.

100 (6) one daughter inherits n , the other inherits $n - 1$ (decreasing dysploidy), and both inherit the same hidden state
 101 *i*, which occurs with rate δ_i^c ;
 102 (7) both daughters inherit n from the ancestor, but one daughter changes hidden state (*i* to *ii*), which occurs at rate
 103 χ^c .
 104 These events are depicted in Fig. 1. Additionally, all lineages go extinct at rate μ , independent of n or the hidden state.
 105 The lineages evolve forward in time until the present, at which point they are sampled independently with probability
 106 f . Extinct and unsampled lineages are pruned from the tree and the hidden state for sampled lineages is ignored;
 107 this produces a realization comprised of a reconstructed phylogeny relating the sampled lineages and a chromosome
 108 number for each sampled lineage. This stochastic process allows us to compute the probability of an observed dataset
 109 (*i.e.*, the probability that a realization under this process corresponds to our observed data) given a set of parameter
 110 values.

111 Note that the model presented here excludes polyploidization because previous analyses of *Carex* have found few
 112 polyploids in *Carex*, mostly concentrated in the small *Carex* subgenus *Siderostictae*—sister to the rest of *Carex*—and
 113 which has had no effect when modeling chromosomes and diversification previously (Márquez-Corro et al., 2021). We
 114 have also assumed that there are only two hidden states, and that rates of change between hidden states are symmetric;
 115 *i.e.*, the anagenetic rate of change from *i* to *ii* is the same as the rate of change from *ii* to *i*, and likewise for cladogenetic
 116 changes. Finally, we have assumed that the rate of extinction is constant among all lineages, regardless of the number
 117 of chromosomes or hidden state. We present the full ChromoHiSSE model that relaxes these assumptions and includes
 118 polyploidization (and demipolyploidization) in Supplementary Material S2.

119 Results

120 We recover two distinct “modes” of chromosome number change, which correspond to the two hidden states i, ii . The
 121 total speciation rate (λ) is very similar between these two modes (Fig. 2C), but dysploidy rates vary significantly (Fig.
 122 2A,B,D). Hidden state i is characterized by fast rates of anagenetic and cladogenetic chromosome number change (Fig.
 123 2, solid lines, and Table 1). Anagenetic increasing and decreasing dysploidy rates (γ_i^a and δ_i^a) are both remarkably
 124 fast, ~ 14 events per lineage per million years (E/L/Myr) (Table 1, Fig. 2B). Cladogenetic increasing and decreasing
 125 dysploidy (γ_i^c and δ_i^c) are significantly higher than 0 (Table 1) and faster than the cladogenetic rate of no character
 126 change (speciation without change in chromosome number, ϕ_i^c). While δ_i^c is slightly faster than γ_i^c , this difference is
 127 not significant (Table 1). The difference between speciation associated with chromosome number change and specia-
 128 tion without chromosome number change is greater than 0 E/L/Myr, indicating that there is a significant association
 129 between chromosome number change and faster speciation rates (Fig. 2D, blue).

130 In contrast, hidden state ii is characterized by slower rates of chromosome number change (Fig. 2, dashed lines,
 131 and Table 1). Anagenetic rates of change (γ_{ii}^a and δ_{ii}^a) are quite low, approximating 0 (Table 1, Fig. 2B), suggesting that
 132 little to no anagenetic change in chromosome number happens in hidden state ii . Cladogenetic rates are also quite low,
 133 and while the rate of decreasing dysploidy (δ_{ii}^c) is slightly higher than increasing dysploidy (γ_{ii}^c), this difference is not
 134 significant (Table 1). The difference between speciation associated with chromosome number change and speciation
 135 without chromosome number change is significantly less than 0 E/L/Myr, suggesting that speciation is actually slower
 136 when associated with a chromosome number change in hidden state ii (Fig. 2D, orange).

Table 1: Summary statistics of posterior distributions for parameter estimates for the ChromoHiSSE model. Light blue rows correspond to parameter estimates for hidden state i , and light orange rows correspond to parameter estimates for hidden state ii . All rate estimates are given in units of events per lineage per million years (E/L/Myr)

Model parameter	Parameter Type	Hidden State	Median	2.5% Quantile	97.5% Quantile	
χ^c	Hidden state change	Cladogenetic	i, ii	0.113	0.051	0.215
γ_i^c	Increasing dysploidy	Cladogenetic	i	0.330	0.021	0.772
γ_{ii}^c	Increasing dysploidy	Cladogenetic	ii	0.077	0.003	0.261
δ_i^c	Decreasing dysploidy	Cladogenetic	i	0.539	0.120	0.916
δ_{ii}^c	Decreasing dysploidy	Cladogenetic	ii	0.099	0.007	0.250
ϕ_i^c	No character Change	Cladogenetic	i	0.072	0.003	0.363
ϕ_{ii}^c	No character Change	Cladogenetic	ii	0.849	0.642	1.058
χ^a	Hidden state change	Anagenetic	i, ii	0.021	0.001	0.093
γ_i^a	Increasing dysploidy	Anagenetic	i	14.638	12.282	17.626
γ_{ii}^a	Increasing dysploidy	Anagenetic	ii	0.397	0.121	0.769
δ_i^a	Decreasing dysploidy	Anagenetic	i	14.191	11.903	17.246
δ_{ii}^a	Decreasing dysploidy	Anagenetic	ii	0.142	0.005	0.505

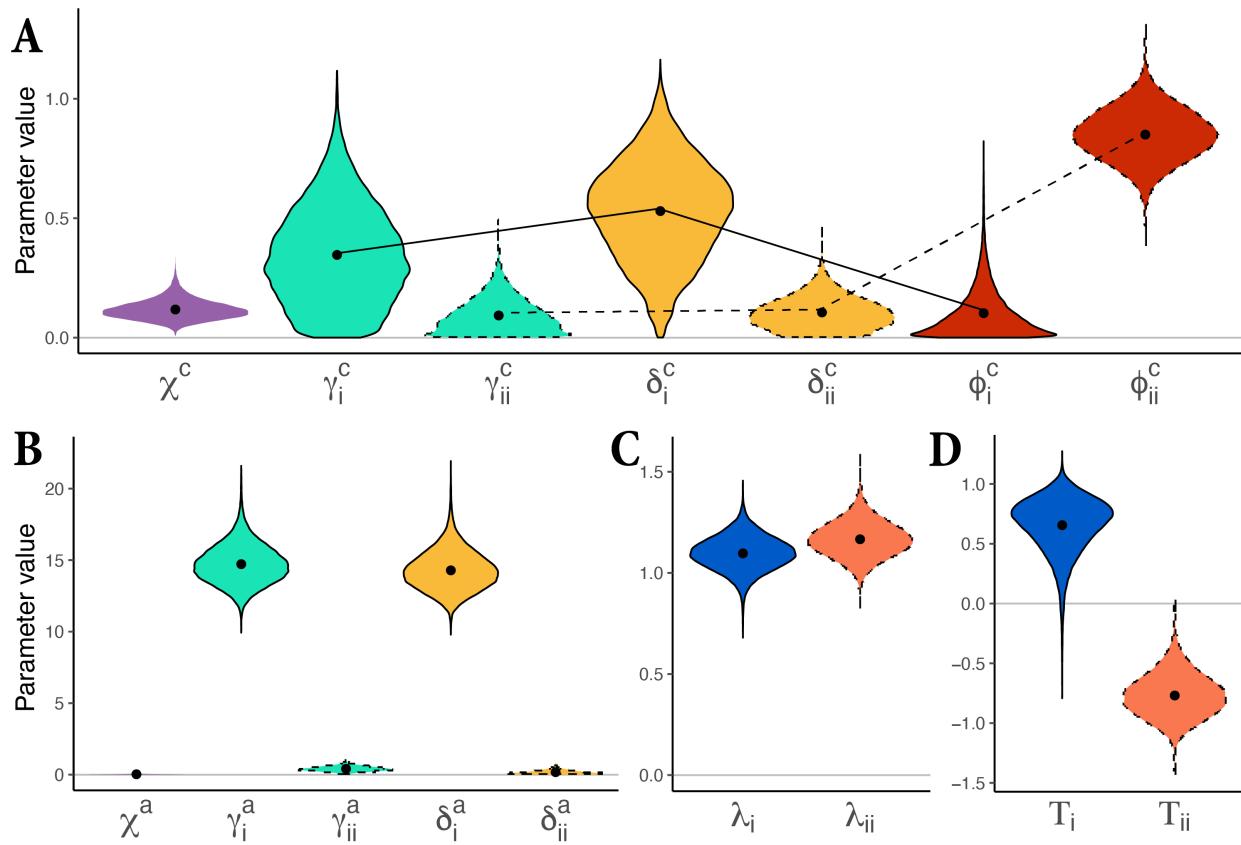


Figure 2: Posterior distributions of rate estimates. Solid lines indicate rates corresponding to hidden state i and dashed lines indicate hidden state ii . Panel (A) shows the posterior distributions of cladogenetic rates, panel (B) shows the anagenetic rates, panel (C) shows the total speciation rate per hidden state (λ), and panel (D) shows the total difference (TD) per hidden state between speciation associated with chromosome number change and speciation without a chromosome number change.

137 We also reconstructed the evolution of chromosome number and hidden state across the phylogeny of *Carex* (Fig.
 138 3) using stochastic character mapping (Freyman and Höhna, 2019). Just over half (51.85%) of all branches showed a net
 139 change in chromosome number along the branch. Most clades in the phylogeny vary in chromosome number despite
 140 some shallow evolutionary divergences (Fig. 3A). For example, clade 2—which includes sect. *Pictae*, the Hirta Clade,
 141 and sect. *Praelongae*—shows substantial variation in chromosome number, from $n = 13$ to $n = 66$. However, a clade
 142 of hooked sedges (*Carex* sect. *Uncinia*; Fig. 3, clade 1 in grey), has a constant chromosome number ($n = 44$) across the
 143 33 species included in this study, with one exception: *Carex perplexa* has a count of $n = 66$, suggesting that this species
 144 may be a demiploid (see Discussion). While both clades highlighted in Fig. 3 have similar crown ages, number
 145 of species, and average chromosome number ($n = 35.7$ vs. $n = 44.6$), they differ dramatically in karyotype variability
 146 and, consequently, in the inferred hidden state (clade 1 = ii , clade 2 = i , Fig. 3C). Overall, the dominant pattern of
 147 chromosome number in *Carex* is one of frequent but gradual change; 75.05% of per-branch net chromosome number
 148 changes are 3 or fewer gains or losses.

149 **Discussion**

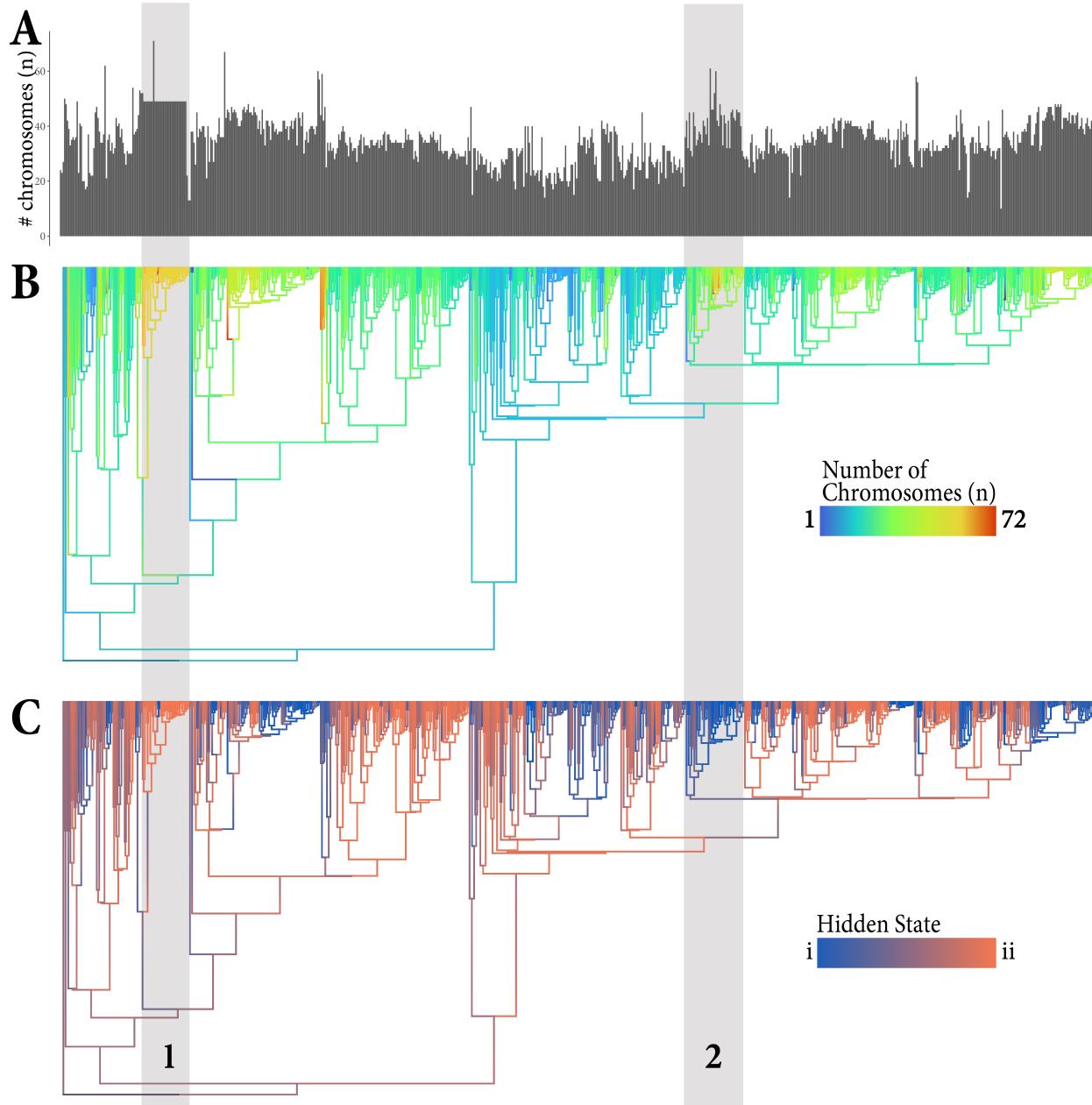


Figure 3: Reconstruction of chromosome numbers (A and B) and hidden states (C) on the *Carex* phylogeny. Panel (A) shows the distribution of haploid chromosome numbers for all extant taxa included in the analysis. Panel (B) shows the reconstructed evolution of chromosome number along branches of the phylogeny, where lighter colors indicate more chromosomes. Panel (C) shows the reconstructed evolution of the hidden state along branches of the phylogeny, where blue indicates strong statistical support for state A, orange indicates strong support for state B, and intermediary colors indicate uncertainty in the estimates. Grey bars highlight two clades (labeled 1 and 2) that are discussed in the main text.

150 We demonstrate that dysploidy plays an important yet complex role in diversification in *Carex*. Although the

151 impact of dysploidy on *Carex* diversification has been addressed previously (e.g., Faulkner, 1972; Hipp, 2007; Márquez-
152 Corro et al., 2021, 2019b), this is the first study to jointly model chromosome number change and diversification, and
153 to demonstrate an association between higher speciation rates and dysploidy in parts of the phylogeny despite het-
154 erogeneity in the process of diversification. While gains and losses in chromosome number spur diversification along
155 parts of the phylogeny (hidden state *i*), they have the opposite effect elsewhere in the tree (hidden state *ii*, see Fig. 3).
156 We propose that these discrepancies may be due to the nature of holocentric chromosomes, where a single dysploidy
157 event in isolation may not be enough to trigger reproductive isolation (Escudero et al., 2016a; Hipp et al., 2010; Lucek
158 et al., 2022; Márquez-Corro et al., 2019b; Whitkus, 1988). However, the accumulation of sufficient dysploidy events in a
159 lineage may form a reproductive barrier and thus trigger speciation (Escudero et al., 2016a; Whitkus, 1988). This theory
160 is described as the recombination suppression/hybrid dysfunction chromosomal speciation model (Figure 4 in Lucek
161 et al., 2022). Below, we discuss the evidence supporting this model and provide suggestions for future research.

162 Chromosomal speciation modes in *Carex*

163 Our new ChromoHiSSE model allows us to identify variation in modes of chromosomal evolution across the tree. In
164 one mode, we observe high rates of anagenetic dysploidy, which indicates that dysploidy does not always create an
165 immediate reproductive barrier. In this mode, every estimated dysploidy-related cladogenetic rate was significantly
166 higher than non-dysploidy rates (e.g., speciation with no state change, Fig. 2A), which suggests that speciation happens
167 more frequently when associated with changes to karyotype. The results of our model show that while most dysploidy
168 does not lead to speciation, most speciation is associated with dysploidy. This conclusion is also supported by addi-
169 tional evidence from prior studies, discussed below. The other mode, by contrast, is characterized by lower rates of
170 cladogenetic dysploidy, and anagenetic dysploidy rates are also quite low. However, the overall total speciation rate
171 (λ) between the two modes is very similar (Fig. 2C), demonstrating that—in parts of the tree characterized by this latter
172 mode—additional traits may be contributing to the fast speciation rates.

173 We can see these these different modes of macroevolution illustrated in specific clades of our *Carex* phylogeny.
174 For example, *Carex* sect. *Uncinia* (hook sedges, highlighted as clade 1 in Fig. 3) is characterized by hooked utricles
175 that allow for long-distance dispersal through epizoochory (García-Moro et al., 2022). The hook sedges exemplify a
176 *Carex* clade that is characterized by low-to-zero dysploidy but fast rates of speciation as an apparently young radiation
177 (Martín-Bravo et al., 2019)—though this was not formally tested in our study—and thus may be a particularly appeal-
178 ing candidate for future studies focusing on potential adaptive traits (not related to chromosome number) that led to
179 such biodiversity. This lineage is characterized by karyotypes with numerous chromosomes (Márquez-Corro et al.,
180 2021), mostly reported from New Zealand, where ca. half of the section diversified. However, this only gives partial
181 information on their evolutionary history, as the karyotypes of the Andean relatives have not been studied in detail yet.
182 Most of the New Zealand chromosome counts correspond to a single, old report and there is some variation in the few
183 existing counts from South America, so these results may be taken with caution. If the South American species show

184 wider karyotypic variation than currently detected in comparison to the New Zealand lineage, there may be different
185 drivers enhancing speciation on each side of the South Pacific.

186 Some *Carex* species are known to have striking chromosome-number polymorphism, even within populations (Es-
187 cudero et al., 2023a, 2013b; Luceño and Castroviejo, 1991; Whitkus, 1988). For example, *Carex scoparia* varies from
188 $n = 28$ to $n = 35$ (Escudero et al., 2013b), and individuals with different chromosome numbers are able to reproduce
189 and exchange alleles, maintaining gene flow despite chromosome number differences. This polymorphism suggests
190 that some chromosome number differences are not sufficient to create reproductive barriers (Hipp et al., 2009), which is
191 supported by our results; often, inferred chromosome number changes do not result in an immediate speciation event
192 on the phylogeny. The question remains, why does dysploidy result in speciation in some cases and not in others? One
193 possibility is that an accumulation of changes may eventually lead to reproductive isolation, where one “last straw”
194 dysploidy event triggers speciation (referred to as the last-straw hypothesis). We discuss potential model developments
195 that could test this theory below in the *Modeling chromosomal speciation* section. Another possibility is that rearrange-
196 ments in some parts of the genome are more stable than others, and the genomic architecture—where the fragmentation
197 or fusion occurs in the genome—determines the evolutionary effects of dysploidy.

198 The genomic architecture of clades might point to why dysploidy has a stochastic effect on speciation. A recent
199 study (Cornet et al., 2023) argues that patterns of repeat DNA—e.g., LINEs, LTRs, and Helitrons—are significantly
200 different when comparing fast vs. slow chromosome evolving *Carex* lineages—while this was only tested with a small
201 number of species, those species represent all major *Carex* clades—and, interestingly, repeat DNA regions often serve
202 as hotspots for genome rearrangements (Escudero et al., 2023b; Höök et al., 2023). These repeat regions are significantly
203 more common in the genomes of rapidly evolving lineages (Cornet et al., 2023). It may well be that holocentrism and
204 dysploidy evolution together form an adaptive mechanism that enables the evolution of adaptive linkage blocks. Com-
205 parative genomics may also help to decipher the relationships between dysploidy, diversification, and supergenes in
206 *Carex*. Synteny in holocentric sedge chromosomes is more conserved than we would expect if chromosome evolution
207 were unconstrained, even in comparisons between species that span deep nodes in the phylogeny (Escudero et al.,
208 2023b). This is surprising given the high rates of chromosome evolution inferred in this study. The massive diversity
209 of sedges is likely an outcome of both processes: recombination and reproductive isolation evolving as chromosomes
210 split and fuse.

211 An important caveat to our study is the presence of missing data—particularly for tropical lineages—both in terms
212 of sequenced taxa represented in the phylogeny and for available chromosome counts. While the phylogeny used in
213 this study was assembled with a HybSeq backbone and three DNA regions for ca. 1400 out of 2000 species, phyloge-
214 netic relationships in some areas of the genus are still tenuous (Jiménez-Mejías et al., 2016; Martín-Bravo et al., 2019;
215 Roalson et al., 2021), and sequencing more individuals from the uncertain clades may help resolve those relationships.
216 Additionally, there are only chromosome counts for ~ 700 species in the phylogeny. Filling gaps in our karyological
217 knowledge—especially for tropical taxa—will promote a better understanding of chromosome evolution across the
218 phylogeny of *Carex* and its relationship with other adaptive traits (Spalink et al., 2018). Thus, molecular and karyolog-

ical studies can still continue to improve our knowledge of how dysploidy is taking part in *Carex* evolution (Escudero et al., 2023a, 2013a,b; Márquez-Corro et al., 2021). This is particularly true within a few noteworthy clades. One of the most species-diverse lineages within *Carex*—the Decora Clade/*Carex* sect. *Indicae* (Roalson et al., 2021)—only includes five species with reported chromosome numbers (Márquez-Corro et al., 2021). This pantropical lineage alone would constitute ca. 10% of the genus (Roalson et al., 2021). Also, we include only a few New Zealand species from *Carex* sect. *Uncinia* (clade 1 in Fig. 3), as there are few known karyotypes for the South American representatives of the lineage. Other traits such as hooked utricles and epizoochory might be as or more important for diversification as karyotype in this clade, but we cannot tease these effects apart without additional chromosome count data. While *Carex* biodiversity is greatest in temperate regions including the Global North, this bias in data availability impedes our ability to detect evolutionary patterns of the genus as a whole.

229 Modeling chromosomal speciation

230 The methodological innovations presented here—at the cutting edge of macroevolutionary model development—allow us to model process variation in chromosome number evolution, despite the computational challenges associated with 231 the huge state space of such a model. Process variation is fundamental to our conclusions; only by incorporating 232 multiple modes do we discover that—in some parts of the phylogeny—dysploidy is rare and does not lead to faster 233 speciation. In fact, when we implement our model without process variation, our results suggest a strong, uniform 234 boost in speciation rate associated with dysploidy (results presented in Supplemental Section S3). Future work that 235 builds off of our novel modeling approach will allow us to pursue promising avenues for innovative research; we 236 highlight two examples below.

237 First, like all birth-death models, our ChromoHiSSE model operates with species as the fundamental unit of analysis 238 (the tips in the tree) and thus does not formally model chromosome number polymorphism that is present in some *Carex* 239 lineages. Second, while ChromoHiSSE tests for the effect of single changes in chromosome number on diversification 240 rates, it cannot test for the effect of an accumulation of changes (the last-straw hypothesis). However, ChromoHiSSE 241 could be modified to include tip-state polymorphism (e.g., a dysploid series) as additional hidden states (e.g., a par- 242 ticular tip either has 12, 13, or 14 chromosomes). Additionally, Goldberg and Foo (2020) describe a mechanism for 243 modeling memory (thus the accumulation of chromosome number changes) in a macroevolutionary framework using 244 hidden states, which could be applied to test the last-straw hypothesis.

246 Conclusions

247 Our work demonstrates the important role of dysploidy on diversification in *Carex*, a model lineage for understanding 248 how karyotype rearrangements via dysploidy affect speciation and macroevolutionary dynamics. Our results—using 249 the new ChromoHiSSE model—paint a complex picture of how dysploidy affects speciation in a clade characterized 250 by high species diversity, high morphological disparity, and holocentric chromosomes (Martín-Bravo et al., 2019), and

251 our results support the recombination suppression/hybrid dysfunction chromosomal speciation model, in which only
252 some karyotype rearrangements trigger reproductive isolation and thus speciation. Future work on the underlying
253 genomic mechanisms of chromosomal speciation via comparative genomics will be particularly powerful for linking
254 across scales, from molecules to lineages. Ultimately, our novel modeling approach also serves as a critical step towards
255 even more complex and powerful macroevolutionary analyses that incorporate intraspecific chromosome number vari-
256 ation and track the accumulation of change through time.

257 Materials and Methods

258 To test the role of chromosome number changes on speciation and extinction patterns in the genus *Carex*, we developed
259 the ChromoHiSSE model (Fig. 1). This model estimates cladogenetic and anagenetic rates linked to dysploidy, plus an
260 unmeasured variance that might explain the observed data (*i.e.*, hidden state).

261 Chromosome and phylogenetic data

262 We performed all analyses on a large dataset, which includes a phylogeny of *Carex* with 755 taxa (~ 40% of extant
263 diversity), representing all *Carex* subgenera and most of the sections for which chromosome counts have been reported.
264 Our dataset also includes haploid chromosome number (n) for all tips in the tree; both the tree and chromosome number
265 data come from Márquez-Corro et al. (2021). The original tree, based on a HybSeq backbone and three DNA regions
266 (ITS, ETS and *matK*) from ca. 1400 species out of 2000 *Carex* species, was published by Martín-Bravo et al. (2019). Tips
267 without chromosome number information were pruned for the current study. Chromosome number in *Carex* evolves
268 through dysploid events, except for in the small subgenus *Siderostictae* (13 species in our tree)—sister to the rest of
269 the genus—which includes species with different reported ploidy levels (Márquez-Corro et al., 2021, 2019a). To avoid
270 modeling rare polyploidy events that occur only in a small part of the tree, we removed *Siderostictae* from the primary
271 analysis (though see Supplemental Section S3 for results with this clade included). For the remaining taxa, we coded
272 chromosome numbers as the most frequent haploid number or the lowest haploid cytotype in polyploid lineages from
273 the Márquez-Corro et al. (2021) dataset for those tips. The final data matrix included n -values ranging from 5 to 66
274 chromosomes for 742 taxa.

275 Model implementation

276 We implemented ChromoHiSSE in RevBayes (Höhna et al., 2016), a software for specifying Bayesian probabilistic
277 graphical models primarily for phylogenetics and phylogenetic comparative methods. Due to the large state space
278 of our model and cladogenesis, we used the newly-developed *TensorPhylo* plugin (May and Meyer, 2022) to acceler-
279 ate likelihood calculations and thus achieve convergence in a more reasonable time frame. We ran two chains of the
280 analysis and assessed convergence in the R programming language (R Core Team, 2013). We processed the traces and

281 removed 10% of the generations per chain as burnin using **RevGadgets**. We then calculated the effective sample size
282 (ESS) value for each parameter in each chain using **coda** (Plummer et al., 2006) and verified that the harmonic mean
283 of the ESS values of each chain was greater than 200. We additionally visually inspected all model parameters across
284 both chains in **Tracer** (Rambaut et al., 2018). For any parameters that appeared to have strikingly non-normal posterior
285 distributions, we also estimated a transformed ESS following Vehtari et al. (2021). We subsequently combined both
286 runs for all downstream analyses, discarding 10% of the total generations per chain as burnin prior to combining.

287 **Analysis and postprocessing**

288 We summarized posteriors and plotted results in R (R Core Team, 2013) using the R package **RevGadgets** (Tribble et al.,
289 2022). We additionally transformed model parameters to produce two types of useful summary statistics. First, we
290 calculated the total speciation rate in hidden state i vs. ii as $\lambda = \chi^c + \gamma^c + \delta^c + \phi^c$. Second, we wanted to know if the
291 rate of speciation concurrent with changes in chromosome number ($\gamma^c + \delta^c$) is greater or less than the rate of speciation
292 with no change in chromosome number ($\chi^c + \phi^c$). We thus estimated an additional metric: $TD = (\gamma^c + \delta^c) - (\chi^c + \phi^c)$,
293 such that positive values of TD indicate more speciation with chromosome number change and negative values indicate
294 less speciation with chromosome number change. We estimate TD for each hidden state to estimate how chromosome
295 number changes associated with speciation vary between modes of the model.

296 All code for implementing and running the model and processing and plotting the results is available at Zenodo
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